

Precision Hadron Spectroscopy of Light and Heavy Quarks

Meike Küßner

Ruhr-Universität Bochum and now University of Bonn

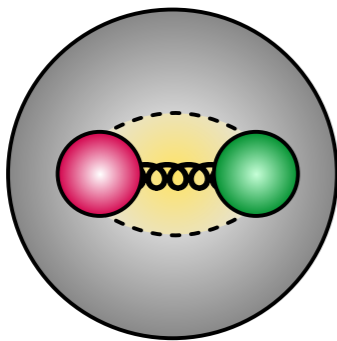
Present and future perspectives in Hadron Physics - Frascati

19th of June 2024

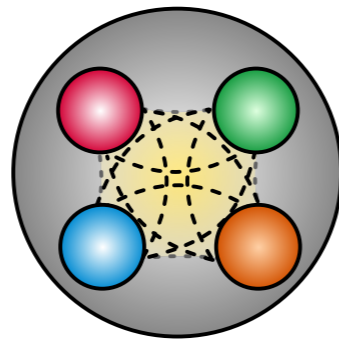


From the Perspective of Strong Interaction

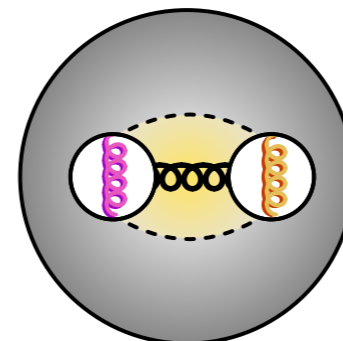
- The mass of hadrons is predominantly generated by strong interaction (>90% in case of the proton)
- To understand how mass is generated we investigate other systems, e.g. with explicit gluonic degrees of freedom



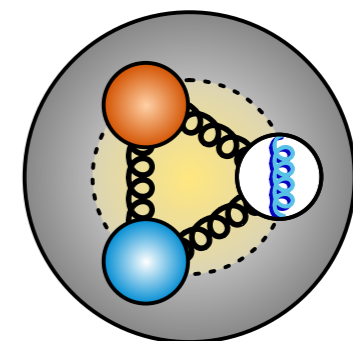
Meson



Tetraquark



Glueball



Hybrid

- For a fermion-antifermion system not all quantum numbers can be formed

$$P = (-1)^{L+1}, C = (-1)^{L+S}$$

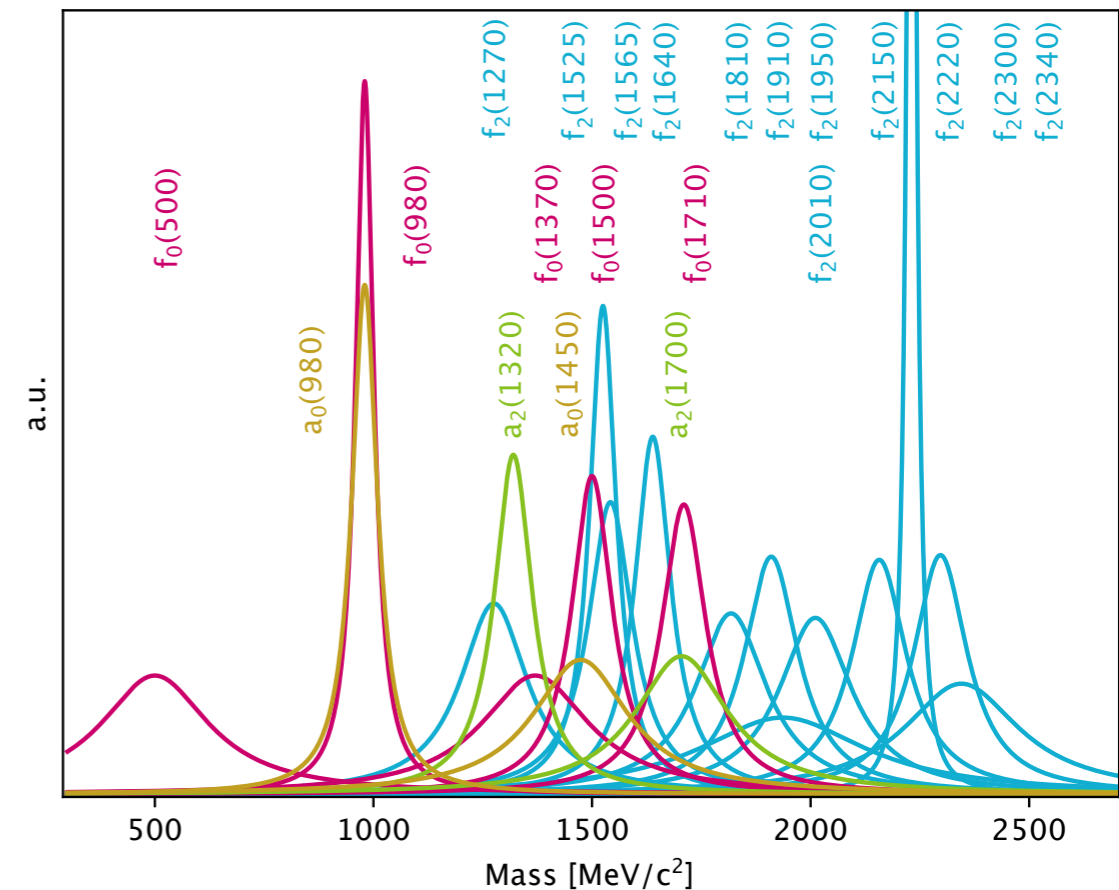
- Exotic quantum numbers: $J^{PC} = 0^{+-}, 0^{-+}, 1^{-+}, 2^{+-}, \dots$

- But: Further states have been found which show odd properties or even exotic quantum numbers!

Light Meson Regime

- Light meson regime is extremely populated!
- Several (broad) interfering resonances of the same q.n.
- Various inelastic channels and thresholds opening
- Identifying and measuring resonance properties is not straight forward
- Resonances not always look like peaks
 - ↔ Peaks not necessarily caused by a resonance
- Analysing a single channel is not enough to disentangle states unambiguously
- More sophisticated tools and descriptions needed!

spectrum of well established states



We should start thinking beyond experimental collaborations!

Experimental Possibilities

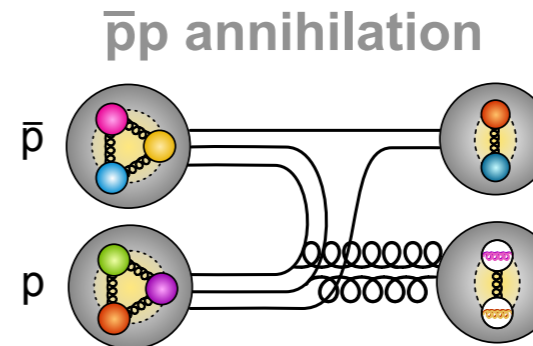
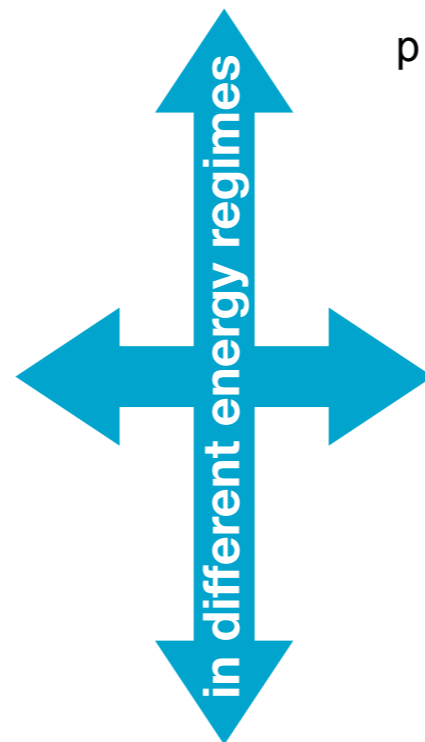
- Each experiment, detector and process has its own advantages
- To tackle these challenges, we need to combine forces

Gluon rich processes

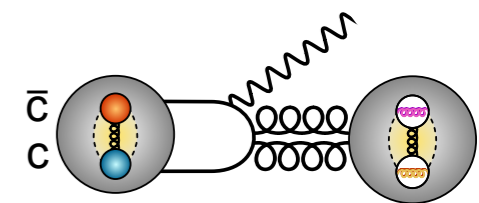
- Radiative charmonium decays
- $\bar{p}p$ annihilation
- pp central production
- ...

QED mediated process

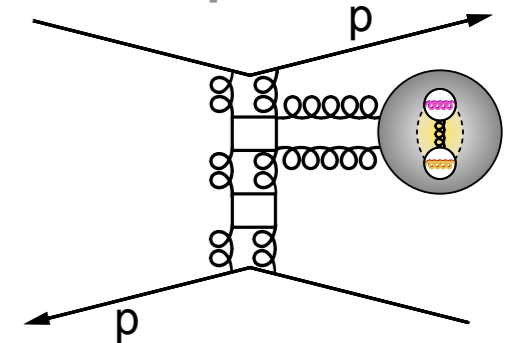
- Two-photon production



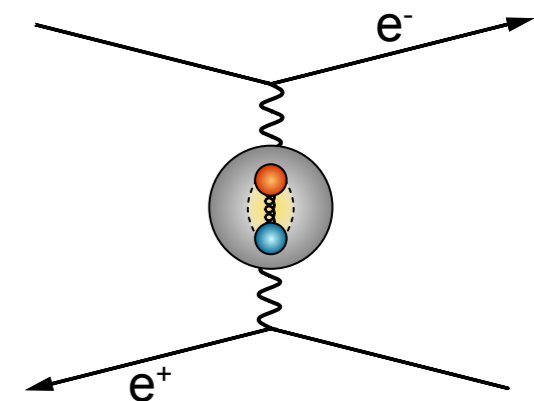
radiative J/ψ decays



central production



two-photon production

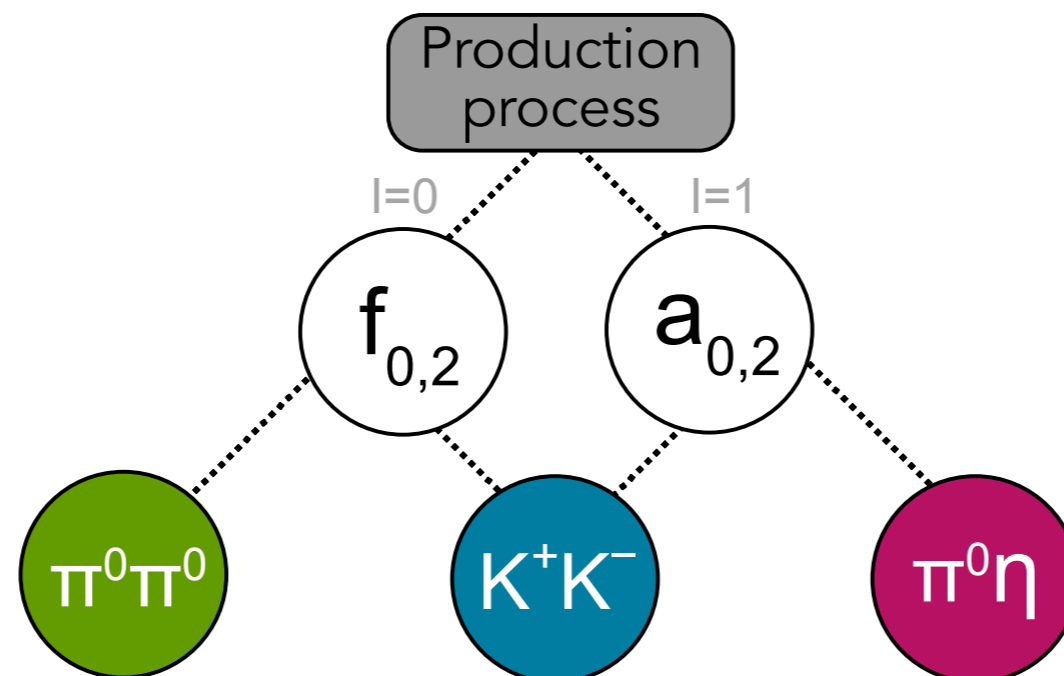


Combine different production mechanisms and decay channels to reveal a particle's nature

Why Coupled Channel Approach?

Advantages compared to single channel fits:

- More constraints due to common amplitudes and shared parameters
- Conservation of unitarity by using sophisticated models as e.g. K-matrix, N/D, ...
- Better description of threshold effects
- Multiple resonances directly measurable in one analysis
- Proper determination of pole parameters and coupling strengths

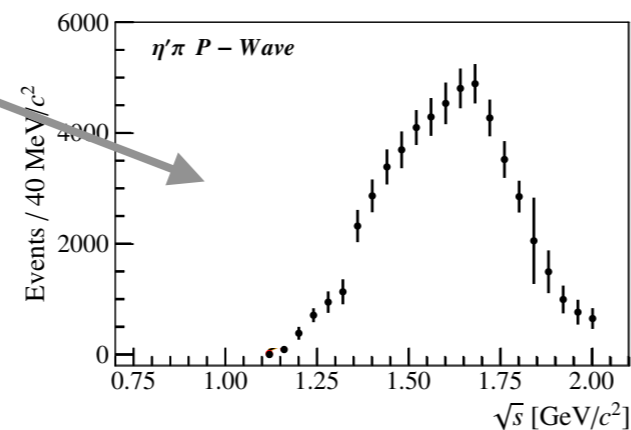
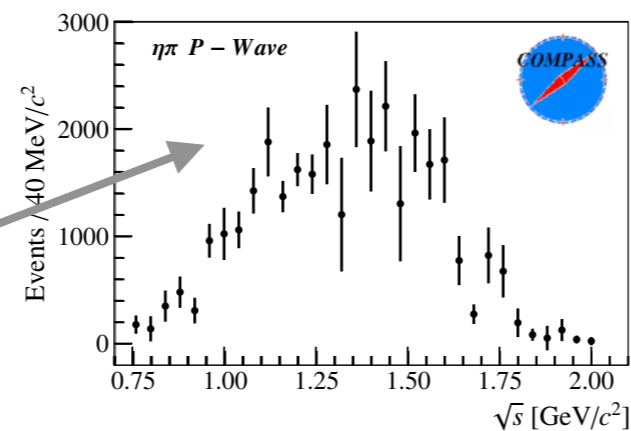


One Prominent Example: The Lightest Hybrid Candidate

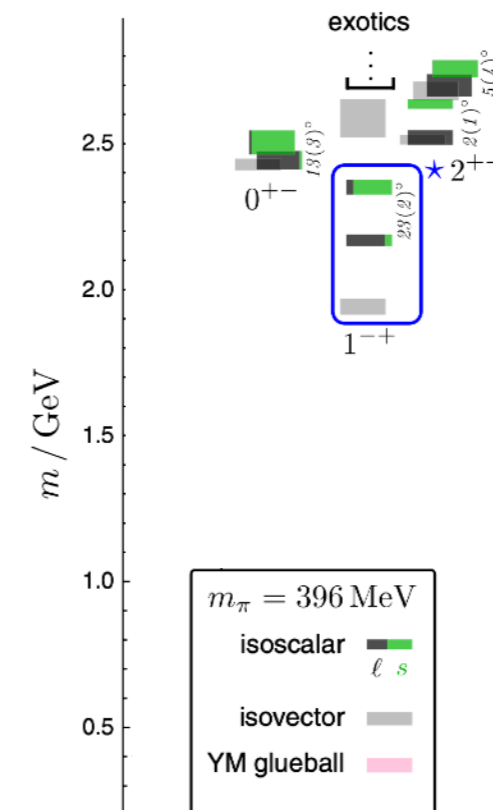
Two π_1 hybrid candidates below 2 GeV are listed in PDG

- one at around 1.4 GeV only seen in $\pi\eta$
 - the other at around 1.6 GeV seen in $\pi\eta'$ but not in $\pi\eta$
- ➔ Parameters obtained by Breit-Wigner fits!
- ➔ Theory: Only one π_1 state predicted slightly below 2 GeV

200 MeV apart!

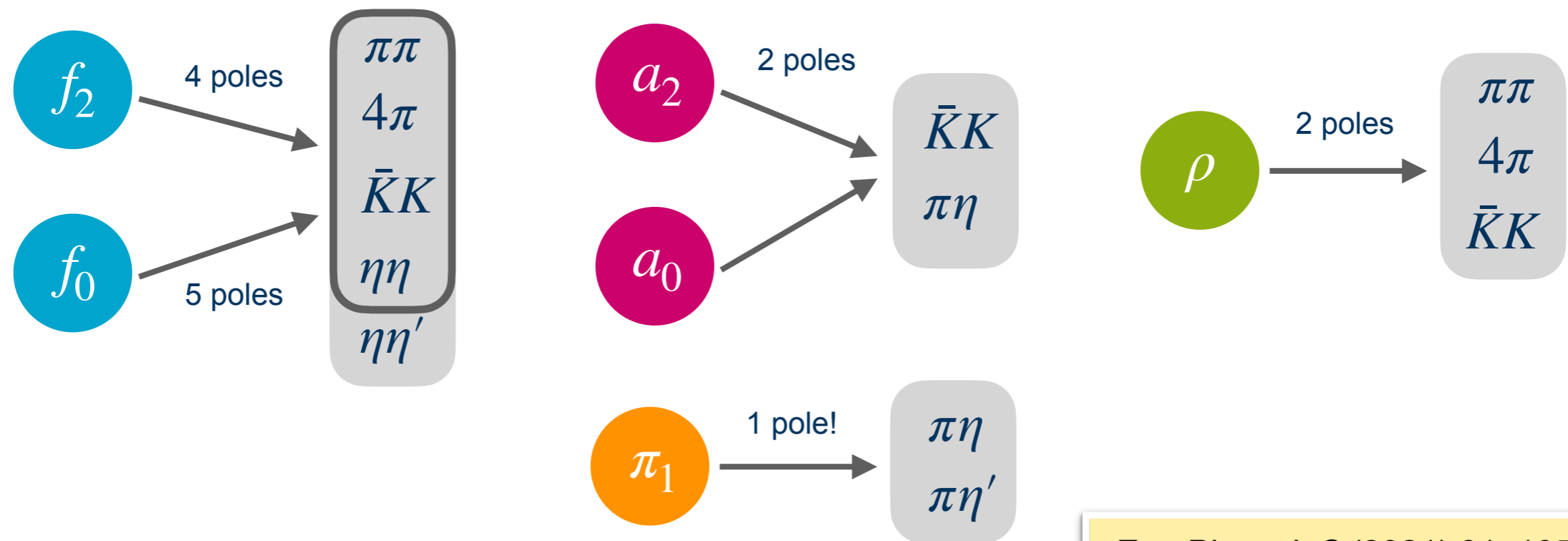


Phys.Rev. D84 (2011) 074023



Coupled Channel Analysis of $\bar{p}p \rightarrow \pi^0 \pi^0 \eta$, $\pi^0 \eta \eta$ and $K^+ K^- \pi^0$

- Combining data from different experiments:
- $\bar{p}p \rightarrow \pi^0 \pi^0 \eta$, $\pi^0 \eta \eta$ and $K^+ K^- \pi^0$ data in flight from Crystal Barrel at LEAR
- COMPASS data of P- and D-waves in the $\pi\eta$ and $\pi\eta'$ systems
- 11 different $\pi\pi$ scattering data samples
- Simultaneously described using the K-Matrix formalism in the P-vector approach
- The whole process from the initial to the final state is described in all phase space dimensions

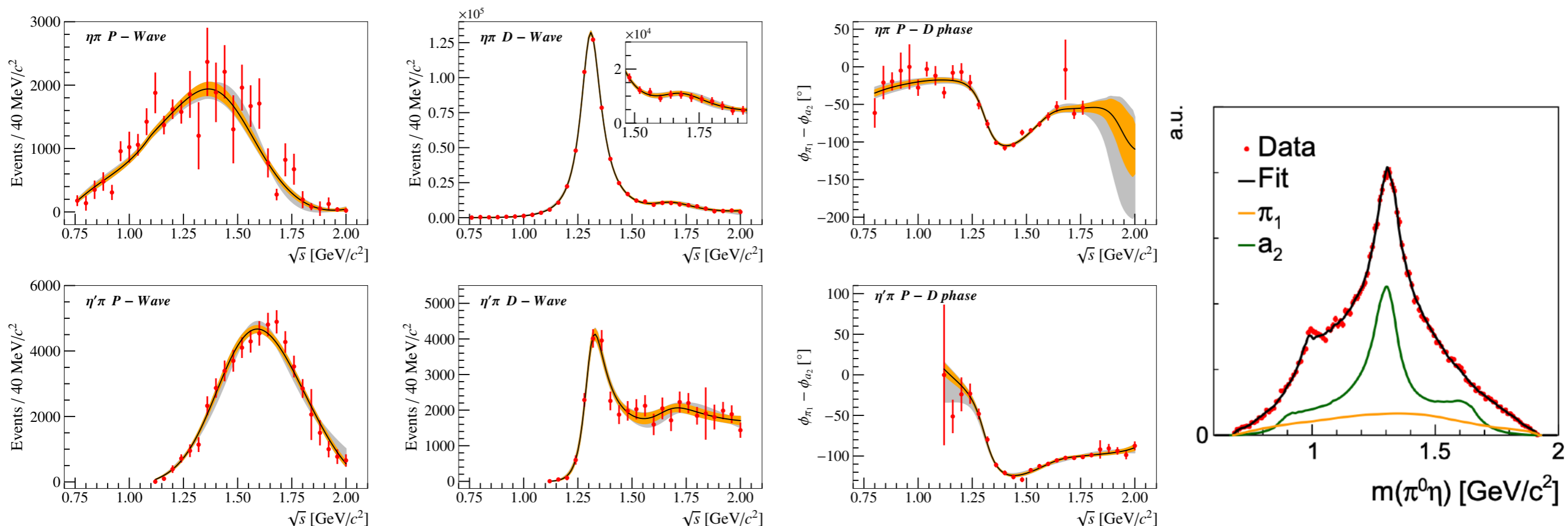


Eur. Phys. J. C (2021) 81, 1056

Coupled Channel Analysis of $\bar{p}p \rightarrow \pi^0 \pi^0 \eta$, $\pi^0 \eta \eta$ and $K^+ K^- \pi^0$

Eur. Phys. J. C (2021) 81, 1056

- Exotic π_1 wave significantly contributing in the $\pi^0 \eta$ system!
- Description with one pole possible!
- ➔ Confirmation of the JPAC analysis based on N/D-method *Phys. Rev. Lett.* 122 (2019) 4, 042002

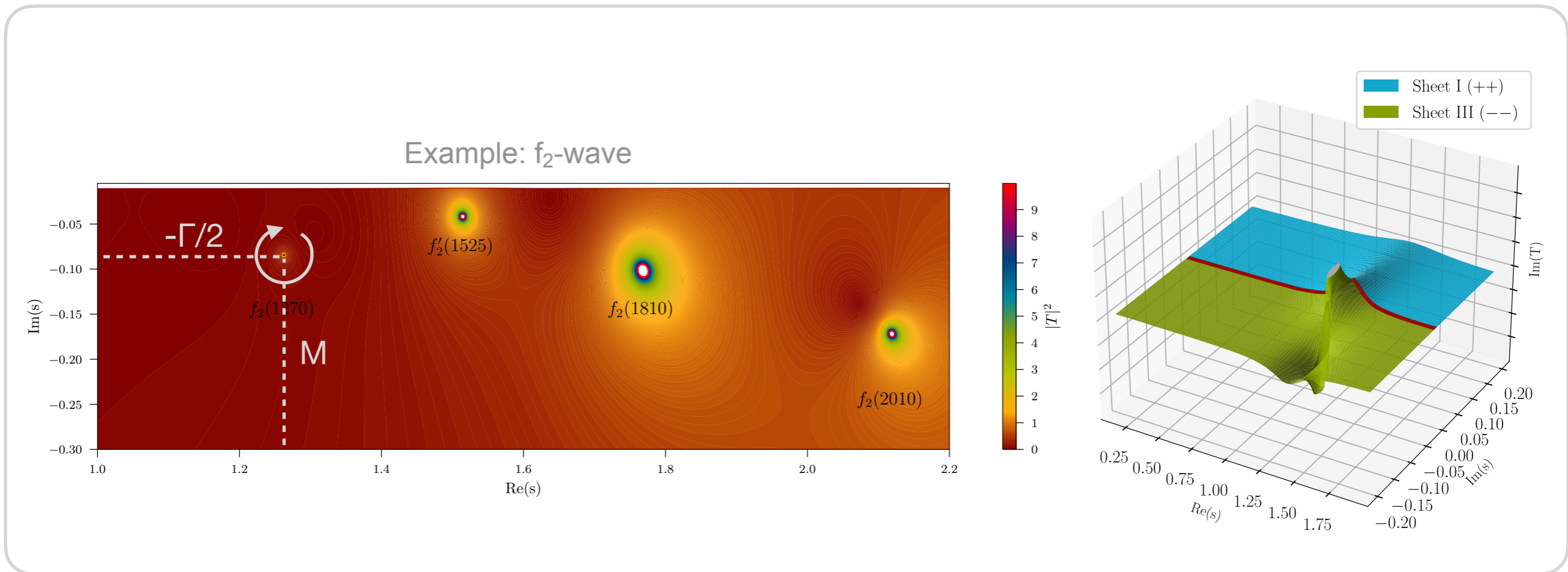


Obtained pole position:

$$M = 1623 \pm 47_{-75}^{+24} \text{ MeV}/c^2$$

$$\Gamma = 455 \pm 88_{-175}^{+144} \text{ MeV}$$

Extraction of Resonance Properties



- K-matrix and thus the pole itself contain all resonance properties
- Masses and widths defined by the pole position in the complex energy plane of the T-matrix sheet closest to the physical sheet

$$Res_{k \rightarrow k}^{\alpha} = \frac{1}{2\pi i} \oint_{C_{z\alpha}} \sqrt{\rho_k} \cdot T_{k \rightarrow k}(z) \cdot \sqrt{\rho_k} dz$$

Coupled Channel Analysis of $\bar{p}p$ and COMPASS Data

name	relevant data	Breit-Wigner mass [MeV/ c^2]	Breit-Wigner width Γ [MeV]
$K^*(892)^\pm$	$\bar{p}p$	$893.8 \pm 1.0 \pm 0.8$	$56.3 \pm 2.0 \pm 1.0$
$\phi(1020)$	$\bar{p}p$	$1018.4 \pm 0.5 \pm 0.2$	4.2 (fixed)

name	relevant data	pole mass [MeV/ c^2]	pole width Γ [MeV]
$f_0(980)^{----++}$	scat	$977.8 \pm 0.6 \pm 1.4$	$98.8 \pm 6.6 \pm 11.2$
$f_0(980)^{--++++}$	scat	$992.6 \pm 0.3 \pm 0.5$	$61.2 \pm 1.2 \pm 1.7$
$f_0(1370)$	scat	$1281 \pm 11 \pm 26$	$410 \pm 12 \pm 50$
$f_0(1500)$	$\bar{p}p + \text{scat}$	$1511.0 \pm 8.5^{+3.5}_{-14.0}$	$81.1 \pm 4.5^{+26.9}_{-0.5}$
$f_0(1710)$	$\bar{p}p + \text{scat}$	$1794.3 \pm 6.1^{+47.0}_{-61.2}$	$281 \pm 32^{+12}_{-80}$
$f_2(1810)$	scat	$1769 \pm 26^{+3}_{-26}$	$201 \pm 57^{+13}_{-87}$
$f_2(X)$	scat	$2119.9 \pm 6.4^{+25.7}_{-1.1}$	$343 \pm 11^{+32}_{-11}$

name	relevant data	pole mass [MeV/ c^2]	pole width Γ [MeV]	$\Gamma_{\pi\eta'}/\Gamma_{\pi\eta}$ [%]
π_1	$\bar{p}p + \pi p$	$1623 \pm 47^{+24}_{-75}$	$455 \pm 88^{+144}_{-175}$	$554 \pm 110^{+180}_{-27}$

name	relevant data	pole mass [MeV/ c^2]	pole width Γ [MeV]	$\Gamma_{KK}/\Gamma_{\pi\eta}$ [%]
$a_0(980)^{--}$	$\bar{p}p$	$1002.7 \pm 8.8 \pm 4.2$	$132 \pm 11 \pm 8$	$14.8 \pm 7.1 \pm 3.6$
$a_0(980)^{-+}$	$\bar{p}p$	$1003.3 \pm 8.0 \pm 3.7$	$101.1 \pm 7.2 \pm 3.0$	$13.5 \pm 6.2 \pm 3.1$
$a_0(1450)$	$\bar{p}p$	$1303.0 \pm 3.8 \pm 1.9$	$109.0 \pm 5.0 \pm 2.9$	$396 \pm 72 \pm 72$

name	relevant data	pole mass [MeV/ c^2]	pole width Γ [MeV]	$\Gamma_{KK}/\Gamma_{\pi\eta}$ [%]	$\Gamma_{\pi\eta'}/\Gamma_{\pi\eta}$ [%]
$a_2(1320)$	$\bar{p}p + \pi p$	$1318.7 \pm 1.9^{+1.3}_{-1.3}$	$107.5 \pm 4.6^{+3.3}_{-1.8}$	$31 \pm 22^{+9}_{-11}$	$4.6 \pm 1.5^{+7.0}_{-0.6}$
$a_2(1700)$	$\bar{p}p + \pi p$	$1686 \pm 22^{+19}_{-7}$	$412 \pm 75^{+64}_{-57}$	$2.9 \pm 4.0^{+1.1}_{-1.2}$	$3.5 \pm 4.4^{+6.9}_{-1.2}$

name	relevant data	pole mass [MeV/ c^2]	pole width Γ [MeV]	$\Gamma_{\pi\pi}/\Gamma$ [%]	Γ_{KK}/Γ [%]	$\Gamma_{\eta\eta}/\Gamma$ [%]
$f_2(1270)$	$\bar{p}p + \text{scat}$	$1262.4 \pm 0.2^{+0.2}_{-0.3}$	$168.0 \pm 0.7^{+1.7}_{-0.1}$	$87.7 \pm 0.3^{+4.8}_{-4.4}$	$2.6 \pm 0.1^{+0.1}_{-0.2}$	$0.3 \pm 0.1^{+0.0}_{-0.1}$
$f_2'(1525)$	$\bar{p}p + \text{scat}$	$1514.7 \pm 5.2^{+0.3}_{-7.4}$	$82.3 \pm 5.2^{+11.6}_{-4.5}$	$2.1 \pm 0.3^{+0.8}_{-0.0}$	$67.2 \pm 4.2^{+5.0}_{-3.8}$	$9.8 \pm 3.8^{+1.7}_{-3.3}$
$\rho(1700)$	$\bar{p}p + \text{scat}$	$1700 \pm 27^{+13}_{-16}$	$181 \pm 25^{+0.0}_{-16}$	$13.6 \pm 1.2^{+0.9}_{-0.5}$	$0.8 \pm 0.1^{+0.0}_{-0.0}$	-

Several resonance properties measured simultaneously within one fit!

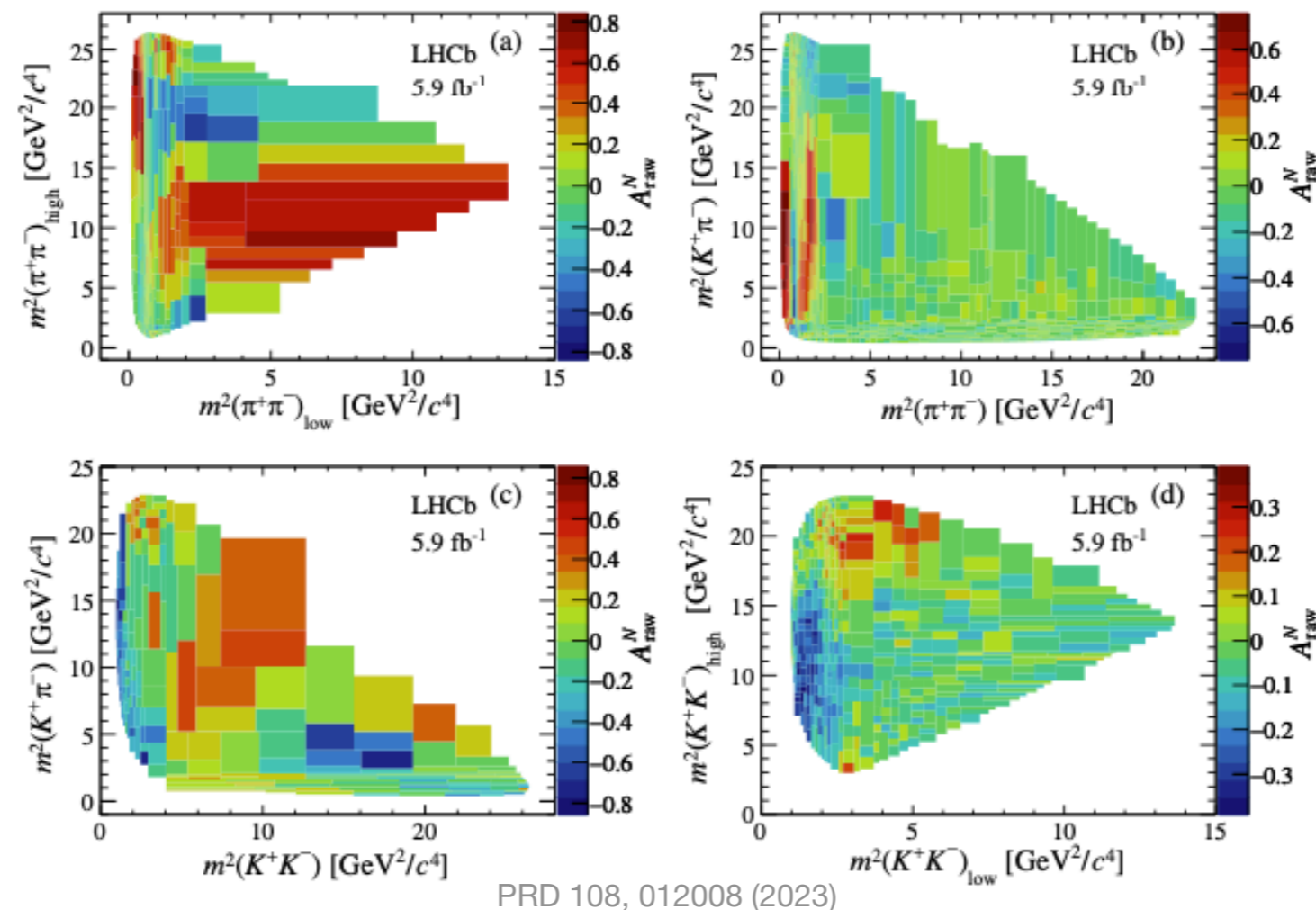
**This parameterisation is universal -
Can be used in other analyses!**



PArtial Wave Interactive ANalysis

Input for CP Violation Studies?

- CP violation in $B \rightarrow 3h$ is very much depending on intermediate resonances
- Strong and weak phase CPV contributions need to be separated
- ➔ Mechanisms from strong interaction as final state interaction assumed to play a big role!
- The hadron spectroscopy community has the tools!
- Descriptions for $(\pi\pi)_{S/D}$ above $2 \text{ GeV}/c^2$ needed - scattering data missing



Learning More About the Inner Structure

Besides measuring resonance parameters as mass, width, ...

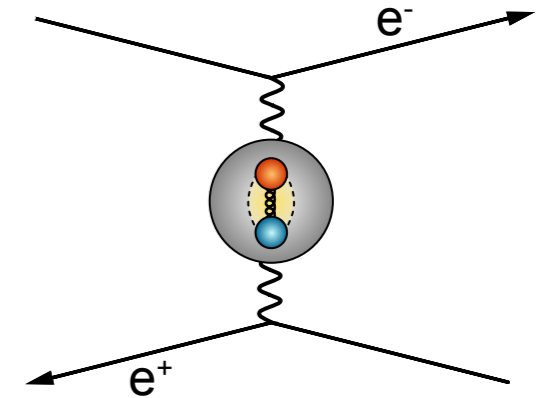
Usually: Measure form factors!

Two photon physics

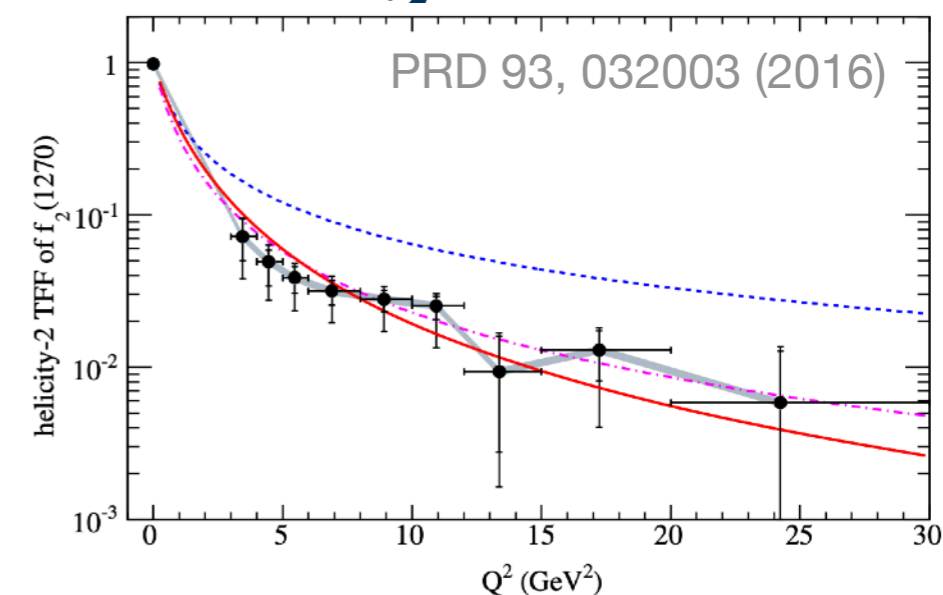
- Clean e.m. process, only sensitive to charge
- Complementary information on glueball candidates!
- States with even C-parity $0^{\pm+}, 2^{\pm+}, \dots$ can be directly produced

Untagged reactions:

- Scattering angles of electron and positron are small and are not detectable
- Quasi real photons carrying small virtuality \rightarrow spin 1 strongly suppressed

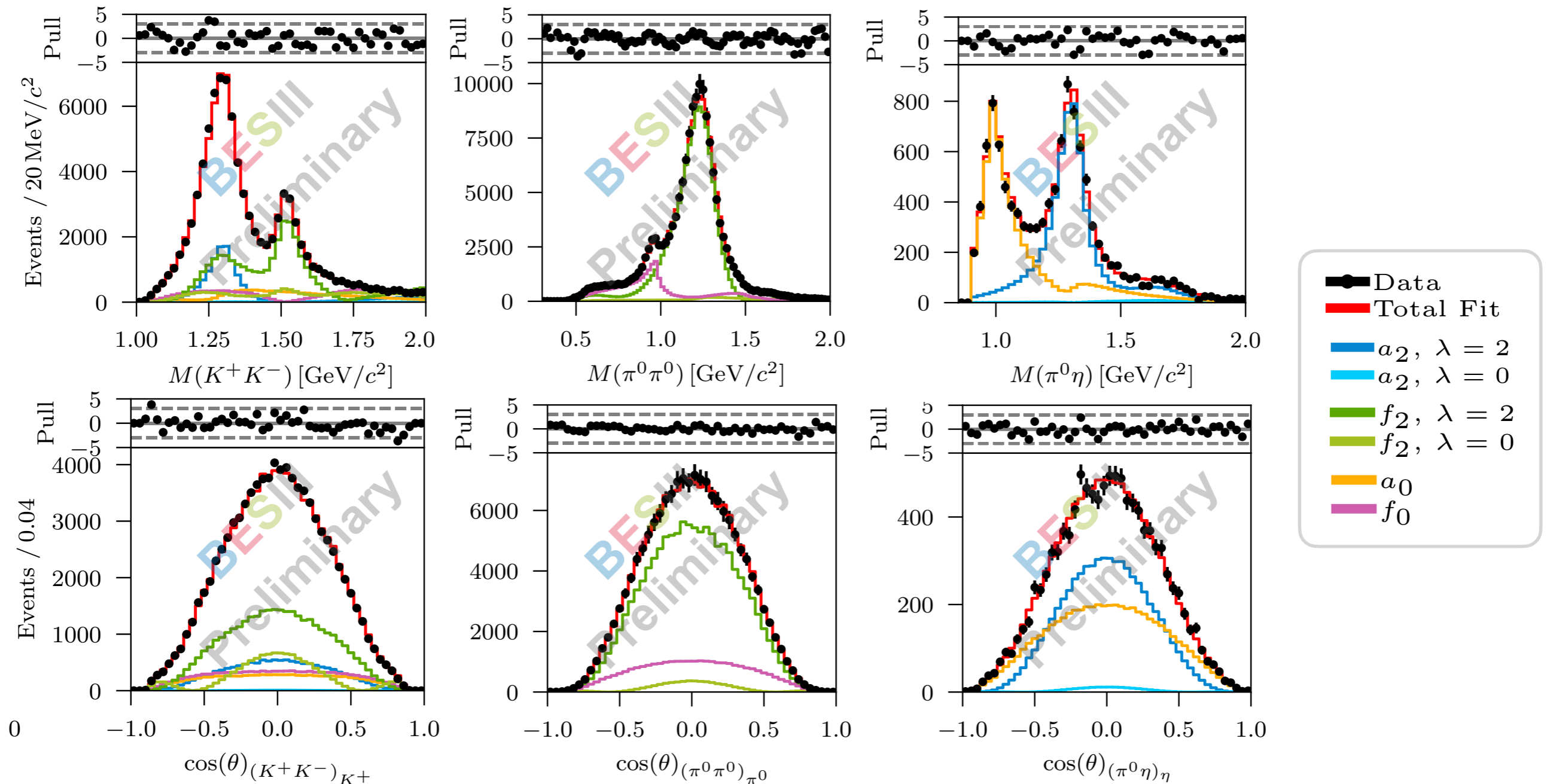


TFF of $f_2(1270)$ by BELLE



Coupled Channel Analysis of Two-Photon Data

- K-matrix parameterisation (*EPJ C* (2021) 81, 1056) fixing all pole parameters on decay side
- Determination of two-photon width based on pole residue (even for f_0 wave)

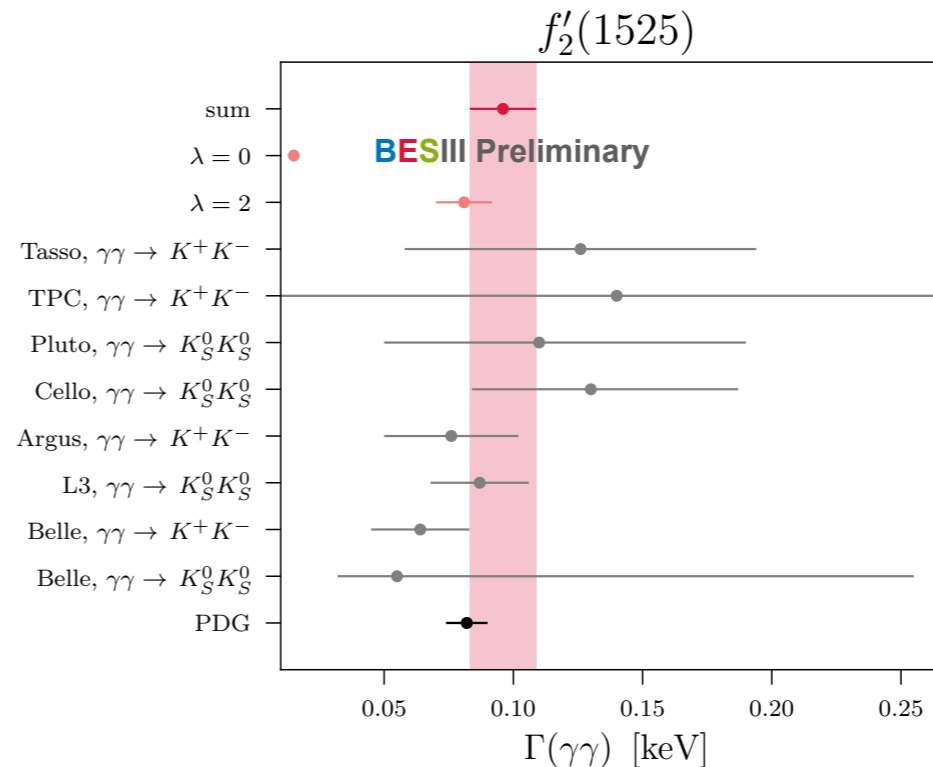
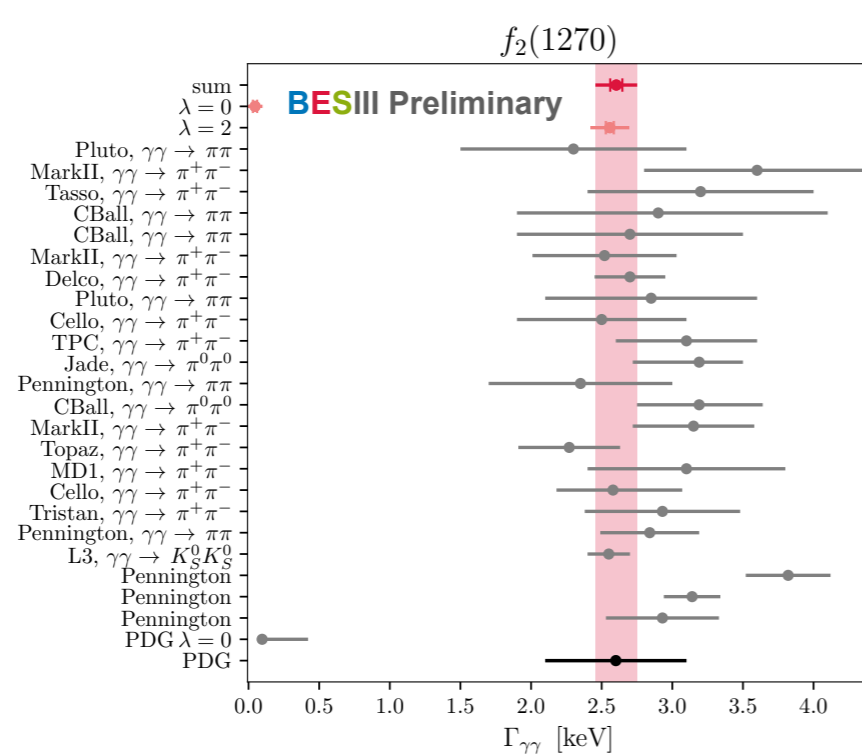


Determination of the Coupling Strength

- Determination of the two-photon width using the F-vector pole residue itself

$$\Gamma(X \rightarrow \gamma\gamma) = \frac{\alpha^2}{4(2J+1)M_R} \cdot \frac{\text{Res}_X(\gamma\gamma \rightarrow FS)}{\Gamma_{dec}}$$

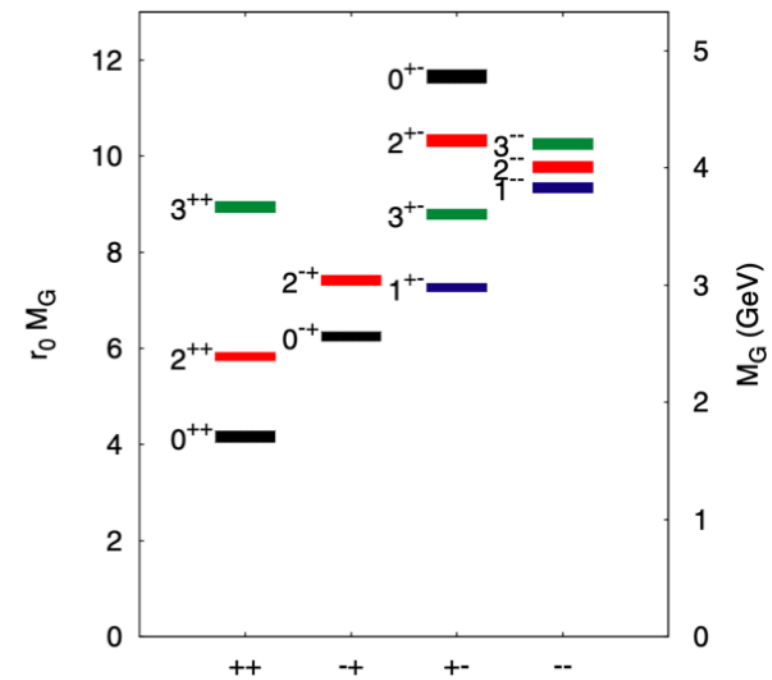
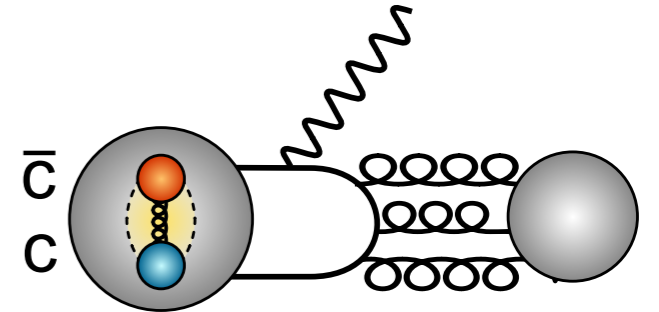
Phys. Rev. D **90**, 036004



- First determination of the helicity contributions for the $f'_2(1525)$
- Most accurate measurement for $f_2(1270)$ and $a_2(1320)$
- Scalar mesons $f_0(1370)$, $f_0(1500)$ und $f_0(1710)$ measured for the first time

Unique Features of Radiative J/ψ decays

- Gluon-rich process → production of glueballs expected
- Lightest glueball 0^{++} is predicted below $2 \text{ GeV}/c^2$
- Observed states $f_0(1370)$, $f_0(1500)$, $f_0(1710)$ likely to be mixtures of pure glueball and quark component
- BESIII has accumulated very high statistics at J/ψ
 - 50 times more than 10 years ago!



Phys. Rev. D 73, 014516 (2006)

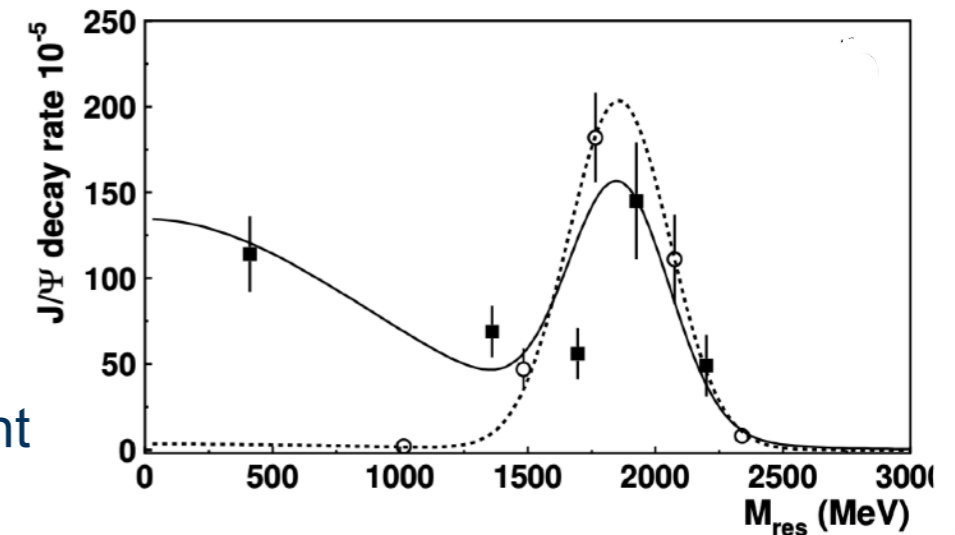
Physics-, statistics- and phase space-wise great opportunities to search for glueball candidates!

Recent Analyses

Coupled channel fit by Sarantsev et. al.:

Phys. Lett. B 816 (2021), 136227

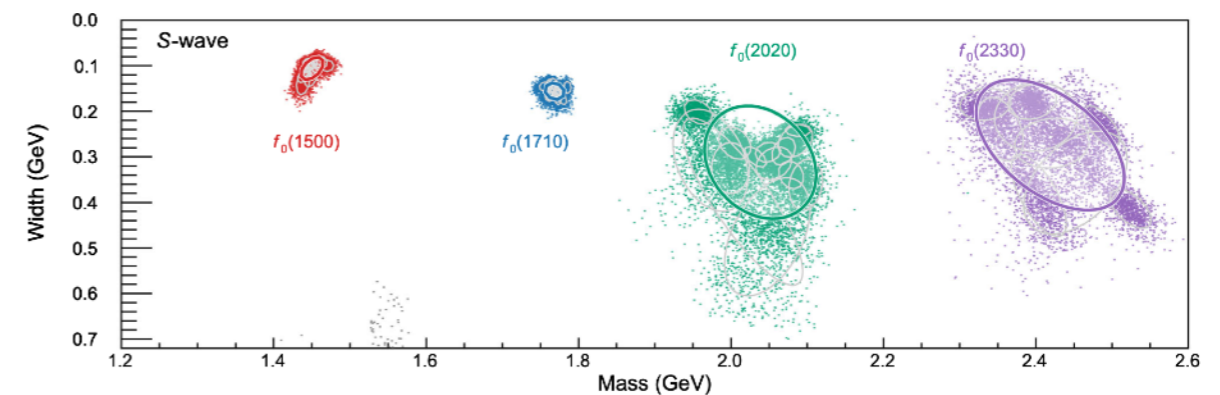
- $J/\psi \rightarrow \gamma + (\pi^0\pi^0, K_S^0K_S^0, \eta\eta, \omega\phi)$ (BESIII)
 - $\pi^+\pi^-$ - scattering data (CERN-Munich, GAMS, BNL)
 - $\bar{p}N \rightarrow 3$ mesons (CB-LEAR)
- Indirect hint for the light scalar glueball candidate by measuring production strengths of scalar states
 - 0^{++} glueball mixing interpretation via coupling of the 10 different scalar singlet and octet states



Coupled channel fit by JPAC group:

EPJ C 82, 80 (2022)

- Used $J/\psi \rightarrow \gamma \pi^0\pi^0, \gamma K_S^0K_S^0$ (BESIII) data
- Only 4 scalar poles needed - not as 10
- No statement towards glueball contributions
- But: Theory has only access to binned data based on older data samples

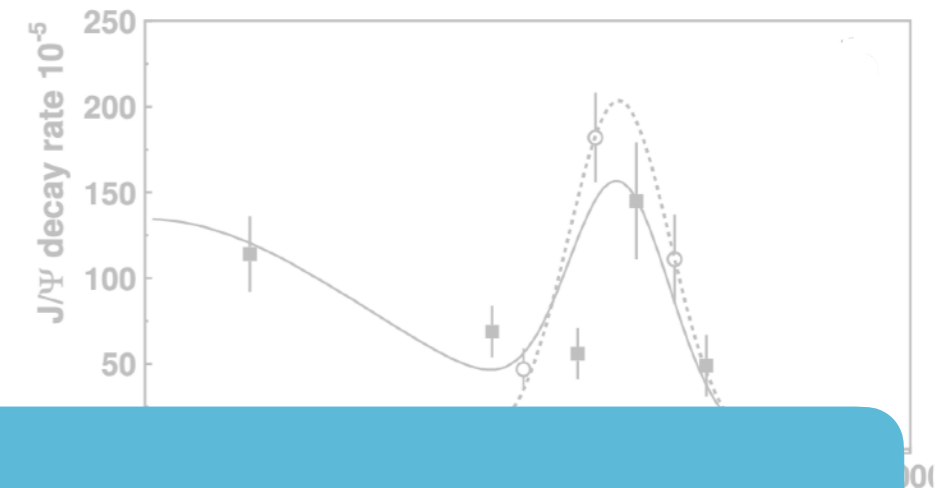


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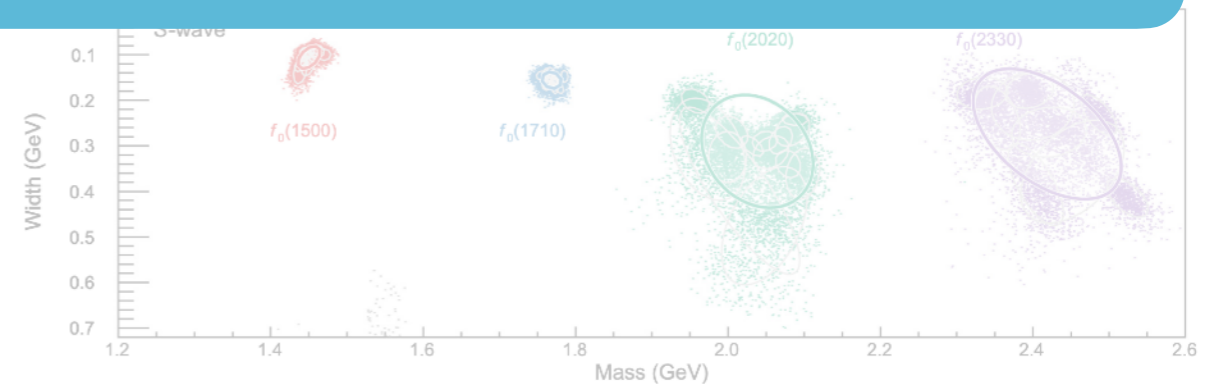
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- Indirect hint for the light scalar glueball candidate by measuring production strengths of scalar states



Much higher statistics available now - *50 times more!*

Event based mass-independent and coupled channel amplitude analyses in preparation for $J/\psi \rightarrow \gamma\pi^0\pi^0$, $\gamma K_S^0K_S^0$ and $\gamma\eta\eta$!

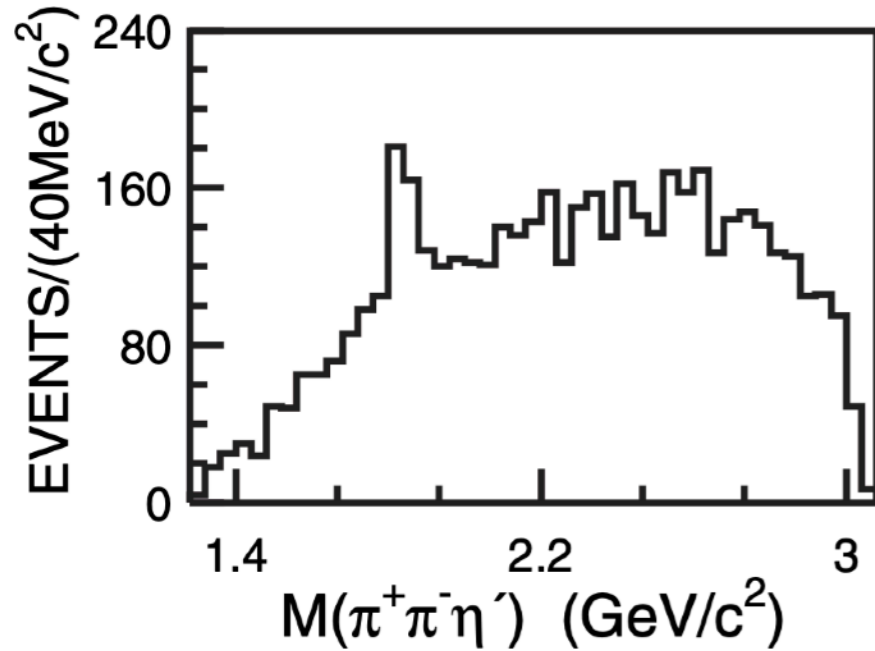
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- But: Theory has only access to binned data based on older data samples



$$J/\psi \rightarrow \gamma \eta' \pi^+ \pi^-$$

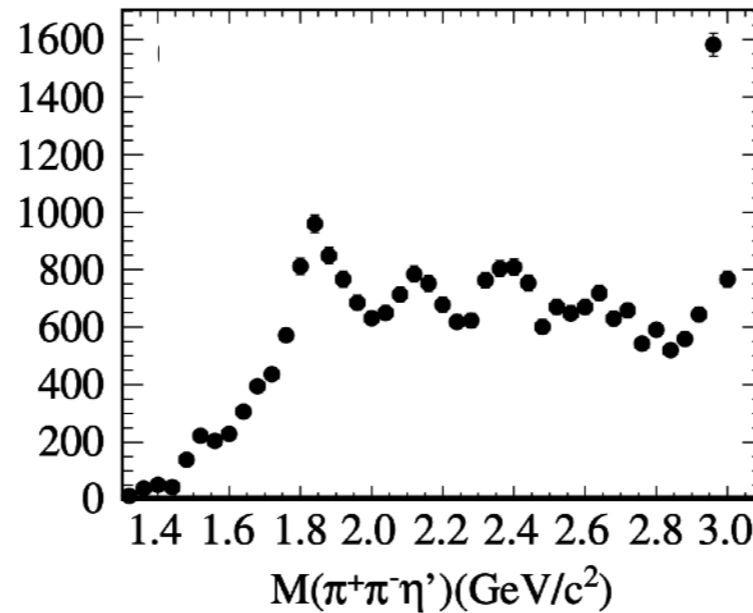
PRL 129, 042001 (2022)

58M J/ψ events



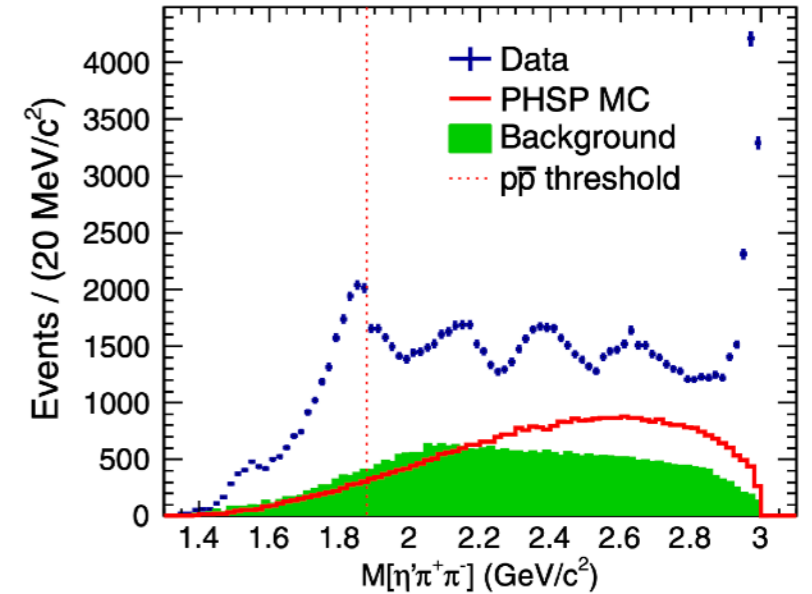
BES, PRL 95, 262001 (2005)

225M J/ψ events



BESIII, PRL 106, 072002 (2011)

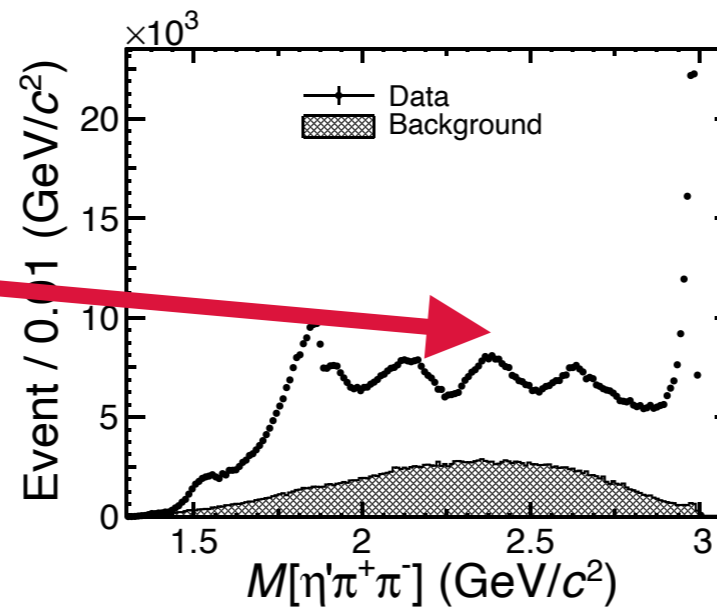
1090M J/ψ events



BESIII, PRL 117, 042002 (2016)

- Spin-parity of $X(2370)$ recently determined to be 0^{-+} !

PRL 132 181901 (2024)



BESIII, PRL 129, 042001 (2022)

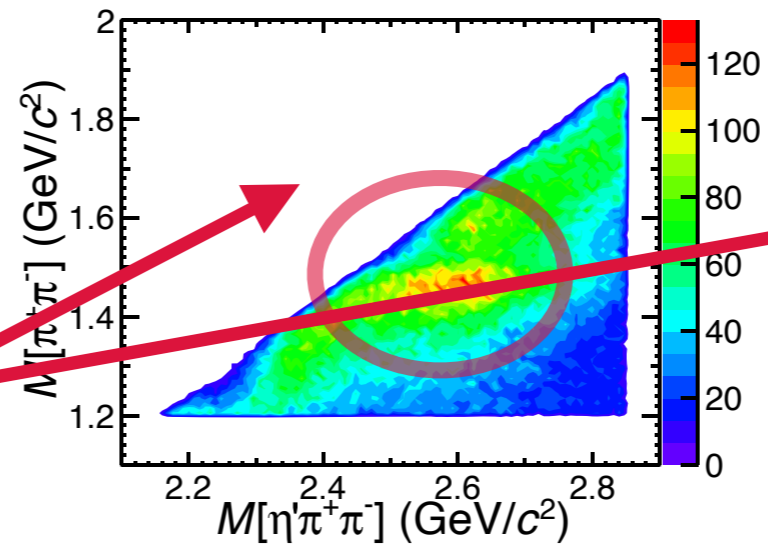
10B J/ψ events

$$J/\psi \rightarrow \gamma \eta' \pi^+ \pi^-$$

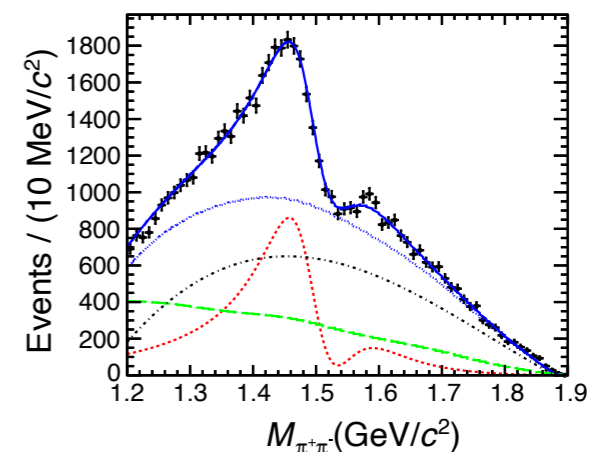
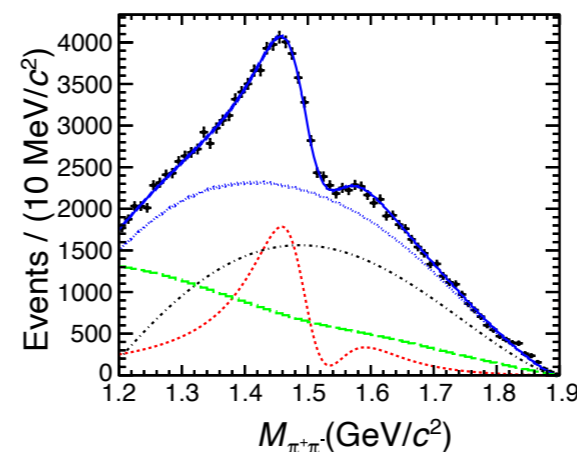
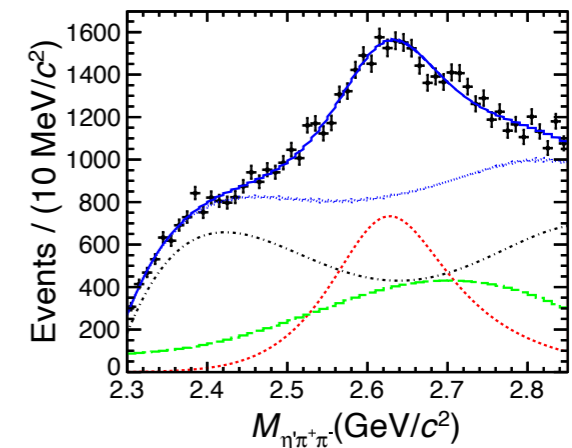
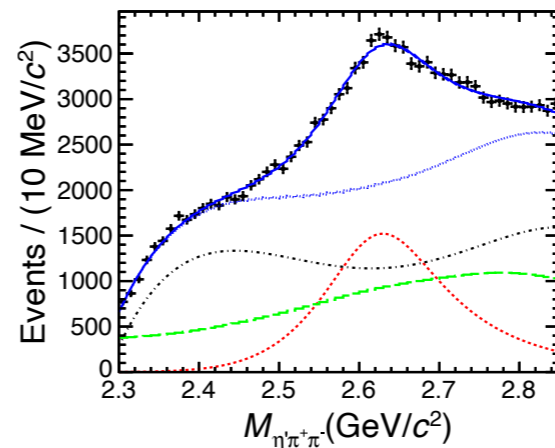
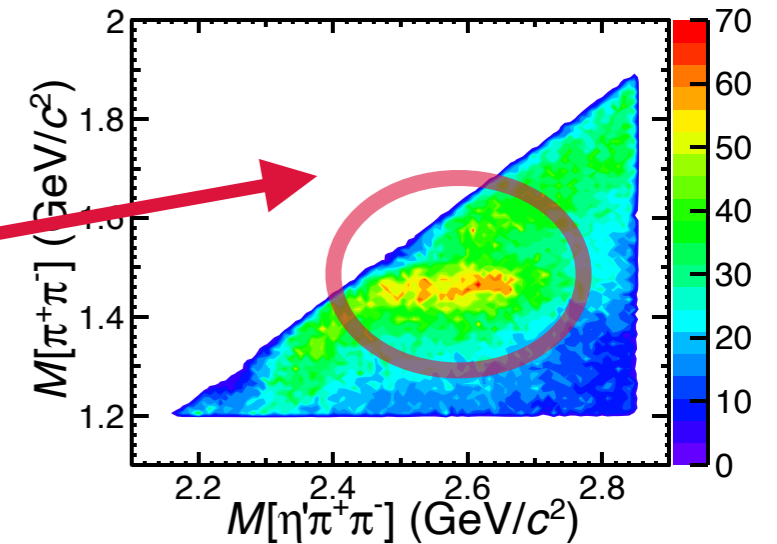
PRL 129, 042001 (2022)

- Interesting structure at 2.6 GeV
- Likely connected to a non trivial structure at $1500 \text{ MeV}/c^2$ in $\pi^+ \pi^-$ system
- Further studies ongoing, full PWA needed...

$$\eta' \rightarrow \gamma \pi^+ \pi^-$$



$$\eta' \rightarrow \eta \pi^+ \pi^-$$



Era of High Statistics

- One is suddenly sensitive to effects one could safely neglect in former times...
- (systematical errors $>$ statistical errors...)
- The model is more important than ever!
- Such computational expensive coupled analyses demand us to get faster!

Development of faster algorithms required:

- Including AI methods where ever helpful

Leads also to:

- More sustainable use of resources and data!

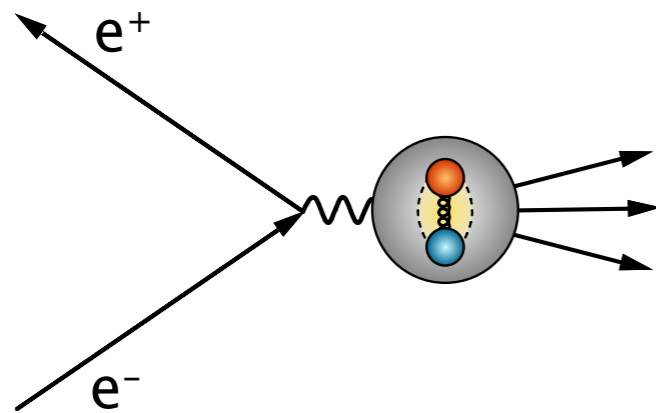
New network project working on techniques to accelerate PWA:

- Automated differentiation
- Improved gradient decent methods
- Pseudo event clustering

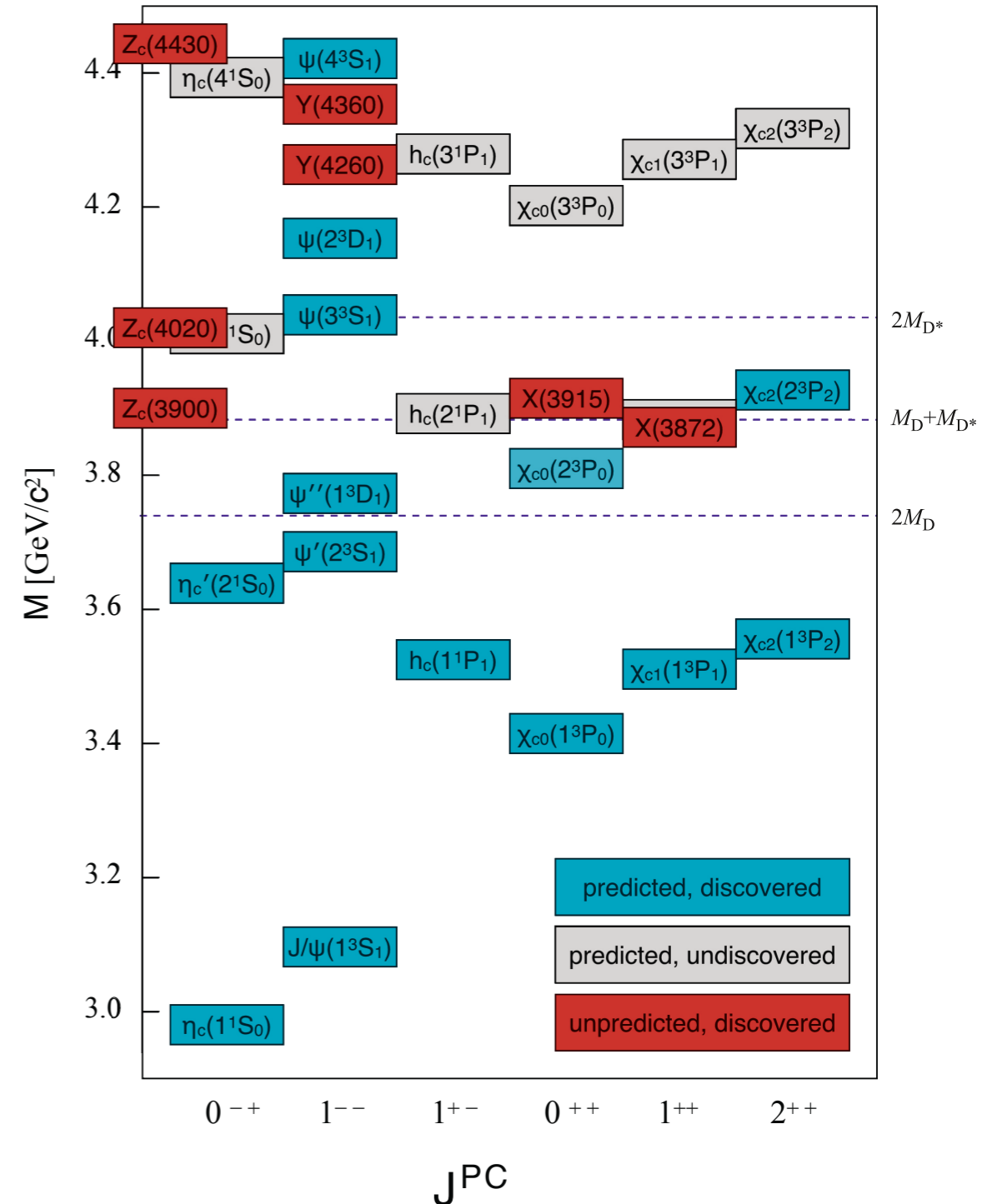


Charmonium Sector

- Charmonia with vector q.n. can be directly created at e^+e^- colliders

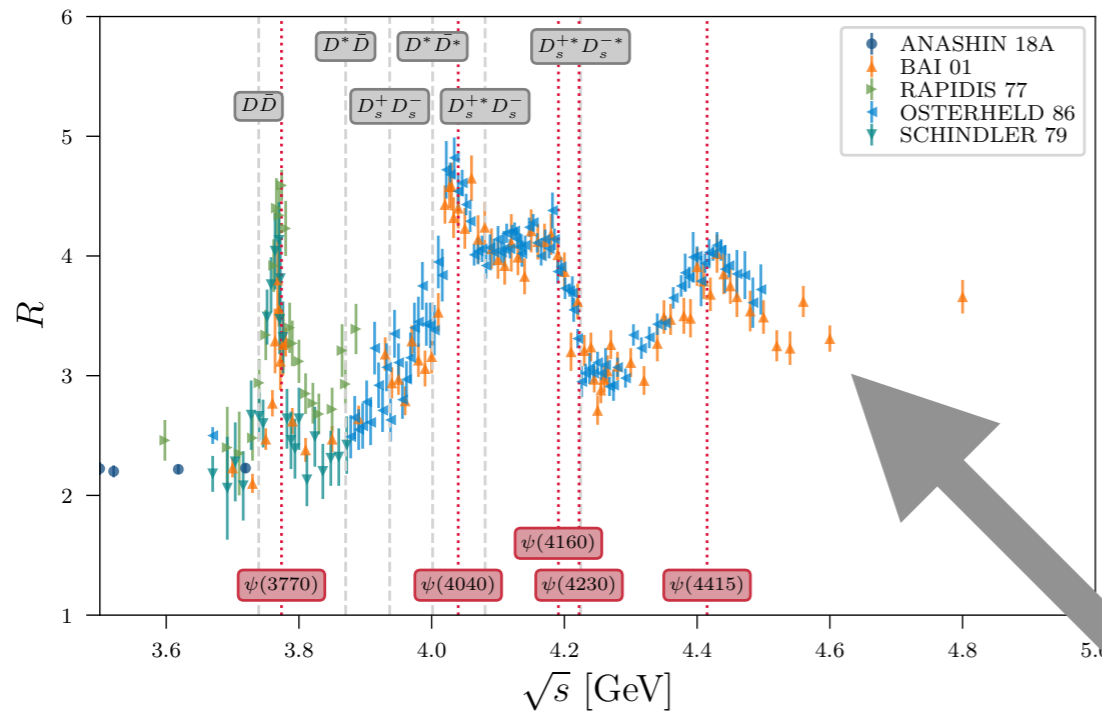


- Other q.n. can only be accessed by sequential decays which limits the statistics

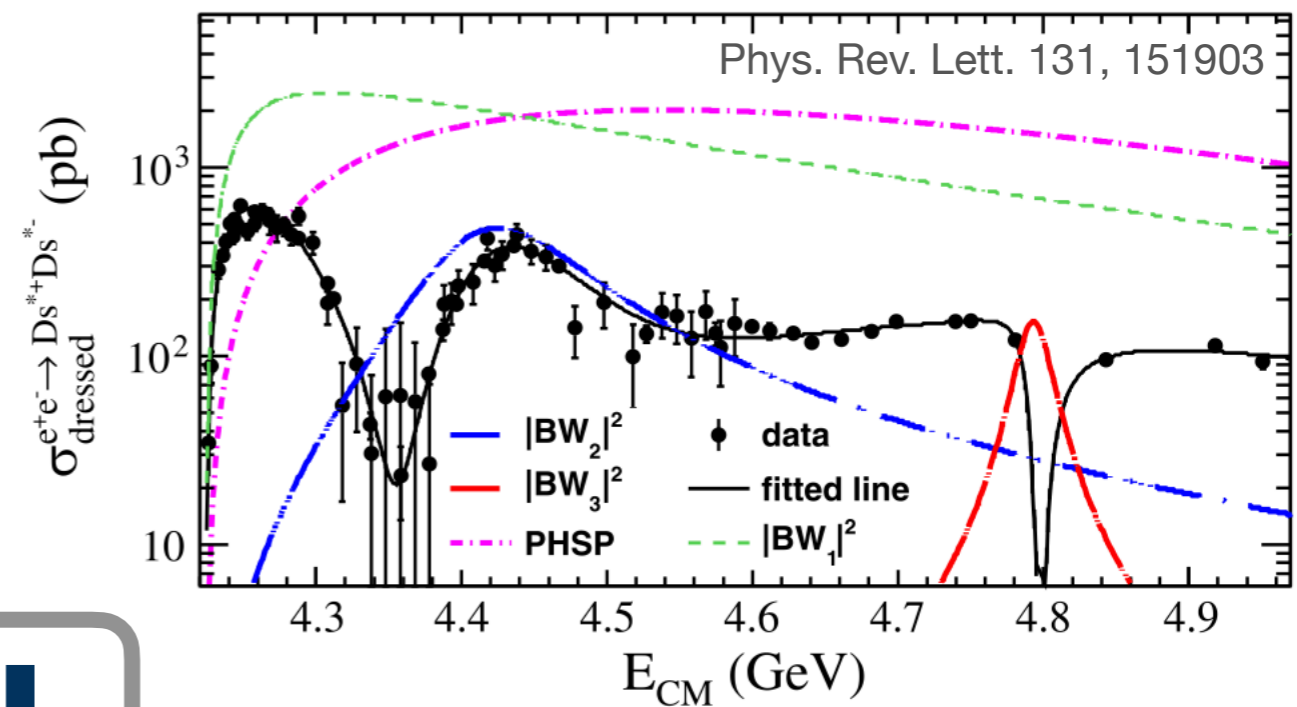


- Besides expected states, additional „unconventional“ states were observed!

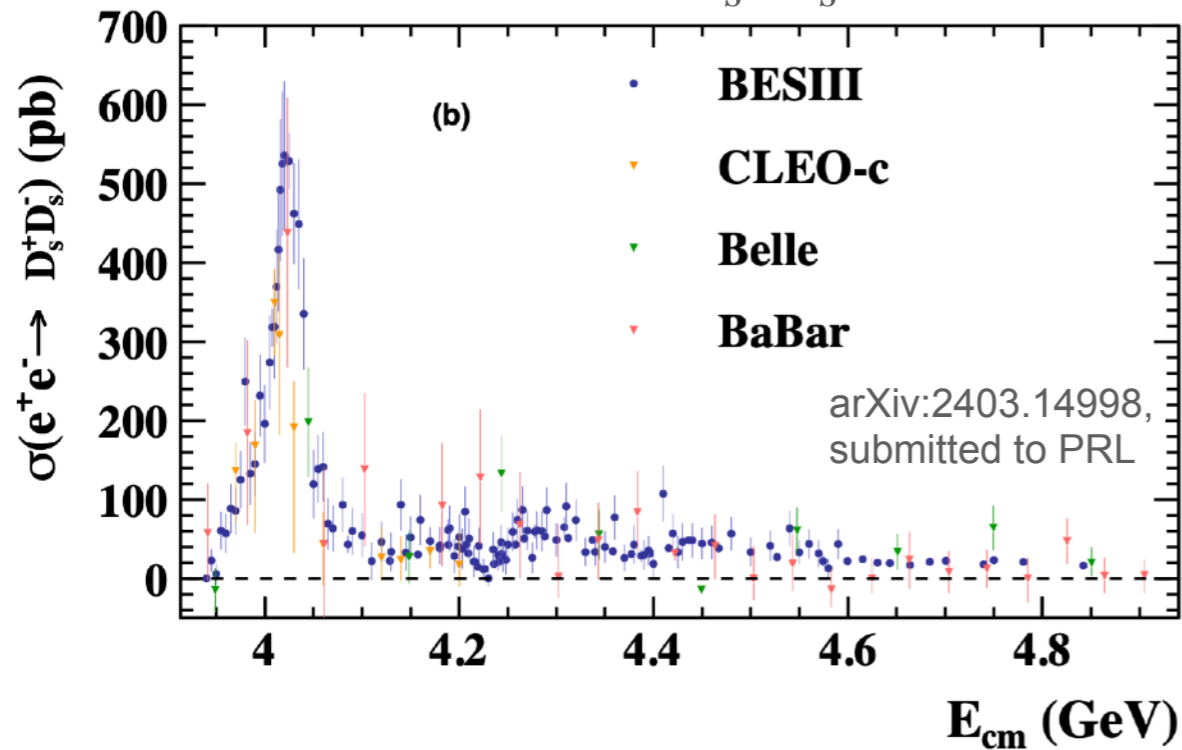
Vector Charmonia



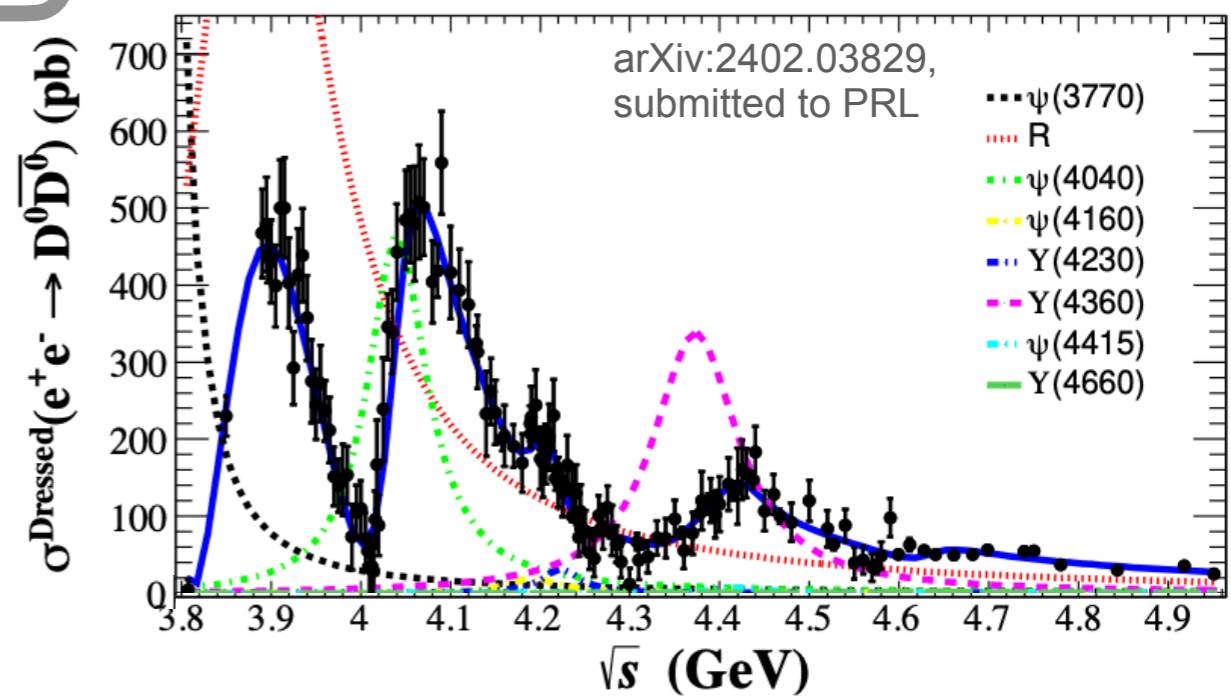
$$e^+e^- \rightarrow D_s^{*+} D_s^{*-}$$



$$e^+e^- \rightarrow D_s^+ D_s^-$$



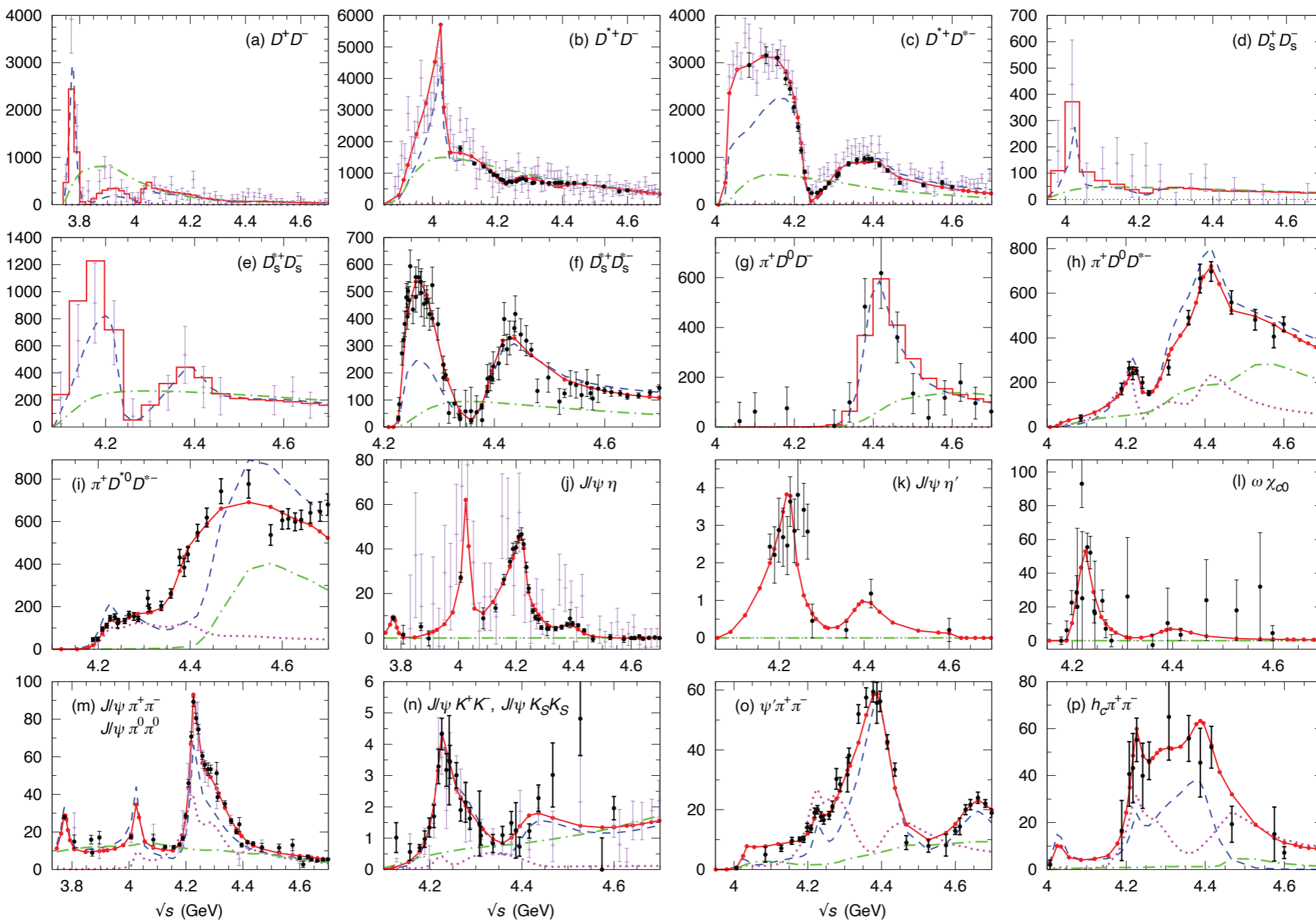
$$e^+e^- \rightarrow D^0 \bar{D}^0$$



A first Step Towards a Global Description

- Combined fit to 19 BESIII and Belle cross section results

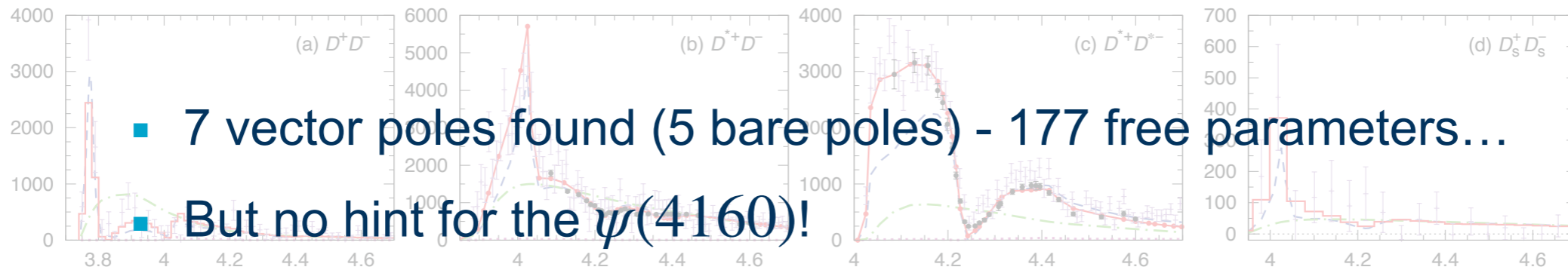
arXiv:2312.17658



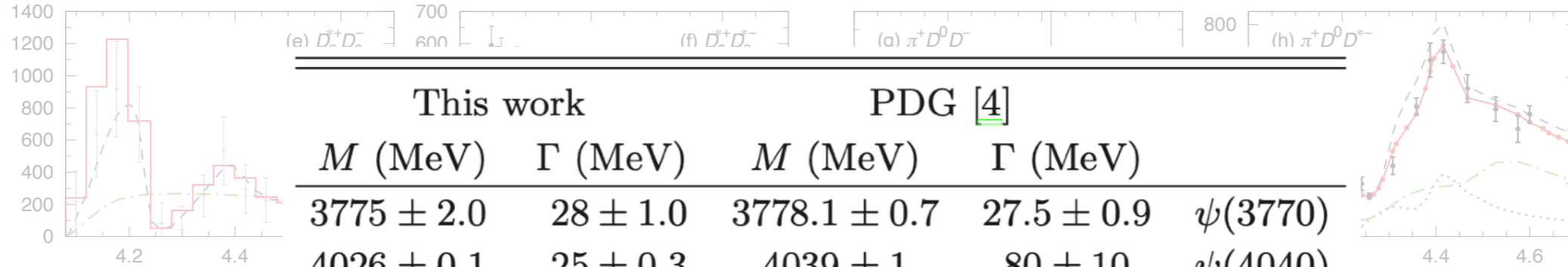
A first Step Towards a Global Description

arXiv:2312.17658

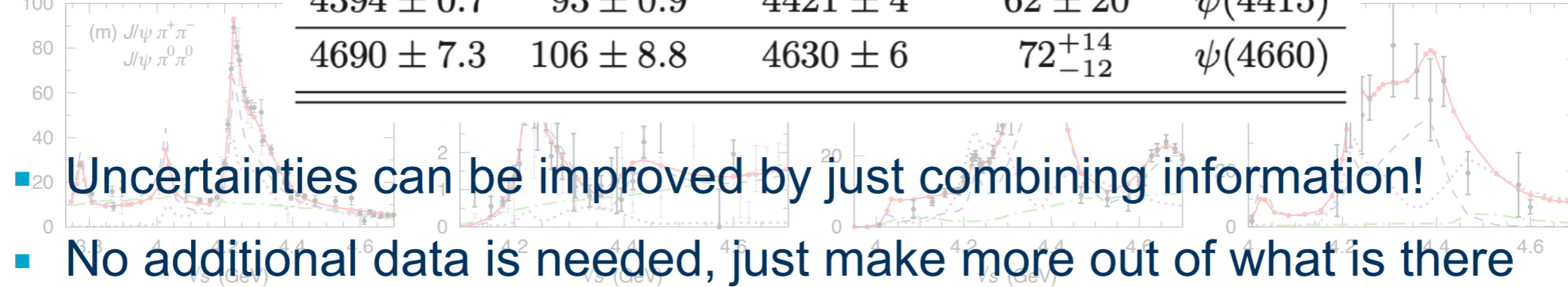
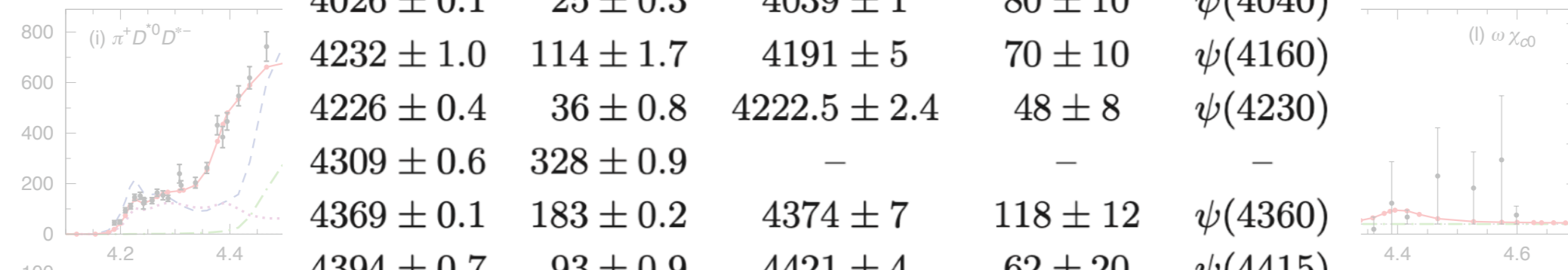
- Combined fit to 19 BESIII and Belle cross section results



- 7 vector poles found (5 bare poles) - 177 free parameters...
- But no hint for the $\psi(4160)$!



This work		PDG [4]		
M (MeV)	Γ (MeV)	M (MeV)	Γ (MeV)	
3775 ± 2.0	28 ± 1.0	3778.1 ± 0.7	27.5 ± 0.9	$\psi(3770)$
4026 ± 0.1	25 ± 0.3	4039 ± 1	80 ± 10	$\psi(4040)$
4232 ± 1.0	114 ± 1.7	4191 ± 5	70 ± 10	$\psi(4160)$
4226 ± 0.4	36 ± 0.8	4222.5 ± 2.4	48 ± 8	$\psi(4230)$
4309 ± 0.6	328 ± 0.9	—	—	—
4369 ± 0.1	183 ± 0.2	4374 ± 7	118 ± 12	$\psi(4360)$
4394 ± 0.7	93 ± 0.9	4421 ± 4	62 ± 20	$\psi(4415)$
4690 ± 7.3	106 ± 8.8	4630 ± 6	72^{+14}_{-12}	$\psi(4660)$

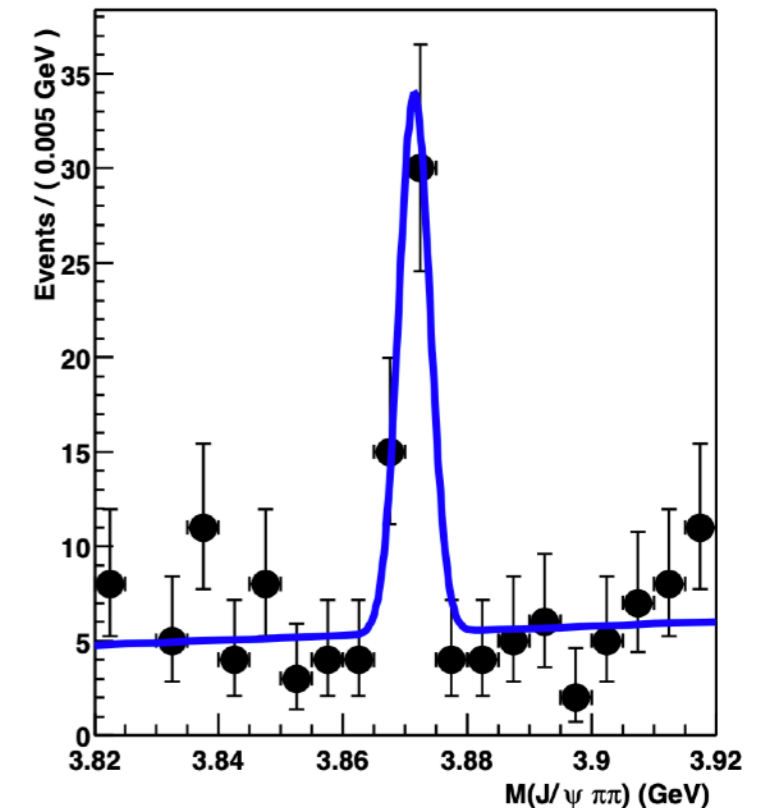


- Uncertainties can be improved by just combining information!
- No additional data is needed, just make more out of what is there

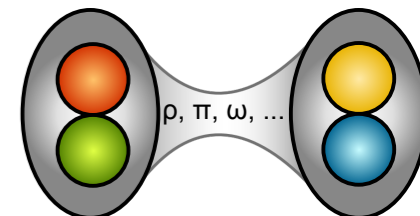
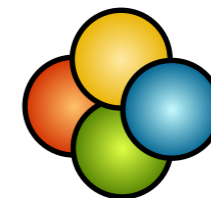
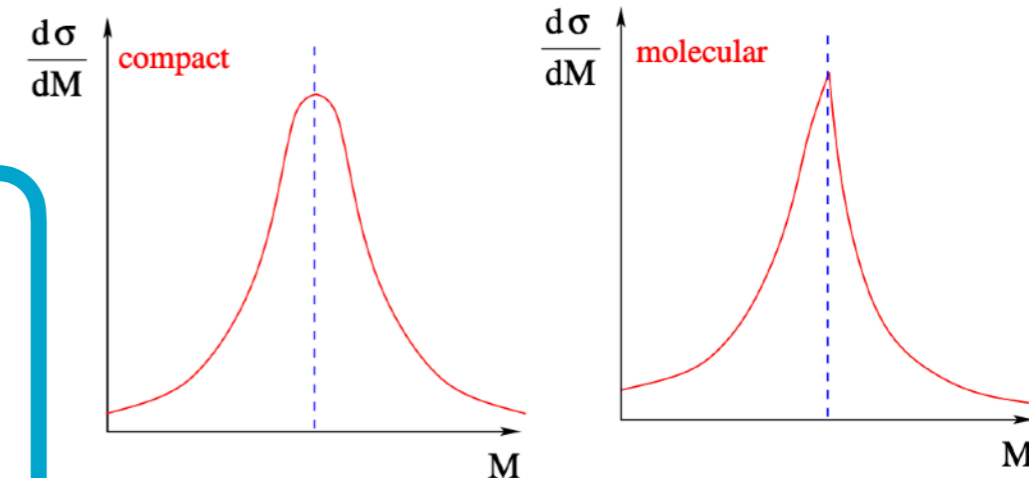
The Story of $\chi_{c1}(3872)/X(3872)$

- First observed by Belle in 2003 in $X(3872) \rightarrow \pi^+ \pi^- J/\psi$
- Very narrow 1^{++} state, sitting just at the $D^0 \bar{D}^{*0}$ threshold
- Well established production channel: $\psi(4230) \rightarrow \gamma \chi_{c1}(3872)$
 - ➔ Precision studies possible!
- Seen in various production channels by now: B/Λ_b decays, pp , Pb Pb, e^+e^-
- ... and in various decay modes: $J/\psi(\pi^+ \pi^-)\rho$, $D^0 \bar{D}^{*0}$, $J/\psi \gamma$, $\psi(2S)\gamma$, $\chi_{c1}\pi^0$, ...
- Isospin violating decay is enhanced by a factor of 5 compared to „ordinary“ charmonia

PRL 91, 262001 (2003)

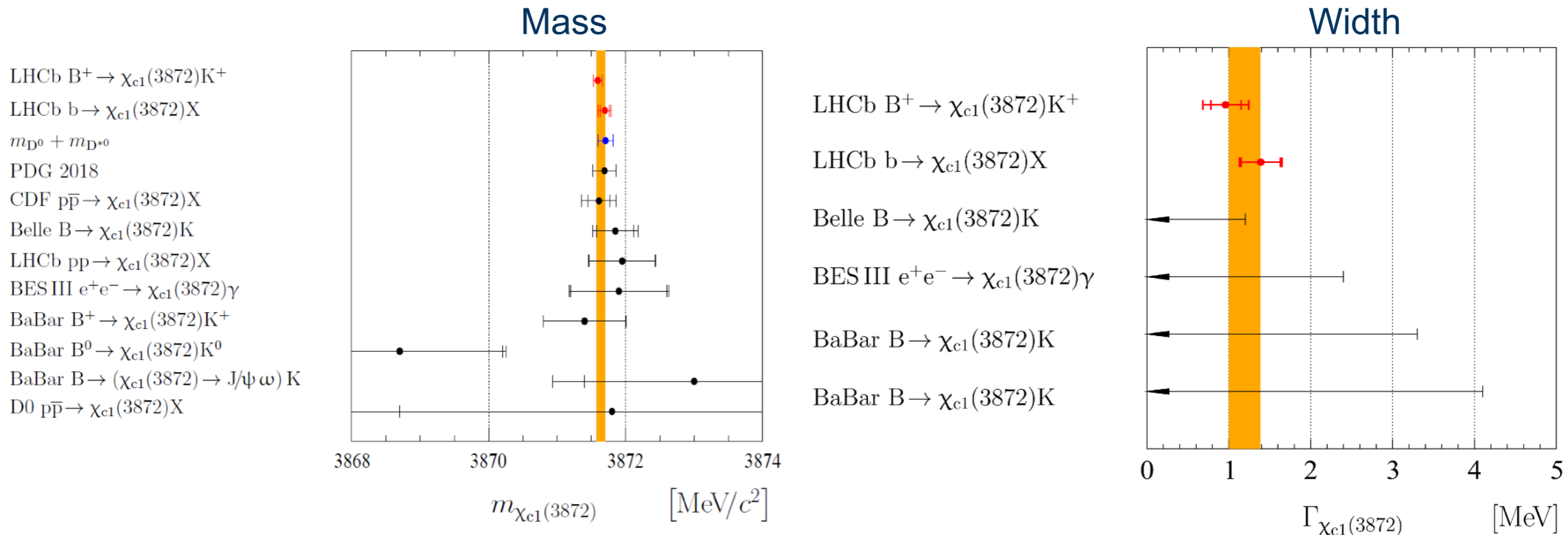


- Similar structures seen in $D^0 D^0 \pi^+ : T_{cc}(3875)$
- How are they related? Is it the same underlying physics?
- Can we describe both with one model?



The Story of $\chi_{c1}(3872)$

- Precision has increased a lot
- First width and QN measurement by LHCb
- But: still the state is compatible with the $D^0\bar{D}^{*0}$ threshold!

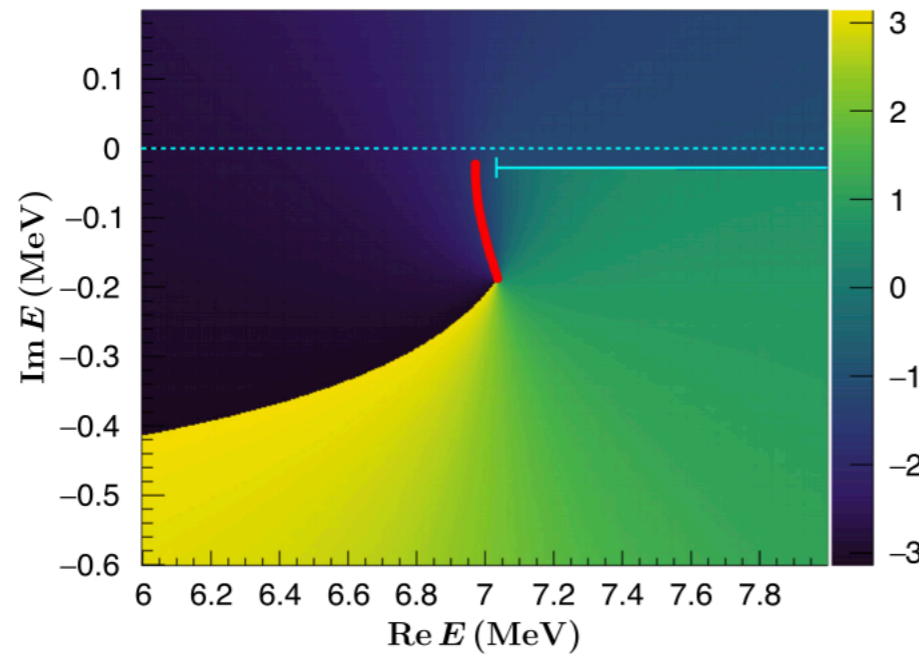
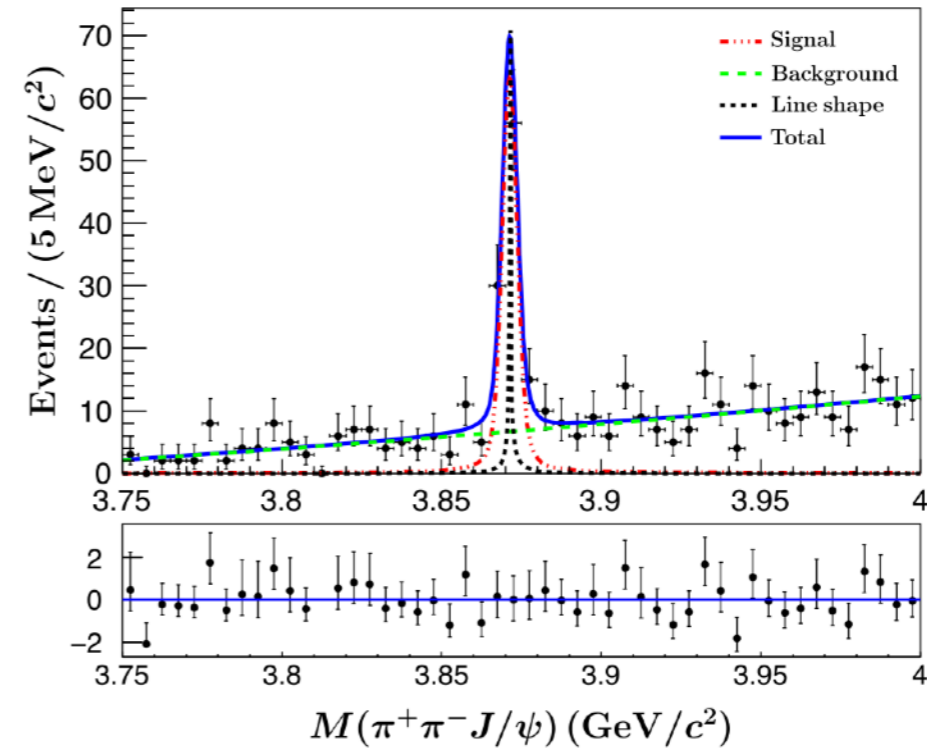
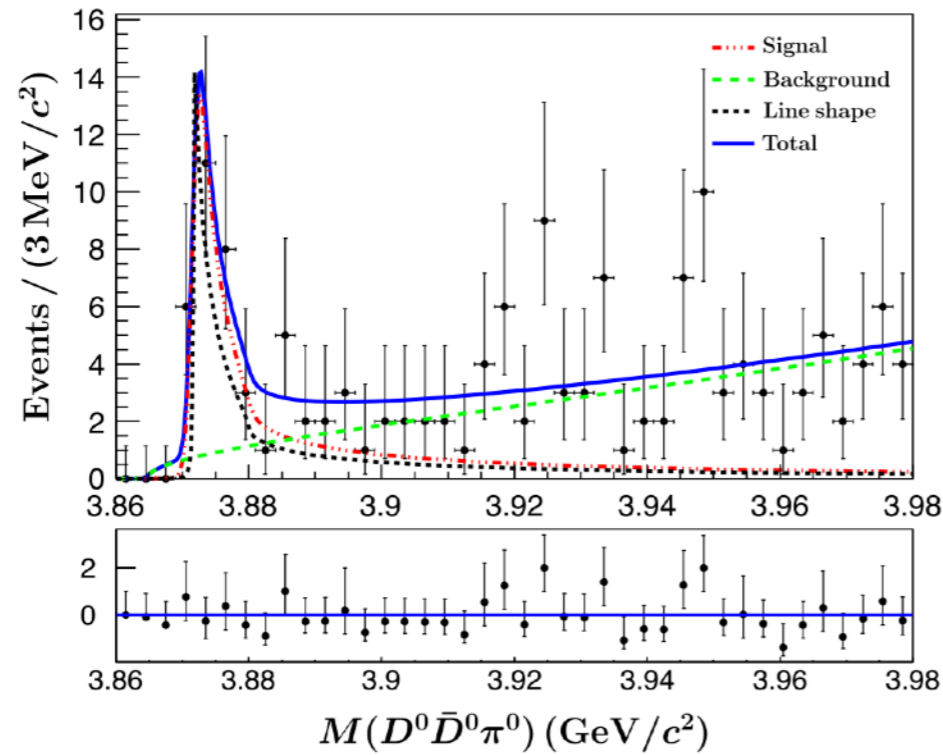


- Sensitivity to the underlying lineshape is washed out by the detector resolution
- If we want to clarify this we need \ll MeV resolution! No detector can do this.

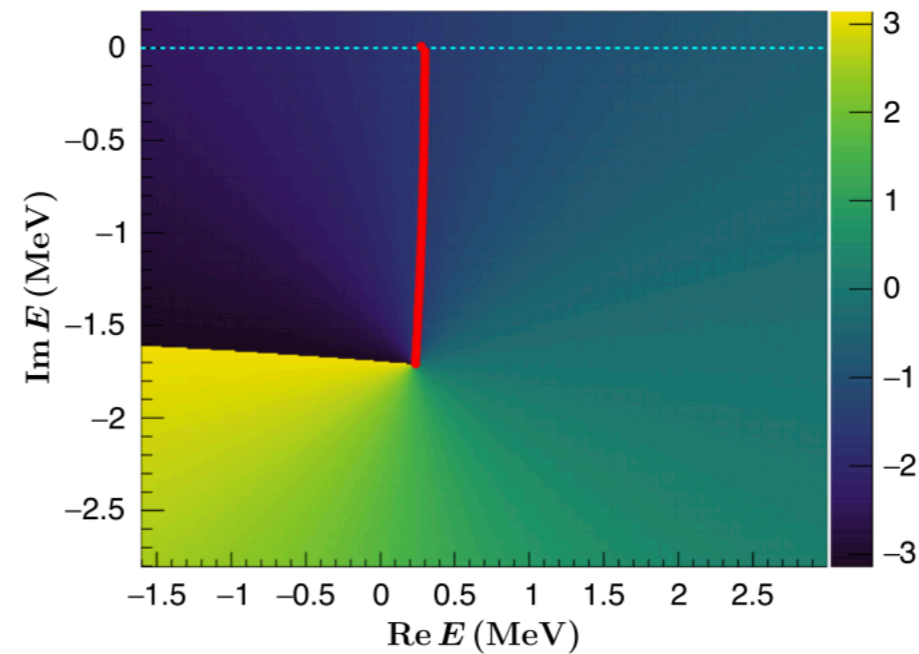
Coupled Channel Fit to $\chi_{c1}(3872)$

PRL 132 (2024) 15, 151903

- Simultaneous fit to $D^0\bar{D}^0\pi^0$ and $\pi^+\pi^-J/\psi$



(a) Sheet I: $E_I = 7.04 - 0.19i$ MeV

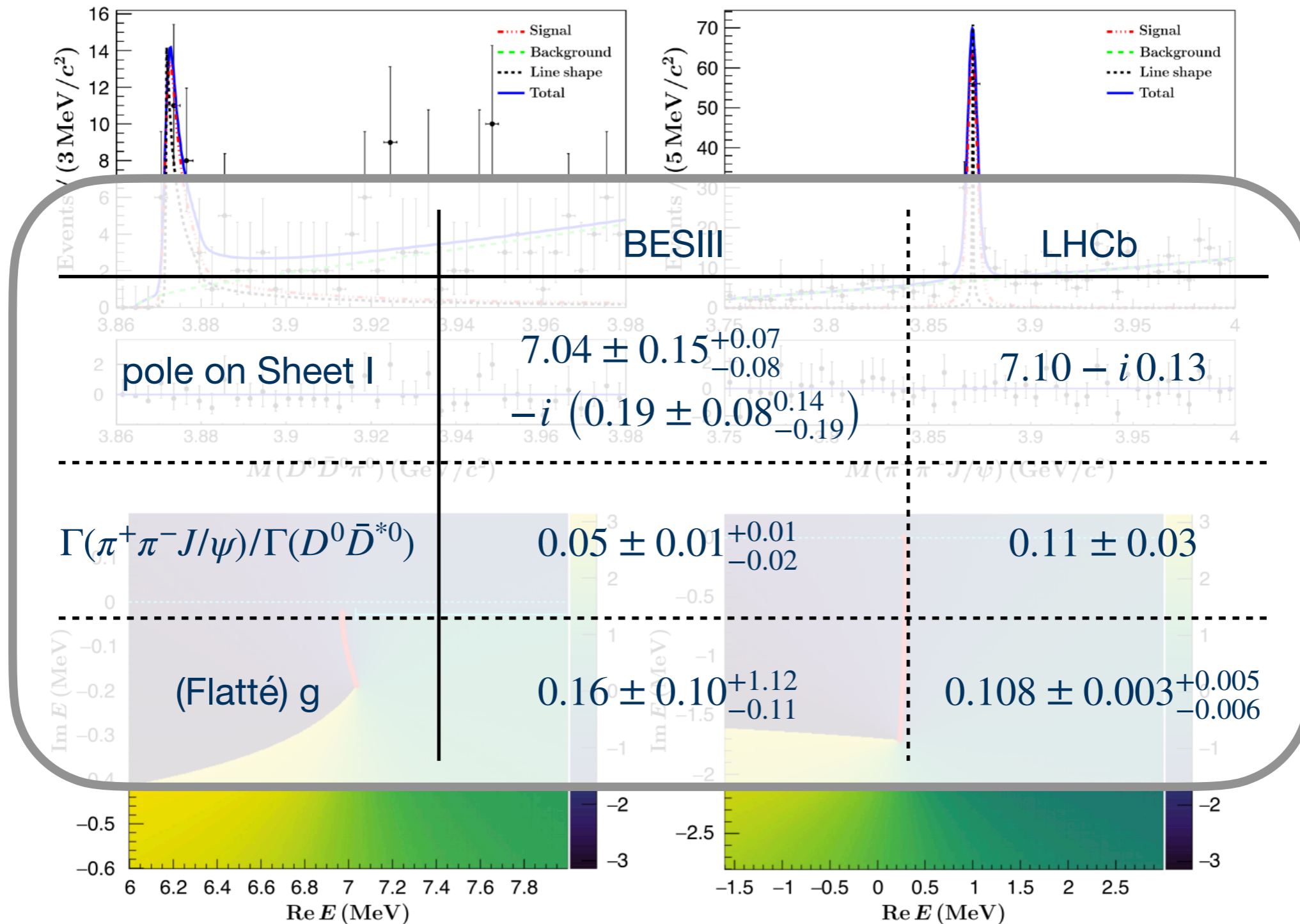


(b) Sheet II: $E_{II} = 0.26 - 1.71i$ MeV

Coupled Channel Fit to $\chi_{c1}(3872)$

PRL 132 (2024) 15, 151903

- Simultaneous fit to $D^0\bar{D}^0\pi^0$ and $\pi^+\pi^-J/\psi$

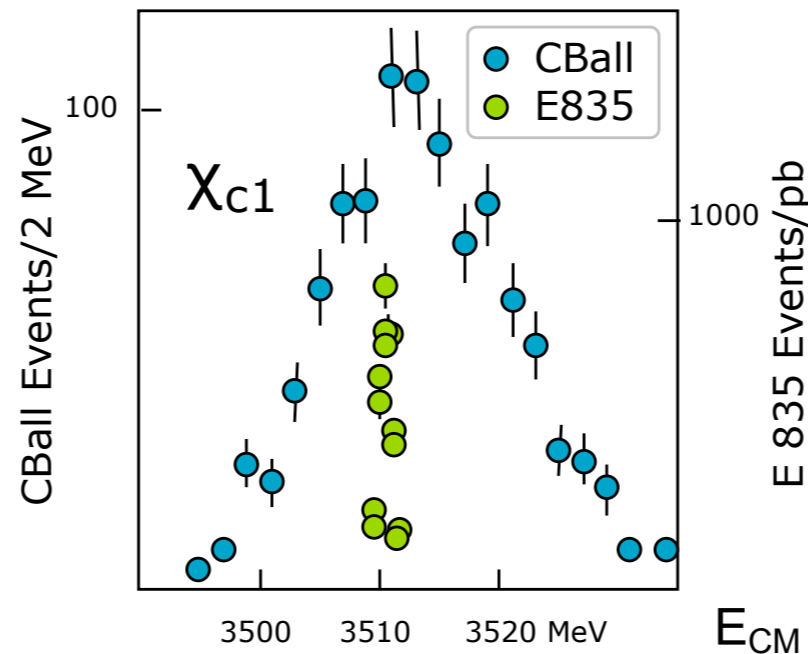
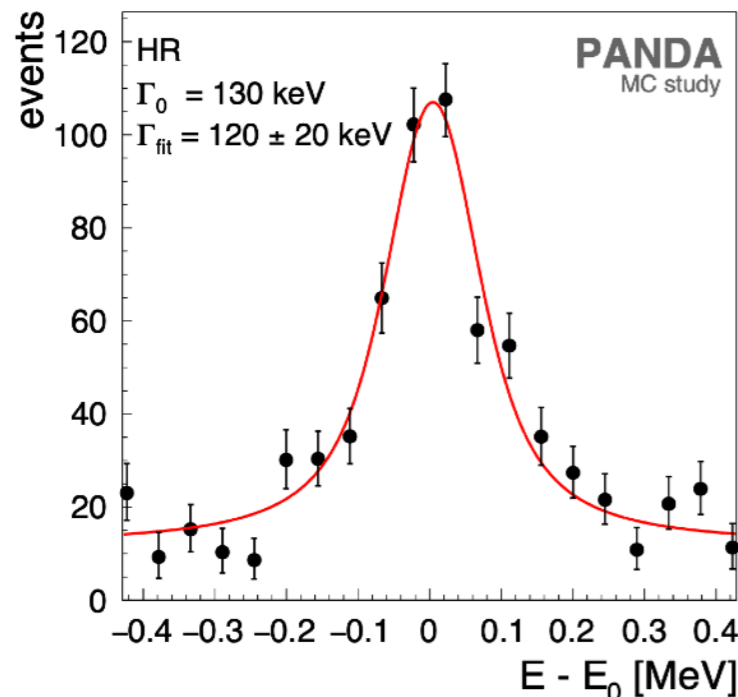
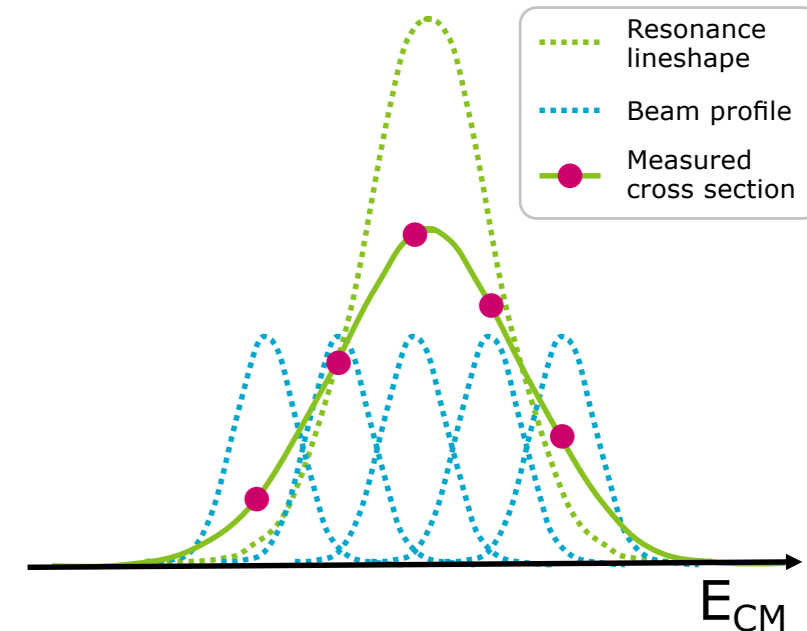


(a) Sheet I: $E_I = 7.04 - 0.19i$ MeV

(b) Sheet II: $E_{II} = 0.26 - 1.71i$ MeV

Line Shape Scans at \bar{P} ANDA

- Measure the lineshape with high precision by scanning the resonance in production
- Line shape resolution is only limited by the beam resolution, not the detector resolution here!**
- Analysis performed for 20 energy points around nominal mass
- In sensitivity studies able to distinguish the two scenarios
- ➔ With the \bar{P} ANDA setup this corresponds to only about a month of data taking!
- ➔ In $\bar{p}p$ annihilation almost all Q.N. can be produced directly!

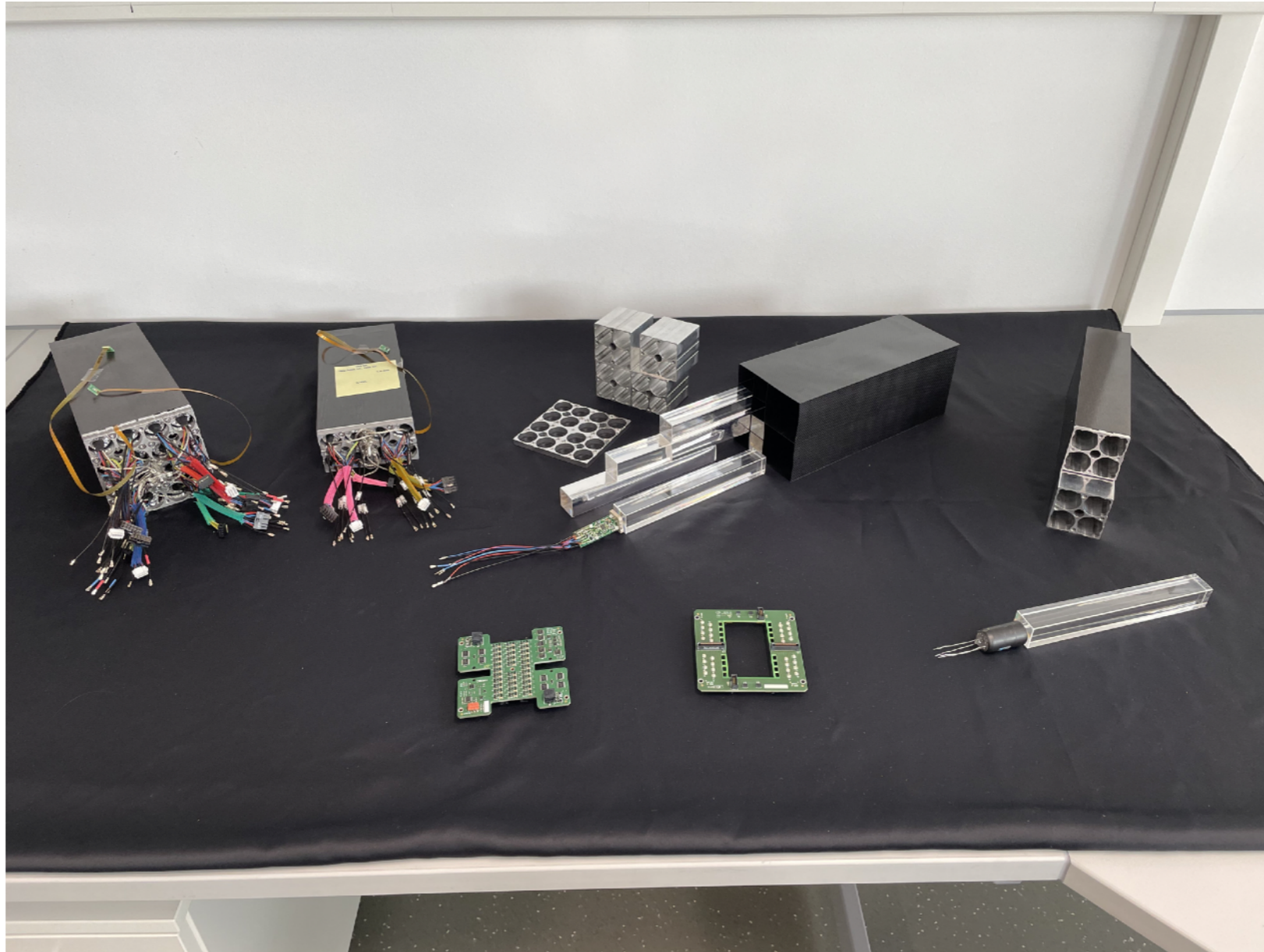


\bar{P} ANDA will be able to study all this!

Design beam resolution:

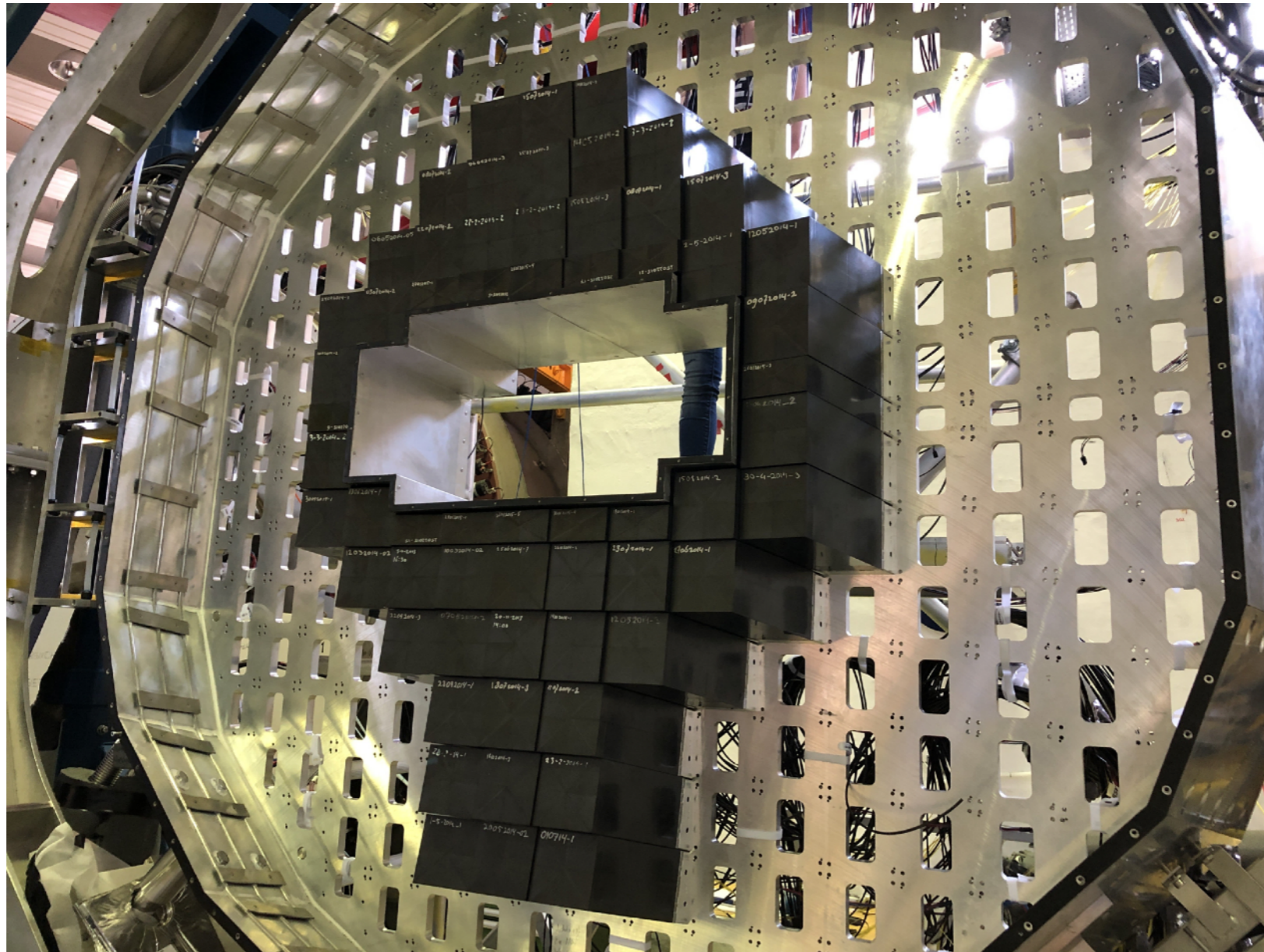
$\Delta p/p = 4 \cdot 10^{-5}$

PANDA Forward Endcap EMC Beam Test



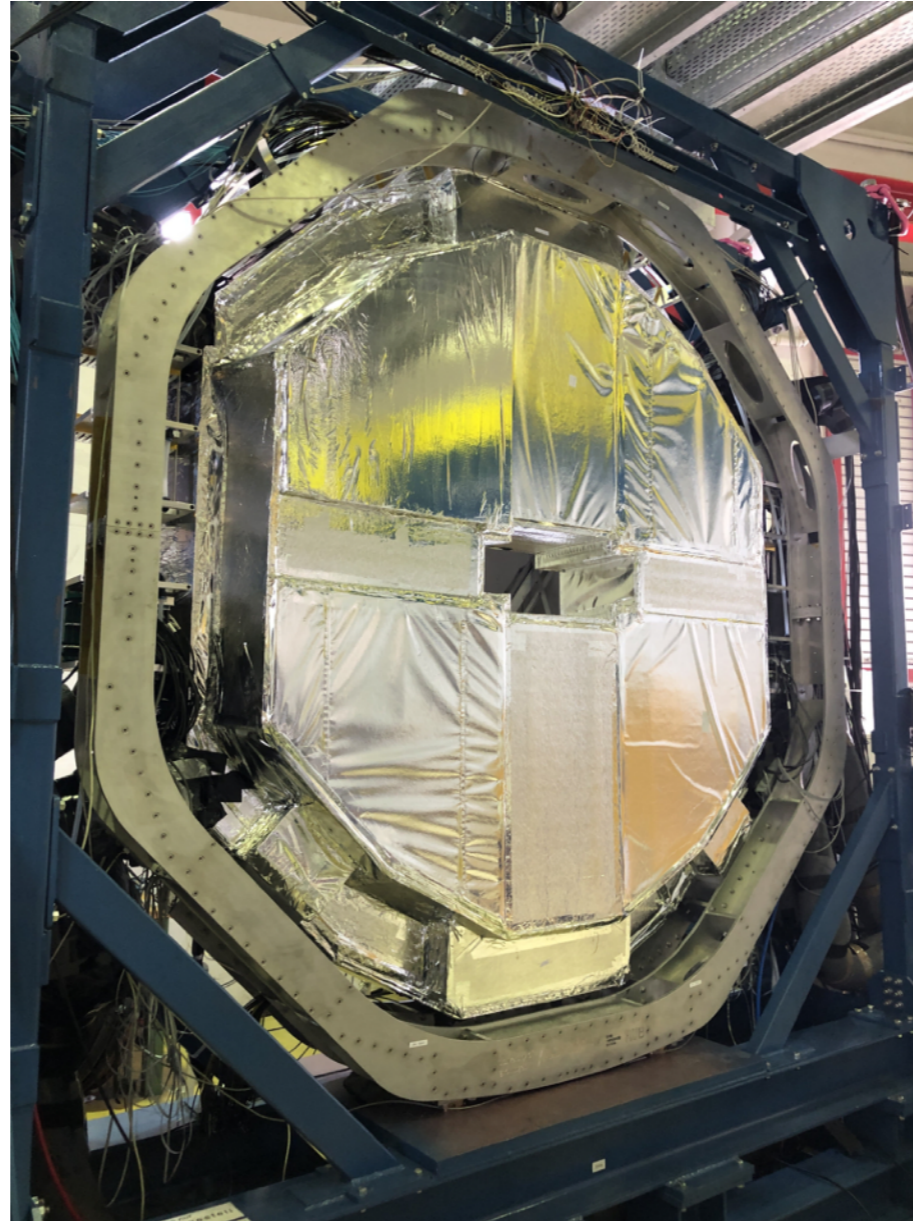
- Consisting of 15604 PbWO₄ crystals
- Operated at $-25 \pm 0.1^\circ\text{C}$ for best energy resolution
- Just recently successful test beam operation at COSY@FZJ with final detector design!
- Preliminary results show leading edge performance

PANDA Forward Endcap EMC Beam Test



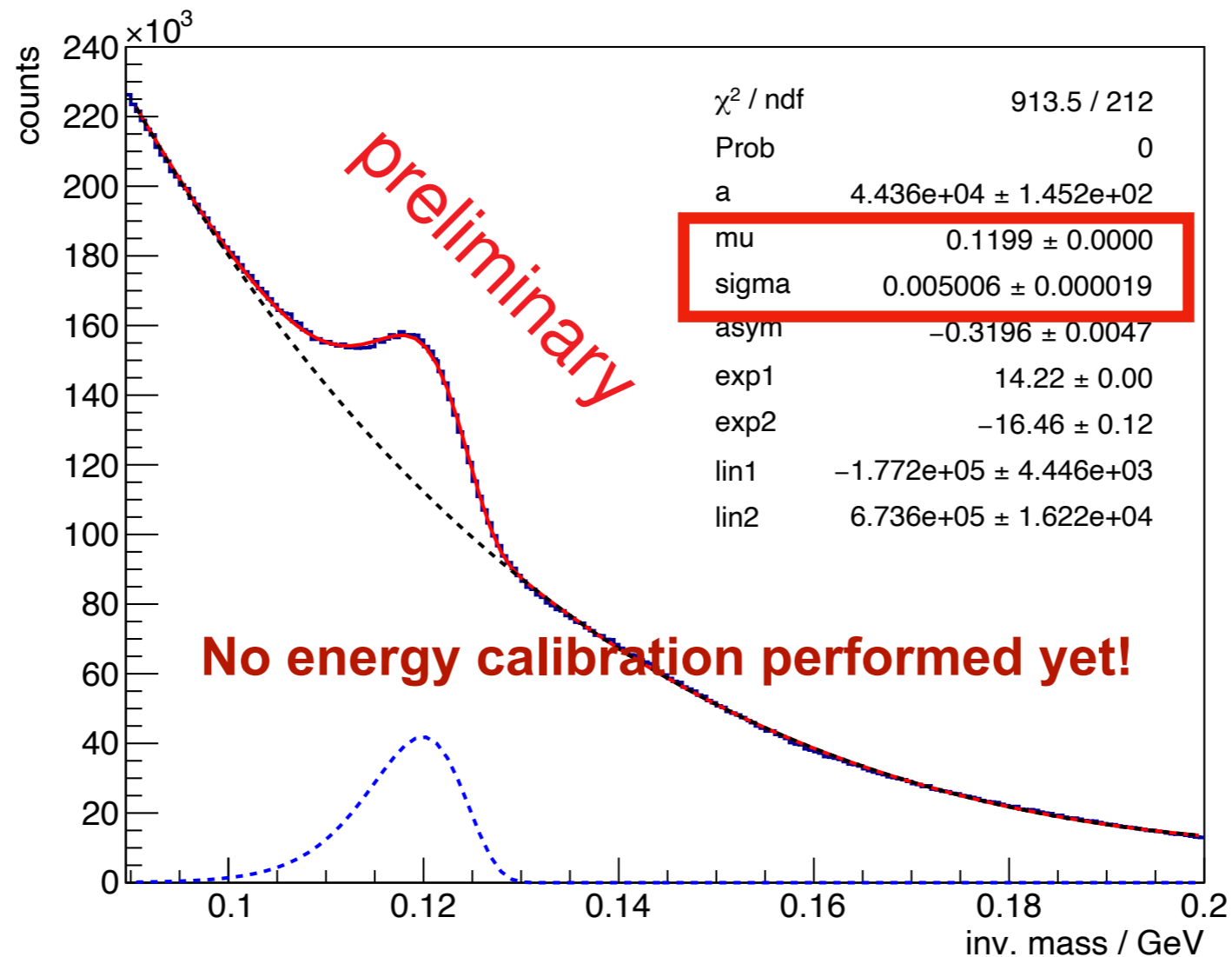
- Consisting of 15604 PbWO_4 crystals
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Summary

- Although light mesons are studied for decades, there are still many open questions
- This affects also other sectors as CP violation!
- Different experiments and theory need to collaborate to solve this
- Coupled channel analyses seem to be a good tool to disentangle crowded spectra
- ...and to even increase precision without additional data!
- Work closer together in the community - common effort is needed to answer fundamental questions
- And to prepare our toolsets in times of high statistic data awaiting us
- This strengthens the research field, especially in times when basic research is experiencing more headwinds



Thank You!