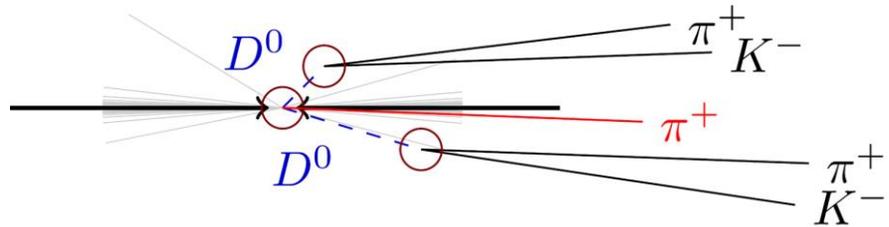


# **$T_{cc}$ and TS**

**Misha Mikhasenko  
Ruhr University Bochum**

**FDSA, Genoa**

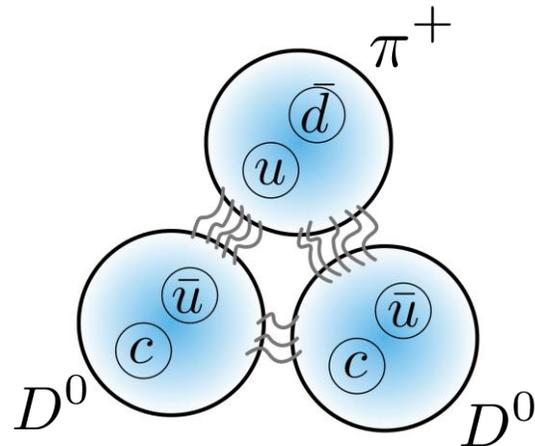
# Observation of the doubly-charm tetraquark $T_{cc}^+$



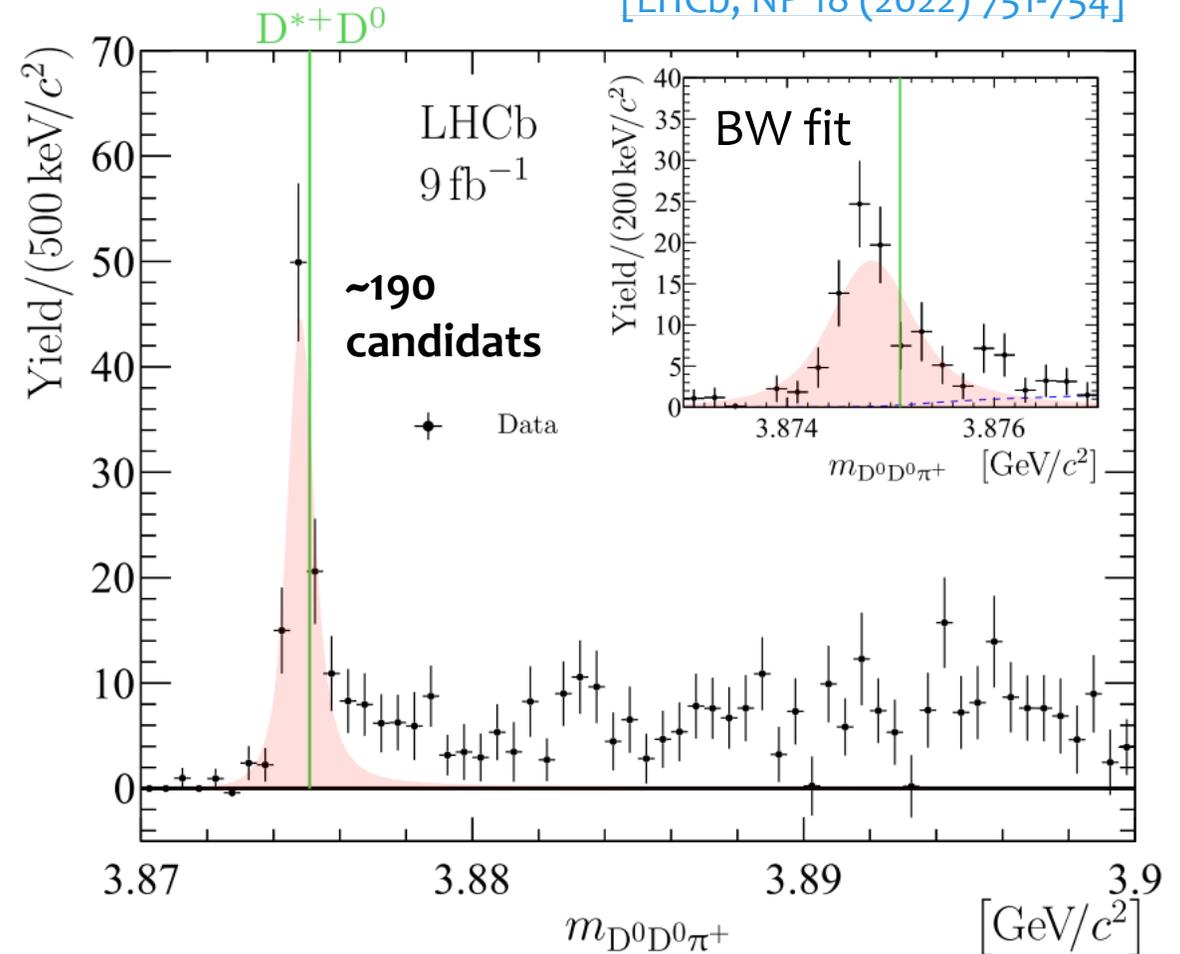
Peak in  $D^0 D^0 \pi^+$  just below  $D^{*+} D^0$  threshold

Extremely narrow,  $\sim 300$  keV  
(resolution)

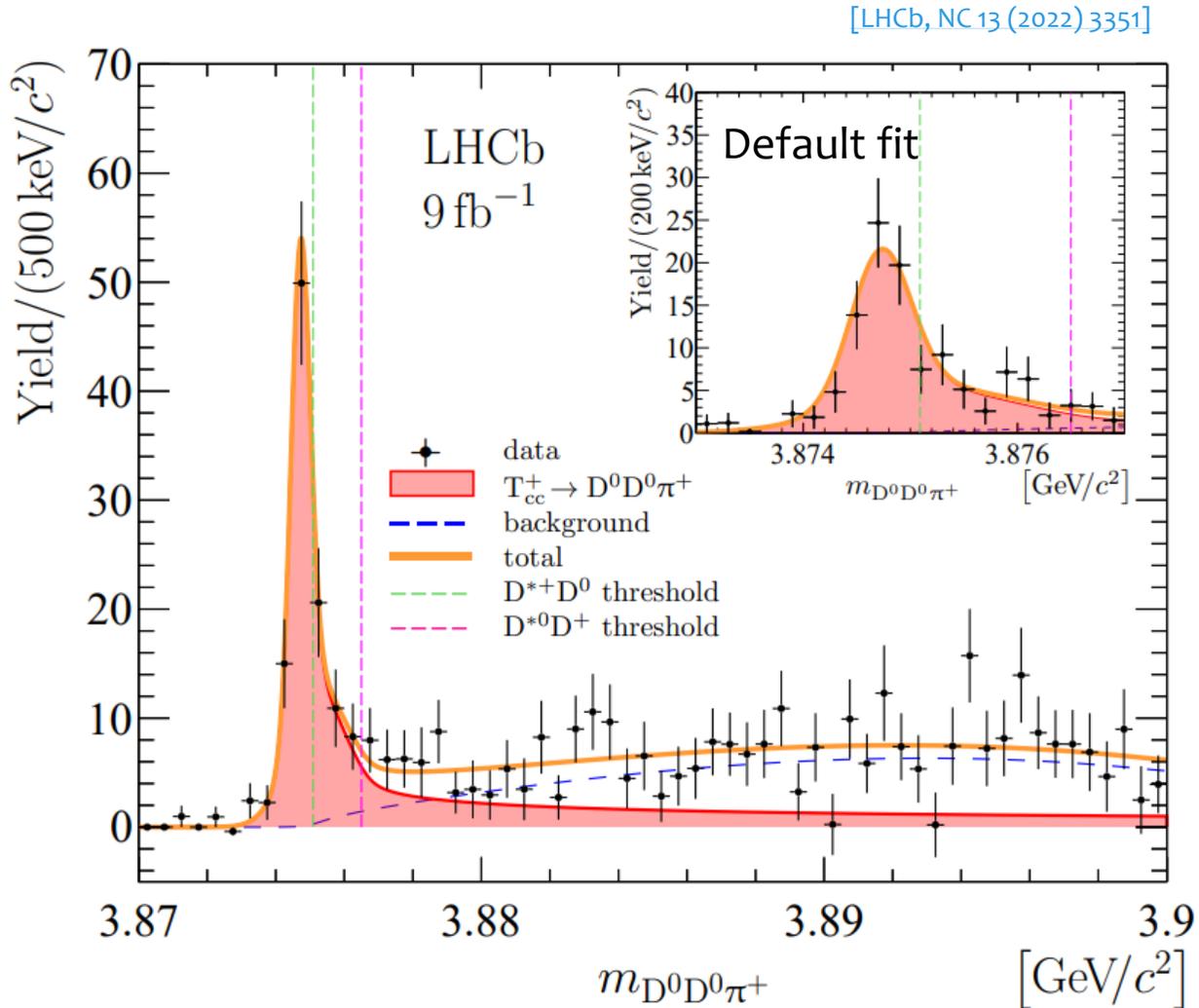
Needs to be treated as  
three-body effect



[LHCb, NP 18 (2022) 751-754]



# Studies of the doubly-charm tetraquark $T_{cc}^+$



QN: isoscalar ( $I = 0$ ), axial ( $J^{PC} = 1^{++}$ )

Coupled channel model

$$D^{*+}D^0 + D^{*0}D^+$$

$$\rightarrow \{D^0D^0\pi^+, D^0D^+\pi^0, D^0D^+\gamma\}$$



Yields pole parameters:

❖ Binding energy:  $-360 \pm 40_{-0}^{+4}$  keV

❖ Width:  $48 \pm 2_{-14}^{+0}$  keV

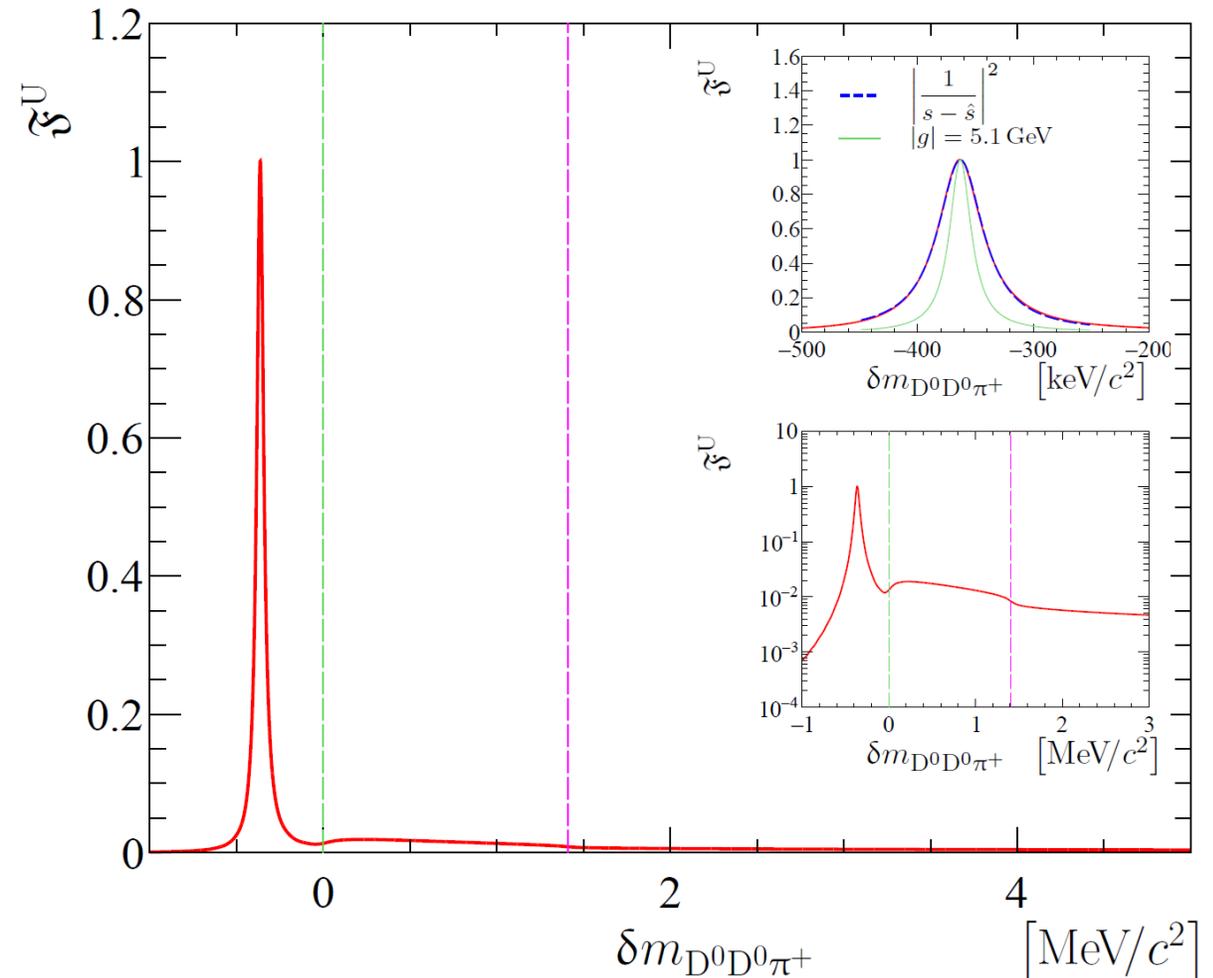
# Prediction of the three-body spectrum

- The narrow peak below the lowest threshold
- Long tail with cusps at the thresholds

$$T(s) = \frac{\text{production}}{\text{rescattering}(s | \delta m, g)}$$

Analytic solution enables us:

- Obtain pole mass and width
- Compute scattering parameters



# Tcc model and analytic continuation

similar to [MM et al. (JPAC), PRD 98 (2018) 096021]

Dynamic amplitude of  $D^*D \rightarrow D^*D$  scattering:

$$T_{2 \times 2}(s) = \frac{K}{1 - \Sigma K} = \frac{K(m^2 - s)}{m^2 - s - i g^2 (\rho_{\text{tot}}(s) + i \xi(s))}$$

where  $K$  is the isoscalar potential:

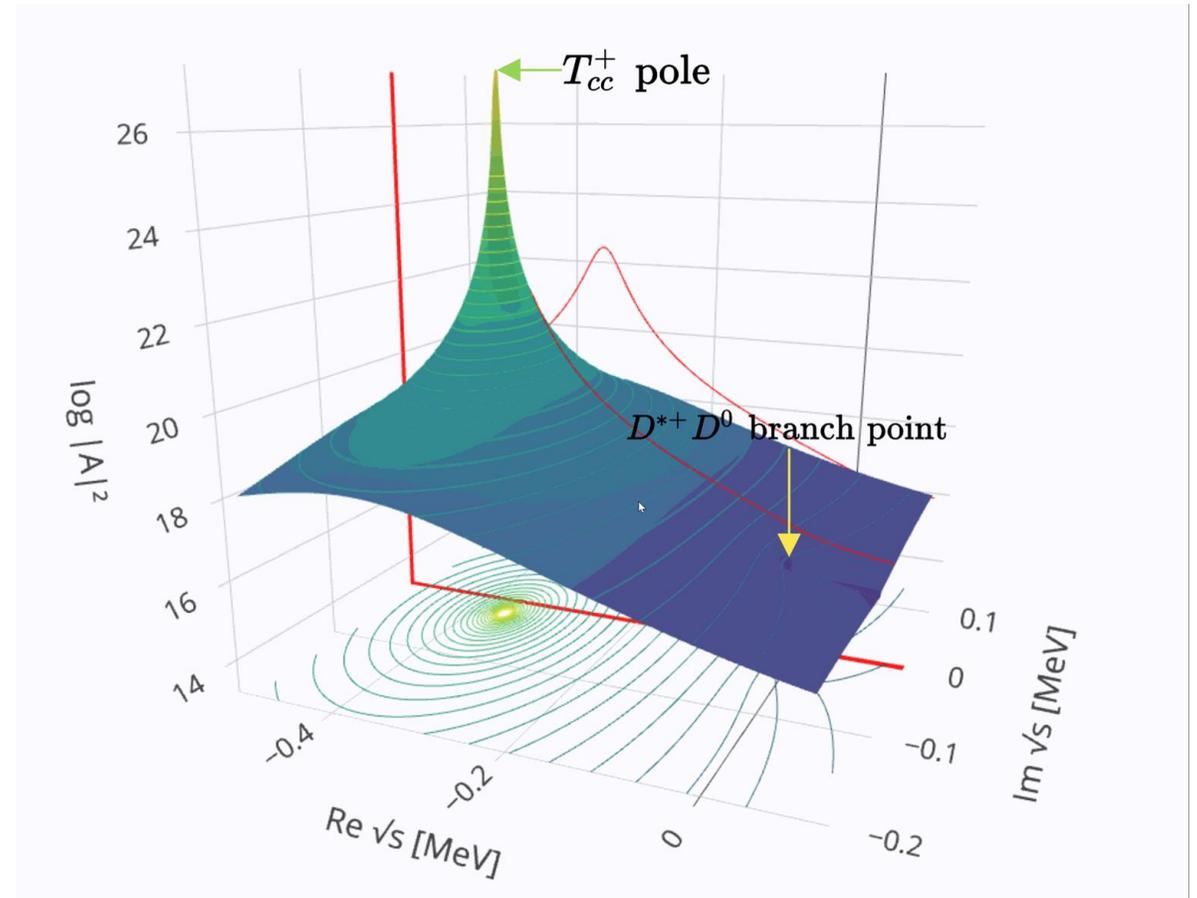
$$K = \frac{1}{m^2 - s} \begin{pmatrix} g \cdot g & -g \cdot g \\ -g \cdot g & g \cdot g \end{pmatrix},$$

and  $\Sigma$  is the loop function:

$$\Sigma(s) = [D^*D \rightarrow DD\pi(\gamma) \rightarrow D^*D]$$

$$= \left[ \text{diagram 1} + \text{diagram 2} \right].$$

**Model parameters:  $|g|^2$  and  $m^2$  – bare**



# Effective range expansion

## Expansion coefficients

$$k \cot \delta(k) = \frac{1}{a} + r \frac{k^2}{2} + O(a^3 k^4)$$

- $k$  is a break-up momentum
- $1/a, r$  are coefficient in expansion

Can be done by computing derivatives of regular ( $k \cot \delta$ )

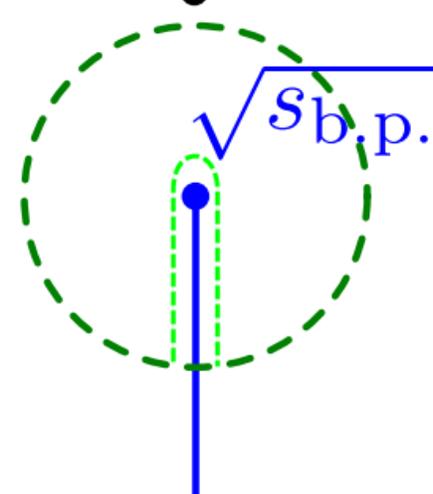
$D^*$  is unstable,  
complex branch point

sheet I

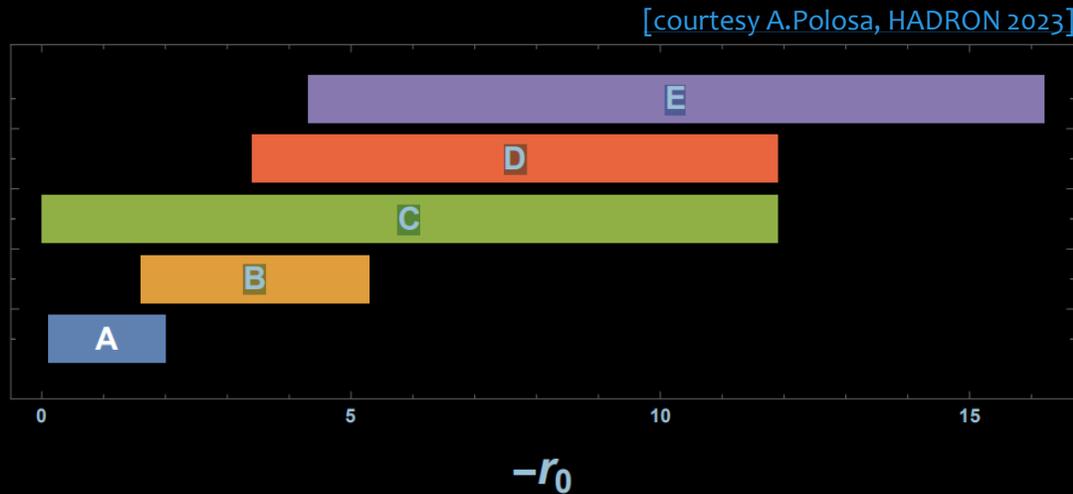


$$m_{D^{*+}} + m_{D^0}$$

$T_{cc}^+$



sheet II



- A: Baru et al., 2110.07484
- B: Esposito et al., 2108.11413
- C: LHCb, 2109.01056
- D: Maiani & Pilloni GGI-Lects
- E: Mikhasenko, 2203.04622

# Different values on Effective range discussion

Scattering parameters  $(a,r)$  gives simplified description of the amplitude near threshold.

Scattering length is well constrained by the binding energy

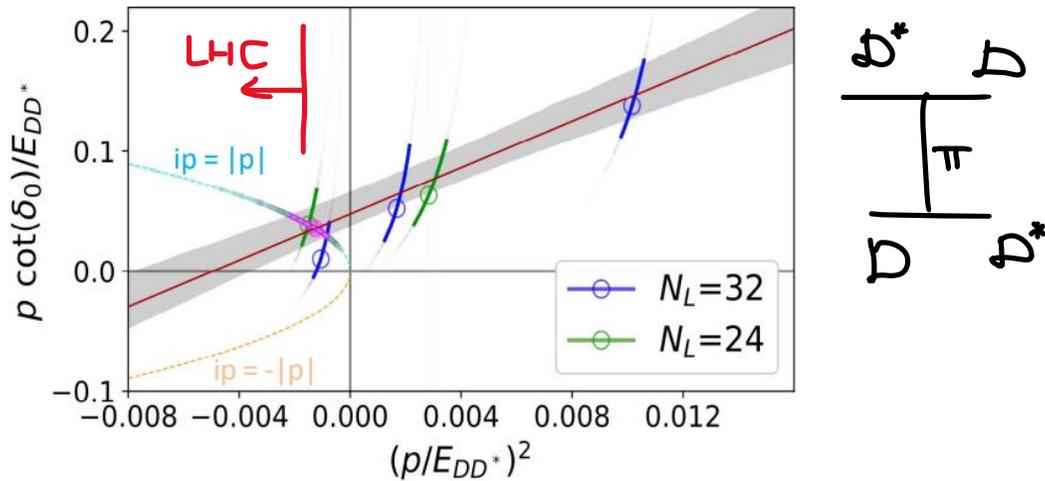
Limit is set in the effective range (related to the width)

**High Weinberg compositeness is obtained**

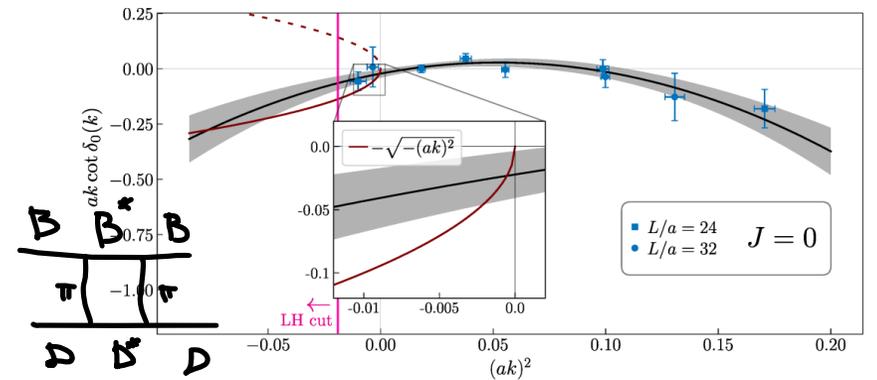
# $T_{QQ}$ in Lattice: left hand cut

Tbc

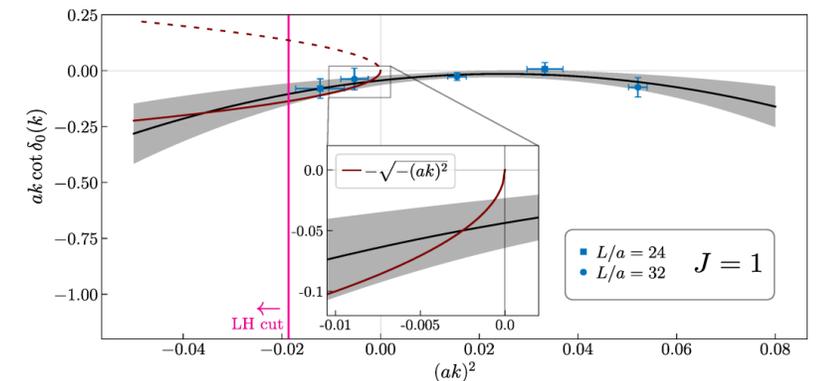
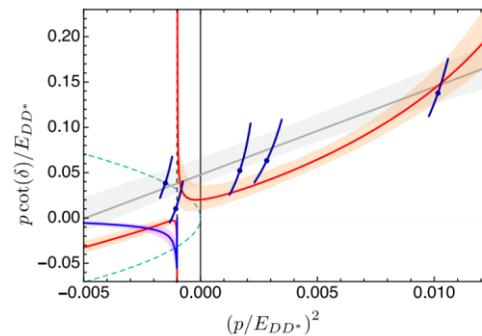
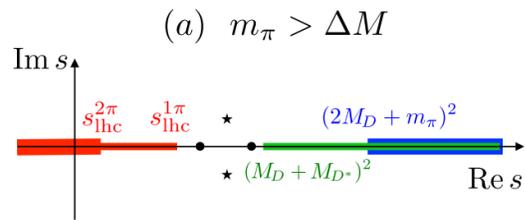
Padmanath, SP: 2202.10110, PRL,  $m_\pi \approx 280$  MeV



[Mark Wagner 2312.02925]



[Baru et al., 2303.09441]



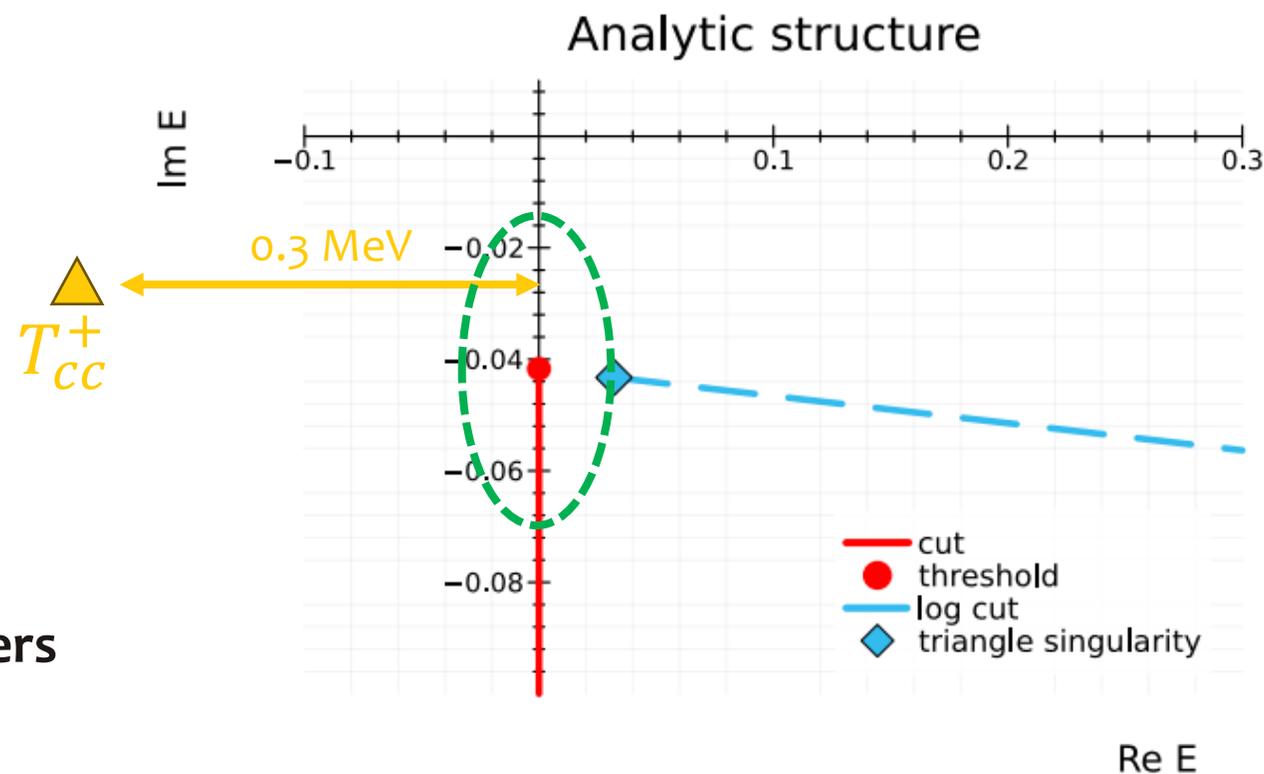
# Effective range expansion

# Convergence of the expansion

## Effective range expansion

- First observation: dependence of expansion parameters on radius of Cauchy integrals
- Reason: log branch point nearby
- Convergence radius  $\sim 20\text{keV}$
- Rethinking of the effective range parameters & Weinberg compositeness is needed

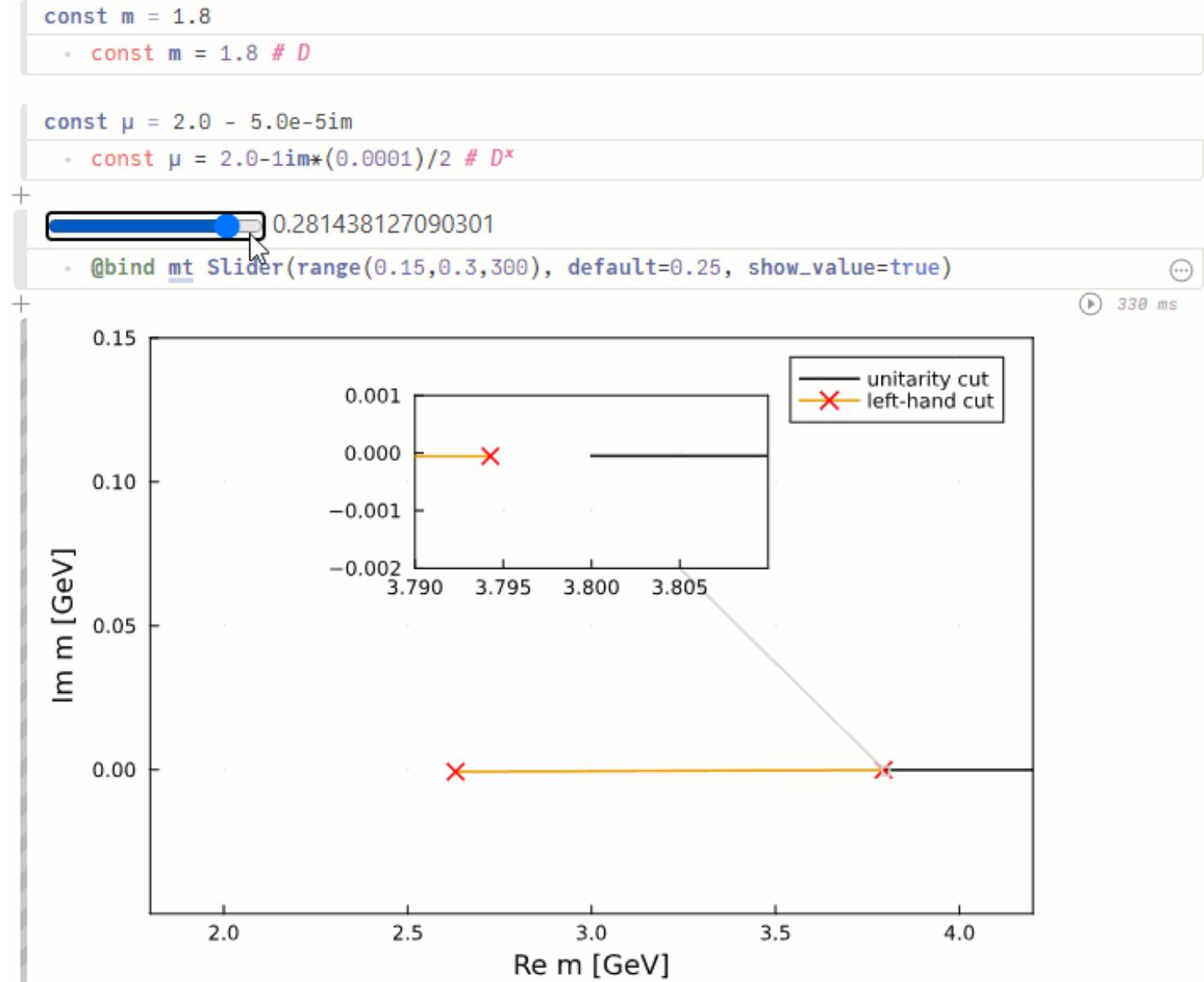
## Small radius of convergence



# Triangle Singularity & LHC

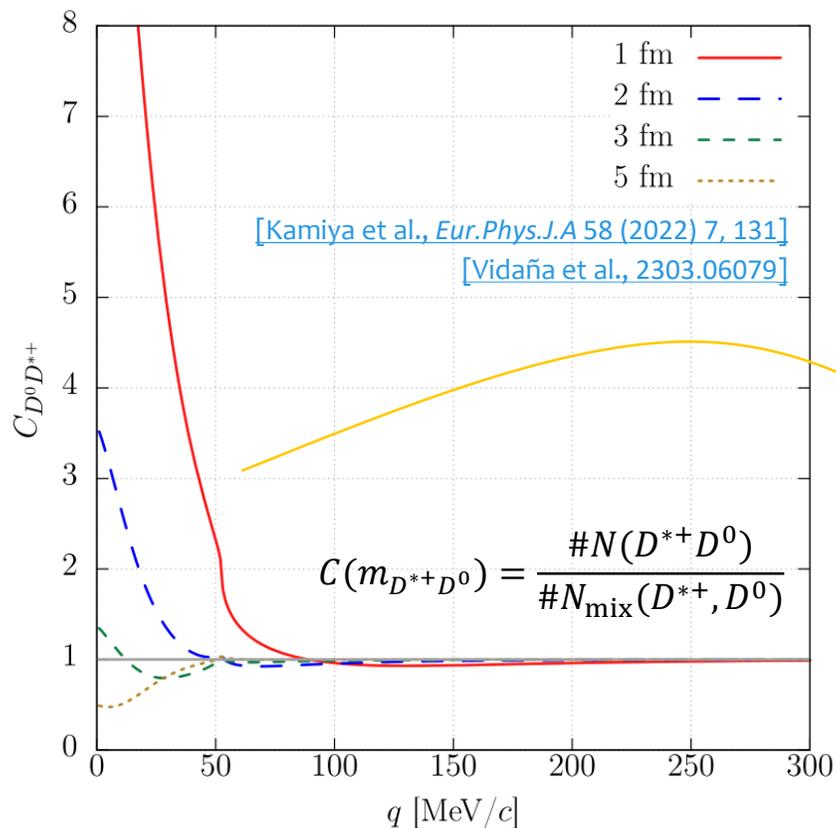
## Simple setup

- $m_D = 1.8$
- $m_{D^*} = 2.0$
- Mass of pion is varied
- Red crosses – location of log branch points

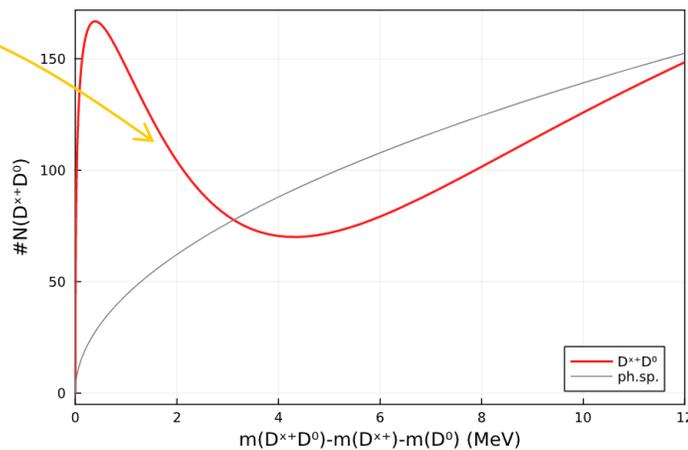


# Femtoscscopy and Unitarization

# Tcc: discussion on production and femtoscopy

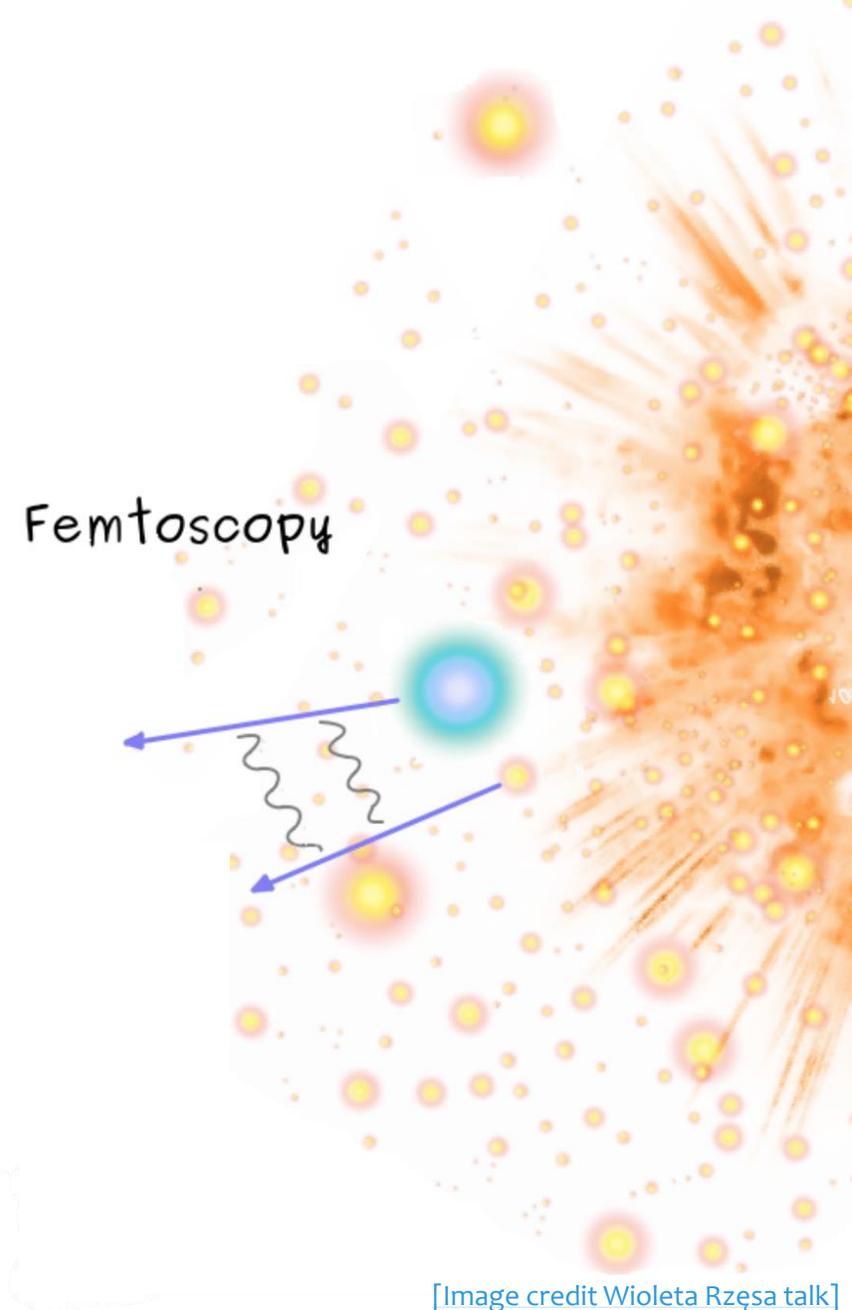


On-shell  $D^{*+}$ ,  $D^0$  produced independently may experience residual  $T_{CC}^+$ -interaction



[\[GitHub/mmikhasenko\]](#)

Femtoscopy



[\[Image credit Wioleta Rzęsa talk\]](#)

# Basdevant Unitarization

## Unitarization with background

$$T_D^u(M^2) = T_D(M^2) - \frac{1}{2i\pi} D(M^2) \int_{M_{R^2}}^{\infty} ds' \frac{\text{disc}(D^{-1}(s')) T_D(s')}{(s' - M^2)}. \quad (3.5)$$

<https://journals.aps.org/prd/pdf/10.1103/PhysRevD.16.657>

## Interference with spherical wave

$$C_{D+D^*0}(p_{D+}) = 1 + 4\pi\theta(q_{\max} - p_{D+}) \times \int_0^{+\infty} dr r^2 S_{12}(r) \left\{ |j_0(p_{D+}r) + T_{22}(E)\tilde{G}^{(2)}(r;E)|^2 + |T_{12}(E)\tilde{G}^{(1)}(r;E)|^2 - j_0^2(p_{D+}r) \right\}$$

<https://arxiv.org/pdf/2303.06079.pdf>

# Summary

## Part1:

Effective range parameters can be mathematically well defined for three-body scattering

The convergence radius is small -- due to one-pion exchange singularity (Triangle singularity)

=>  $a, r$  do not reflect properties of  $T_{cc}$

## Part2:

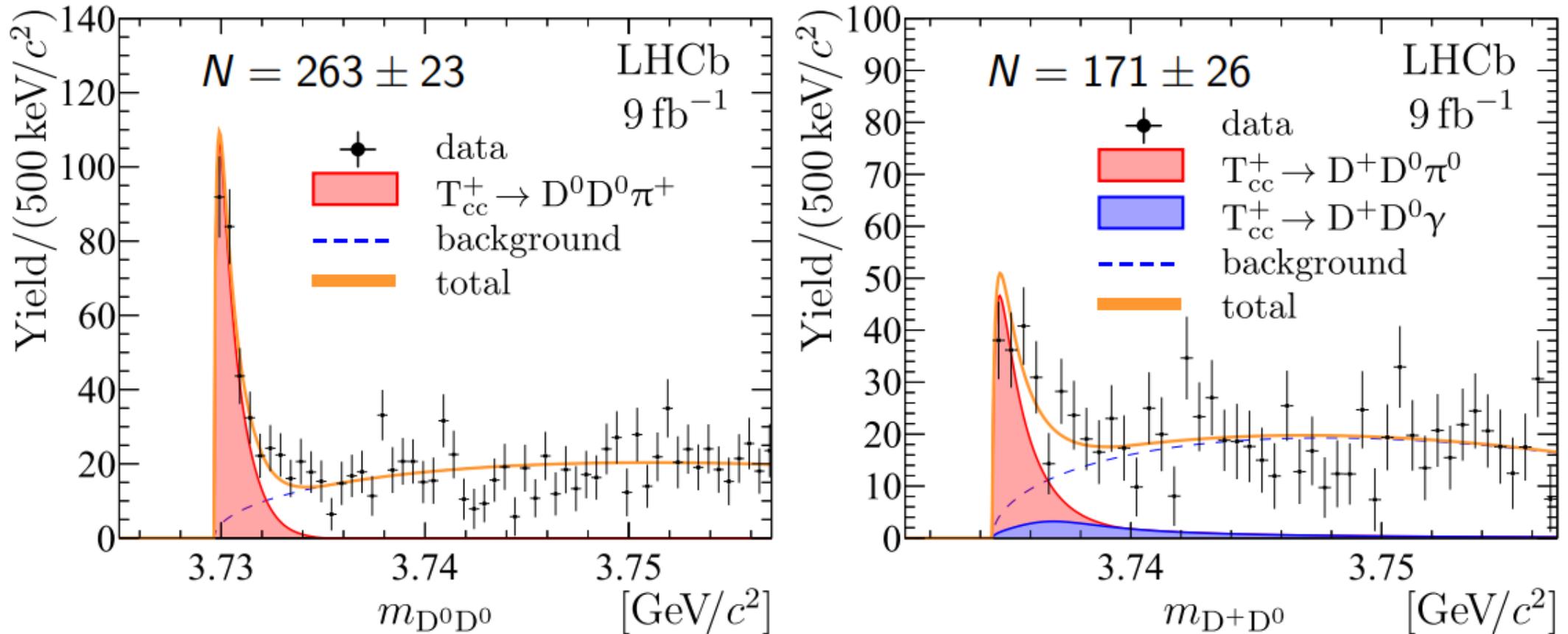
Approach to Femtoscopy & Dispersion Unitarization has similarities in physical picture and mathematical approach. Differences are also prominent:

- Inclusive vs Exclusive,
- Wave-functions vs S-matrix scattering

Clarification is needed.

# Backup

# Partially reconstructed $T_{cc}^+$



- Lineshape of  $D^0 D^0$  and  $D^0 D^+$  spectra are predicted well by the model
- Relative yields of  $D^0 D^0$  and  $D^0 D^+$  is in good agreement with the model predictions