



NMMA : nuclear-physics and multi-messenger astrophysics framework

Pang P. T. H., et al., 2023, Nature Communications., 14, 8352




Credit: Tohoku University



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GRB170817A |
Gamma-ray burst &
afterglow

GW170817 |
Gravitational
waves

AT2017gfo |
Kilonova

Credit: Tohoku University



NMMA : nuclear-physics and multi-messenger astrophysics framework

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New insights

- constrained nuclear EOS
- confirmed predictions of General Relativity
- production site of heavy elements
- alternative method to infer the expansion rate of the Universe

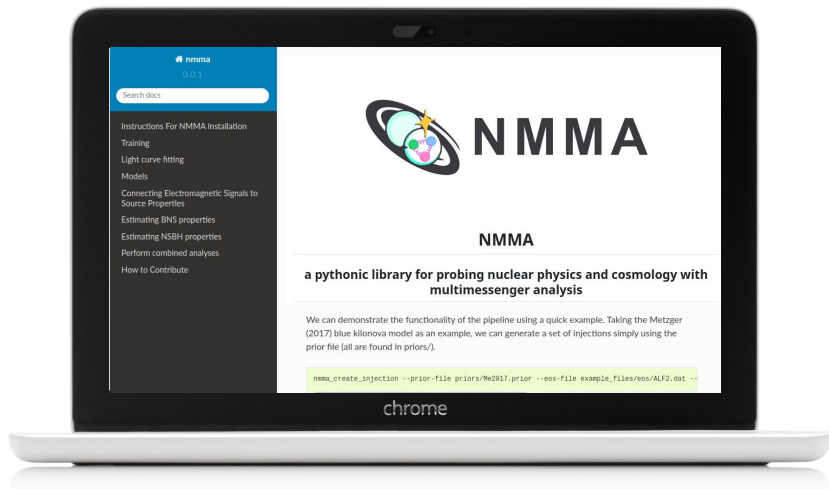
GRB170817A |
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waves

AT2017gfo |
Kilonova

Credit: Tohoku University

NMMA | Functionalities



GitHub: <https://github.com/nuclear-multimessenger-astronomy/nmma>

Bayesian inference

- observational data & injections
- gravitational-wave signals
- electromagnetic signals
- joint inference of GW+ EM signals

Including nuclear physics

- neutron star equation of state (EOS)

Estimating binary source properties

- Binary neutron star (BNS)
- Neutron star black hole (NSBH)

Other

- estimating the Hubble Constant

Bayesian inference

Parameter estimation through **Bayes theorem**

$$p(\vec{\theta}|d, \mathcal{H}) \equiv \frac{\overset{\text{Likelihood}}{\mathcal{L}(\vec{\theta})} \overset{\text{Prior}}{\pi(\vec{\theta})}}{\underset{\text{Evidence}}{\mathcal{Z}}}$$

Probability of the hypothesis given the data

Gravitational-wave inference | [Bilby](#)

Ashton, et al. (2019)

$$\mathcal{L}_{GW} \propto \exp\left(-\frac{1}{2}\langle d - h(\vec{\theta}) | d - h(\vec{\theta}) \rangle\right)$$

Electromagnetic inference | [NMMA](#)

Pang et al. (2023)

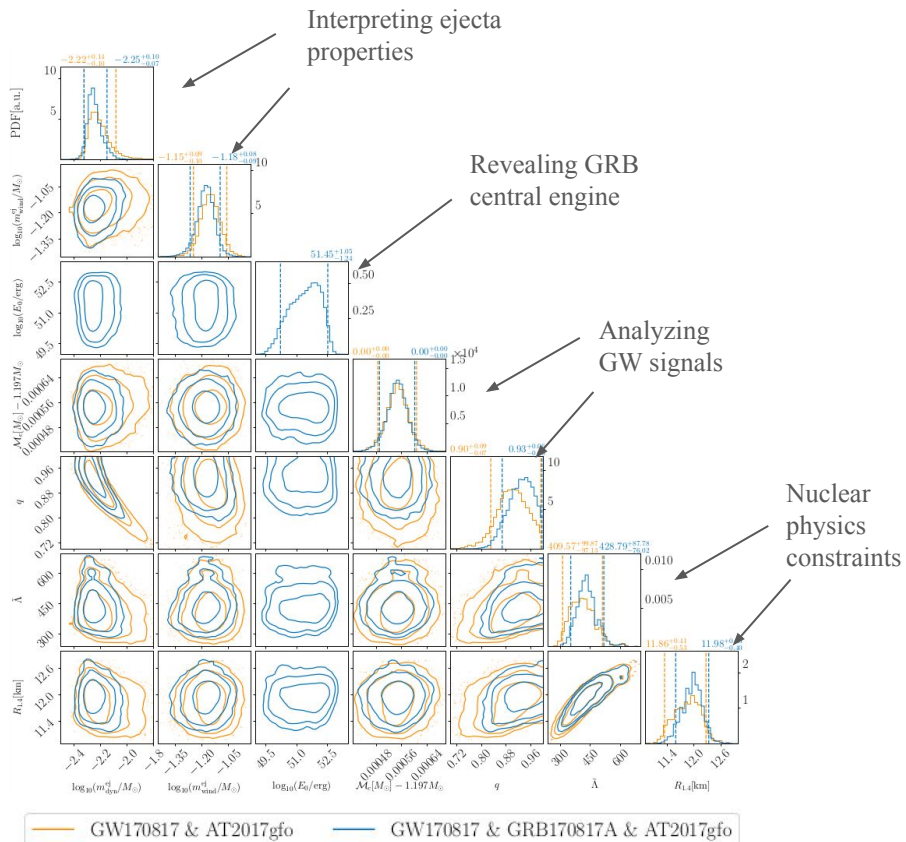
$$\mathcal{L}_{EM} \propto \exp\left(-\frac{1}{2} \sum_{ij} \frac{(m_i^j - m_i^{j,\text{est}}(\vec{\theta}))^2}{(\sigma_{i,\text{stat}}^j)^2 + \sigma_{\text{sys}}^2}\right)$$

Joint inference | [NMMA](#)

Pang et al. (2023)

$$\mathcal{L}(\vec{\theta}) = \mathcal{L}_{GW}(\vec{\theta}_{GW}) \times \mathcal{L}_{EM}(\vec{\theta}_{EM})$$

Bayesian inference



Pang et al. (2023)

Science case: Pang et al. 2023 | [NMMA](#)

- GW170817 + GRB170817A + AT2017gfo

$$\mathcal{L}(\vec{\theta}) = \mathcal{L}_{GW}(\vec{\theta}_{GW}) \times \mathcal{L}_{EM}(\vec{\theta}_{EM})$$

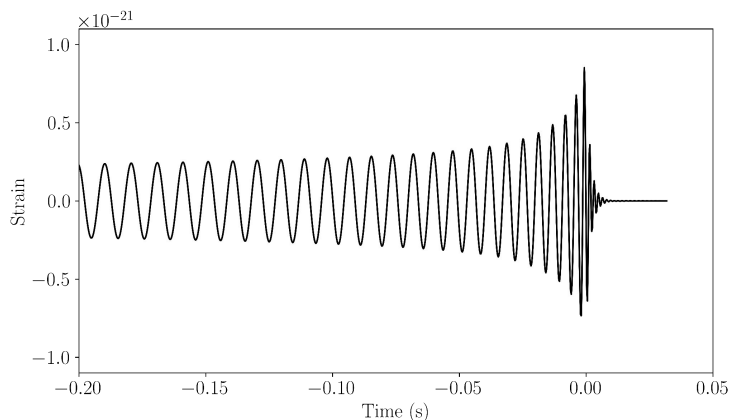
- including nuclear physics information | EOS

Models

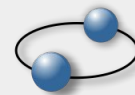
Gravitational waveform models

- Gravitational waveform in time domain

$$h(t) = \underbrace{A(t)}_{\text{Amplitude}} e^{-i\Psi(t)} \text{ Phase}$$



BNS sources



Post-Newtonian models

- TaylorF2

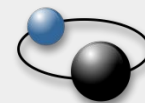
Effective-One-Body models

- SEOBNRv4_ROM_NRTidal

Phenomenological models

- PhenomD_NRTidal,
- PhenomPv2_NRTidal(v2, v3 | Abac et al. 2023)

NSBH sources



Phenomenological models

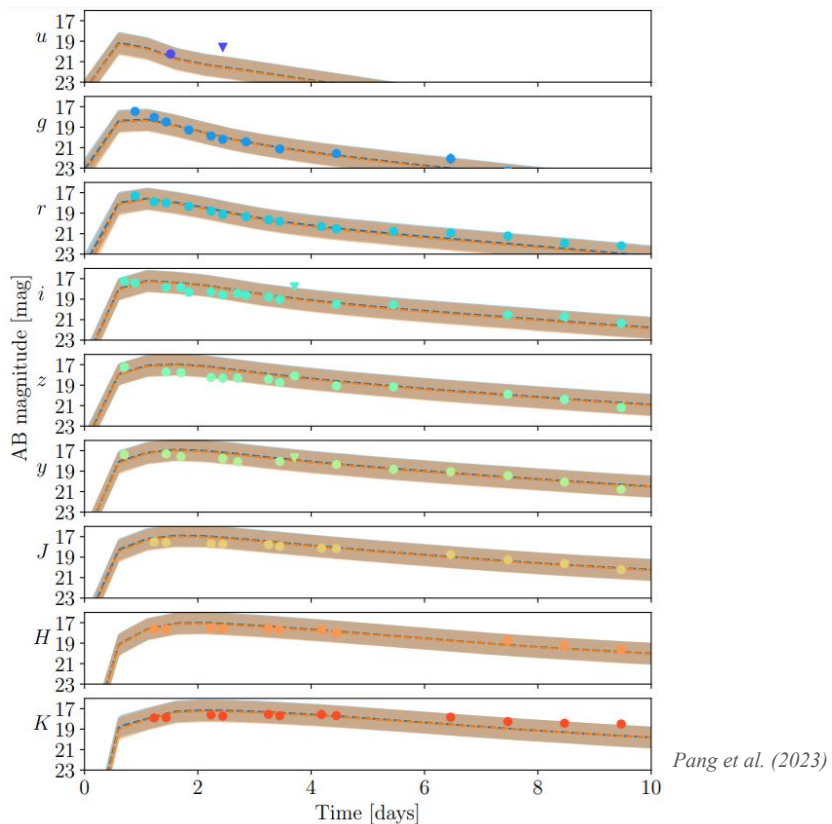
- IMRPhenomNSBH
- SEOBNRv4_ROM_NRTidalv2_NSBH

All GW models are enabled with: **LALsimulation**

(LIGO Scientific Collaboration, Algorithm Library LALsuite)

Models

Best-fit light curves | GW170817+GRB170817A+AT2017gfo



Electromagnetic (EM) transient models

Gamma-ray burst afterglow

- **afterglowpy** | Van Eerten et al. (2010), Ryan et al. (2020)
- soon: **Pyblastafterglow** | Nedora et al. (2021)

Kilonovae

- analytic models
- models based on radiative transfer simulations (POSSIS, Kasen et al.)

Supernovae

- SN models in **sncosmo** | (Levan et al. 2005)

Models

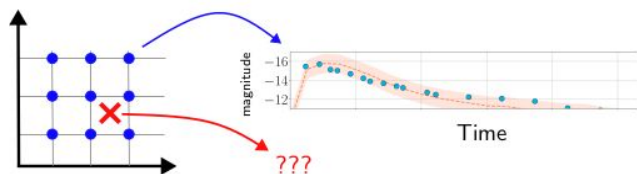
Kilonovae

- **radiative transfer simulation models**

e.g. POSSIS

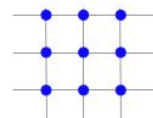
→ simulation at **grid points** provide light curves

→ light curve at arbitrary parameter values arise from **surrogate models**



Methods | EM transient models

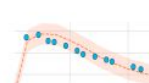
Grid points



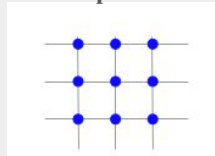
Neural networks



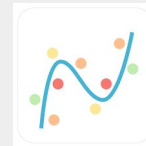
Light curve



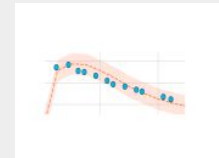
Grid points



Gaussian Process



Light curve

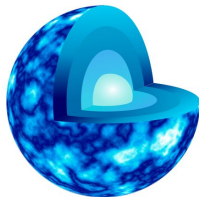


Regression

Including nuclear physics

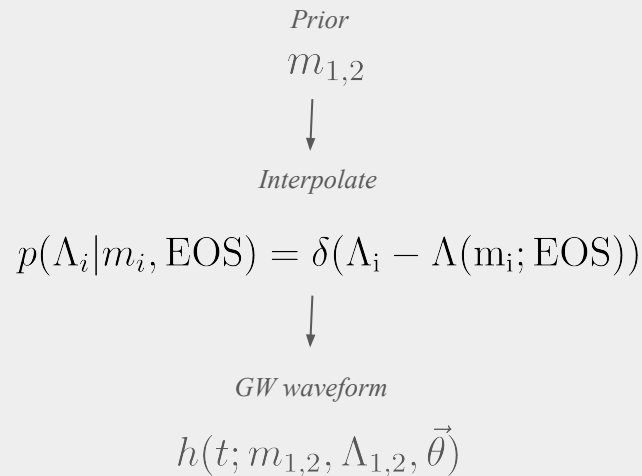
- use nuclear physics models to obtain

Equation-of-state



- ↓
- mass m ,
 - radius R ,
 - tidal deformability Λ

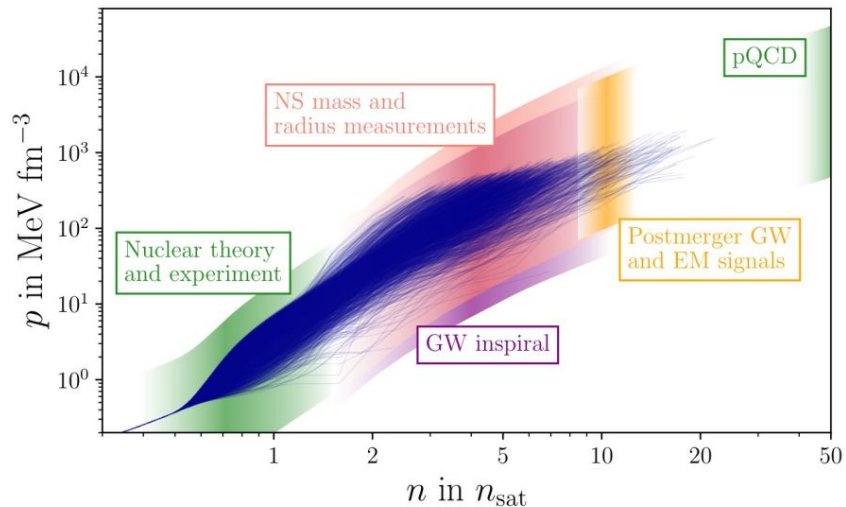
- sample on EOS during parameter estimation



Including nuclear physics

Science case: Study of Koehn et al. 2024

Constraints on the EOS from different research fields



Koehn et. al. (2024)

arXiv:2402.04172v1

Employed constraints

Nuclear

- Chiral EFT
- pQCD
- PREX-II
- CREX
- Heavy ion collisions

Isolated neutron stars

- Heavy pulsars
- NICER
- HESS object
- qLMXBs
- Thermo-nuclear accretion bursts

Binary neutron stars

- GW170817 + AT2017gfo + GRB170817A
- GW190425
- GRB211211A
- Post-merger constraint from GW170817

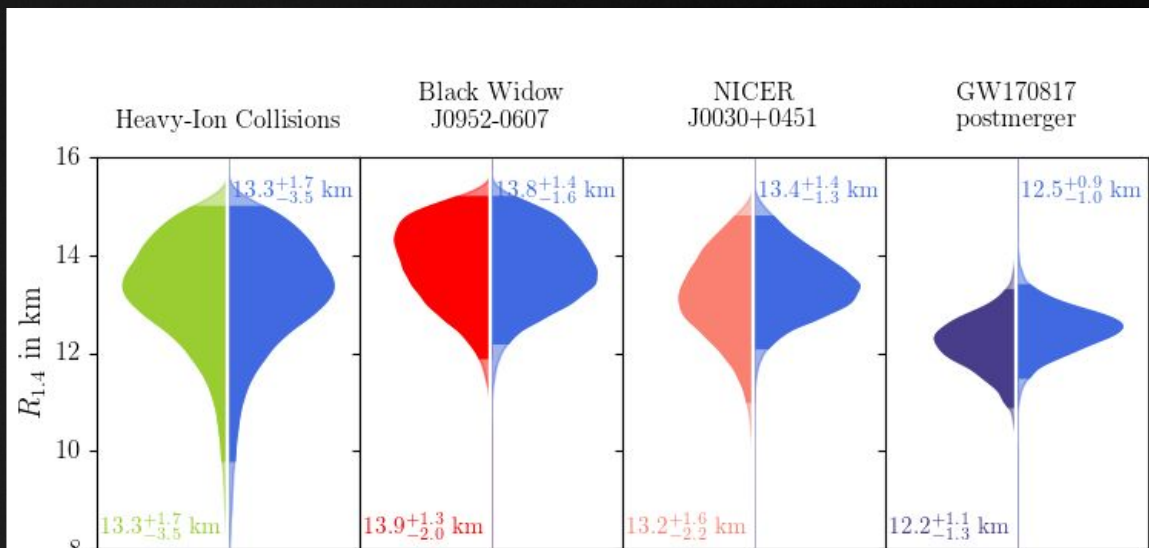
Combining different constraints on the EOS from different research fields



Science case:
Koehn et al. 2024
arXiv:2402.04172v1



Combining different constraints on the EOS from different research fields



Science case:

Koehn et al. 2024

arXiv:2402.04172v1



Bayesian inference

Hypothesis testing using **Bayes theorem**

$$\frac{p(\mathcal{H}_1|d, I)}{p(\mathcal{H}_2|d, I)} = \frac{p(d|\mathcal{H}_1, I)p(\mathcal{H}_1|I)}{p(d|\mathcal{H}_2, I)p(\mathcal{H}_2|I)}$$

\downarrow \downarrow \downarrow

$$\mathcal{O}_2^1 = \mathcal{B}_2^1 \times \Pi_2^1$$

Odds ratio *Bayes factor* *Prior Odds*

→ investigate the plausibility of competing models

Application: model selection

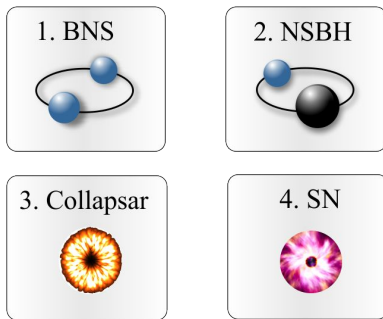
Interpreting: Bayes Factors

$\ln[\mathcal{B}_{\text{ref}}^1] < -4.61$	decisive evidence
$-4.61 \leq \ln[\mathcal{B}_{\text{ref}}^1] \leq -2.30$	strong evidence
$-2.30 \leq \ln[\mathcal{B}_{\text{ref}}^1] \leq -1.10$	substantial evidence
$-1.10 \leq \ln[\mathcal{B}_{\text{ref}}^1] \leq 0$	no strong evidence

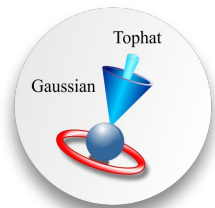
Bayesian inference

Studying the origin of GRB211211A

possible
scenarios



possible
GRB jet types



Science case: Study of Kunert et al. 2023

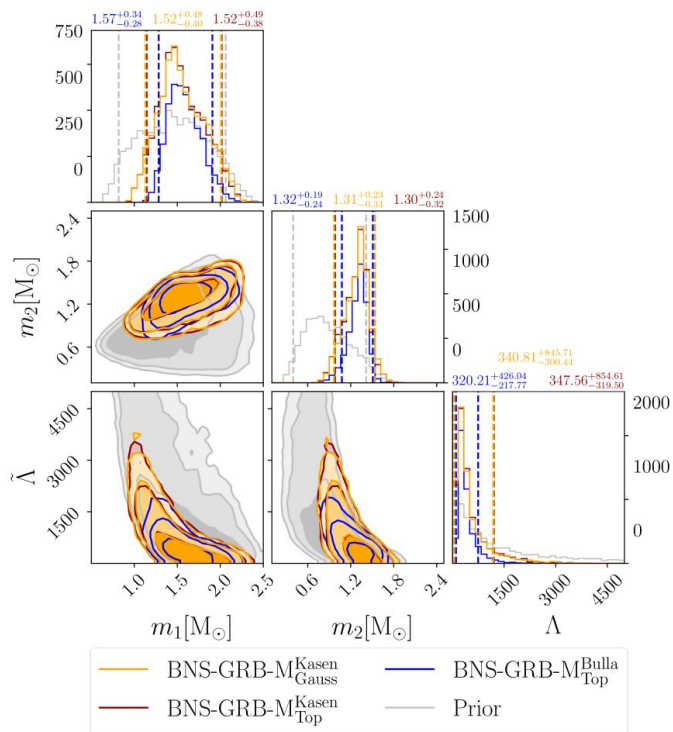
Results: Bayes factors

Name	Astrophysical Processes	GRB Jet Structure	Model dimension	Bayes factor $\ln[\mathcal{B}_{\text{ref}}^1]$
BNS-GRB- $M_{\text{top}}^{\text{Kasen}}$	Kilonova + GRB	Tophat	11	ref.
BNS-GRB- $M_{\text{Gauss}}^{\text{Kasen}}$	Kilonova + GRB	Gaussian	12	-1.21 ± 0.12
BNS-GRB- $M_{\text{top}}^{\text{Bulla}}$	Kilonova + GRB	Tophat	11	-4.51 ± 0.12
BNS-GRB- $M_{\text{Gauss}}^{\text{Bulla}}$	Kilonova + GRB	Gaussian	12	-6.26 ± 0.12
NSBH-GRB- M_{top}	Kilonova + GRB	Tophat	11	-8.41 ± 0.12
NSBH-GRB- M_{Gauss}	Kilonova + GRB	Gaussian	12	-10.56 ± 0.12
SNCOL-GRB- M_{top}	r CCSNe + GRB	Tophat	14	-15.24 ± 0.13
SNCOL-GRB- M_{Gauss}	r CCSNe + GRB	Gaussian	15	-16.97 ± 0.13
SN98bw-GRB- M_{top}	CCSNe + GRB	Tophat	8	-12.66 ± 0.12
SN98bw-GRB- M_{Gauss}	CCSNe + GRB	Gaussian	9	-12.59 ± 0.12
GRB- M_{top}	GRB	Tophat	8	-12.47 ± 0.12
GRB- M_{Gauss}	GRB	Gaussian	9	-12.65 ± 0.12

Kunert et al. (2023)

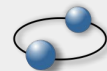
Connecting electromagnetic signals to binary properties

BNS properties of GRB211211A



Kunert et al. (2023)

BNS sources | phenomenological relations



- relation of **dynamical ejecta mass** | [Krueger & Foucart, (2020)]

$$\frac{m_{\text{dyn,fit}}^{\text{ej}}}{10^{-3} M_{\odot}} = \left(\frac{a}{C_1} + b \left(\frac{m_2}{m_1} \right)^n + c C_1 \right) + (1 \leftrightarrow 2)$$

- relation of **disk mass** | [Dietrich et al., (2020)]

$$\log_{10} \left(\frac{m_{\text{disk}}}{M_{\odot}} \right) = \max \left(-3, a \left(1 + b \tanh \left(\frac{c - (m_1 + m_2) M_{\text{threshold}}^{-1}}{d} \right) \right) \right)$$

Estimate the Hubble Constant

- evaluate linear Hubble relation

$$c \cdot z = v_H = H_0 \cdot D$$

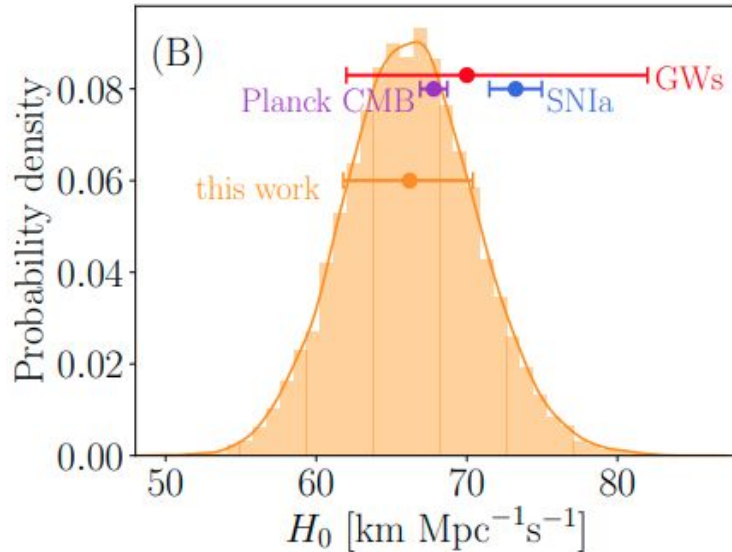
Applications:

- Gravitational-wave standard sirens
- Kilonovae standard candels
- Joint estimates (GW + EM)



H_0

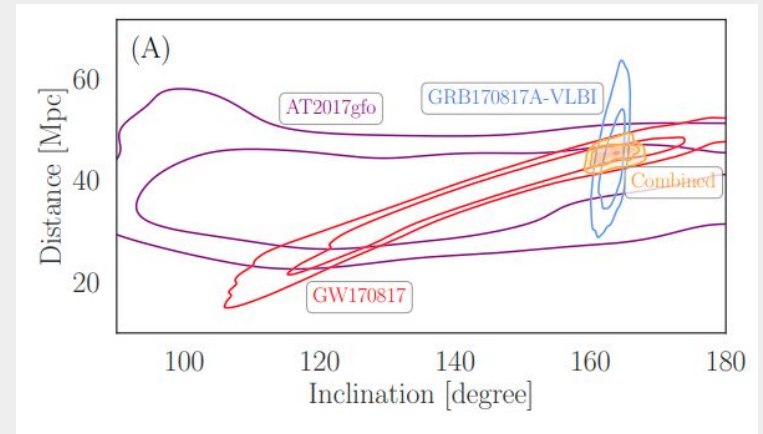
Estimate the Hubble Constant



Dietrich et. al, (2020)

Science case: Study of Dietrich et al. 2020

- use joint estimate of distance from GW170817+GRB170817A+AT2017gfo data



Dietrich et. al, (2020)

Current code developments

- Implementing new GRB model | pyblastafterglow
- Accelerating GW inference
- Sampling on nuclear parameters directly
- **Sampling on dark matter parameters**

> dark matter mass, m_χ

> dark matter fraction, f_χ

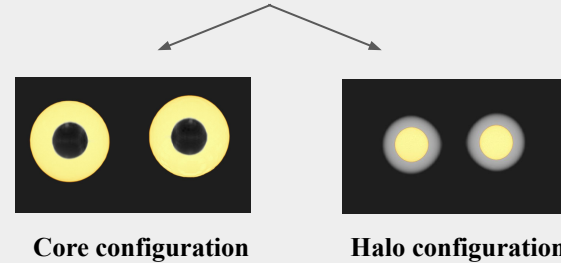
→ requires constructing DM EOS set



Dark matter | Theory

- Introduction by Violetta Sagun
 - simple case: fermionic dark matter
 - baryonic and dark matter only interact gravitationally

→ there are 2 possible configurations



NMMA: worldwide contributions



University Potsdam and Max Planck Institute
for Gravitational Physics

- computational astrophysics
- gravitational-wave modelling
- multi-messenger data analysis



University of Minnesota

- optical and near-infrared observations
- multi-messenger data analysis



Observatory of Côte d'Azur

- optical and near-infrared observations
- multi-messenger data analysis



Utrecht University

- gravitational-wave data analysis
- multi-messenger data analysis



University of Ferrara

- modelling of electromagnetic signals



Los Alamos National Lab

- nuclear physics

Observations

Theory



The  **NMMA** collaboration thanks for your attention!



Credit: Tohoku University