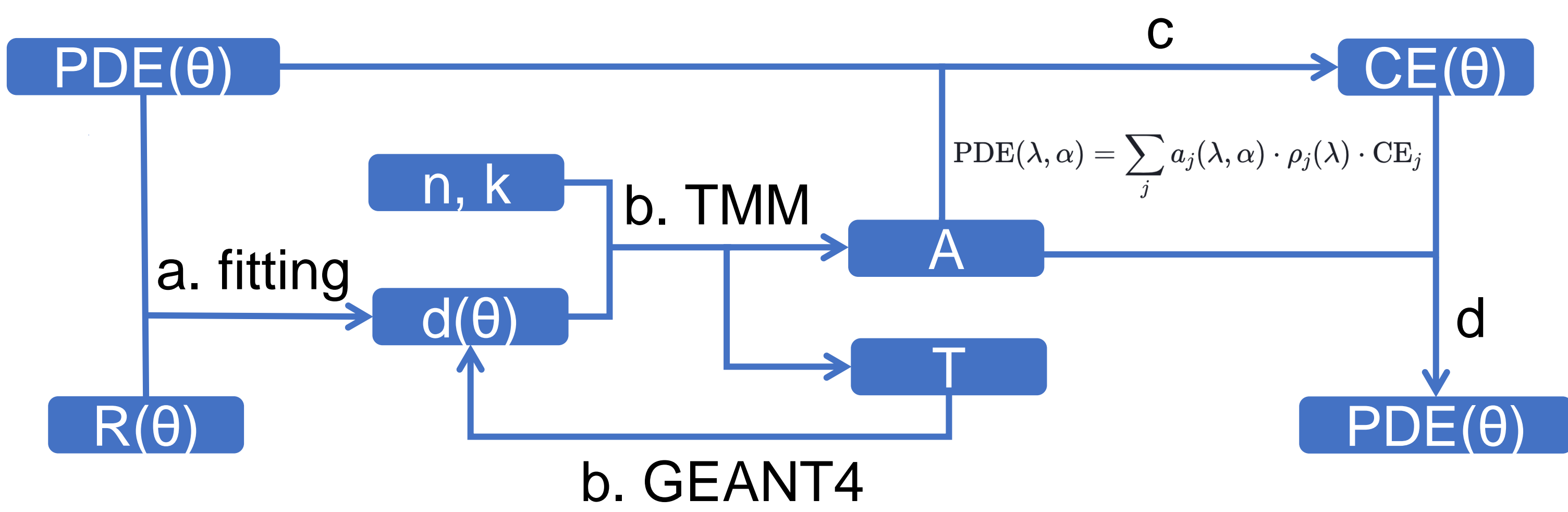
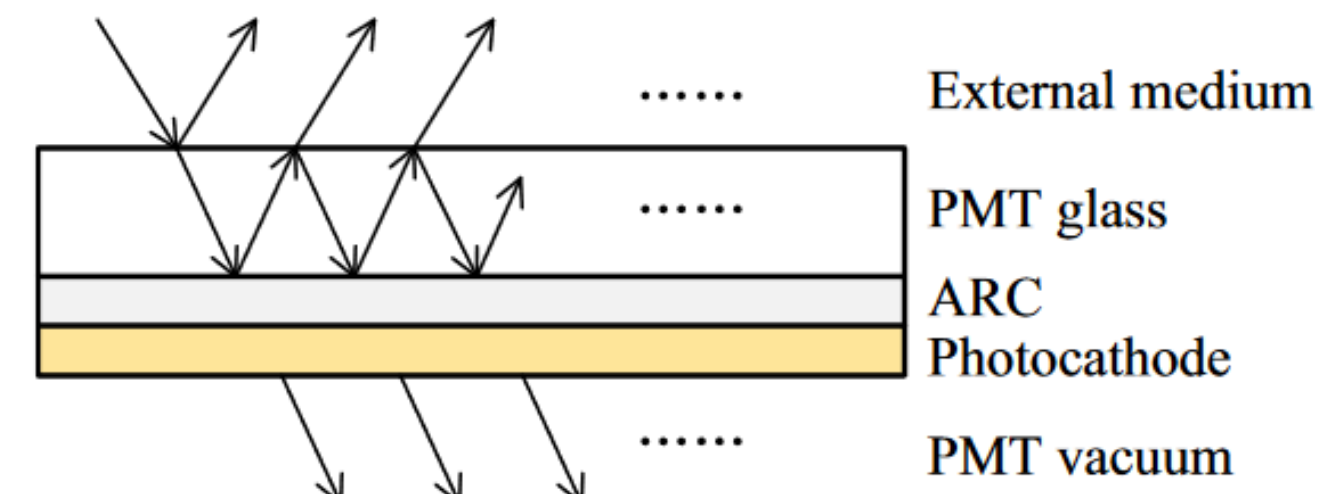


Introduction

- The main goal of JUNO is to determine the neutrino mass ordering.
 - desired energy resolution: 3% @ 1 MeV
- 17,612 20" photomultiplier tubes (PMTs) in central detector
 - 4,997 HPK dynode PMTs and 12,615 NNVT MCP PMTs
 - high photon detection efficiency (PDE) (~29%) [1]
 - large photocathode coverage (~75%)
- An accurate PMT optical model is critical for building a precise simulation and understanding the energy response.
 - PDE angular and spectral responses in water
 - PDE non-uniformity in a single PMT or among PMTs

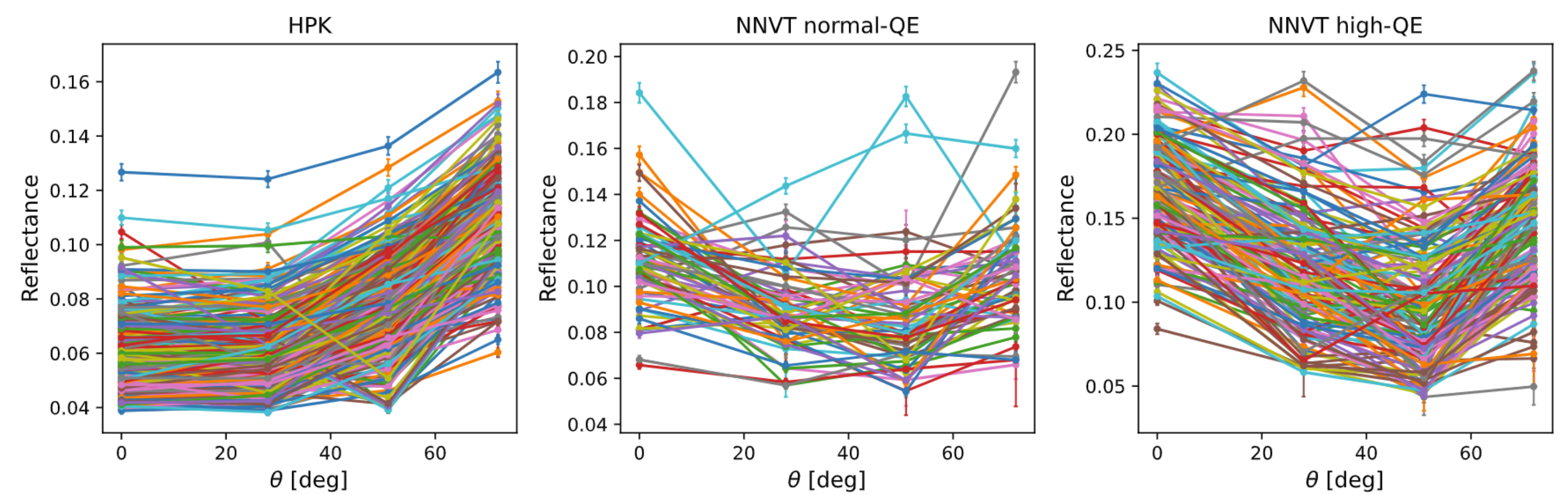
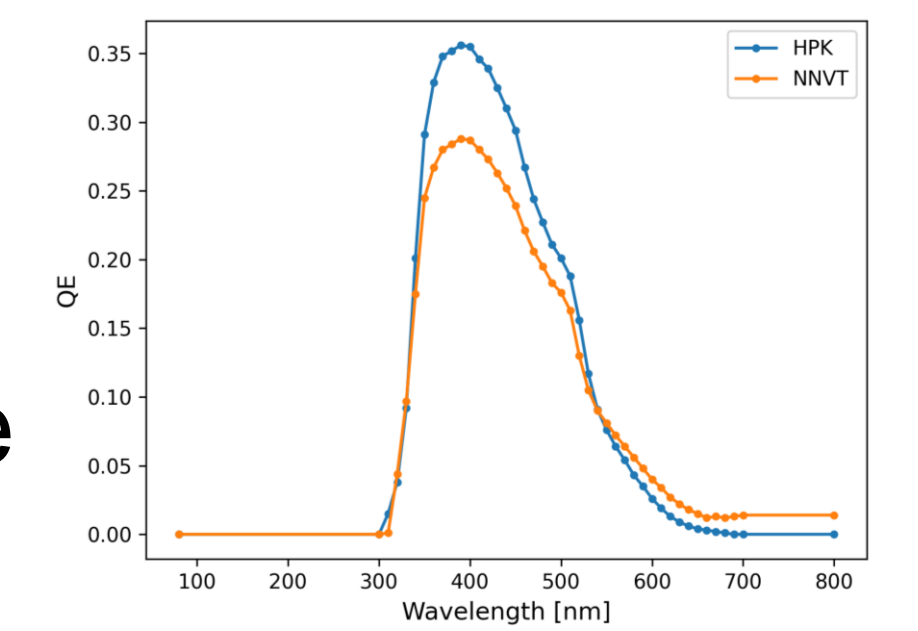
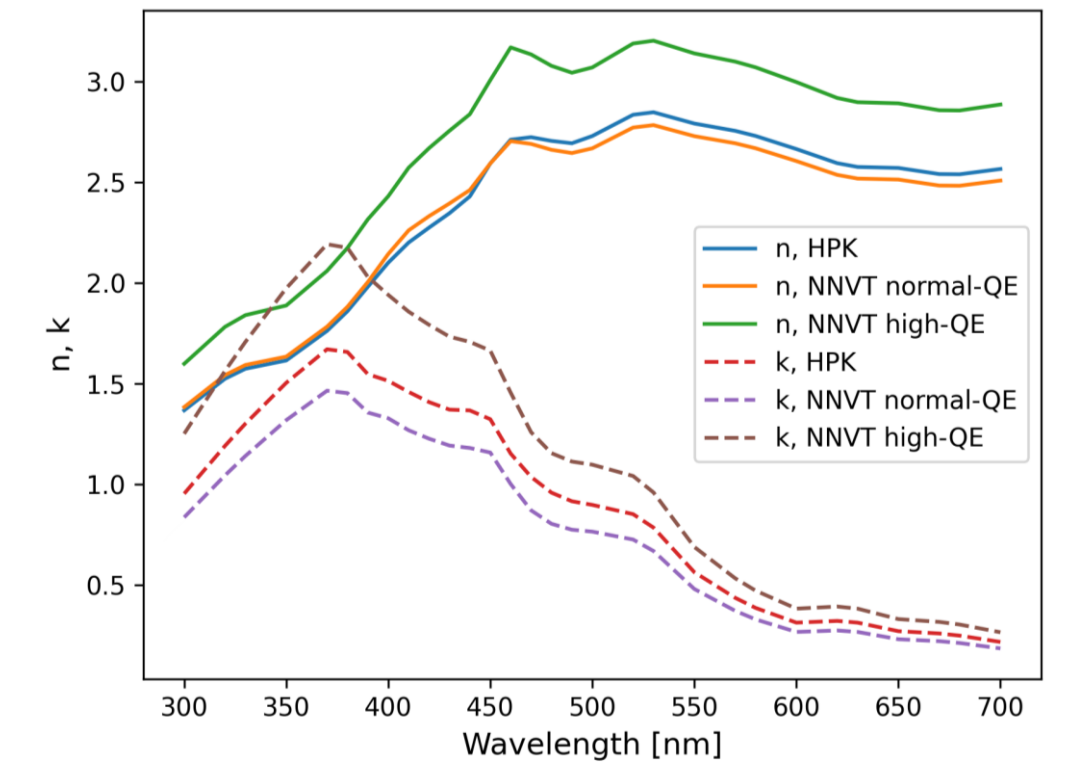
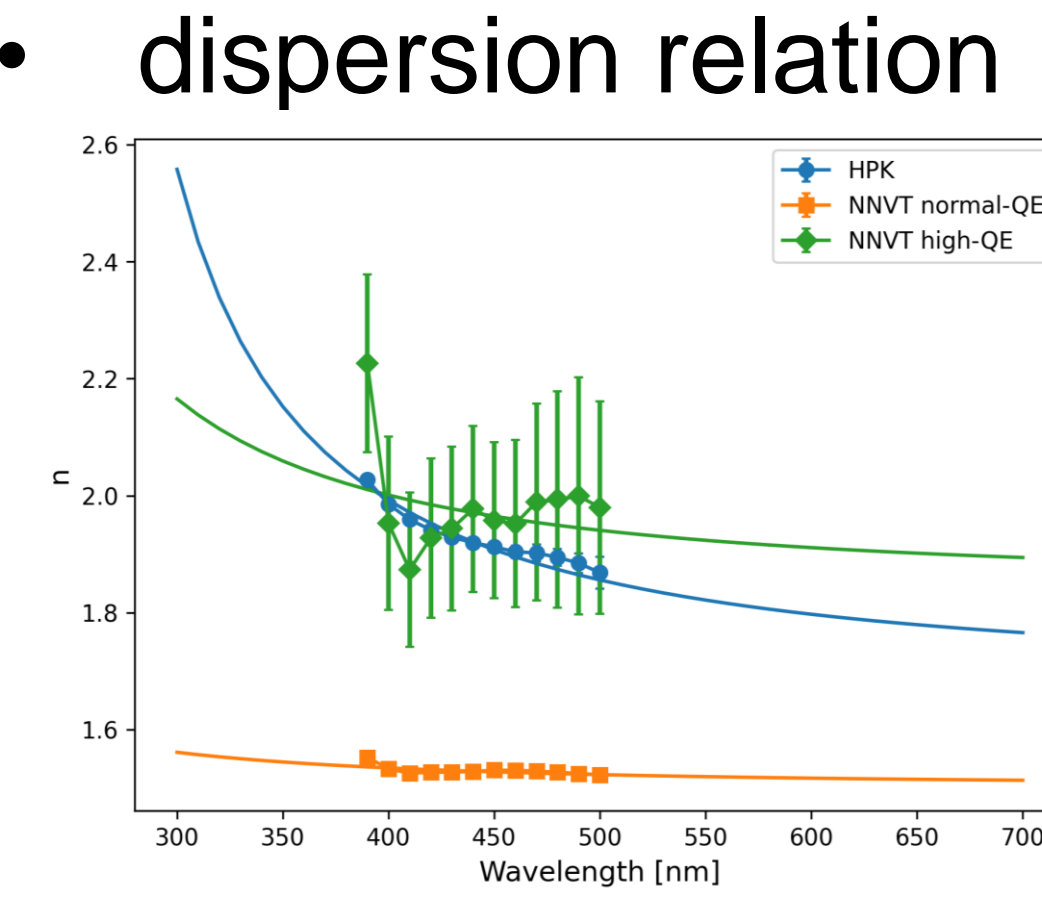
PMT optical model

- Fit $R(\theta)$ and $PDE(\theta)$ to obtain **thickness (d)** of anti-reflective coating (ARC) and photocathode (PC)
 - assume $d(\theta)$ is a quadratic function θ : zenith angle
- Simulate photon absorption and distinguish contributions from incident and transmitted photons [2]
 - transfer matrix method (TMM)
 - reflectance (R)
 - transmittance (T)
 - absorbance (A)
 - GEANT4
 - track the transmitted photons inside PMTs
- Obtain **collection efficiency (CE)** [2]
 - interpolation based on reference points
 - solve the equations
$$PDE(\lambda, \alpha) = \sum_j a_j(\lambda, \alpha) \cdot \rho_j(\lambda) \cdot CE_j \iff \begin{pmatrix} PDE_1 \\ \vdots \\ PDE_n \end{pmatrix} = \begin{pmatrix} \beta_{1,1} & \dots & \beta_{1,n} \\ \vdots & \ddots & \vdots \\ \beta_{n,1} & \dots & \beta_{n,n} \end{pmatrix} \begin{pmatrix} CE_1 \\ \vdots \\ CE_n \end{pmatrix}$$
- Simulate non-uniform PMT **PDE** with angular and spectral dependence using the above equation



Input data for model

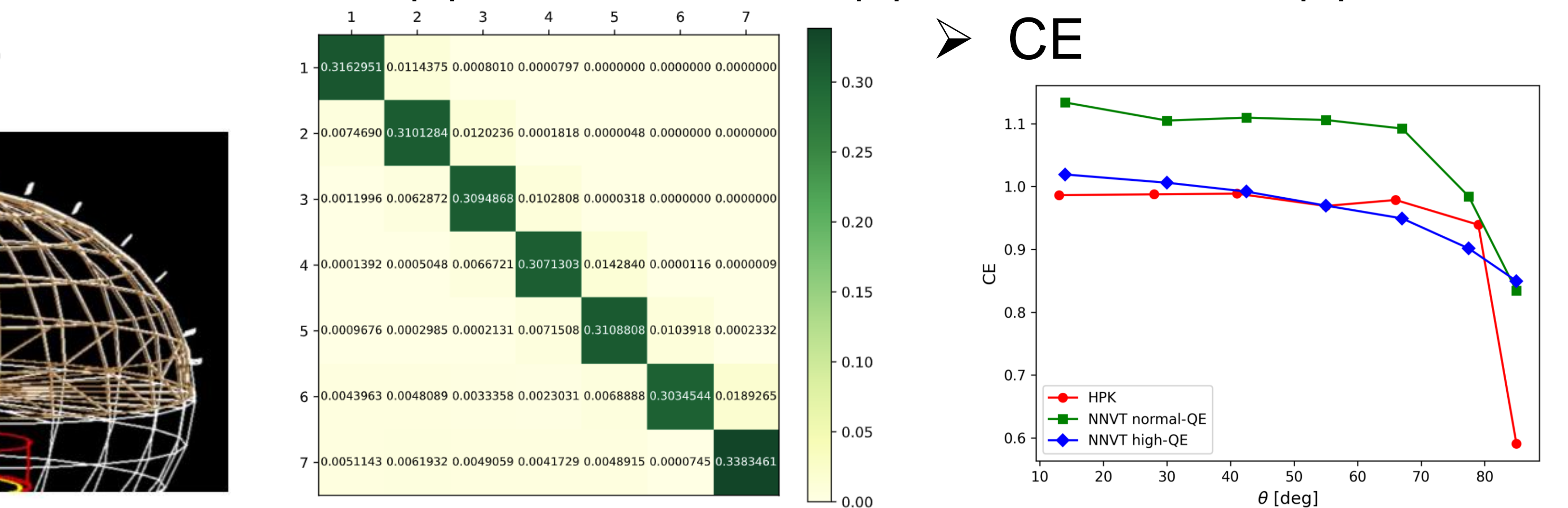
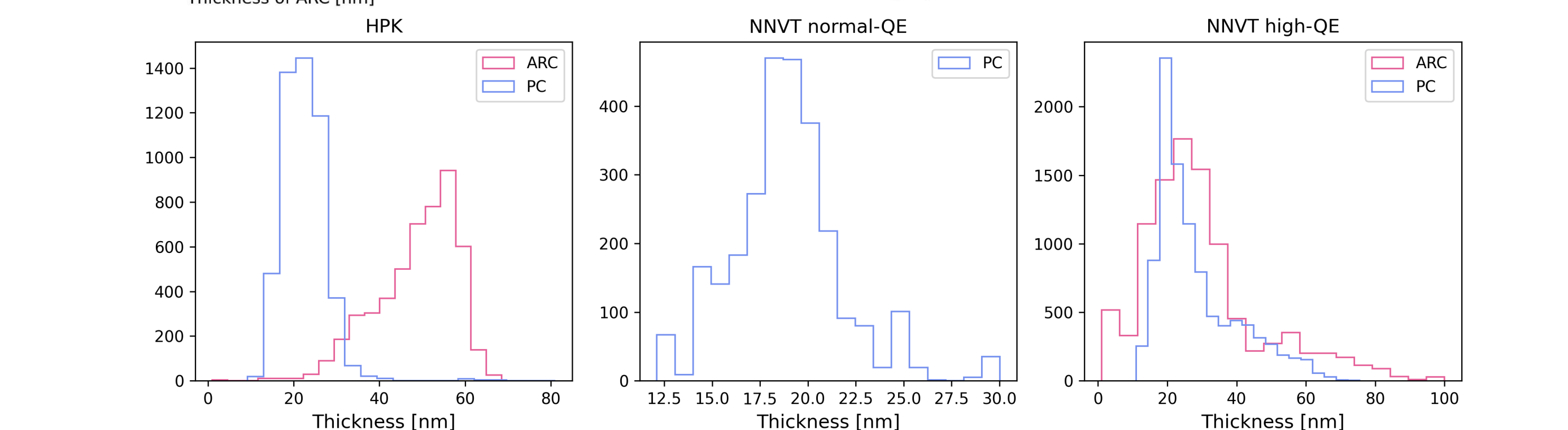
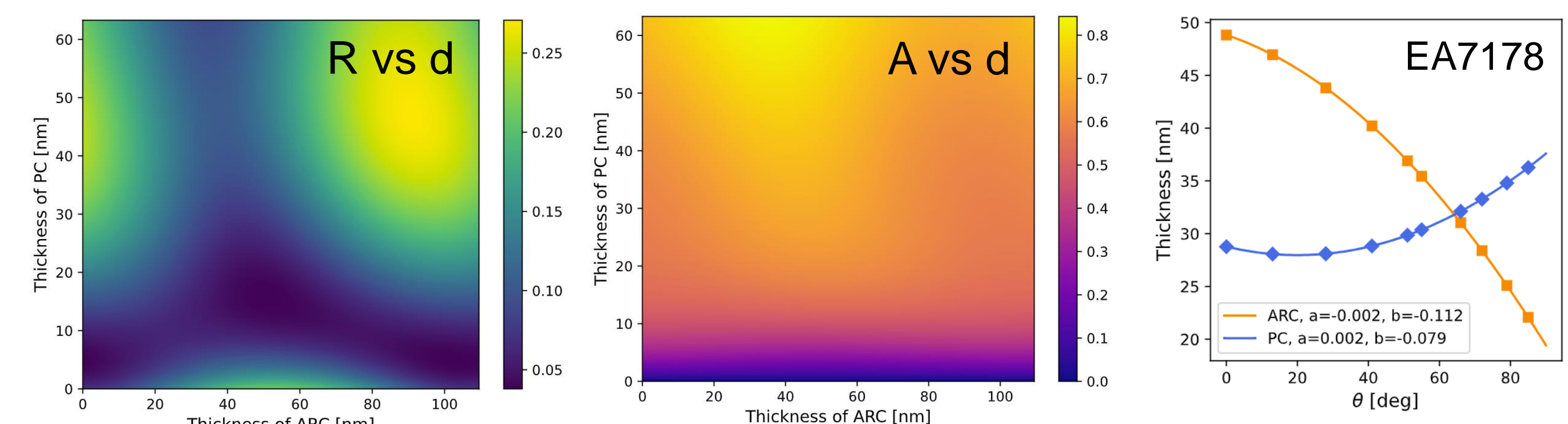
- Refractive index (n) of ARC
 - data from [2]
 - dispersion relation
- Refractive index (n,k) of PC
 - data from [2, 3]
- Quantum efficiency (QE)
 - calculate escape factor = QE/A
 - constrain PDE spectral dependence
- Averaged PDE and PDE(θ) (PDE uniformity)
 - tested in container system and scanning station respectively [1]
- $R(\theta)$
 - tested at 4 zenith angles
 - 8 degree incident angle at 415 nm



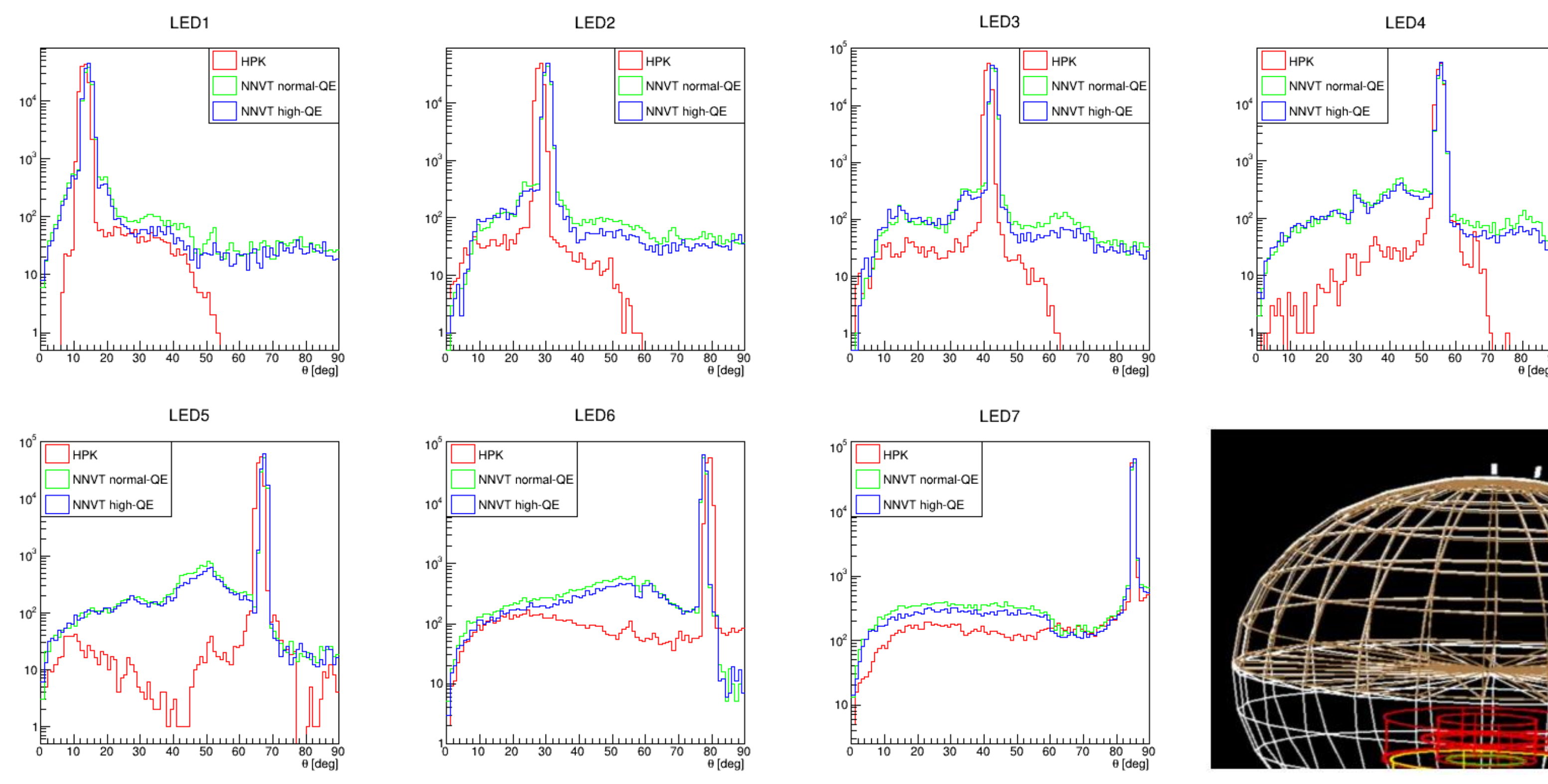
- Generate a random $R(\theta)$ or $PDE(\theta)$ curve sample from data distribution under averaged PDE constraint for PMTs without R or PDE uniformity test

Results

- Thickness of ARC and PC



- Simulate photon absorption position of $PDE(\theta)$



Summary

- A complete PMT optical model for JUNO is established.
- Non-uniform PMT PDE can be simulated with angular and spectral responses.
- The impact of PMT PDE non-uniformity on JUNO energy resolution will be evaluated.

References

- [1] A. Abusleme et al., Mass testing and characterization of 20-inch PMTs for JUNO. Eur. Phys. J. C 82, 1168 (2022).
- [2] Y. Wang et al., A new optical model for photomultiplier tubes, Eur. Phys. J. C 82, 329 (2022).
- [3] S.W. Harmer et al., Variation in optical constants between photocathodes. Nucl. Instrum. Methods A 564(1), 439–450 (2006).