

MODELLING OF GRB 221009A THROUGH AN ANALYTICAL DESCRIPTION OF VHE AFTERGLOW LIGHT CURVES



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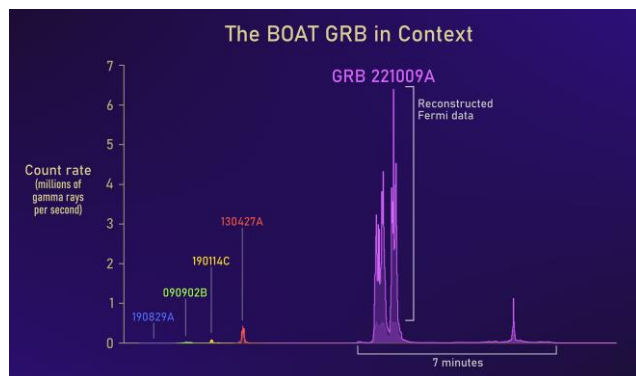
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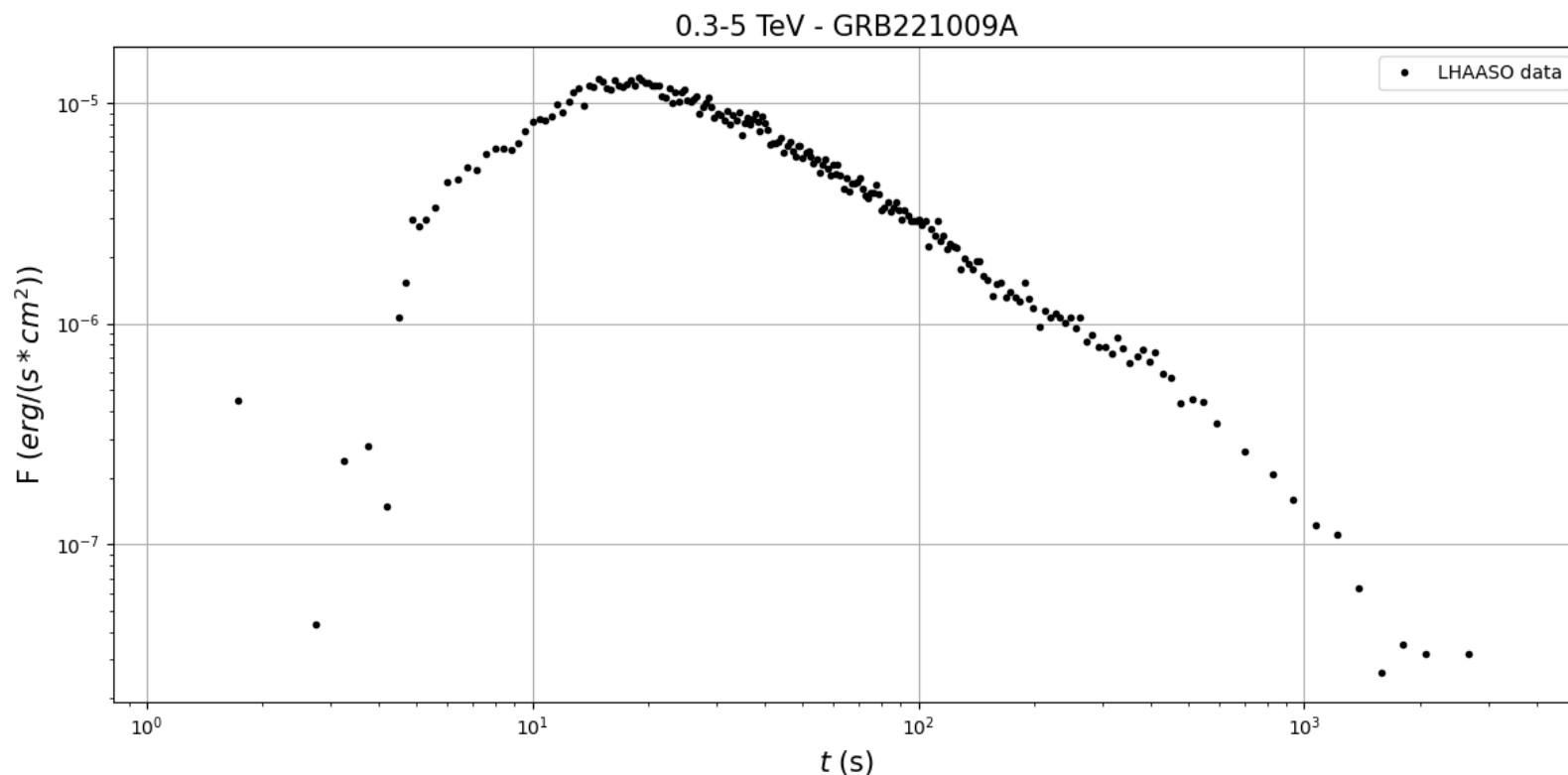
Image by: Anna Fortunati

GRB 221009A: LHAASO OBSERVATIONS OF THE B.O.A.T.



Credit: NASA's Goddard Space Flight Center and Adam Goldstein (USRA)

- Redshift: $z = 0.151$ (724 Mpc)
 $E_{k,iso} \approx 10^{55} \text{ erg}$
- Available dataset - LHAASO-WCDA
 $[T_0, T_0 + 3000 \text{ s}]$
0.3 – 5 TeV
 $\sigma > 250$



Data from: https://www.nhepsdc.cn/files/20230518/Figure3A_4.txt

LHAASO Collab. (Science 2023)

NUMERICAL MODEL AND ANALYTICAL DESCRIPTION

- Numerical model: *Miceli, Nava – Galaxies 2022, 10, 66*
- LCs produced varying a set of *physical* parameters:
- Analytical description: we can define a smooth BPL:

ϵ_e = electron energy fraction
 ϵ_b = magnetic energy fraction
 Γ_0 = bulk Lorentz factor
 n_0 = ISM density [cm^{-3}]
 p = injected electrons index

$$F(t) = \Phi \left(\frac{t}{\tau}\right)^{a_1} \left[\frac{a_1\left(\frac{t}{\tau}\right)^{1/s} + a_2}{a_1 + a_2}\right]^{-(a_1 + a_2)s}$$

Depending on some *fit* parameters:

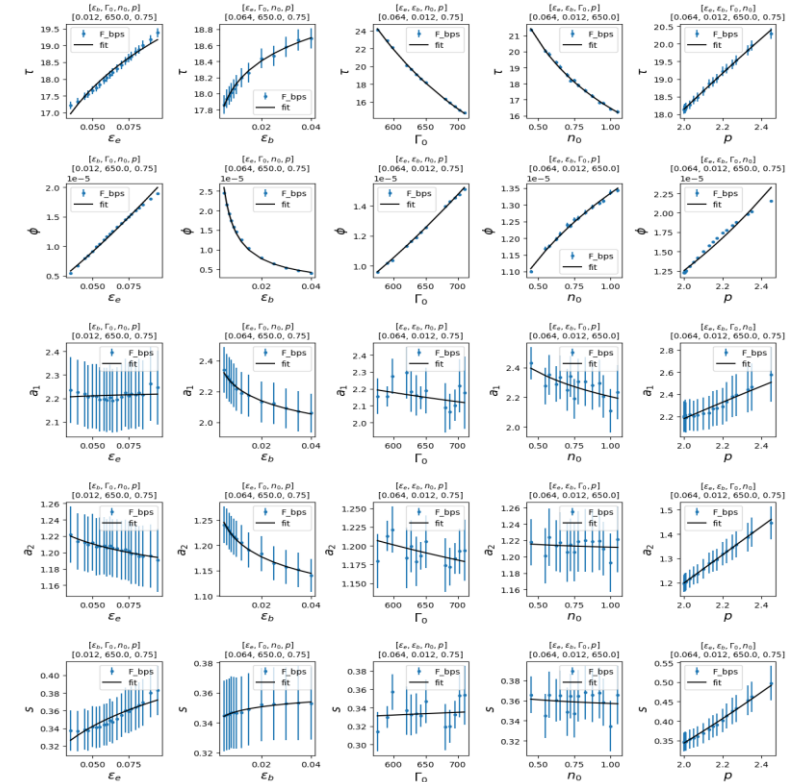
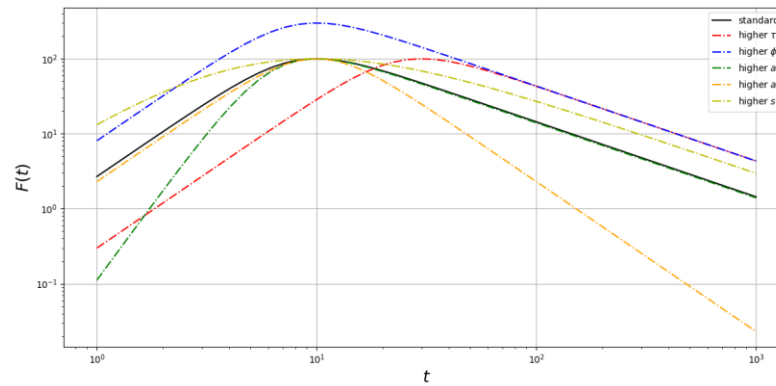
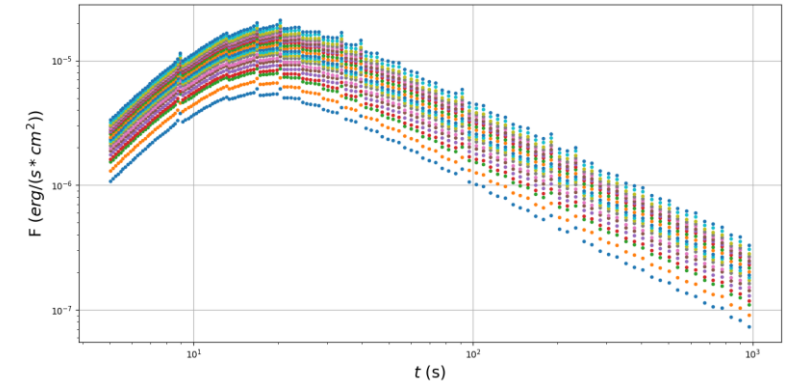
τ = peak time
 Φ = peak flux
 a_1 = low time PL index
 a_2 = high time PL index
 s = smoothing parameter

- Link each fit par to each phys par through:

$$y = A x^b \longrightarrow$$

- To have, ultimately:

$$(fit\ par) = A \left(\frac{\epsilon_e}{\epsilon_e}\right)^{b_e} \left(\frac{\epsilon_b}{\epsilon_b}\right)^{b_b} \left(\frac{\Gamma_0}{\Gamma_0}\right)^{b_\Gamma} \left(\frac{n_0}{n_0}\right)^{b_n} \left(\frac{p}{p}\right)^{b_p}$$



GRB 221009A: MODELLING

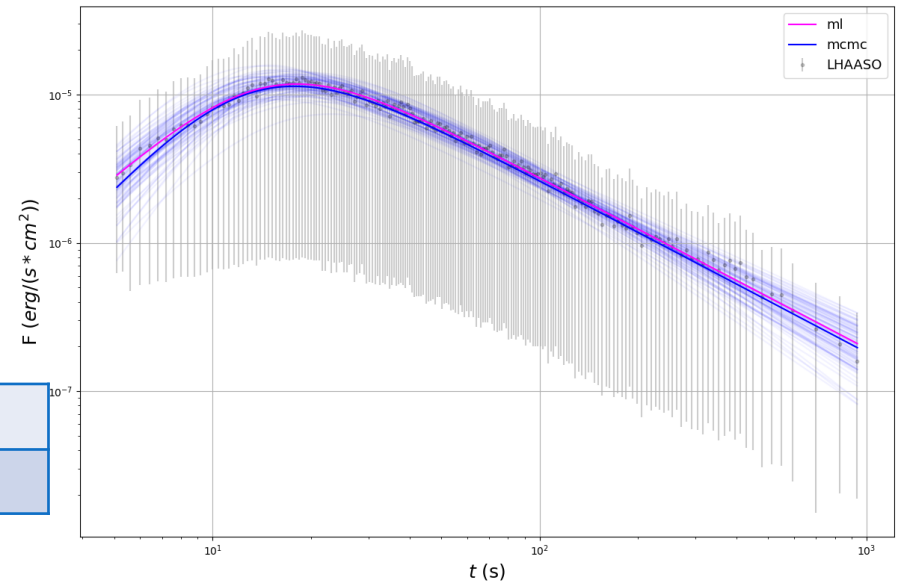
- Flux now expressed as function of the *physical* parameters!

- Log-likelihood:

$$\ln P(y | t, \sigma, \epsilon_e, \epsilon_b, \Gamma_0, n_0, p) = -\frac{1}{2} \sum_n \left[\frac{(y_n - F(\text{phys}))^2}{\sigma^2} + \ln(\sigma^2) \right]$$

- Through a **Maximum Likelihood Estimation**, we get a first approx for the parameters

$\bar{\epsilon}_e = 6.5 \times 10^{-2}$	$\bar{\epsilon}_b = 1.0 \times 10^{-2}$	$\bar{\Gamma}_0 = 650$	$\bar{n}_0 = 0.75 \text{ (cm}^{-3}\text{)}$	$\bar{p} = 2.01$
$\epsilon_e^{ML} = 1.0 \times 10^{-1}$	$\epsilon_b^{ML} = 2.5 \times 10^{-2}$	$\Gamma_0^{ML} = 580$	$n_0^{ML} = 2.1 \text{ (cm}^{-3}\text{)}$	$p^{ML} = 2.0$



- Markov-Chain Monte Carlo:

“ML” as initial values

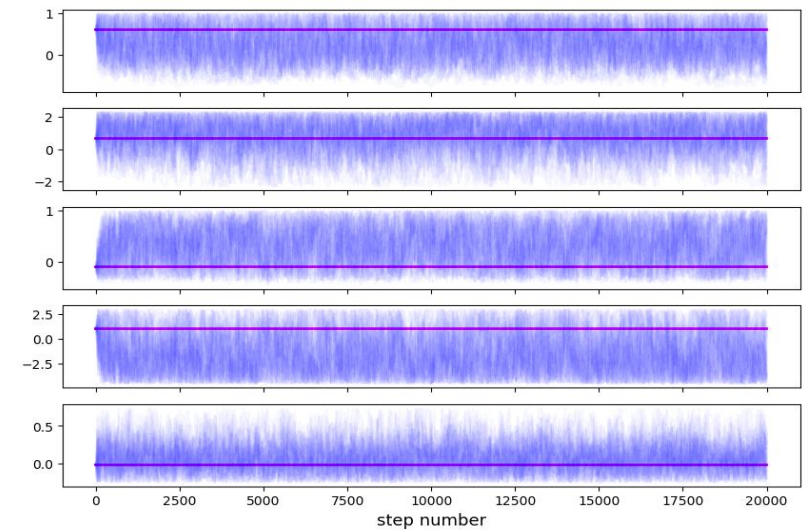
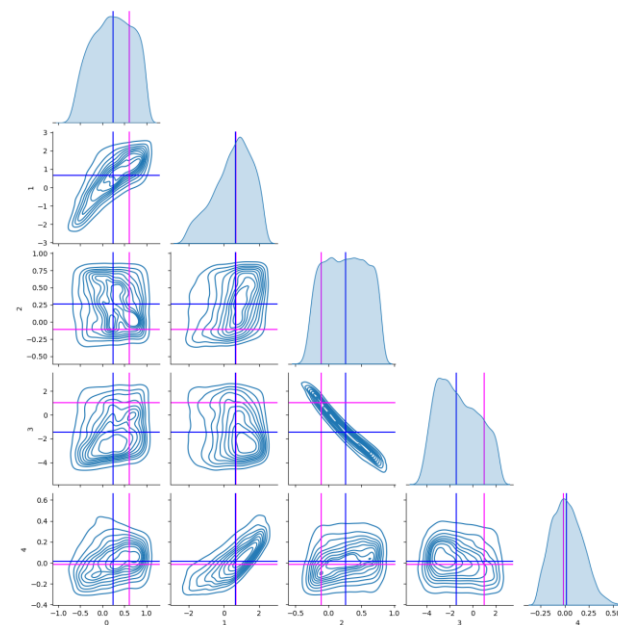
Walkers: $32 \times \# \text{ par}$ (5 phys pars)

2×10^4 steps

$$\begin{aligned} \theta_{\epsilon_e} &= \frac{\epsilon_e}{\bar{\epsilon}_e} - 1 \\ \theta_{\epsilon_b} &= \ln\left(\frac{\epsilon_b}{\bar{\epsilon}_b}\right) \\ \theta_{\Gamma_0} &= \frac{\Gamma_0}{\bar{\Gamma}_0} - 1 \\ \theta_{n_0} &= \ln\left(\frac{n_0}{\bar{n}_0}\right) \\ \theta_p &= \ln\left(\frac{p}{\bar{p}}\right) \end{aligned}$$

MCMC results:

$$\begin{aligned} \epsilon_e &= 0.079_{-0.03}^{+0.03}, & \epsilon_b &= 0.023_{-0.017}^{+0.038}, \\ \Gamma_0 &= 820_{-240}^{+240}, & n_0 &= 0.18_{-0.15}^{+1.55}, \\ p &= 2.04_{-0.29}^{+0.39} \end{aligned}$$



- In this work, we got two main results:
 - we showed the developed analytical method to describe generic broken power law LCs, explaining the workflow for the modelisation of a GRB, with precise estimates of the parameters driving the emission,
 - performed a preliminar study of GRB 221009A - quite good agreement
- To do:
 - production of new data for other sets of parameters
 - try a different function for the *fit – physical parameters* relation
- Better results soon to come!



Thanks for your attention!