







Muon g-2: Theory vs Experiment

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Present and Future perspectives in Hadron Physics – LNF – 19 June 2024



How to measure $a_{\mu} = (g-2)/2...$



• The frequency with which the spin moves ahead of the momentum in a magnetic field B (anomalous precession frequency ω_a) is:

$$\omega_a = \omega_s - \omega_c = a \frac{eb}{m}$$

• If g>2 (a>o) spin advances respect to the momentum



However there are beam dynamics effects μ

- The muon beam oscillates and breathes as a whole
- The full equation is more complex and corrections due to radial (x) and vertical (y) beam motion are needed



$$\vec{\omega}_{a} = \vec{\omega}_{s} - \vec{\omega}_{c} = -\frac{e}{mc} \left[a_{\mu} \vec{B} - \left(a_{\mu} - \frac{1}{\gamma^{2} - 1} \right) \vec{\beta} \times \vec{E} - a_{\mu} \left(\frac{\gamma}{\gamma + 1} \right) (\vec{\beta} \cdot \vec{B}) \vec{\beta} \right]$$

Running at $\gamma_{\text{magic}} = 29.3$ (p=3.094 GeV/c) this coefficient is null
Because of momentum spread (<0.2%) \rightarrow
Field Correction

Extracting a_{μ}





All these quantities have been evaluated throughout in the analysis of Run2/3 data: Total correction is **622 ppb**, dominated by **E-field & Pitch**

Collected statistics from Muon g-2: x21.9 BNL datasets



On 27 February 2023: proposal Goal of x21 BNL datasets!



7 April 2021: We released our first result





4 Phys Rev journals on April 2021(>1700 citations)





10 August 2023: We released our new result





More than 4 times the statistics of Run1

submitted to PRL on 10 August 2023



hep-ex: 2402.15410 accepted per publication in PRD

Run-2/3 Improvement: Statistics





• Factor 4.7 more data in Run-2/3 than Run-1

Dataset	Statistical Error [ppb]
Run-1	434
Run-2/3	201
Run-1 + Run-2/3	185

Run-2/3 Improvement: Systematics



• Systematic improvements in **all parameters**



Run-2/3 Uncertainties

μ	Ž		
000	g_2	2)~	R
Mu	ion	g-2	

Quantity	Correction [ppb]	Uncertainty [ppb]
$\overline{\omega_c^m}$ (statistical)	[PP~]	201
ω_a^m (systematic)	_	25
$\overline{C_e}$	451	32
C_p	170	10
$\dot{C_{pa}}$	-27	13
$\hat{C_{dd}}$	-15	17
C_{ml}	0	3
$\overline{f_{\rm calib}\langle\omega_p'(\vec{r})\times M(\vec{r})\rangle}$	_	46
B_k	-21	13
B_q	-21	20
$\overline{\mu_{p}'(34.7^{\circ})/\mu_{e}}$	_	11
$\dot{m_{\mu}}/m_{e}$	_	22
$g_e/2$	_	0
Total systematic	_	(70)
Total external parameters	_	\times
Totals	622	215

Total uncertainty is 215 ppb

[ppb]	Run-1	Run-2/3	Ratio
Stat.	434	201	2.2
Syst.	157	70	2.2

 Near-equal improvement: We're still statistically dominated

Systematic uncertainty of 70 ppb surpasses our proposal goal of 100 ppb!

Run-2/3 Result: FNAL + BNL Combination



$a_{\mu}(FNAL) = 116\ 592\ 055(24)\ x10^{-11}\ [203\ ppb]$ $(..) = 10^{-11}$ BNL · [540 ppb] (63) FNAL Run-1 + + [463 ppb] (54) Ð FNAL Run-2/3 [215 ppb] (25) [203 ppb] (24) FNAL Run-1 + Run-2/3 [190 ppb] (22) **World Average** 18.5 21.0 17.5 18.0 19.0 19.5 20.0 20.5 21.5 $a_{,,} \times 10^9 - 1165900$

- FNAL combination:
 203 ppb uncertainty
- Both FNAL and BNL dominated by statistical error
- Combined world average dominated by FNAL values.

a_μ(Exp) = 116 592 059(22) x 10⁻¹¹ [190 ppb]

Run-2/3 Result: FNAL + BNL Combination



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- FNAL combination:
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Size of a_{μ}^{EW} = 153.6(1.0) × 10⁻¹¹

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HVP Calculation: Dispersive (e⁺e⁻) Method

 $\rightarrow a_{\mu}^{\text{HVP,LO}} = \frac{\alpha^2}{3\pi^2} \int_{-\infty}^{\infty} \frac{K(s)}{s}$

Calculated from data for $\sigma(e^+e^- \rightarrow hadrons)$

Analyticity & Unitarity Uses **data** from different experiments from **20+ years**

1/s weights low energy strongly: 73% from $\pi^+\pi^-$ channel



had.



adronic R-ratio

(Data Driven)

K(s) ~1/s

HVP Calculation: Lattice QCD Method





Comparison with SM prediction (2023)





- Comparison of FNAL Run1-3 result with the Theory Initiative's calculation wp20 is at 5 sigma
- Waiting for a clarification of the theory

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Plan to **publish result of the full dataset in 2025** with twice improved statistical precision

~75% of total statisics

~25% of total statisics

Prospects: Theory: HLbL





precision < 15%

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Prospects: Theory: HVP - Lattice

New lattice QCD result for HVP from BMWc (2020) with 0.8% accuracy

 $a_{\mu}^{\rm HVP;LO} = 7075(55) \cdot 10^{-11}$ S. Borsanyi et al., Nature 593, 7857 (2021)





Prospects: Theory: HVP - Lattice





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 $a_{\mu}^{HVP;LO} = 6931 (40) \times 10^{-11} (0.6\%)$ (wp20)

Prospects: Theory: HVP - Lattice



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$$a_{\mu}^{HVP;LO} = 6931 (40) \times 10^{-11} (0.6\%)$$
 (wp20)

 \sqrt{s} [GeV]



Prospects: Theory: HVP – e⁺e⁻ data



Prospects: Theory: HVP – e⁺e⁻ data



Perspectives: $e^+e^- \rightarrow \pi^+\pi^-$



•**BaBar**: a new analysis of $\pi^+\pi^-$ cross section using ISR based on the full statistics (x7) with new analysis technique. A dedicated study of RC show difference with Phokhara MC generator, with possible impact on other experiment. Final results are expected in 2024.

•SND 2020: analysis of $e^+e^- \rightarrow \pi^+\pi^-$ on full statistics (x10) is in progress.

•**BESIII**: Analysis of the $e^+e^- \rightarrow \pi^+\pi^-$ cross section using ISR with ~x6 statistics in progress. Normalization of the di-pion event yield by di-muon events.

• **KLOE**: analysis of x7 larger statistics in progress with improved versions of the Monte Carlo generators for radiative corrections and modern analysis techniques. To avoid possible biases with published KLOE or other experiments the analysis will be blinded.

•Belle-II: measurement of the $e^+e^- \rightarrow \pi^+\pi^-$ cross section, based on the current full data set, is expected by 2025 with a precision comparable to the BABAR 2009 result.



(for more details see https://muon-gm2-theory.illinois.edu)

Other e+e- channels





Perspectives: radiative corrections



- Recent effort on MC (arXiv:2201.12102) and analyses at BaBar [PRD108 11, L111103 (2023)] and CMD-3 [PLB 833 137283 (2022)] have shown the importance of improved treatment of RC and hadron-photon modelization.
 - **Renovated effort** on RC and MC tools towards NNLO MC $\sigma(e+e- \rightarrow hadrons (+\gamma)) \rightarrow$ report by 2024



Team: P. Beltrame, E. Budassi, C. Carloni Calame, G. Colangelo, M. Cottini, A. Driutti, T. Engel, L. Flower, A. Gurgone, M. Hoferichter, F. Ignatov, S. Kollatzsch, B. Kubis, A. Kupsc, F. Lange, D. Moreno, F. Piccinini, M. Rocco, K. Schönwald, A. Signer, G. Stagnitto, D. Stöckinger, P. Stoffer, T. Teubner, W. Torres Bobadilla, Y. Ulrich, G. Venanzoni

WP1:QED for leptons at NNLOWP2:Form factor contributions at N³LOWP3:Processes with hadronsWP4:Parton showersWP5:Experimental input



5th Workstop / Thinkstart: Radiative corrections and Monte Carlo tools for Strong 2020, 5-9 June 2023, Zurich

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Conclusions



- FNAL-E989 (g-2) $_{\mu}$ result at 0.20 ppm (<1/6 of EW contribution) and on the right course to achieve a measurement at 0.14ppm
- Theory situation at the moment limits the comparison:
- Tensions at the level of HVP:
 - between KLOE and BABAR
 - between CMD-3 and earlier experiments (incl. CMD-2!)
 - between BMWc and data-based evaluations (except CMD-3)
- Results on HLbL at $\leq 15\%$ within reach
- More data are being analyzed (BaBar, KLOE) or will become available in the future (BESIII, BelleII,...)

Conclusions



- Important to have independent confirmation of the full BMWc result
- Possibility (in future) for inclusive measurements of HVP in the space-like region (MUonE at CERN)
- Reappraisal of τ -data-based evaluation of HVP [M. Davier, A. H[°]ocker, A. M. Lutz, B. Malaescu, Z. Zhang, arXiv:2312.02053]
- Next milestone on the theory side: updated WP: to be ready before release of FNAL-E989 final analysis (Spring 2025?)

Personal note



 I was very saddened by the news of Carlo. I was lucky to known Carlo since more than 20 years and I was always impressed by his scientific curiosity, his mild and gentle manner, his contagious smile, and his willingness to give his time with great ease. I remember Carlo with great affection and I miss him very much



Thanks Carlo for all your advice, support and friendship!



END

t [µs]

Conclusions



• We've measured a_{μ} to an unprecedented **203 ppb** precision



- New result is in **excellent agreement** with **Run-1 & BNL →** new **world average** has an uncertainty of **190 ppb**
- More than **halved the total uncertainty** from Run-1
- Went beyond our design goal with systematic uncertainty of **70 ppb**.

- A factor ~ x 3 **data** from Run4-6 with a projected twofold improvement on the uncertainty (analysis should be completed by 2025)
- Expect theory improvement on a similar timescale (<u>https://muon-gm2-theory.illinois.edu/</u>)
- Look out for other analyses too: EDM, CPT/LV and Dark Matter searches.

Muon g-2 Collaboration





USA

- Boston
- Cornell
- Illinois
- James Madison
- Kentucky
- Massachusetts
- Michigan
- Michigan State
- Mississippi
- North Central
- Northern Illinois
- Regis
- Virginia
- Washington

USA National Labs

- Argonne
- Brookhaven
- Fermilab

181 collaborators33 Institutions7 countries



China

Shanghai Jiao Tong

Germany

- Dresden
- Mainz

Italy

- Frascati
- Molise
- Naples
- Pisa
- Roma Tor Vergata
- Trieste
- Udine



orea - CAPP/IBS



Ru

- มนนหอากางบงบอเมแจk
- JINR Dubna



United Kingdom

- Lancaster/Cockcroft
- Livarociol
- Manchester
- University College London

Muon g-2 Collaboration

7 countries, 33 institutions, 181 collaborators





Muon g-2 Collaboration Meeting @ Elba, May 2019

Muon g-2 Collaboration (2023)





G. Venanzoni, EPS-HEP2023, Hamburg, 22 August 2023

Running Conditions: Damaged Quad Resistors

رt) [mm] (t) الس] 13.7 (t)

13.6

13.5

- Run-1 had damaged resistors in 2/32 quad plates leading to unstable beam storage
- Resistors replaced before Run-2



13.4 13.3 Vertical beam width change 13.2 50 100 150 200 Time [us] φ_{pa}(t) [mrad] -22.2 ω_a phase change -22.25 -22.3 -22.4 Run-1d -22.45 Run-3a 50 100 200 150 Time [µsB7

Muon g-2

• Run-1d

Run-3a

- C_{pa} uncertainty is reduced (**75 ppb** \rightarrow **13 ppb**) -22.35 thanks to a more stable beam
- Beam oscillation frequencies are also more stable

G. Venanzoni, EPS-HEP2023, Hamburg, 22 August 2023

Other systematic improvements



• Running conditions:

- Improved cooling of the hall and added insulation of the magnet which made the magnetic field more stable
- Improved kicker strength which made the orbit more centered and reduced the E-field correction

Improved measurements:

- Extensive measurement of vibration the quadrupoles in multiple locations around the ring
- Reduced vibration noise for kicker transient field measurement
- Analysis improvements:
 - Improved treatment of the pileup for ω_{a} analysis
 - Improved analysis of E-field correction including correlations between momentum & time of injection.

July 24th 2023: Unblinding



- Muon g-2 analysis has software & hardware blinding
- Unblinding meeting in Liverpool:



Photo credits: McCoy Wynne

- Unanimous vote from all collaborators to unblind!
- Secret envelopes were finally opened to reveal the hidden clock frequencies and the result...



Measuring the wobble frequency



SM prediction



Contribution	Section	Equation	Value $\times 10^{11}$	References
Experiment (E821)		Eq. (8.13)	116 592 089(63)	Ref. [1]
HVP LO (e^+e^-)	Sec. 2.3.7	Eq. (2.33)	6931(40)	Refs. [2–7]
HVP NLO (e^+e^-)	Sec. 2.3.8	Eq. (2.34)	-98.3(7)	Ref. [7]
HVP NNLO (e^+e^-)	Sec. 2.3.8	Eq. (2.35)	12.4(1)	Ref. [8]
HVP LO (lattice, udsc)	Sec. 3.5.1	Eq. (3.49)	7116(184)	Refs. [9–17]
HLbL (phenomenology)	Sec. 4.9.4	Eq. (4.92)	92(19)	Refs. [18–30]
HLbL NLO (phenomenology)	Sec. 4.8	Eq. (4.91)	2(1)	Ref. [31]
HLbL (lattice, <i>uds</i>)	Sec. 5.7	Eq. (5.49)	79(35)	Ref. [32]
HLbL (phenomenology + lattice)	Sec. 8	Eq. (8.10)	90(17)	Refs. [18–30, 32]
QED	Sec. 6.5	Eq. (6.30)	116584718.931(104)	Refs. [33, 34]
Electroweak	Sec. 7.4	Eq. (7.16)	153.6(1.0)	Refs. [35, 36]
HVP (e^+e^- , LO + NLO + NNLO)	Sec. 8	Eq. (8.5)	6845(40)	Refs. [2–8]
HLbL (phenomenology + lattice + NLO)	Sec. 8	Eq. (8.11)	92(18)	Refs. [18–32]
Total SM Value	Sec. 8	Eq. (8.12)	116 591 810(43)	Refs. [2-8, 18-24, 31-36]
Difference: $\Delta a_{\mu} := a_{\mu}^{\exp} - a_{\mu}^{SM}$	Sec. 8	Eq. (8.14)	279(76)	



Creating the Muon Beam for g-2 Muon g-2

- 8 GeV p batch into Recycler
- Split into 4 bunches
- Extract 1 by 1 to strike target
- Long FODO channel to collect $\pi \rightarrow \mu v$
- p/ π/μ beam enters DR; protons kicked out; π decay away
- μ enter storage ring



APRIL 2017

RING

24 Calorimeter stations located all around the ring

NMR probes and electronics located all around the ring

Kicker

QUADS

Inflector

ω_p' measurement



- Trolley maps of the magnetic field at about 9000 locations over the entire azimuth every 3 days
- Fixed probes at 72 locations to interpolate the field during muon storage between the trolley runs
- Need calibration to convert the 17 NMR trolley to water sample

$$\delta_{\omega_p'} \sim 48 ppb$$

Uncertainty due to: 1.Temperature Corrections 2.Configuration Corrections 3.Trolley Map Systematics 4.Fixed Probe Systematics 5.Tracking Drift Uncertainty



$\omega_p' \to \widetilde{\omega}_p'$: muon weighted average



- Need field actually experienced by muons
- Muon decay point estimated from e+ track reconstructed by the two straw trackers inside storage vacuum
- Use beam dynamics models, tuned to the tracker data, to get distribution all around the ring
- Systematic uncertainty due to probe calibrations, field map, tracker alignment and BD model

$$\delta_{\widetilde{\omega'}_p}$$
 ~56 ppb

Muon's view of a tracker





The magnetic field is measured using pulsed-proton NMR where the proton "wobble" frequency ω_p is measured

