

# *Multiquark States*

*Elena Santopinto*  
*INFN, Sezione di Genova*

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*Physics Department, Genoa University*

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# Hidden charm and beauty hadrons reveal *tetraquarks* and *pentaquarks*

- Heavy quark pairs are difficult to be created or destroyed by QCD forces inside hadrons.
- Hadrons with a  $c\bar{c}$  or  $b\bar{b}$  pair *and* electrically charged *must* contain additional light quarks, *realising the hypothesis advanced by Gell-Mann in the Sixties*

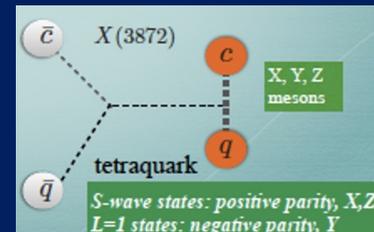
## M. Gell-Mann, A Schematic Model of Baryons and Mesons, PL 8, 214, 1964

- These are the exotic X, Y, Z mesons and the pentaquarks discovered over the last decade

Baryons can now be constructed from quarks by using the combinations  $(qqq)$ ,  $(qqqq\bar{q})$ , etc., while mesons are made out of  $(q\bar{q})$ ,  $(qq\bar{q}\bar{q})$ , etc. It is assuming that the lowest

There are indeed new valence quark configurations !!

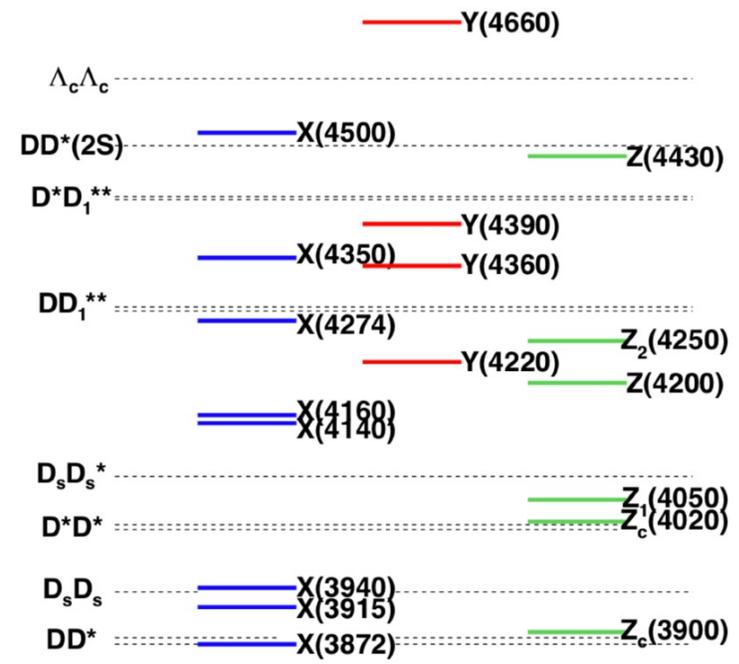
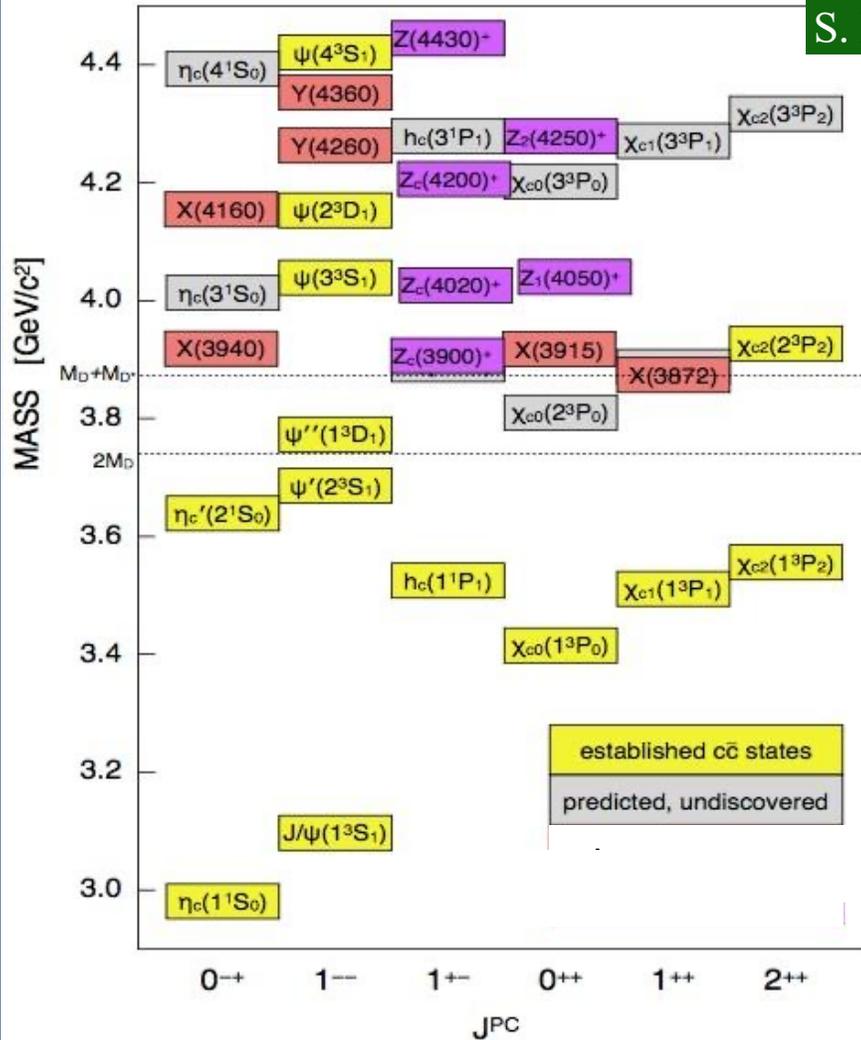
- Tetraquarks are more easy to find at the increase of the quark mass, just as pentaquarks
- The presence of heavy quarks appears to increase the possibility of binding
- Hidden heavy flavors have been the first, now we also have the LHCb open heavy flavor  $X_0(2900) J^P=0^+$  and  $X_1(2900) J^P=1^-$  in the  $D^+ K^-$  channel ( $\bar{c}\bar{s}ud$  or  $D^* K^*$  molecule ?)
  - First *unexpected charmonium* is the still controversial  $X(3872)$  (discovered by Belle 2003)
- Still controversial because very close to the threshold



# Expected and Unexpected Charmonia

figures by:

S. L. Olsen, arXiv:1511.01589, arXiv:1812.10947,



**Figure 4.** XYZ meson masses compared with charmed meson pair thresholds.

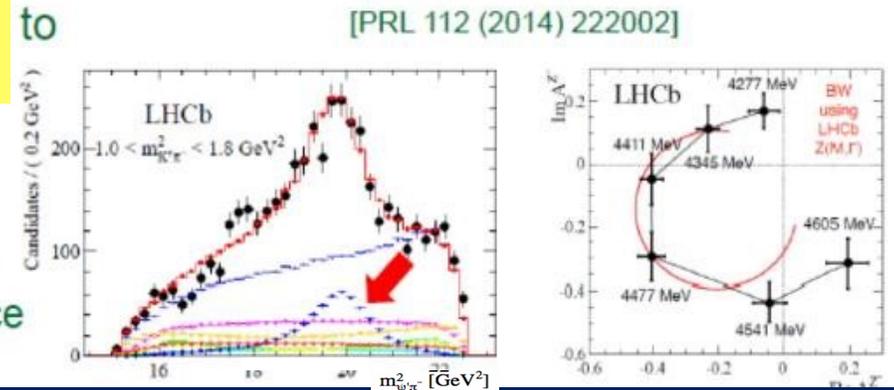
# Explicit Tetraquarks:

$$\mathbf{Z_c(4430)^\pm} \quad 13.9 \sigma$$

$\mathbf{Z_c(4430)^\pm} \rightarrow \Psi' + \pi$  discovered by Belle,  
valence quark composition:  $c\bar{c}u\bar{d}$

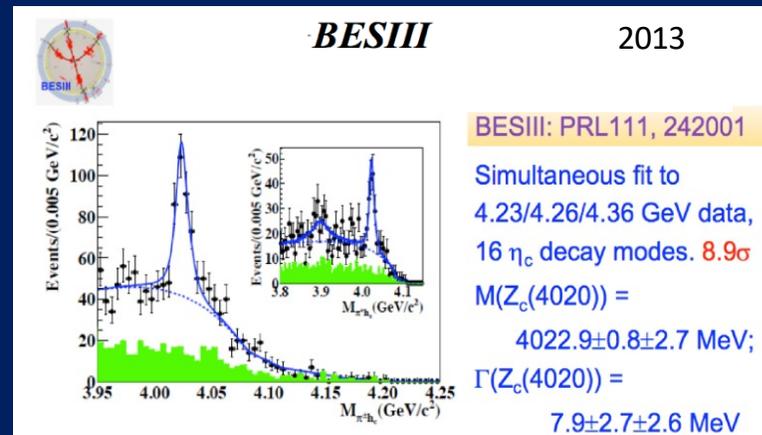
of a four-quark state, the Z(4430).

1. Confirm Belle's observation of 'bump'
2. Can NOT be built from standard states
3. Textbook phase variation of a resonance



"Observation of the resonant character of the Z(4430)<sup>-</sup> state". LHCb, *Physical Review Letters*. **112** (22): 222002(2014).

Argand diagram of Z(4430) is consistent with this structure being a resonance



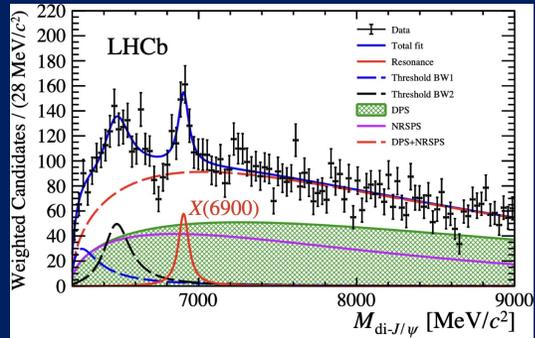
$\mathbf{Z_c(4020)^\pm} \rightarrow h_c + \pi$

$$\mathbf{Z_c(4020)^\pm. 8.9\sigma}$$

# Recent reports of Exotic hadrons!

## $\Delta X(6900) (cccc)$

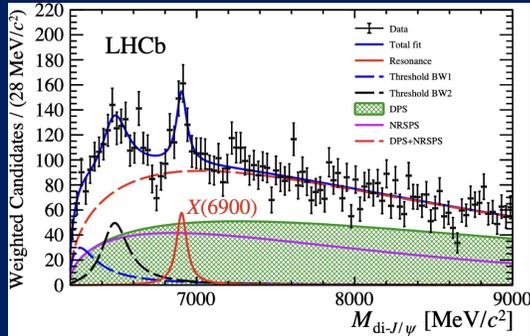
Science Bulletin 65 (2020) 1983



# Recent reports of Exotic hadrons

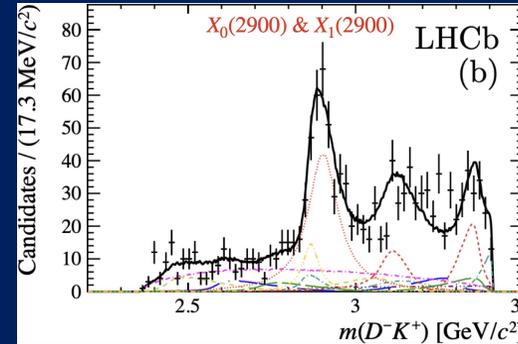
## ▷ $X(6900)$ ( $c\bar{c}c\bar{c}$ )

Science Bulletin 65 (2020) 1983



## ▷ $X_{0,1}(2900)$ ( $\bar{c}sud$ )

LHCb, PRL125, 242001 (2020), Phys. Rev. D 102, 112003 (2020)



3.9 standard deviation  
statistical significance

Amplitude  
analysis of

$$B^+ \rightarrow D^+ D^- K^+$$

$X_{0,1}$  observed in  $D^- K^+$  channel

$$X_0(2900): M = 2.866 \pm 0.007 \pm 0.002 \text{ GeV}/c^2,$$

$$\Gamma = 57 \pm 12 \pm 4 \text{ MeV},$$

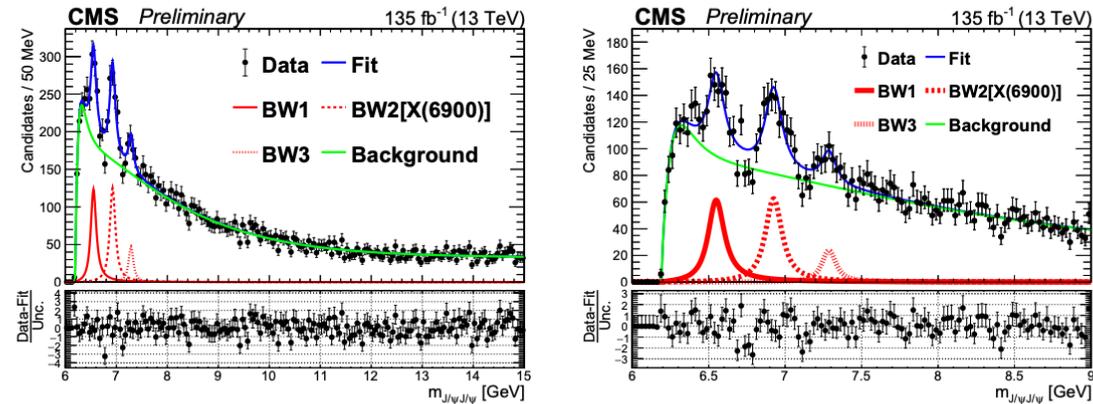
$$X_1(2900): M = 2.904 \pm 0.005 \pm 0.001 \text{ GeV}/c^2,$$

$$\Gamma = 110 \pm 11 \pm 4 \text{ MeV},$$

# ICHEP 2022, July 2022 , X(6600), X(6900) and X(7300)

CMS Collaboration, [Jingqing Zhang et al., 2212.00504 \[hep-ex\]](#), *PoS ICHEP2022 775*

of the three structures are  $6.5\sigma$ ,  $9.4\sigma$ , and  $4.1\sigma$  for X(6600), X(6900) and X(7300), respectively. The measured masses and widths of three structures are summarized in Table 1.



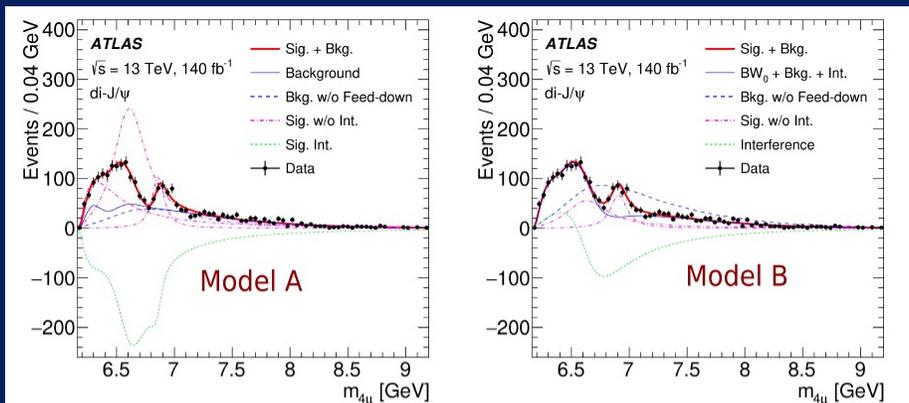
**Figure 3:** The CMS  $J/\psi J/\psi$  mass spectrum with a fit consisting of three signal BW functions and a background model [12]. The left plot shows the fit over the full mass range, and on the right is the same fit expanded by only displaying masses below 9 GeV.

	BW1	BW2	BW3
$m$	$6552 \pm 10 \pm 12$	$6927 \pm 9 \pm 5$	$7287 \pm 19 \pm 5$
$\Gamma$	$124 \pm 29 \pm 34$	$122 \pm 22 \pm 19$	$95 \pm 46 \pm 20$
$N$	$474 \pm 113$	$492 \pm 75$	$156 \pm 56$
	<b><math>6.5\sigma</math></b>	<b><math>9.4\sigma</math></b>	<b><math>4.1\sigma</math></b>

**Table 1:** Summary of the fit results of the CMS  $m(J/\psi J/\psi)$  distribution: the mass  $m$  and natural width  $\Gamma$ , in MeV, and the signal yields  $N$  are given for three signal structures [12]. The first uncertainties are statistical and the second systematic.

# ATLAS Confirmation of the X(6900) ( $>5\sigma$ ) Phys. Rev. Letters 131,151902, 2003)

## Di- $J/\psi$ channel

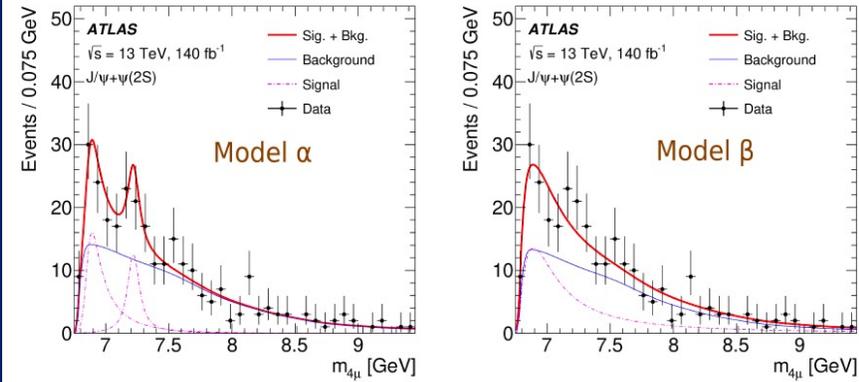


- ▶ Model A: 3 *interfering* BW resonances
- ▶ Model B: 1 BW interfering with SPS background, 1 BW standalone

di- $J/\psi$	model A	model B
$m_0$	$6.41 \pm 0.08^{+0.08}_{-0.03}$	$6.65 \pm 0.02^{+0.03}_{-0.02}$
$\Gamma_0$	$0.59 \pm 0.35^{+0.12}_{-0.20}$	$0.44 \pm 0.05^{+0.06}_{-0.05}$
$m_1$	$6.63 \pm 0.05^{+0.08}_{-0.01}$	—
$\Gamma_1$	$0.35 \pm 0.11^{+0.11}_{-0.04}$	—
$m_2$	$6.86 \pm 0.03^{+0.01}_{-0.02}$	$6.91 \pm 0.01 \pm 0.01$
$\Gamma_2$	$0.11 \pm 0.05^{+0.02}_{-0.01}$	$0.15 \pm 0.03 \pm 0.01$
$\Delta s/s$	$\pm 5.1\%^{+8.1\%}_{-8.9\%}$	—

# $J/\psi + \psi(2S)$ channel in ATLAS

( $< 5 \sigma$ )



- ▶ Model  $\alpha$ : same 3 resonances decaying to  $J/\psi + \psi(2S)$  and a 4th standalone BW resonance –  $4.7\sigma$ 
  - ▶ parameters fixed from di- $J/\psi$  fit
- ▶ Model  $\beta$ : a single BW resonance –  $4.3\sigma$
- ▶  $3\sigma$  significance of the 7.2 GeV resonance in model  $\alpha$

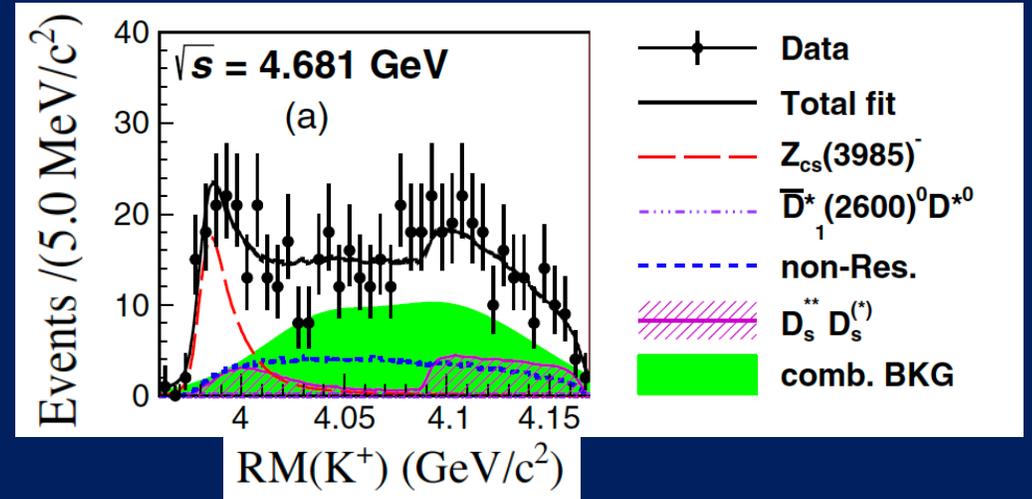
$J/\psi + \psi(2S)$	model $\alpha$	model $\beta$
$m_3$ or $m$	$7.22 \pm 0.03^{+0.01}_{-0.03}$	$6.96 \pm 0.05 \pm 0.03$
$\Gamma_3$ or $\Gamma$	$0.09 \pm 0.06^{+0.06}_{-0.03}$	$0.51 \pm 0.17^{+0.11}_{-0.10}$
$\Delta s/s$	$\pm 21\% \pm 14\%$	$\pm 20\% \pm 12\%$

$Z_{cs}(3985)^-$  ( $c\bar{c}s\bar{u}$ ) (BESIII, Phys. Rev. Lett. 126, 102001 (2021)) (5.3 statistical significance)

Mass and width are respectively

$(3982.5_{-2.6}^{+1.8} \pm 2.1) \text{ MeV}/c^2$  and  $(12.8_{-4.4}^{+5.3} \pm 3.0) \text{ MeV}$

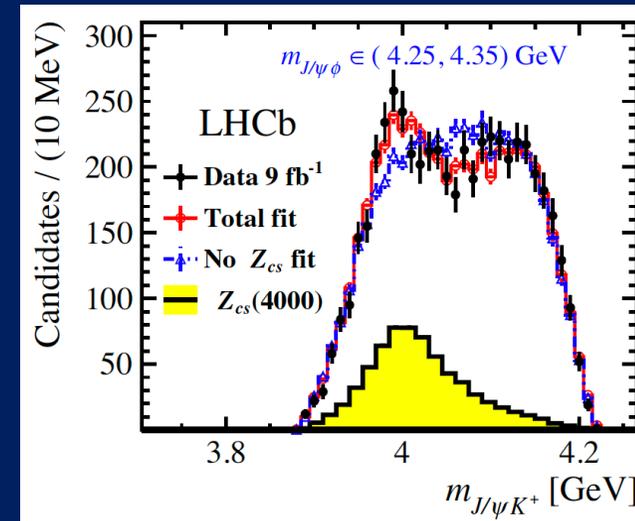
$$e^+e^- \rightarrow (Z_{cs}(3985)^-)K^+ \rightarrow (D_s^- D^{*0} + D_s^{-*} D^0)K^+$$



$Z_{cs}(4003)^+$  ( $c\bar{c}u\bar{s}$ ) (LHCb, Phys. Rev. Lett. 127, 082001 (2021)) (15 statistical significance)

$4003 \pm 6_{-14}^{+4} \text{ MeV}$ , a width of  $131 \pm 15 \pm 26 \text{ MeV}$

$$B^+ \rightarrow (Z_{cs}^+(4003))\phi \rightarrow (J/\Psi K^+) \phi$$



Discovery of the doubly charmed  $T_{cc}^+$  in  $D^0 D^0 \pi^+$  invariant mass distribution with a 22 standard deviations arXiv:2109.01038 (Nature Physics 2022) and arXiv:2109.01056 (Nature Physics Communication 2022).

The minimal quark content for this newly observed state is  $cc\bar{u}\bar{d}$

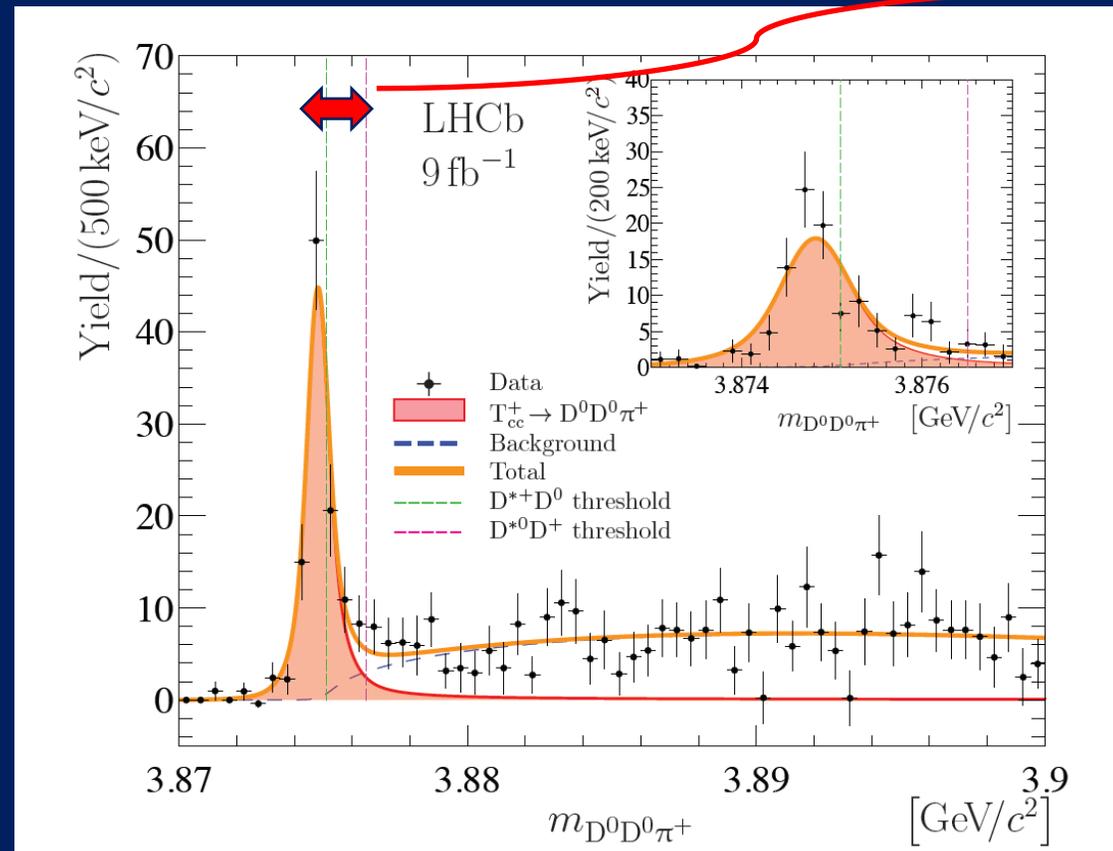
Mass and width

$$M \simeq 3875 \text{ MeV}$$

$$\Gamma \simeq 0.410 \text{ MeV}$$

‘This is the narrowest exotic state observed to date’

‘Moreover, a combination of the near-threshold mass, narrow decay width and its appearance in prompt hadroproduction show its genuine resonance nature. This is the first such exotic resonance ever observed.’ *Nature Physics* volume 18, pages 751–754 (arXiv:2109.01038)



Found to be below the  $D^{*+} D^0$  threshold (with  $4.3\sigma$  significance for “below  $D^{*+} D^0$ ”)

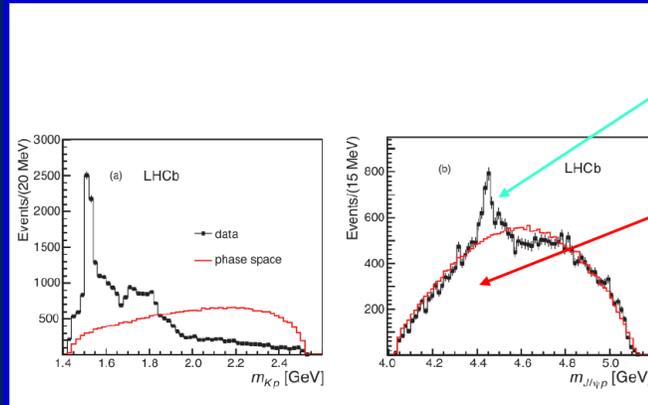
$D^{*+} D^0$  threshold is at 3875.1 MeV

# More new valence quark configurations

$$\Lambda_b \rightarrow K^- + J/\psi + P$$

LHCb

Phys. Rev. Lett. 115(2015) 072001



$$M_{P_c^+}(4450) = (4449.8 \pm 8 \pm 29) \text{ MeV}$$

$$\Gamma = (39 \pm 5 \pm 19) \text{ MeV}$$

$$M_{P_c^+}(4380) = (4380 \pm 1.7 \pm 2.5) \text{ MeV}$$

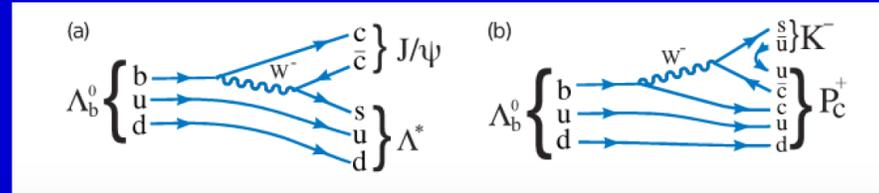
$$\Gamma = (205 \pm 18 \pm 86) \text{ MeV}$$

statistic significance greater than 9 sigma !

$P_c (uudc\bar{c})$

$$\Lambda_b^0 \rightarrow J/\psi + \Lambda^*, \Lambda^* \rightarrow K^- + p$$

$$\Lambda_b^0 \rightarrow P^{0+} + K^-, P^{0+} \rightarrow J/\psi + p$$



The LHCb observation [1] was further supported by another two articles by the same group [2,3]:

[1] R. Aaij *et al.* [LHCb Collaboration], Phys. Rev. Lett. **115** (2015) 072001  
 [2] R. Aaij *et al.* [LHCb Collaboration], Phys. Rev. Lett. **117** (2016) no.8, 082002  
 [3] R. Aaij *et al.* [LHCb Collaboration], Phys. Rev. Lett. **117** (2016) no.8, 082003

# Why pentaquark states?

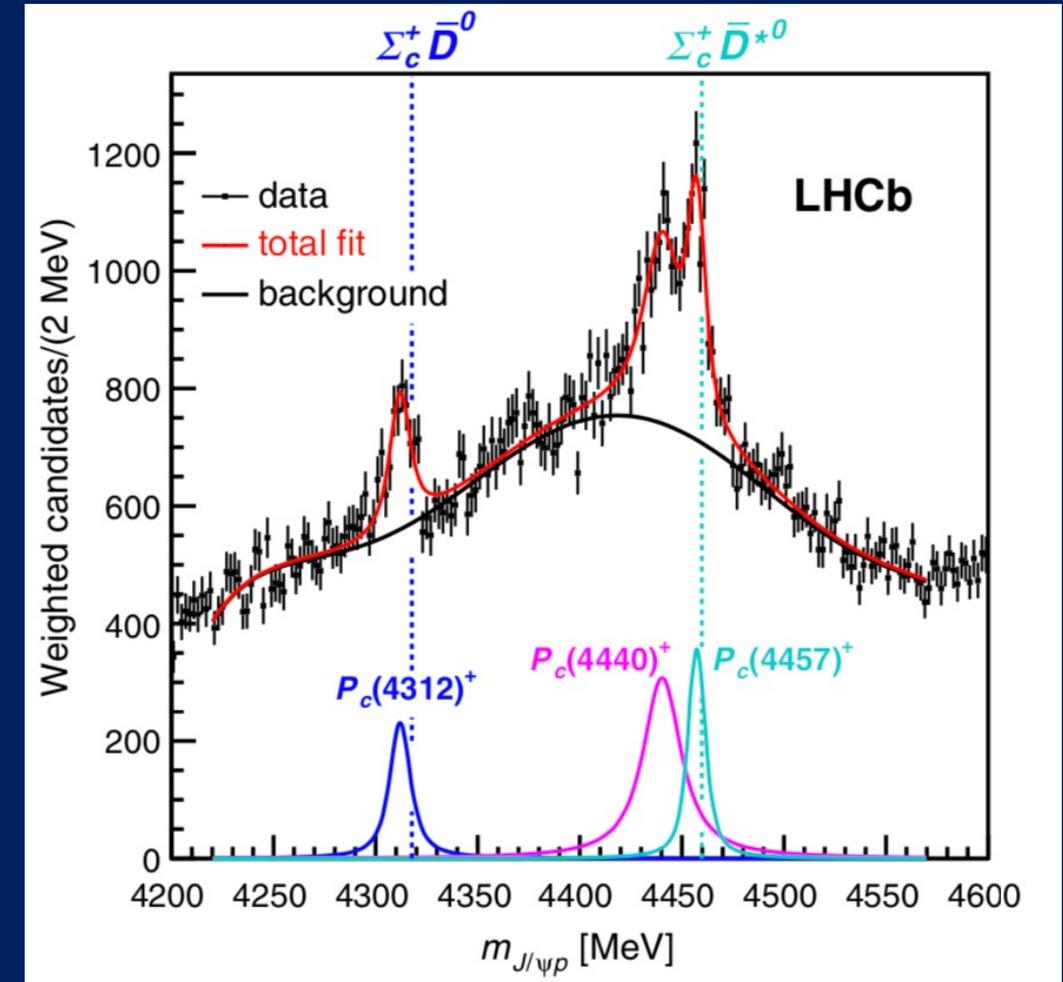
As well as revealing the new  $P_c(4312)$  state with 7.3 sigma statistical significance, the LHCb 2019 analysis also uncovered **a more complex structure of  $P_c(4450)$ , consisting of two narrow nearby separate peaks,  $P_c(4440)$  and  $P_c(4457)$**  with the two-peak structure hypothesis having a statistical significance of 5.4 sigma with respect to the single-peak structure hypothesis.

The masses and widths of the three narrow pentaquark states are as follows

State	$M$ [MeV]	$\Gamma$ [MeV]
$P_c(4312)^+$	$4311.9 \pm 0.7^{+6.8}_{-0.6}$	$9.8 \pm 2.7^{+3.7}_{-4.5}$
$P_c(4440)^+$	$4440.3 \pm 1.3^{+4.1}_{-4.7}$	$20.6 \pm 4.9^{+8.7}_{-10.1}$
$P_c(4457)^+$	$4457.3 \pm 0.6^{+4.1}_{-1.7}$	$6.4 \pm 2.0^{+5.7}_{-1.9}$

[\*] R. Aaij et al. (LHCb), Phys. Rev. Lett. 122, 222001 (2019).

$\Lambda_b^0 \rightarrow J/\Psi p K^-$  channel ( $P_c \rightarrow J/\Psi p$ )



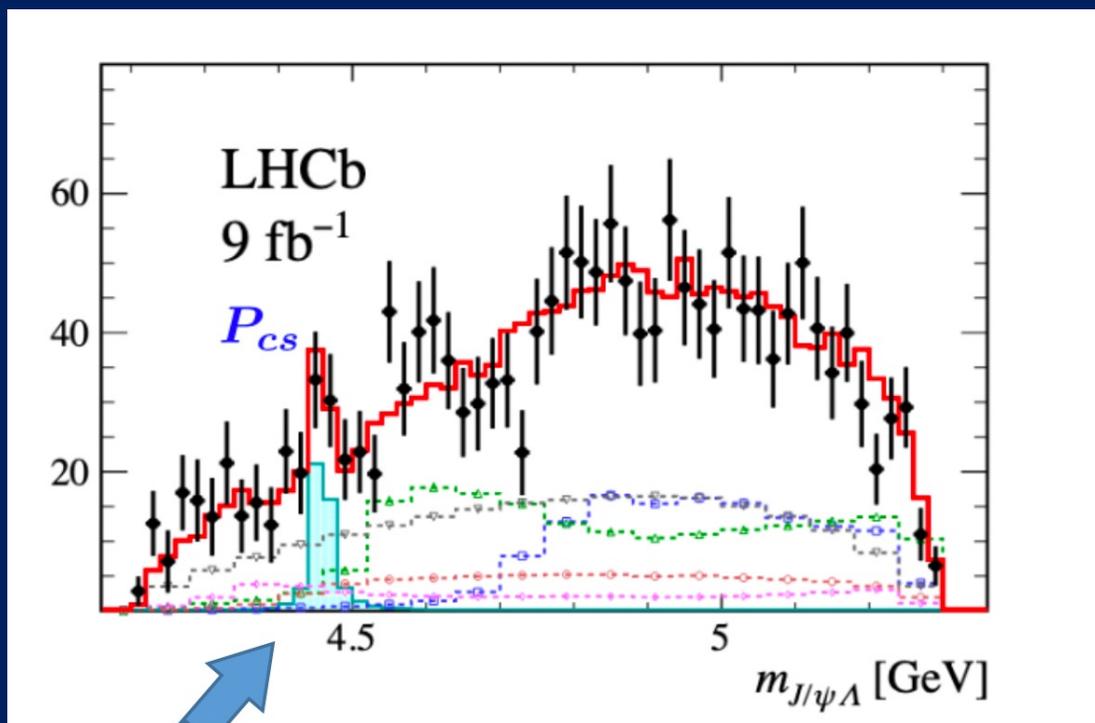
Number of events versus J/Psi p invariant mass [\*]. The mass thresholds for the  $\Sigma_c \bar{D}$  and  $\Sigma_c \bar{D}^*$  final states are superimposed.

# 2020

$\Lambda_b^0 \rightarrow J/\Psi \Lambda K^-$  channel ( $P_{cs} \rightarrow J/\Psi \Lambda$ )

$P_{cs} (udsc\bar{c})(4459)$  LHCb, *Sci.Bull.* 66 (2021) 1278-1287

Significance of  $P_{cs}^0(4459)$  exceeds  $3\sigma$  after considering all the systematic uncertainties.



The mass of  $P_{cs}(4459)$  is about 19 MeV below the  $\Xi_c^0 \bar{D}^{*0}$  threshold

▷ One  $P_{cs}$  state ?

$$M = 4458.8 \pm 2.9_{-1.1}^{+4.7} \text{ MeV}, \Gamma = 17.3 \pm 6.5_{-5.7}^{+8.0} \text{ MeV}$$

(below the  $\Xi_c^0 \bar{D}^{*0}$  threshold)

A good description of the data is provided also with the

▷ Two-peak structure hypothesis

$$M_1 = 4454.9 \pm 2.7 \text{ MeV}, \Gamma_1 = 7.5 \pm 9.7 \text{ MeV}$$

$$M_2 = 4467.8 \pm 3.7 \text{ MeV}, \Gamma_2 = 5.2 \pm 5.3 \text{ MeV}$$

This is similar to the two  $P_c(4440)$  and  $P_c(4457)$  which are just below the  $\Sigma_c^+ \bar{D}^{*0}$  threshold

# August 2021

Evidence for a new structure  
in the  $J/\psi p$  and  $J/\psi \bar{p}$  systems  
in  $B_s^0 \rightarrow J/\psi p \bar{p}$  decays

arXiv:2108.04720v1 [hep-ex] 10 Aug 2021,  
[Phys. Rev. Lett. 128,062001 \(2022\)](#)

$$B_s^0 \rightarrow (P_c^+) \bar{p} \rightarrow (J/\Psi p) \bar{p}$$
$$\bar{B}_s^0 \rightarrow (P_c^-) p \rightarrow (J/\Psi \bar{p}) p$$

$$M_{P_c} = 4337 \begin{matrix} +7 & +2 \\ -4 & -2 \end{matrix} \text{ MeV},$$

$$\Gamma_{P_c} = 29 \begin{matrix} +26 & +14 \\ -12 & -14 \end{matrix} \text{ MeV},$$

The  $P_c(4437)$  statistical significance is in the range of 3.1 to 3.7 depending on the assigned  $J^P$  hypothesis:

3.1 sigma for  $J^P = \frac{1}{2}^+$

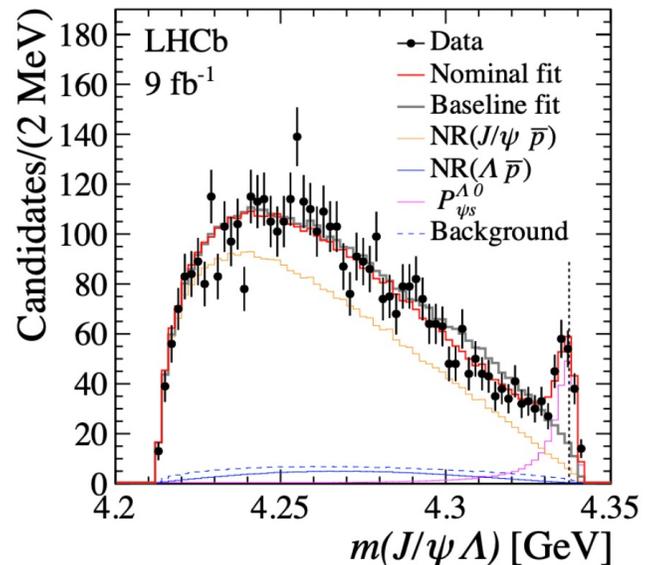
3.7 sigma for  $J^P = \frac{3}{2}^+$

# Pcs(4338) October 2022.

- the Pcs(4338) was announced by LHCb at around  $M = 4338$  MeV in the  $B^- \rightarrow J/\Psi \Lambda \bar{p}$  channel ( $P_{cs} \rightarrow J/\Psi \Lambda$ )

## ► $P_{cs}(4338)$ in 2022

LHCb coll. arXiv:2210.10346



Significance of  $P_{cs}^0(4338)$  exceeds  $10 \sigma$ !

$$M = 4338.2 \pm 0.7 \pm 0.4 \text{ MeV}$$

$$\Gamma = 7.0 \pm 1.2 \pm 1.3 \text{ MeV}$$

(near the  $\Xi_c \bar{D}$  threshold)

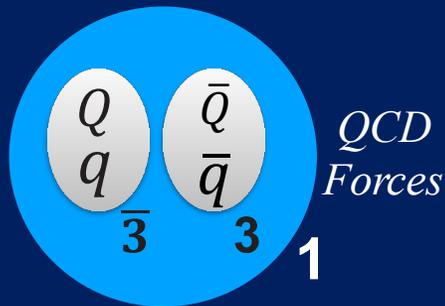
The preferred quantum numbers are  $J^P = 1/2^-$

# No consensus, yet



Hadronic Molecule

F-K. Guo, C. Hanhart, Christoph, U-G Meißner, Q. Wang, Q. Zhao, and B-S Zou, arXiv 1705.00141 (2017)



Compact Diquark-Antidiquark

L. Maiani, F. Piccinini, A. D. Polosa and V. Riquer, Phys. Rev. **D 89** (2014) 114010.

# For pentaquarks

*Nuclear  
Forces*

Hadronic Molecule?

$(\bar{D}\Sigma_c^*, \bar{D}^*\Sigma_c, \dots)$

JaJun Wu, R. Molina, E. Oset, B. S. Zou, PRC84(2011)015202

*QCD  
Forces*

Compact pentaquark

$(5q)$

E. Santopinto, A. Giachino, Phys. Rev. D96 (2017) 014014

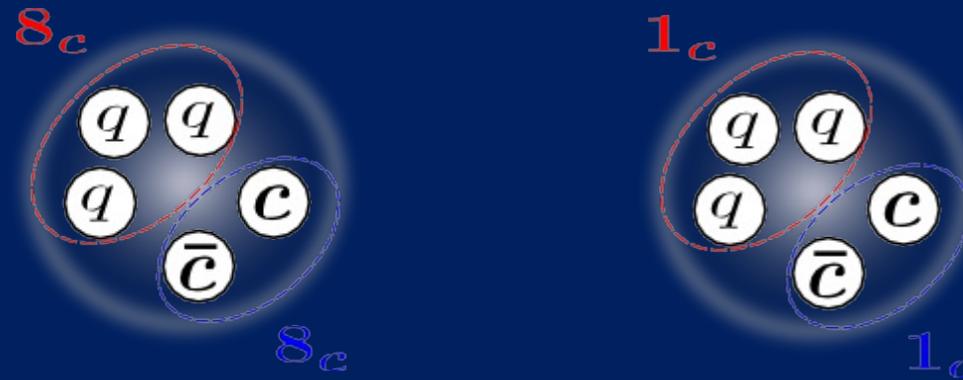
*Nuclear  
Forces* + *QCD  
Forces*

Baryon-meson  
molecule with  
5-quark core

Y. Yamaguchi, A. Giachino, A. Hosaka, E. Santopinto, S. Takeuchi and M. Takizawa, Phys. Rev. D 96, no. 11, 114031 (2017).  
Y. Yamaguchi, H. Garcia-Tecocoatzi, A. Giachino, A. Hosaka, E. Santopinto, S. Takeuchi and M. Takizawa, Phys. Rev. D 101 (2020) no.9, 091502

# Compact $5q$ state

- ▶ E. Santopinto, A. Giachino, **Phys. Rev. D**96 (2017) 014014.  
 $P_c$  states by an algebraic model
- ▶ 5-quark configurations



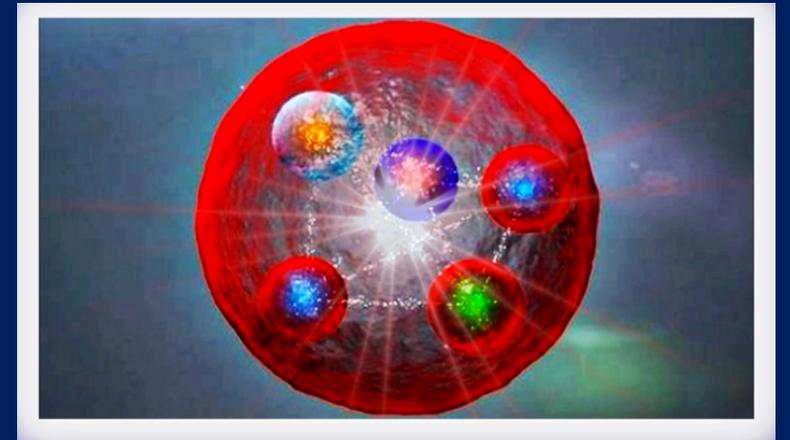
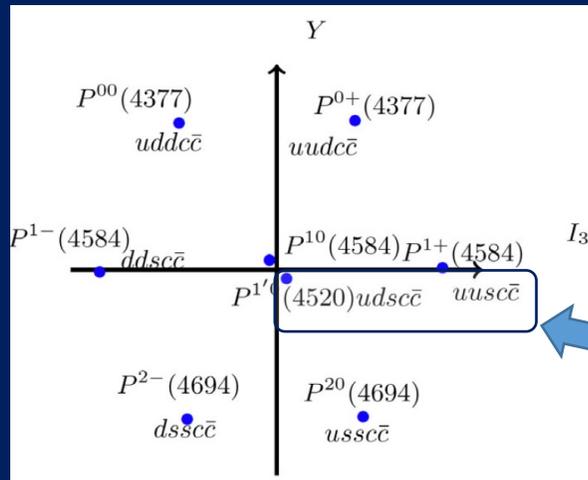
$$S_{q^3} = 1/2, 3/2, S_{c\bar{c}} = 0, 1 \quad S_{q^3} = 1/2, S_{c\bar{c}} = 0, 1$$

Using only symmetry considerations, and an equal spaced mass formula, we have predicted the strange pentaquark with  $I=0$   $P_{cs}(4457)$  for which LHCb reported evidence (LHCb, *Sci.Bull.* 66 (2021) 1278-1287) and suggested to look for it in the  $\Lambda J/\Psi$  channel (in fact cited by LHCb). According to our model also  $I=1$   $P_{cs}$  should exist (in the  $\Sigma J/\Psi$  channel) and  $I=1/2$   $P_{css}$  (in  $\Xi J/\Psi$  channel)

# Compact $5q$ state?

We have predicted the strange pentaquark with  $I=0$ ,  $P_{CS}^0$ , for which LHCb reported evidence at  $M=4459$  MeV and suggested to look for it in the  $\Lambda J/\Psi$  channel. According to our model also  $I=1$   $P_{CS}$  should exist (in the  $\Sigma J/\Psi$  channel) and  $I=1/2$   $P_{CSS}$  (in  $\Xi J/\Psi$  channel).

$$J^P = \frac{3}{2}^-$$

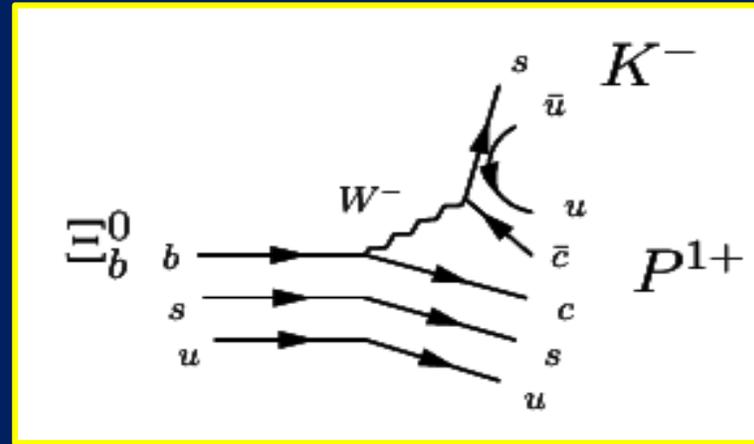
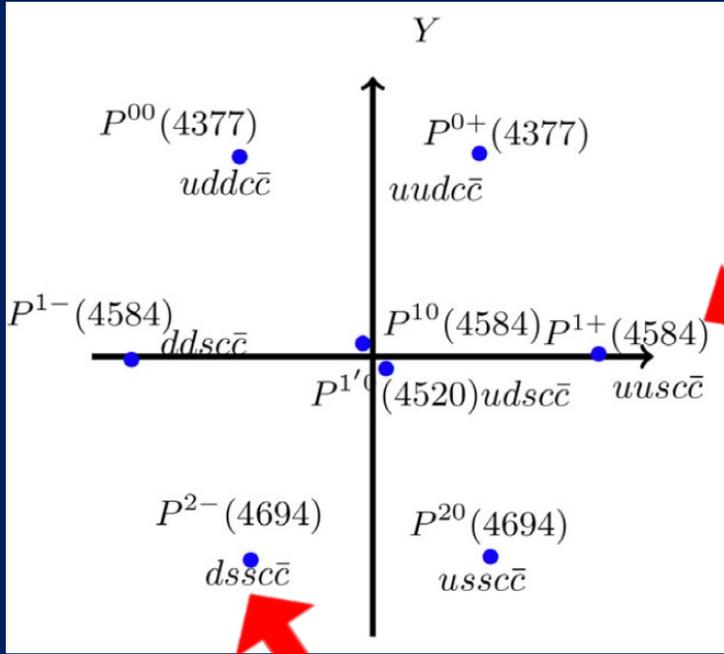


$P_{CS}^0(4459)$  The LHCb Coll. **LHCb, *Sci.Bull.* 66 (2021) 1278-1287,**

Evidence of a  $J/\Psi\Lambda$  structure and observation of excited  $\Xi^-$  states in the  $\Xi_b^- \rightarrow J/\Psi\Lambda K^-$  decay

from E. Santopinto and A. Giachino, **Phys. Rev. D96 (2017) 014014**

In which channels the other hidden charm pentaquarks which fill the SU(3) flavor octet can be observed?

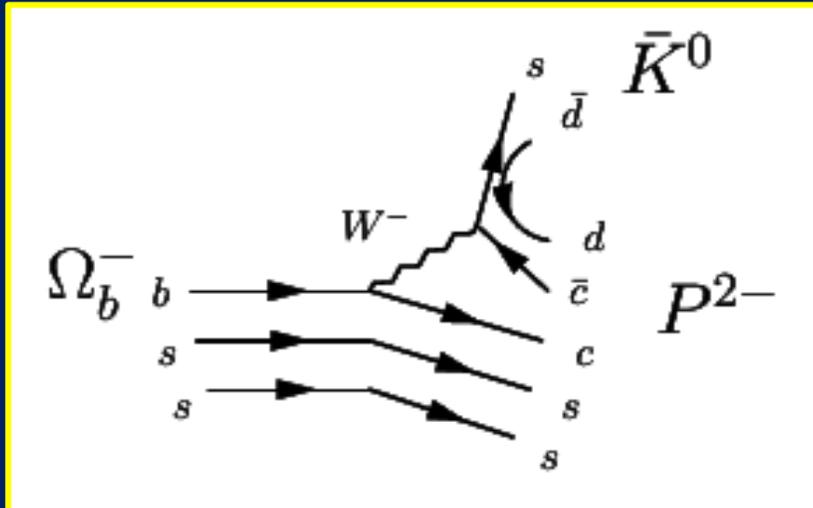


$$\Xi_b^0 \rightarrow P^{1+} + K^-, \quad P^{1+} \rightarrow J/\Psi + \Sigma^+$$

$P^{1+}(4584)$  a  $c\bar{c}uus$  state with isospin 1 so it can be observed in  $J/\Psi\Sigma^+$  invariant mass spectrum; it is important to perform an amplitude analysis of  $\Xi_b^0 \rightarrow J/\Psi\Sigma^+K^-$  decays!

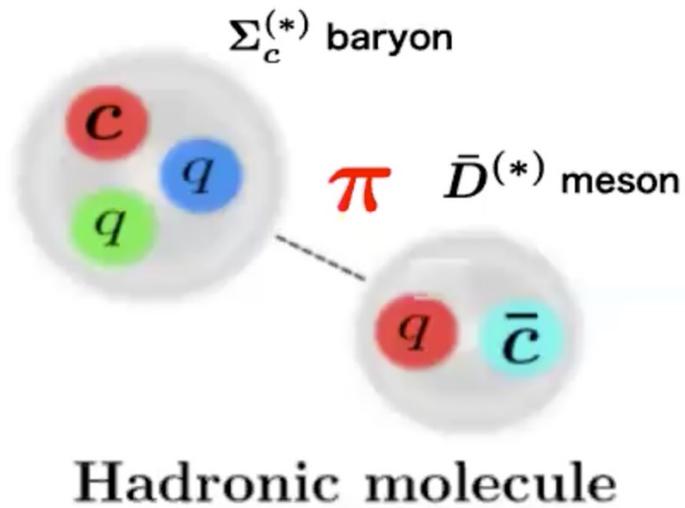
$$\Omega_b^- \rightarrow P^{2-} + \bar{K}^0, \quad P^{2-} \rightarrow J/\Psi + \Xi^-.$$

$P^{2-}(4694)$  a  $c\bar{c}uss$  state with isospin  $\frac{1}{2}$ ; this state can be observed in  $J/\Psi\Xi^-$  invariant mass spectrum after performing an amplitude analysis of  $\Omega_b^- \rightarrow J/\Psi\Xi^-\bar{K}^0$  decays!

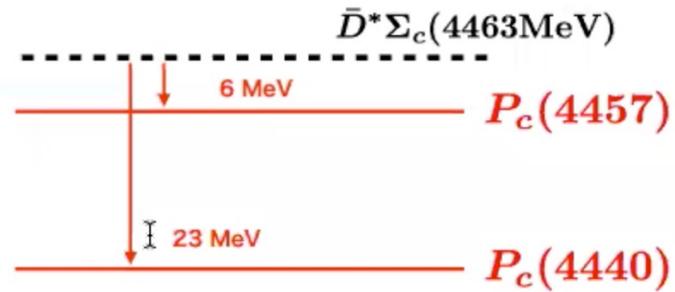


# Hadronic molecules?

- ▶ Exotics as Hadronic molecule  $\Rightarrow$  Hadron (quasi) bound state
- $\rightarrow$  expected **near the thresholds**



$P_c = \bar{D}^{(*)}\Sigma_c^{(*)}$  molecules?



- ▶ Q. Interactions?: **Heavy hadron interactions** are not established yet...
- $\Rightarrow$  Importance of  **$\pi$  exchange** is expected due to the heavy quark symmetry! S. Yasui and K. Sudoh, Phys. Rev. D **80** (2009), 034008
- $\Rightarrow$  Hadronic molecular structure is favored?

Hidden-charm pentaquarks as a meson-baryon molecule with coupled channels  
for  $\bar{D}^{(*)}\Lambda_c$  and  $\bar{D}^{(*)}\Sigma_c^{(*)}$

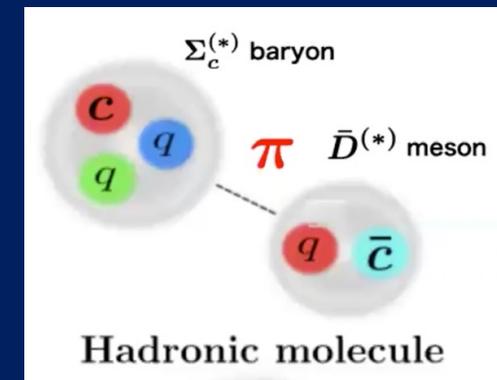
Y. Yamaguchi, E. Santopinto, Phys. Rev. D Phys.Rev. D96 (2017) no.1, 014018

This description is motivated by the fact that the observed pentaquarks are found to be just below the  $\Sigma_c\bar{D}$  threshold ( $P_c(4312)$ ),  $\Sigma_c^*\bar{D}$  ( $P_c(4380)$ ) and  $\Sigma_c\bar{D}^*$  ( $P_c(4440)$  and  $P_c(4457)$ )

Near the threshold, resonances are expected to have an exotic structure, like the hadronic molecules



In Phys.Rev. D96 (2017) no.1, 014018 E. Santopinto e Y. Yamaguchi considered the coupled channel systems of  $\bar{D}\Lambda_c$ ,  $\bar{D}^*\Lambda_c$ ,  $\bar{D}\Sigma_c$ ,  $\bar{D}\Sigma_c^*$ ,  $\bar{D}^*\Sigma_c$  and  $\bar{D}^*\Sigma_c^*$  to predict the bound and the resonant states in the hidden-charm sector. **The binding interaction between the meson and the baryon is given by the One Meson Exchange Potential (OMEP).**



This is similar to the work by Wu et al. [\*] but it is based on SU(3) flavor symmetry

# Upgrade of the model: Coupled channel between the meson-baryon states and the five quark states

Hidden-charm and bottom meson-baryon molecules coupled with five-quark states, Y. Yamaguchi, A. G., A. Hosaka, E. Santopinto, S. Tacheuchi, M. Takizawa, Phys .Rev. D96 (2017) no.11, 114031

## Model setup in this study

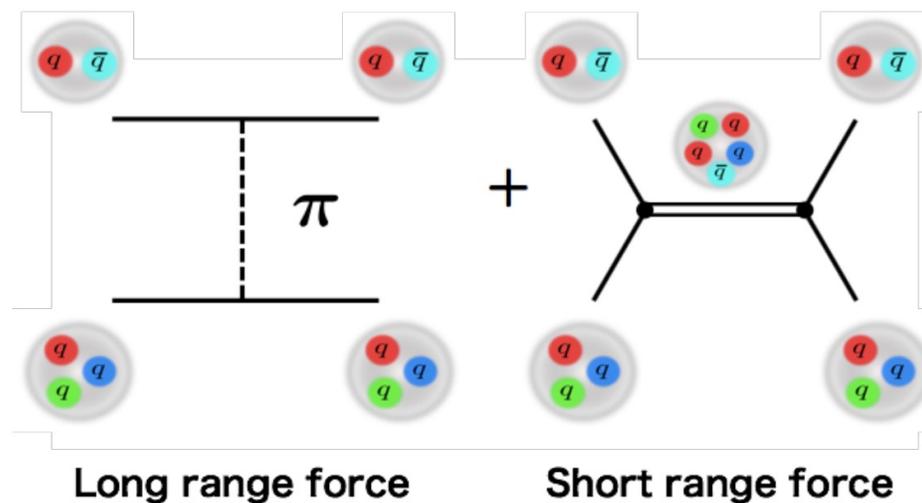
- ▶ **Hadronic molecule + Compact state ( $5q$ )**  
⇒ Meson-Baryon couples to  $5q$  (Fashbach projection)
- ▶ **Long range** interaction: One pion exchange potential (OPEP)
- ▶ **Short range** interaction:  $5q$  potential

Meson-baryon interactions are obtained from the EFFECTIVE LAGRANGIANS satisfying the heavy quark and chiral symmetries

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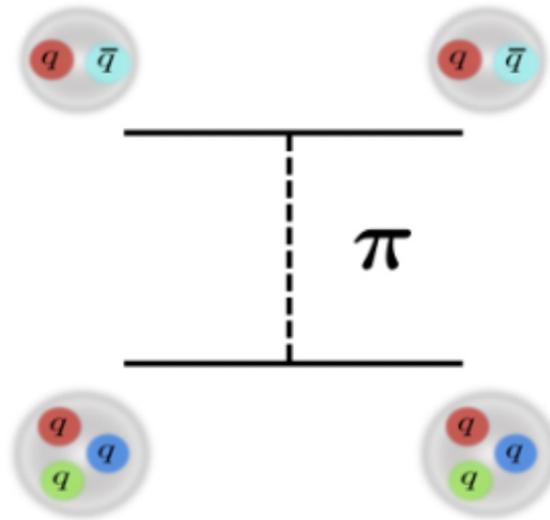
### Meson-Baryon interactions



- ▶ **Long range** interaction: One pion exchange potential (OPEP)
- ▶ **Short range** interaction:  $5q$  potential

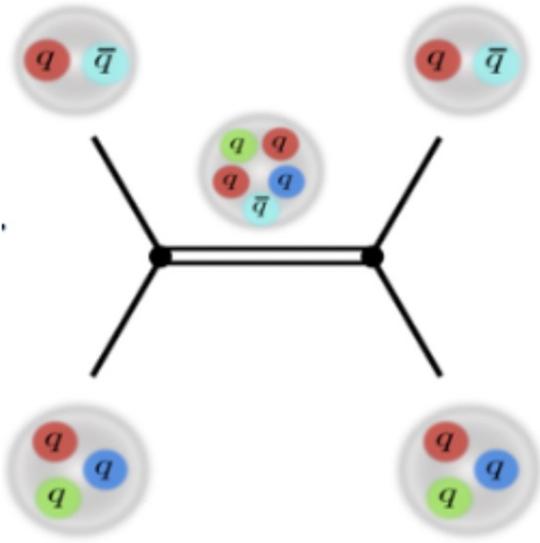
Meson-baryon interactions are obtained from the EFFECTIVE LAGRANGIANS satisfying the heavy quark and chiral symmetries  
(see next slides)

# 1. Long range force: One pion exchange potential



Long range force

## 2. Short range force: 5-quark potential



Short range force

# EFFECTIVE LAGRANGIANS

Coupling between the heavy mesons and the light pseudoscalar mesons [1]:

In Dirac space

$$A_\mu = \frac{i}{2} (\xi^\dagger \partial_\mu \xi - \xi \partial_\mu \xi^\dagger),$$

Definition of the axial current

$$\mathcal{L}_{psHH} = g_\pi \text{Tr}[H_b \gamma_\mu \gamma_5 A_{ba}^\mu \bar{H}_a],$$

$$H_a = \frac{1 + \not{v}}{2} [P_{a\mu}^* \gamma^\mu - P_a \gamma_5], \quad \bar{H}_a = \gamma_0 H_a^\dagger \gamma_0,$$

$$\xi = e^{\frac{iM}{2f_\pi}}, \quad f_\pi = 92.3 \text{ MeV}$$

M is the traceless 3 × 3 Hermitian matrix of the pseudoscalar mesons

$$\mathcal{M} = \sqrt{2} \begin{pmatrix} \frac{\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{6}} & \pi^+ & K^+ \\ \pi^- & -\frac{\pi^0}{\sqrt{2}} + \frac{\eta}{\sqrt{6}} & K^0 \\ K^- & \bar{K}^0 & -\frac{2}{\sqrt{6}}\eta \end{pmatrix}$$

Static limit approximation (= non relativistic limit)  
 $v_\mu \rightarrow (1,0,0,0)$

$$\begin{aligned} \langle 0 | P | Q \bar{q}(0^-) \rangle &= \sqrt{M_H} \\ \langle 0 | P^{*\mu} | Q \bar{q}(1^-) \rangle &= \epsilon^\mu \sqrt{M_H} \end{aligned}$$

The coupling constant  $g_\pi$  is determined by the strong decay of  $D^* \rightarrow D\pi$

[1] R. Casalbuoni, A. Deandrea, N. Di Bartolomeo, R. Gatto, F. Feruglio and G. Nardulli, Phys. Rept. **281**, 145 (1997) doi:10.1016/S0370-1573(96)00027-0 [hep-ph/9605342].

## Hidden-charm and bottom meson-baryon molecules coupled with five-quark states [3]

- In Refs. [3] we studied the hidden-charm pentaquarks by coupling the  $\Lambda_c \bar{D}^{(*)}$  and  $\Sigma_c^* \bar{D}^{(*)}$  meson-baryon channels to a  $uudc\bar{c}$  compact core with a meson-baryon binding interaction satisfying the heavy quark and chiral symmetries.

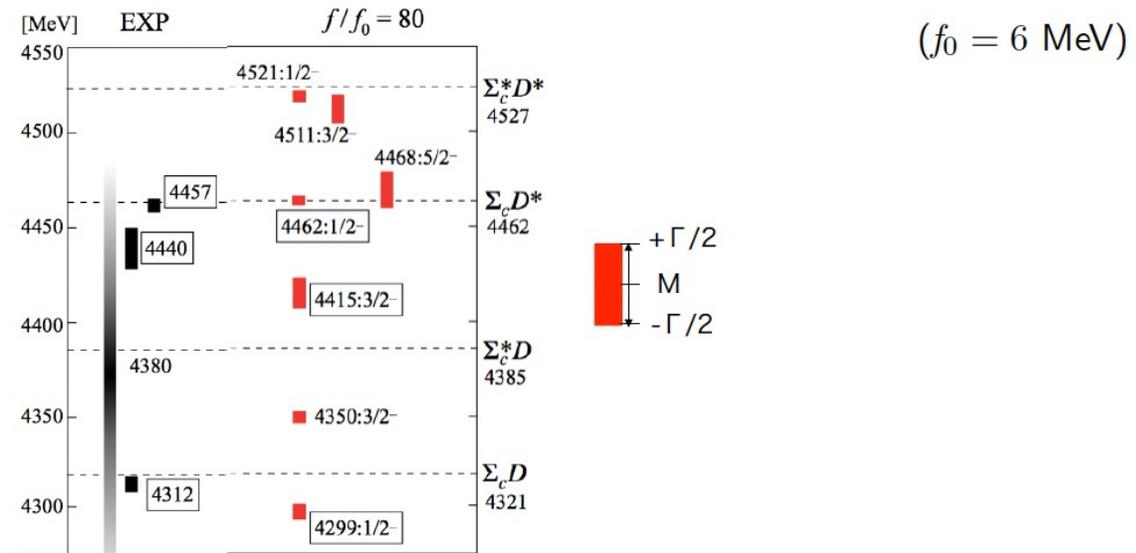
We predicted the three pentaquark states,  $P_c(4312)$ ,  $P_c(4440)$  and  $P_c(4457)$  two years before the experimental observation by LHCb.

For this reason we wrote a Rapid Communication, Y. Yamaguchi, H. Garcia-Tecocoatzi, A. Giachino, A. Hosaka, E. Santopinto, S. Takeuchi and M. Takizawa Phys.Rev.D **101** (2020) 091502 (R)

[3] Y. Yamaguchi, A. Giachino, A. Hosaka, E. Santopinto, S. Takeuchi, M. Takizawa, Phys. Rev. D **96** 114031 (2017)

# For New $P_c$ states by LHCb in 2019

Y.Y., H.Garcia-Tecocoatzi, A.Giachino, A.Hosaka, E.Santopinto, S.Takeuchi, M.Takizawa, PRD **101** (2020) 091502(R)





Very recently the LHCb Collaboration announced the observation of a new strange pentaquark

$$P_{cs}(4338) [*]$$

significance  $> 10 \sigma$

$$M_{P_{cs}} = 4338.2 \pm 0.7 \pm 0.4 \text{ MeV}$$

$$\Gamma_{P_{cs}} = 7.0 \pm 1.2 \pm 1.3 \text{ MeV}$$

$\Rightarrow$  Spin-parity:

$J = \frac{1}{2}$  determined

$P = -1$  favored,  $\frac{1}{2}^+$  rejected @90% CL

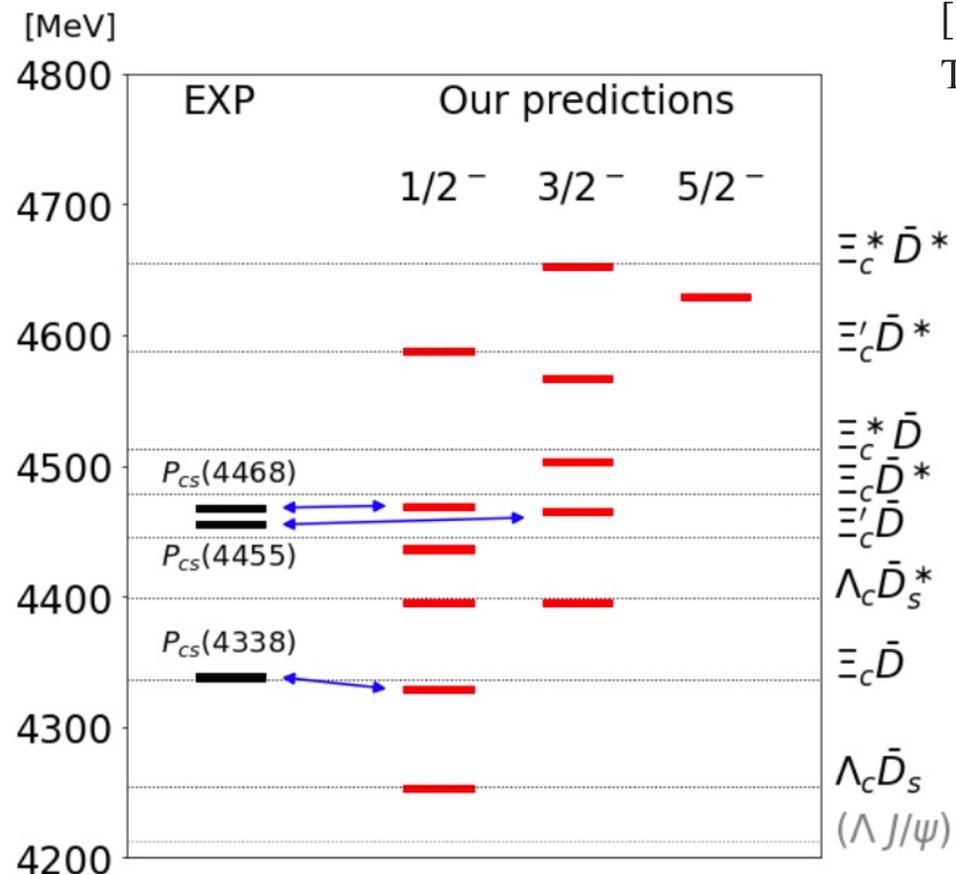
This new state has been observed in the  $B^- \rightarrow J/\Psi \Lambda \bar{p}$  decay process as a resonance in  $J/\Psi \Lambda$  invariant mass (minimal quark content  $c\bar{c}uds$ ) with a statistical significance  $> 10$  standard deviations [\*]

[\*] Aaij et al. (LHCb collaboration), arXiv:2210.10346, Phys. Rev. Lett. **131**, 031901 – Published 17 July 2023

In [1] we constructed a coupled-channel model for the hidden-charm pentaquarks with strangeness whose quark content is  $udsc\bar{c}$ ,  $P_{cs}$ , described as  $\Lambda_c \bar{D}_s^{(*)}$ ,  $\Xi_c^{(',*)} \bar{D}^{(*)}$  molecules coupled to the five-quark states. The meson baryon interactions satisfy heavy quark and chiral symmetries.

We reproduce the experimental mass and quantum numbers  $J^P$  of  $P_{cs}(4338)$  for which LHCb has just announced the discovery. We make other predictions for new  $P_{cs}$  states as molecular states near threshold regions that can be studied by LHCb.

## Comparing EXP with the predicted masses



[1] A.Giachino, A. Hosaka, E. Santopinto, S. Takeuchi, M. Takizawa, Y. Yamaguchi, Phys. Rev. D 108, 074012 (2023)

Consistence with the two-peak structure hypothesis by LHCb,  $P_{cs}(4468)$  and  $P_{cs}(4455)$

**Thanks for your  
attention!**

