



Analysis of nuclear clustering at intermediate energies with the FOOT experiment

*FOOT Collaboration Meeting
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Introduction to nuclear clustering

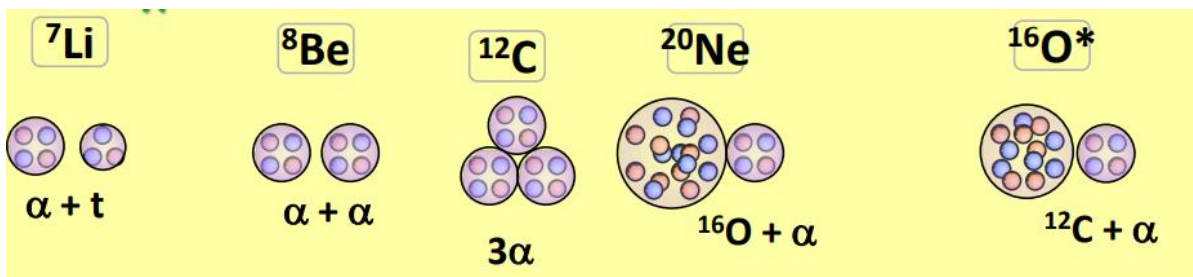
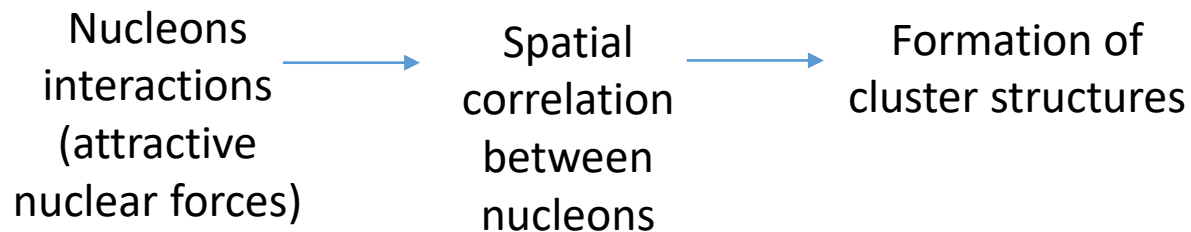


Fig. 1: Typical cluster structures known in the stable nuclei.

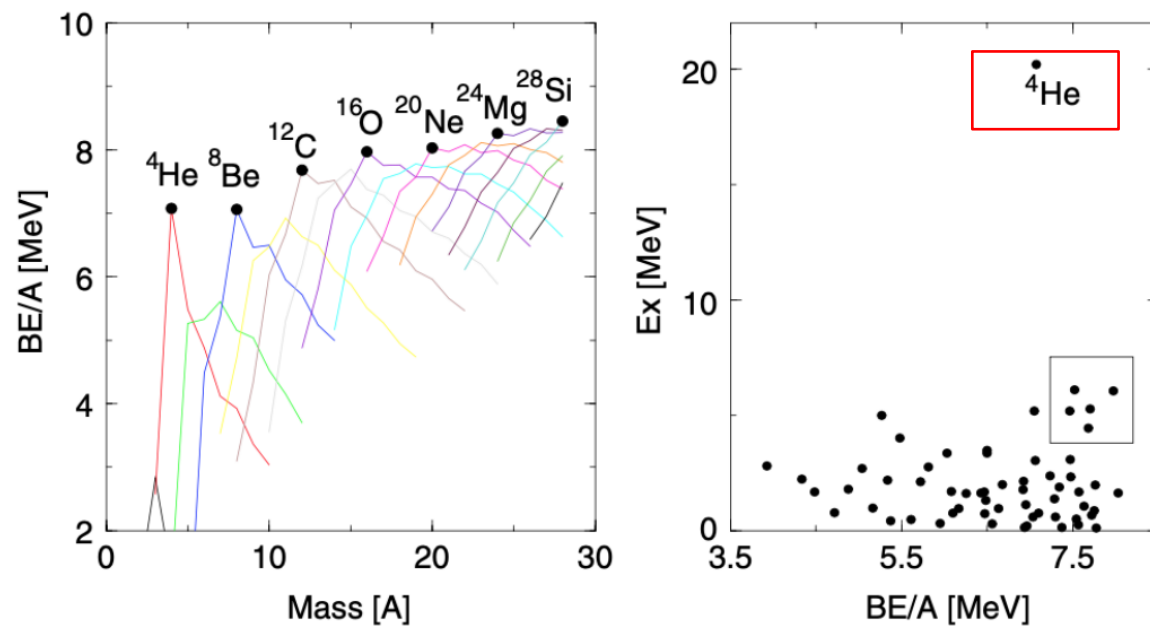


Fig. 2: (Left) Binding energy per nucleon of light nuclear systems up to $A = 28$. (Right) Excitation energy of first excited states plotted versus binding energy per nucleon for nuclei up to $A = 20$.

[M. Freer. *Reports on Progress in Physics*, 70(12):2149, (nov 2007)]

Introduction to nuclear clustering

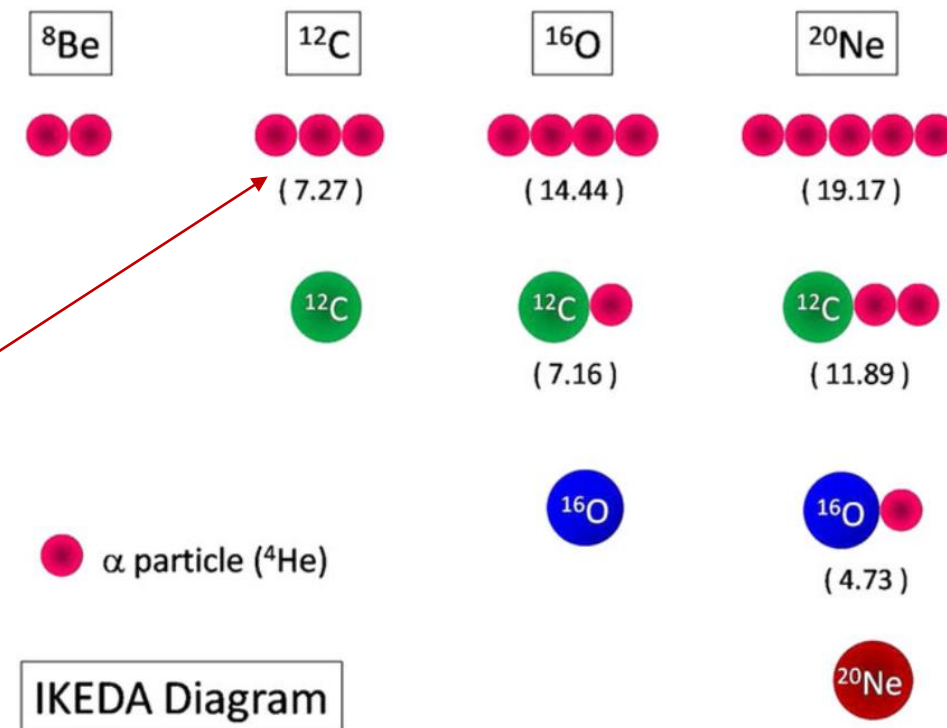
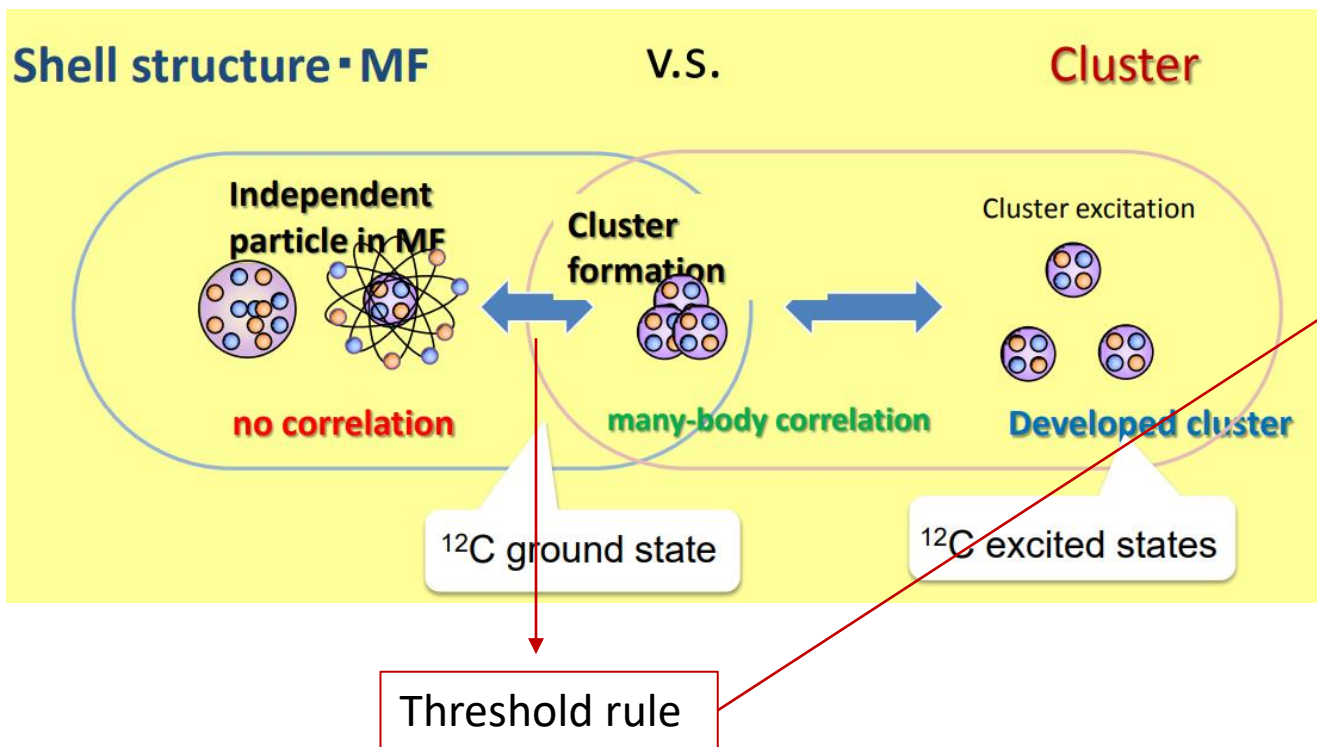
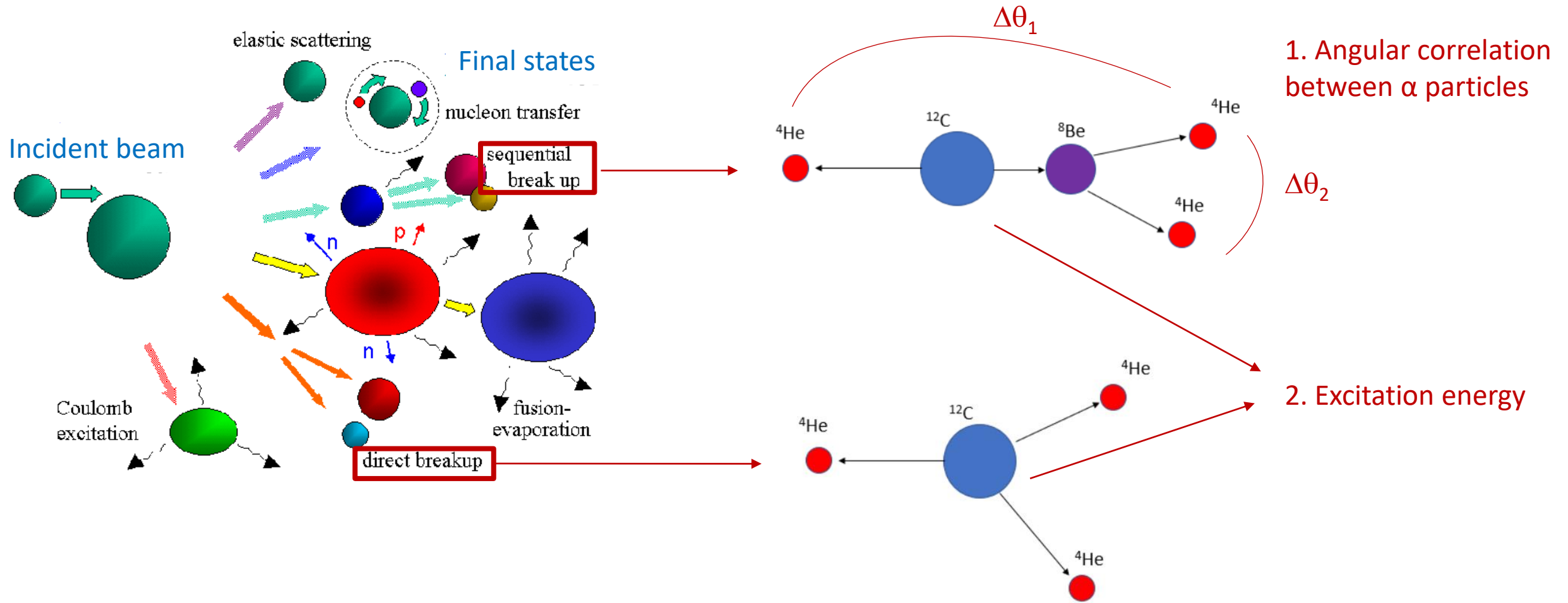


Fig. 3: The so-called 'Ikeda' diagram showing how above particle-breakup thresholds, the structure of light α -conjugate nuclei can be thought of as comprised of α clusters.

[K. Ikeda, et al. *Progress of Theoretical Physics Supplement*, E68:464–475, 07 (1968)]

Techniques for the study of clusters in nuclei



Experimentally Observed Clusters in α -Particle Nuclei at **low energies** in literature

Excitation energy: ${}^8\text{Be}$ \longrightarrow Yields of correlated 2α emissions

${}^{40}\text{Ca} + {}^{12}\text{C}$ at 25 MeV/u

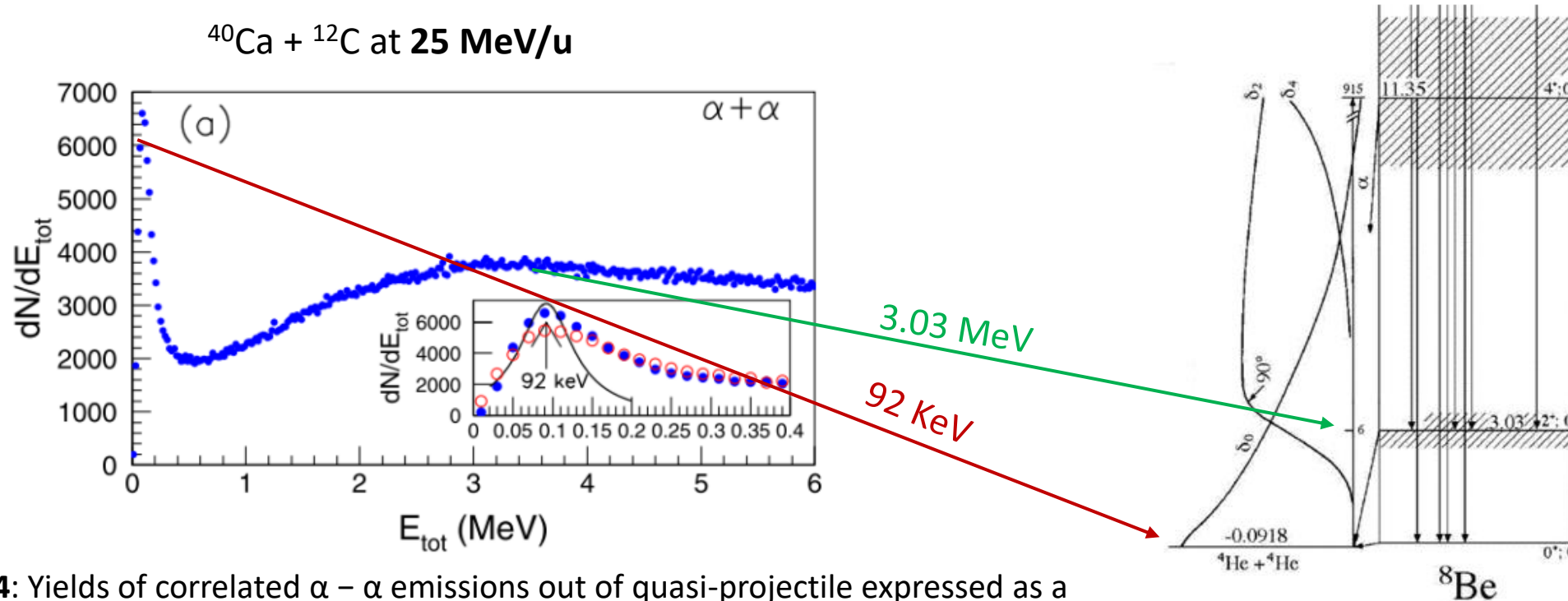


Fig. 4: Yields of correlated $\alpha - \alpha$ emissions out of quasi-projectile expressed as a function of total kinetic energy. The inset corresponds to zooms on the ${}^8\text{Be}$ peak.

[Ad.R. Raduta, et al. *Physics Letters B*, 705(1):65–70, (2011)].

Experimentally Observed Clusters in α -Particle Nuclei at **low energies** in literature

Excitation energy: ^{12}C \longrightarrow Yields of correlated 3α emissions

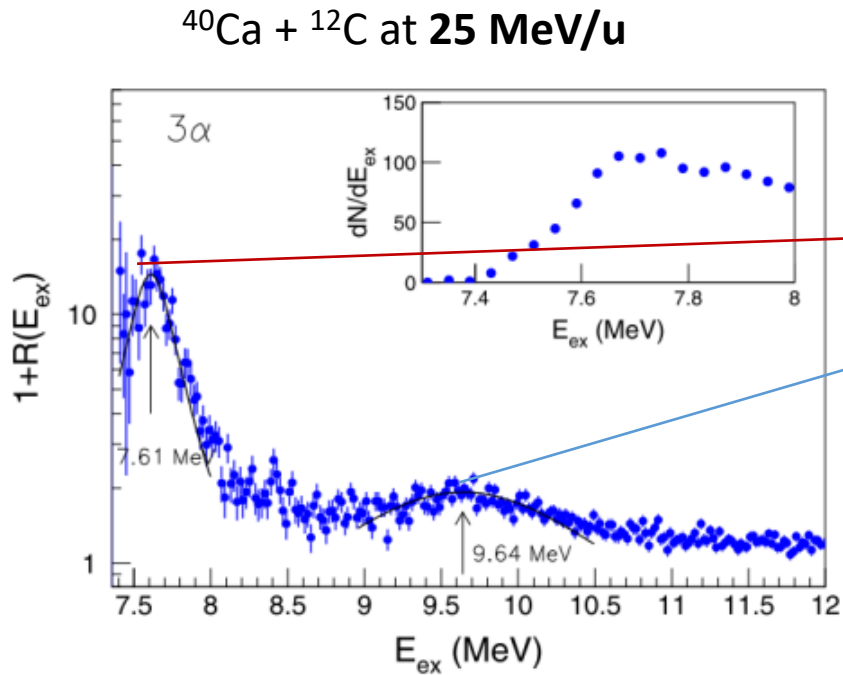


Fig. 5: 3α correlation function as a function of excitation energy.

[Ad.R. Raduta, et al. *Physics Letters B*, 705(1):65–70, (2011)].

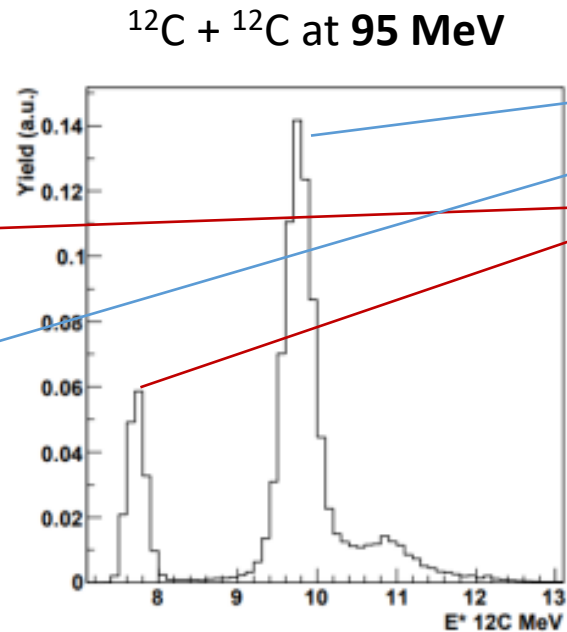
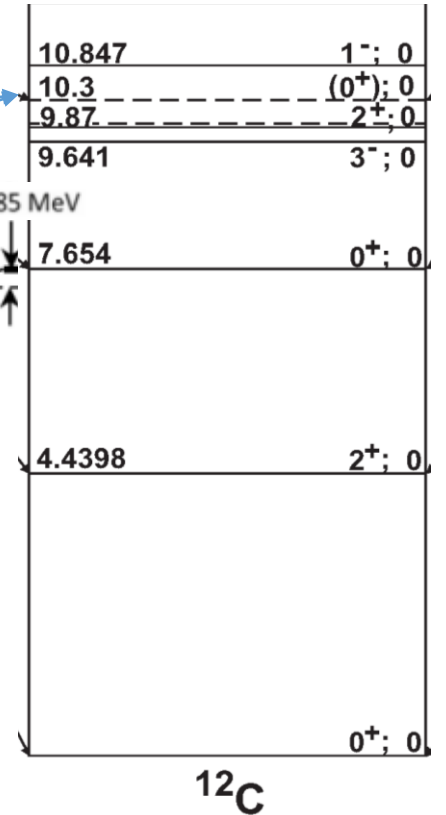


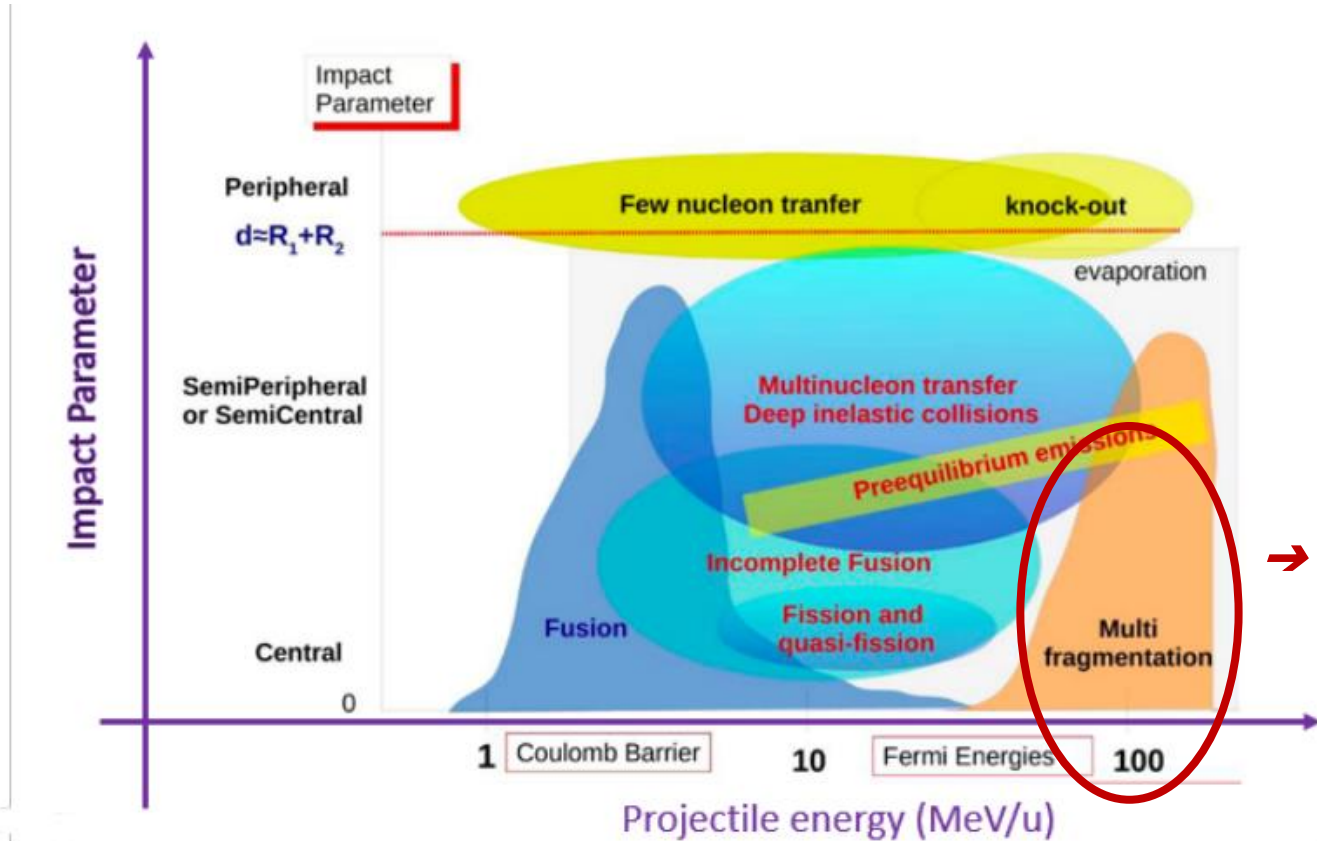
Fig.6: Excitation energy spectrum for the breakup of ^{12}C into three α -particles

[L. Morelli, et al. *Annual Report Laboratori Nazionali di Legnaro INFN* (2014)].



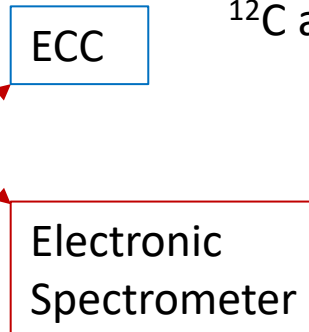
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Experimentally Observed Clusters in α -Particle Nuclei at **intermediate energies**



[G. De Lellis, et al. *Nuclear Physics A*, 853(1):124–134, (2011)]

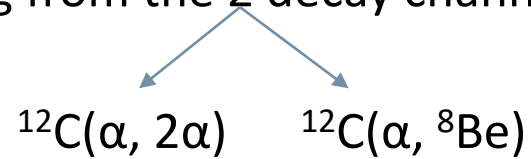
→ *The FOOT experiment*



^{12}C at 400 MeV/u
HIMAC

Performed analyses

Aim: exploring the possibility to analyze α clustering phenomenology through the FOOT experiment by quantifying α correlation arising from the 2 decay channels of ^{12}C .



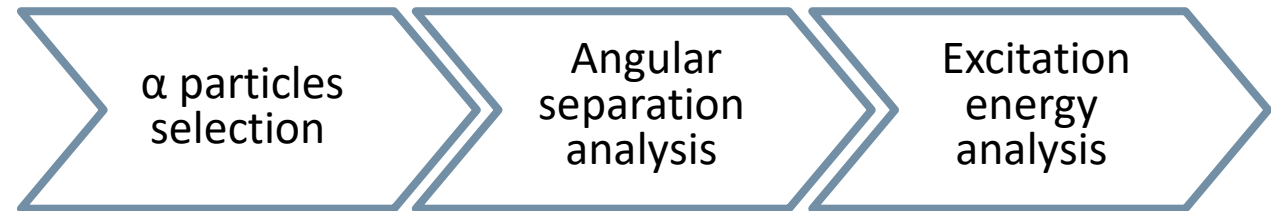
MC Simulation:

- $^{12}\text{C} + ^{12}\text{C}$ at **200 MeV/u** with the full FOOT experimental setup;
- Campaign: **12C_C_200_2023v2**;
- **5.000.000** simulated primaries.

MC Truth

Reconstruction:

- **7** points for reconstruction;
- **5.000.000** reconstructed events.



In this presentation, for the first time, we attempt to use reconstructed tracks by SHOE (Genfit) using a full magnetic setup

α particles selection

MC Truth

- Particle generated from a primary;
- Particle forward directed (initial momentum > 0);
- Production region: TGT;
- Detection region: TW;
- Angular acceptance: 10° ;
- Initial Kinetic energy > 50 [MeV/u];
- Charge = 2;
- Baryonic number = 4;

Reconstruction

- Detection region: TW;
- Reconstruction charge from TW = 2;
- Reconstructed mass in range $3.2 \div 4.3 \text{ GeV}/c^2$;

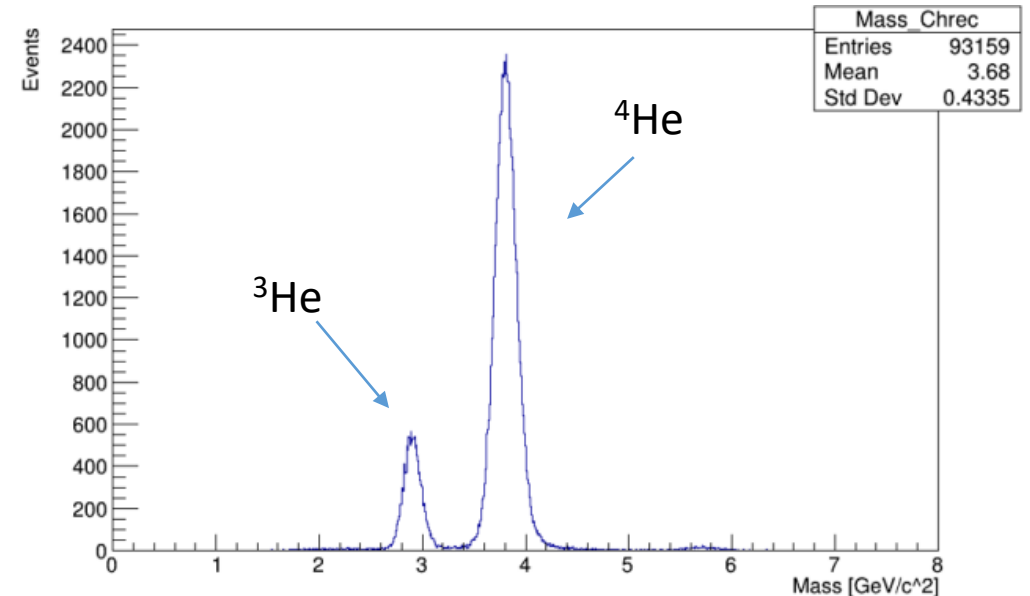


Fig. 7: Reconstructed mass distribution of reconstructed particles with the reconstructed charge $Z_{\text{rec}} = 2$ generated on target that arrive on TW.

α particles selection

from the
GetMcMainTrackId();

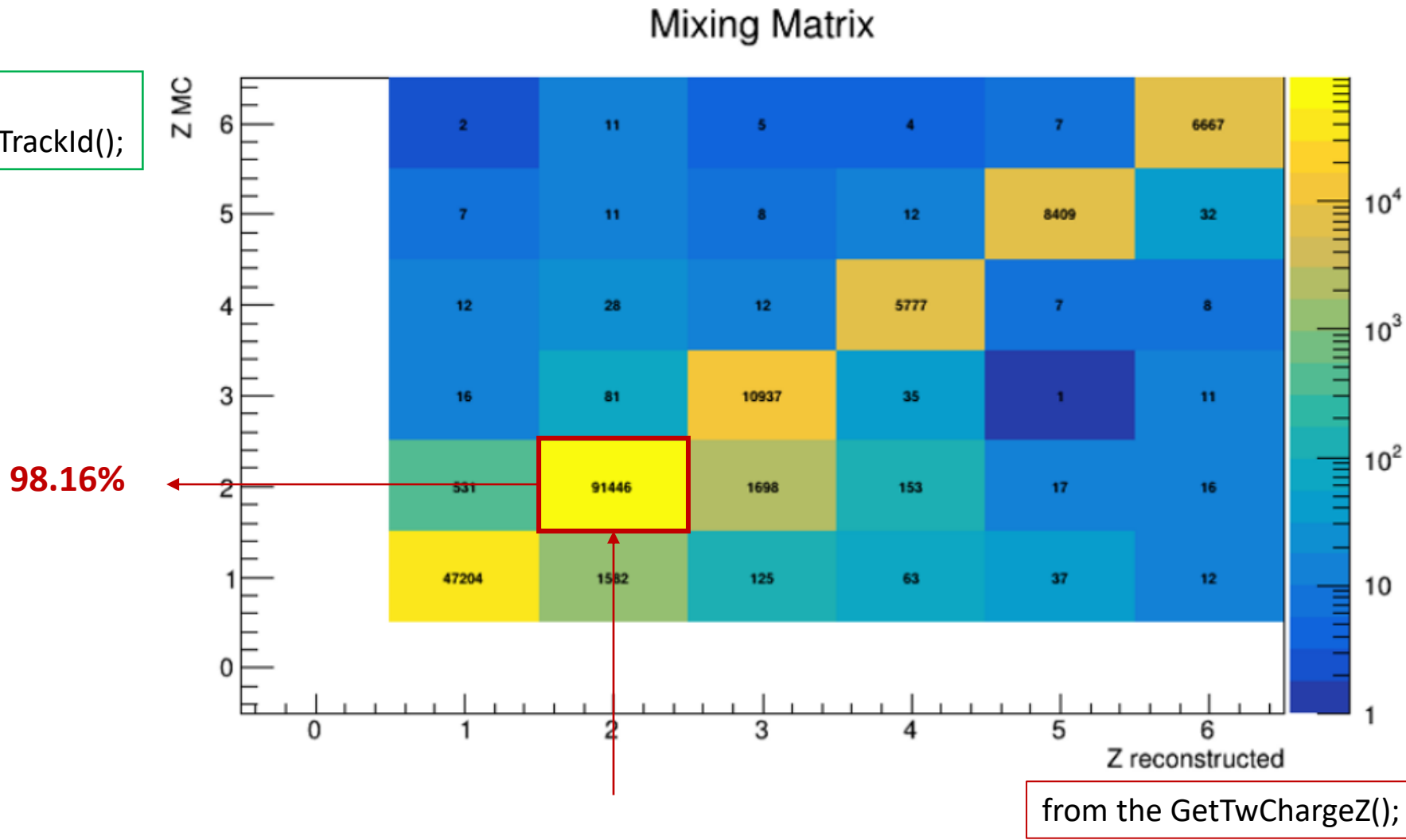


Fig. 8: Correlation between the charge reconstructed by the TW and the MC charge.

Angular Separation Analysis

MC Truth

$$p_k = \sqrt{P_{x_k}^2 + P_{y_k}^2 + P_{z_k}^2};$$

$$\Delta\theta = \arccos\left(\frac{P_{x_i}P_{x_j} + P_{y_i}P_{y_j} + P_{z_i}P_{z_j}}{p_i p_j}\right)$$

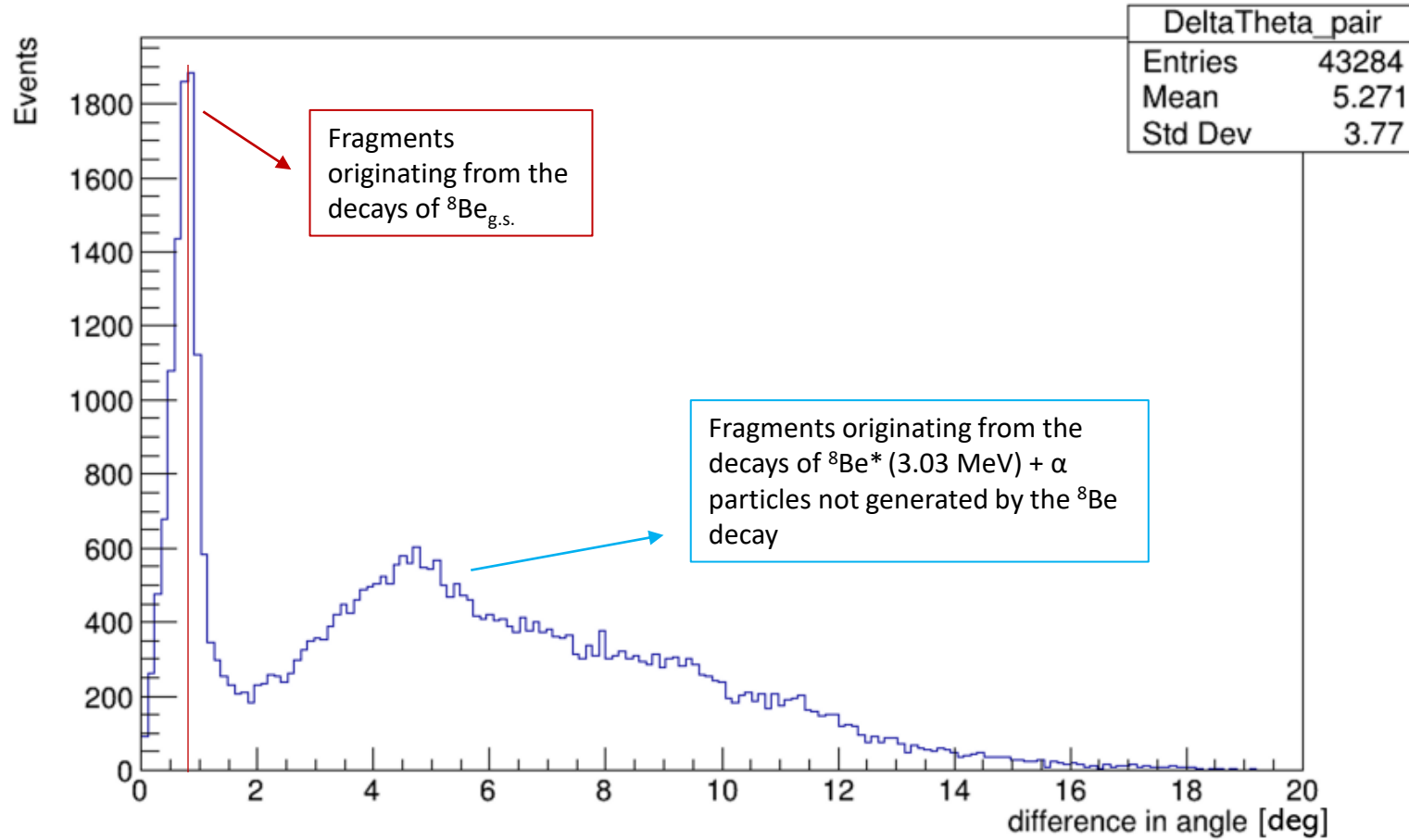


Fig. 9: Opening angle between pairs of MC simulated α particles **out of target** from events producing two and three α particles together

Angular Separation Analysis

Reconstruction

Reconstruction efficiency:

$$Eff = \frac{\text{Number of reconstructed } \alpha \text{ particles}}{\text{Number of MC } \alpha \text{ particles}} = 67.2\%$$

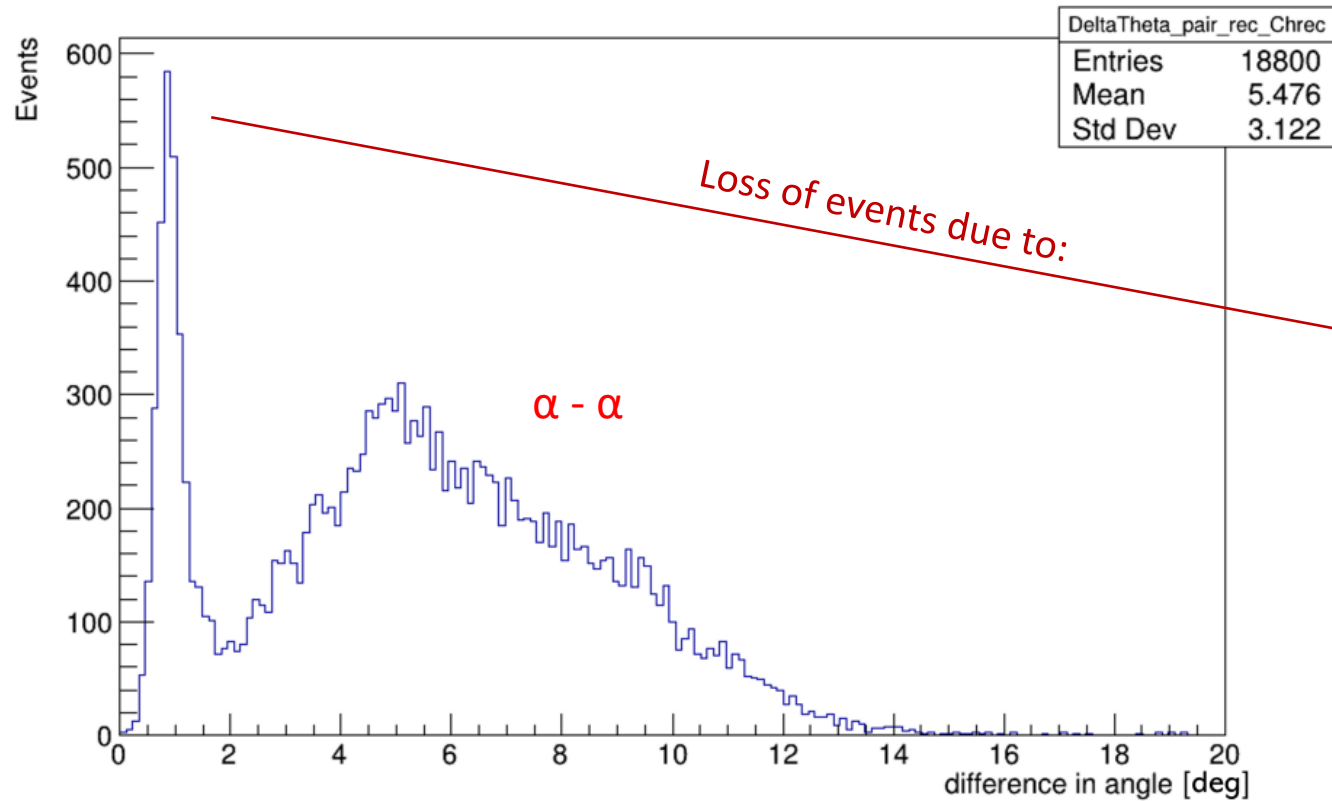


Fig. 10: Opening angle between **pairs of reconstructed α particles at TW** from events producing two and three α particles together.

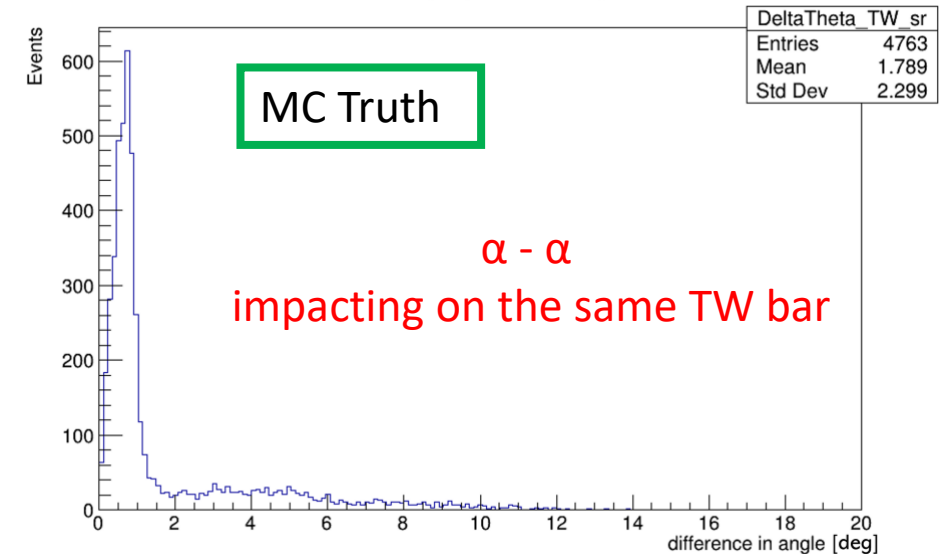
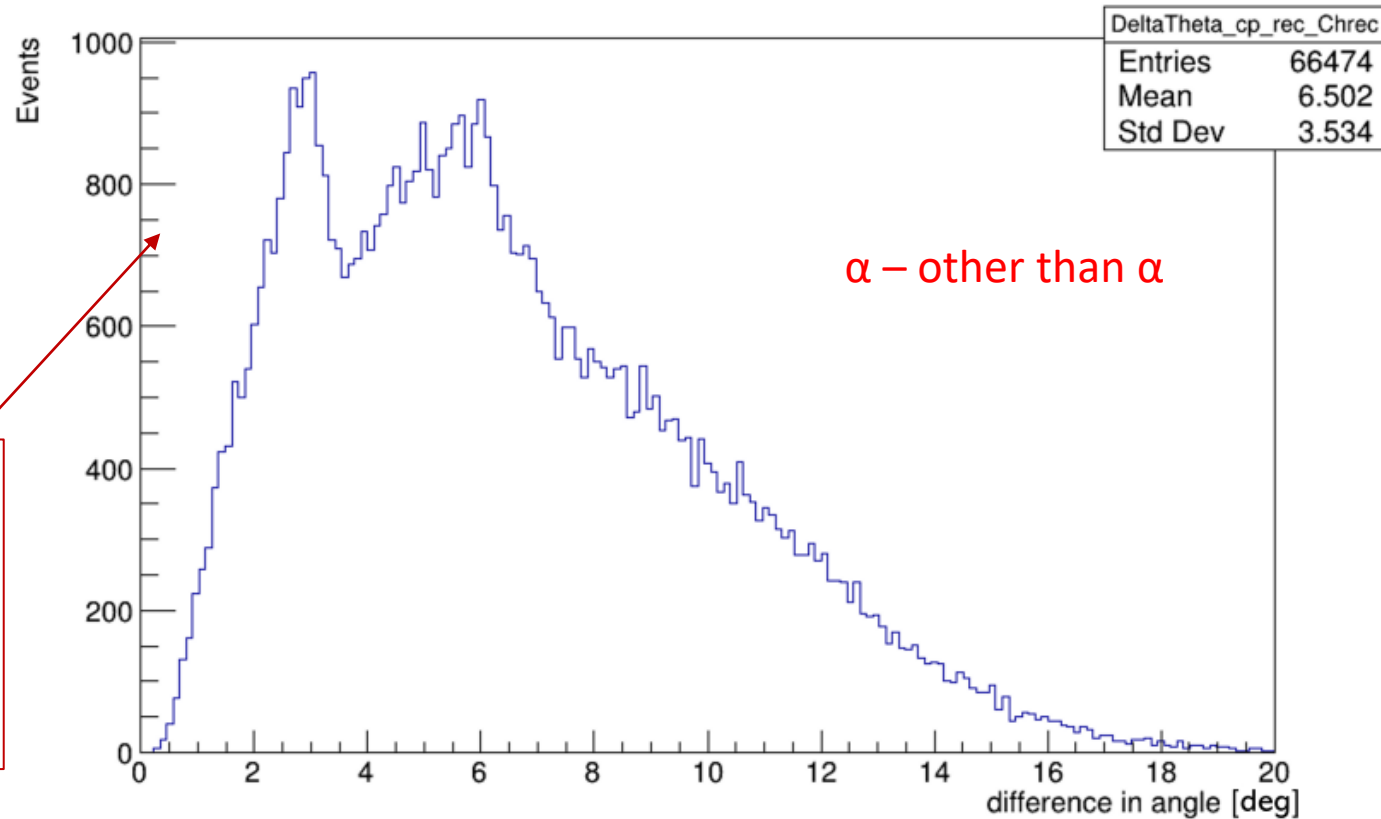


Fig. 11: Opening angle between pairs of MC α particles at TW **impacting on the same TW bar** from events producing two and three α particles together.

Angular Separation Analysis

Reconstruction



No angular correlations between particles are visible at angle of 0.6° .

Fig. 12: Opening angle on TW between reconstructed α and particles other than ^4He .

Excitation energy Analysis: ${}^8\text{Be} \longrightarrow {}^{12}\text{C}(\alpha, {}^8\text{Be})$

MC Truth

$${}^8\text{Be} E_{ex} = \sqrt{(E_{kin_i} + E_{kin_j} + 2m_\alpha)^2 - (\bar{p}_i + \bar{p}_j)^2} - 2m_\alpha$$

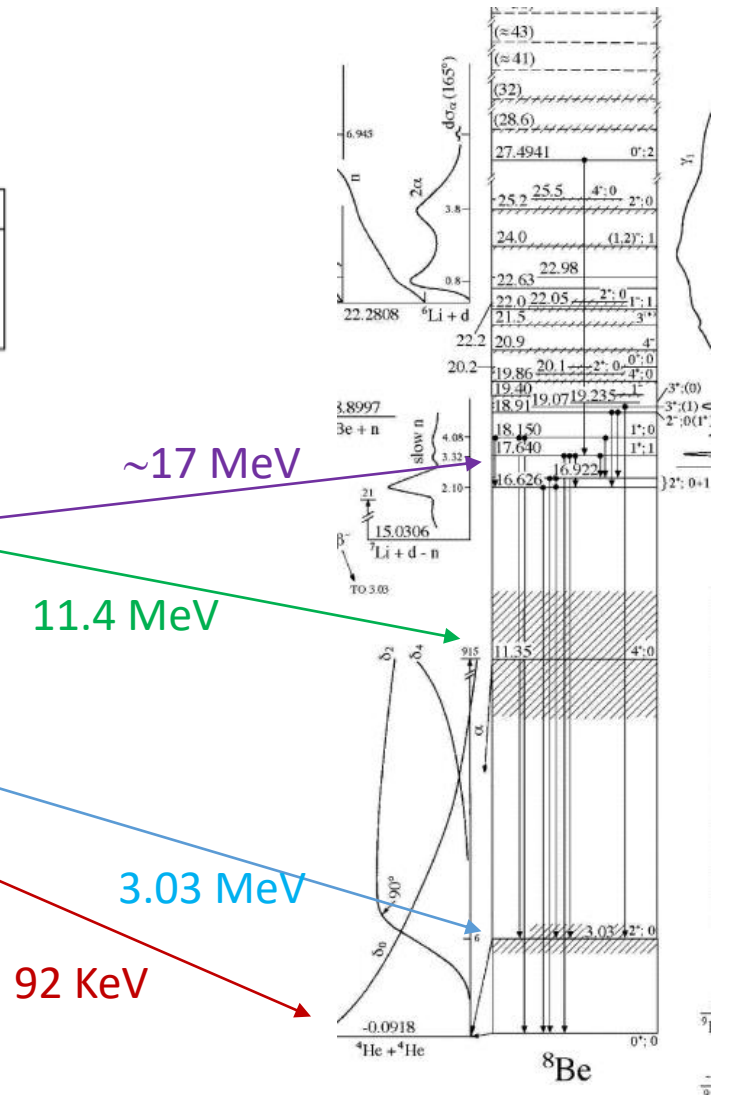
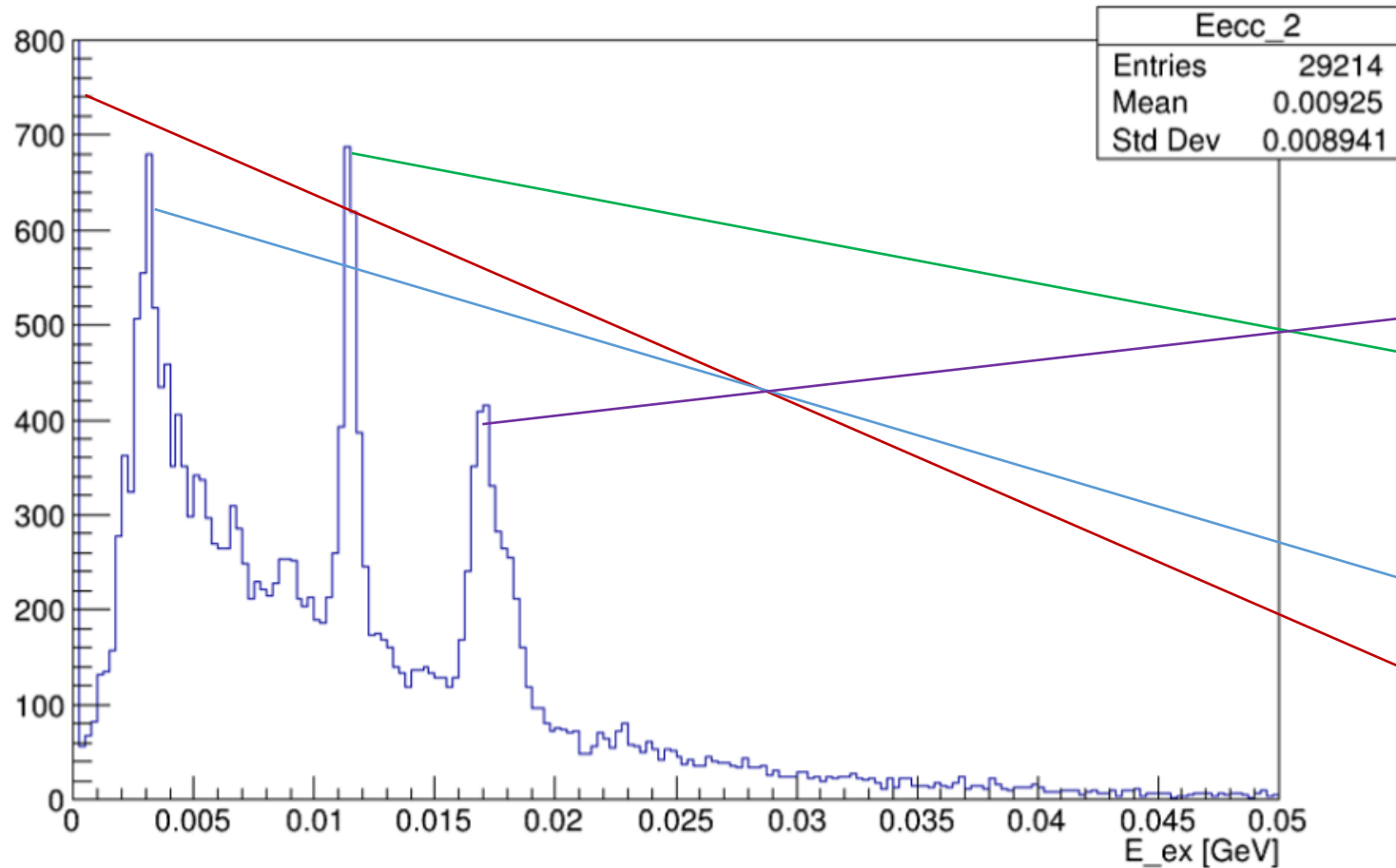


Fig. 13: Excitation energy spectrum for the breakup of ${}^8\text{Be}$ intermediate stage of ${}^{12}\text{C}$ into two α particles from MC α particles analysis.

Excitation energy Analysis: ${}^8\text{Be} \longrightarrow {}^{12}\text{C}(\alpha, {}^8\text{Be})$

MC Truth

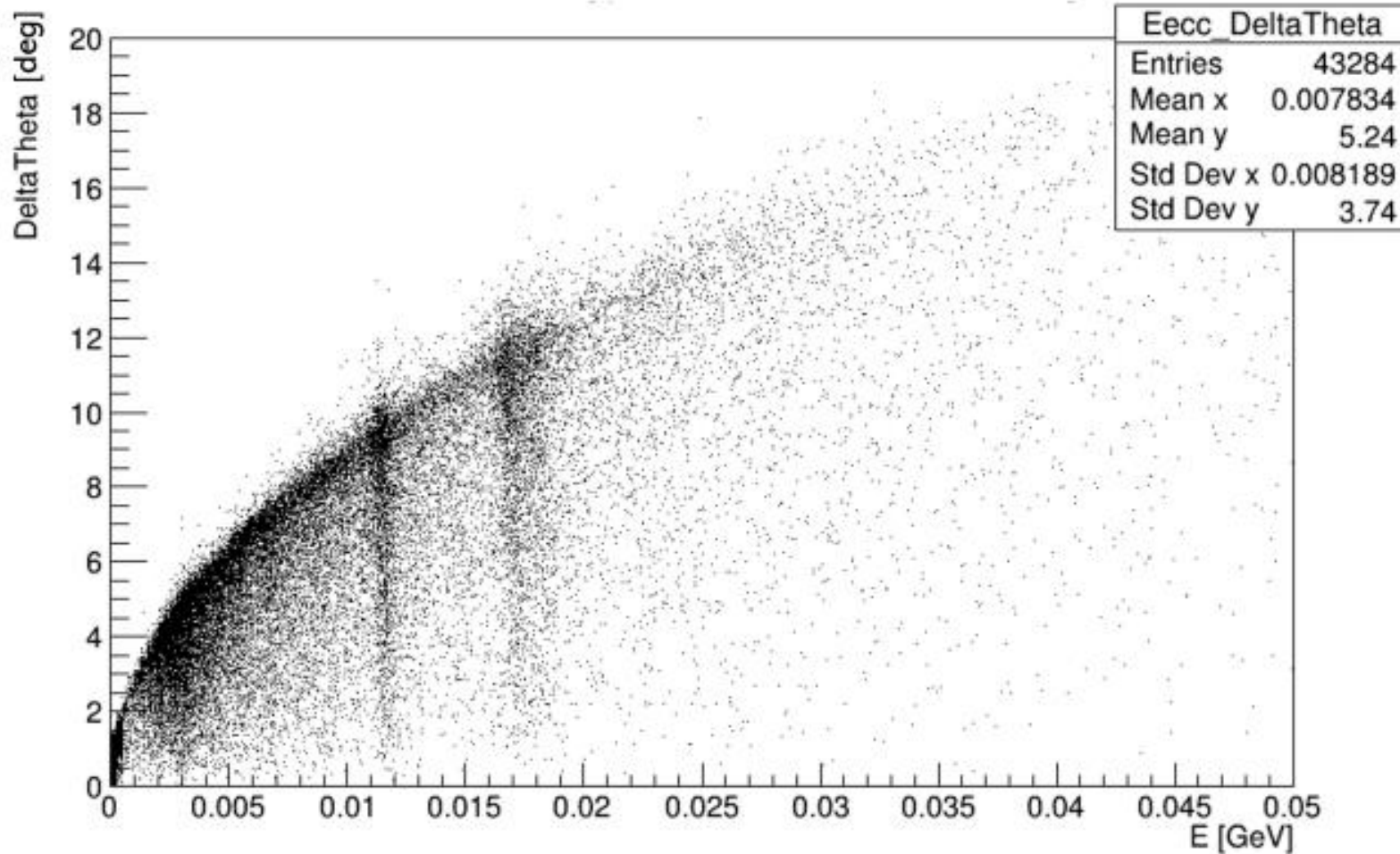


Fig. 14: Excitation energy spectrum of the breakup of ${}^8\text{Be}$ intermediate stage of ${}^{12}\text{C}$ into 2 α particles VS the opening angular distribution between α particles in the MC Truth analysis.

Excitation energy Analysis: $^8\text{Be} \rightarrow ^{12}\text{C}(\alpha, ^8\text{Be})$

Reconstruction

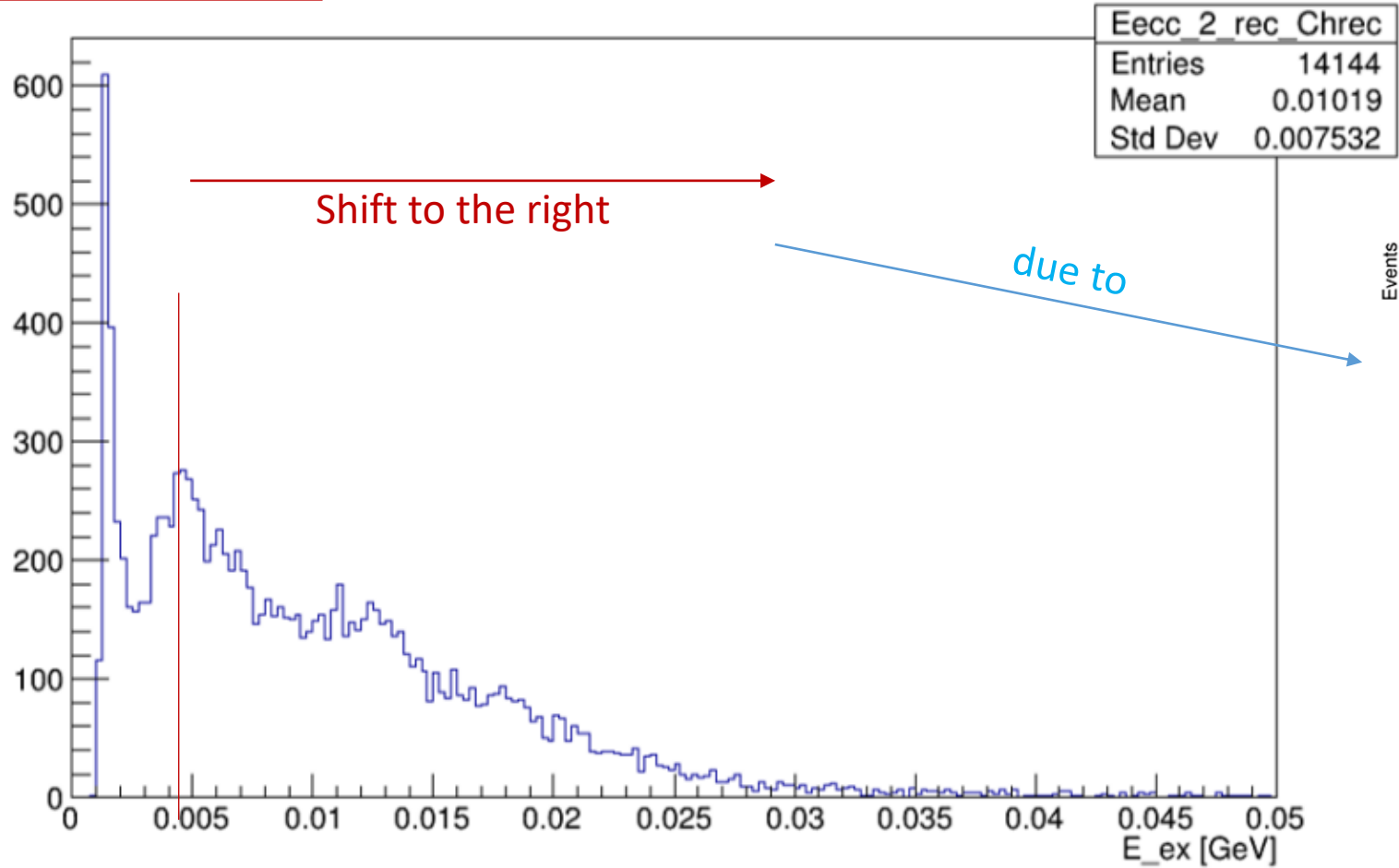


Fig. 15: Excitation energy spectrum for the breakup of ^8Be intermediate stage of ^{12}C into 2 α particles from reconstructed α particles analysis.

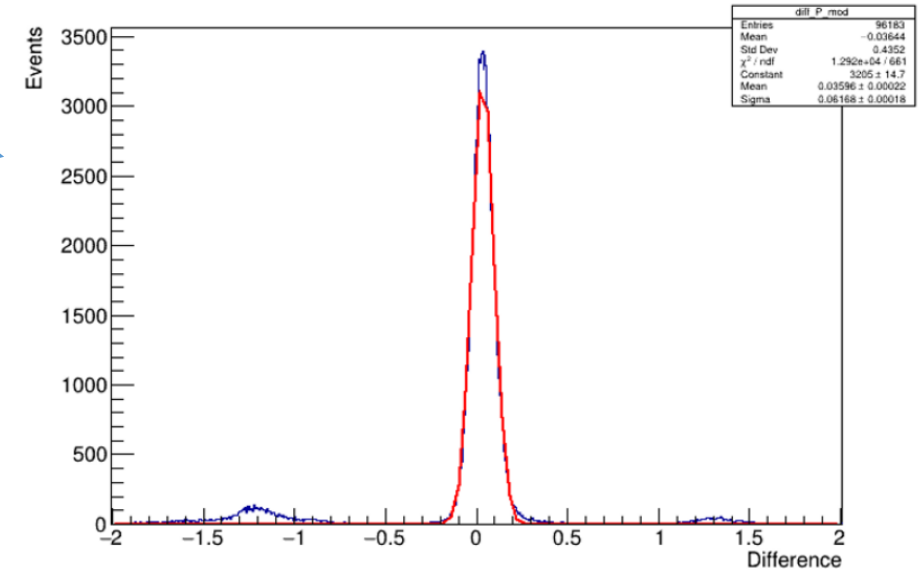


Fig. 16: Difference between the modulus of reconstructed and MC momenta. In red is reported the Gaussian distribution.

Excitation energy Analysis: $^{12}\text{C} \longrightarrow ^{12}\text{C}(\alpha, 2\alpha)$

$$^{12}\text{C} E_{ex} = \sqrt{(E_{kin_i} + E_{kin_j} + E_{kin_k} + 3m_\alpha)^2 - (p_i + p_j + p_k)^2} - 3m_\alpha$$

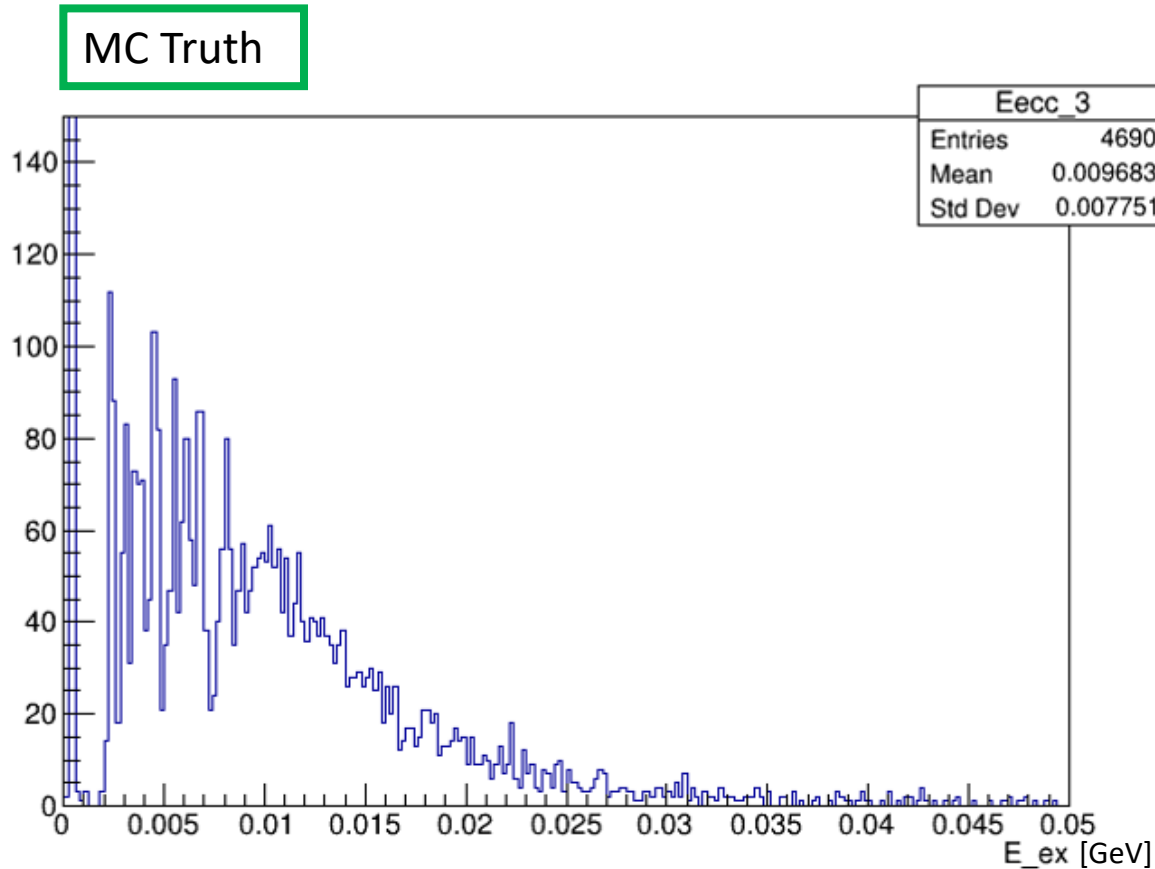


Fig. 17: Excitation energy spectrum for the breakup of ^{12}C into 3 α particles from MC Truth α particles analysis.

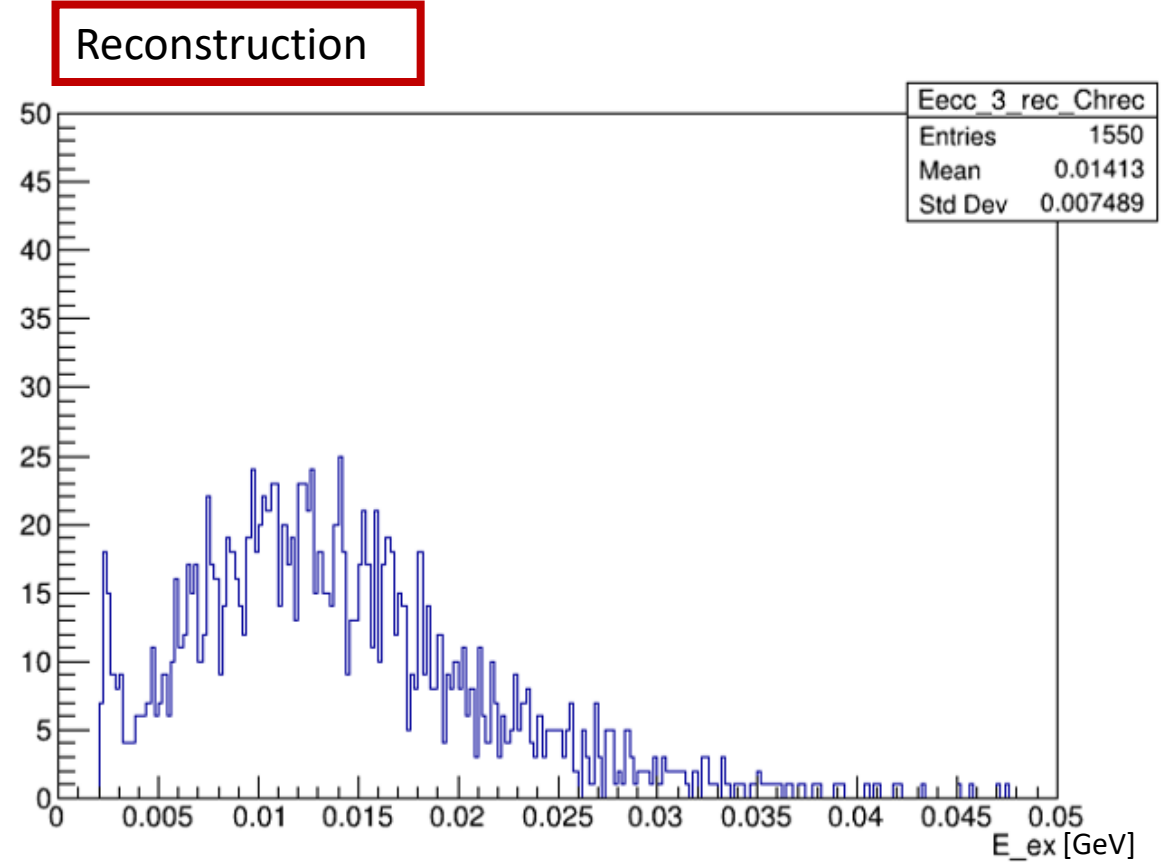




Fig. 18: Excitation energy spectrum for the breakup of ^{12}C into 3 α particles from Reconstruction α particles analysis.

Conclusions

- ✓ With reconstructed data, it can still observe the expected **angular correlations** between α particles. A minimum statistics of $\sim 5 \cdot 10^6$ events have to be collected  Study of sequential decay.
- ✓ Possibility to investigate **excitation levels** from α particles detection in reconstructed events  Reconstruction energy calibration

Future Developments

- ✓ Future nucleus to be studied: ^{16}O
- ✓ Future experimental setup to be used: EEC

Backup Reconstruction efficiency

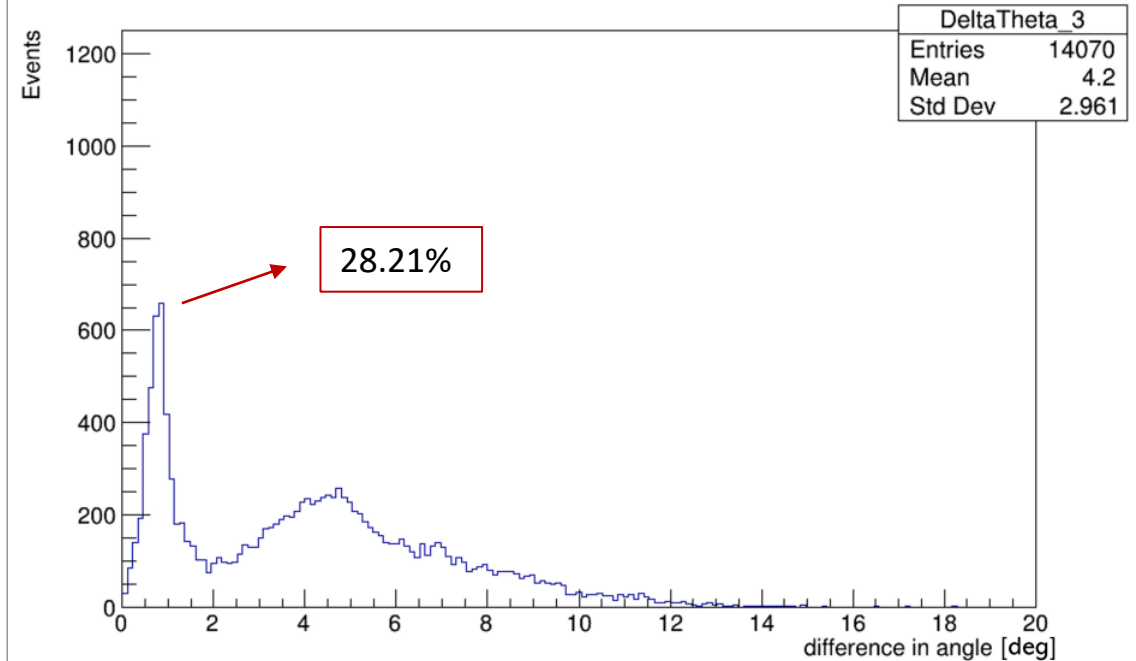
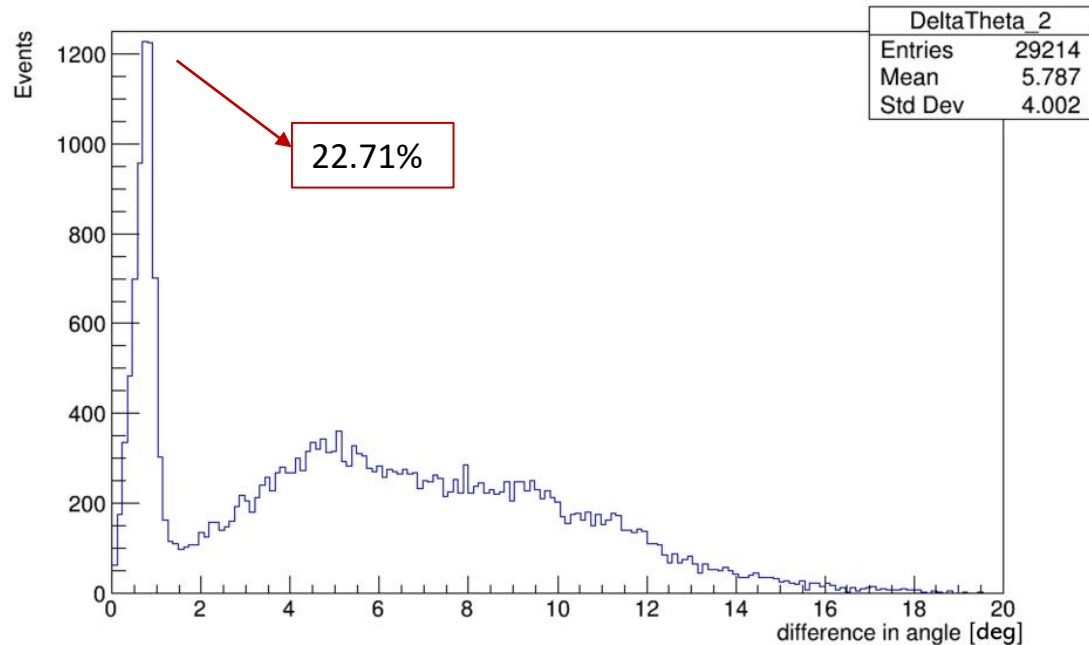
$$Eff_1 = \frac{\text{No. of reconstructed } \alpha \text{ from MC charge selection}}{\text{No. of MC } \alpha \text{ particles}} = 84.7\%$$

$$Eff_2 = \frac{\text{No. of reconstructed } \alpha \text{ from reco charge selection}}{\text{No. of MC } \alpha \text{ particles}} = 67.2\%$$

$$Eff_3 = \frac{\text{No. of reconstructed } \alpha \text{ from reco charge selection (No MC info)}}{\text{No. of MC } \alpha \text{ particles}} = 74.2\%$$

Backup Angular Separation Analysis

MC Truth



Opening angle between pairs of MC simulated α particles at target from events producing **2** (left) and **3** (right) α particles.

Backup Angular Separation Analysis

MC Truth

