Frascati, June 2011

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The CKM Triangle(s) -a Rosetta Stone for Flavour Dynamics

Ikaros Bigi (Notre Dame du Lac)

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or

"The Achaeans outside Troy"

Why "The Achaeans outside Troy"?

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Remember: Achaeans had besieged Troy for more than nine years without success and losing their hero --Achill. They needed a new leader. The favored candidate was Ajax, clearly their strongest fighter. But the Achaeans elected another hero -Odysseus known for his thinking and ideas, not just for his physical strength!

Remember what happened:

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and they took Troy and their prize -Helen, daughter of Zeus!

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(give credit to Homeric Achaeans)

- to find the new dynamics we cannot study only high p_T processes
 - we need `low energies' with precision!

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- the Achaeans knew that beauty existed in the form of Helen they saw Helen from a long distance on the towers of Troy;
- the beauty of New Physics hidden in the SM is implied `only' by theorists!

another lesson from German literature:

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3 examples from FNAL 2nd run:

• D0 data on $A_{SL}(B_s)$: ibi comm.: no way!

• CDF data on $p\bar{p} \rightarrow WjjX$: ibi comm.: maybe??

◆ CDF data on $p\bar{p} \rightarrow t\bar{t}X$: ibi comm.: good chance; CP violation in top prod.?

"Was this the face that launch'd a thousand ships, and burnt the topless towers of Ilium?-"

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Menelaus intending to strike Helen -- struck by her beauty -drops his sword -only true beauty does it!

Outline after the Prologue

I. Nicola Cabibbo - Pioneer of Our View of Weak Forces

II. Cabibbo-Kobayashi-Maskawa Matrix (and Five more)

III. Status of Cabibbo-Kobayashi-Maskawa Matrix

IV. Rosetta Stone for Understanding Flavour Dynamics

V. The Future – and Memory of Nicola Cabibbo



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 in his 1963 PRL Nicolo showed and pointed out importance of weak universality
 ➢ Nicola's task has been achieved!

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 This is even much more true for New Physics!

Cabibbo showed no arrogance and kept a nice sense of irony about theorists' confidence of their understandings!





II. Cabibbo-Kobayashi-Maskawa Matrix (and 5 more)

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`genius loci' of Nagoya University

- home of the Sakata School
 - quarks readily accepted as physical objects

home of Prof. Niu -- expert in cosmic ray experiments in '71 Niu reported a candidate for charm seen

2 complete families were `known'



















I can see the hidden `Helen' on the towers

→ 3 classes of 2 triangles
□
$$\lambda + \lambda + \lambda^5$$

sd triangle: $V^*_{ud}V_{us} + V^*_{cd}V_{cs} + V^*_{td}V_{ts} = \delta_{sd} = 0$ K
cu triangle: $V^*_{ud}V_{cd} + V^*_{us}V_{cs} + V^*_{ub}V_{cb} = \delta_{cu} = 0$
□ $\lambda^{2+} \lambda^{2} + \lambda^{4}$
bs triangle: $V^*_{us}V_{ub} + V^*_{cs}V_{cb} + V^*_{ts}V_{tb} = \delta_{bs} = 0$
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all six triangles have equal area!

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"The" CKM (= Cabibbo-Kobayashi-Maskawa) Triangle bd triangle: $V^*_{ub}V_{ud}$ + $V^*_{cb}V_{cd}$ + $V^*_{tb}V_{td}$ = δ_{bd} = 0 B λ^3 + λ^3 + λ^3 "The" CKM (= Cabibbo-Kobayashi-Maskawa) Triangle bd triangle: $V^*_{ub}V_{ud}$ + $V^*_{cb}V_{cd}$ + $V^*_{tb}V_{td}$ = δ_{bd} = 0 B λ^3 + λ^3 + λ^3

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> sin $2\phi_2 \sim S(B_d \rightarrow \pi^+ \pi^-) = -0.61 \pm 0.08$











reproduced observables spanning several orders of magnitude accommodated with parameter choices

 $|V(us)| \sim 0.22, |V(ts)| \sim 0.04$ $|V(td)| \sim 0.004$ $m_u \sim 5$ MeV, $m_c \sim 1.2$ GeV $m_t \sim 180$ GeV, $m_d \sim 10$ MeV $m_s \sim 0.15$ GeV, $m_b \sim 4.6$ GeV that a priori would seem `frivolous'! There could easily have been inconsistencies!

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Averages of *b*-hadron, *c*-hadron, and τ -lepton Properties

Heavy Flavor Averaging Group (HFAG):

arXiv: 1010.1589 [hep-ex] lists 601 references

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References

[1] N. Cabibbo, Phys. Rev. Lett. 10, 531–533 (1963).

[2] M. Kobayashi and T. Maskawa, Prog. Theor. Phys. 49, 652-657 (1973).

IV. Rosetta Stone for Understanding Flavour Dynamics

Cathedral of Flavour Dynamics has begun

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 $--SM = SU(3)_{C} \times SU(2)_{L} \times U(1) + CKM + PMNS -$
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accidental miracle

`only' thing not even greatest thing

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Have the atrium



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 $--SM = SU(3)_{c} \times SU(2)_{L} \times U(1) + CKM + PMNS --$



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but not completed!

Have the atrium & vestibule & the central nave & an idea about the transept -

but not more!



inspired by Kandinsky's several paintings from 1920's



"Composition VIII" 1923 triangles of different shapes

inspired by Kandinsky's several paintings from 1920's



"Composition VIII" 1923 triangles of different shapes

Kandinsky did not understand that triangles have same area – after all he is not a theorist!

inspired by Kandinsky's several paintings from 1920's





"Composition VIII" 1923 triangles of different shapes

"Black & Violet" 1923 are they triangles, quadrangle, ???

(1) $\lambda^{2+} \lambda^{2} + \lambda^{4}$

bs triangle: $V_{us}^*V_{ub} + V_{cs}^*V_{cb} + V_{ts}^*V_{tb} = \delta_{bs} = 0$ $S(B_s \rightarrow J/\psi \phi)|_{CKM} \sim 0.03$

(1) $\lambda^2 + \lambda^2 + \lambda^4$

bs triangle: V^{*}_{us}V_{ub}+ V^{*}_{cs}V_{cb}+ V^{*}_{ts}V_{tb} = δ_{bs} = 0 B_s S(B_s → J/ψ φ)|_{CKM} ~ 0.03 (2) λ + λ + λ⁵ cu triangle: V^{*}_{ud}V_{cd}+ V^{*}_{us}V_{cs}+ V^{*}_{ub}V_{cb} = δ_{cu} = 0 D S(D⁰ → K_s φ)|_{CKM} ~ 10⁻⁵, S(D⁰ → h⁺h⁻)|_{CKM} ~ 10⁻⁴

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neutrons, protons, deuterons, ...

neutrons, protons, deuterons, ...

and for electrons, muons, τ

neutrons, protons, deuterons, ...

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and CP violations for neutral and charged leptons ...

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a lot to be learnt and done!















"thinkers"







"thinkers"

Schlaeft ein Lied in allen Dingen, Die da traeumen fort und fort, Und die Welt hebt an zu singen, Findst Du nur das Zauberwort.

There sleeps a song in all things That dream on and on, And the world will start to sing, If only you find the magic word.

J. v. Eichendorff

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symmetry

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Thank you, Nicola Cabibbo!

to Madame Cabibbo:

to Madame Cabibbo: in some years from now on people will not remember which physicists were invited to Stockholm or not –

to Madame Cabibbo: in some years from now on people will not remember which physicists were invited to Stockholm or not – they will remember what the legacy was! to Madame Cabibbo: in some years from now on people will not remember which physicists were invited to Stockholm or not – they will remember what the legacy was! Your great(& great)-children can say:

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and scientists will understand it!

