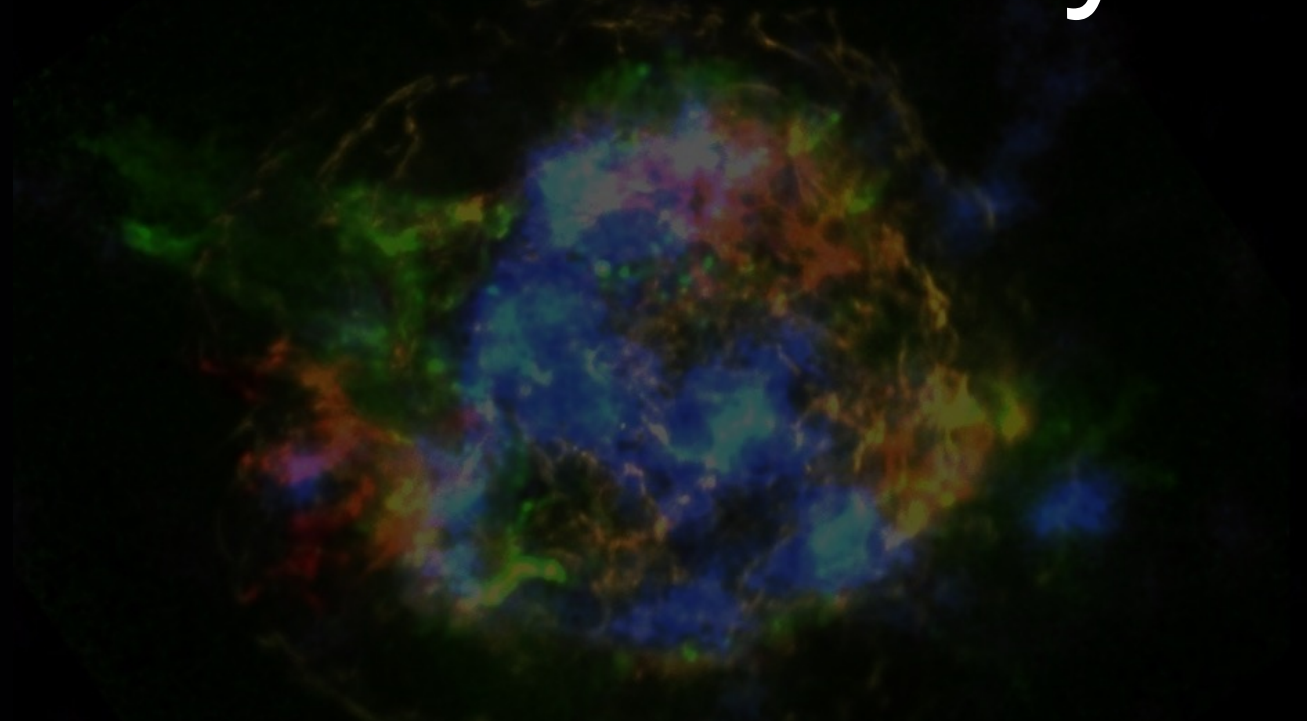


Supernova Nucleosynthesis



Carla Fröhlich

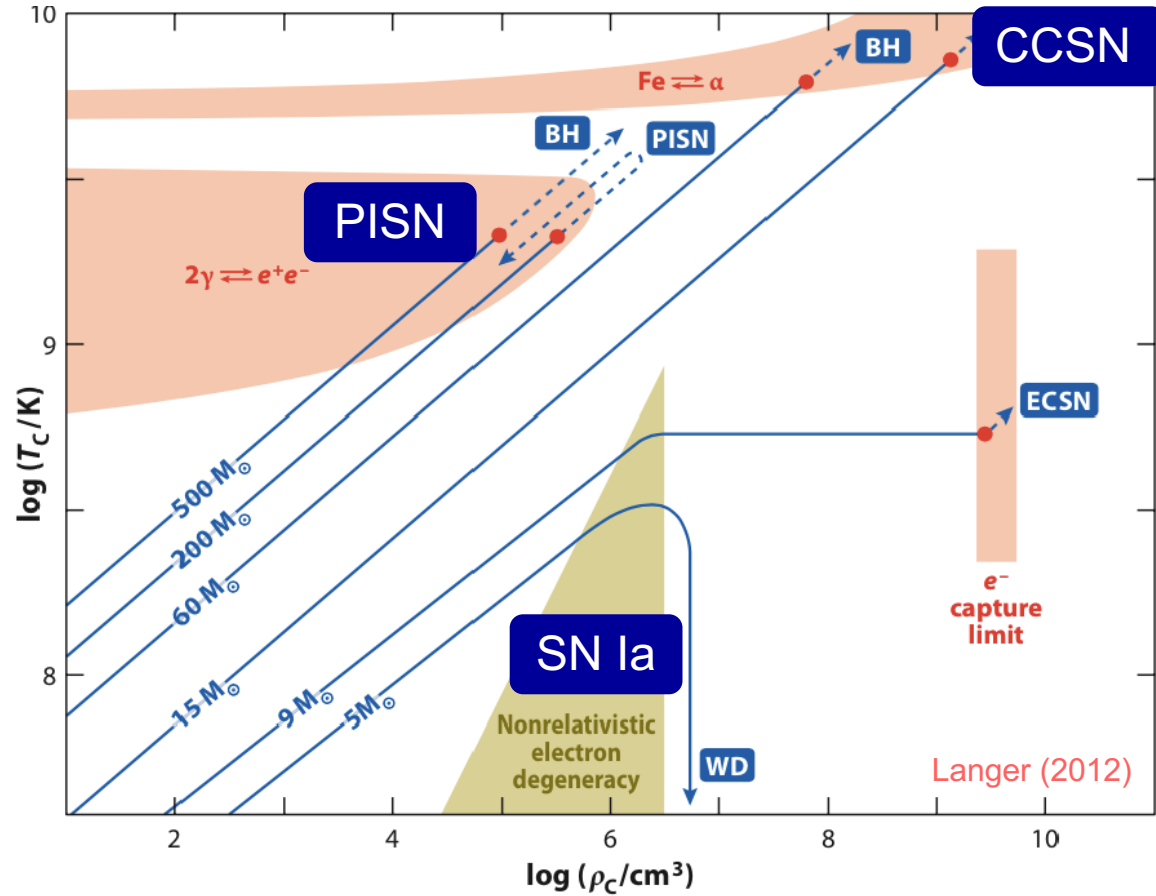
North Carolina State University



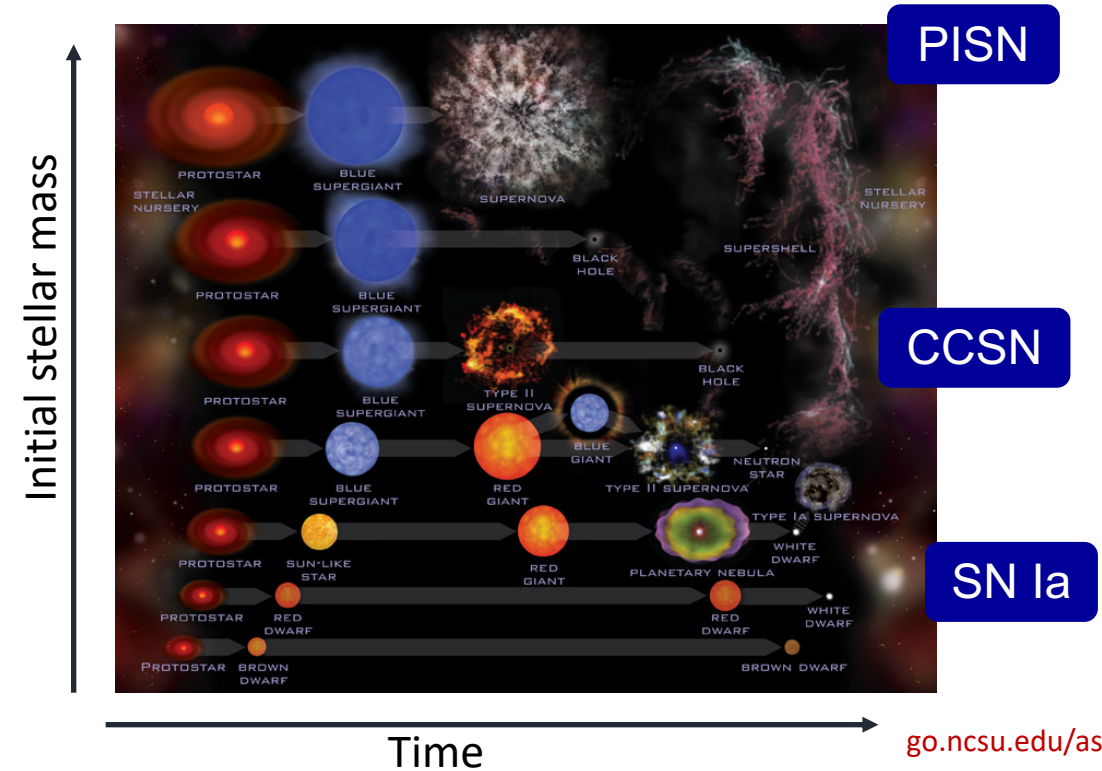
- Study of Physics and Computer science
 - University of Basel, Switzerland
 - 2 semesters at Simon Fraser University, Vancouver, Canada
- PhD in theoretical physics (Advisor: Friedel Thielemann)
 - University of Basel, Switzerland
- Enrico Fermi Postdoctoral Fellow
 - University of Chicago, USA
- Since 2010: Professor
 - North Carolina State University, USA

"I'll go to the US for 3 years"

Supernovae

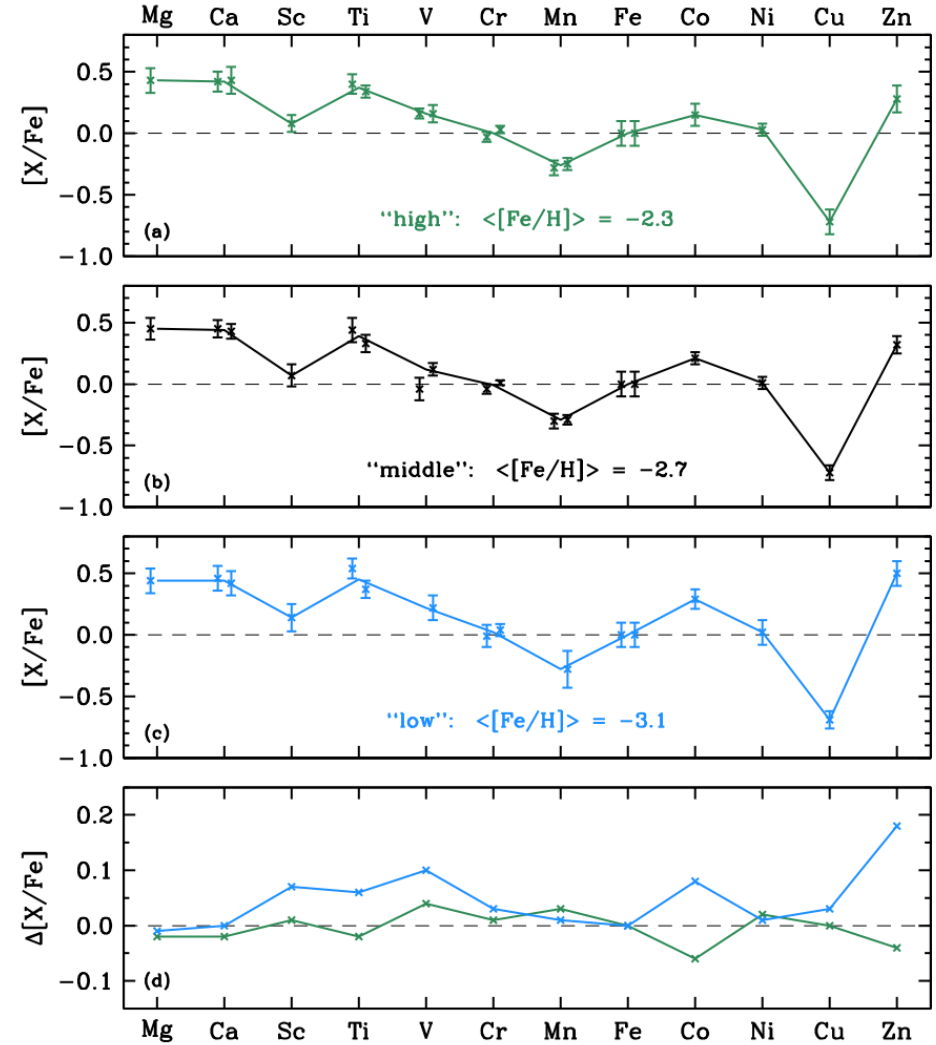
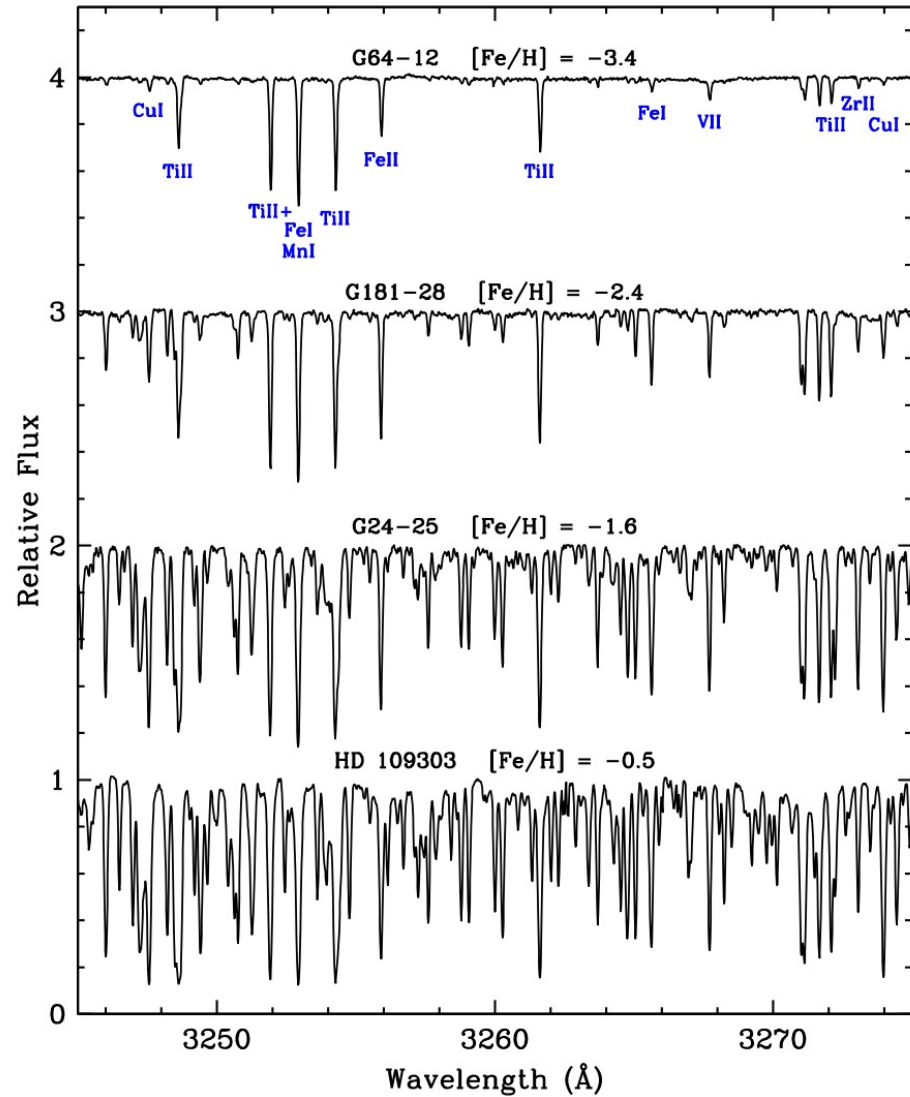


Supernovae happen when stellar evolution reaches a region of instability



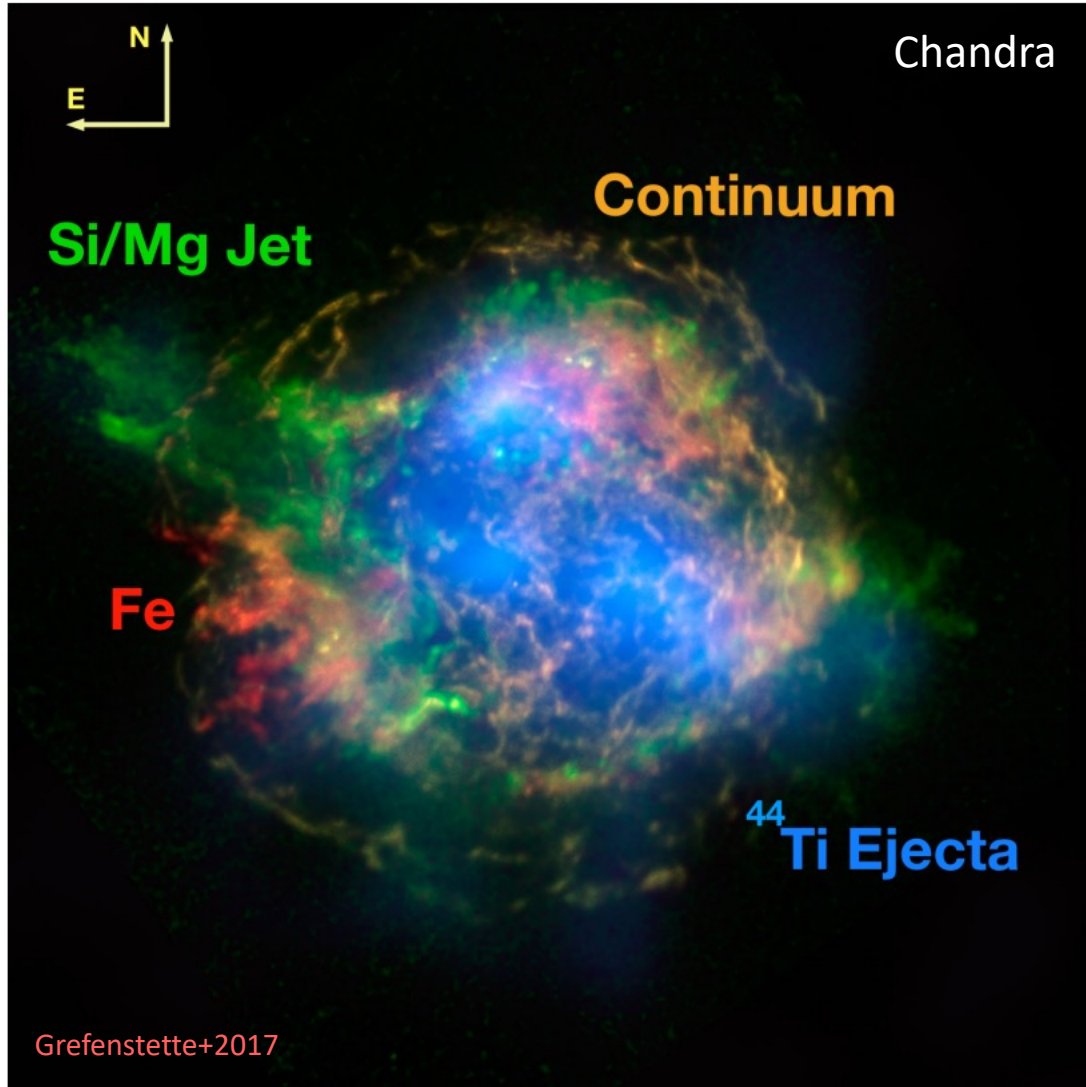
Where do we see the nucleosynthetic imprints of CCSNe?

Old Metal Poor Stars

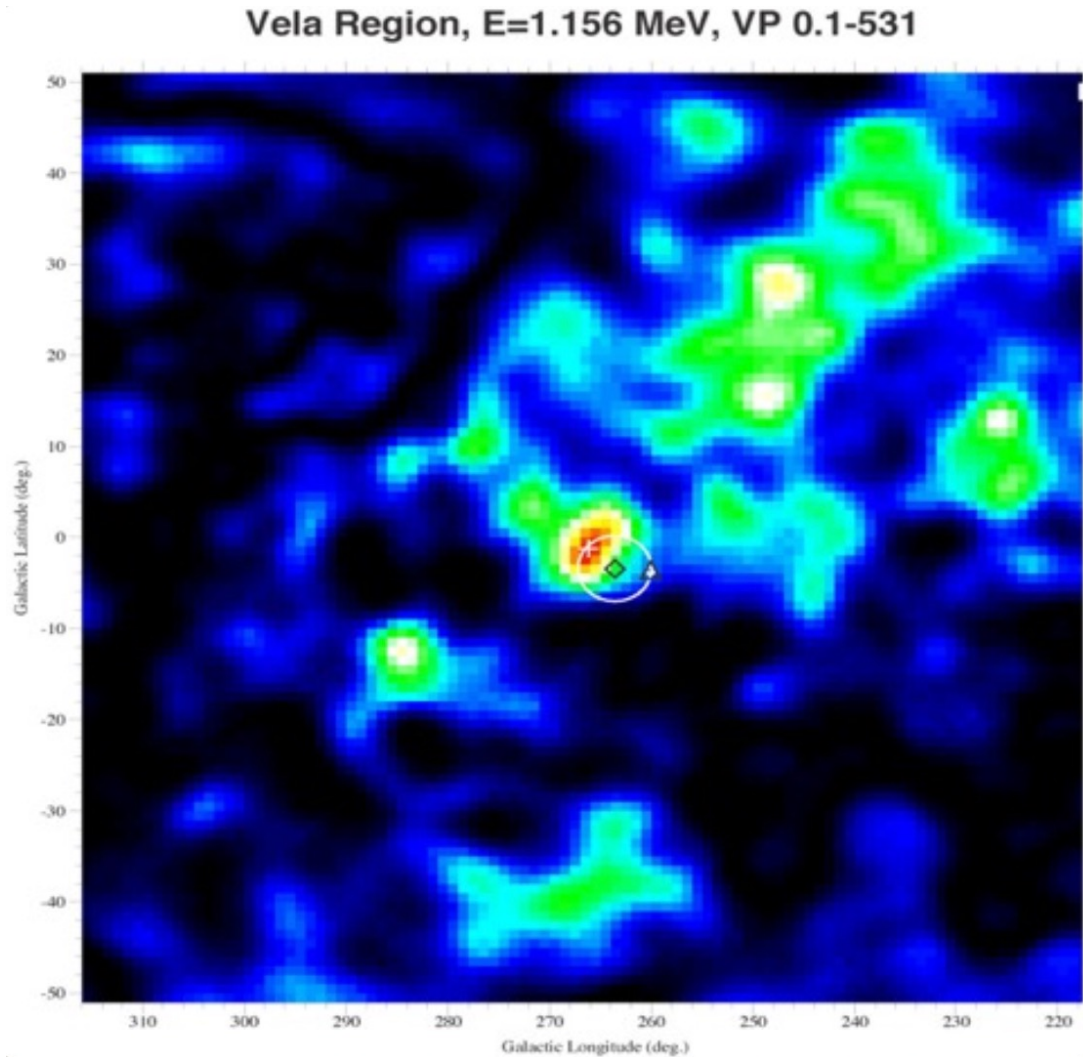


Snedden+2023

Supernova Remnants



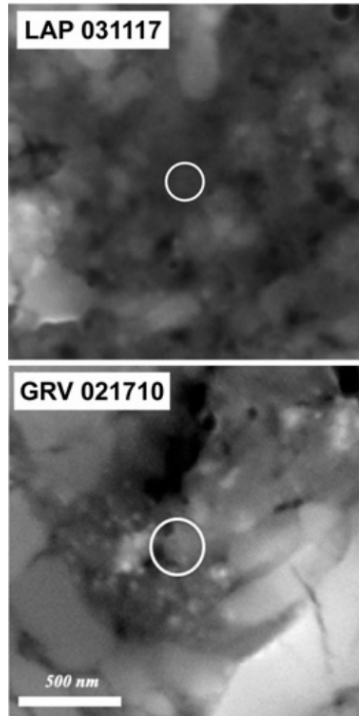
In gamma-rays (signatures of freshly made nuclei)



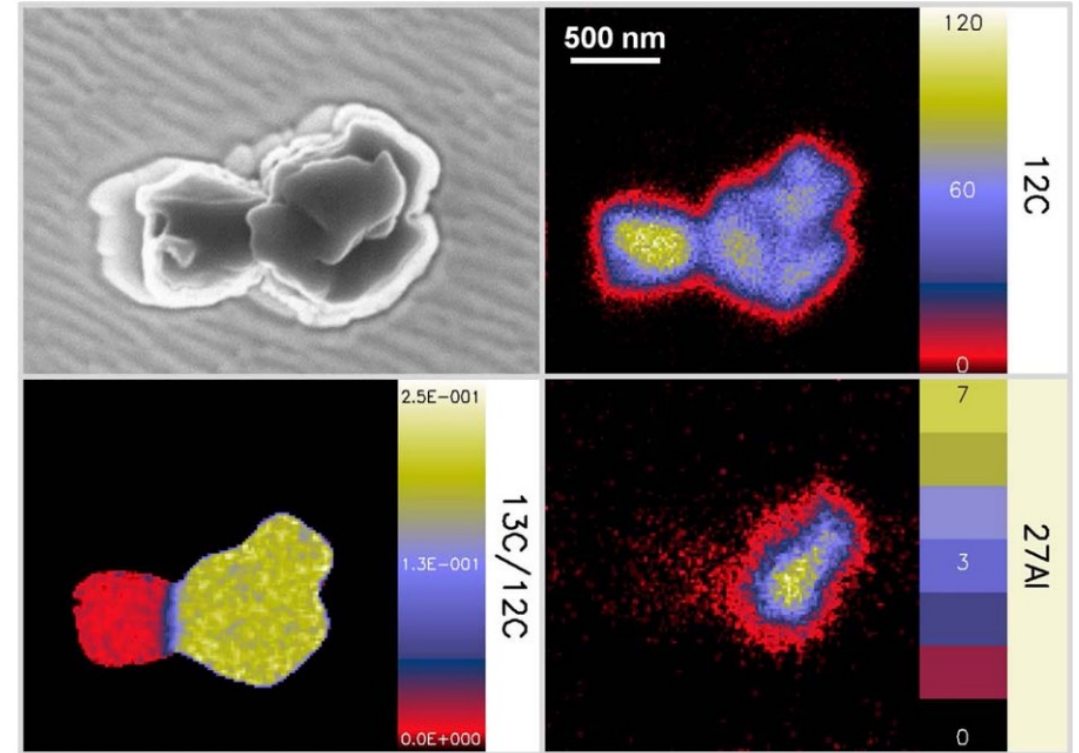
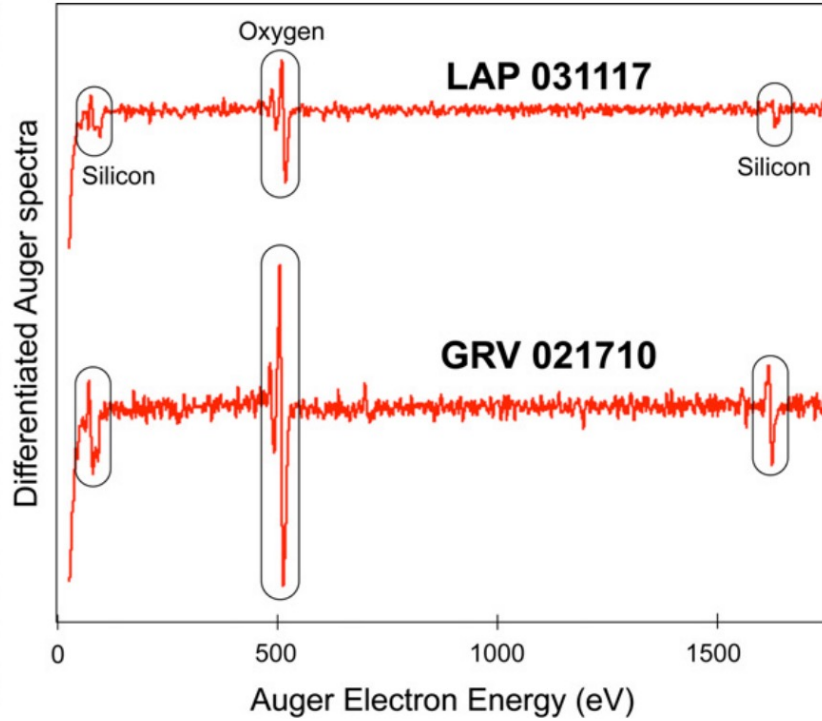
Characteristic gamma-lines:

- ^{56}Ni ($t_{1/2} = 6$ days)
- ^{57}Ni ($t_{1/2} = 36$ hrs)
- ^{56}Co ($t_{1/2} = 77$ days)
- ^{57}Co ($t_{1/2} = 272$ days)
- ^{44}Ti ($t_{1/2} = 60$ yrs)

Pre-solar grains

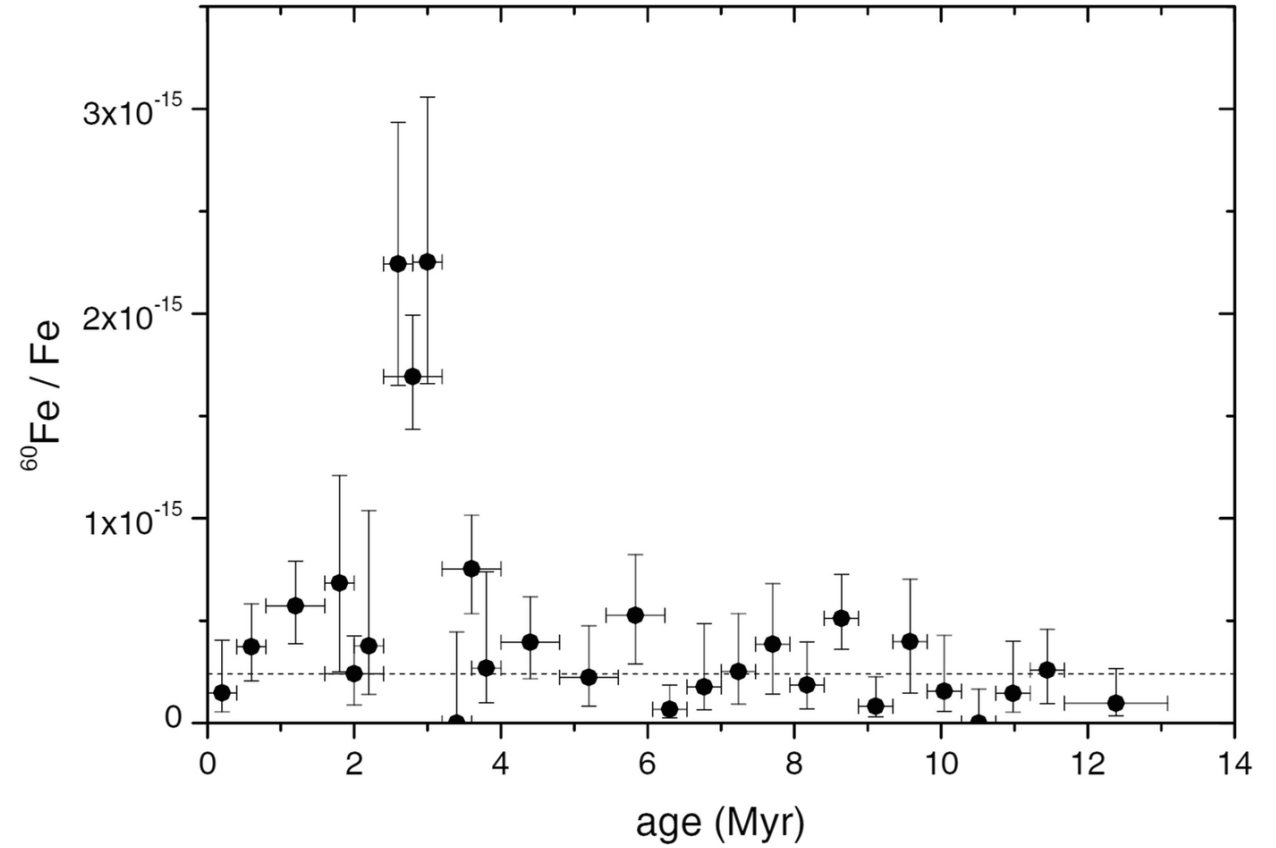
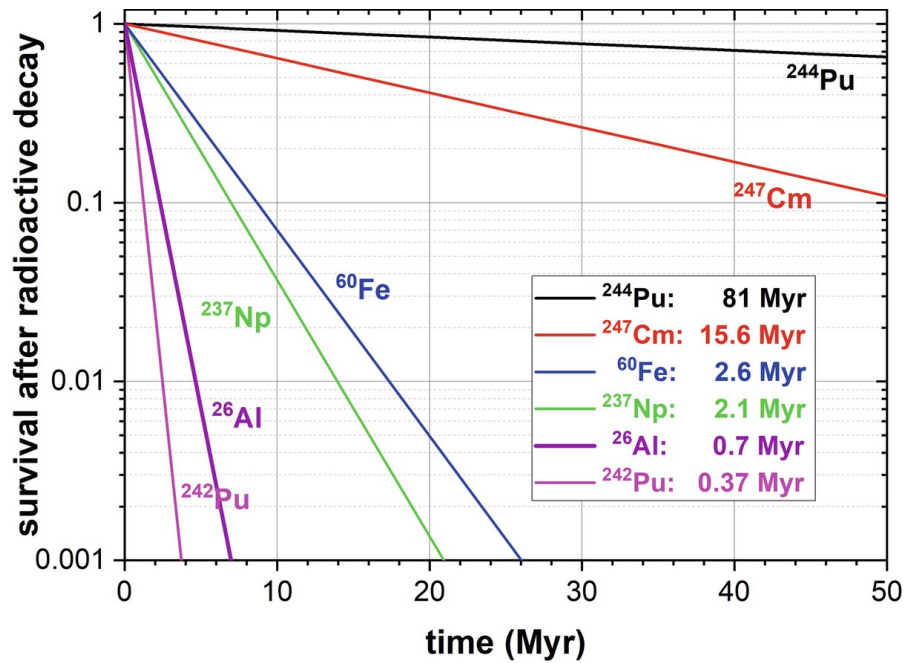


Haenecour+2013



Hoppe+2019

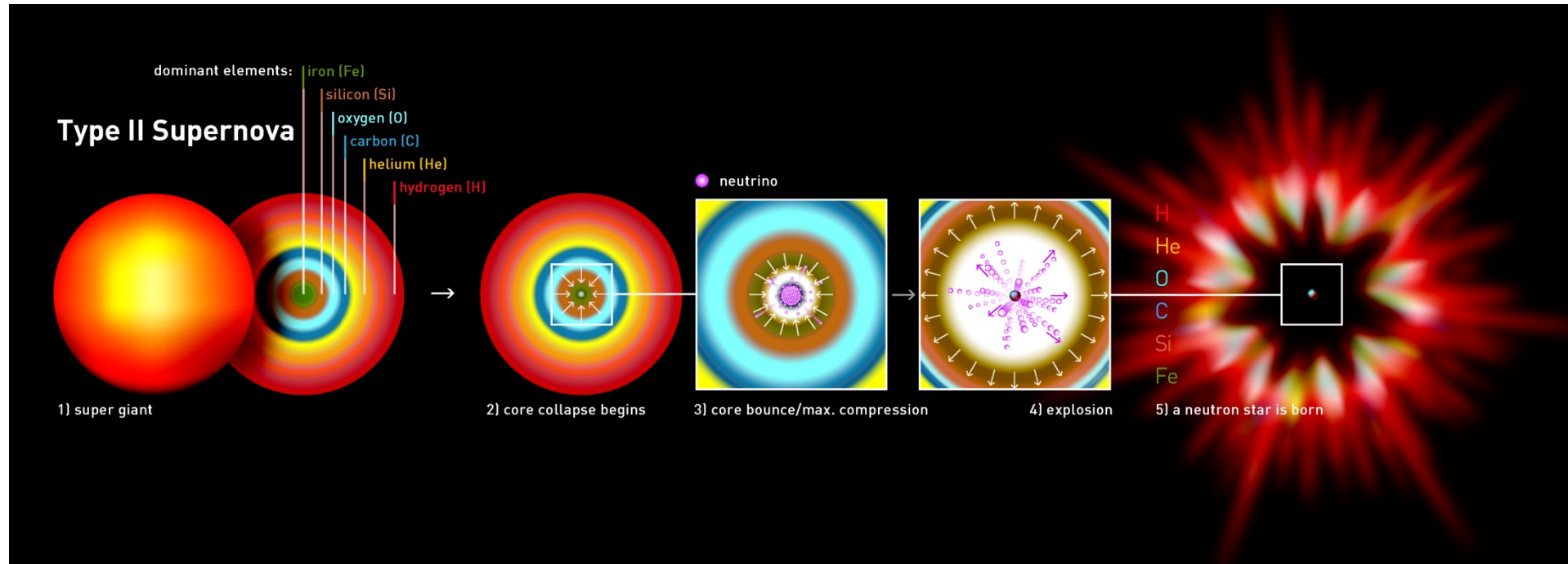
Deep Sea Crust



Figures from Wallner 2023

Understanding Core-Collapse Supernovae

Core-collapse supernovae



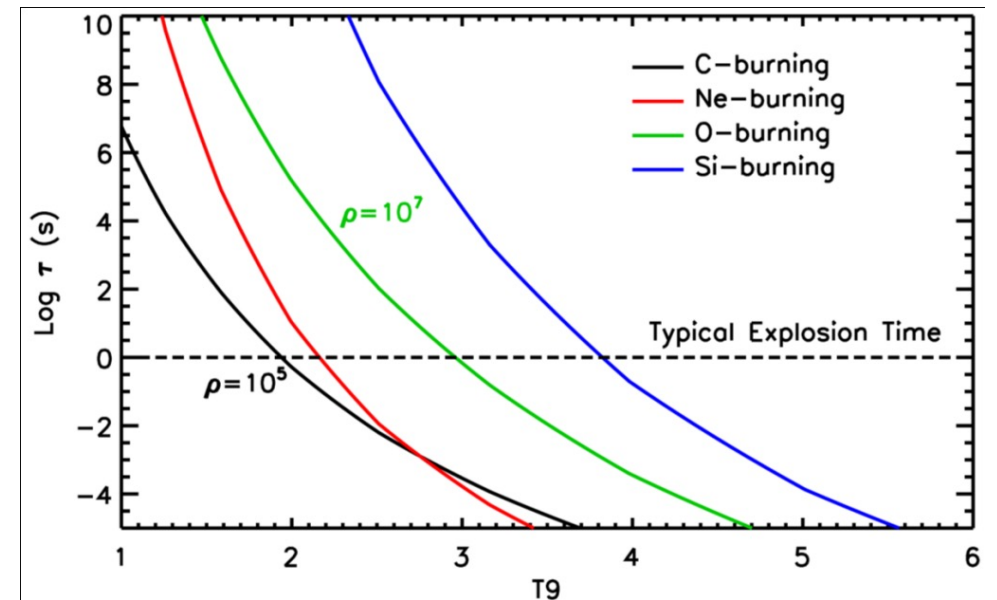
Massive star
at the end
of its life ...

... collapses
under gravity ...

... and
explodes
(sometimes)

Explosive nucleosynthesis

- Typical burning timescales: $\tau \sim \frac{1}{r_{ij}}$
 - Stellar reaction rate: $r_{ij} = n_i n_j \langle \sigma v \rangle_{ij}$
- Typical explosion timescale: 1 second
- Explosive burning:
 - Si burning: $T \gtrsim 4$ GK
 - O burning: $T \gtrsim 3.3$ GK
 - Ne burning: $T \gtrsim 2.1$ GK
 - C burning: $T \gtrsim 1.9$ GK



Explosive nucleosynthesis

- Complete Si-burning:
 - Temperature $T \gtrsim 5$ GK
 - Electron fraction $Y_e > 0.49$
 - Abundances from nuclear statistical equilibrium (NSE)
 - Products: Sc, Ti, Co, Ni, Zn
- Incomplete Si-burning:
 - Temperature between 4 and 5 GK
 - Electron fraction $Y_e > 0.49$
 - Abundances from quasi-statistical equilibrium (QSE)
 - Products: V, Cr, Mn

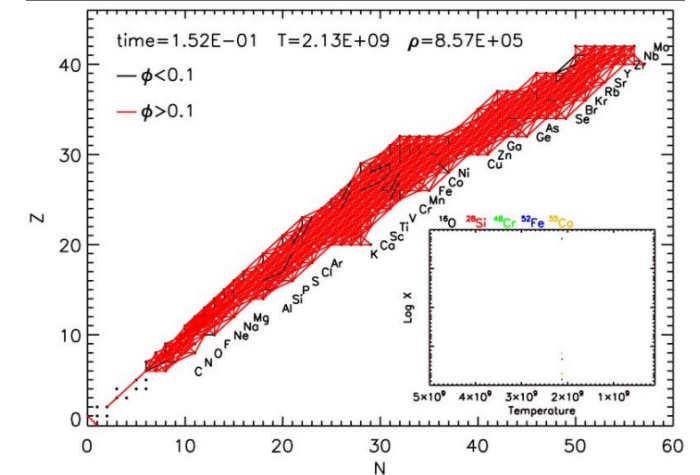
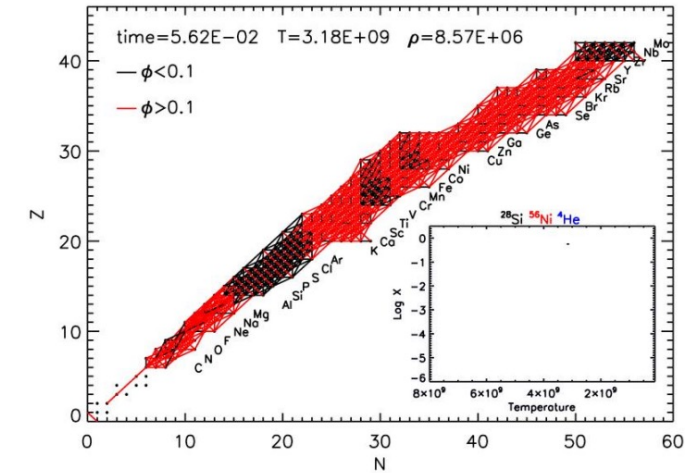


Figure: Limongi

Explosive nucleosynthesis

- Oxygen burning:

- Temperature between 3.3 and 4 GK
- Electron fraction $Y_e > 0.49$
- Abundances from QSE and sequences of nuclear reactions

Products:
Si, S, Ar, K, Ca

- Explosive burning below 3.3 GK

- Abundances through sequences of nuclear reactions
- Ne-burning: temperatures between 2.1 and 3.3 GK
- C-burning: temperatures between 1.9 and 2.1 GK

Products:
Mg, Al, P, Cl
Ne, Na

- Below 1.9 GK: no nuclear processing on explosive timescales

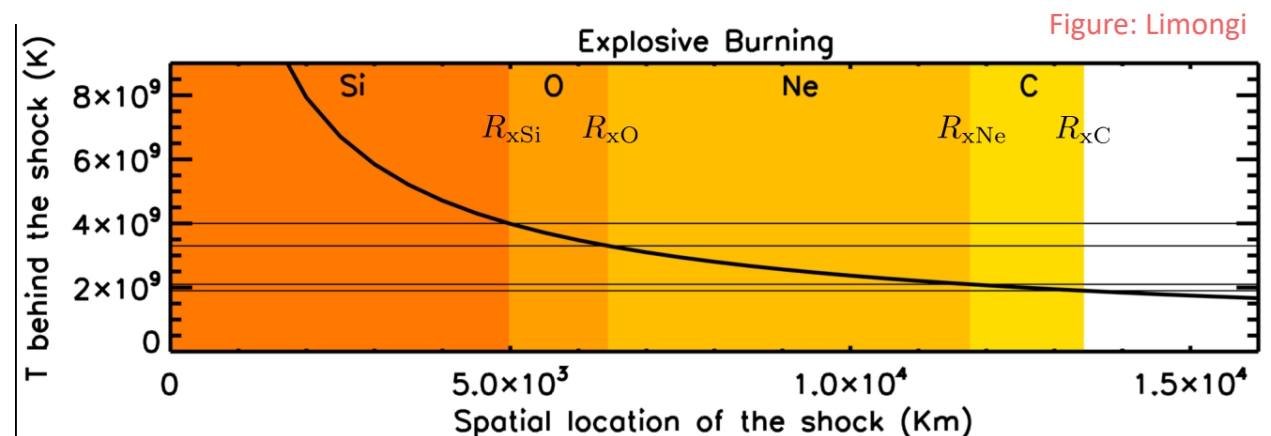
Energy considerations

- Shock temperature can be approximated by:

$$T_{shock} = \left(\frac{3 E_{expl}}{4\pi a R_{shock}^3} \right)^{1/4}$$

- Shock location for a typical explosion energy of 1 Bethe (10^{51} erg):

- Si-burning: 5000 km
- O-burning: 6400 km
- Ne-burning: 11750 km
- C-burning: 13400 km



Energy considerations

$$T_{shock} = \left(\frac{3 E_{expl}}{4\pi a R_{shock}^3} \right)^{1/4}$$

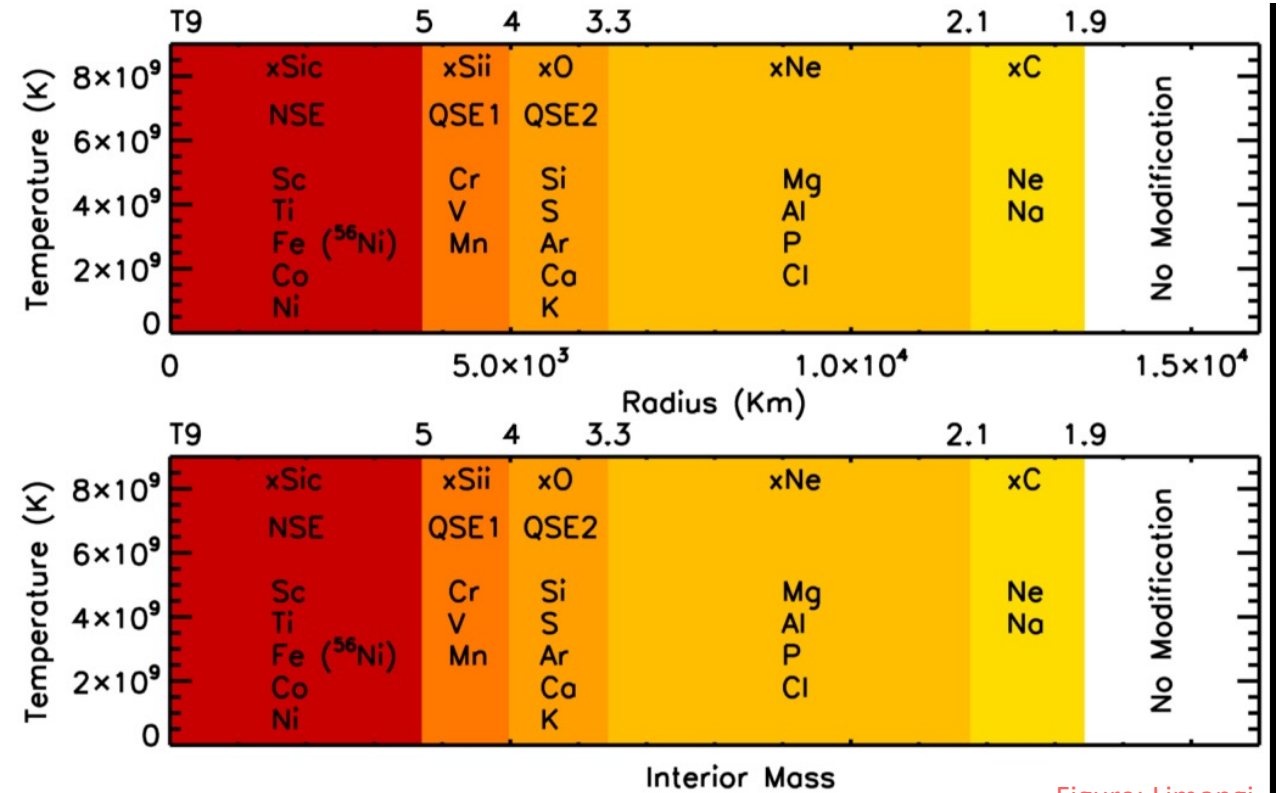
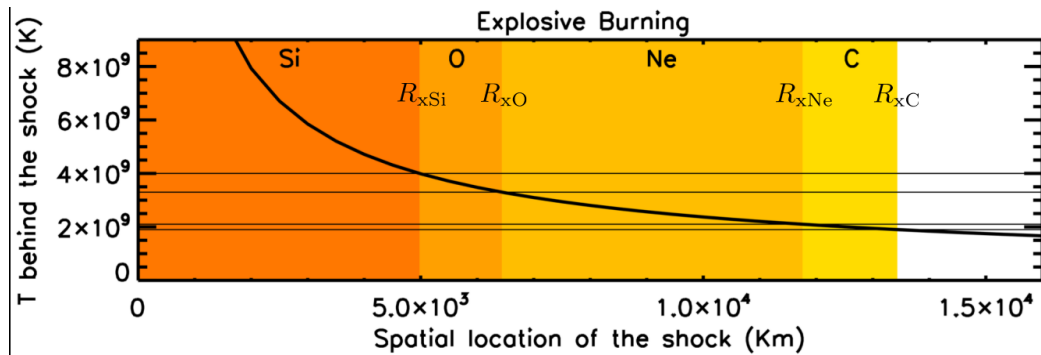
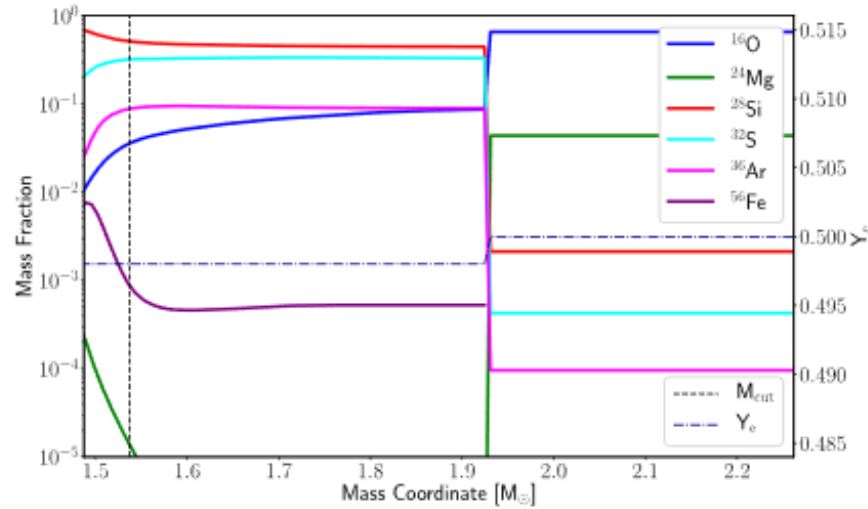


Figure: Limongi

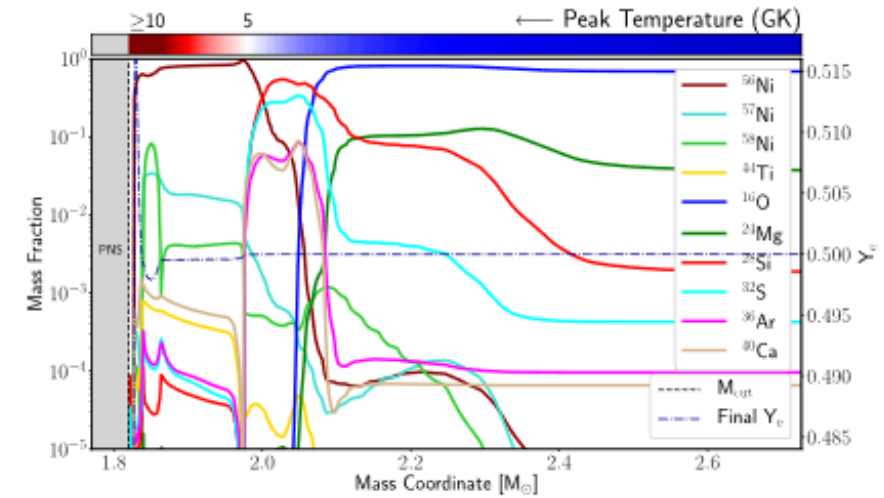
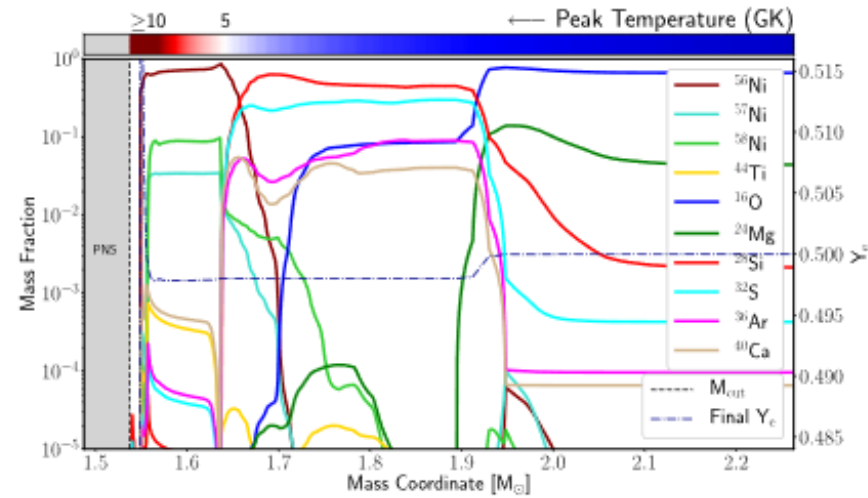
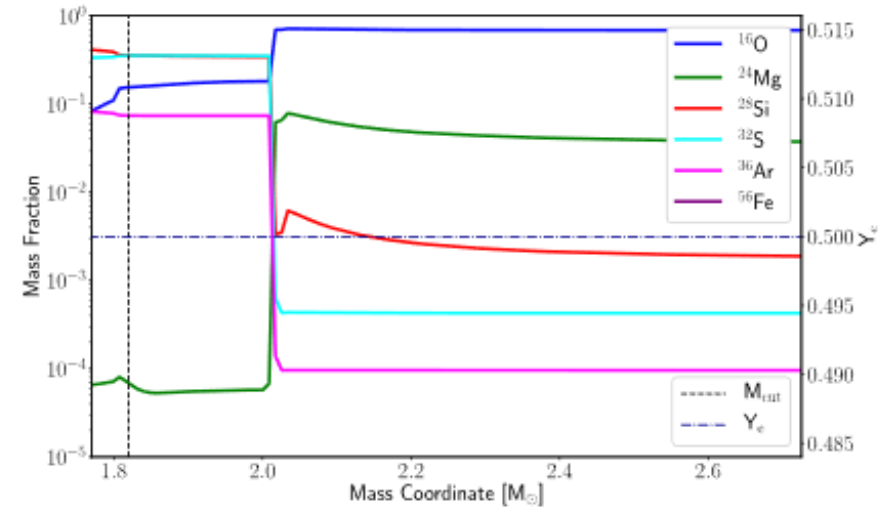
Explosive nucleosynthesis: Now in a simulation

16Msun

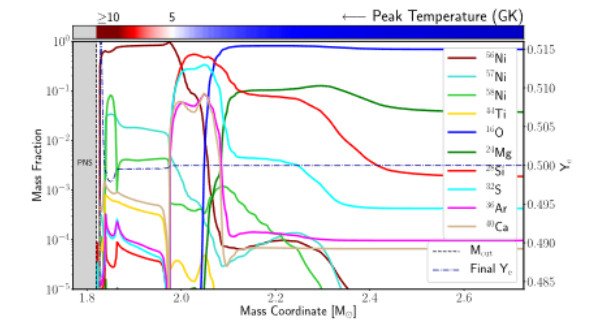
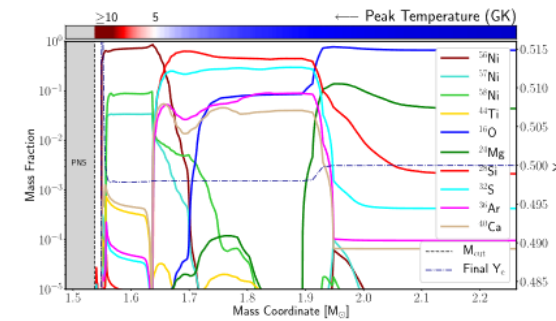
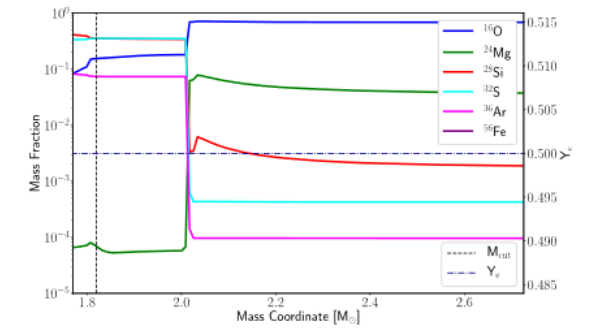
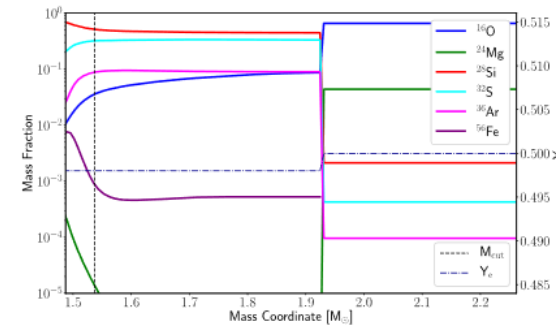
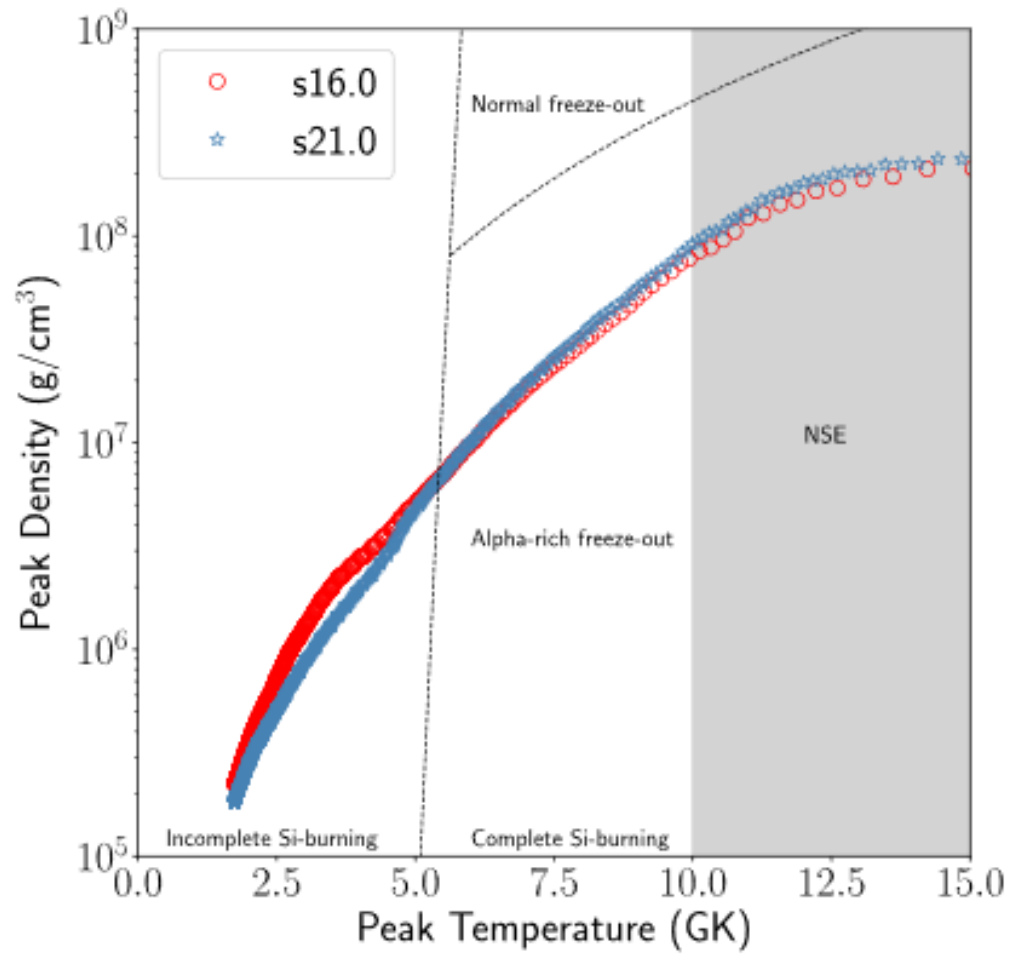
Curtis+2019



21Msun



Explosive nucleosynthesis



Does it matter how we seed the shock wave?

- Inner-most ejecta / iron-group elements: yes!
 - Intermediate mass elements: no
 - We need a consistent explosion which includes all the physics, not just an explosion energy
- What is the status of CCSN simulations?

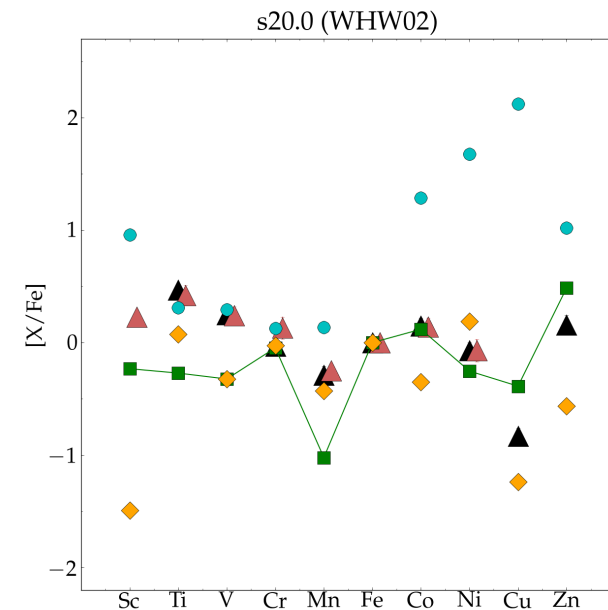
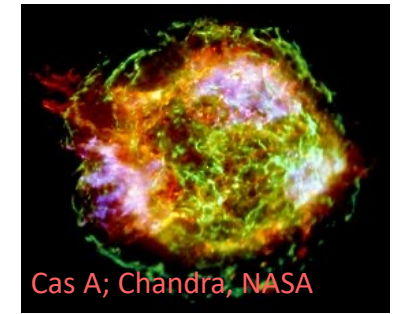
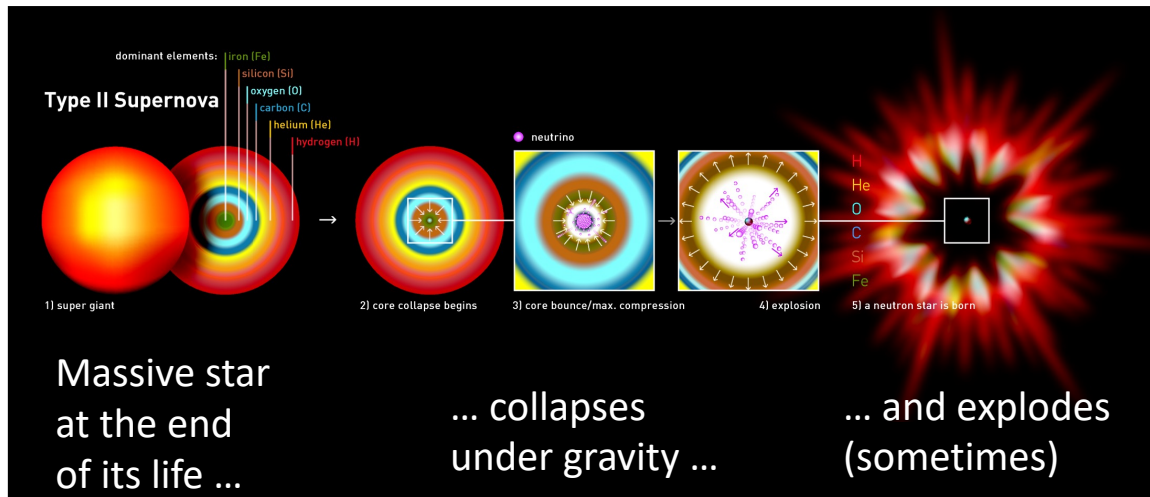


Figure: Curtis

Core-collapse supernova simulations



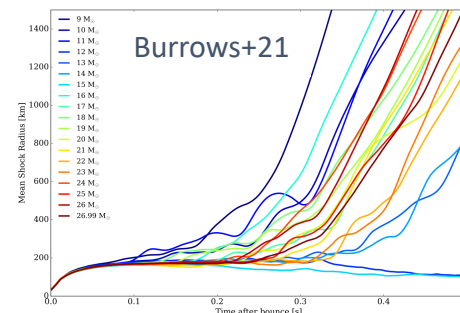
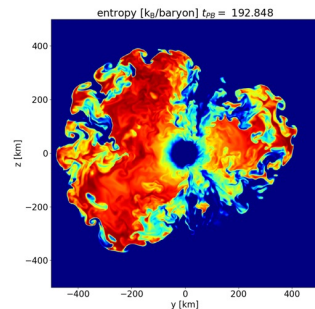
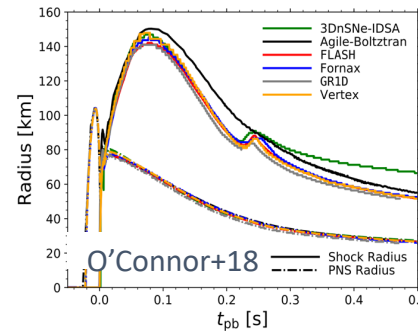
- Multi-dimensional problem
- Multi-physics problem:
 - General relativity
 - Nuclear physics of dense matter
 - Neutrino transport (trapped, diffusive, free-streaming regimes)
- Multi-scale problem:
 - shock formation at ~ 200 km vs entire star 10^8 km
 - collapse and shock formation ~ 1 s vs shock breakout ~ 1 day

Simulation Status:

1D: in general no self-consistent explosions
 ~ 10 CPUh/model

2D: models have converged

3D: mixed results
 \sim Mio CPUh/model



Current paths forward:

- Self-consistent 3D simulations (few, $O(10)$)
- Effective models (many, $O(1000)$)

The path forward

- Self-consistent 3D simulations
 - The ultimate goal :-)
 - Computationally expensive → can do $O(10)$
- Effective models
 - Simplify part of the problem, but have free parameters
 - Physically reliable
 - Computationally efficient → can do $O(1000)$
- We need both path for the open science questions:
 - Prediction of nucleosynthesis yields (and other observables)
 - Connection between progenitor and remnant?
 - Which massive stars explode successfully? Which ones do not?

Effective CCSN Models

- Parametrize a multi-dimensional aspect in 1D simulations
 - Mixing above the PNS, enhanced neutrino heating, etc
- Calibrate parametrization, then apply to many models
 - Eg a suitable model should reproduce observables of SN1987A
 - Predictive within the framework

- **PUSH**: Parametrized neutrino heating

Perego+15, Ebinger+19, Curtis+19, Ebinger+20, Ghosh+23

- **PHOT-B**: Parametrized neutrino heating

Ugliano+12, Ertl+15, Sukhbold+16

- **STIR**: Parametrized mixing above PNS

Couch+20

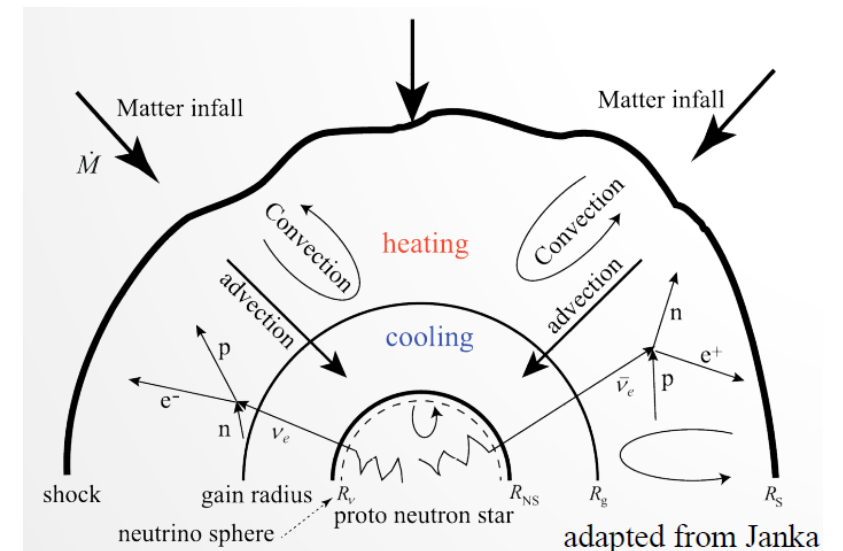
- Also: semi-analytic models and remnant mass formulae

O'Connor+13; Mueller+15; Pejcha15; Fryer+12,22; ...

Effective CCSN Models

- Parametrize a multi-dimensional aspect in 1D simulations
 - Mixing above the PNS, enhanced neutrino heating, etc
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 - Eg a suitable model should reproduce observables of SN1987A
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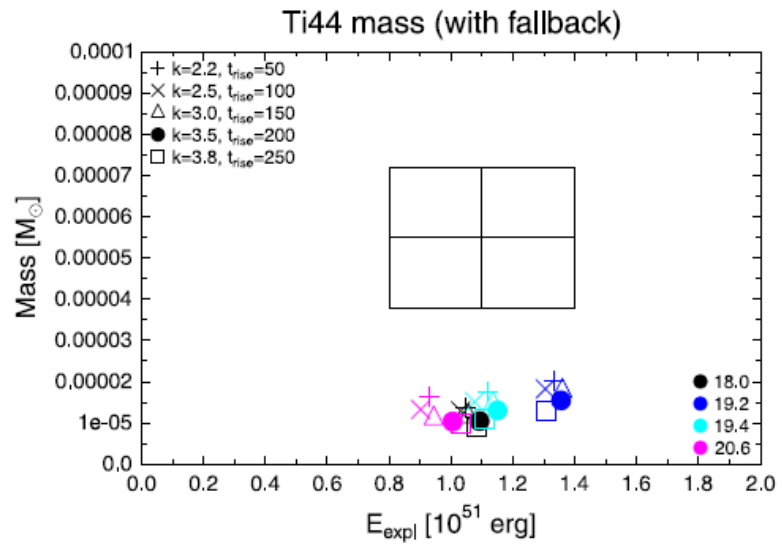
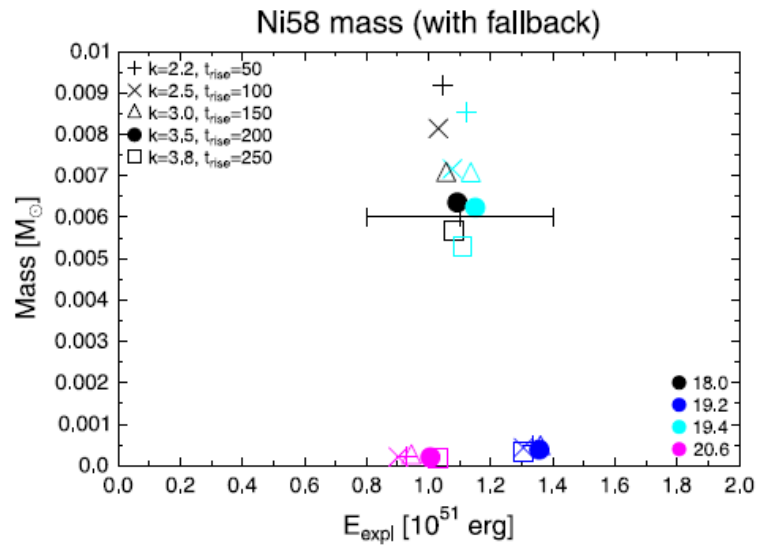
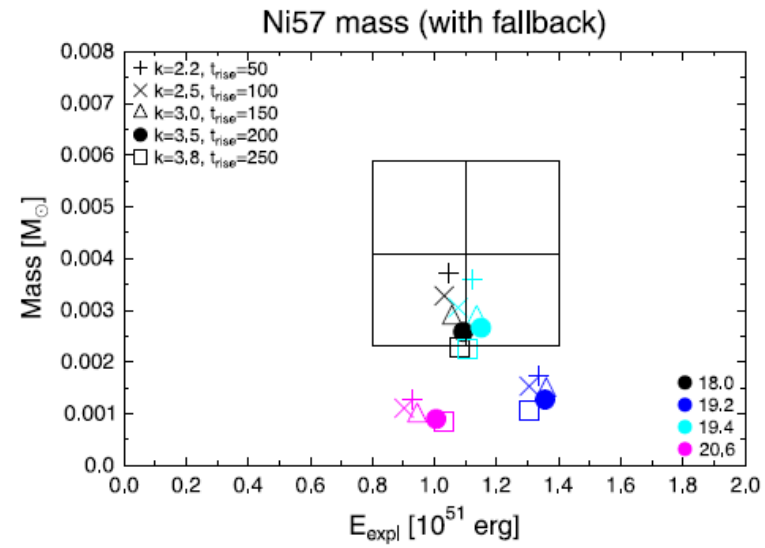
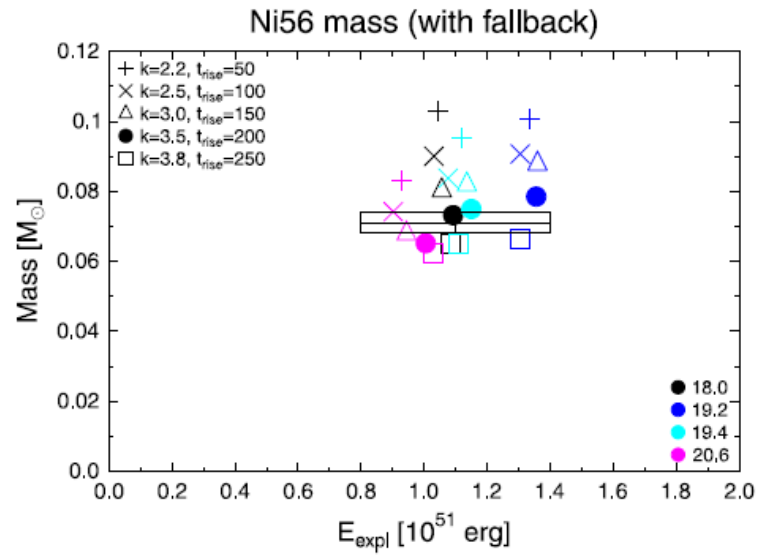
- **PUSH**: Parametrized neutrino heating
- **PHOT-B**: Parametrized neutrino heating
- **STIR**: Parametrized mixing above PNS



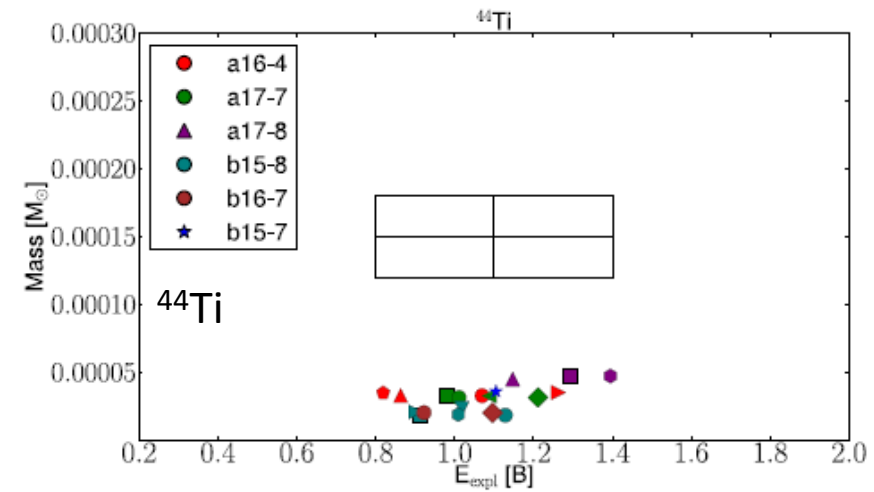
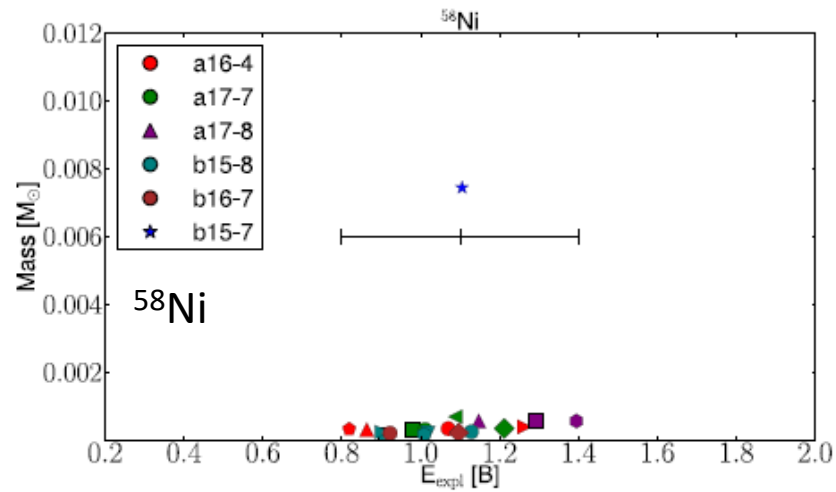
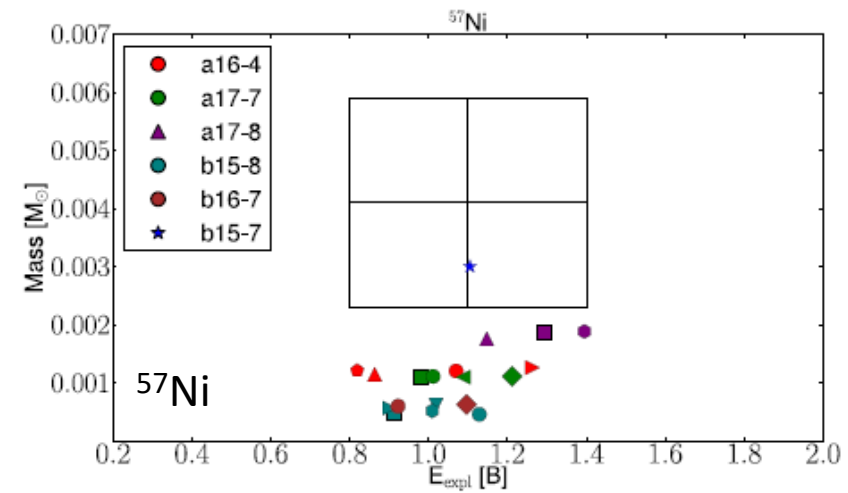
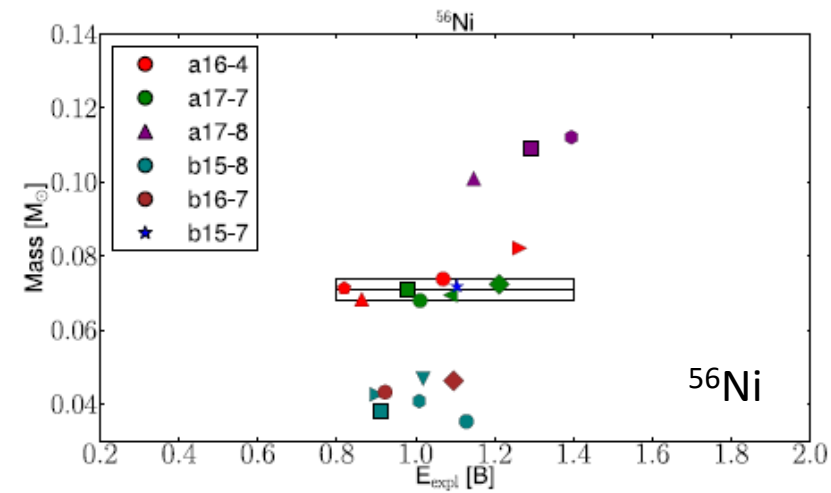
- Also: semi-analytic models and remnant mass formulae

O'Connor+13; Mueller+15; Pejcha15; Fryer+12,22; ...

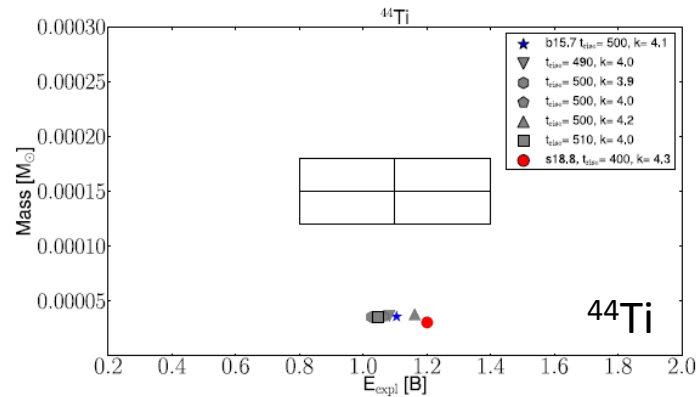
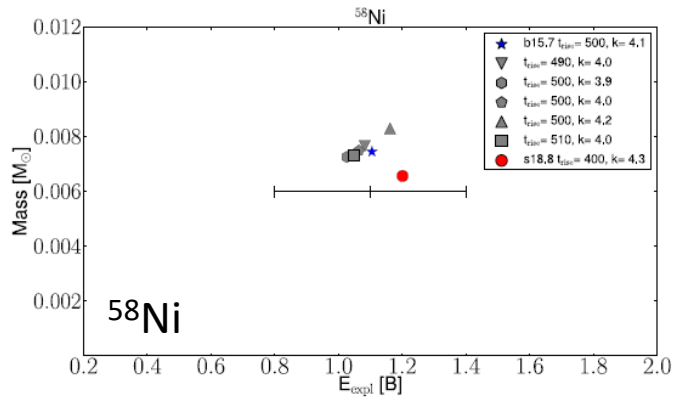
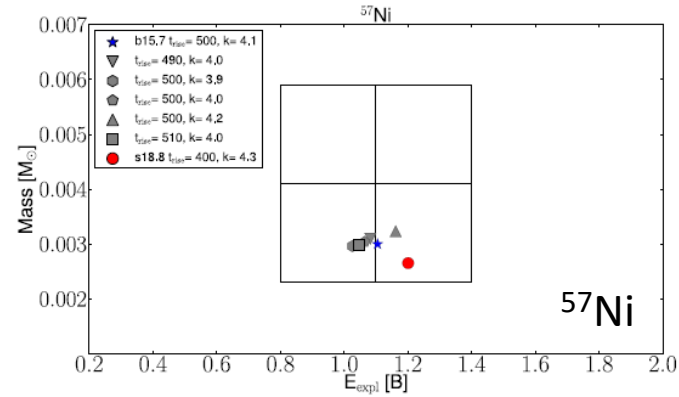
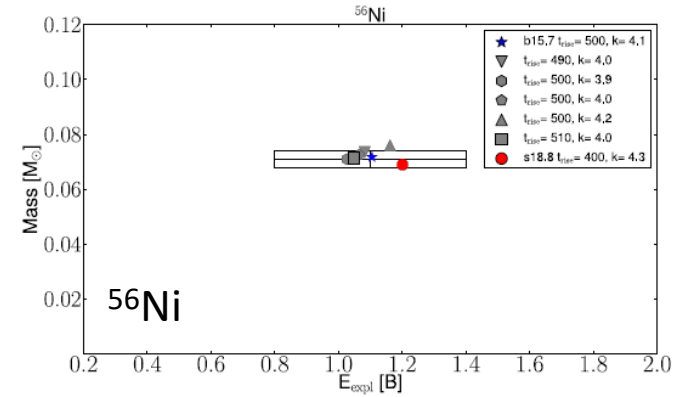
SN1987A: Calibration of PUSH



SN1987A: Calibration of PUSH



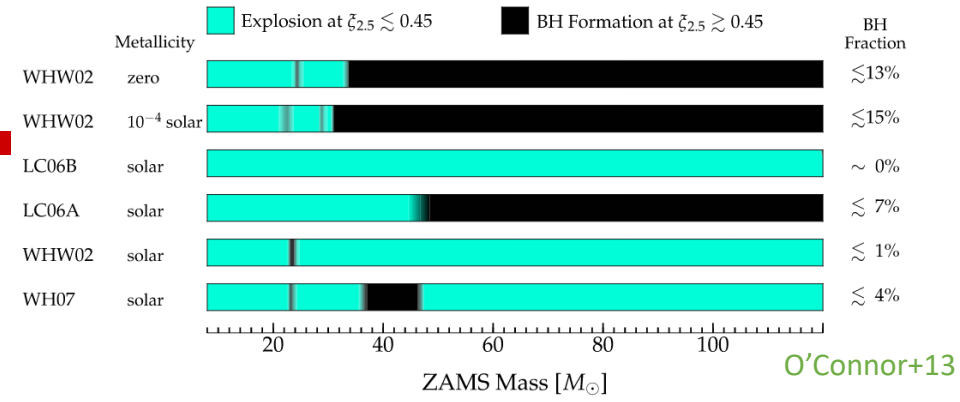
SN1987A: Calibration of PUSH



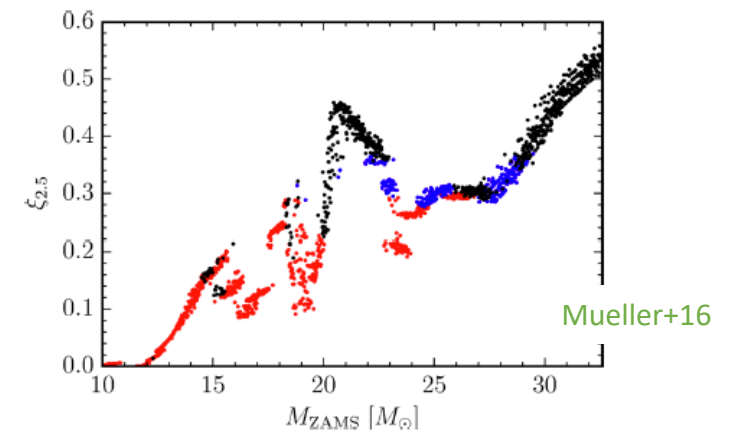
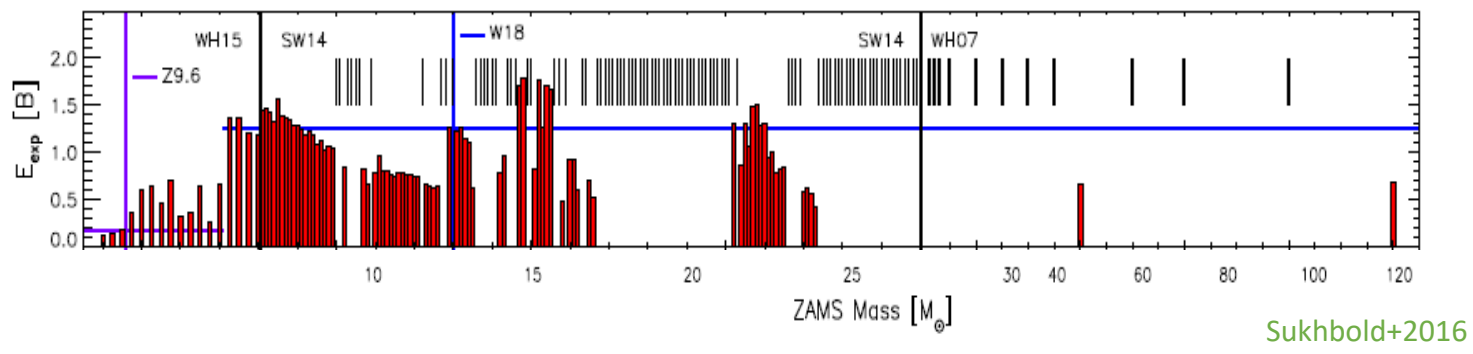
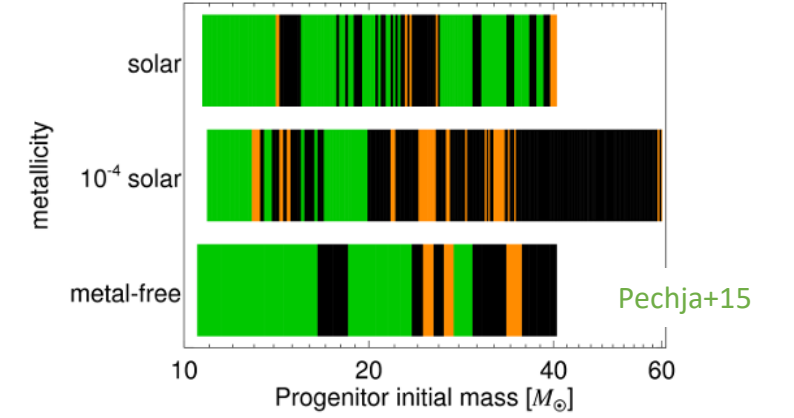
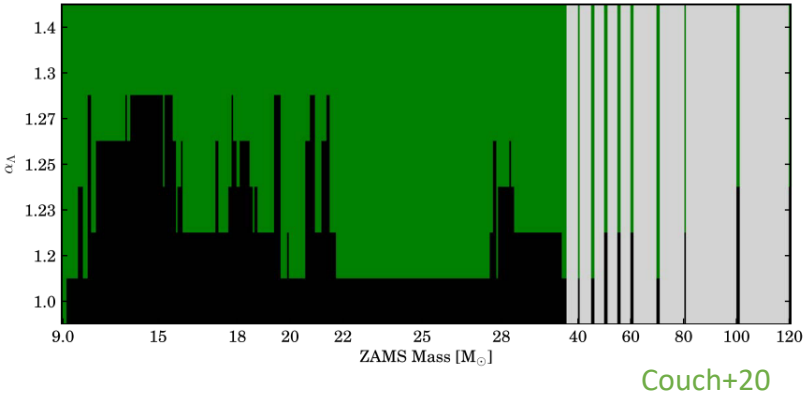
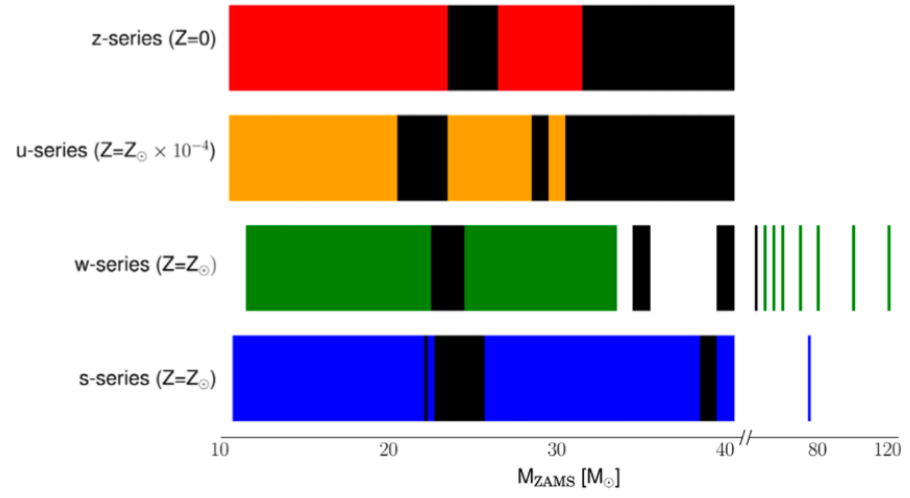
Comparing calibrations using **red supergiants** and **blue supergiants**

Name	k_{PUSH} (-)	t_{rise} (ms)	E_{expl} (10^{51} erg)	$m(^{56}\text{Ni})$ (M_{\odot})	$m(^{57}\text{Ni})$ (M_{\odot})	$m(^{58}\text{Ni})$ (M_{\odot})	$m(^{44}\text{Ti})$ (M_{\odot})
SN 1987A	—	—	1.1 ± 0.3	0.071 ± 0.003	0.0041 ± 0.0018	0.006	1.5×10^{-4} $\pm 0.3 \times 10^{-4}$
b15-7	4.1	500	1.1	0.072	0.0030	0.0074	3.60×10^{-5}
s18.8	4.3	400	1.2	0.069	0.0027	0.0066	3.05×10^{-5}

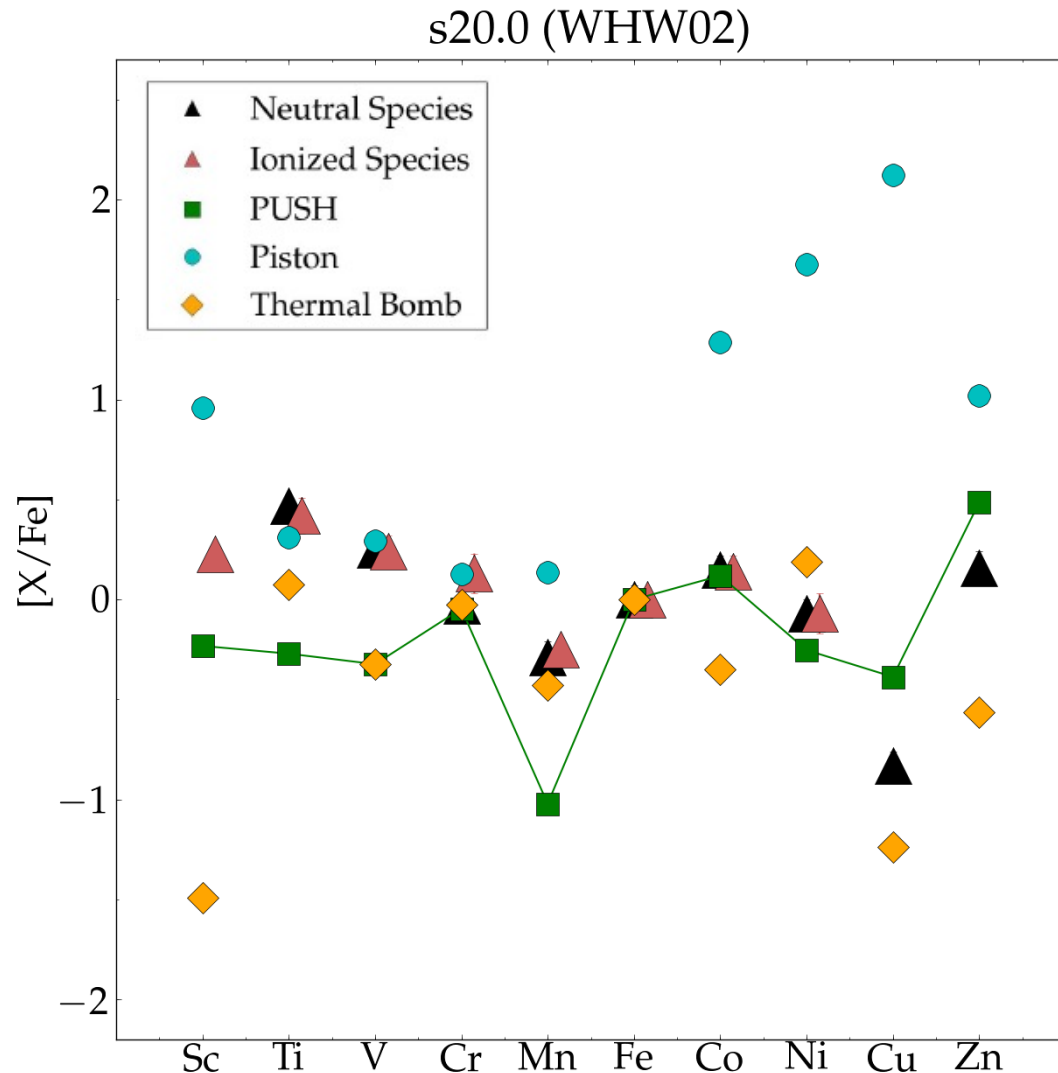
Effective CCSN Models



Ebinger+20



Comparison of methods



Thermal bomb:

- Skips the collapse and onset of explosion phase
- Deposits thermal energy over a few interior zones
- Mass cut is determined by integrating the ^{56}Ni yield from the outside in until the desired value is reached

Piston:

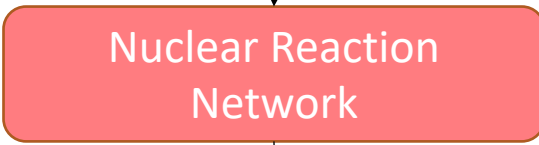
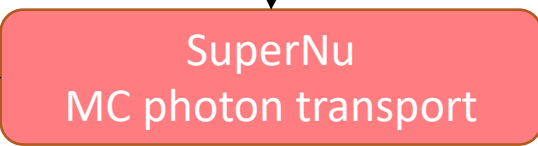
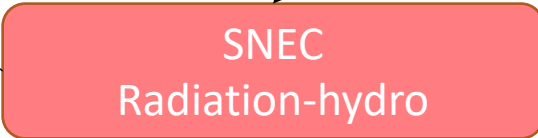
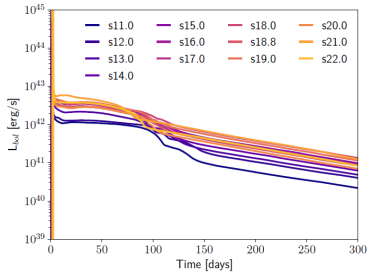
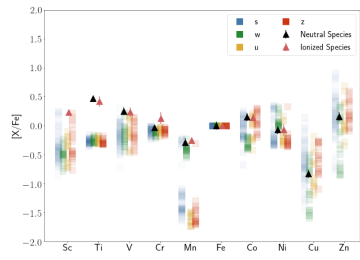
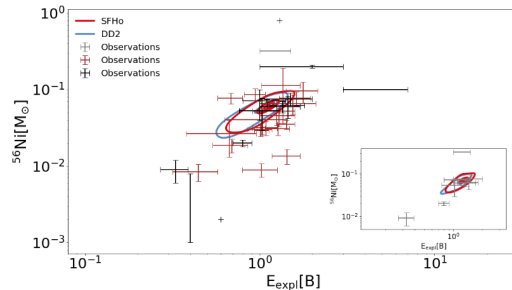
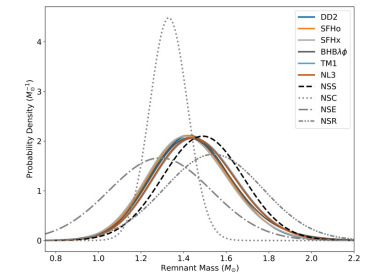
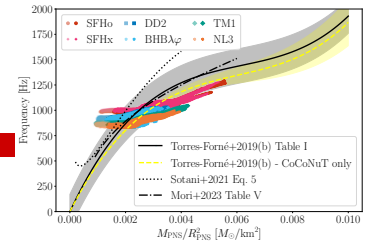
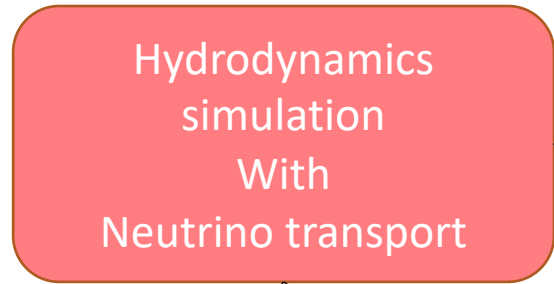
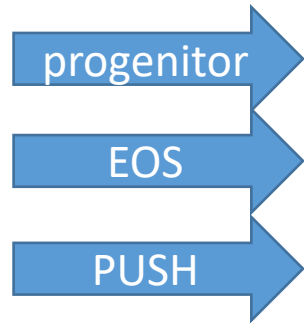
- Skips the weak physics of collapse and onset of explosion
- Trajectory of a particular mass zone is prescribed (infall and outwards motion)
- Mass cut is set by location of the piston

PUSH:

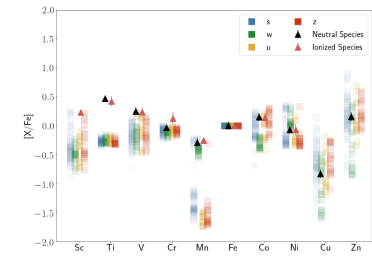
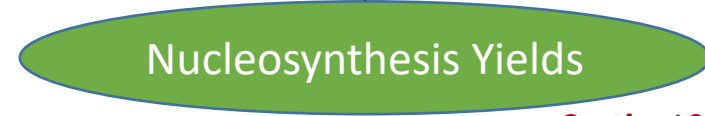
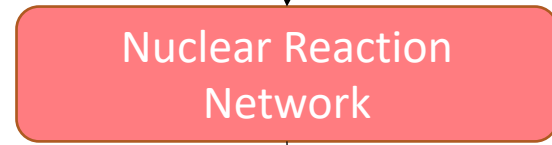
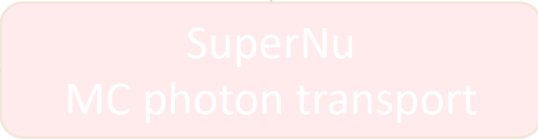
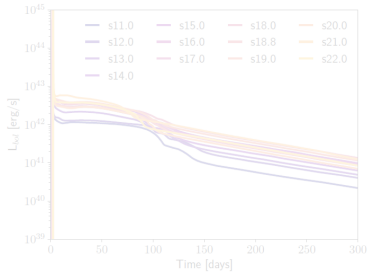
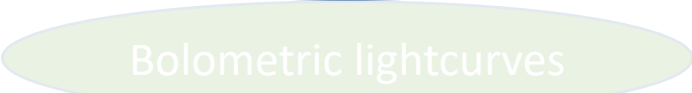
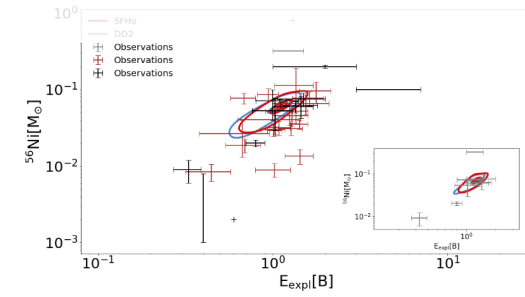
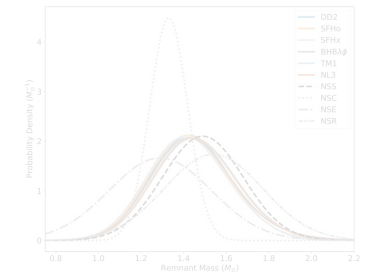
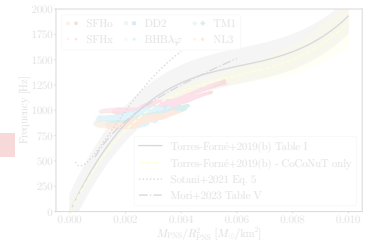
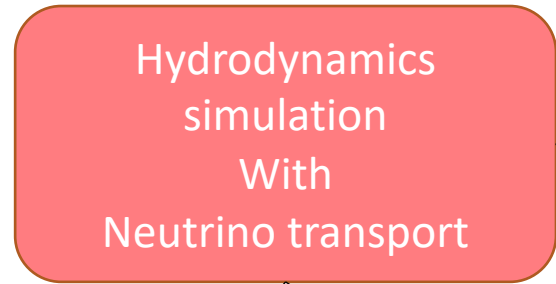
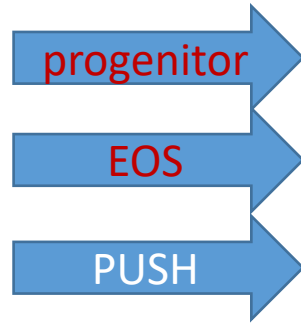
- Mimics a neutrino-driven explosion
- Includes changes in the electron fraction from weak reaction during collapse and neutrino reactions during collapse and explosion
- Calibration required

Some recent results from the NC State University Group

From explosions to observables

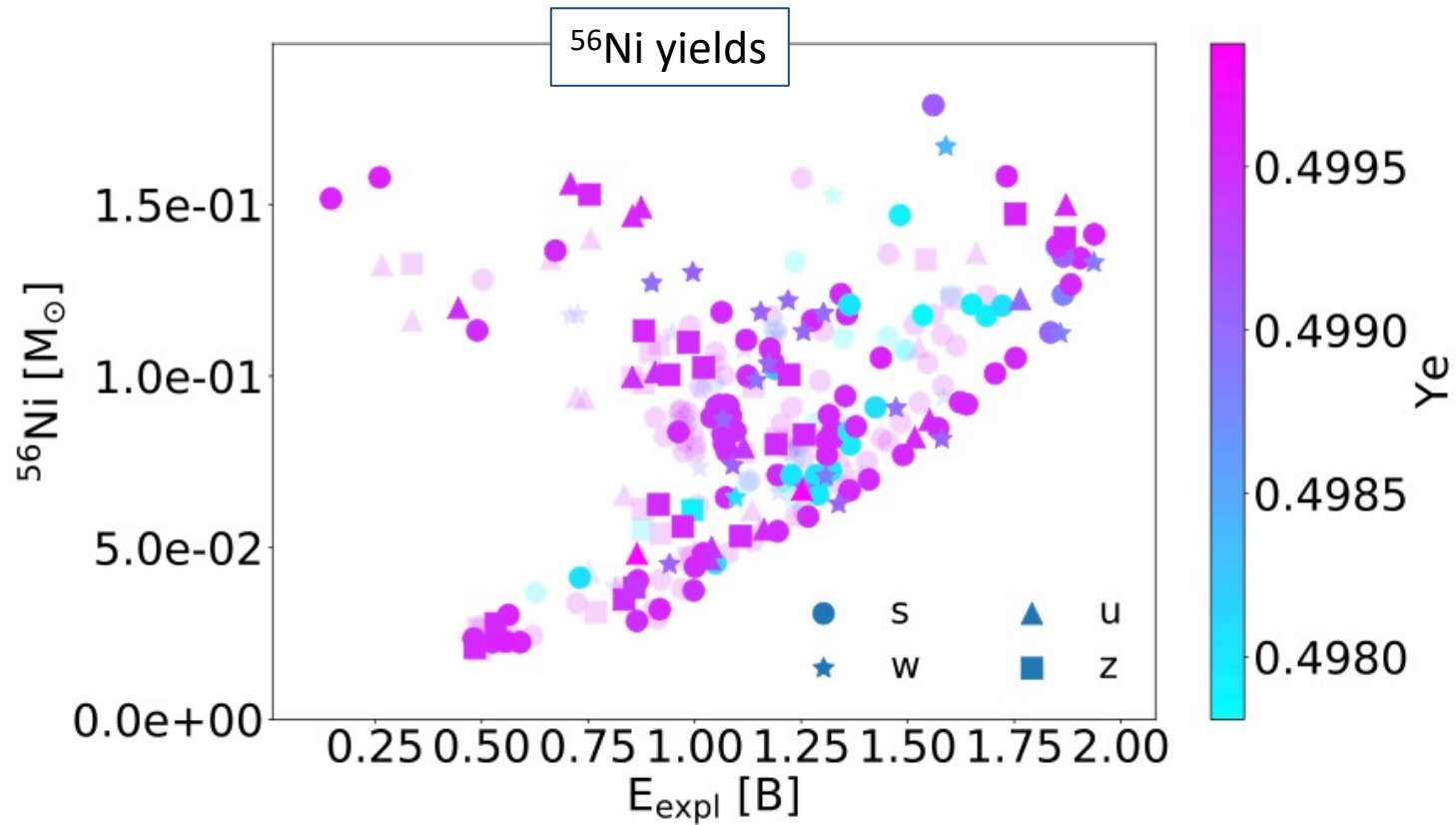


From explosions to observables



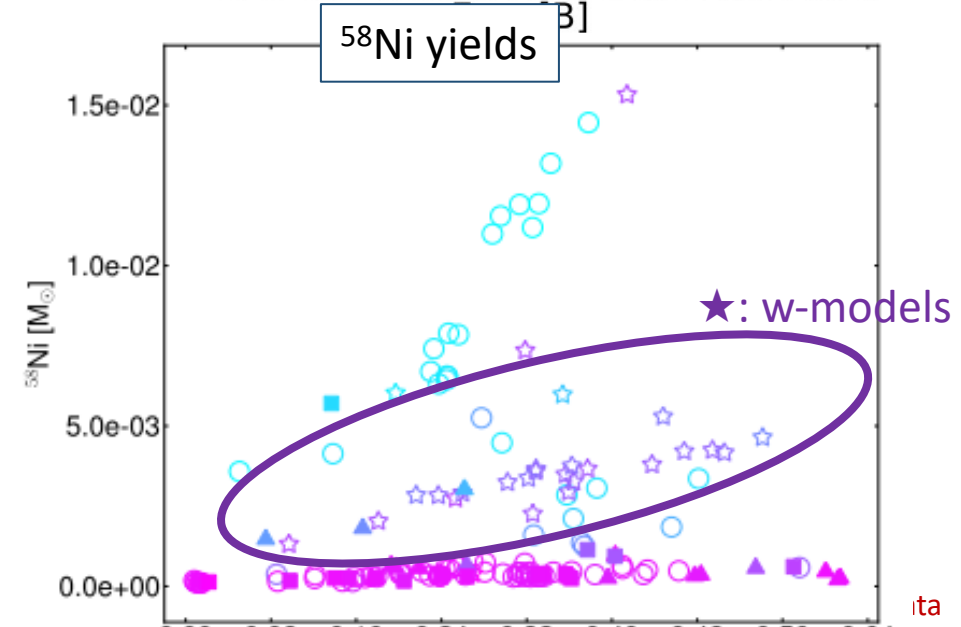
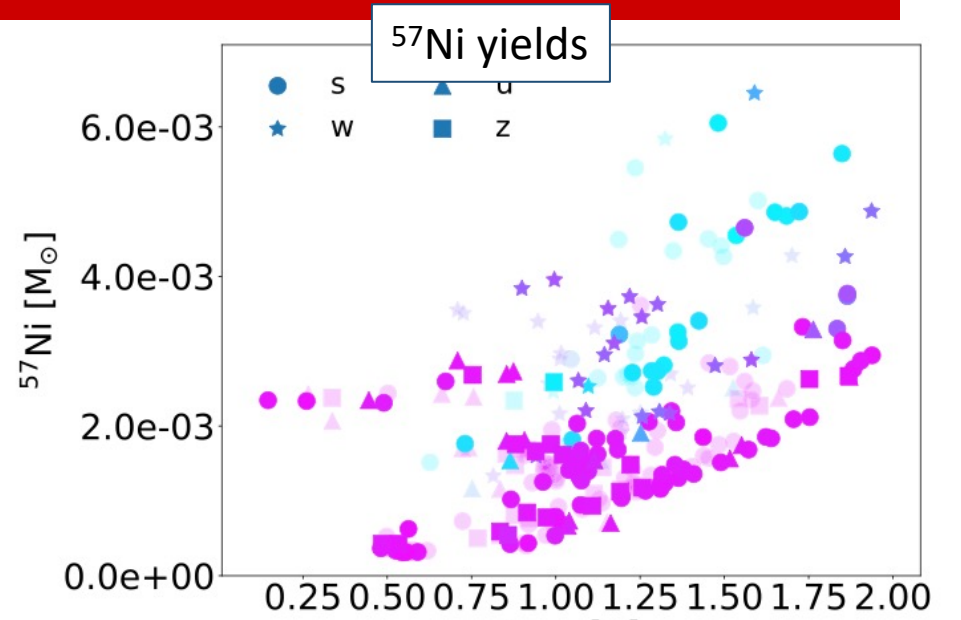
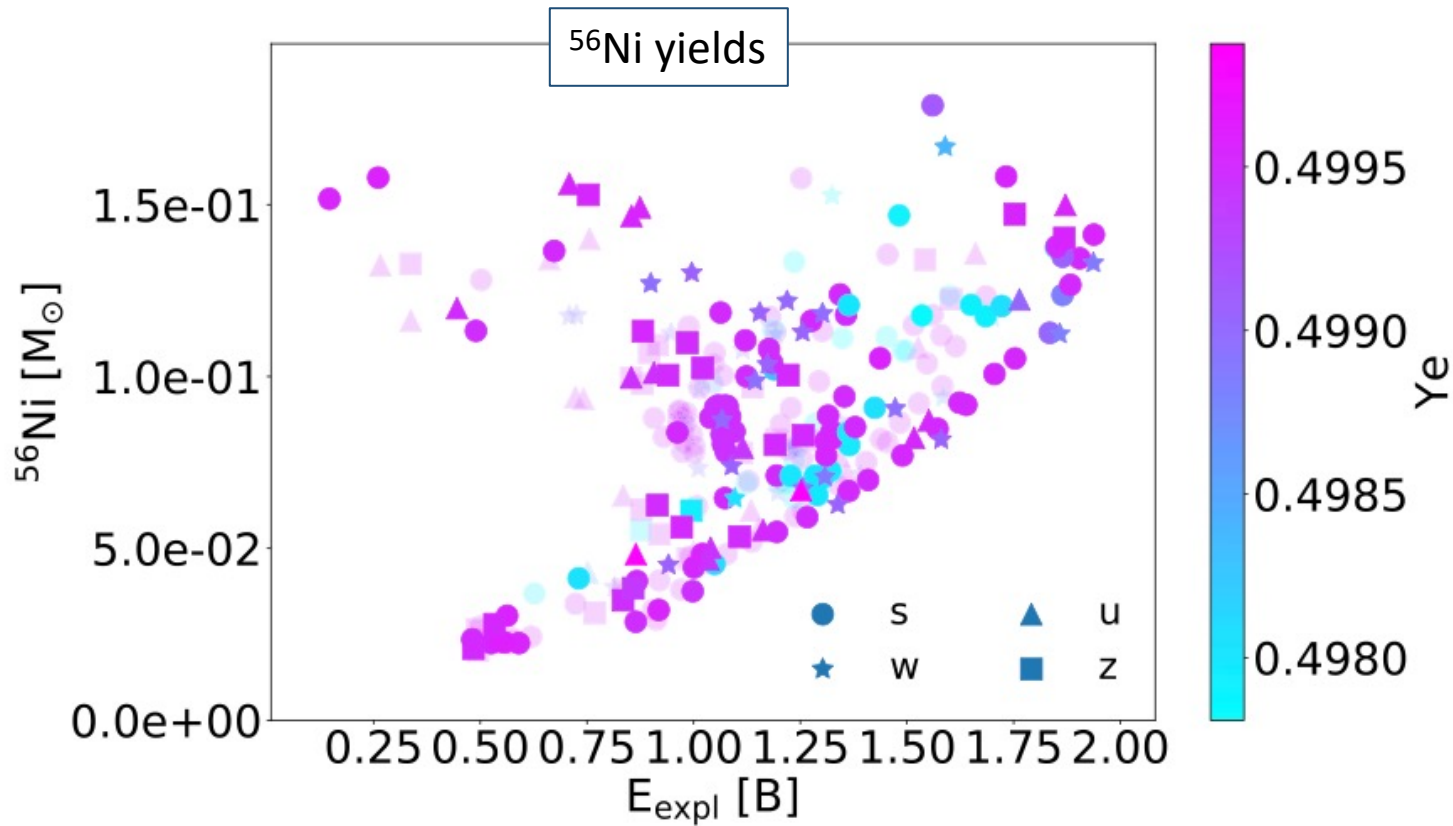
Isotopic and Elemental Nickel Yields

Curtis+19
Ghosh+22



Isotopic and Elemental Nickel Yields

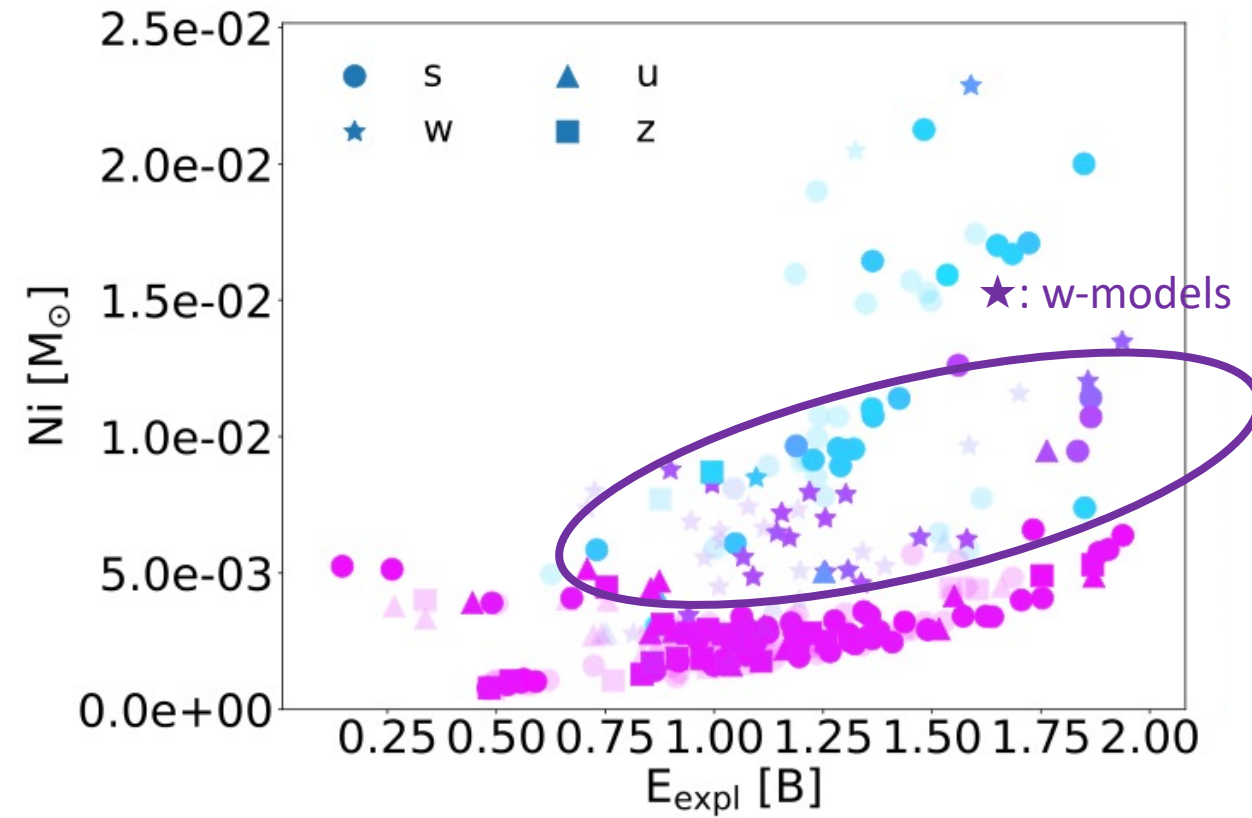
Curtis+19
Ghosh+22



w-models: 100s of isotopes during stellar evolution
s/u/z-models: 21 isotope network during stellar evolution

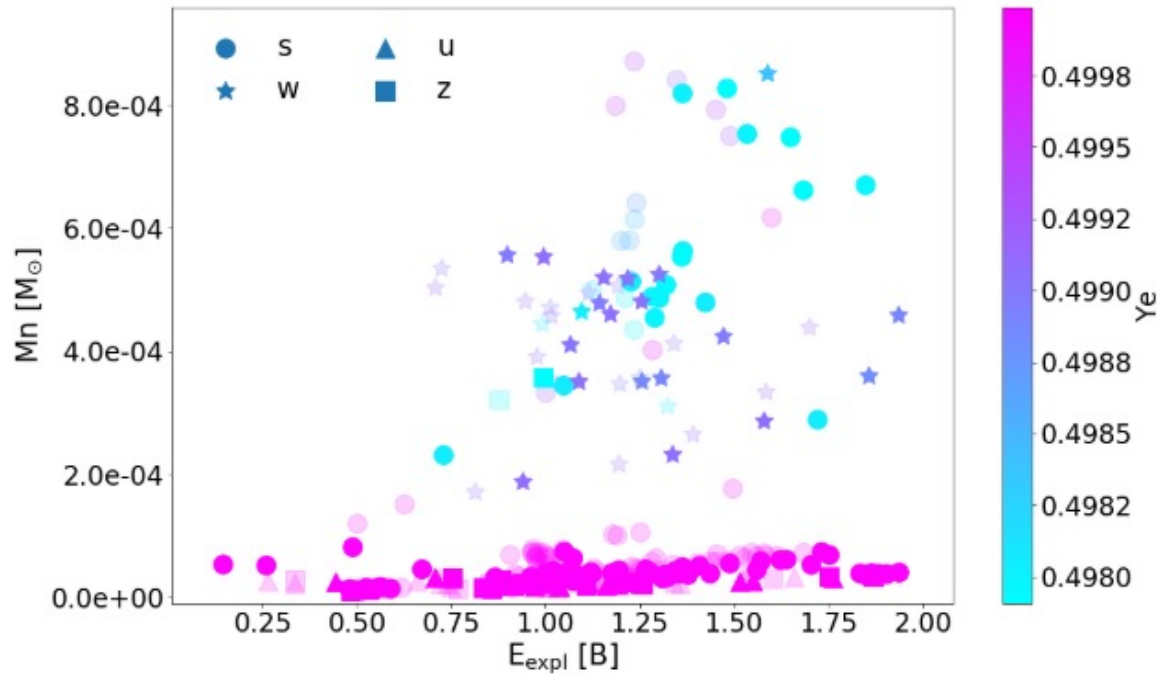
Isotopic and Elemental Nickel Yields

Curtis+19
Ghosh+22

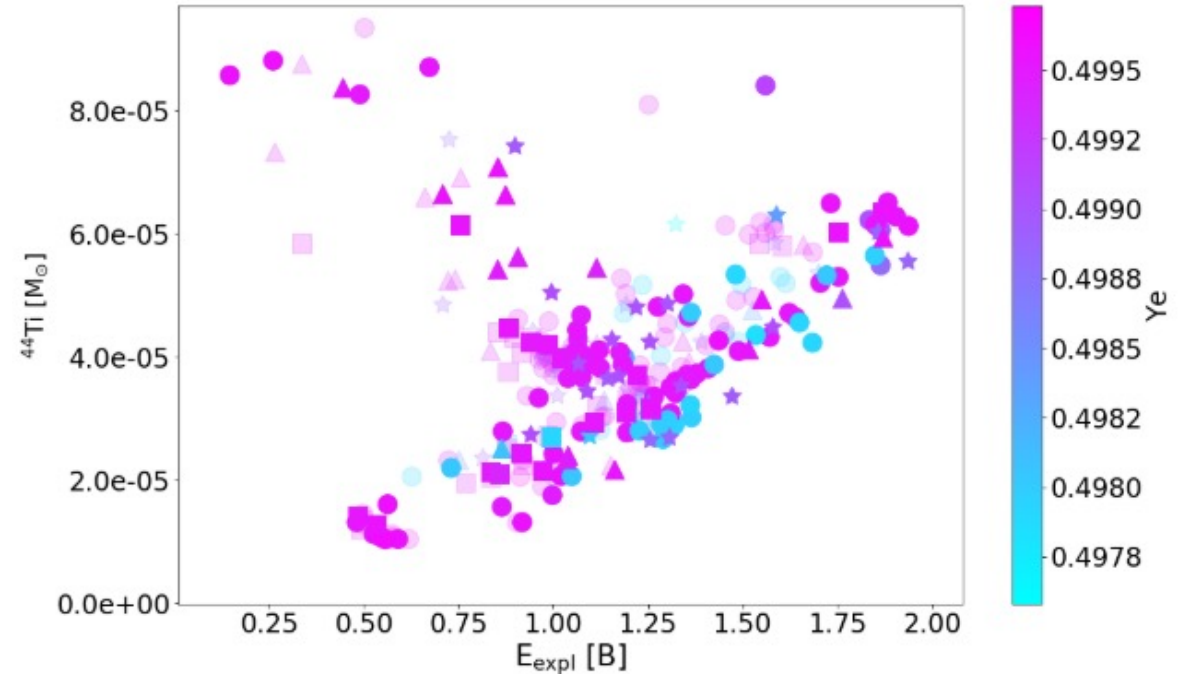


Other Fe-group elements

Elemental Mn yields



Isotopic ⁴⁴Ti yields



★: w-models

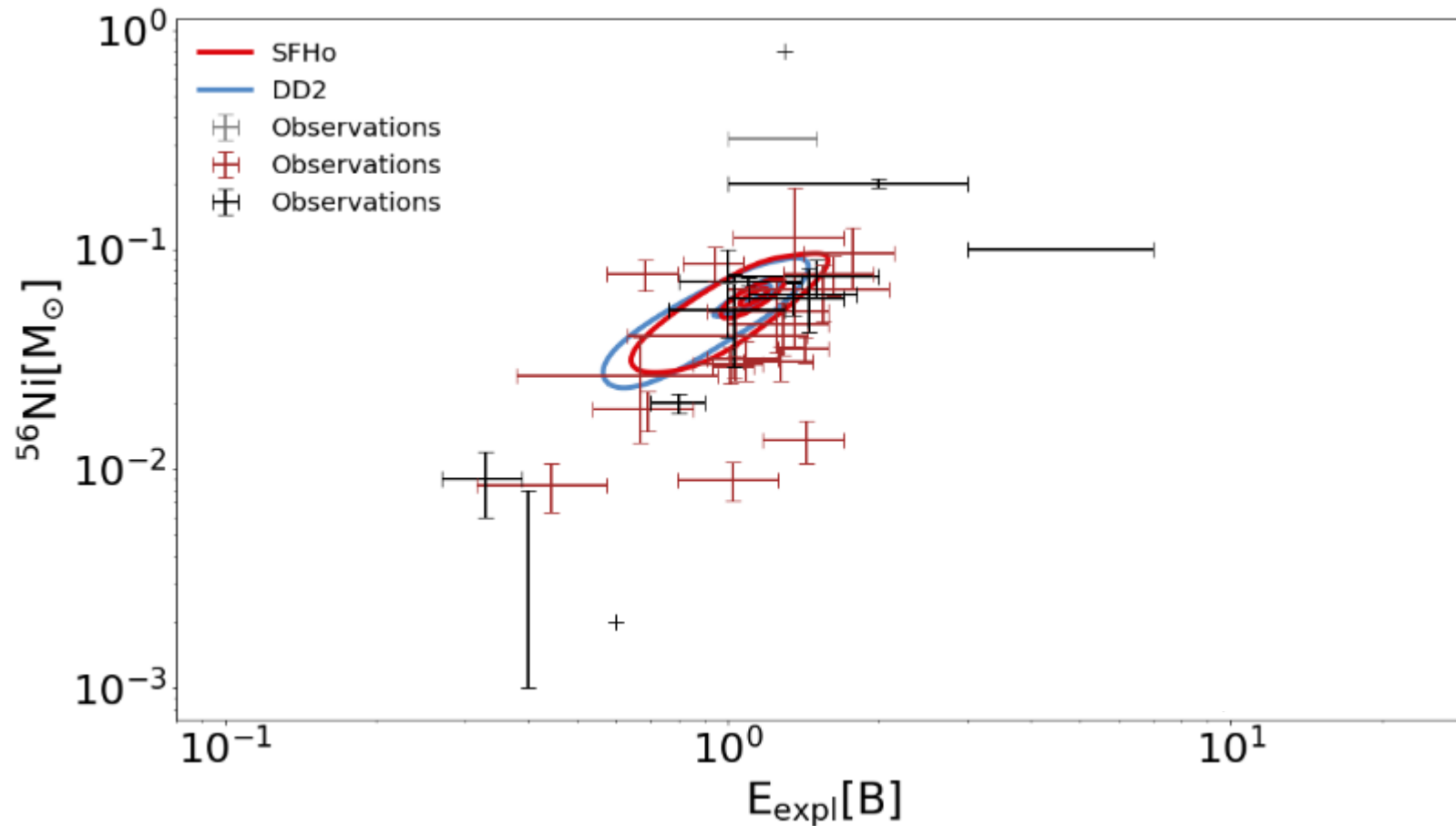
w-models: 100s of isotopes during stellar evolution
s/u/z-models: 21 isotope network during stellar evolution

→ The progenitor (structure and network size) matters

Explosion energy and ^{56}Ni yields

Ghosh+22

→ In PUSH: Explosion energy and ^{56}Ni mass emerge self-consistently with each other

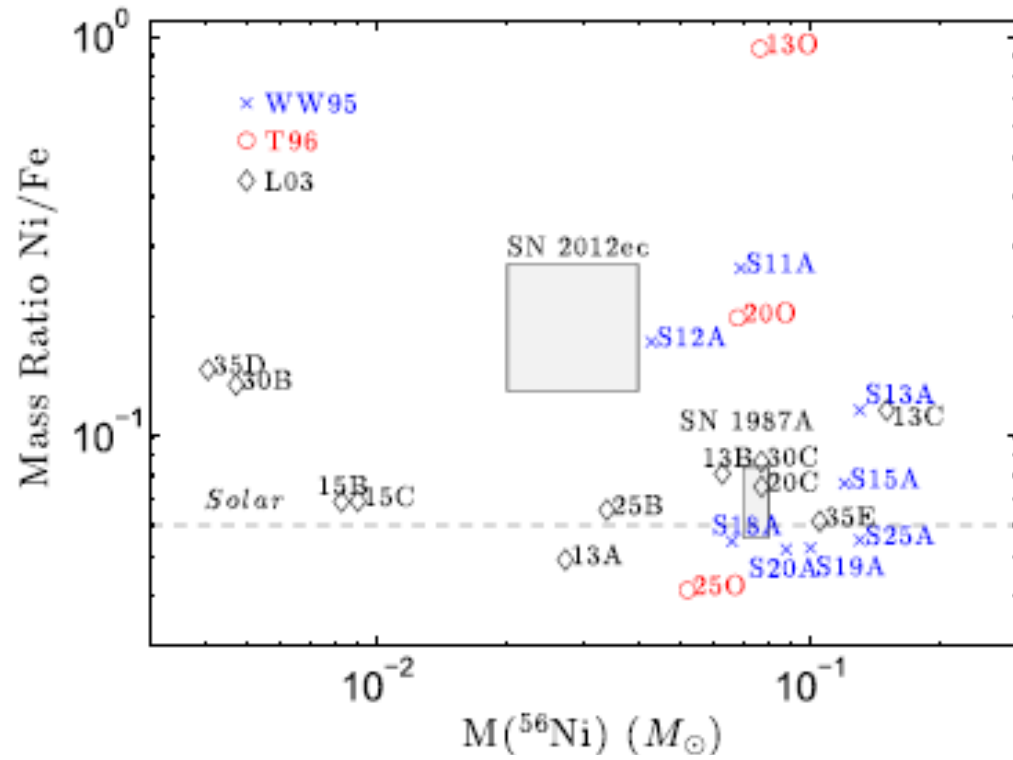


Simulations are IMF weighted for KDE estimation

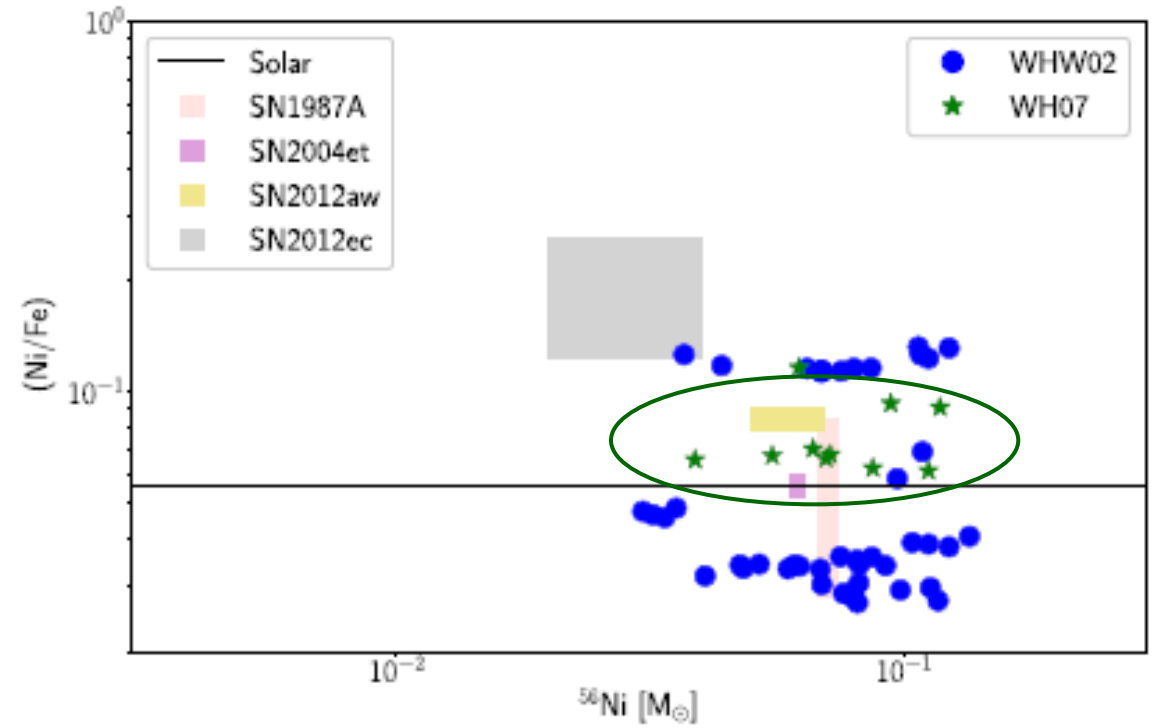
DD2 data from [Ebinger+20](#)

SFHo data from [Ghosh+22](#)

Ni/Fe ratio



Jerkstrand+ 2015

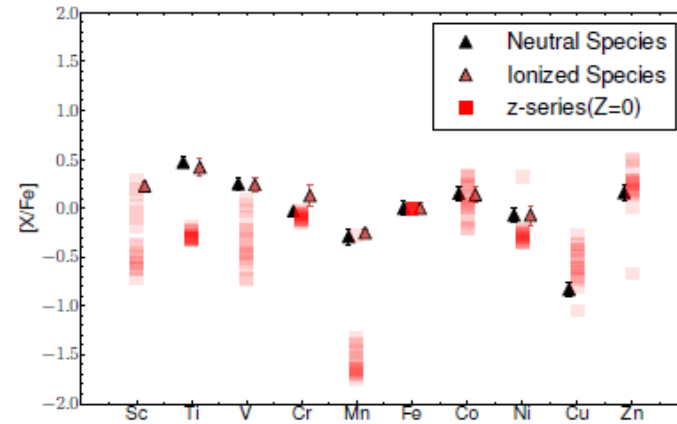
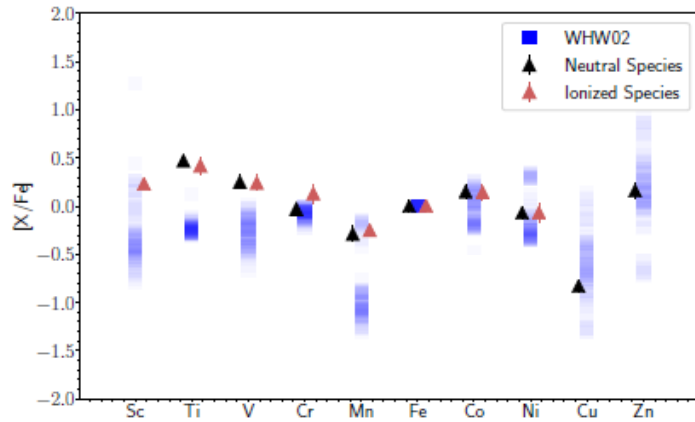


Curtis+19

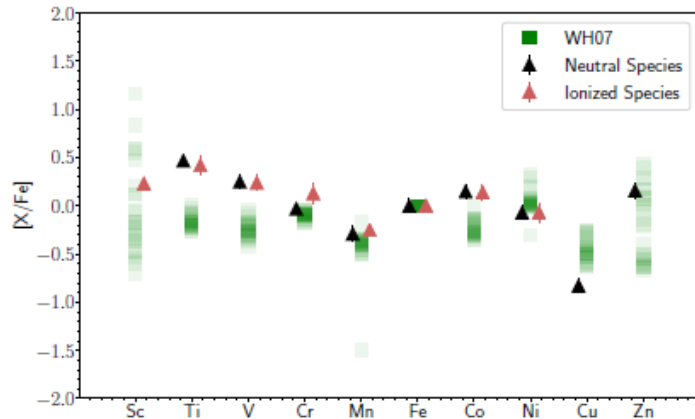
Fe-group elements and metal-poor stars

Observational data (triangles):
Metal-poor star HD84937

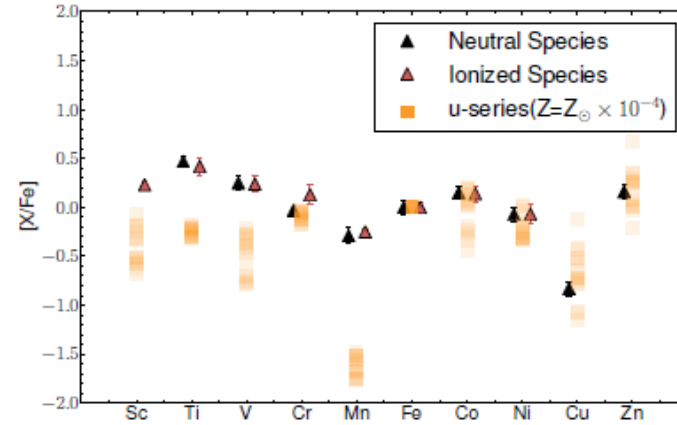
PUSH



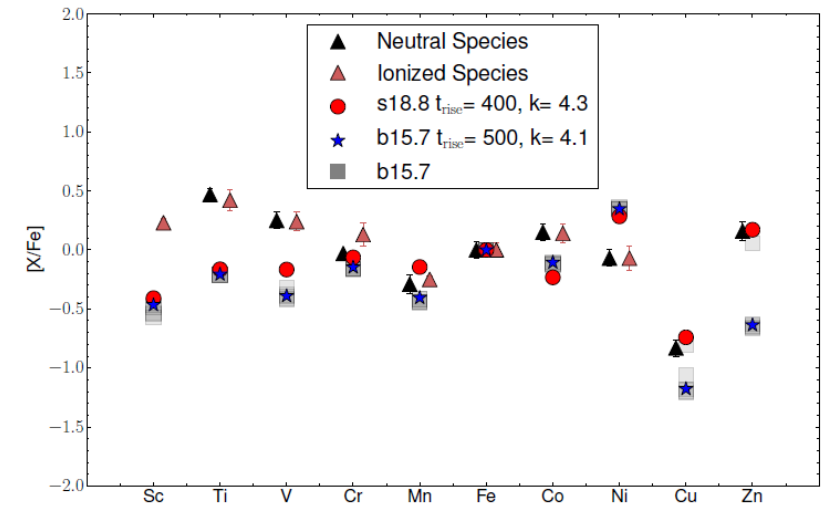
Curtis+19



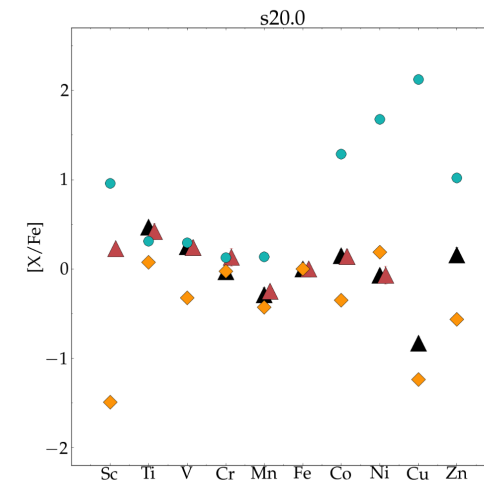
Ebinger, Curtis+20



PUSH (different models for calibration against SN 1987A)



Piston and Thermal Bomb Yields



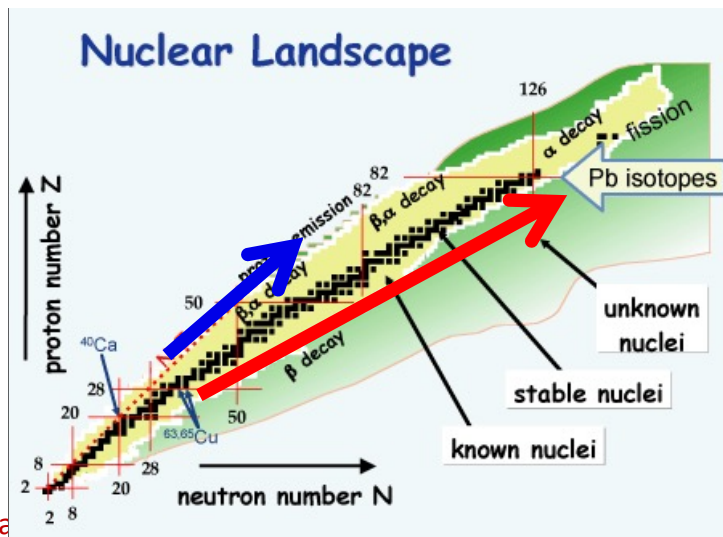
EOS: DD2

Nucleosynthesis Beyond Iron

Note, I ran out of time and did not show the following slides during the lecture.

Neutrino-driven winds

- Strong neutrino flux from PNS
- Drives matter-outflow behind shock wave
- Nucleosynthesis:
 - NSE ($T=10-8\text{GK}$)
 - Charged-particle reactions ($8-2\text{GK}$)
 - r-process and vp-process nucleosynthesis ($3-1\text{GK}$)



Proton-rich conditions:

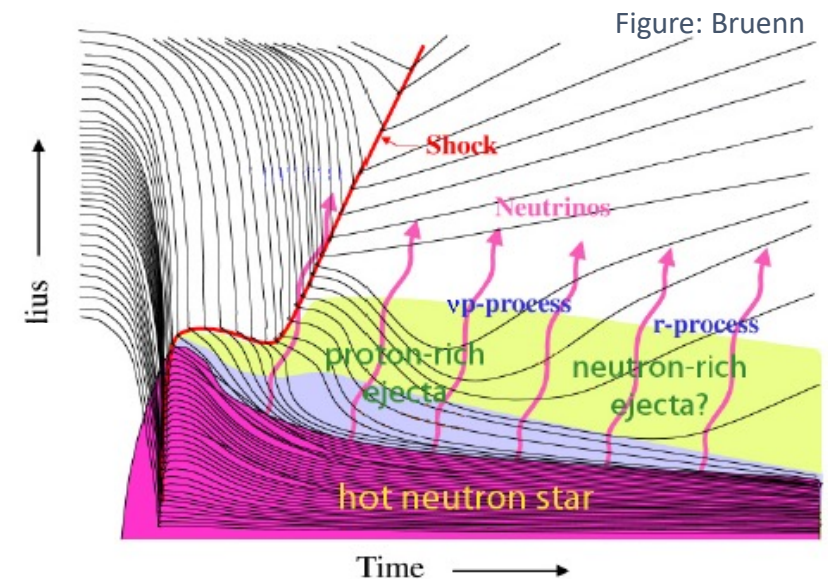
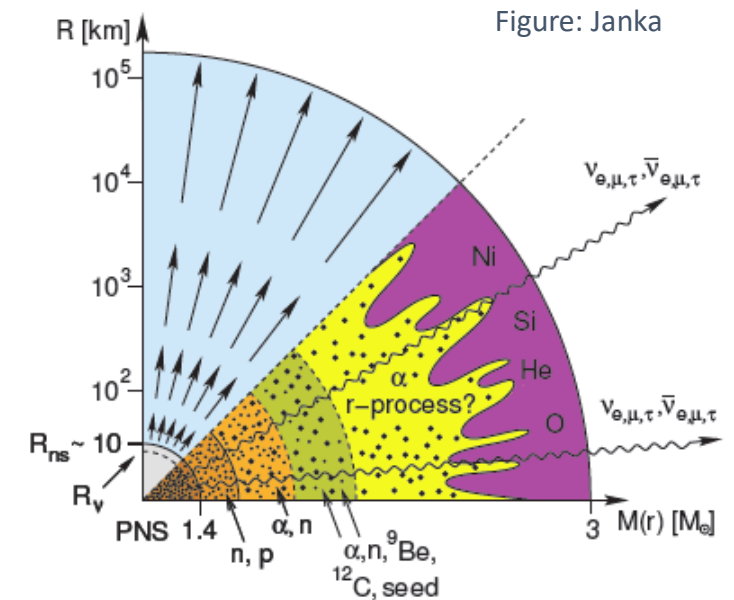
- Elements from Zn to Sn
- (p,γ) and (n,p) reactions

→ vp-process

Neutron-rich conditions:

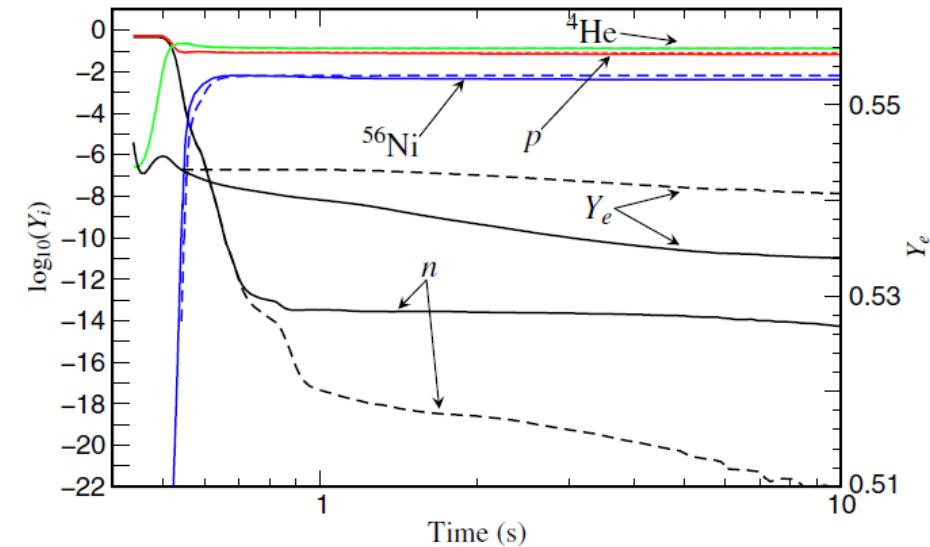
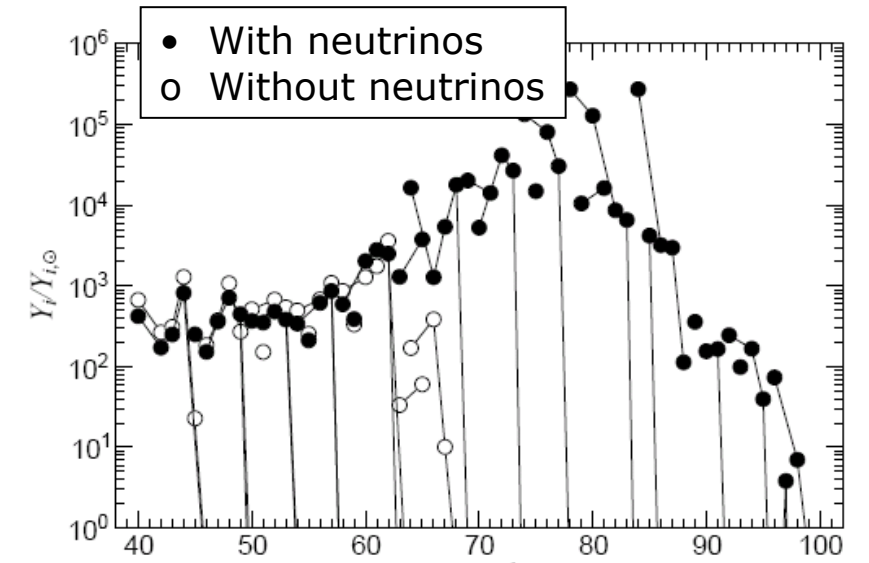
- Elements up to uranium
- (n,γ) reactions and β -decays

→ r-process

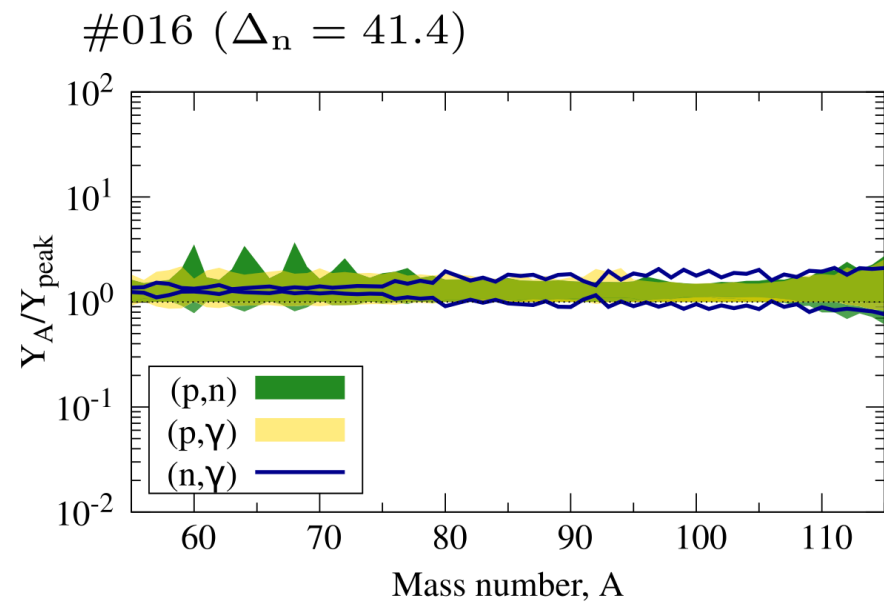
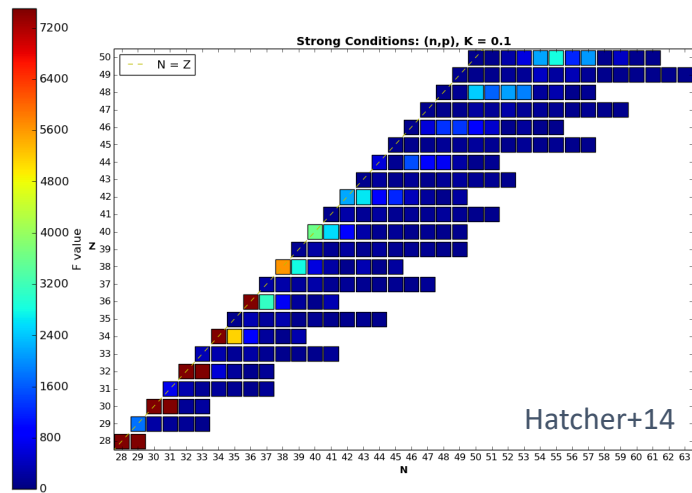
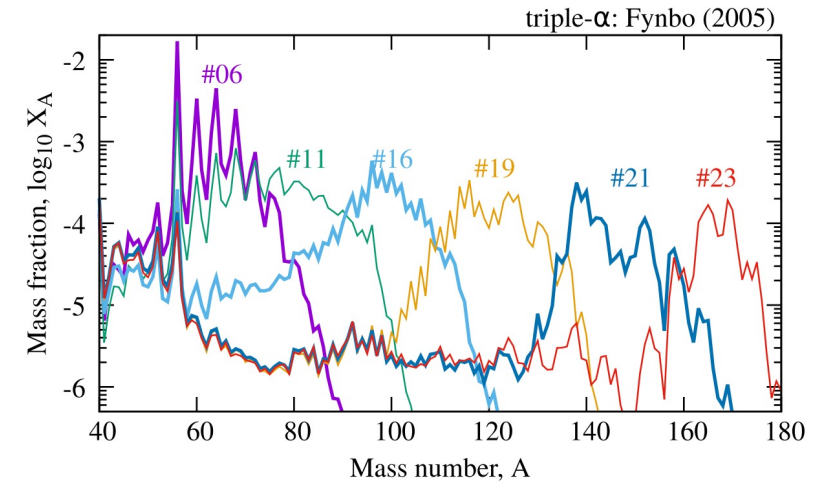
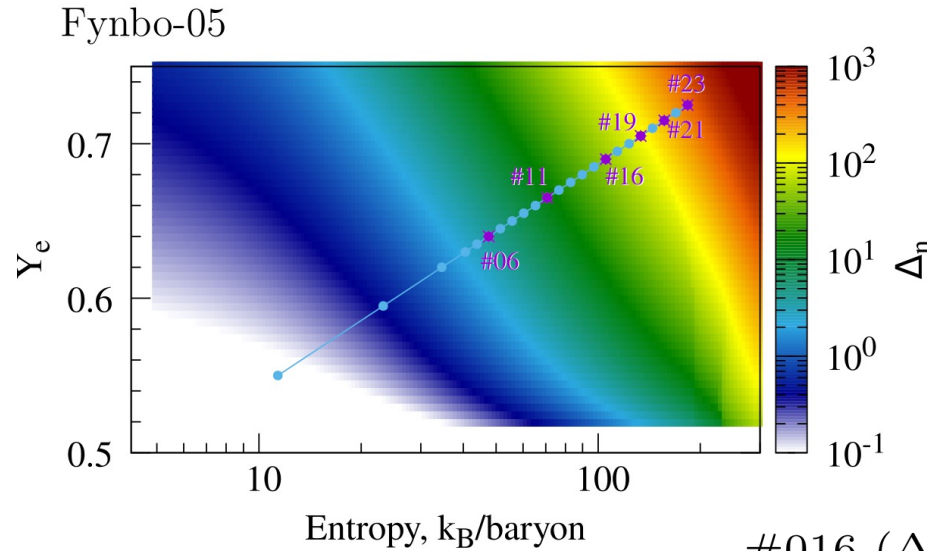
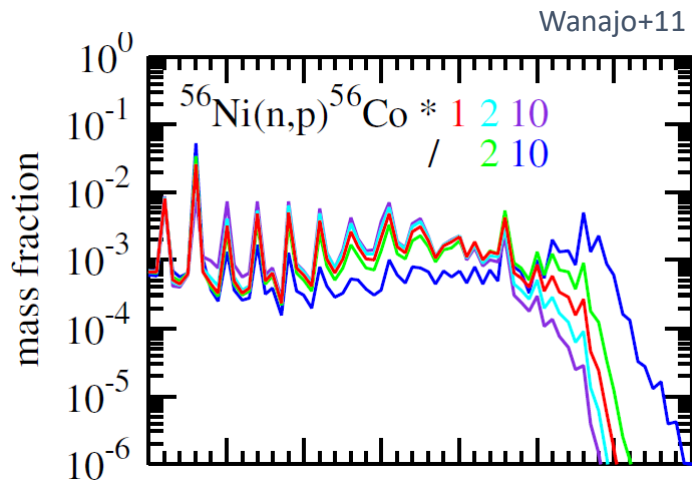


The neutrino-p Process

- proton-rich matter is ejected under the influence of neutrino interactions
- true rp-process is limited by slow β decays, e.g. $\tau(64\text{Ge})$
- Neutron source: $\bar{\nu}_e + p \rightarrow n + e^+$
- Antineutrinos help bridging long waiting points via (n,p) reactions:
 $64\text{Ge} (n,p) 64\text{Ga}; 64\text{Ga} (p,g) 65\text{Ge}$



Sensitivity Studies for the neutrino-p process

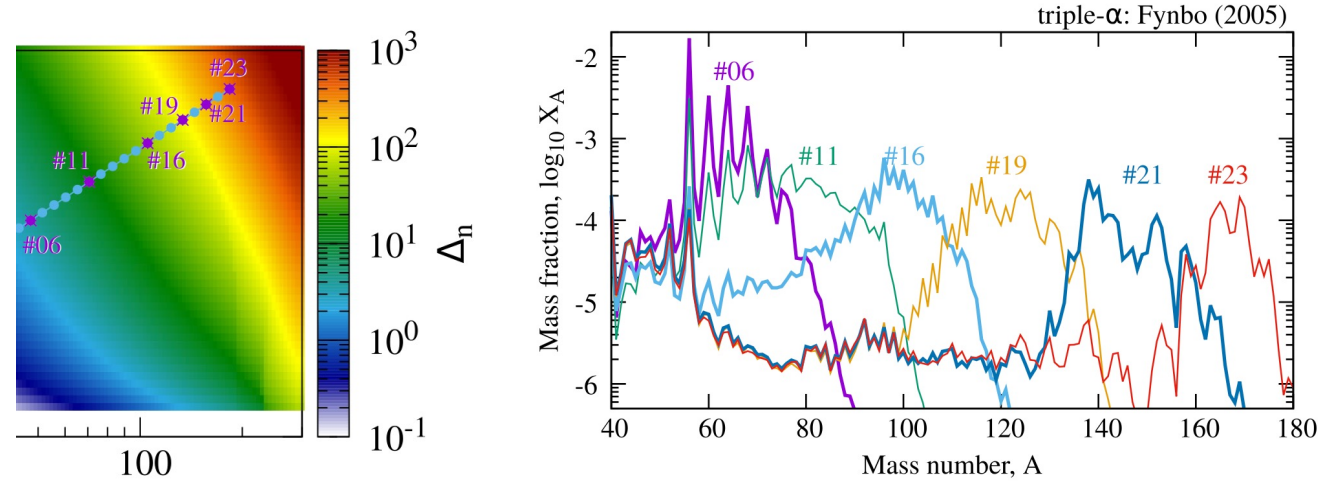


Sensitivity Studies for the neutrino-p process

Nishimura et al.

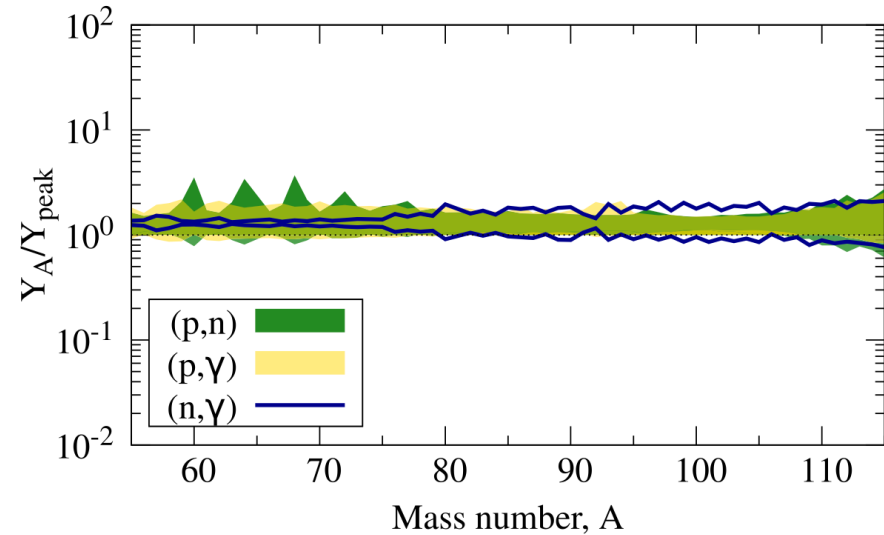
Table 7. Key reaction list sorted by the number of affected nuclides per key rate level and by the counted number of involved trajectories.

Reaction	Level 1	Level 2	Level 3	Number of trajectories
$^{60}\text{Zn}(n,p)^{60}\text{Cu}$	$^{60}\text{Ni}, ^{63}\text{Cu}, ^{64}\text{Zn}$			17
$^{64}\text{Ge}(n,p)^{64}\text{Ga}$	$^{64}\text{Zn}, ^{68}\text{Zn}$			13
$^{68}\text{Se}(n,p)^{68}\text{As}$	^{68}Zn	$^{68}\text{Zn}, ^{69}\text{Ga}, ^{71}\text{Ga}, ^{72}\text{Ge}$	^{69}Ga	16
$^{59}\text{Zn}(n,p)^{59}\text{Cu}$	^{59}Co	$^{60}\text{Ni}, ^{59}\text{Co}$	^{60}Ni	10
$^{63}\text{Ge}(n,p)^{63}\text{Ga}$	^{63}Cu	$^{63}\text{Cu}, ^{64}\text{Zn}$	^{63}Cu	5
$^{72}\text{Kr}(n,p)^{72}\text{Br}$	^{72}Ge	^{72}Ge	$^{72}\text{Ge}, ^{75}\text{As}$	12
$^{57}\text{Ni}(p,\gamma)^{58}\text{Cu}$	^{57}Fe	^{57}Fe	^{57}Fe	13
$^{67}\text{As}(p,\gamma)^{68}\text{Se}$	^{67}Zn	^{67}Zn	^{67}Zn	12
$^{70}\text{Se}(p,\gamma)^{71}\text{Br}$	^{70}Ge	^{70}Ge	^{70}Ge	11
$^{77}\text{Sr}(n,p)^{77}\text{Rb}$	^{77}Se	^{77}Se	^{77}Se	8
$^{75}\text{Sr}(n,p)^{75}\text{Rb}$	^{75}As	^{75}As	^{75}As	7
$^{94}\text{Ru}(p,\gamma)^{95}\text{Rh}$	^{94}Mo	^{94}Mo	^{94}Mo	3
$^{61}\text{Zn}(p,\gamma)^{62}\text{Ga}$	^{61}Ni	^{61}Ni		12
$^{76}\text{Sr}(n,p)^{76}\text{Rb}$	^{76}Se	^{76}Se		7
$^{100}\text{Pd}(n,\gamma)^{101}\text{Pd}$	^{100}Ru	^{100}Ru		2
$^{58}\text{Cu}(p,\gamma)^{59}\text{Zn}$	^{58}Ni		^{58}Ni	12
$^{92}\text{Mo}(p,\gamma)^{93}\text{Tc}$	^{92}Mo			2
$^{97}\text{Rh}(n,\gamma)^{98}\text{Rh}$	^{97}Tc			2
$^{113}\text{In}(n,\gamma)^{114}\text{In}$	^{113}In			1
$^{117}\text{In}(n,\gamma)^{118}\text{In}$	^{117}Sn			1
$^{59}\text{Cu}(p,\gamma)^{60}\text{Zn}$		$^{59}\text{Co}, ^{60}\text{Ni}$	$^{59}\text{Co}, ^{56}\text{Fe}$	11
$^{59}\text{Cu}(p,\alpha)^{56}\text{Ni}$		^{56}Fe	$^{56}\text{Fe}, ^{60}\text{Ni}$	9
$^{57}\text{Ni}(n,p)^{57}\text{Co}$		^{60}Ni	$^{56}\text{Fe}, ^{60}\text{Ni}$	4
$^{62}\text{Zn}(p,\gamma)^{63}\text{Ga}$		^{62}Ni	^{62}Ni	12
$^{60}\text{Cu}(p,\gamma)^{61}\text{Zn}$		^{61}Ni	^{61}Ni	8
$^{71}\text{Br}(p,\gamma)^{72}\text{Kr}$		^{71}Ga	^{71}Ga	7
$^{62}\text{Ga}(p,\gamma)^{63}\text{Ge}$		^{62}Ni	^{62}Ni	6
$^{63}\text{Ga}(p,\gamma)^{64}\text{Ge}$		^{63}Cu	^{63}Cu	6
$^{69}\text{Se}(p,\gamma)^{70}\text{Br}$		^{69}Ga	^{69}Ga	6
$^{74}\text{Kr}(p,\gamma)^{75}\text{Rb}$		^{74}Se	^{74}Se	6
$^{73}\text{Kr}(p,\gamma)^{74}\text{Rb}$		^{73}Ge	^{73}Ge	5



/baryon

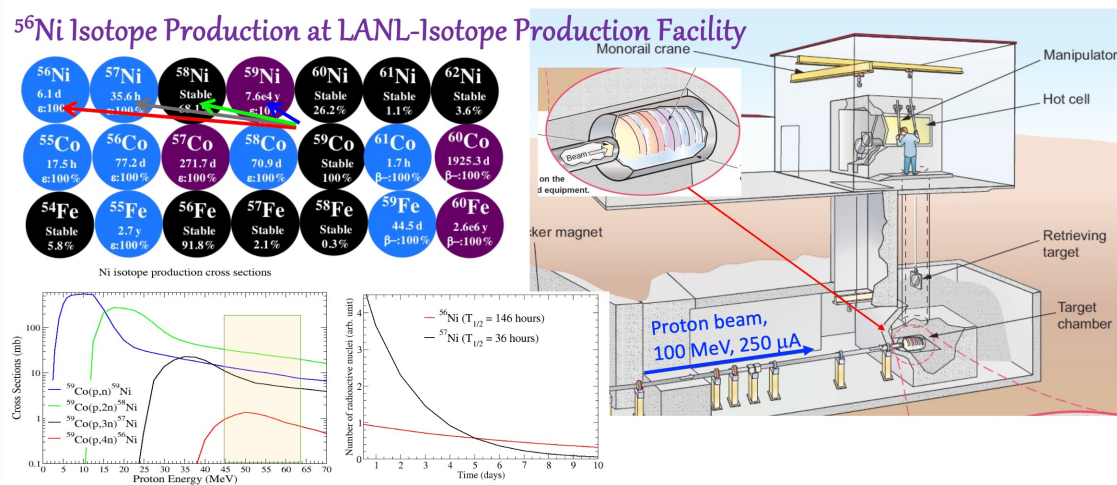
#016 ($\Delta_n = 41.4$)



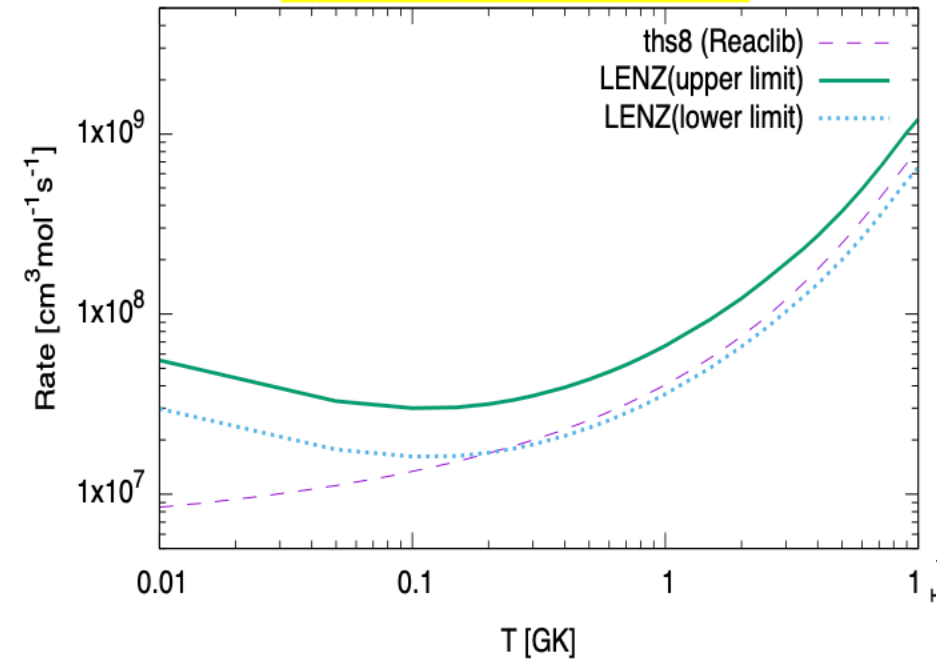
$^{56}\text{Ni}(n,p)^{56}\text{Co}$ and the neutrino p-process

With Hye-Young Lee (LANL)

- Experiment at LANSCE / LANL
- Target production via $^{59}\text{Co}(p,4n)$

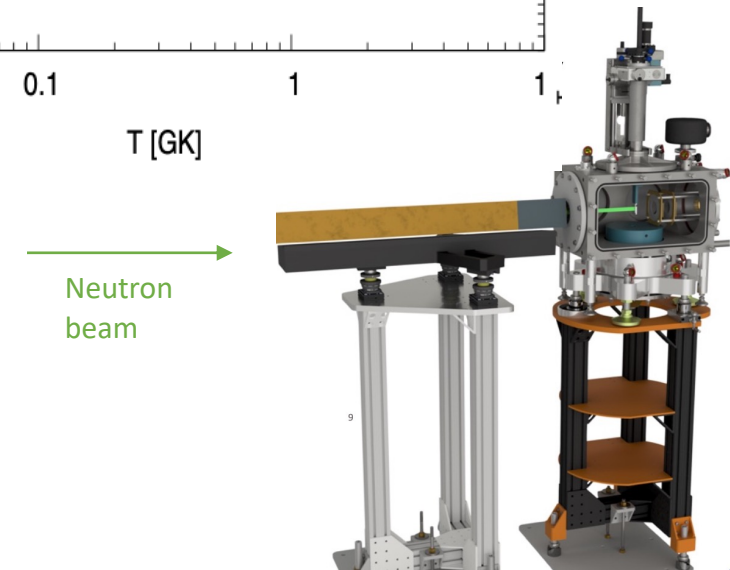
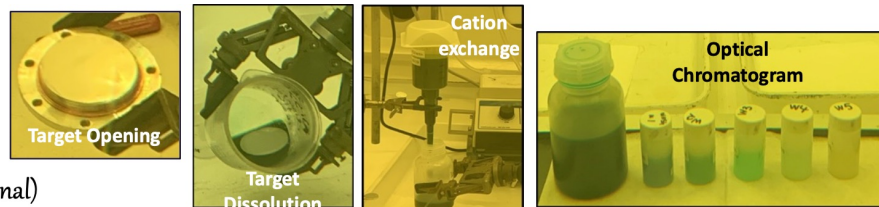


$^{56}\text{Ni}(n,p)$ reaction rate



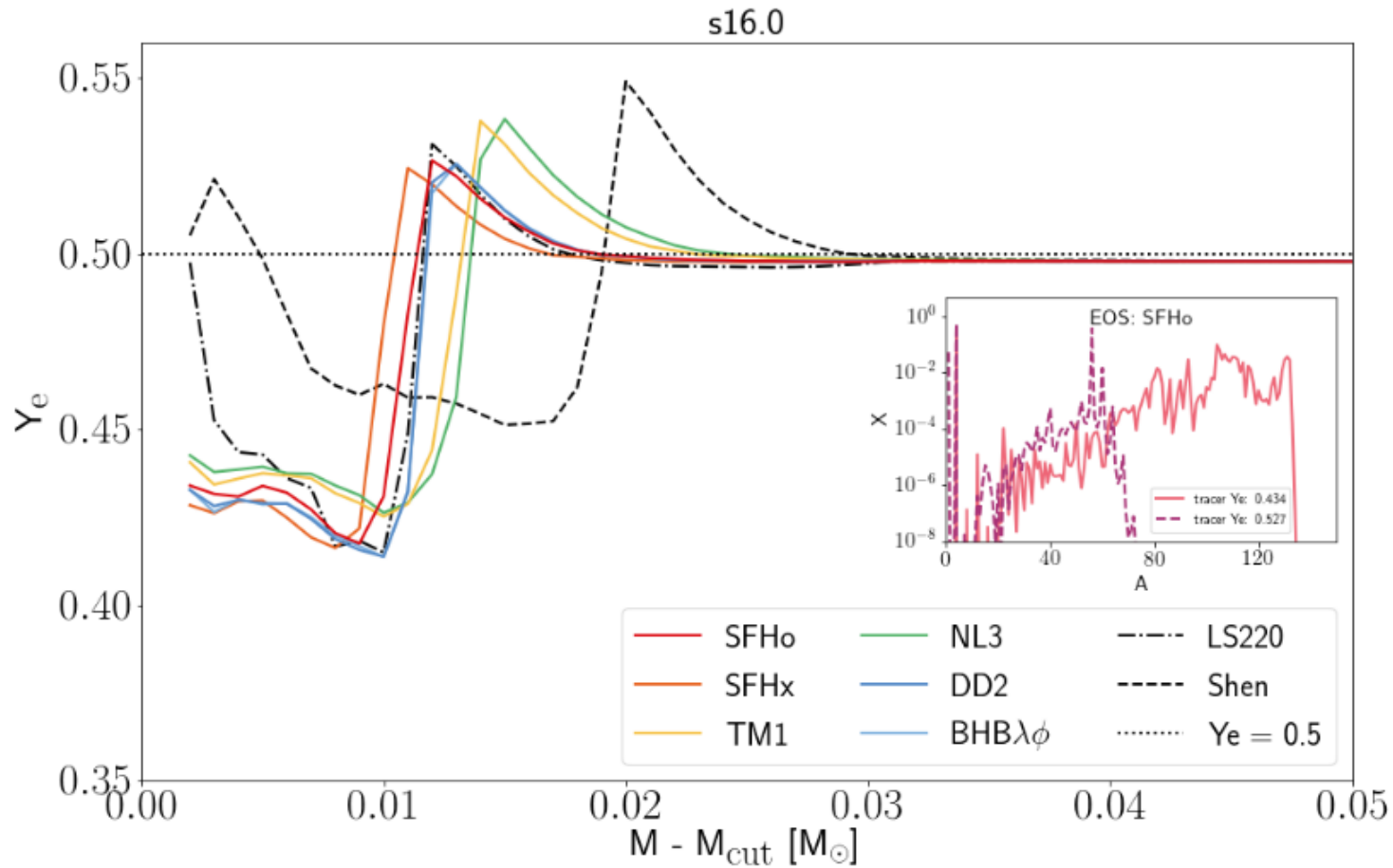
Ni/Co separation and target fabrication

• Improved Ni recovery from 40 % (initial) to 90 % (final)



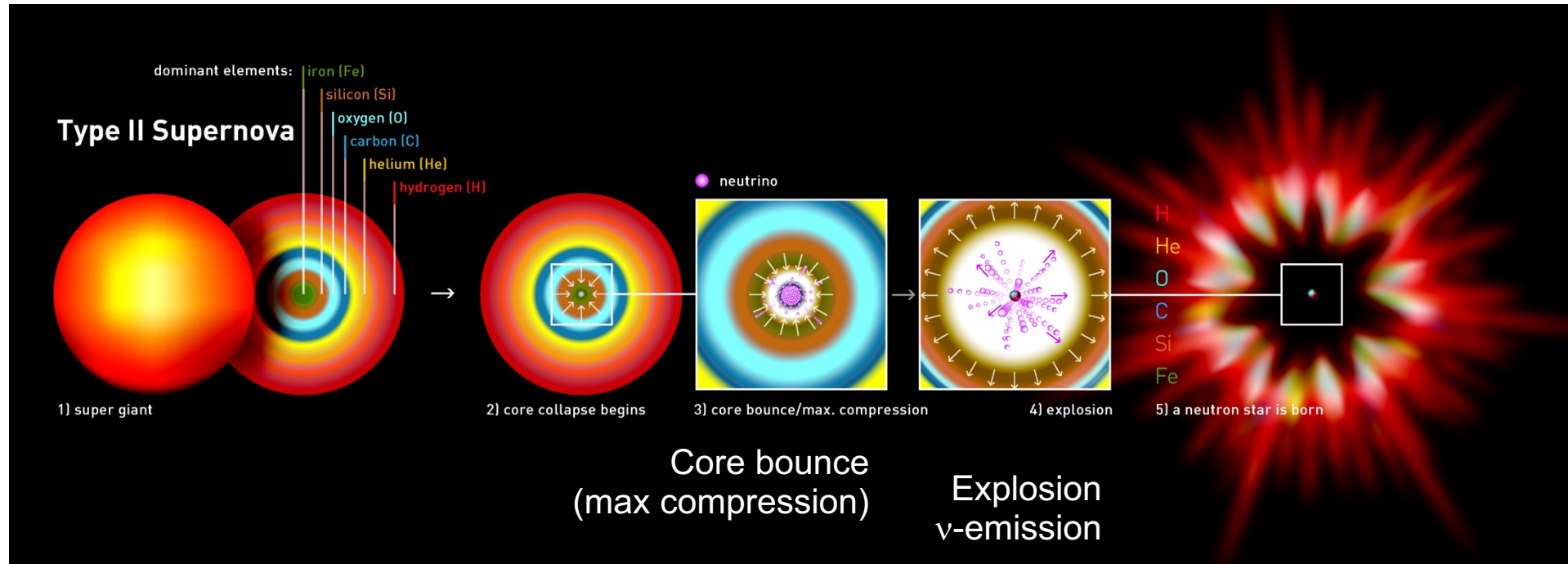
data

Beyond iron: Nuclear EOS matters



Model	EOS	E_{expl} (B)	M_{cut} (M_{\odot})
s16.0	SFHo	1.3650	1.5244
	SFHx	1.2413	1.5300
	TM1	1.4071	1.5293
	NL3	1.4607	1.5263
	DD2	1.2365	1.5372
	BHBλφ	1.2362	1.5372
	LS220	1.4177	1.5183
	Shen	1.5861	1.5142

Summary (so far)

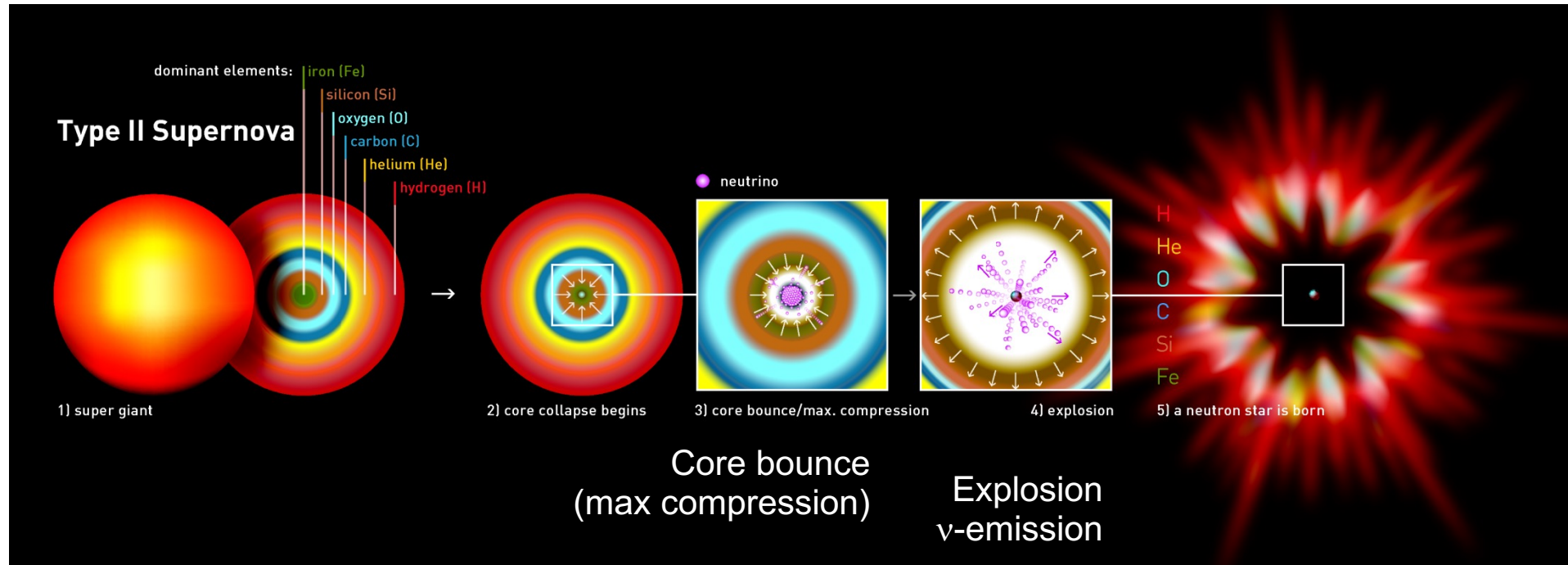


Stellar burning
→ C, O

Explosion mechanism:
Imprint on nucleosynthesis!

Explosive burning
→ Si, S, Ca, Fe, Ni, Zn
vp-process
→ Sr, Y, Zr + Mo, Ru

More CCSN nucleosynthesis



Stellar burning

→ C, O

Weak s-process

→ heavy elements

Explosion mechanism:
Imprint on nucleosynthesis?!

Explosive burning

→ Si, S, Ca, Fe, Ni, Zn

vp-process

→ Sr, Y, Zr + Mo, Ru

r-process ???

γ -process

→ p-nuclides