

# Generalised Partons Distributions at the time of high precision experiments

Cédric Mezrag

Irfu, CEA, Université Paris-Saclay

June 6<sup>th</sup>, 2024

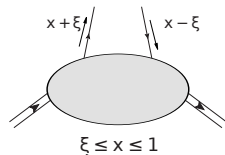
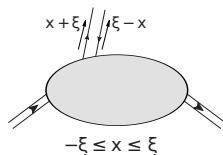
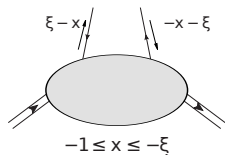
Contributors:

V. Bertone, P. Dall'Olivo, H. Dutrieux, J.M. Morgado Chavez, H. Moutarde, J. Rodriguez Quintero, J. Segovia, P. Sznajder, J. Wagner

# Introduction

- Generalised Parton Distributions (GPDs):

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  - ▶ “hadron-parton” amplitudes which depend on three variables  $(x, \xi, t)$  and a scale  $\mu$ ,



- ★  $x$ : average momentum fraction carried by the active parton
- ★  $\xi$ : skewness parameter  $\xi \simeq \frac{x_B}{2-x_B}$
- ★  $t$ : the Mandelstam variable

- Generalised Parton Distributions (GPDs):

- ▶ “hadron-parton” amplitudes which depend on three variables  $(x, \xi, t)$  and a scale  $\mu$ ,
- ▶ are defined in terms of a non-local matrix element,

$$\begin{aligned} & \frac{1}{2} \int \frac{e^{ixP^+z^-}}{2\pi} \langle P + \frac{\Delta}{2} | \bar{\psi}^q(-\frac{z}{2}) \gamma^+ \psi^q(\frac{z}{2}) | P - \frac{\Delta}{2} \rangle dz^- |_{z^+=0, z=0} \\ &= \frac{1}{2P^+} \left[ H^q(x, \xi, t) \bar{u} \gamma^+ u + E^q(x, \xi, t) \bar{u} \frac{i\sigma^{+\alpha} \Delta_\alpha}{2M} u \right]. \end{aligned}$$

$$\begin{aligned} & \frac{1}{2} \int \frac{e^{ixP^+z^-}}{2\pi} \langle P + \frac{\Delta}{2} | \bar{\psi}^q(-\frac{z}{2}) \gamma^+ \gamma_5 \psi^q(\frac{z}{2}) | P - \frac{\Delta}{2} \rangle dz^- |_{z^+=0, z=0} \\ &= \frac{1}{2P^+} \left[ \tilde{H}^q(x, \xi, t) \bar{u} \gamma^+ \gamma_5 u + \tilde{E}^q(x, \xi, t) \bar{u} \frac{\gamma_5 \Delta^+}{2M} u \right]. \end{aligned}$$

D. Müller *et al.*, Fortsch. Phys. 42 101 (1994)

X. Ji, Phys. Rev. Lett. 78, 610 (1997)

A. Radyushkin, Phys. Lett. B380, 417 (1996)

4 GPDs without helicity transfer + 4 helicity flip GPDs

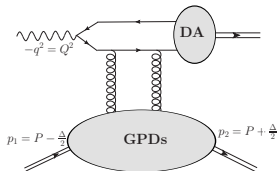
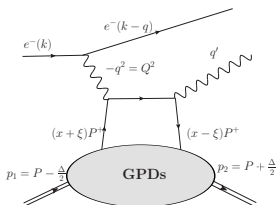
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- ▶ can be split into quark flavour and gluon contributions,
- ▶ are related to PDF in the forward limit  $H(x, \xi = 0, t = 0; \mu) = q(x; \mu)$
- ▶ are universal, *i.e.* are related to the amplitude of various exclusive processes through convolutions

$$\mathcal{H}(\xi, t) = \int dx C(x, \xi) H(x, \xi, t)$$





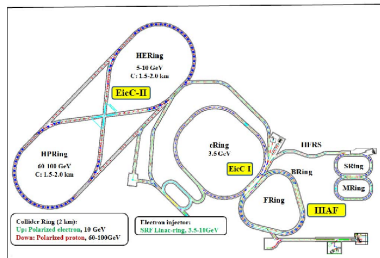
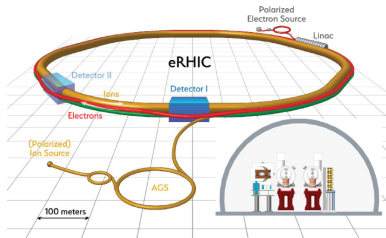
- Current experimental facilities: fixed targets



- Current experimental facilities: fixed targets



- Future facilities: colliders



- Polynomiality Property:

$$\int_{-1}^1 dx x^m H^q(x, \xi, t; \mu) = \sum_{j=0}^{\lfloor \frac{m}{2} \rfloor} \xi^{2j} C_{2j}^q(t; \mu) + \text{mod}(m, 2) \xi^{m+1} C_{m+1}^q(t; \mu)$$

X. Ji, J.Phys.G 24 (1998) 1181-1205  
 A. Radyushkin, Phys.Lett.B 449 (1999) 81-88

Special case :

$$\int_{-1}^1 dx H^q(x, \xi, t; \mu) = F_1^q(t)$$

Lorentz Covariance

- Polynomiality Property:

Lorentz Covariance

- Positivity property:

$$\left| H^q(x, \xi, t) - \frac{\xi^2}{1 - \xi^2} E^q(x, \xi, t) \right| \leq \sqrt{\frac{q\left(\frac{x+\xi}{1+\xi}\right) q\left(\frac{x-\xi}{1-\xi}\right)}{1 - \xi^2}}$$

A. Radysuhkin, Phys. Rev. D59, 014030 (1999)

B. Pire *et al.*, Eur. Phys. J. C8, 103 (1999)

M. Diehl *et al.*, Nucl. Phys. B596, 33 (2001)

P.V. Pobilitza, Phys. Rev. D65, 114015 (2002)

Positivity of Hilbert space norm

- Polynomiality Property:
- Positivity property:
- Support property:

Lorentz Covariance

Positivity of Hilbert space norm

$$x \in [-1; 1]$$

M. Diehl and T. Gousset, Phys. Lett. B428, 359 (1998)

Relativistic quantum mechanics

- Polynomiality Property:

Lorentz Covariance

- Positivity property:

Positivity of Hilbert space norm

- Support property:

Relativistic quantum mechanics

- Continuity at the crossover lines

→ GPDs are continuous albeit non analytical at  $x = \pm\xi$

J. Collins and A. Freund, PRD 59 074009 (1999)

Factorisation theorem

- Polynomiality Property:

Lorentz Covariance

- Positivity property:

Positivity of Hilbert space norm

- Support property:

Relativistic quantum mechanics

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Factorisation theorem

- Scale evolution property

→ generalization of DGLAP and ERBL evolution equations

D. Müller *et al.*, Fortschr. Phys. 42, 101 (1994)

Renormalization

- Polynomiality Property:

Lorentz Covariance

- Positivity property:

Positivity of Hilbert space norm

- Support property:

Relativistic quantum mechanics

- Continuity at the crossover lines

Factorisation theorem

- Scale evolution property

Renormalization

## Problem

- There is hardly any model fulfilling *a priori* all these constraints.
- Lattice QCD computations remain very challenging.



# Interpretation of GPDs I

## 2+1D structure of the nucleon



- In the limit  $\xi \rightarrow 0$ , one recovers a density interpretation:
  - ▶ 1D in momentum space ( $x$ )
  - ▶ 2D in coordinate space  $\vec{b}_\perp$  (related to  $t$ )

M. Burkardt, Phys. Rev. D62, 071503 (2000)

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- Possibility to extract density from experimental data

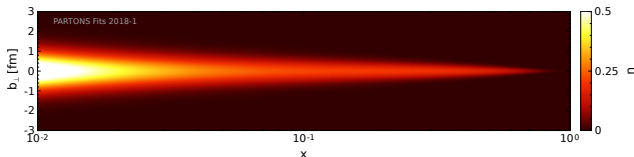


figure from H. Moutarde *et al.*, EPJC 78 (2018) 890

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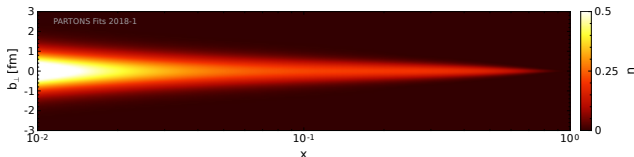


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- Correlation between  $x$  and  $b_\perp \rightarrow$  going beyond PDF and FF.

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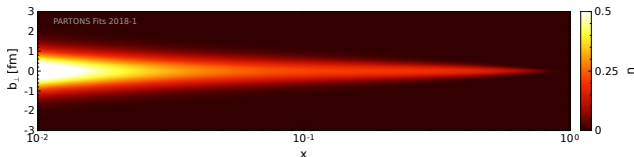
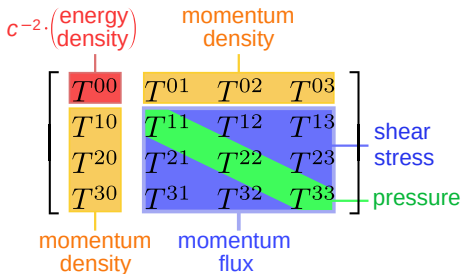


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- Correlation between  $x$  and  $b_\perp \rightarrow$  going beyond PDF and FF.
- Caveat: no experimental data at  $\xi = 0$   
 $\rightarrow$  extrapolations (and thus model-dependence) are necessary

# Interpretation of GPDs II

## Connection to the Energy-Momentum Tensor



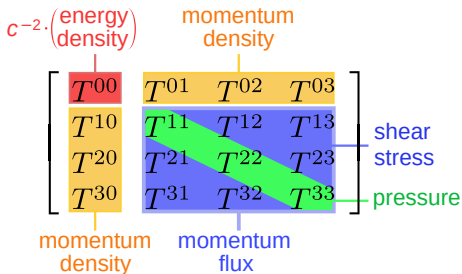
How energy, momentum, pressure are shared between quarks and gluons

Caveat: renormalization scheme and scale dependence

- C. Lorcé *et al.*, PLB 776 (2018) 38-47,
- M. Polyakov and P. Schweitzer, IJMPA 33 (2018) 26, 1830025
- C. Lorcé *et al.*, Eur.Phys.J.C 79 (2019) 1, 89

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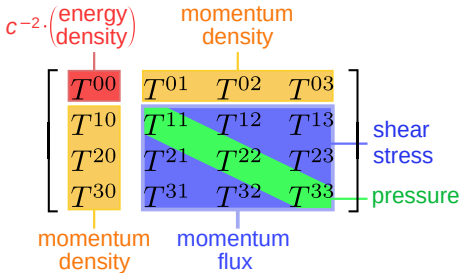
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$$\begin{aligned}
 \langle p', s' | T_{q,g}^{\mu\nu} | p, s \rangle = & \bar{u} \left[ P^{\{\mu\gamma\nu\}} A_{q,g}(t; \mu) + \frac{\Delta^\mu \Delta^\nu - g^{\mu\nu} \Delta^2}{M} C_{q,g}(t; \mu) \right. \\
 & \left. + M g^{\mu\nu} \bar{C}_{q,g}(t; \mu) + \frac{P^{\{\mu i \sigma^\nu\} \Delta}}{2M} B_{q,g}(t; \mu) + \frac{P^{\{\mu i \sigma^\nu\} \Delta}}{2M} D_{q,g}(t; \mu) \right] u
 \end{aligned}$$

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$$\int_{-1}^1 dx x H_q(x, \xi, t; \mu) = A_q(t; \mu) + (2\xi)^2 C_q(t; \mu)$$

$$\int_{-1}^1 dx x E_q(x, \xi, t; \mu) = B_q(t; \mu) - (2\xi)^2 C_q(t; \mu)$$

- Ji sum rule
- Fluid mechanics analogy  
 X. Ji, PRL 78, 610-613 (1997)  
 M.V. Polyakov PLB 555, 57-62 (2003)

## Accessing GPDs from experimental data



PARTONS

partons.cea.fr



B. Berthou *et al.*, EPJC 78 (2018) 478

Gepard

gepard.phy.hr



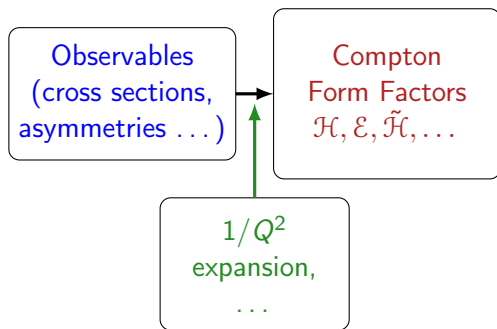
K. Kumericki, EPJ Web Conf. 112 (2016) 01012

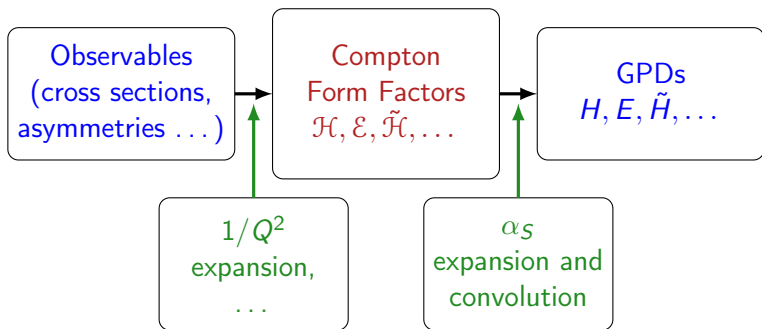
- Similarities : NLO computations, BM formalism, ANN, ...
- Differences : models, evolution, ...

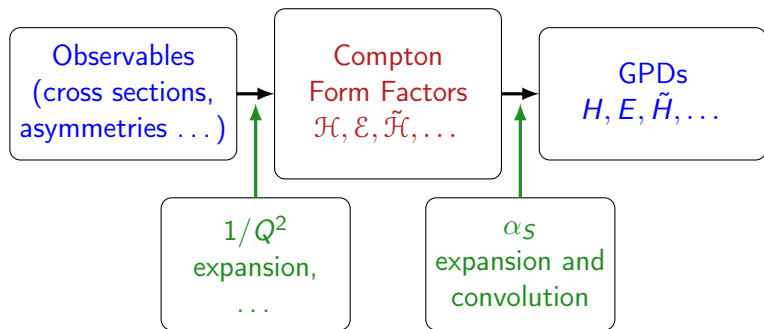
## Physics impact

These integrated softwares are the mandatory path toward reliable multichannel analyses.

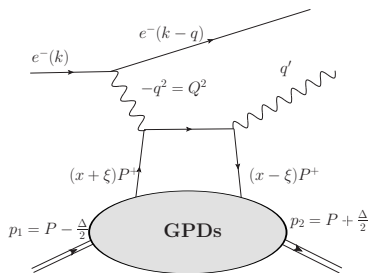
Observables  
(cross sections,  
asymmetries ...)



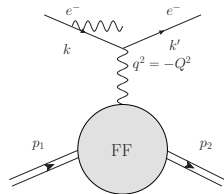
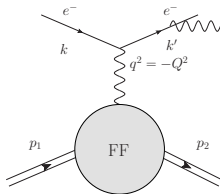
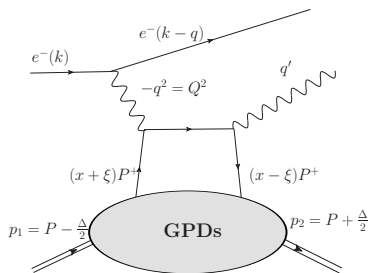




- CFFs play today a central role in our understanding of GPDs
- Extraction generally focused on CFFs

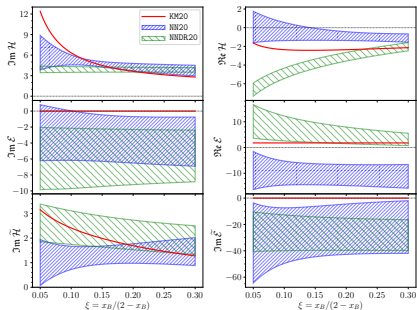


- Best studied experimental process connected to GPDs  
→ Data taken at Hermes, Compass, JLab 6, JLab 12

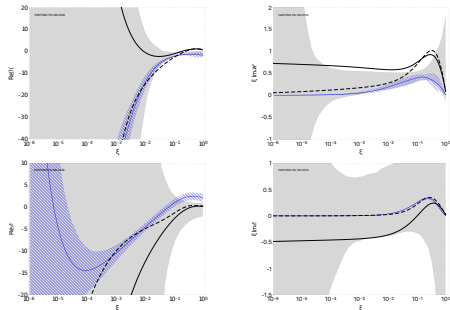


- Best studied experimental process connected to GPDs
  - Data taken at Hermes, Compass, JLab 6, JLab 12
- Interferes with the Bethe-Heitler (BH) process
  - ▶ Blessing: Interference term boosted w.r.t. pure DVCS one
  - ▶ Curse: access to the angular modulation of the pure DVCS part difficult

M. Defurne *et al.*, Nature Commun. 8 (2017) 1, 1408



M. Cuić *et al.*, PRL 125, (2020), 232005



H. Moutarde *et al.*, EPJC 79, (2019), 614

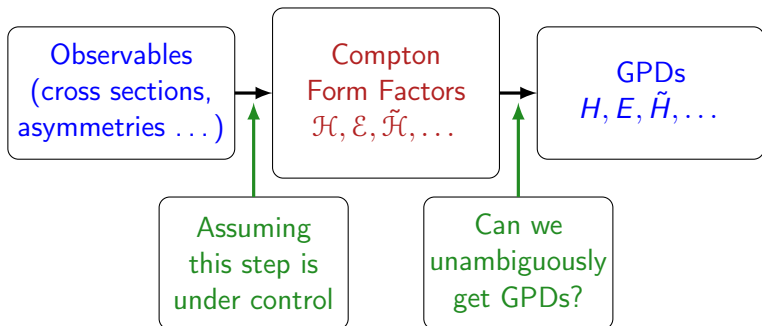
- Recent effort on bias reduction in CFF extraction (ANN)
  - additional ongoing studies, J. Grigsby *et al.*, PRD 104 (2021) 016001
- Studies of ANN architecture to fulfil GPDs properties (dispersion relation, polynomiality, . . .)
- Recent efforts on propagation of uncertainties (allowing impact studies for JLAB12, EIC and EicC)

see e.g. H. Dutrieux *et al.*, EPJA 57 8 250 (2021)



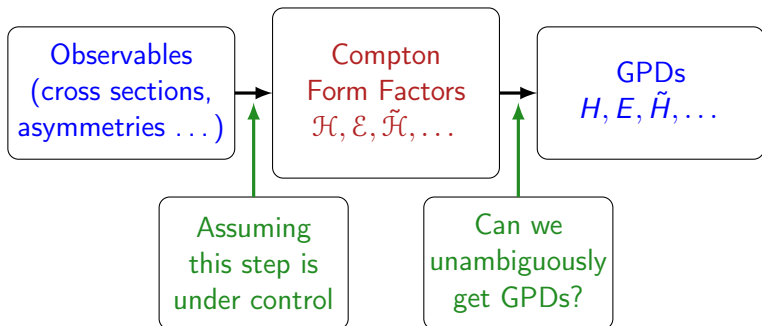
# The DVCS deconvolution problem I

From CFF to GPDs



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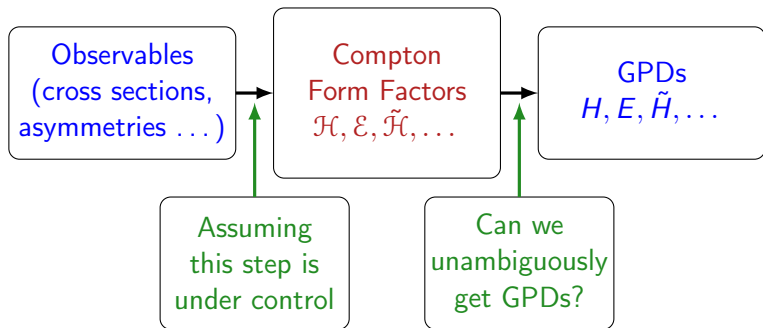
From CFF to GPDs



- It has been known for a long time that this is not the case at LO  
Due to dispersion relations, any GPD vanishing on  $x = \pm\xi$  would not contribute to DVCS at LO (neglecting D-term contributions).

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- It has been known for a long time that this is not the case at LO  
Due to dispersion relations, any GPD vanishing on  $x = \pm\xi$  would not contribute to DVCS at LO (neglecting D-term contributions).
- Are QCD corrections improving the situation?

## CFF Definition

$$\underbrace{\mathcal{H}(\xi, t, Q^2)}_{\text{Observable}} = \int_{-1}^1 \frac{dx}{\xi} \underbrace{T\left(\frac{x}{\xi}, \frac{Q^2}{\mu^2}, \alpha_s(\mu^2)\right)}_{\text{Perturbative DVCS kernel}} H(x, \xi, t, \mu^2)$$

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## Shadow GPD definition

We define shadow GPD  $H^{(n)}$  of order  $n$  such that when  $T$  is expanded in powers of  $\alpha_s$  up to  $n$  one has:

$$0 = \int_{-1}^1 \frac{dx}{\xi} T^{(n)}\left(\frac{x}{\xi}, \frac{Q^2}{\mu_0^2}, \alpha_s(\mu_0^2)\right) H^{(n)}(x, \xi, t, \mu_0^2) \quad \text{invisible in DVCS}$$

$$0 = H^{(n)}(x, 0, 0) \quad \text{invisible in DIS}$$

A part of the GPD functional space is invisible to DVCS and DIS combined

- We want our shadow GPDs to fulfill all the good theoretical properties of standard GPDs, especially polynomiality

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- We look for solution in the Double Distribution space:

$$H_{\text{shadow}}(x, \xi) = \int_{-1}^1 d\beta \int_{-1+|\beta|}^{1-|\beta|} d\alpha f_{\text{shadow}}(\beta, \alpha) \delta(x - \beta - \alpha\xi)$$

which is in one to one correspondance with the polynomiality property

N. Chouika *et al*, EPJC 77 (2017)

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N. Chouika *et al*, EPJC 77 (2017)

- We expanded  $f_{\text{shadow}}$  on polynomials of order  $N$ , so that we have a number of coefficient of order  $N^2$ .



We impose the following conditions :

- No forward limit  $H(x, 0) = 0 \rightarrow N + 2$  equations

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Adding Mellin moments (computed on the Lattice) provides other sets of order  $N$  equations.

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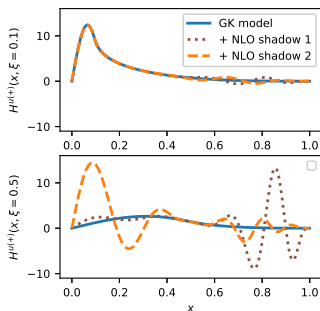
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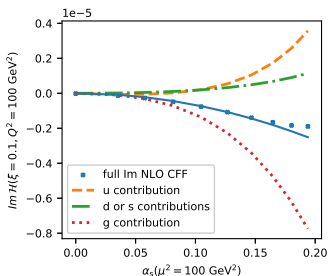
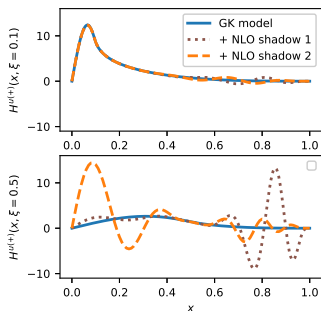
- We expect CFF computed from evolved NLO shadow GPDs to exhibit an  $\alpha_s^2$  behaviour under evolution (provided that the logs remain small enough).



## • NLO analysis of shadow GPDs:

- ▶ Cancelling the line  $x = \xi$  is necessary but **no longer** sufficient
- ▶ Additional conditions brought by NLO corrections reduce the size of the “shadow space”...
- ▶ ... but do not reduce it to 0  
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H. Dutrieux *et al.*, PRD 103 114019 (2021)



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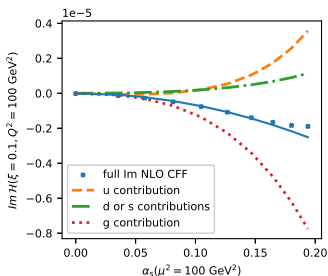
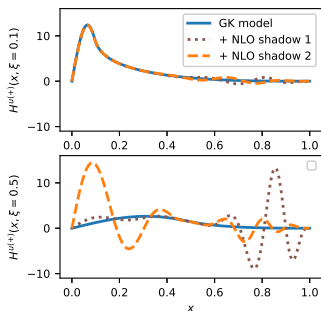
## • Evolution

- ▶ it was argued that evolution would solve this issue

A. Freund PLB 472, 412 (2000)  
E. Moffat *et al.*, PRD 108 (2023)

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Theoretical uncertainties promoted  
to main source of GPDs uncertainties

- Introduce theoretical inputs coming from QCD constraints
  - ▶ Change of methods with introduction of theoretical bias
  - ▶ Positivity is going to play an important role

- Introduce theoretical inputs coming from QCD constraints
  - ▶ Change of methods with introduction of theoretical bias
  - ▶ Positivity is going to play an important role
- Go to multichannel analysis
  - ▶ Shadow GPDs are process-dependent, *i.e.* some processes can see the shadow GPDs of others
  - ▶ Some exclusive processes are expected *not* to have shadow GPDs at all (but they are harder to measure).
    - ★ Double DVCS is the most obvious one  
K. Deja *et al.*, PRD 107 (2023) 9, 094035
    - ★ New 2  $\rightarrow$  3 exclusive processes are also good candidates  
R. Boussarie *et al.*, JHEP 02 (2017) 054  
O. Grocholski *et al.*, Phys.Rev.D 104 (2021) 11,  
J.-W. Qiu and Z. Yu, JHEP 08 (2022) 103
  - ▶ View IQCD Ioffe-time ratios as an additional process to be included in a global fit

Model  $H = H_{\text{visible}} + H_{\text{shadow}}$  with two different neural networks fulfilling by construction all the properties but one, the positivity property.

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## The positivity property

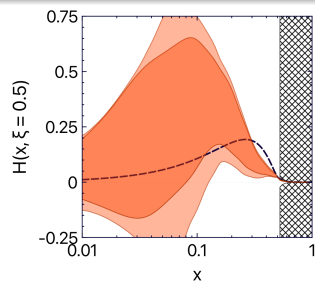
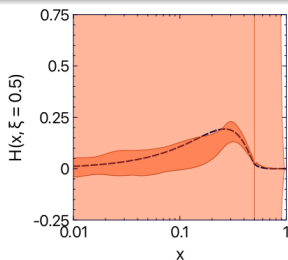
$$\left| H^q(x, \xi, t) - \frac{\xi^2}{1 - \xi^2} E^q(x, \xi, t) \right| \leq \sqrt{\frac{1}{1 - \xi^2} q\left(\frac{x + \xi}{1 + \xi}\right) q\left(\frac{x - \xi}{1 - \xi}\right)}$$



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H. Dutrieux *et al.*, EPJC 82 (2022) 3, 252

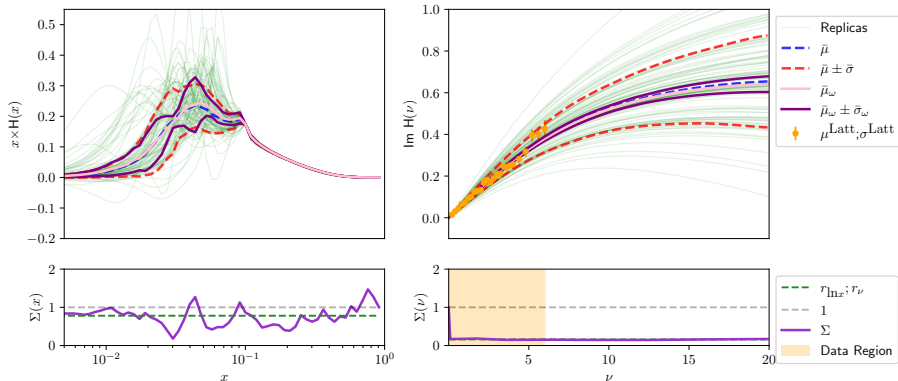


Lattice QCD can now compute matrix elements connected to GPDs:

$$I(\nu, \xi, t, z^2) = \int dx C(x, \nu, \xi, z^2, \mu^2) H(x, \xi, t, \mu^2)$$

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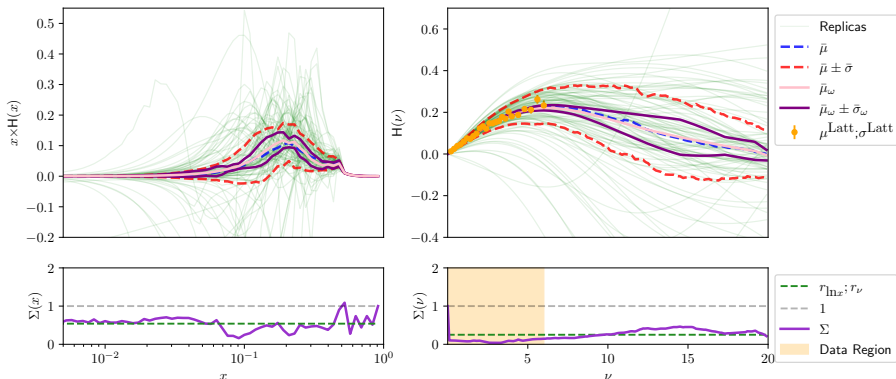
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M. Riberdy et al., Eur.Phys.J.C 84 (2024) 2, 201

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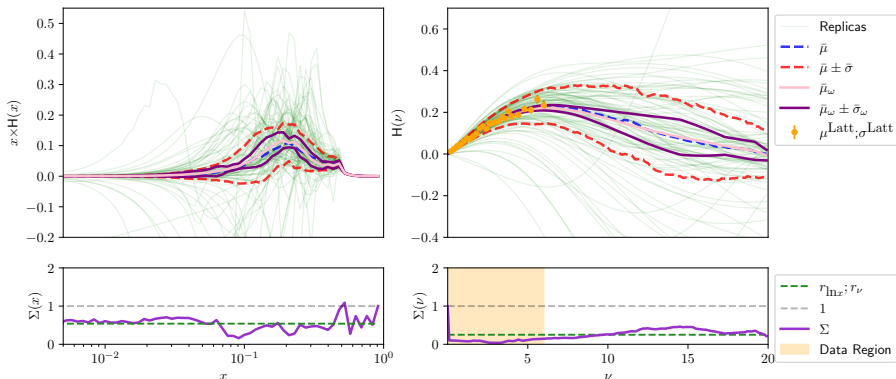
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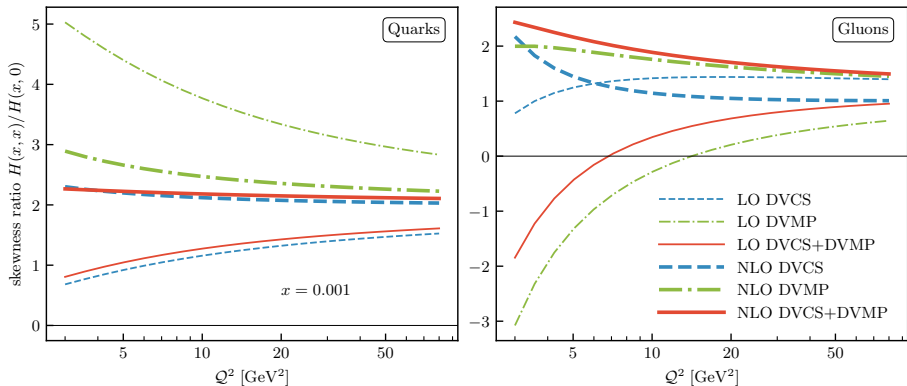
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We can expect a reduction of the deconvolution uncertainties

# Multichannel Fit of GPDs



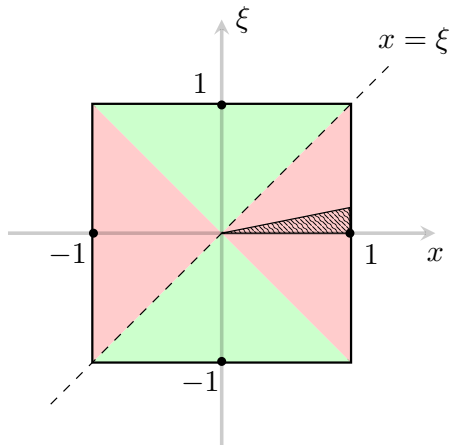
M. Cuic *et al.*, JHEP 12 (2023) 192

- Extraction of quark and gluon GPDs from NLO-DVCS and NLO-DVMP
- Inverse problem regularised through moments parametrisation and truncation

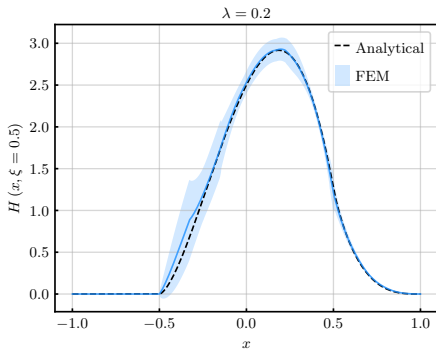
# GPD reconstruction from incomplete knowledge



Idea : exploit  $x$  and  $\xi$  entanglement triggered by the Radon Transform.



$\lambda = 0.2$



P. Dall'Olio *et al.*, PRD 109 (2024) 9, 096013

## Sullivan process and access to pion GPDs

Can we measure DVCS on a virtual pion ?

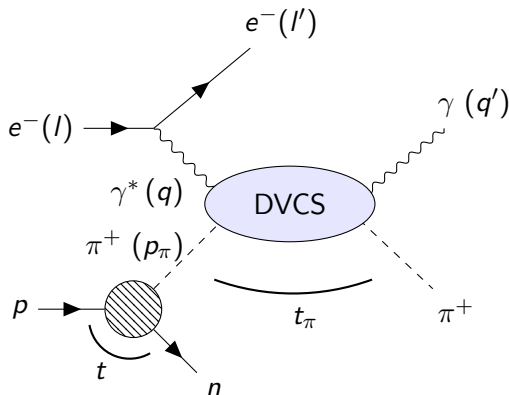
D. Amrath *et al.*, EPJC 58 (2008) 179-192  
J. M. Morgado Chavez *et al.*, PRL 128 202501

If yes, it is a good way to challenge many computations in the literature.

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D. Amrath *et al.*, EPJC 58 (2008) 179-192  
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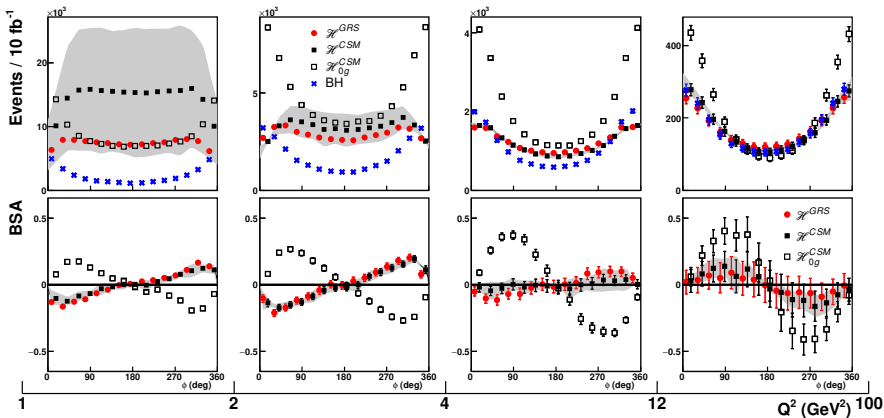
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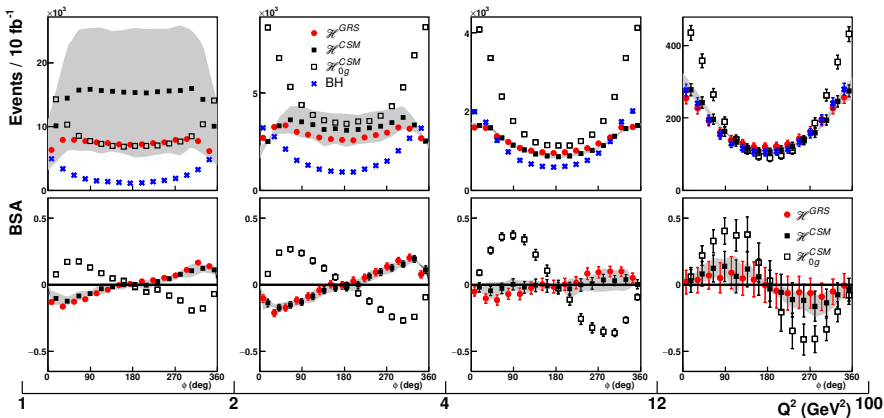


- $e^- p \rightarrow e^- \gamma \pi^+ n$
- kinematical cuts to avoid  $N^*$  resonances
- Already used to extract pion EFF at JLab
- Considered for pion structure function at EIC and EicC

EIC Yellow report, Nucl.Phys.A 1026 (2022) 122447

EicC white paper, Front.Phys.(Beijing) 16 (2021) 6, 64701





DVCS off virtual pion may be measurable at EIC and EicC

- Event generator EpIC for EIC E.C. Aschenhauer *et al.*, Eur.Phys.J.C 82 (2022) 9, 819
- Impact studies at JLab 12 O. Bessidskaia *et al.*, Phys.Rev.D 107 (2023) 1, 014020
- Small- $x$  GPDs and connection with gluon PDFs H. Dutrieux *et al.*, Phys.Rev.D 107 (2023) 11, 114019
- Feasibility of DDVCS K. Deja *et al.*, Phys.Rev.D 107 (2023) 9, 094035
- Nucleon GPD modelling from LFWFs M. Riberdy *et al.*, in preparation
- Extraction of pressure distributions at NLO H. Dutrieux *et al.*, in preparation
- Structure of heavy mesons on the lattice B. Blossier *et al.*
- Kinematic higher-twist corrections for DVCS, TCS and DDVCS v. Martinez-Fernandez *et al.*
- GPDs in UPC through exclusive quarkonia photoproduction CM *et al.*
- Reconstruction of GPDs from partial DGLAP knowledge P. Dall'Olivo *et al.*, PRD 109 (2024) 9, 096013

## Summary

- A new experimental era is starting with very precise data coming
- It is triggering a precision leap in phenomenology
- The question of theoretical uncertainties (and how to reduce them) becomes crucial

## Perspectives

- Efforts in phenomenology remain to be done (CFF/TFF and GPD)
- Multichannel analysis could help solving the deconvolution problem
- Ab-initio computations will provide insights in the next decade
- No golden solution, at least for now...

The perspective of new and precise data is a real challenge and will trigger leaps in our knowledge of the 3D structure of the nucleon.



Thank you for your attention

# Back up slides