

Decoding the phase structure of QCD via particle production at high energy

A. Andronic - University of Münster



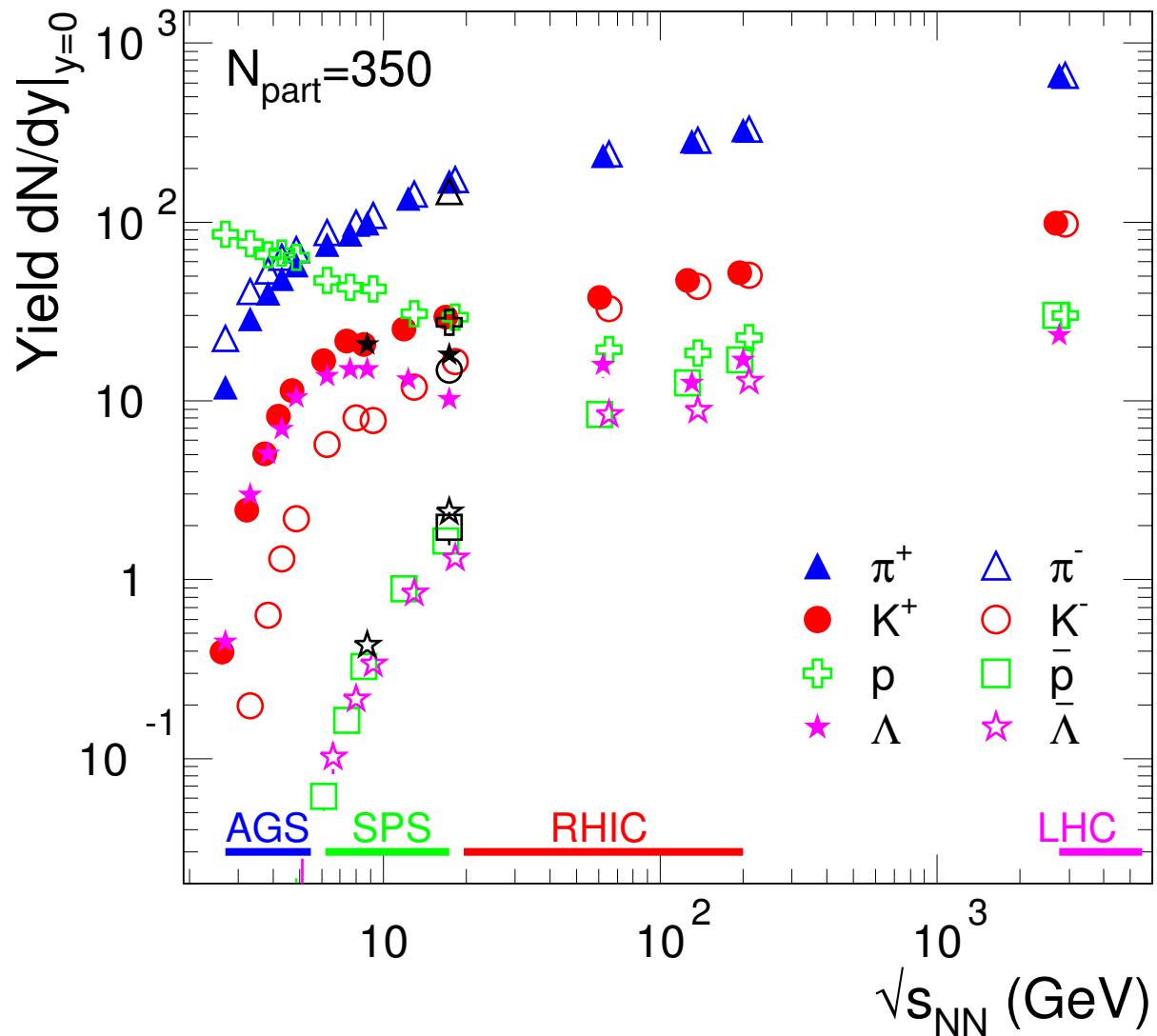
- Hadron production in nucleus-nucleus collisions
- The statistical model and the thermal fits
- Thermal fits and the QCD phase diagram
- Summary (and a glimpse of the charm quarks)

Andronic, Braun-Munzinger, Redlich, Stachel, [Nature 561 \(2018\) 321](#)

Hadron yields at midrapidity (central collisions)

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- lots of particles, mostly newly created ($m = E/c^2$)
- a great variety of species:
 π^\pm ($u\bar{d}, d\bar{u}$), $m=140$ MeV
 K^\pm ($u\bar{s}, \bar{u}s$), $m=494$ MeV
 p (uud), $m=938$ MeV
 Λ (uds), $m=1116$ MeV
also: $\Xi(dss)$, $\Omega(sss)$...
- mass hierarchy in production
(u, d quarks: remnants from the incoming nuclei)

A. Andronic, [arXiv:1407.5003](https://arxiv.org/abs/1407.5003)

...natural to think of the thermal (statistical) model ($e^{-m/T}$)

The statistical (thermal) model

grand canonical partition function for specie (hadron) i :

$$\ln Z_i = \frac{Vg_i}{2\pi^2} \int_0^\infty \pm p^2 dp \ln[1 \pm \exp(-(E_i - \mu_i)/T)]$$

$g_i = (2J_i + 1)$ spin degeneracy factor; T temperature;

$E_i = \sqrt{p^2 + m_i^2}$ total energy; (+) for fermions (-) for bosons

$\mu_i = \mu_B B_i + \mu_{I_3} I_{3i} + \mu_S S_i + \mu_C C_i$ chemical potentials

μ ensure conservation (on average) of quantum numbers, fixed by
“initial conditions”

i) isospin: $\sum_i n_i I_{3i} / \sum_i n_i B_i = I_3^{tot} / N_B^{tot}$, $N_B^{tot} \sim \mu_B$

I_3^{tot} , N_B^{tot} isospin and baryon number of the system ($=0$ at high energies)

ii) strangeness: $\sum_i n_i S_i = 0$

iii) charm: $\sum_i n_i C_i = 0$.

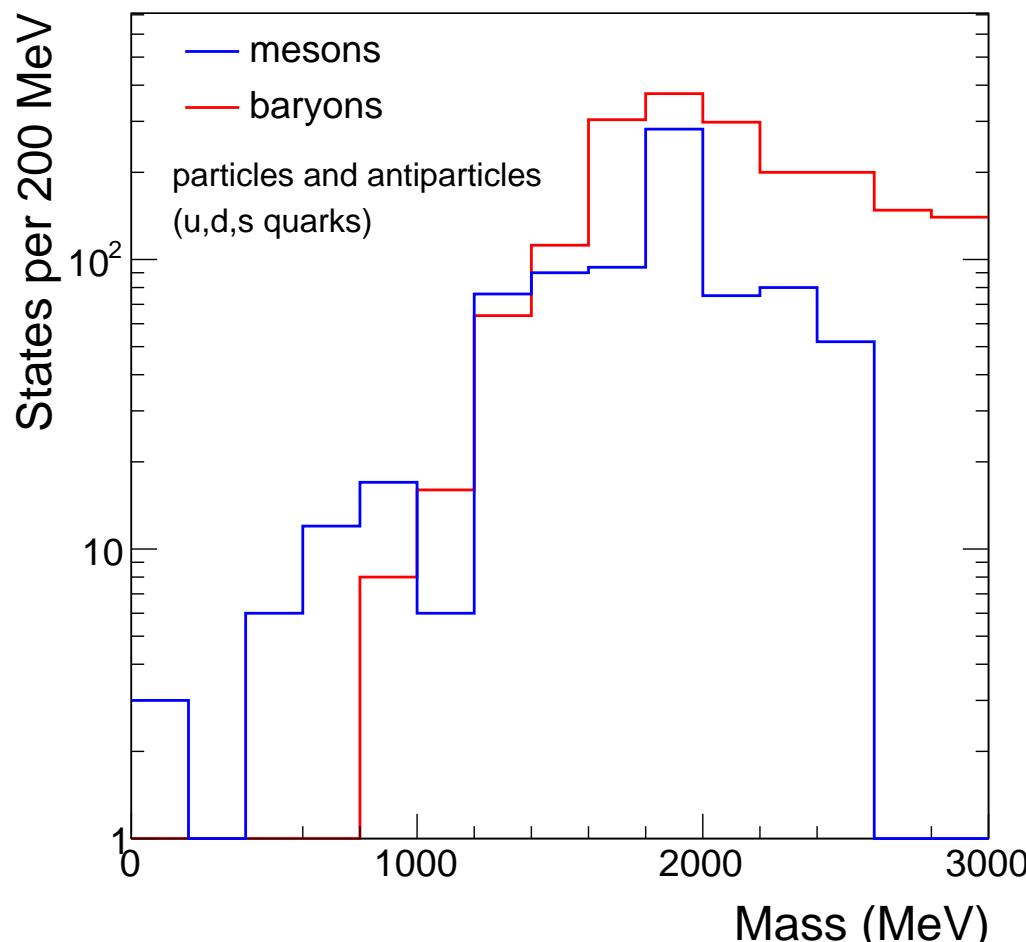
Model input: hadron spectrum

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...embodies low-energy QCD ...vacuum masses

well-known for $m < 2$ GeV; many confirmed states above 2 GeV, still incomplete



for high m , BR not well known, but can be reasonably guessed

T found to be robust in fits with spectrum truncated above 1.8 GeV

$$\rho(m) = c \cdot m^{-a} \exp(-m/T_H)$$

$T_H \simeq 180$ MeV (max T for hadrons)

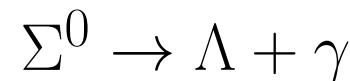
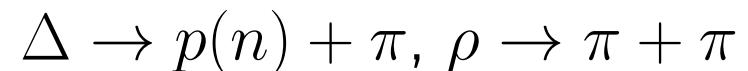
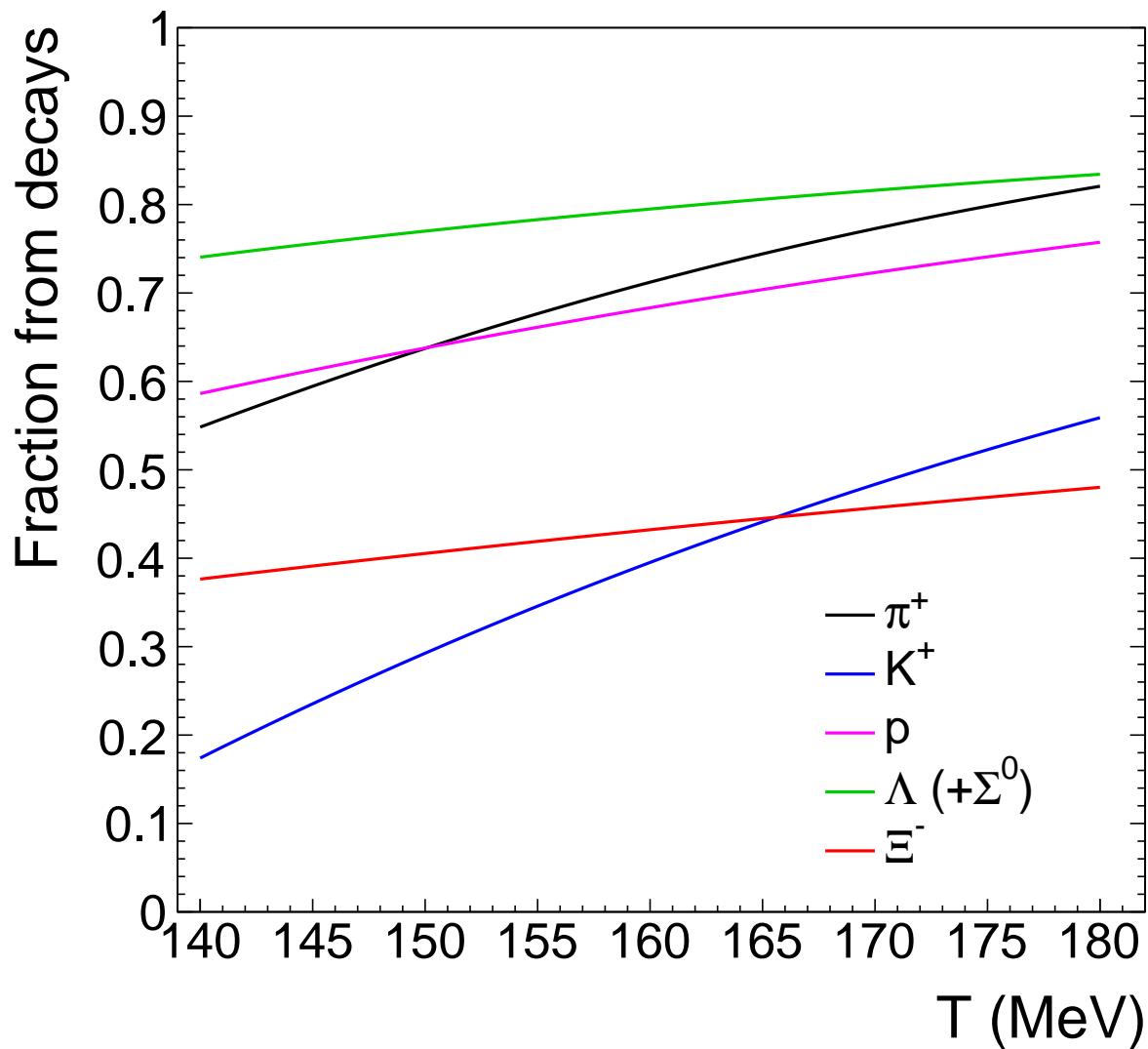
$(2J + 1)$ counted in

Decays (feed-down)

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(almost all) hadrons are subject to strong and electromagnetic decays



weak decays can be treated as well ...to account for the exact experimental situation

contribution of resonances is significant (and particle-dependent)

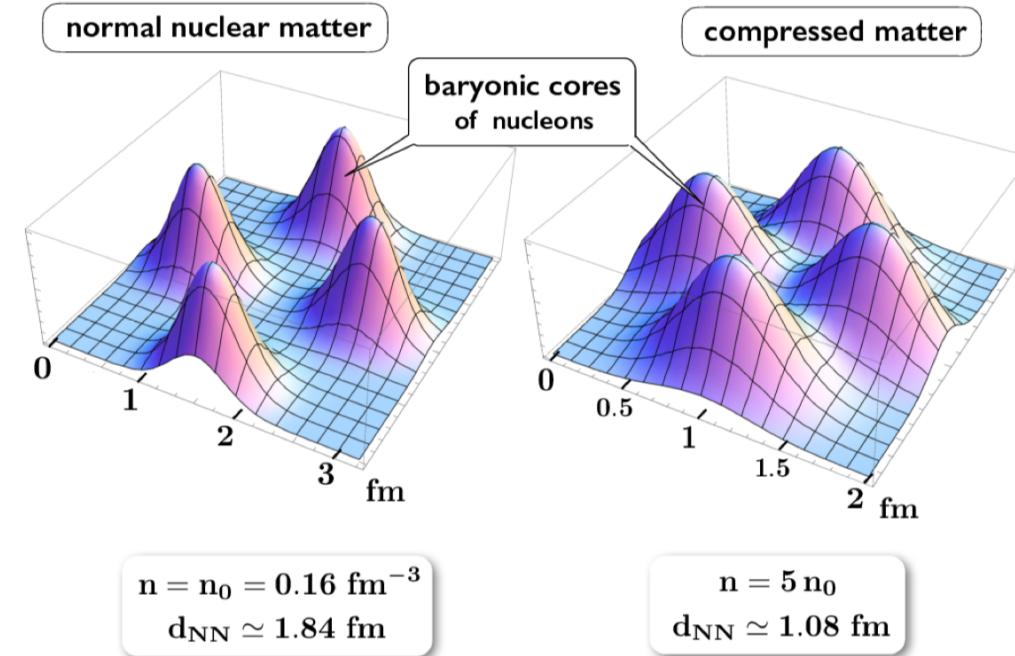
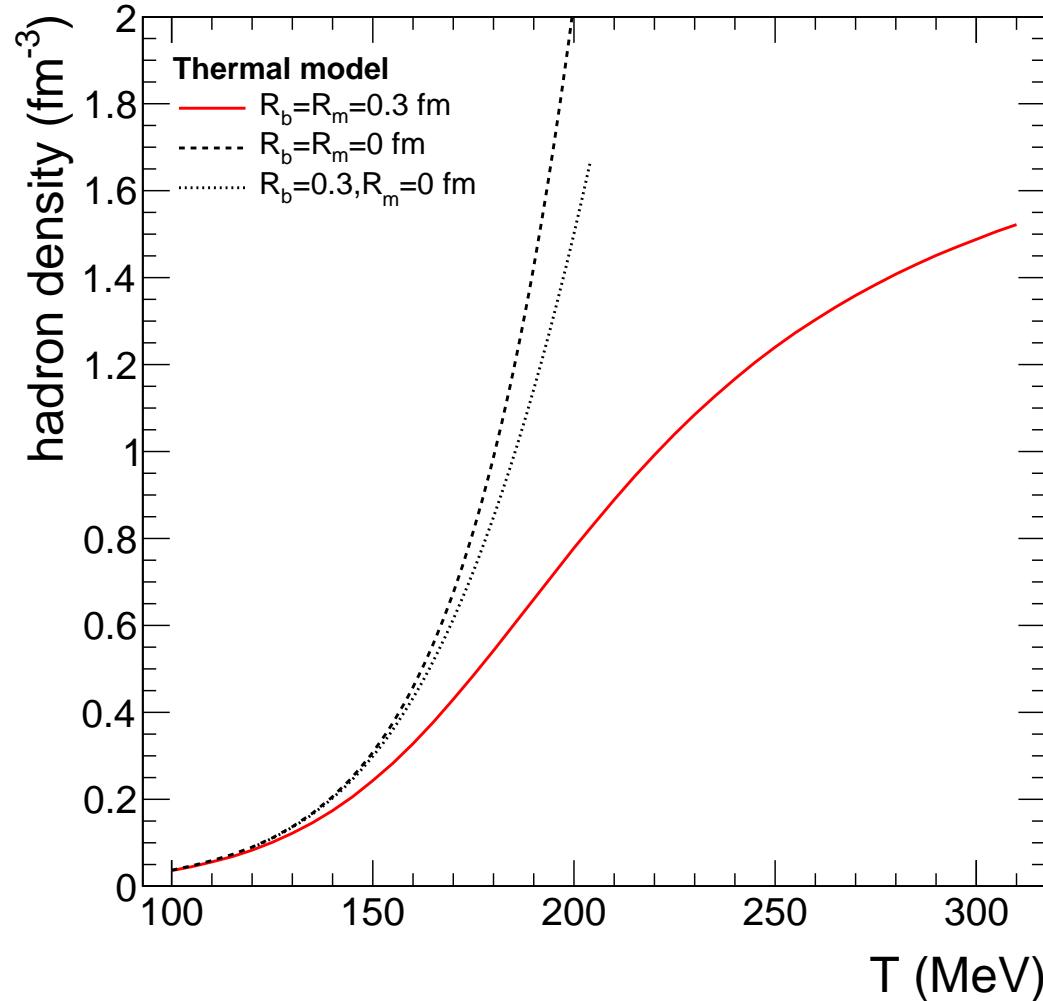
(plot for $\mu_B=0$)

The thermal model: other ingredients

- Canonical treatment (suppression): exact quantum-number conservation
important whenever the abundance of hadrons with a given quantum number is very small
- Widths of resonances (Breit-Wigner)
- Interactions ...several ways tried:
 - hard-sphere
 - T -dependent Breit-Wigner resonance widths
 - S-matrix, based on scattering phase shifts (incl. non-resonant contrib.)

Hadron densities

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Weise, [arXiv:1811.09682](https://arxiv.org/abs/1811.09682)

(baryons: gaussians, $r=0.5 \text{ fm}$)

"hadron gas": a dense system (also nuclear matter is rather a liquid than a gas)

(the usual case is $R_{baryon} = R_{meson} = 0.3 \text{ fm}$...hard-sphere repulsion)

Air at NTP: intermolecule distance $\approx 50 \times$ molecule size

Thermal fits of hadron abundances

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$$n_i = N_i/V = -\frac{T}{V} \frac{\partial \ln Z_i}{\partial \mu} = \frac{g_i}{2\pi^2} \int_0^\infty \frac{p^2 dp}{\exp[(E_i - \mu_i)/T] \pm 1}$$

Latest PDG hadron mass spectrum ...quasi-complete up to $m=2$ GeV;
our code: 555 species (including fragments, charm and bottom hadrons)

for resonances, the width is considered in calculations

canonical treatment whenever needed (small abundances)

$$\text{Minimize: } \chi^2 = \sum_i \frac{(N_i^{exp} - N_i^{therm})^2}{\sigma_i^2}$$

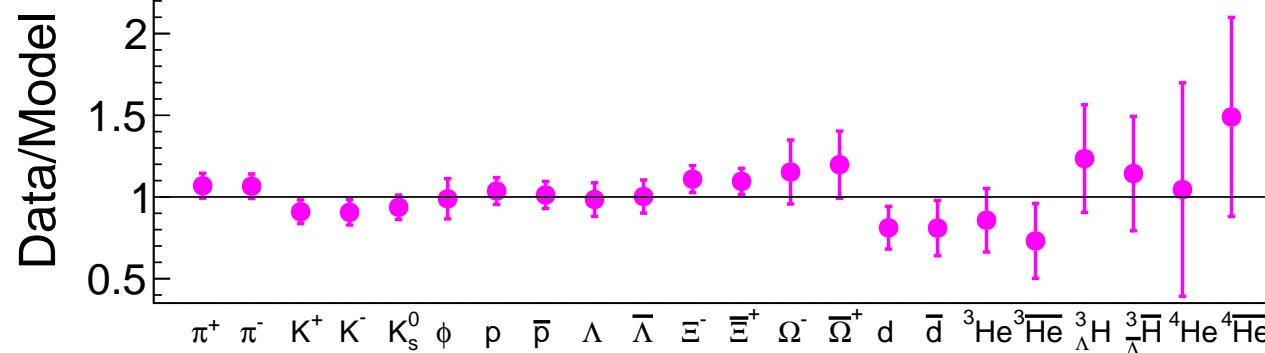
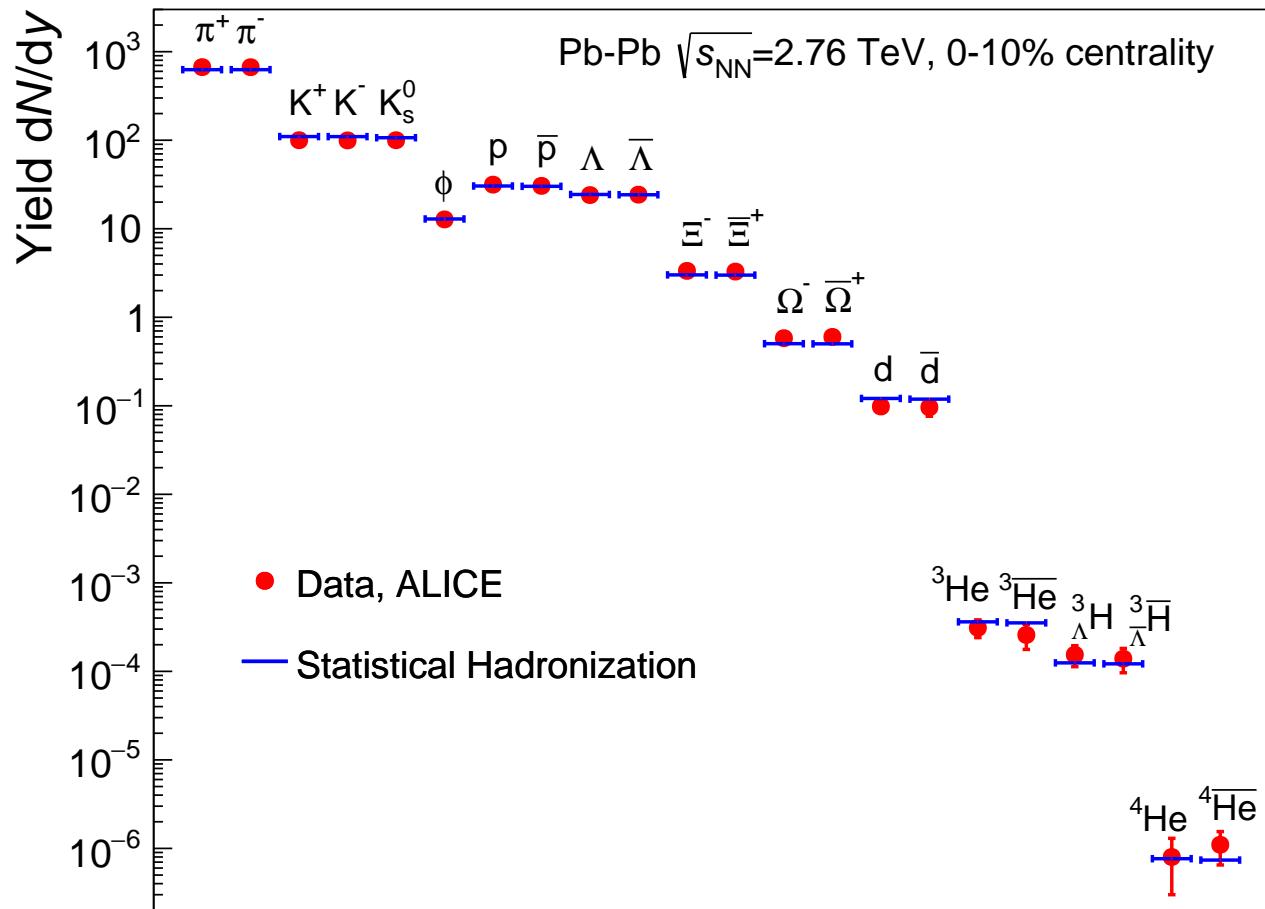
N_i hadron yield, σ_i experimental uncertainty (stat.+syst.)

$\Rightarrow (T, \mu_B, V)$...tests chemical freeze-out (chemical equilibrium)

Thermal fit – LHC, Pb–Pb, 0-10%

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matter and antimatter produced in equal amounts

$$T_{CF} = 156.6 \pm 1.7 \text{ MeV}$$

$$\mu_B = 0.7 \pm 3.8 \text{ MeV}$$

$$V_{\Delta y=1} = 4175 \pm 380 \text{ fm}^3$$

$$\chi^2/N_{df} = 16.7/19$$

S-matrix treatment

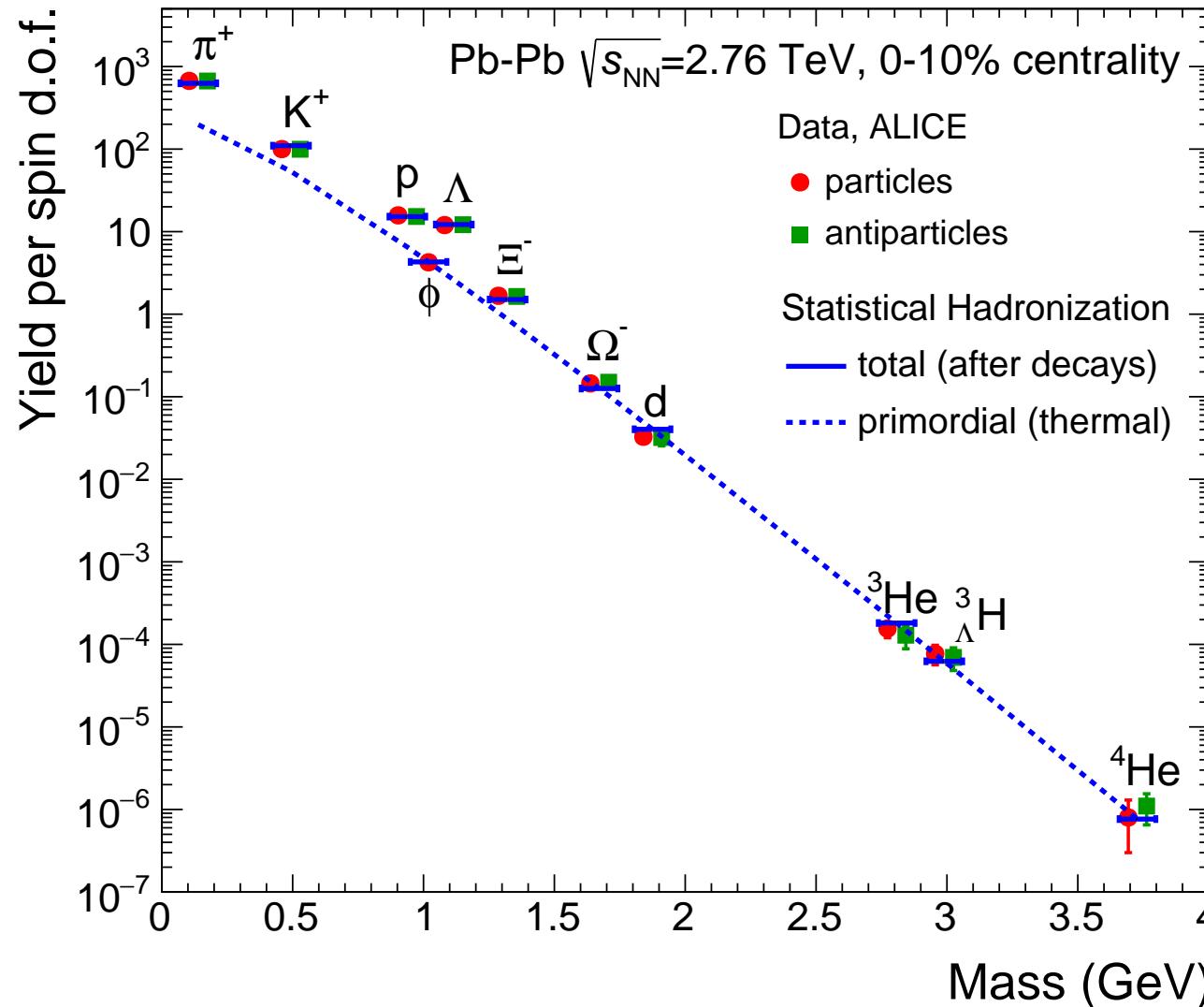
remarkably, loosely-bound objects
are also well described
(${}^3\text{H}$ with 25% B.R.)

hadronization as bags of quarks
and gluons?

Model uncertainties: hadron spectrum

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contribution of resonances
is significant
(and particle-dependent)

Fit of ϕ , Ω , d , ${}^3\text{He}$, ${}^3\text{H}$, ${}^4\text{He}$:

$$T_{CF} = 156 \pm 2.5 \text{ MeV}$$

$$(\chi^2/N_{df} = 7.4/8)$$

Fit of nuclei (d , ${}^3\text{He}$, ${}^4\text{He}$):

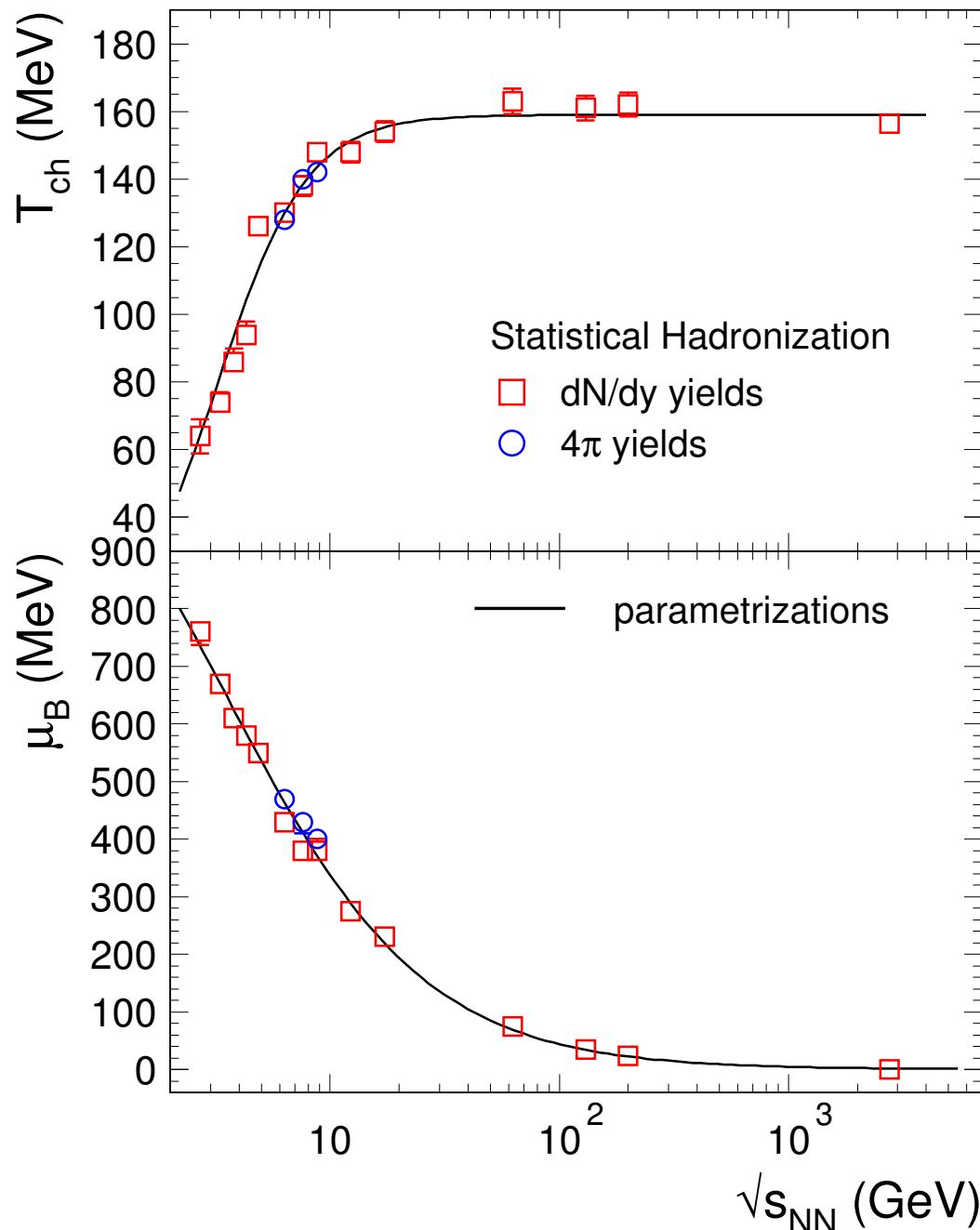
$$T_{CF} = 159 \pm 5 \text{ MeV}$$

3-4 MeV upper bound of systematic uncertainty due to hadron spectrum

Energy dependence of T , μ_B (central collisions)

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thermal fits exhibit a limiting temperature:

$$T_{lim} = 158.4 \pm 1.4 \text{ MeV}$$

$$T_{CF} = T_{lim} \frac{1}{1 + \exp(2.60 - \ln(\sqrt{s_{NN}}(\text{GeV})) / 0.45)}$$

$$\mu_B[\text{MeV}] = \frac{1307.5}{1 + 0.288\sqrt{s_{NN}}(\text{GeV})}$$

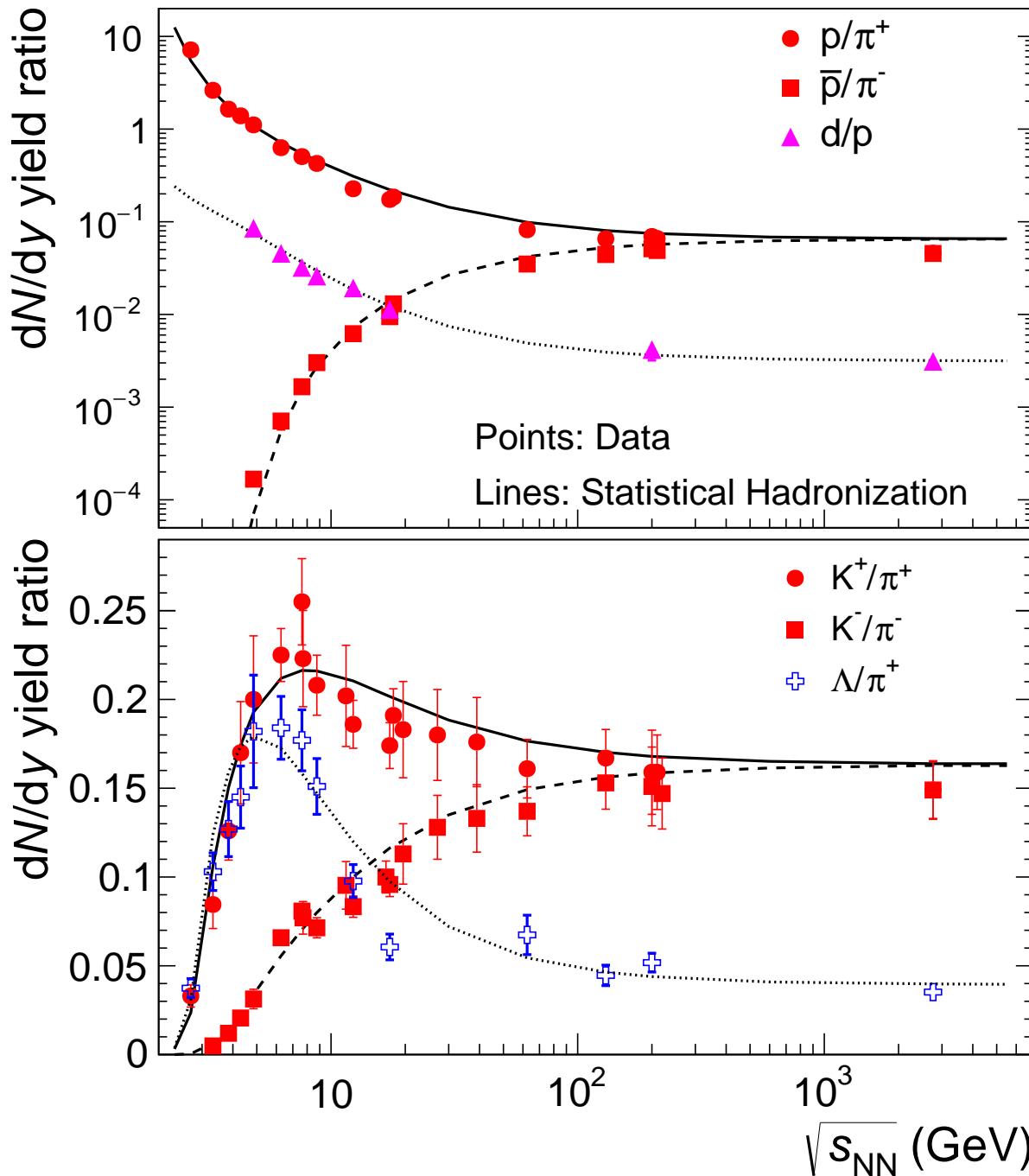
NPA 772 (2006) 167, PLB 673 (2009) 142

μ_B is a measure of the net-baryon density, or matter-antimatter asymmetry

determined by the "stopping" of the colliding nuclei

The grand (albeit partial) view

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Data:

AGS: E895, E864, E866, E917, E877

SPS: NA49, NA44

RHIC: STAR, BRAHMS

LHC: ALICE

NB: no contribution from weak decays

d/p ratio is well described for all energies

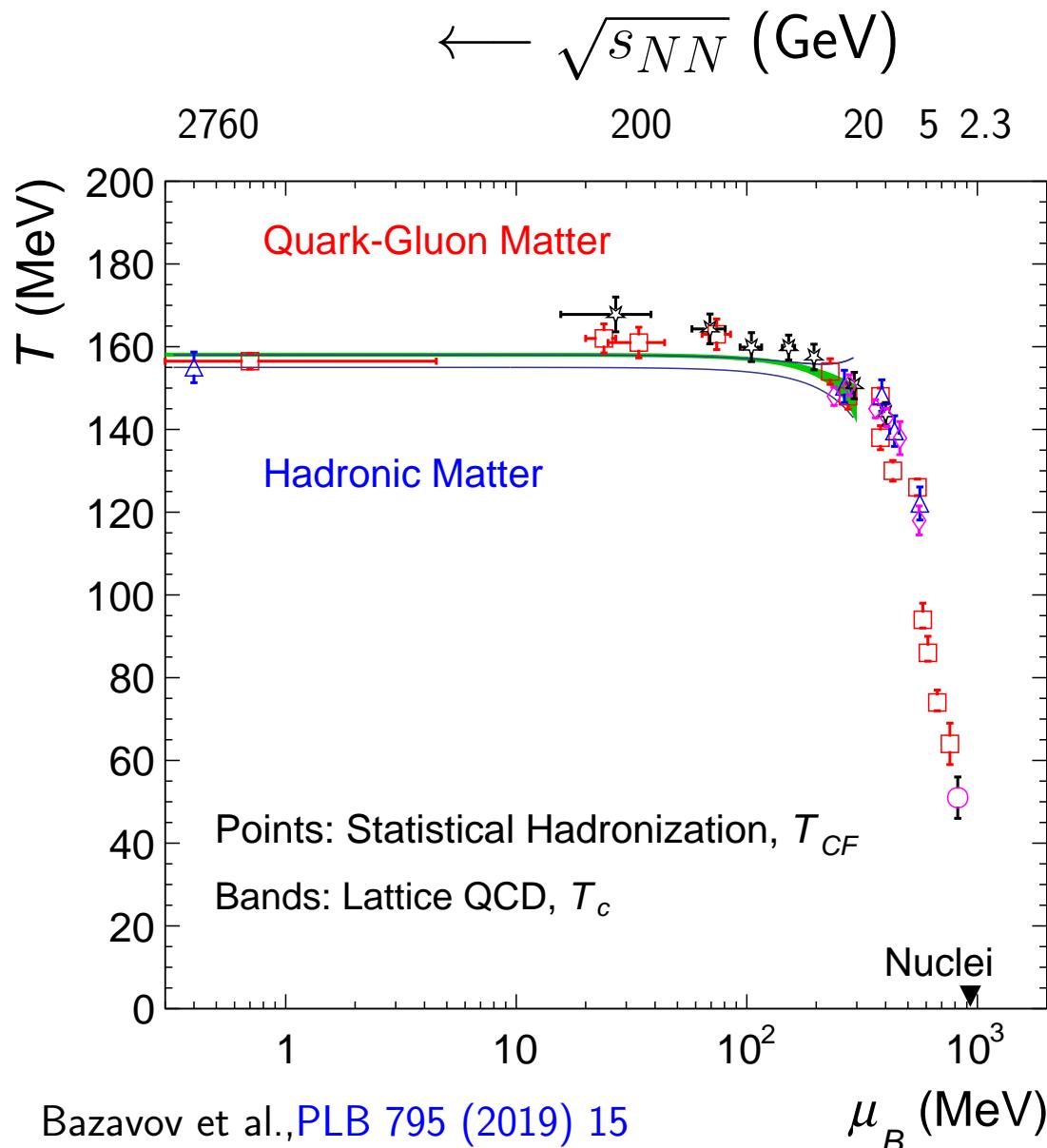
“structures” described by SHM
...determined by strangeness conservation

Λ/π peak reflects increasing T
and decreasing μ_B

The phase diagram of QCD

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at LHC, remarkable “coincidence” with Lattice QCD results

at LHC ($\mu_B \simeq 0$): purely-produced (anti)matter ($m = E/c^2$), as in the Early Universe

$\mu_B > 0$: more matter, from “remnants” of the colliding nuclei

$\mu_B \gtrsim 400$ MeV: *the critical point awaiting discovery*
(RHIC BES / FAIR)

see refs. in Nature 561 (2018) 321

points: independent analyses of same data → "model/code uncert." are small

Summary

- Hadronization: rapid process in which all quark flavors take part concurrently
- Abundance of hadrons with light quarks consistent with chemical equilibration
- There is a variety of approaches ... *a personal bias: the “minimal model”*
a minimal set of parameters, means a well-constrained model
- The thermal model provides a simple way to access the QCD phase boundary
...at high energies (at low energies canonical suppression needs more care)
...but is it more than a 1st order description (of loosely-bound objects)?
...and what fundamental point does it make about hadronization?
(statistical features dominate, but understanding still missing as a dynamical process)
- More insights from higher moments and from heavier (charm) quarks
...(at the LHC) a handle for hadronization T with a mass scale ($m_{c\bar{c}}$) well above T
($T > T_{ch}$ measured with (virtual) photons and through flow via hydrodynamics)

SHM for charm (SHMc)

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$pQCD$ production, "throw in": $N_{c\bar{c}} = 9.6 \rightarrow g_c = 30.1$ ($I_1/I_0 = 0.974$)

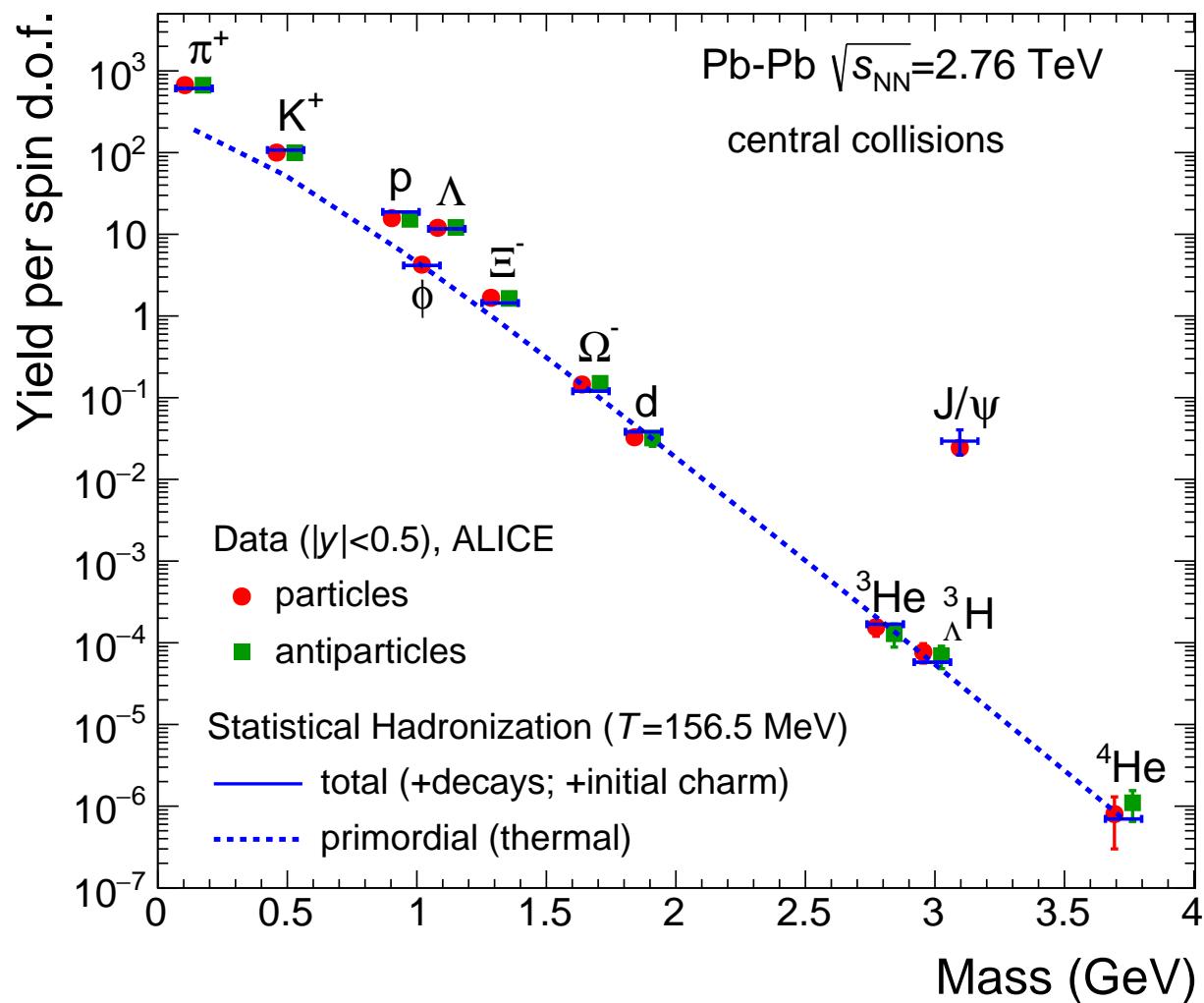
LHC, central collisions

assume:

- full thermalization of c, \bar{c}
("mobility" in $V \simeq 4000 \text{ fm}^3$)
- full color screening
(Matsui-Satz)

Braun-Munzinger, Stachel, [PLB 490 \(2000\) 196](#)

Model predicts all charm
chemistry ($\psi(2S), X(3872)$)



π, K^\pm, K^0 from charm included in the thermal fit
(0.7%, 2.9%, 3.1% for $T=156.5 \text{ MeV}$)

[PLB 797 \(2019\) 134836](#)

Additional material

SHMc: method and inputs

Braun-Munzinger, Stachel, PLB 490 (2000) 196, NPA 690 (2001) 119

- Thermal model calculation (grand canonical) T, μ_B : $\rightarrow n_X^{th}$
- $N_{c\bar{c}}^{dir} = \frac{1}{2}g_c V(\sum_i n_{D_i}^{th} + n_{\Lambda_i}^{th}) + g_c^2 V(\sum_i n_{\psi_i}^{th} + n_{\chi_i}^{th})$
- $N_{c\bar{c}} << 1 \rightarrow \text{Canonical}$ (Cleymans, Redlich, Suhonen, Z. Phys. C51 (1991) 137):

Gorenstein, Kostyuk, Stöcker, Greiner, PLB 509 (2001) 277

$$N_{c\bar{c}}^{dir} = \frac{1}{2}g_c N_{oc}^{th} \frac{I_1(g_c N_{oc}^{th})}{I_0(g_c N_{oc}^{th})} + g_c^2 N_{c\bar{c}}^{th} \quad \rightarrow g_c(N_{part}) \text{ (charm fugacity)}$$

Outcome: $N_D = g_c V n_D^{th} I_1/I_0 + N_D^{\text{corona}}, \quad N_{J/\psi} = g_c^2 V n_{J/\psi}^{th} + N_{J/\psi}^{\text{corona}}$

Inputs: $T, \mu_B, \quad V_{\Delta y=1} (= (dN_{ch}^{exp}/dy)/n_{ch}^{th}), \quad N_{c\bar{c}}^{dir}$ (exp. or pQCD)

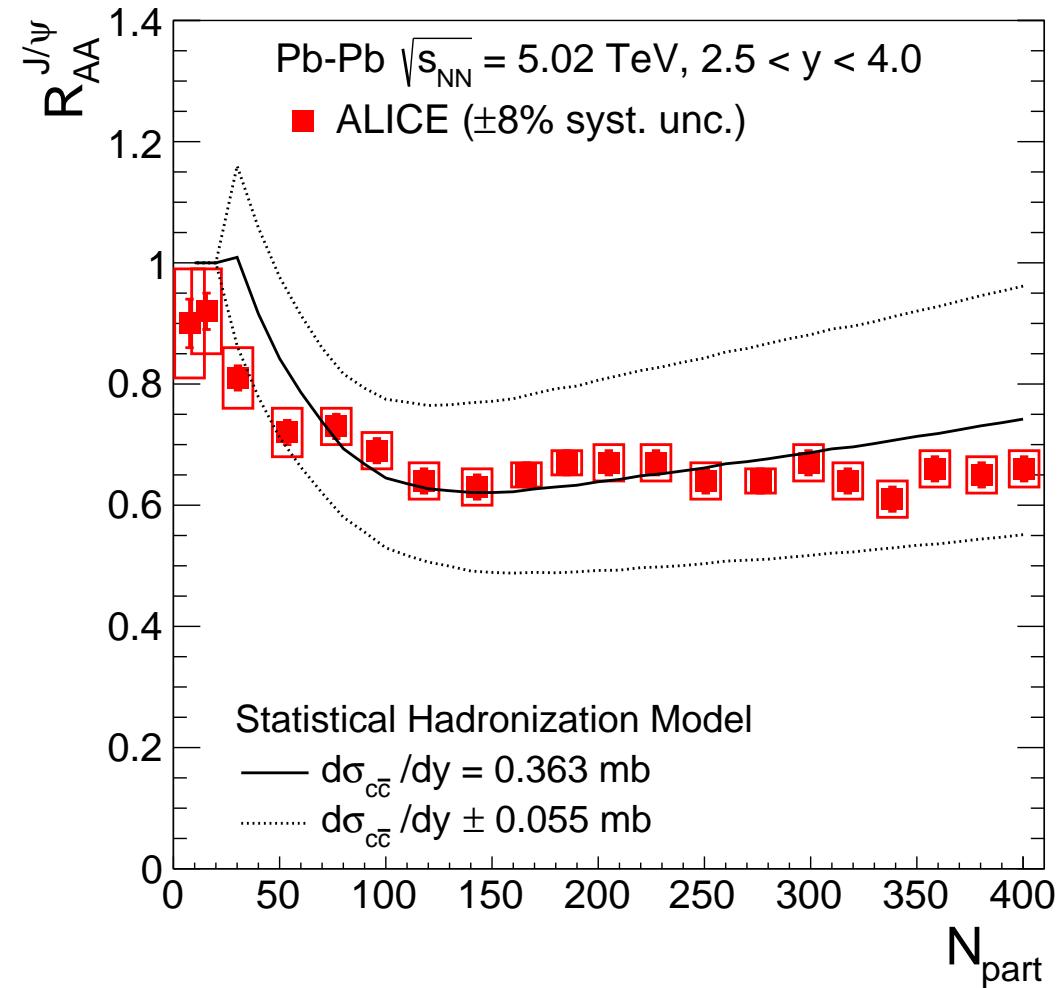
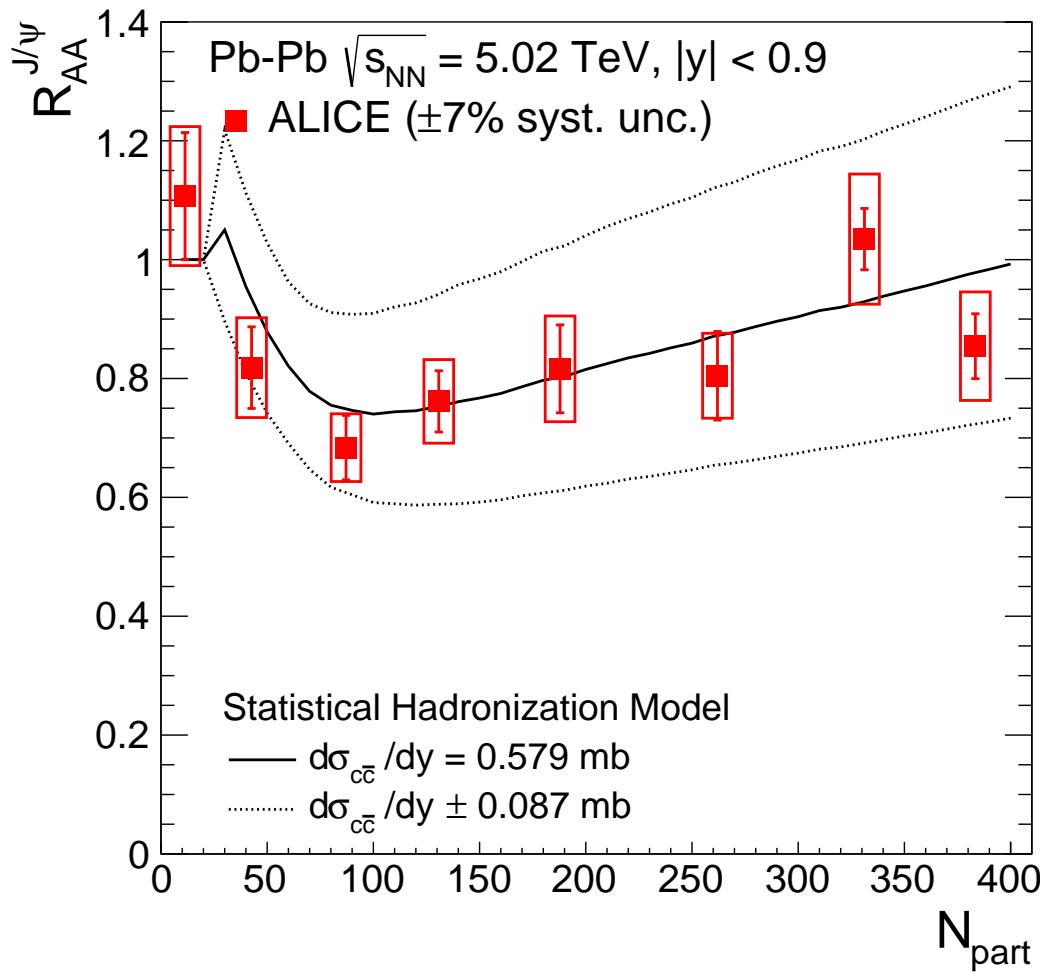
Assumed minimal volume for QGP: $V_{QGP}^{min} = 200 \text{ fm}^3$

SHMc and charmonium data at the LHC

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full thermalization of c quarks in QGP, hadronization at chemical freeze-out



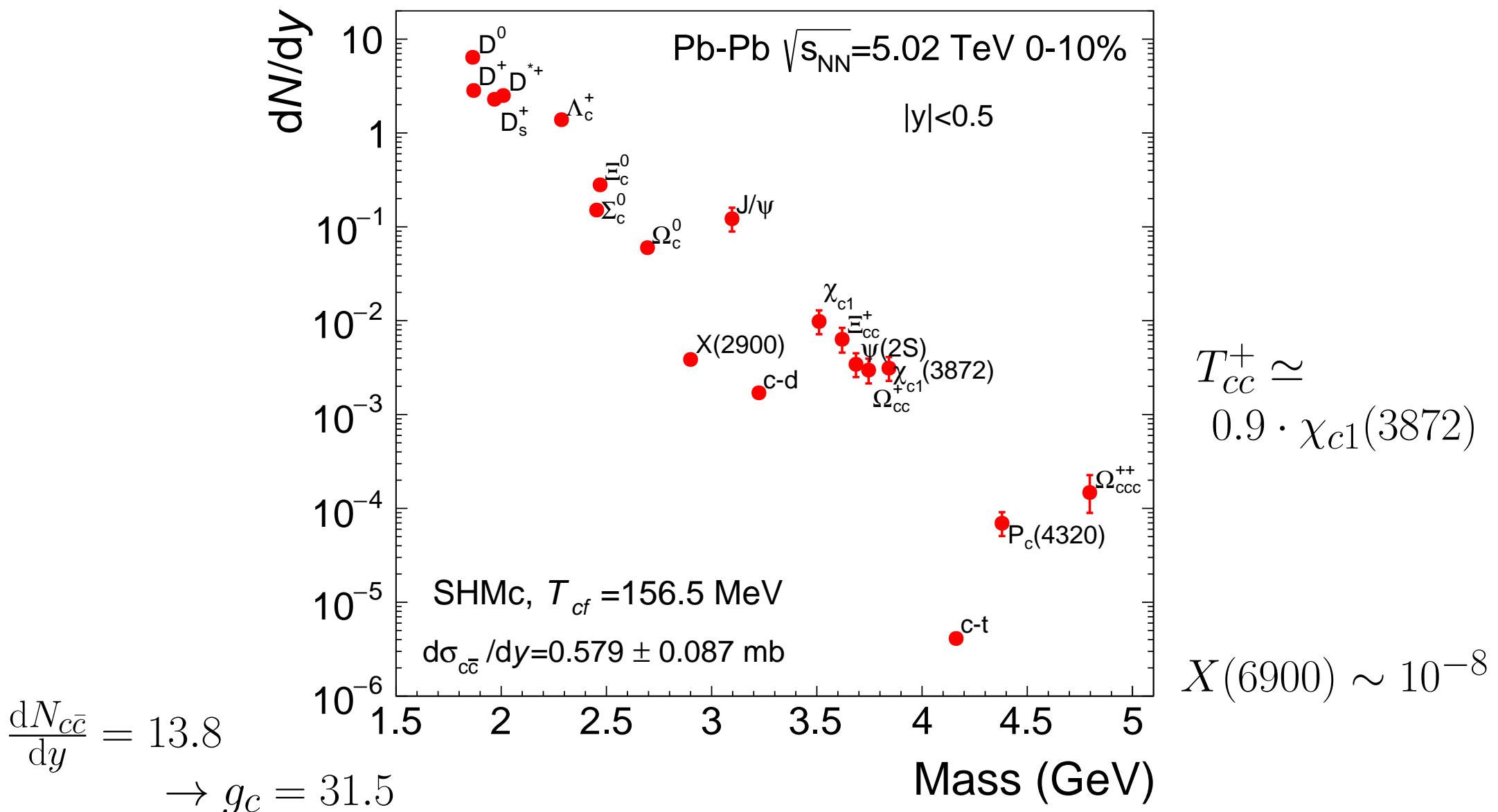
$d\sigma_{c\bar{c}}/dy$ via normalization to D^0 in Pb–Pb 0–10%, ALICE, [arXiv:2110.09420](https://arxiv.org/abs/2110.09420)

$dN/dy = 6.82 \pm 1.03$ ($|y| < 0.5$; FONLL for $y=2.5-4$; assuming hadronization fractions in data as in SHMc)

SHMc: the full charm zoo

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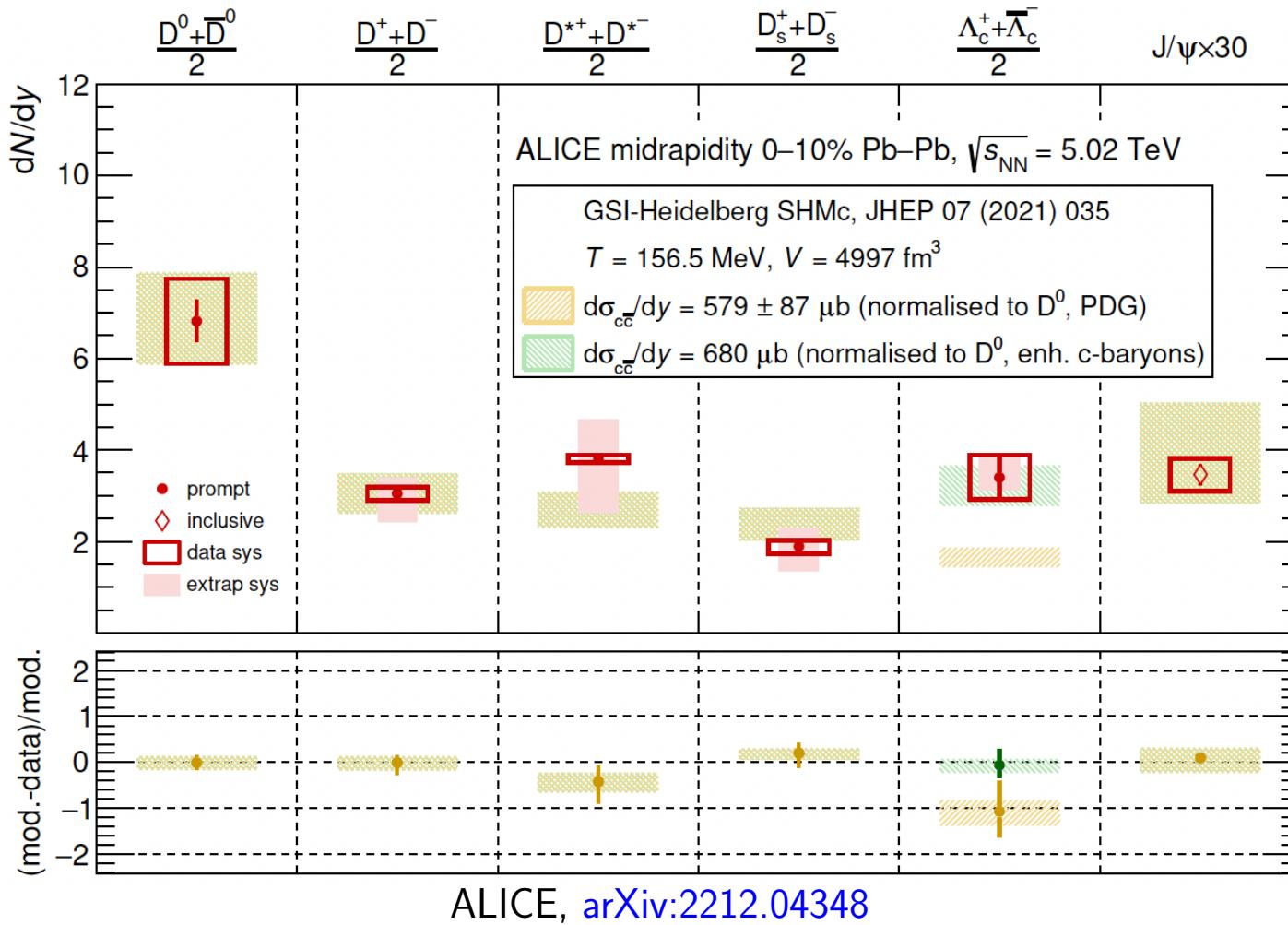


The power of the model: predicting the full suite of charmed hadrons

Charm data and SHMc model

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Enh. c-baryons: tripled the excited charm-baryon states, and $d\sigma_{c\bar{c}}/dy$: +19%

RQM: He,Rapp, PLB 795 (2019) 117; LQCD, Bazavov et al., PLB 737 (2014) 210

leaves the mesonic sector unaffected, for the commensurately larger $\sigma_{c\bar{c}}$

Summary / Conclusions: charm

In the (our) statistical hadronization model:

- The hadronization is a rapid process in which all quark flavors take part concurrently
- All charmonium and open charm states are generated exclusively at hadronization (chemical freeze-out) ...full color screening

The model is very successful in reproducing the J/ψ and open charm data
A handle for hadronization T with a mass scale well above T

"The competition":

the kinetic model, continuous J/ψ destruction and (re)generation in QGP

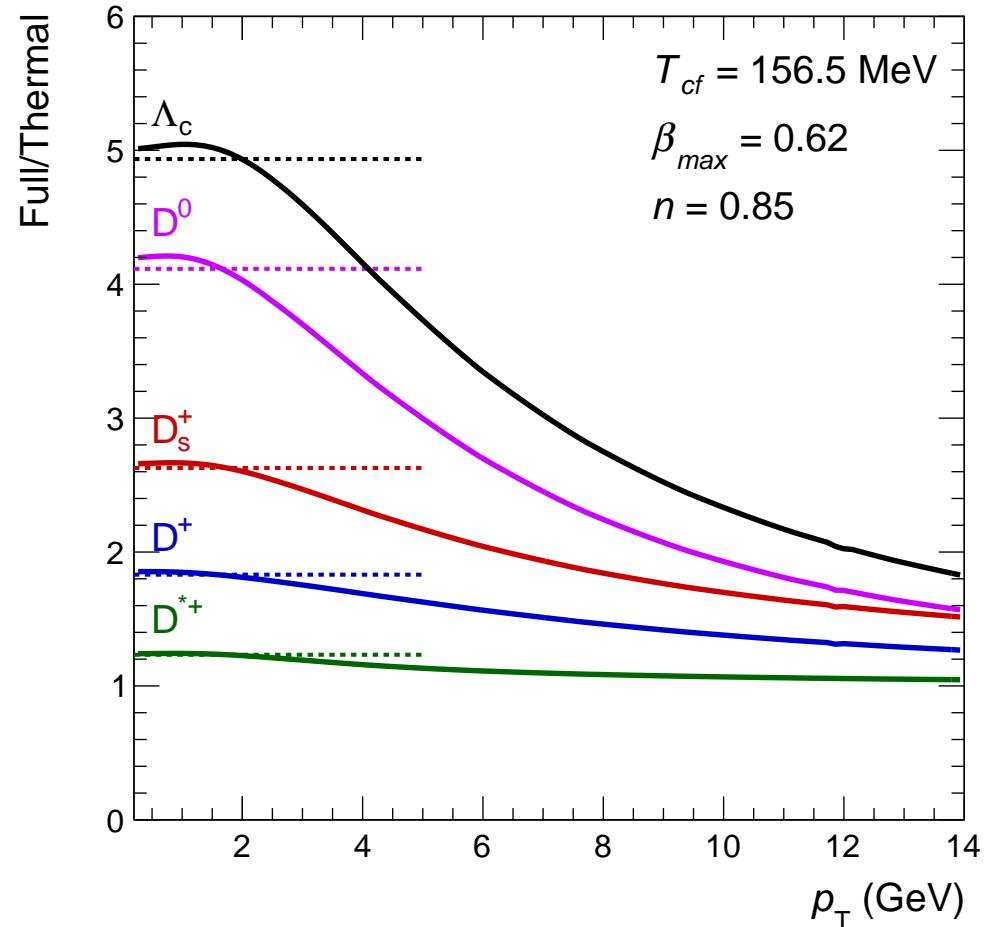
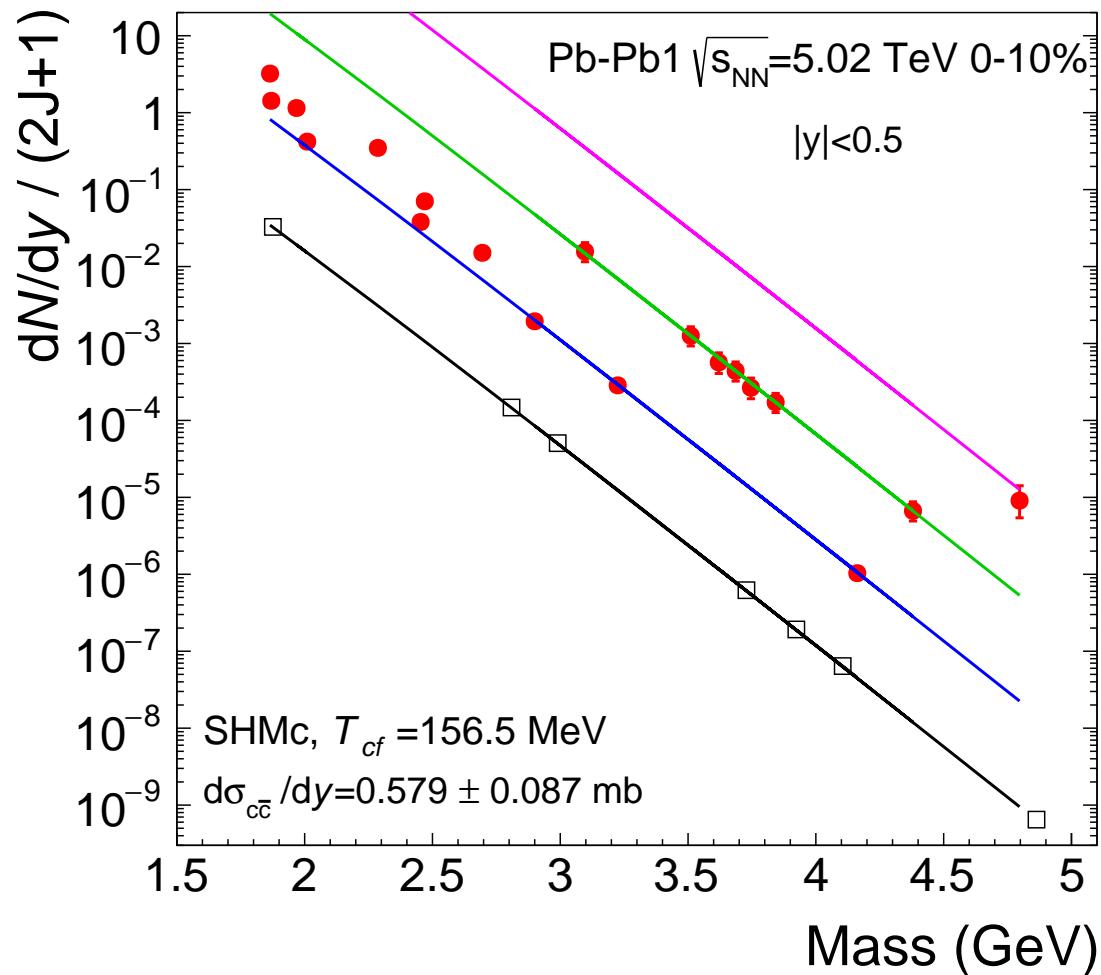
(only up to 2/3 of the J/ψ yield (LHC, central collisions) originates from deconfined c and \bar{c} quarks)

Discriminating the two pictures implies providing an answer to fundamental questions related to the fate of hadrons in a hot deconfined medium.

A precision ($\pm 10\%$) measurement of $d\sigma_{c\bar{c}}/dy$ in Pb-Pb (Au-Au) collisions needed for a stringent test
(within reach with the upgraded detectors at the LHC and RHIC)

Full charm predictions for the LHC

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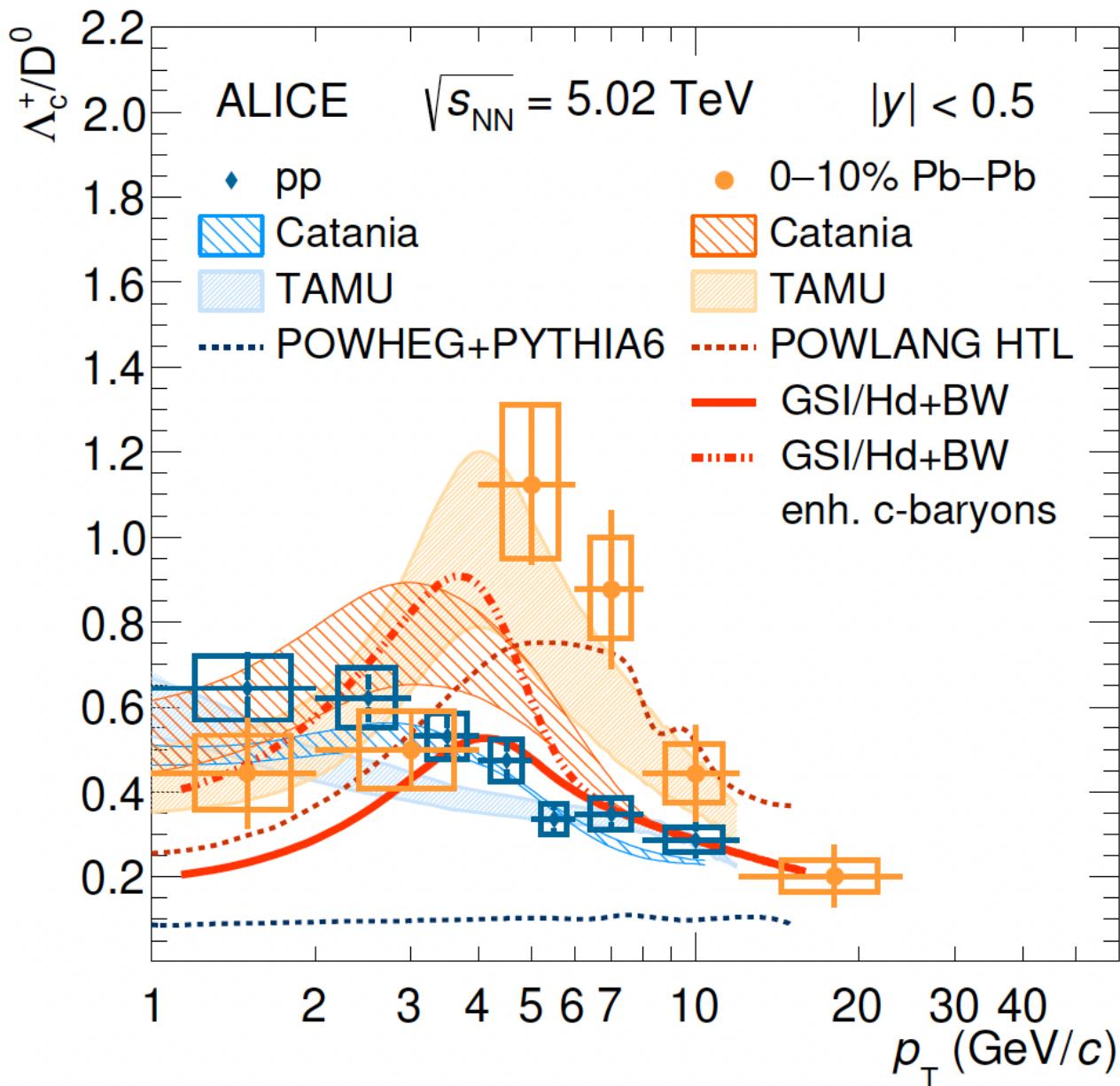


Charm-hadron spectrum as in PDG: 55 c-mesons, 74 c-baryons (part.+antipart.)
...large, but may not be complete (LQCD)

Open charm data vs. models at the LHC

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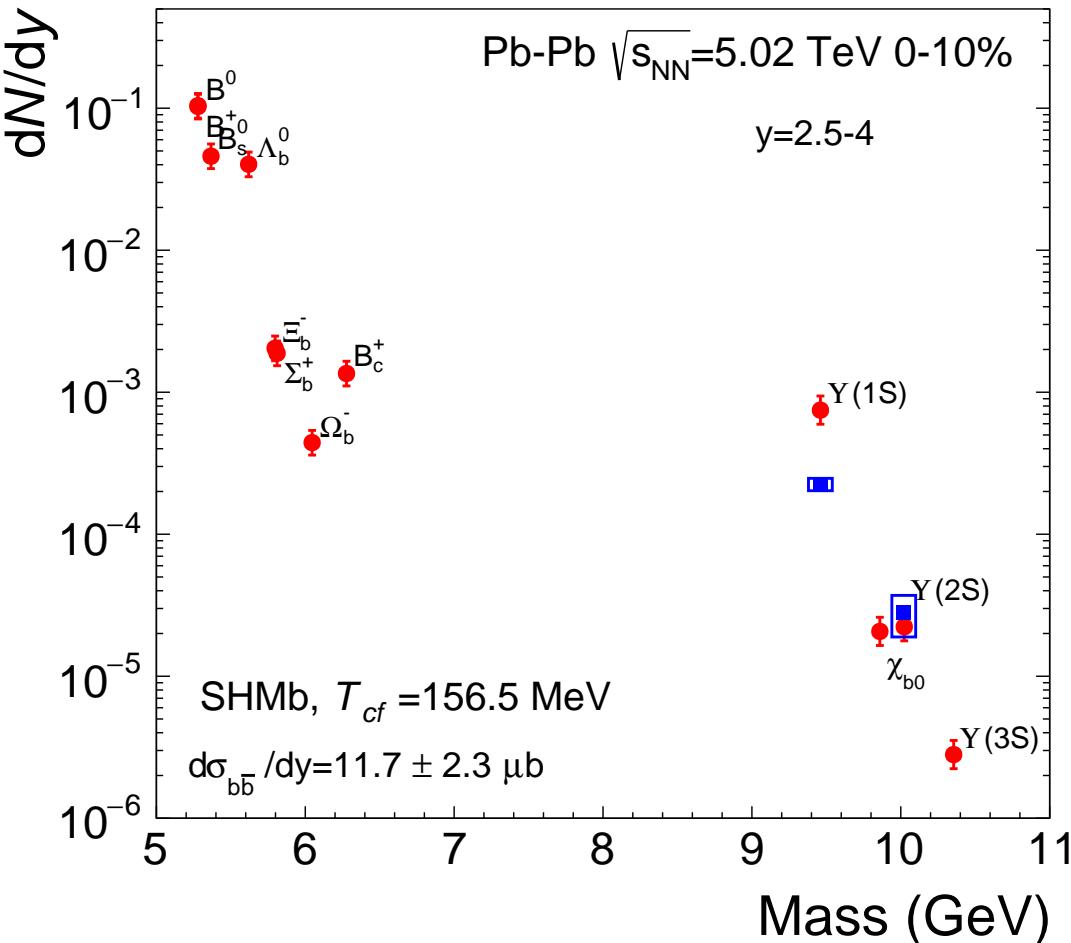
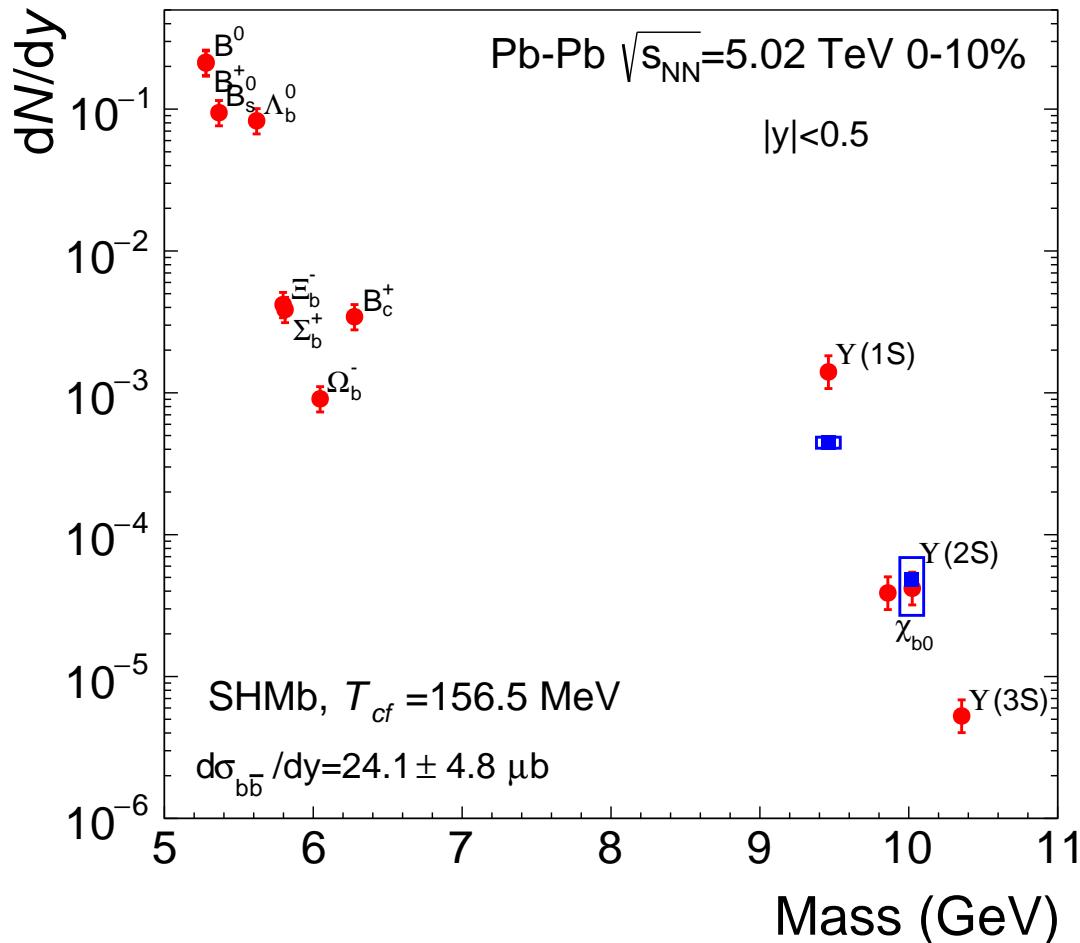
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The limiting case: full beauty thermalization

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$$g_b = 1.05 \cdot 10^9 \quad \left(\frac{dN_{b\bar{b}}}{dy} = 0.57 \right)$$

$$B_c : 3.44 \cdot 10^{-3}$$

$$g_b = 0.86 \cdot 10^9 \quad \left(\frac{dN_{b\bar{b}}}{dy} = 0.28 \right)$$

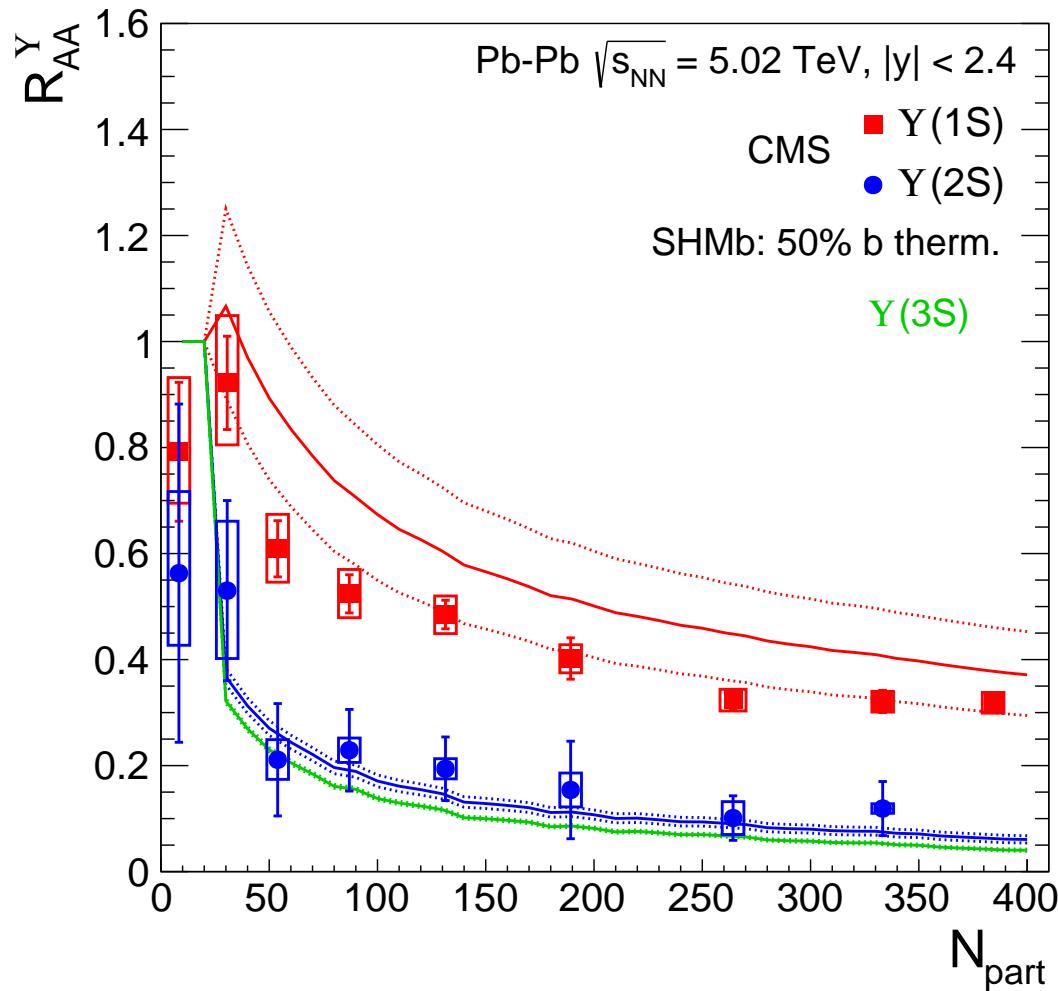
$$B_c : 1.36 \cdot 10^{-3}$$

Blue: Υ data (CMS, ALICE): calc. based on R_{AA} and pp (would be nice to include in publications dN/dy)

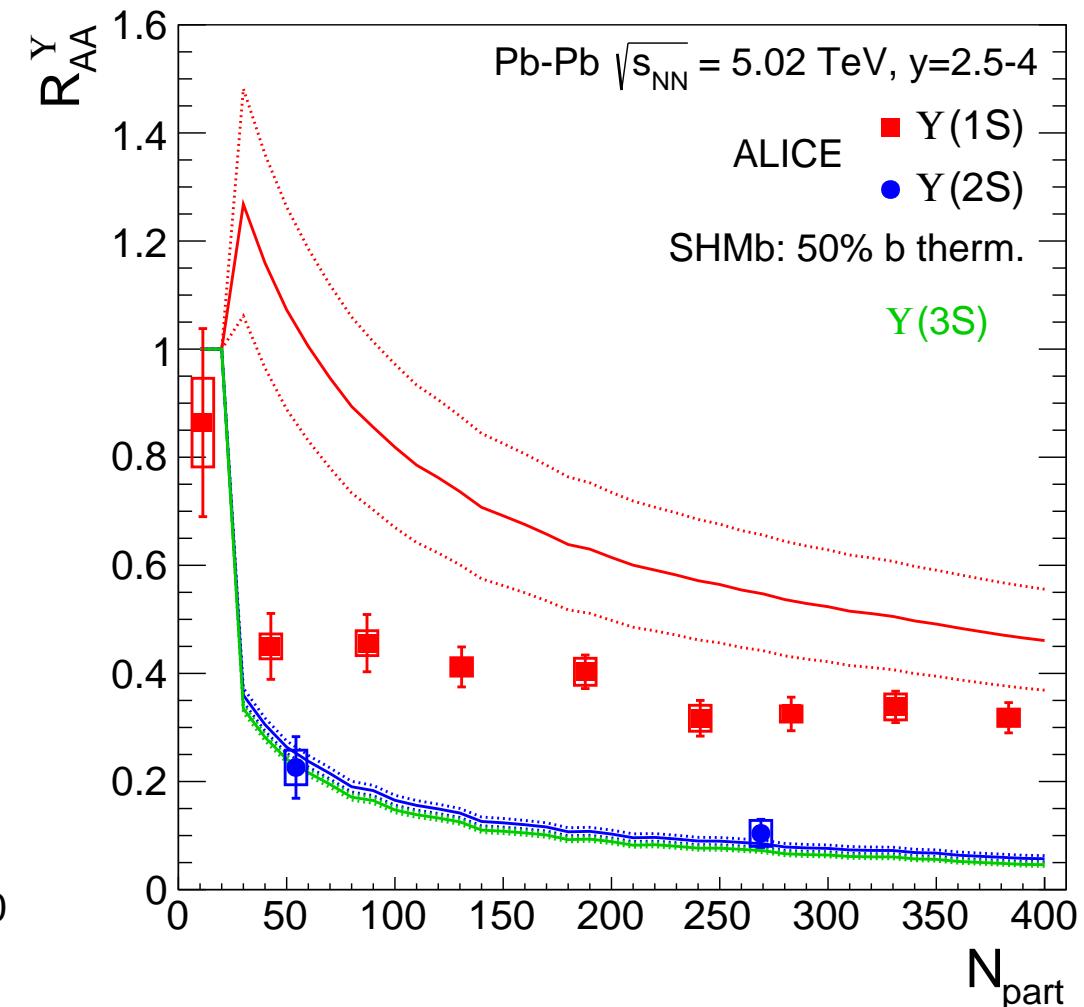
R_{AA} , 50% $b\bar{b}$ thermalized

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CMS, PRL 120 (2018) 142301



ALICE, PLB 822 (2021) 136579

What does non-thermalized beauty produce? (no room for it in SHMb)