## "Present and future perspectives in Hadron Physics"

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## Charge-conjugation asymmetry and molecular content: the $T_{c c}(3875)$ and $D_{s 0}^{*}(2317)$ in nuclear matter PHYSICAL REVIEW C 108 (2023) 035205 \& Phys. Lett. B 853 (2024) 138656

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Table 1 | Parameters obtained from the fit to the $D^{0} D^{0} \pi^{+}$mass spectrum: signal yield, $N$, BW mass relative to the $D^{+} D^{0}$ mass threshold, $\delta m_{\mathrm{Bw}}$, and width, $\Gamma_{\mathrm{Bw}}$. The uncertainties are statistical only

| Parameter | Value |
| :--- | :--- |
| $N$ | $117 \pm 16$ |
| $\delta m_{\mathrm{BW}}$ | $-273 \pm 61 \mathrm{keV} \mathrm{c}^{-2}$ |
| $\Gamma_{\mathrm{BW}}$ | $410 \pm 165 \mathrm{keV}$ |

## LHCb: Observation of an exotic narrow doubly charmed Tetraquark, Nature Phys. 18 (2022) $751 \sim 350$ cites

$$
T_{c c}^{+}(3875)
$$

## colorless compact tetraquark structure?

 $D^{*} D$ hadron-molecule?Conventional, hadronic matter consists of baryons and mesons made of three quarks and a quark-antiquark pair, respectively. Here, we report the observation of a hadronic state containing four quarks in the LHCb experiment. This so-called tetraquark contains two charm quarks, $a \bar{u}$ and $a \bar{d}$ quark. This exotic state has a mass of approximately 3875 MeV and manifests as a narrow peak in the mass spectrum of $D^{0} D^{0} \pi^{+}$mesons just below the $D^{*+} D^{0}$ mass threshold.


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$T_{c c}^{+}(3875) \& T_{\bar{c} \bar{c}}^{-}(3875)$ embedded in a nuclear medium which produces a charge-conjugation asymmetry
one might expect that line-shapes are not longer identical...
In the molecular picture,

$$
\begin{array}{ll}
T_{c c}^{+}(3875) \Rightarrow D^{*} D \text { state } & D^{(*)} \sim c \bar{\ell} \\
T_{\bar{c} \bar{c}}(3875) \Rightarrow \bar{D}^{*} \bar{D} \text { state } & \bar{D}^{(*)} \sim \bar{c} \ell
\end{array}
$$

the nuclear environment would induce different modifications to charmed $D^{*} D$ than to anti-charmed $\bar{D}^{*} \bar{D}$ pairs of interacting mesons because the different strength of the $D^{(*)} N$ and $\overline{\boldsymbol{D}}^{(*)} N$ interactions, which should lead to visible changes among the medium properties of the $T_{c c}^{+}(3875) \& T_{\bar{c} \bar{c}}^{-}(3875)$

$$
\begin{aligned}
\Delta_{Y}(q ; \rho) & =\frac{1}{\left(q^{0}\right)^{2}-\omega_{Y}^{2}\left(\vec{q}^{2}\right)-\Pi_{Y}\left(q^{0}, \vec{q} ; \rho\right)} \\
& =\int_{0}^{\infty} d \omega\left(\frac{S_{Y}(\omega,|\vec{q}|)}{q^{0}-\omega+i \varepsilon}-\frac{S_{\bar{Y}}(\omega,|\vec{q}|)}{q^{0}+\omega-i \varepsilon}\right)
\end{aligned}
$$

with $\omega_{Y}\left(\vec{q}^{2}\right)=\sqrt{m_{Y}^{2}+\vec{q}^{2}}$. From the above equation, it follows that for $q^{0}>0$

## Källen-Lehmann representation

$$
\begin{aligned}
S_{D^{(*)}, \bar{D}^{(*)}}\left(q^{0}, \vec{q} ; \rho\right)= & -\frac{1}{\pi} \operatorname{Im} \Delta_{D^{(*)}, \bar{D}^{(*)}}\left(q^{0}, \vec{q} ; \rho\right) \\
= & -\operatorname{Im} \Pi_{D^{(*)}, \bar{D}^{(*)}}\left(q^{0}, \vec{q} ; \rho\right) \\
& \times \frac{\left|\Delta_{\left.D^{(*)}, \bar{D}^{* *}\right)}\left(q^{0}, \vec{q} ; \rho\right)\right|^{2}}{\pi}
\end{aligned}
$$

## spectral function is determined

 by the self-energy$$
G_{U W}(s)=i \int \frac{d^{4} q}{(2 \pi)^{4}} \Delta_{U}(P-q) \Delta_{W}(q)
$$

$$
\begin{aligned}
& \left.\qquad \begin{array}{l}
T^{-1}(s ; \rho)=V_{0}^{-1}(s)-\Sigma(s ; \rho), \\
\bar{T}^{-1}(s ; \rho)=D^{*} \text { scattering amplitude } \\
V_{0}^{-1}(s)-\bar{\Sigma}(s ; \rho), \\
\bar{D} \bar{D}^{*} \text { scattering amplitude } \\
\\
\begin{array}{l}
\text { identical } D D^{*} \\
\text { and } \bar{D} \bar{D}^{*} \\
\text { potentials }
\end{array} \bar{\Sigma}\left(s=E^{2} ; \rho\right)=\frac{1}{2 \pi^{2}}\left\{\mathcal{P} \int_{0}^{\infty} d \Omega\left(\frac{f_{D^{*} D}(\Omega ; \rho)}{E-\Omega+i \varepsilon}-\frac{f_{\bar{D}^{*} \bar{D}}(\Omega ; \rho)}{E+\Omega-i \varepsilon}\right)-i \pi f_{D^{*} D}(E ; \rho)\right\}, \\
2 \pi^{2}
\end{array}, \mathcal{P} \int_{0}^{\infty} d \Omega\left(\frac{f_{\bar{D}^{*}}(\Omega ; \rho)}{E-\Omega+i \varepsilon}-\frac{f_{D^{*} D}(\Omega ; \rho)}{E+\Omega-i \varepsilon}\right)-i \pi f_{\bar{D}^{*} \bar{D}}(E ; \rho)\right\},
\end{aligned}
$$

where $\mathcal{P}$ stands $\mathrm{f} /$, the principal value of the integral and, in addition,

$$
f_{U W}(\Omega ; \rho)=\int_{0}^{\Lambda} d q q^{2} \int_{0}^{\Omega} d \omega S_{U}(\omega,|\vec{q}| ; \rho) S_{W}(\Omega-\omega,|\vec{q}| ; \rho) .
$$

$D D^{*}$ and $\bar{D} \bar{D}^{*}$ loop functions inside of the

$$
\Sigma(s ; \rho=0)=\bar{\Sigma}(s ; \rho=0) \text { in the vacuum! }
$$ nuclear environment




## Nuclear medium spectral functions:

- L. Tolós, C. García-Recio, JN, Phys. Rev. C80 (2009) 065202; Phys. Lett. B690 (2010) 369
- C. García-Recio, JN, L. L. Salcedo, L. Tolos, Phys. Rev. C85 (2012) 025203


Real and imaginary parts of the $D D^{*}$ and $\bar{D} \bar{D}^{*}$ loop functions inside of the nuclear environment
$\rho=0.1 \rho_{0}$

## Line-shapes for different densities and molecular probabilities

$\rho=0.1 \rho_{0}$




## $P_{0}:$ molecular probability (Weinberg)




Now we study the isoscalar $J^{P}=0^{+}$exotic resonance $D_{S 0}^{*}(2317)^{ \pm}$

- quark content: $c \bar{S}, \bar{c} S$
$D_{s 0}^{*}(2317)^{ \pm}$MASS
$m_{D_{s 0}^{*}(2317)^{ \pm-} m_{D_{2+-}}}^{D_{s 0}^{*}(2317)^{ \pm} \text {WIDTH }}$
$D_{s 0}^{*}(2317)^{ \pm}$DECAY MODES
$D_{s 0}^{*}(2317)^{-}$modes are charge conjugates of modes below.
$\left.\begin{array}{llccccc}\text { Mode } & & \text { Fraction }\left(\Gamma_{i} / \Gamma\right) & \begin{array}{c}\text { Scale Factorl } \\ \text { Conf. Level }\end{array} & \text { P(MeV/c) }\end{array}\right]$
- it cannot be accommodated in CQMs: around 100 MeV lighter than expected
- Molecular picture $D \bar{K}$ and $\bar{D} K$


## $K N$ and $\bar{K} N$ interactions very different!


$\bar{K} N \rightarrow \bar{K} N$ : it appears strong hyperon resonances like


$$
S_{K}(E, q ; \rho) \approx \frac{\delta\left(E-E_{\mathrm{qp}}(q ; \rho)\right)}{2 E_{\mathrm{qp}}(q ; \rho)}
$$

Kaon spectral function in the nuclear medium behaves like a delta function, with a small modification (densitydependent) of the quasi-particle energy $E_{q p}^{(K)}$
$K N: \bar{s} \ell_{1} \ell_{2} \ell_{3} \ell_{4}$ resonance would be a pentaquark. Interaction very weak

Real and imaginary parts of the $D K$ and $\bar{D} \bar{K}$ loop functions inside of the nuclear environment


we dress in the medium both the (anti-)charmed and the (anti-)kaon mesons. Larger charge-conjugation asymmetry $\Rightarrow$ different pattern of density corrections to the line-shapes of $D_{S 0}^{*}(2317)^{+}$and $D_{S 0}^{*}(2317)^{-}$
$\rho=0.5 \rho_{0}$


$$
\rho=\rho_{0}
$$



HQSS partner
$D_{S 1}^{*}(2460)^{ \pm}$ isoscalar $J^{P}=1^{+}$
$D^{*} K$ and $\bar{D}^{*} \bar{K}$ molecules

## CONCLUSIONS

- Particle-antiparticle $\left[D_{S 0, S 1}^{*}(2317,2460)^{+} \& D_{S 0, S 1}^{*}(2317,2460)^{-}\right]$line-shapes are necessarily the same in free space, but we have found different density patterns in matter. This large charge-conjugation asymmetry mainly stems from the very different kaon and antikaon interactions with the nucleons of the dense medium. Medium effects strongly depend on the molecular contents
- With increasing densities and molecular probabilities, the $D_{S 0}^{*}(2317)^{+}$peak shifts towards higher energies and becomes less broad than its chargeconjugation partner $D_{S 0}^{*}(2317)^{-}$, whose wider Breit-Wigner-like shape moves more noticeably at lower energies. At half normal nuclear matter density, the change is already so drastic for high molecular component scenarios that $D_{S 0}^{*}(2317)^{+}$and $D_{S 0}^{*}(2317)^{-}$line-shapes hardly overlap.
- Effects violating charge-conjugation symmetry are larger than those found for the $T_{c c}(3875)^{+} \& T_{\bar{c} \bar{c}}(3875)^{-}$tetraquarks embedded in a nuclear environment.


## In summary:

- The nuclear environment breaks charge-conjugation symmetry, and induces different particle-antiparticle line-shapes. If these distinctive density dependencies were experimentally confirmed, it would give support to the presence of important molecular components in these exotic states. This is because if these states were mostly compact fourquark structures, the density behavior of their in-medium lines-shapes, while certainly different, would likely not follow the same patterns found for molecular scenarios


## Back up

