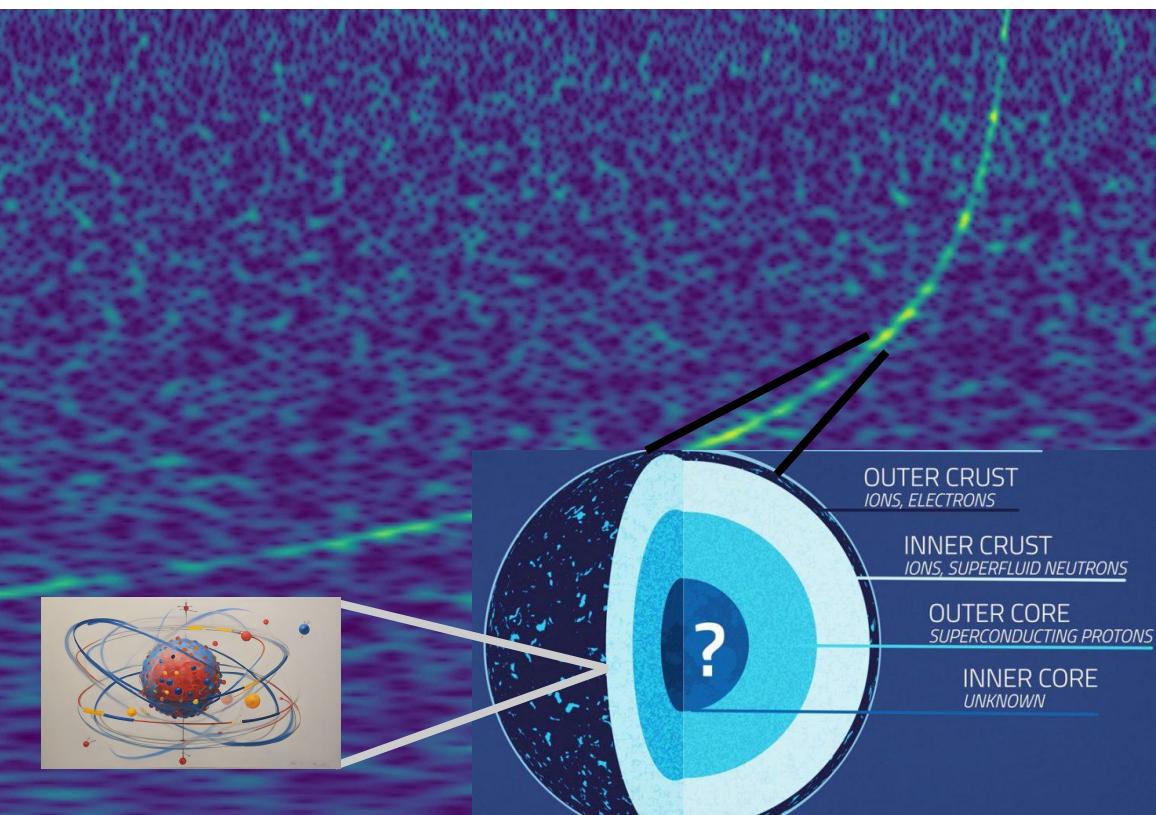
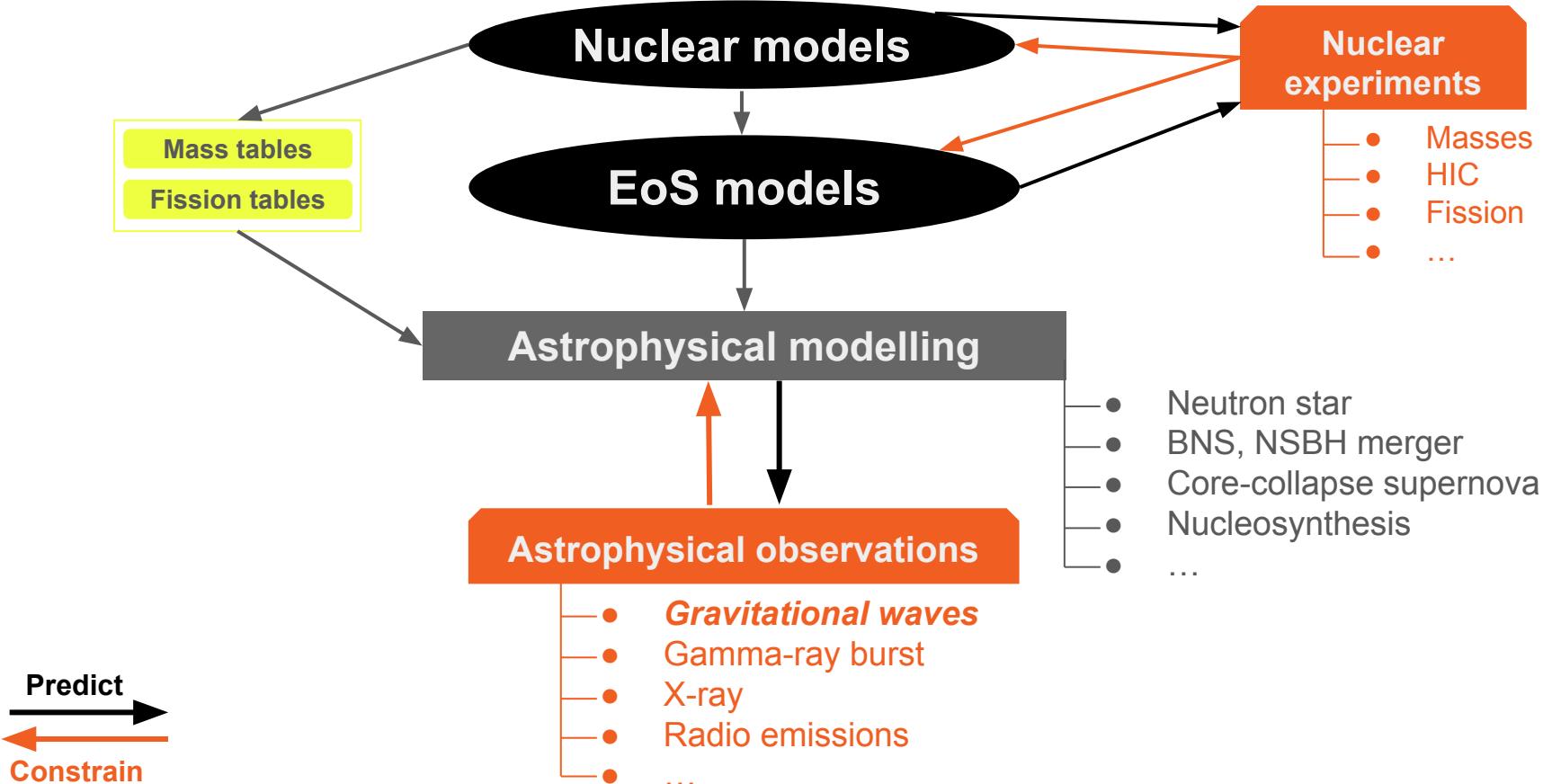


# Nuclear physics inputs for neutron stars and nucleosynthesis simulations

Guilherme Grams

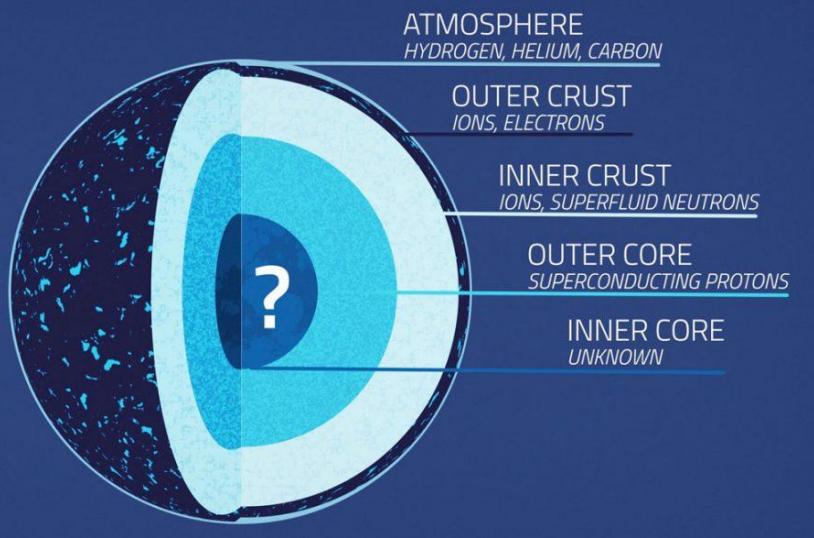


# Nuclear physics role in the multimessenger era



# Motivation

## Neutron star physics

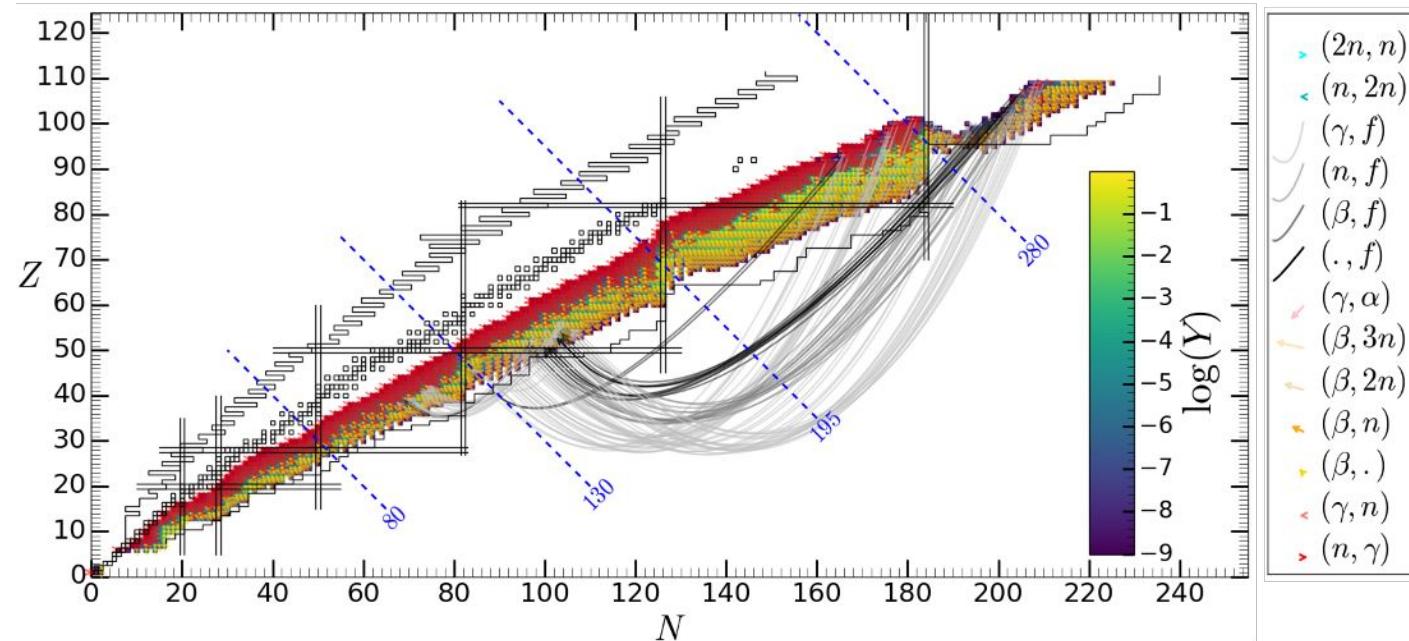


## Nuclear physics inputs:

- **masses** -> crust;
- superfluidity -> inner crust and core.
- **infinite nuclear matter** -> crust and core.
- **interaction** -> crust and core.
- phase transition(s) (quarks, hyperons, mesons,...) - > inner core.

# Motivation

## Nucleosynthesis



Neutron star merger

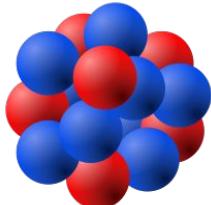


Supernova explosion



Description of **nuclear masses** and **fission path**  
in regions *unknown experimentally*.

# Energy Density Functional (EDF) theory


$$E = C_1(\rho)\rho^2 + C_2(\rho)\rho\tau + C_3(\rho)\nabla\rho\nabla\rho + \dots$$

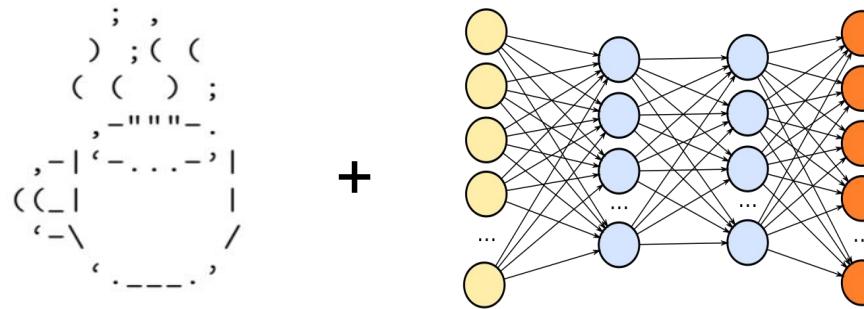
Energy →

Coupling constants

Local densities

- Effective description of nuclei based on one-body densities.
- **Good compromise between ab-initio and macroscopic calculations.**

# Brussels-Skyrme-on-a-grid (BSkG)

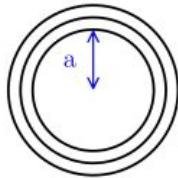


- Hartree-Fock-Bogoliubov (HFB) with a Skyrme force;
- *machine learning* to accelerate the fit.

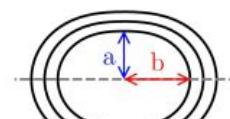
# HFB solver

## Nuclear shapes

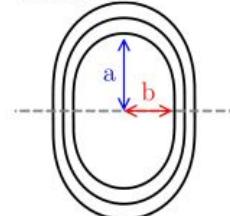
Spherical



Prolate



Oblate

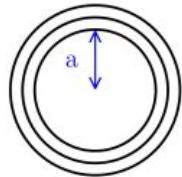


One DOF:  $\beta_{20}$

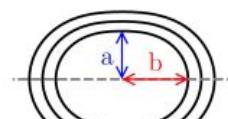
# HFB solver : MOCCa

## Nuclear shapes

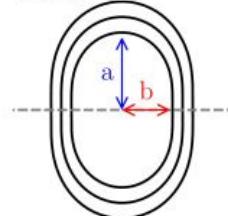
Spherical



Prolate



Oblate

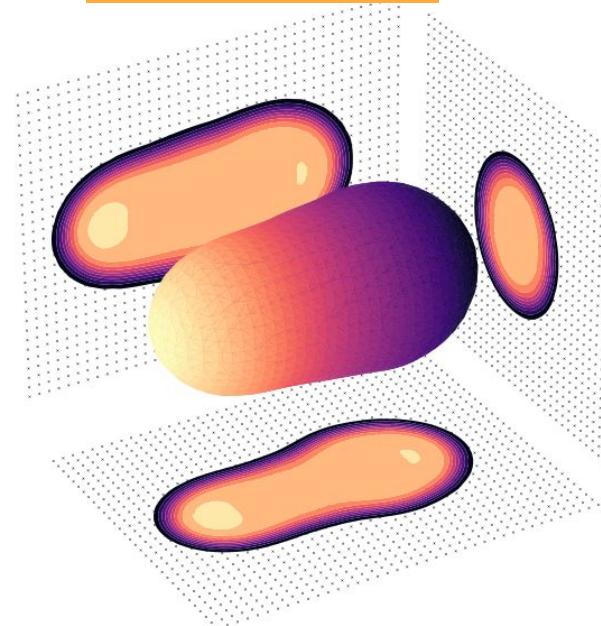


One DOF:  $\beta_{20}$

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Triaxial +  
octupole



HFB solver at 3D coordinate-space.  
W. Ryssens PhD Thesis, ULB (2016).

$\beta_{20}$ ,  $\beta_{22}$  and  $\beta_{30}$

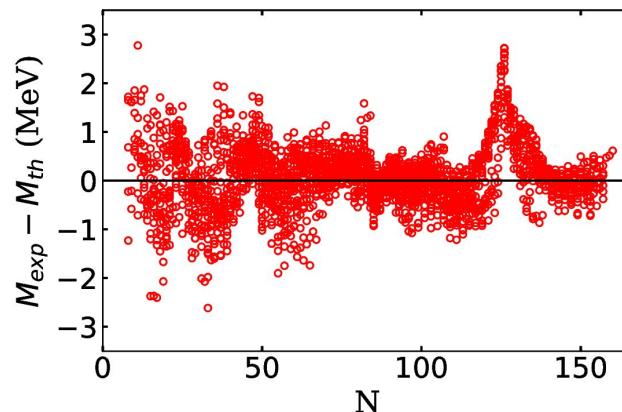
# The BSkG3 mass model

$$\sigma(M) = 0.631 \text{ MeV}$$

$$\sigma(R_C) = 0.0237 \text{ fm}$$

Reproduction of known nuclear masses.

All 2457 nuclei in  
the AME2020.



GG, W. Ryssens, G. Scamps, S. Goriely and N. Chamel, EPJA **59**, 270 (2023).

# The BSkG3 mass model

$$\sigma(M) = 0.631 \text{ MeV}$$
$$\sigma(R_C) = 0.0237 \text{ fm}$$

All 2457 nuclei in the AME2020.

Reproduction of known nuclear masses.

Comparison:

BSkG2

$\sigma(M) = 0.678 \text{ MeV}$

BSkG1

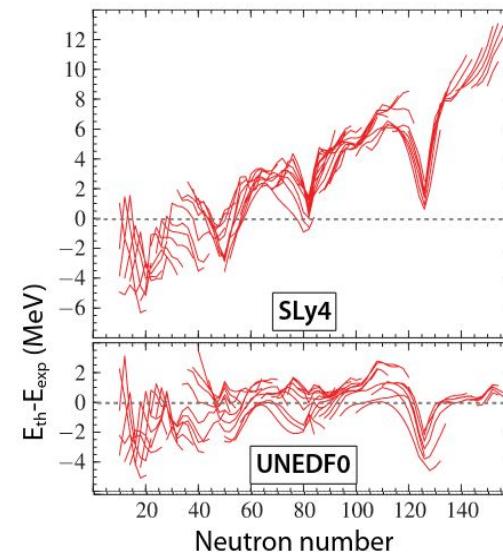
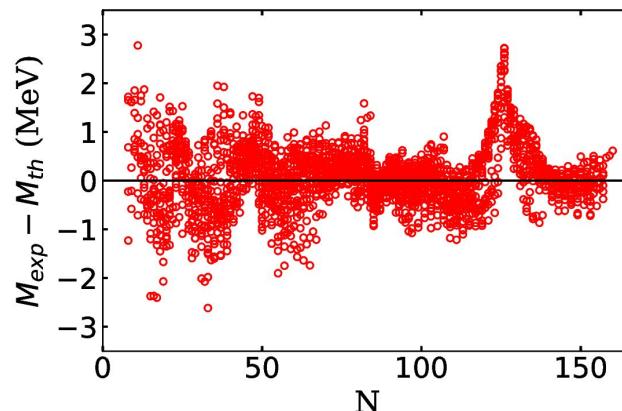
$\sigma(M) = 0.741 \text{ MeV}$

SLy4

$\sigma(M) = 4.80 \text{ MeV}$

UNEDF0

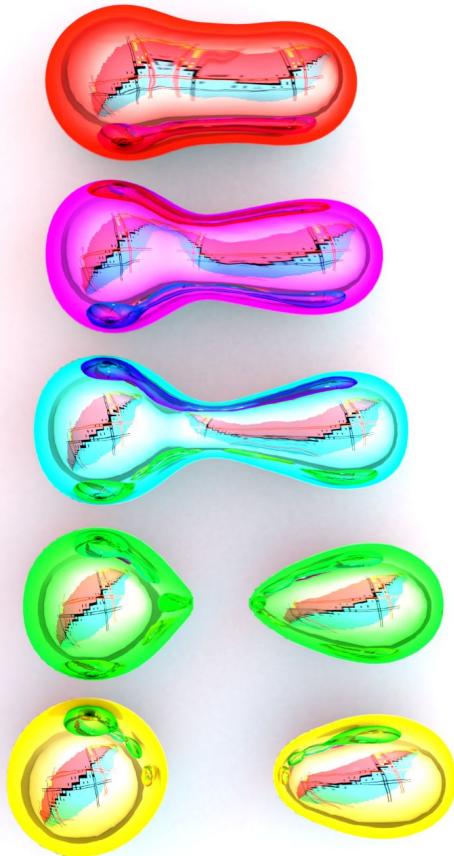
$\sigma(M) = 1.45 \text{ MeV}$



M. Kortelainen, et al.,  
PRC 82, 024313 (2010)

GG, W. Ryssens, G. Scamps, S. Goriely and N. Chamel, EPJA **59**, 270 (2023).

# BSkG3 fission



Impact r-process nucleosynthesis:

- "fission recycling";
- the **r-process abundances** in the  $110 \leq A \leq 170$  region;
- the production of cosmic chronometers such as Th and U;
- the **heating rate of kilonovae**.

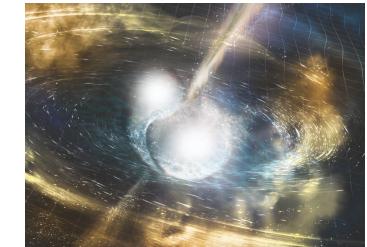
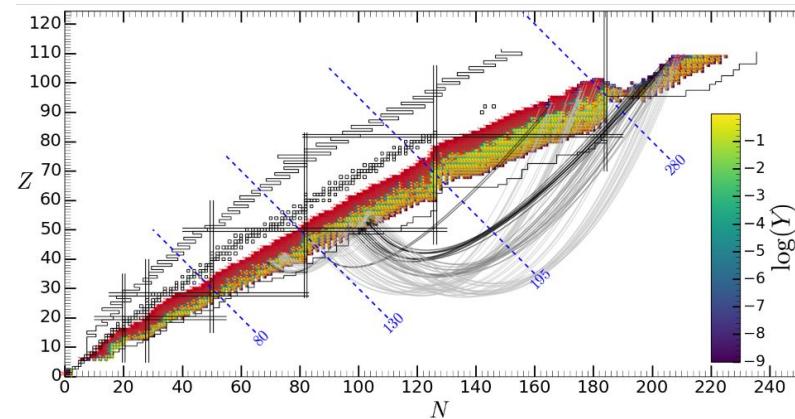


Fig from G. Scamps.

# BSkG3 fission

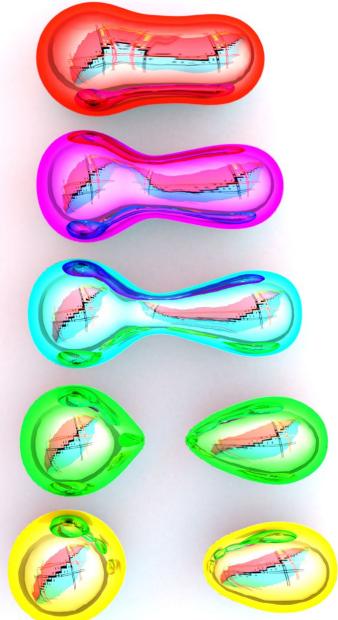


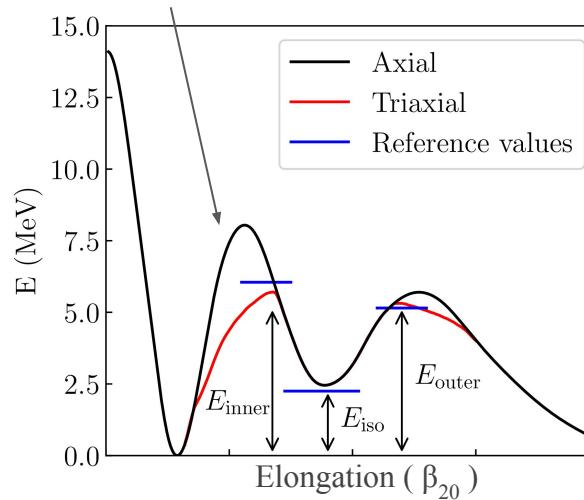
Fig from G. Scamps.

BSkG3:

$$\sigma(E_1) = 0.33 \text{ MeV}$$

$$\varepsilon(E_1) = +0.06 \text{ MeV}$$

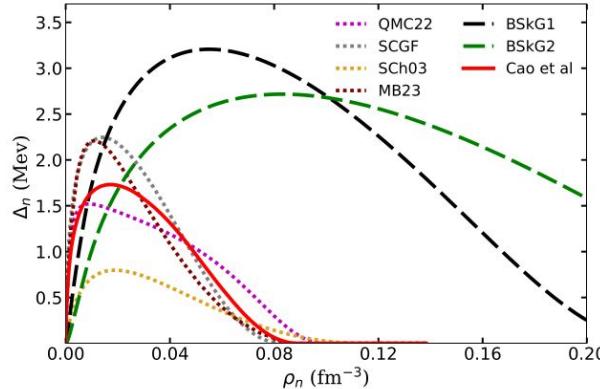
Primary ( $E_1$ ) **fission barrier** heights of actinide nuclei.



Comparison:	
<b>BSkG2</b>	$\sigma(E_1) = 0.44 \text{ MeV}$
<b>HFB-14</b>	$\sigma(E_1) = 0.60 \text{ MeV}$
<b>FRLDM</b>	$\sigma(E_1) = 0.81 \text{ MeV}$
<b>BCPM</b>	$\sigma(E_1) = 1.42 \text{ MeV}$
<b>SLy6</b>	$\sigma(E_1) = 3.89 \text{ MeV}$
<b>NL3</b>	$\sigma(E_1) = 2.18 \text{ MeV}$
<b>DD-ME2</b>	$\sigma(E_1) = 3.35 \text{ MeV}$

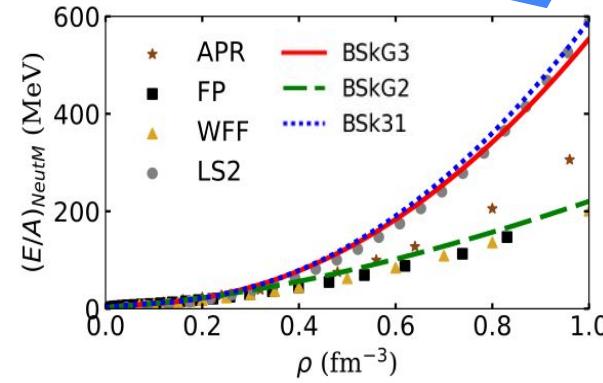
# BSkG3 nuclear matter properties

## NS inner crust



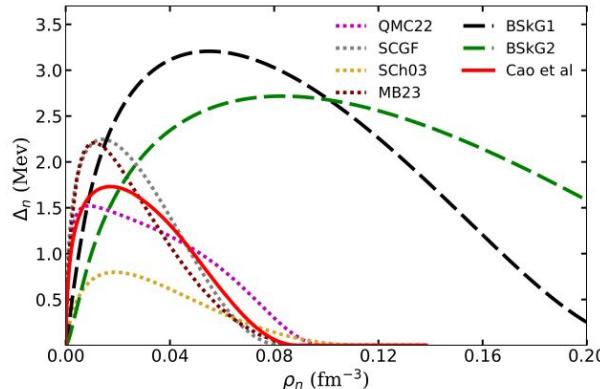
new pairing  
prescription

## heavy neutron stars



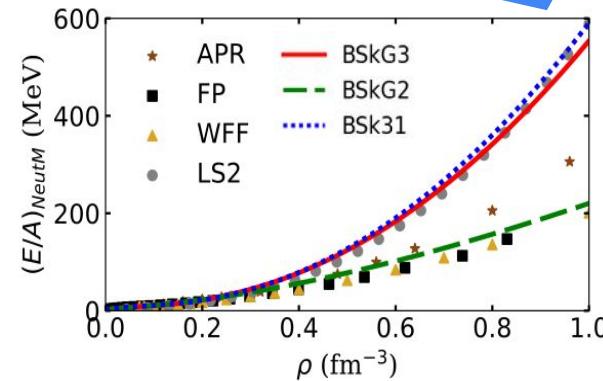
# BSkG3 nuclear matter properties

## NS inner crust



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prescription

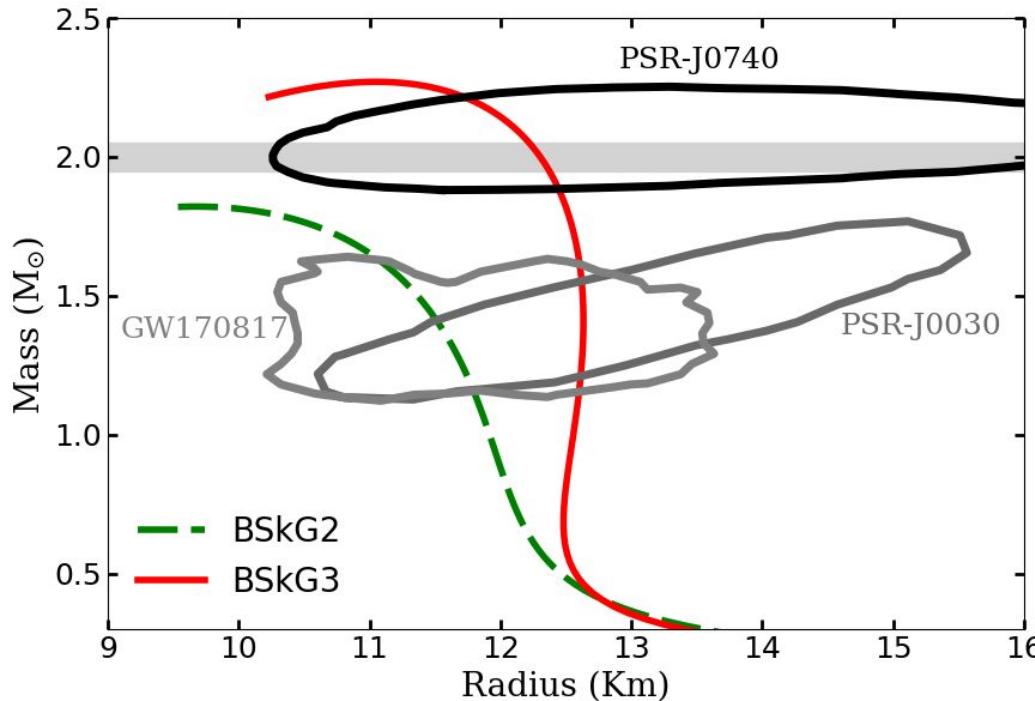
## heavy neutron stars



Impacts NS seismology,  
glitches, cooling, and  
continuous GW emission.

Essential to describe  
heavy pulsars

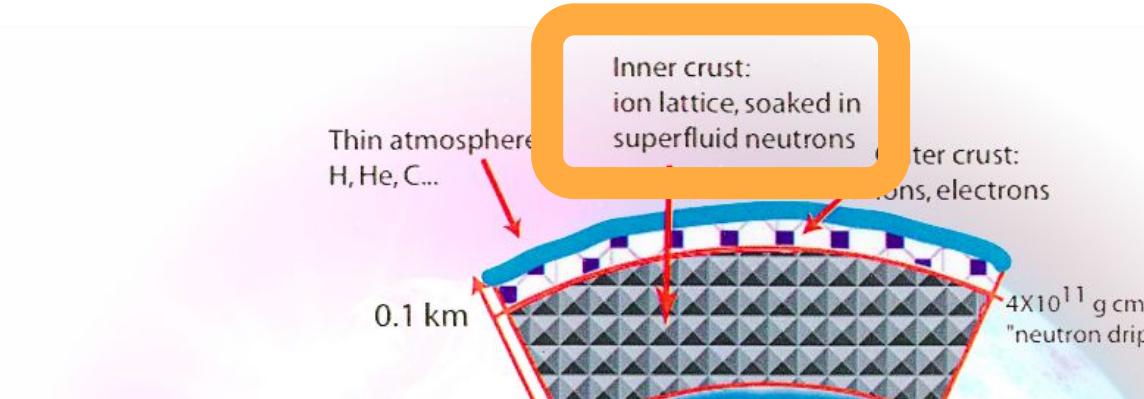
# BSkG3 neutron star



$$\begin{aligned} R_{1.4} &= 12.6 \text{ km} \\ M_{\max} &= 2.3 \text{ Msun} \\ R_{M\max} &= 11.1 \text{ km} \end{aligned}$$

GG, W. Ryssens, G. Scamps, S. Goriely and N. Chamel, EPJA **59**, 270 (2023).

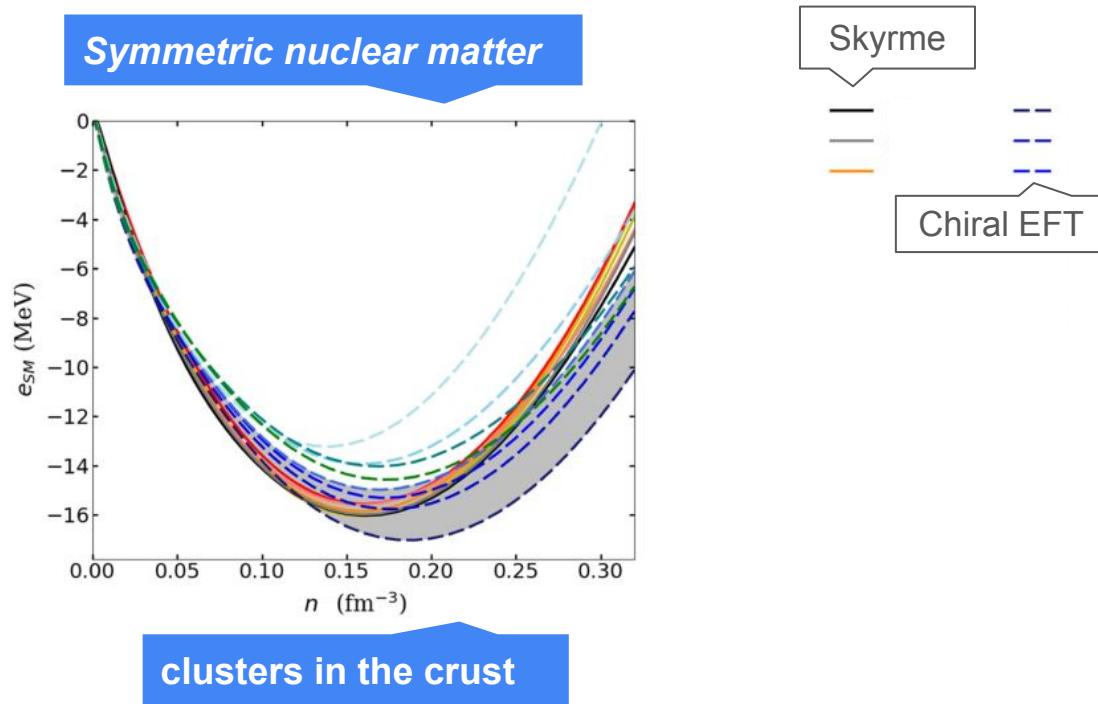
# Nuclear physics in neutron stars crust



- Uncertainties from model predictions in the crust.
- Meta-model<sup>1</sup> + compressible liquid drop model.

1: J. Margueron et. al., PRC 97 025805 (2018).

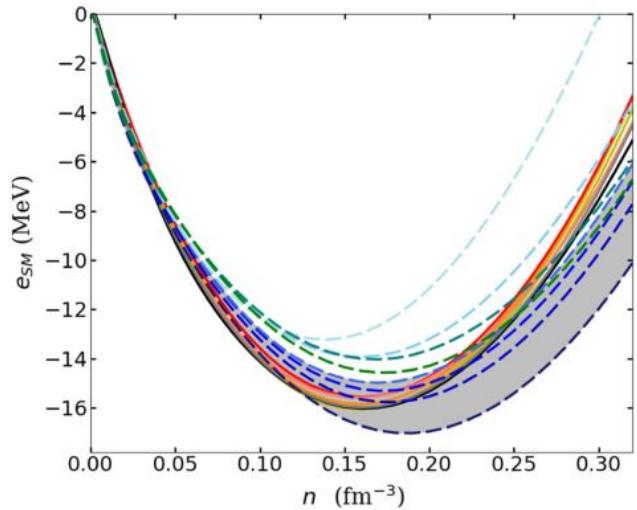
# Nuclear physics in neutron stars crust



GG, J. Margueron, R. Somasundaram, and S. Reddy, EPJA **58**, 56 (2022).

# Nuclear physics in neutron stars crust

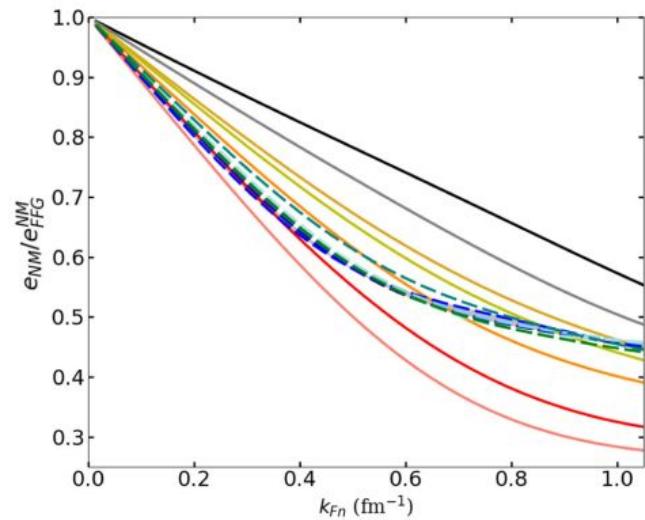
Symmetric nuclear matter



clusters in the crust

Skyrme  
—  
—  
—  
Chiral EFT  
---  
- - -

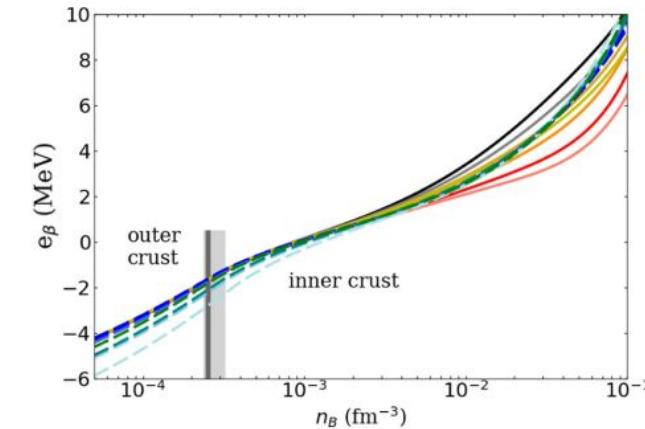
Pure neutron matter



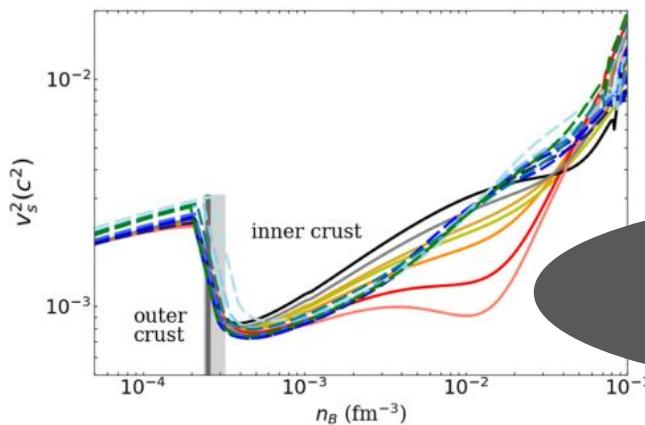
(super)fluid in the inner-crust

GG, J. Margueron, R. Somasundaram, and S. Reddy, EPJA **58**, 56 (2022).

# Role of neutron and symmetric matter at the crust?



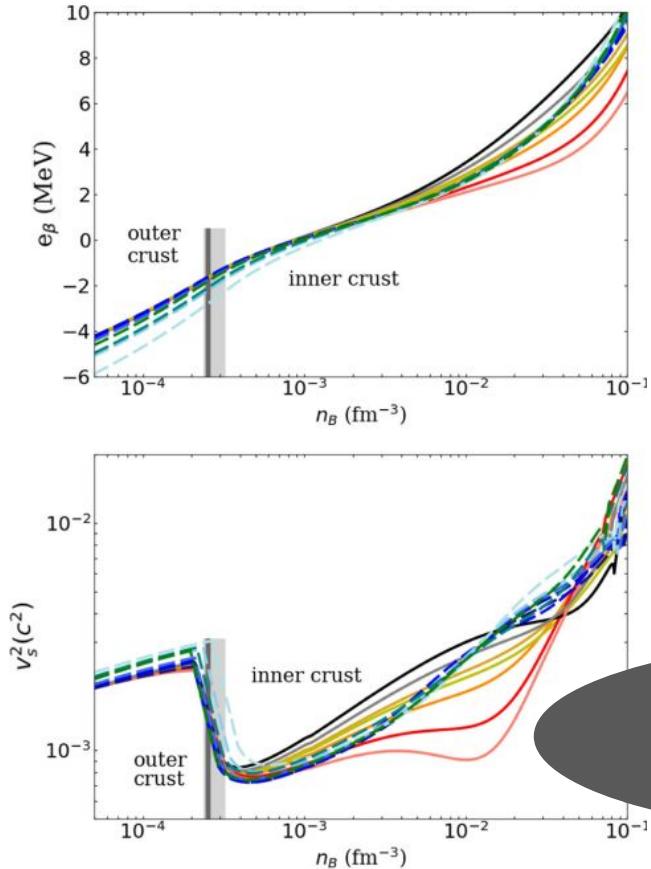
Skyrme  
—  
—  
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Chiral EFT  
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Neutron matter controls  
energy, and its derivatives

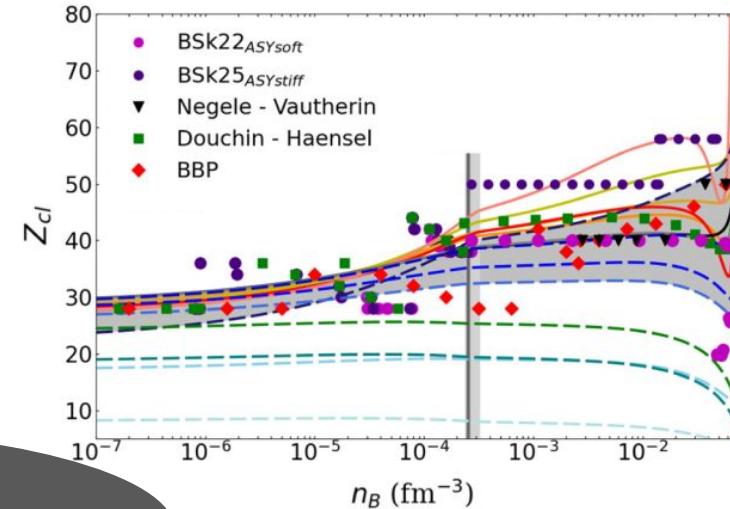
GG, J. Margueron, R. Somasundaram, and S. Reddy, EPJA **58**, 56 (2022).

# Role of neutron and symmetric matter at the crust?



Skyrme  
—  
—  
—  
Chiral EFT  
---  
---

Symmetric matter controls composition ( $Z, A$ )



Neutron matter controls energy, and its derivatives

GG, J. Margueron, R. Somasundaram, and S. Reddy, EPJA **58**, 56 (2022).

# Outlook

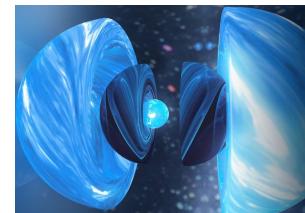
## BSkG nuclear structure models

- Competitive for nuclear masses and radii.
- *Unmatched* for fission barriers.
- Link with experimental data.
- Break symmetries: triaxial, octupole shapes.
- **Inputs for neutron stars and nucleosynthesis.**



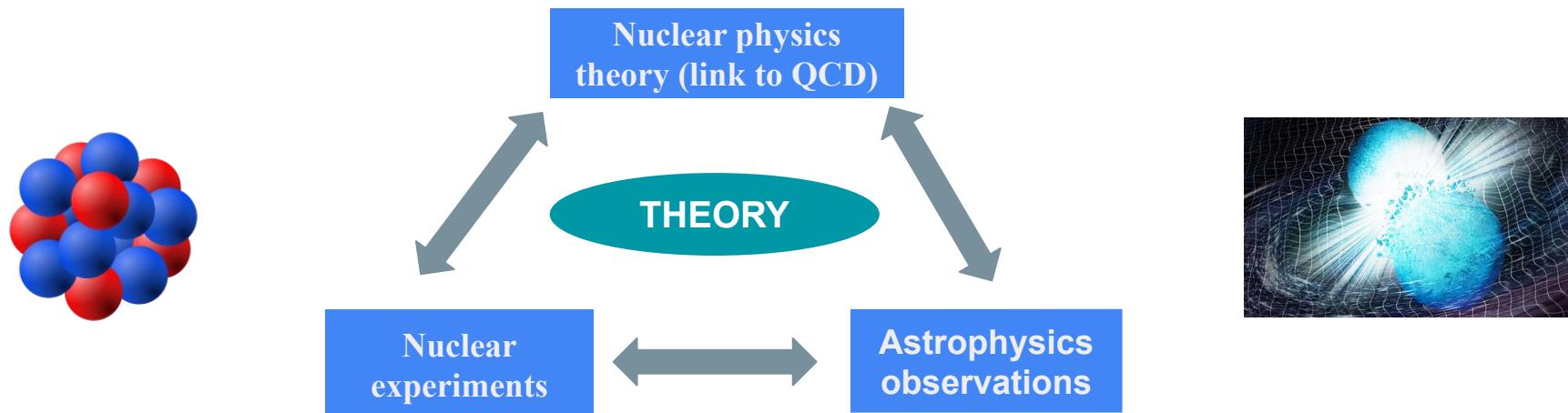
## Uncertainties on NS crust

- Energy, pressure, sound speed,  $Y_e$ , are controlled by *neutron matter* properties.
- Composition ( $Z, A$ ) is controlled by symmetric matter and *experimental masses*.



# Outlook

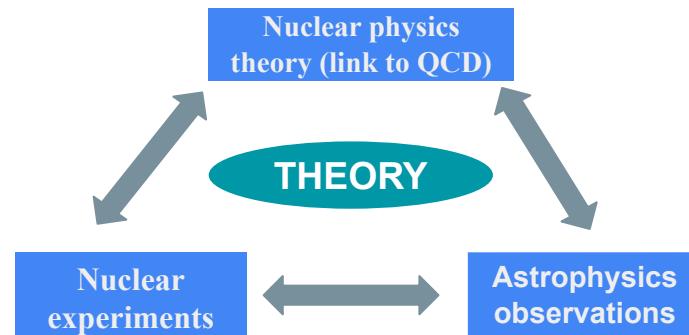
- EoS of (hot) dense matter:
  - macroscopic models-Bayesian,
  - Machine learning,
  - Deformed HFB.
- Impact on multi-messenger observations.



# Acknowledgements

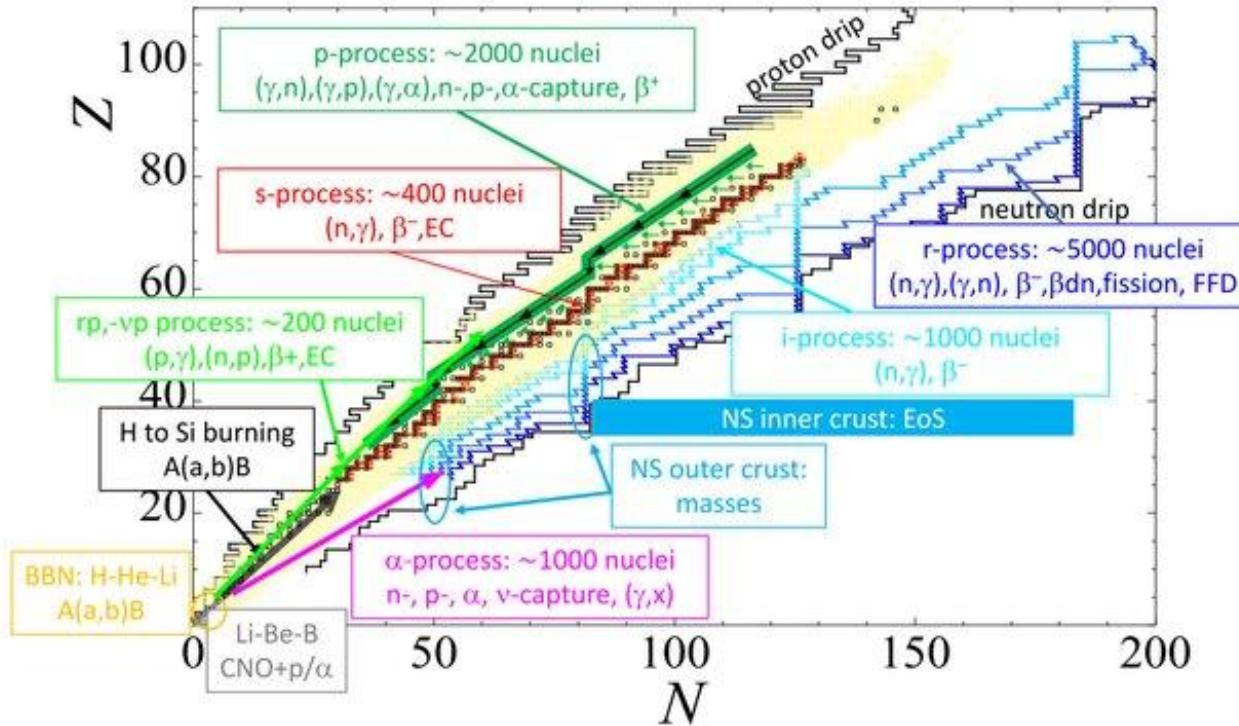
- Collaborators: Wouter Ryssens, Guillaume Scamps, Stephane Goriely, Nicolas Chamel, and Jérôme Margueron.
- Computational resources provided by the *Consortium des Équipements de Calcul Intensif* (CECI).
- Funding agencies FNRS and FWO.
- EVEREST and MANASLU EOS projects.

• Thank you for the attention!

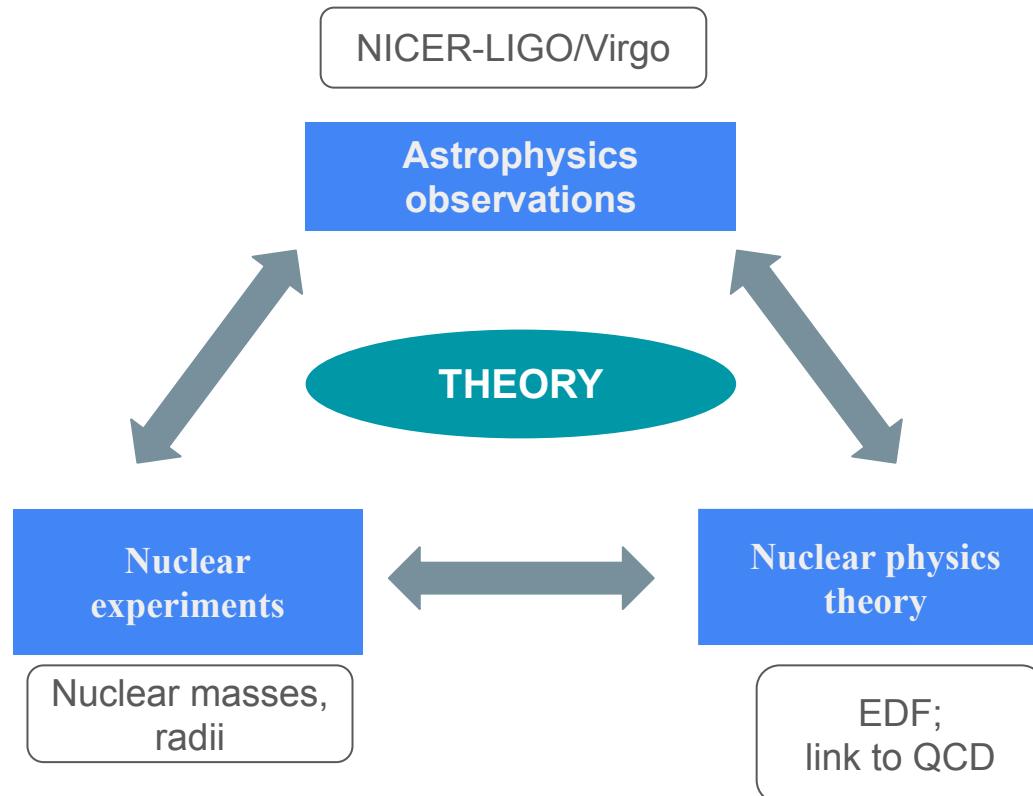


extra slides

# Motivation



# Summary



# Nuclear physics in neutron stars crust

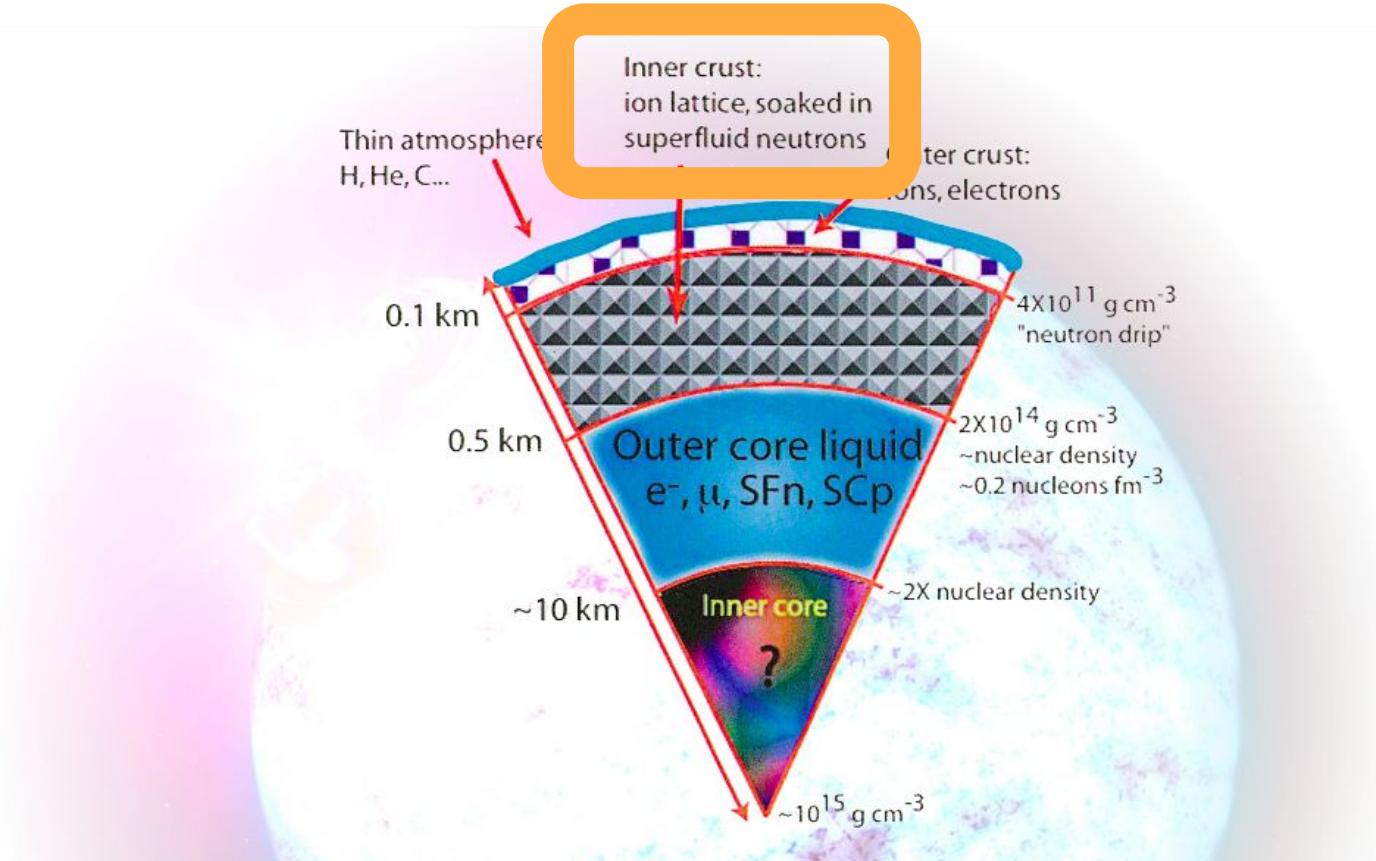
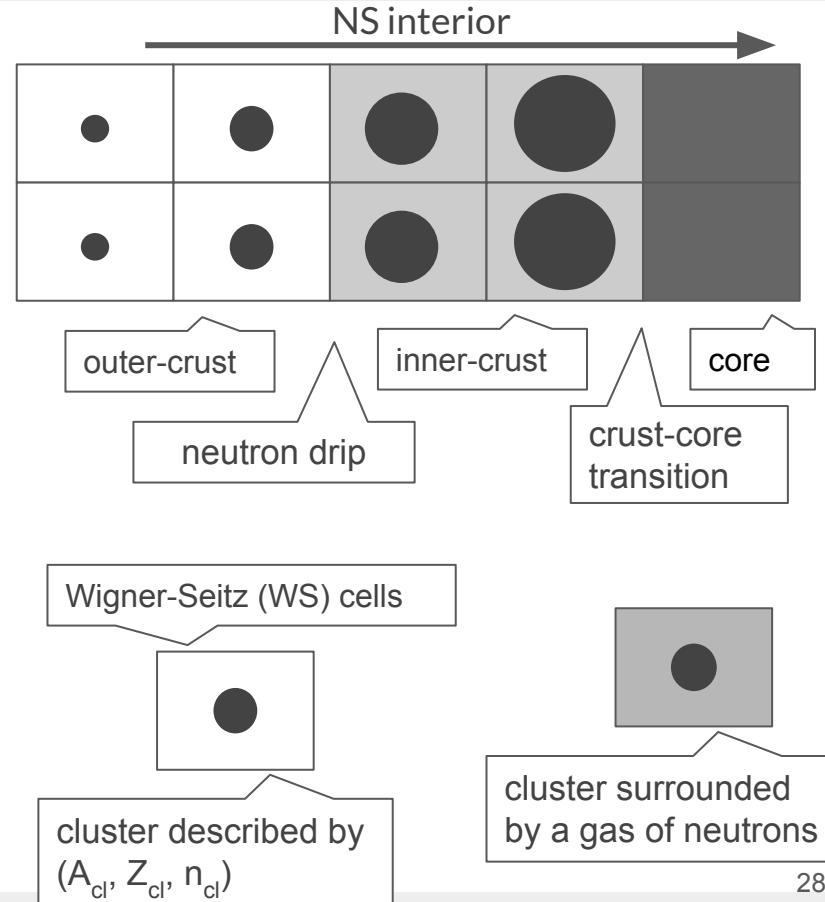
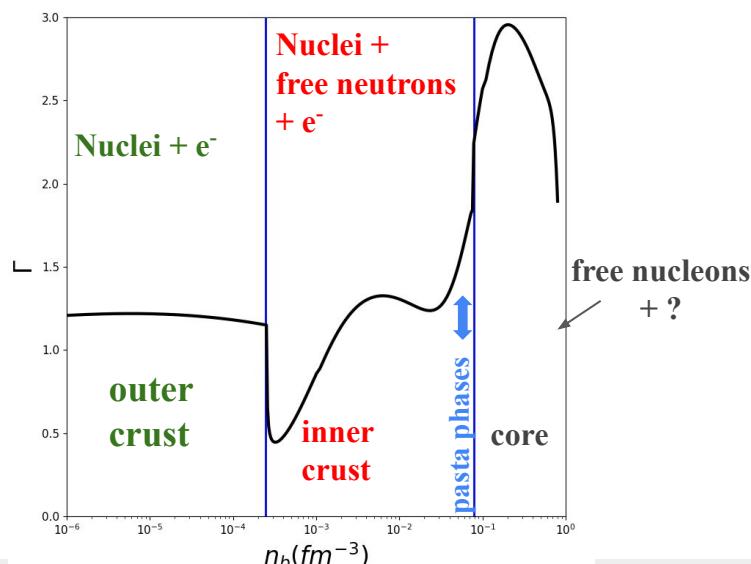


Fig. from Arzoumanian et. al. (2009) arXiv:0902.3264

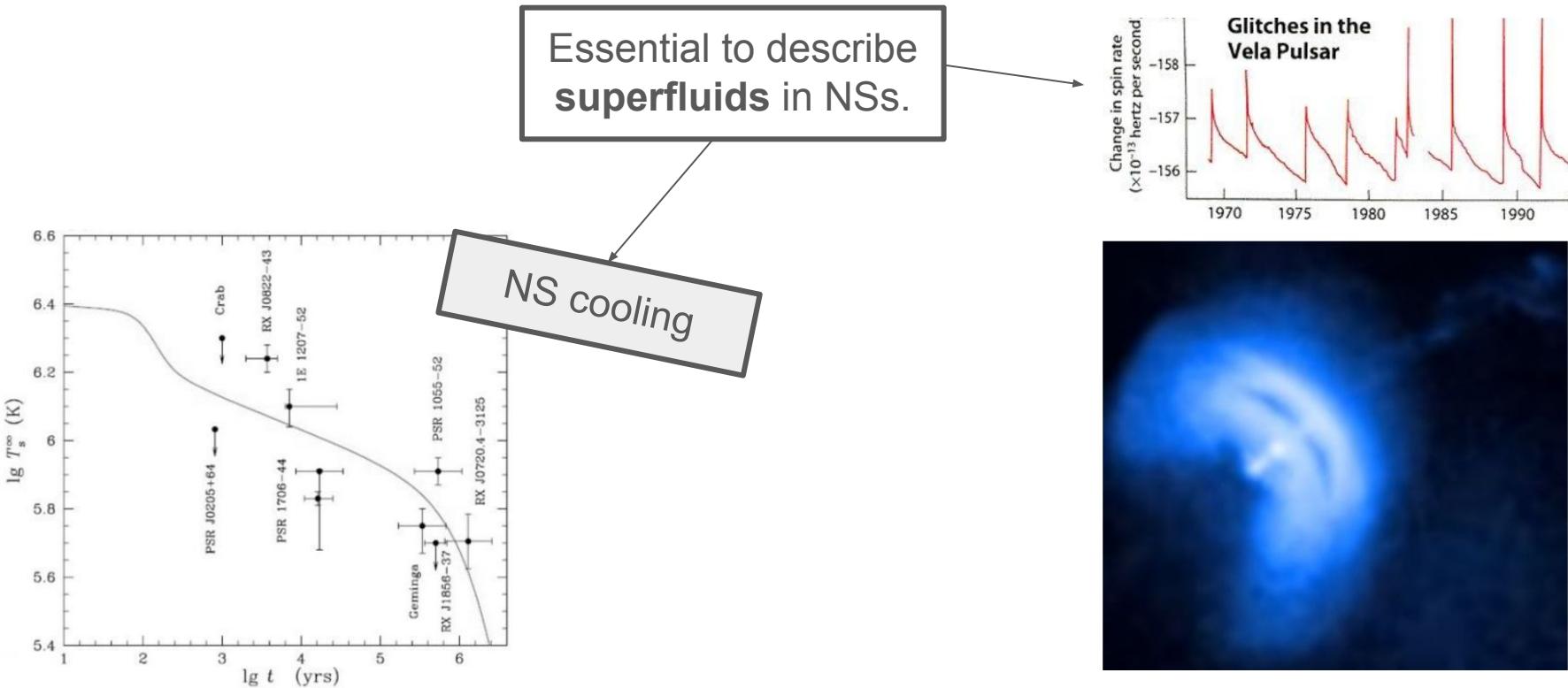
# Finite size effects / nuclei description

Unified EoS = same nuclear interaction to describe:

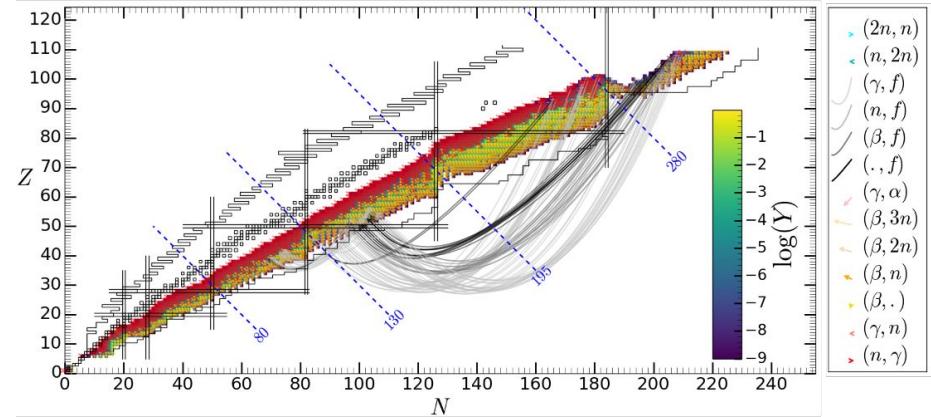
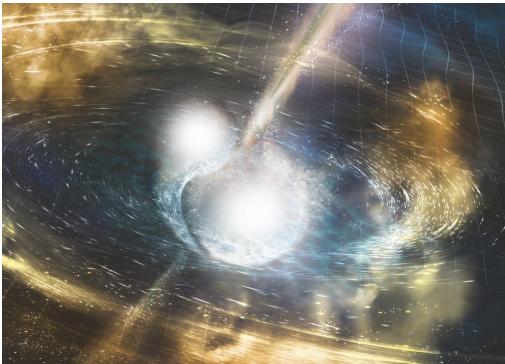
1. Bulk contribution in the cluster ( $A_{\text{cl}}, Z_{\text{cl}}$ );
2. Neutron gas;
3. Homogeneous matter (core).



# Pairing on NS inner crust

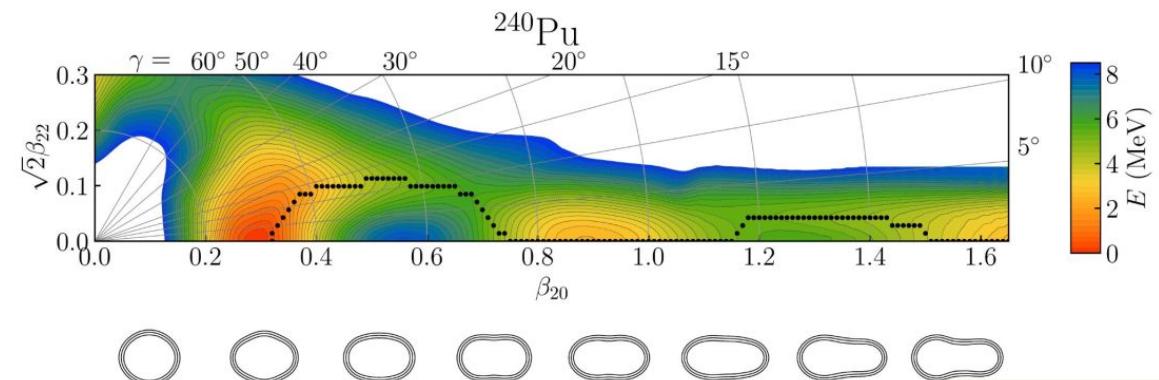


# BSkG3 fission barriers

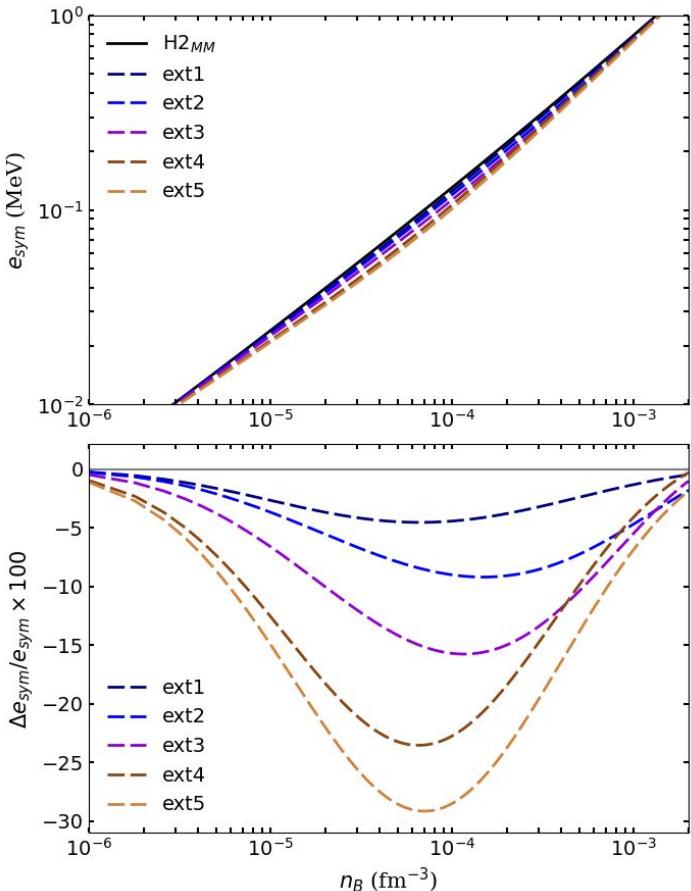


Fission properties impact several aspects of the r-process such as:

- the details of "**fission recycling**";
- the **r-process abundances** in the  $110 \leq A \leq 170$  region;
- the production of cosmic chronometers such as Th and U;
- the **heating rate of kilonovae**.

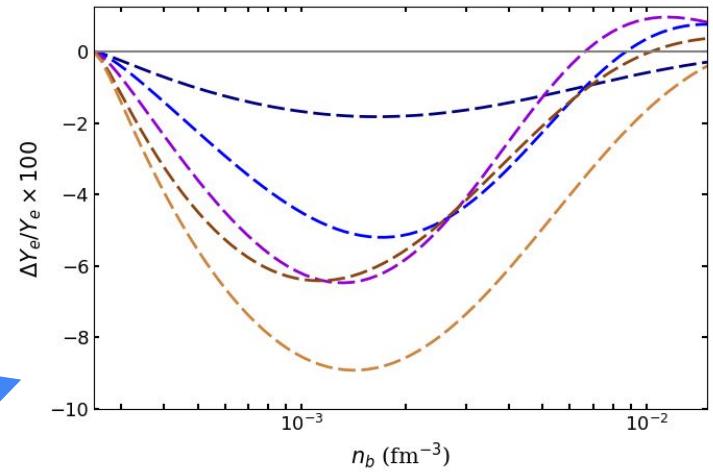


# Dilute neutron matter in the NS inner crust



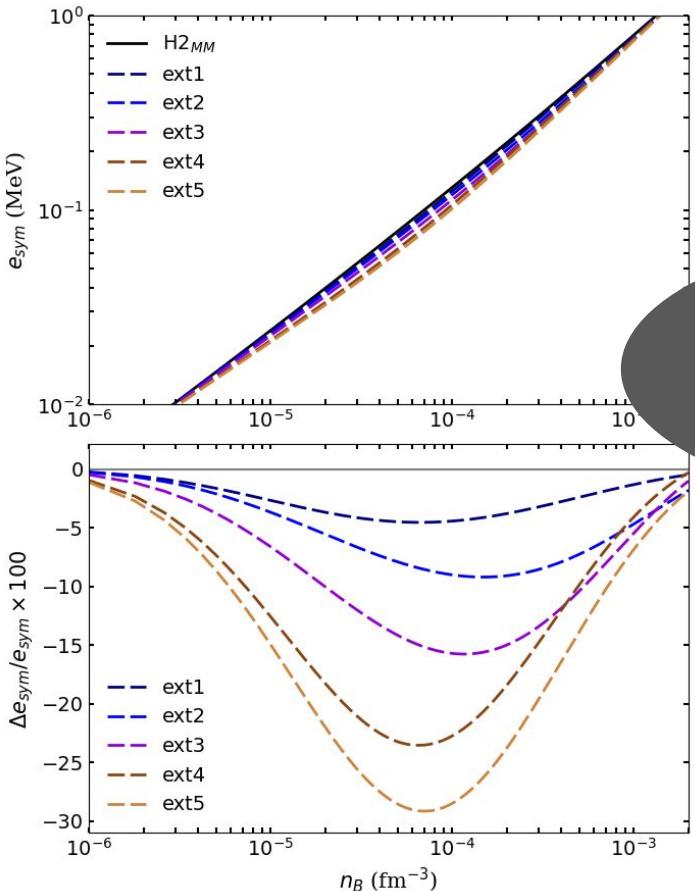
Neutron matter energy impacts  
the *symmetry energy*:  
 $e_{\text{sym}} = e_{\text{NeutM}} - e_{\text{SM}}$

Symmetry energy  
controls  
particle fractions



GG and J. Margueron, arXiv:2401.13590 (2024).

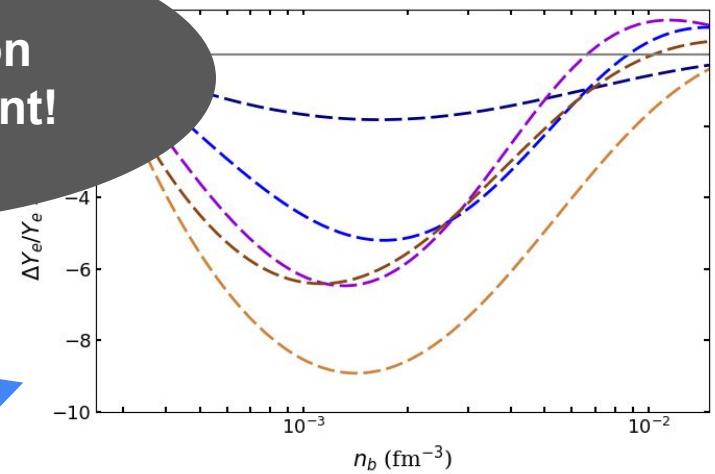
# Dilute neutron matter in the NS inner crust



Neutron matter energy impacts  
the *symmetry energy*:  
 $e_{\text{sym}} = e_{\text{NeutM}} - e_{\text{SM}}$

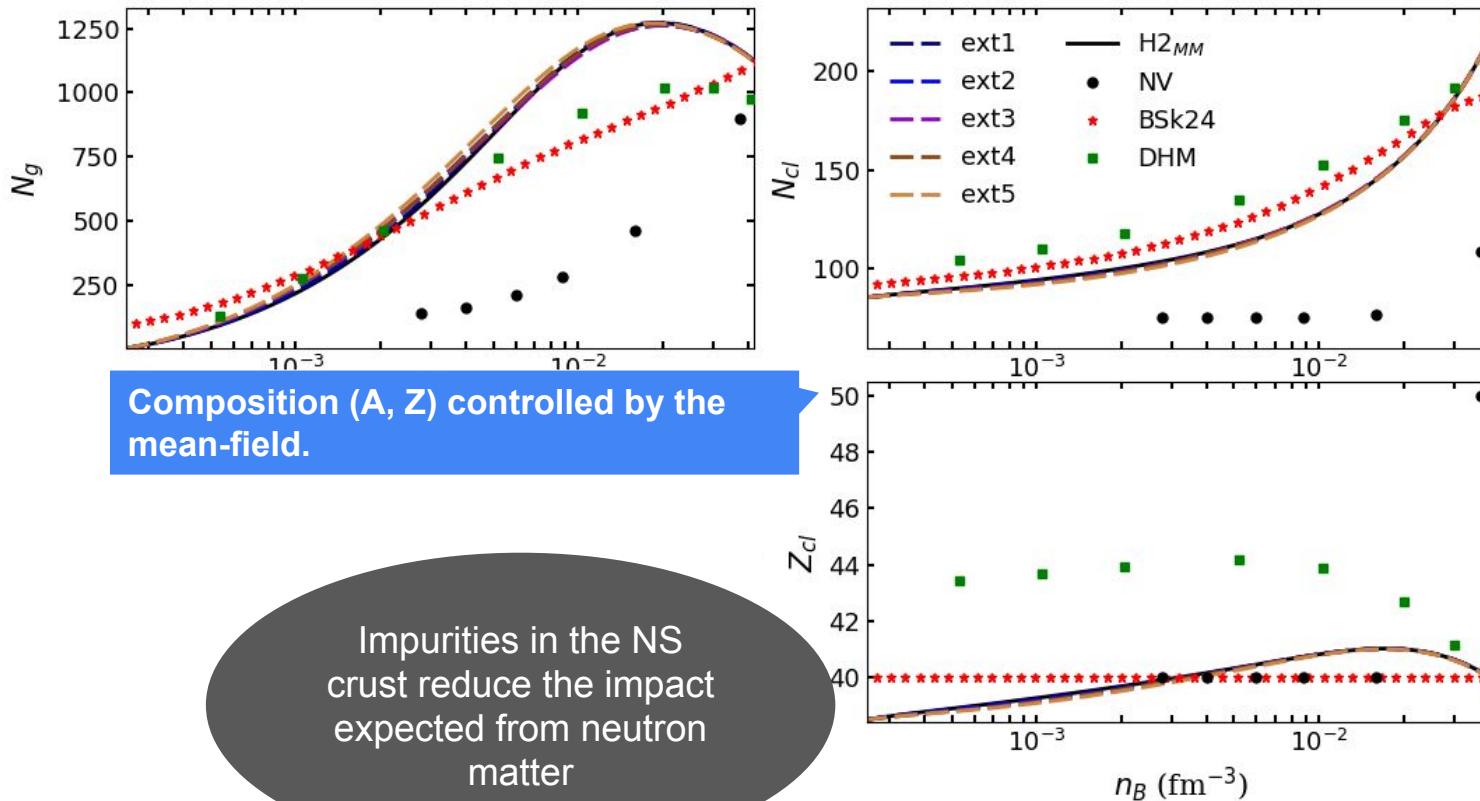
Effect on neutron  
matter is important!

Symmetry energy  
controls  
particle fractions



GG and J. Margueron, arXiv:2401.13590 (2024).

# Dilute neutron matter in the NS inner crust



GG and J. Margueron, arXiv:2401.13590 (2024).