

Global Network of Cavities to Search for Gravitational Waves: GravNet

A novel scheme to hunt gravitational waves signatures from the early universe

"Gravitational Wave probes of Fundamental Physics", Rome, 2024

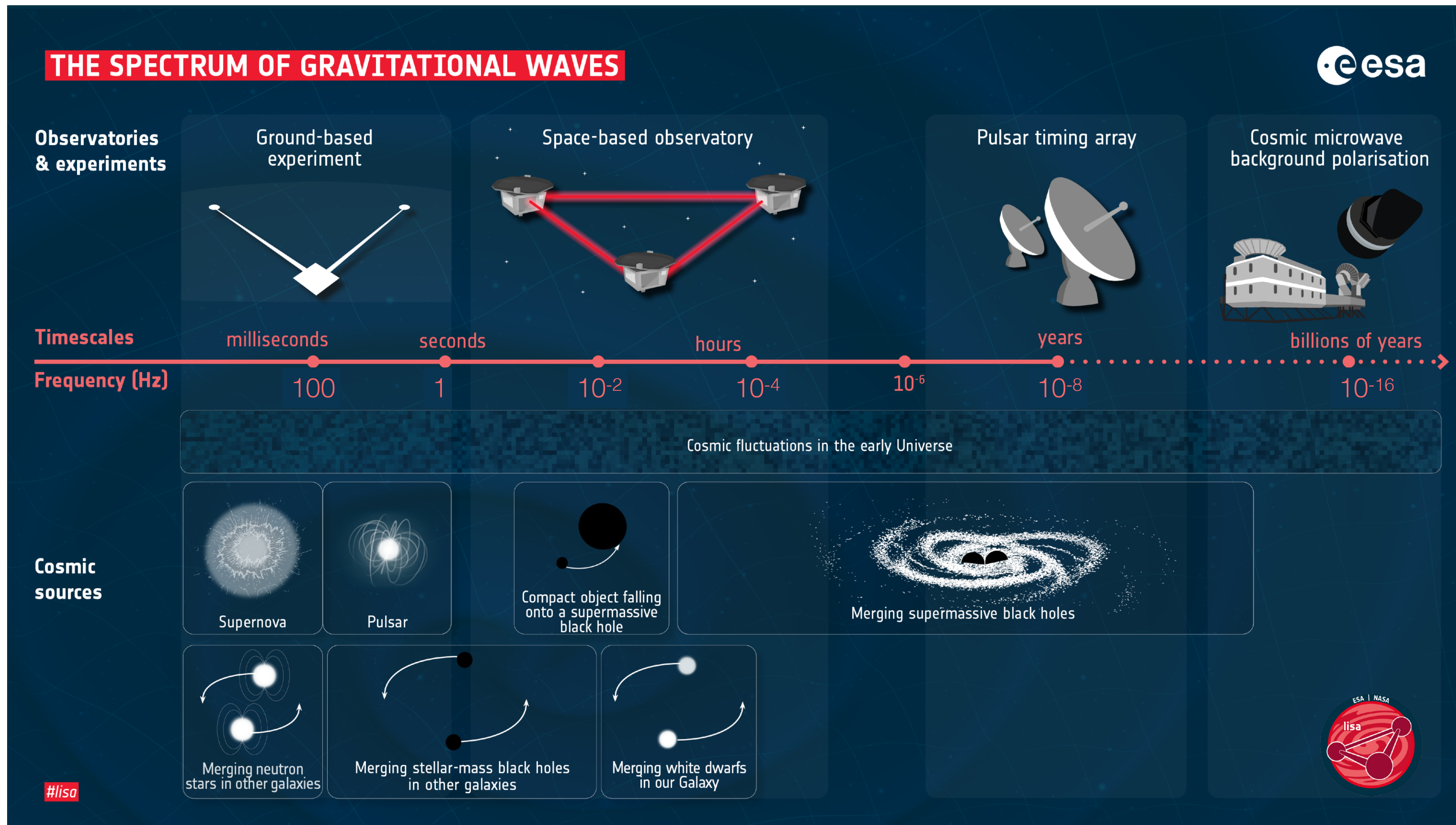
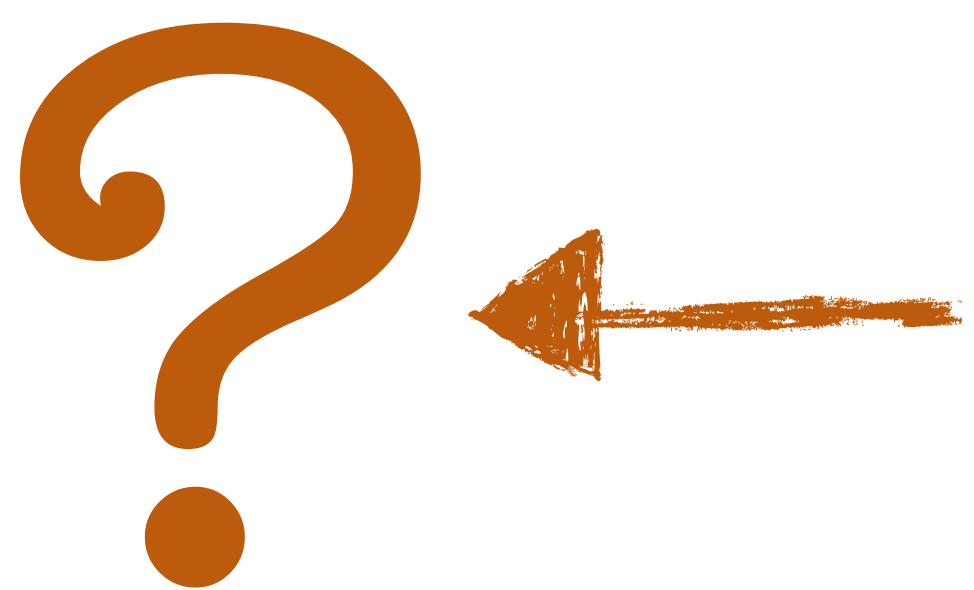
Kristof Schmieden*, Tim Schneemann*, Matthias Schott **

*: University of Mainz, **: University of Bonn

SUPA⁰X
a RADES
experiment



Based on [[arXiv:2308.11497](https://arxiv.org/abs/2308.11497)]



[<https://www.esa.int/>]

Introduction - Gravitational Waves

- Observation of gravitational waves by LIGO/Virgo is certainly a breakthrough in fundamental physics!

• However, there should/could be **other sources** of gravitational waves

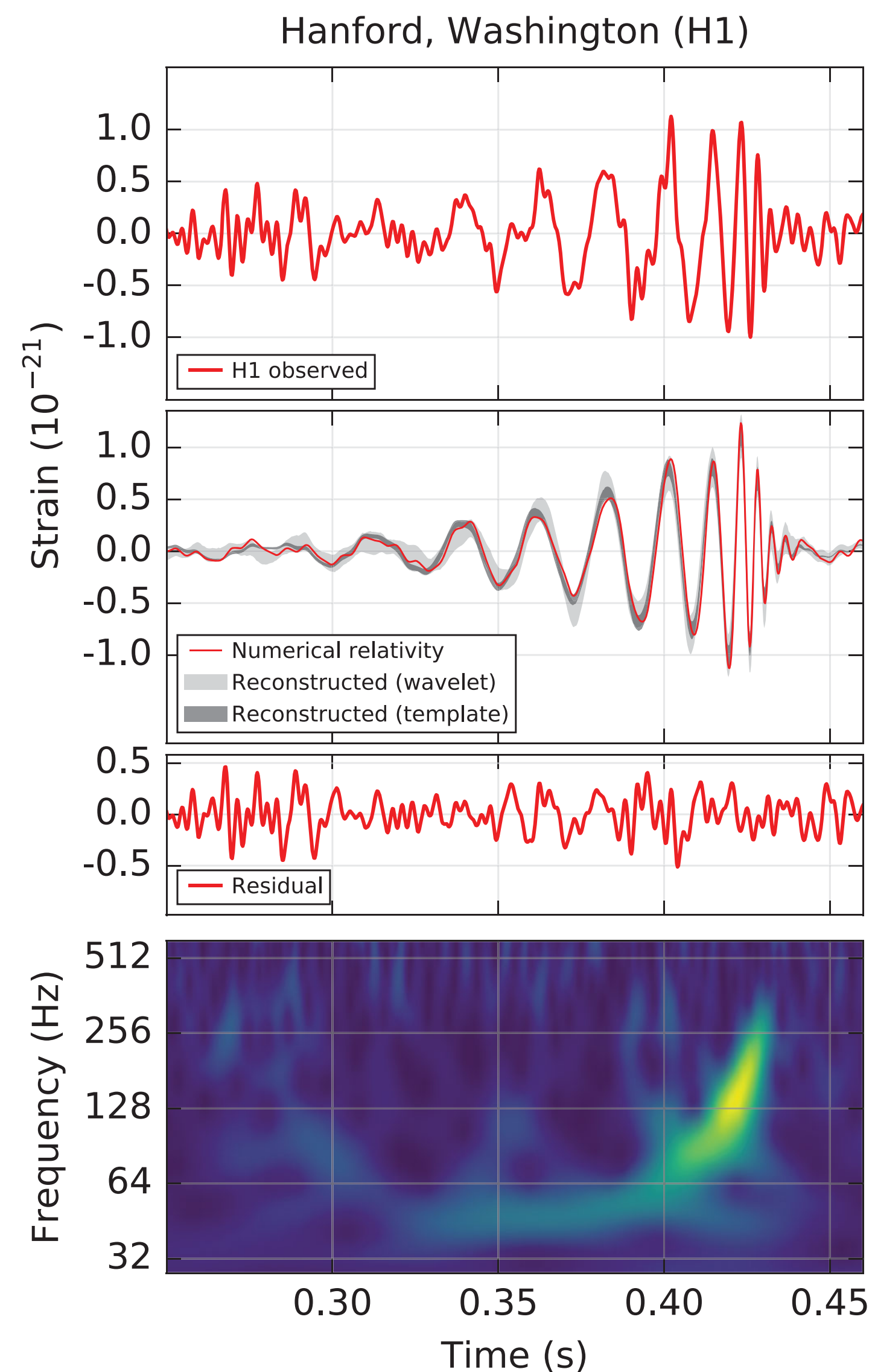
- Primordial black hole merges
- Boson clouds (BH superradiance)
- ...

• Those GW would have **frequencies in the GHz regime**

- **Should search for high frequency GW**

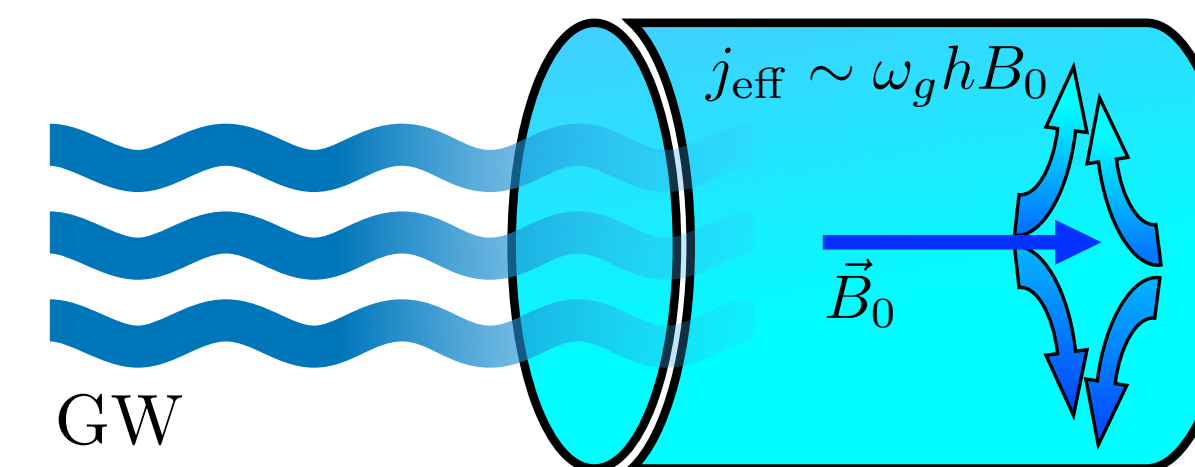
But how?

- Frequency range: 10-1000 Hz



[PRL 116, 061102 (2016)]

[arXiv:2112.11465]



- Two contributing effects
 - Assuming conversion cavity with volume V within static B-Field

- GW deforms cavity
 - Oscillating change of magnetic flux
 - Excitation of EM field

- Direct conversion of gravitons to photons via the inverse Gertsenshtein effect

- Resonant excitation of EM field in Cavity
 - Produced EM power given by:

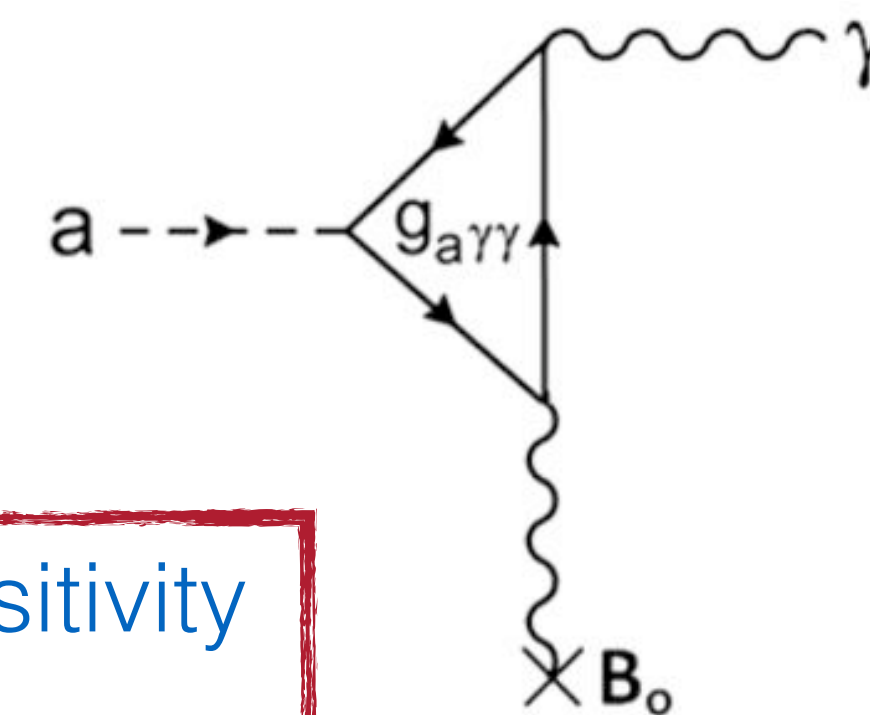
$$P_{sig} = \frac{1}{2} Q \omega_g^3 V^{5/3} (\eta_n h_0 B_0)^2 \frac{1}{\mu_0 c^2}$$

Similarity to Axion Searches

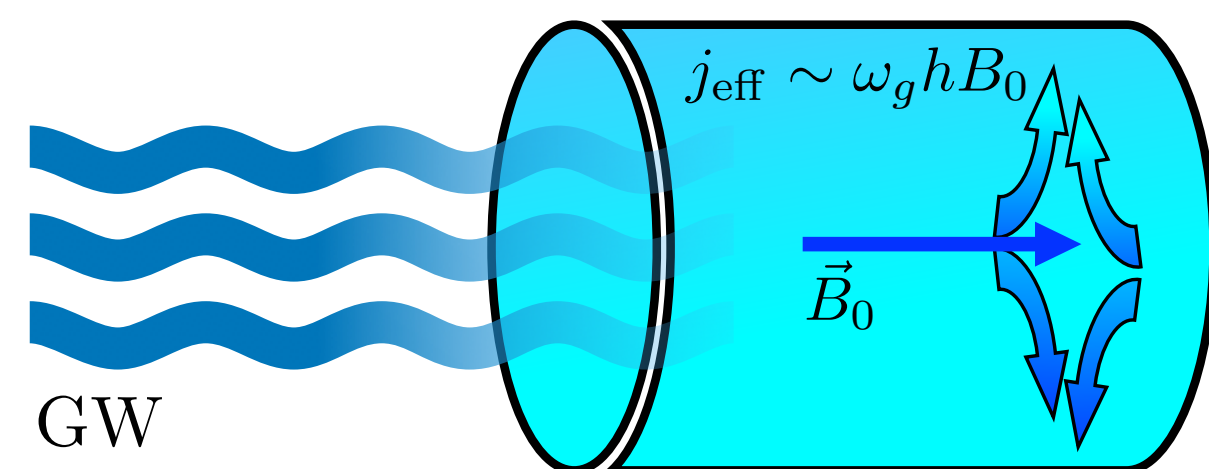
- Axion Haloscopes:

- RF cavity in magnetic field → Primakov conversion of axions to photons
- Resonant excitation of cavity mode

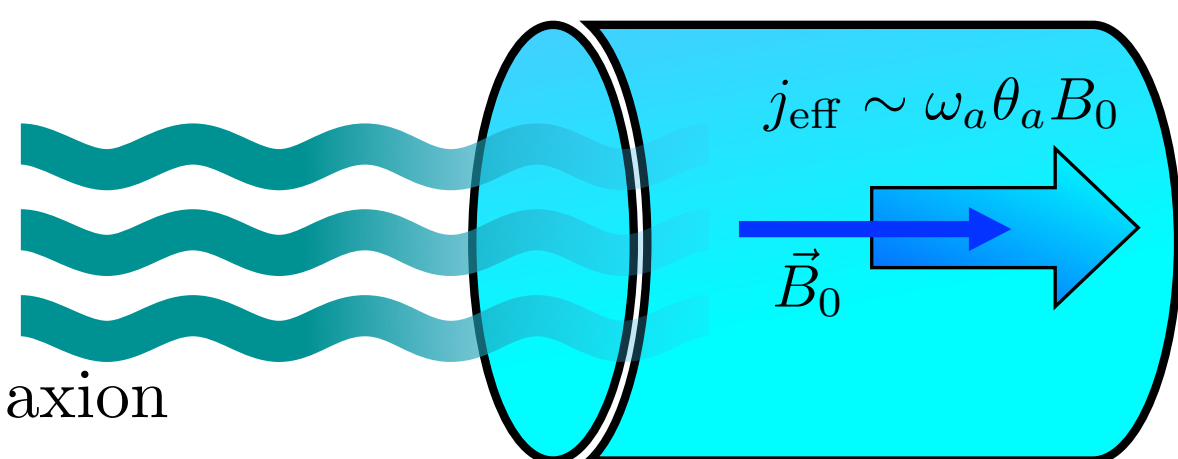
- **Cavity based haloscopes are sensitive to GWs**



Interesting sensitivity range for PBH

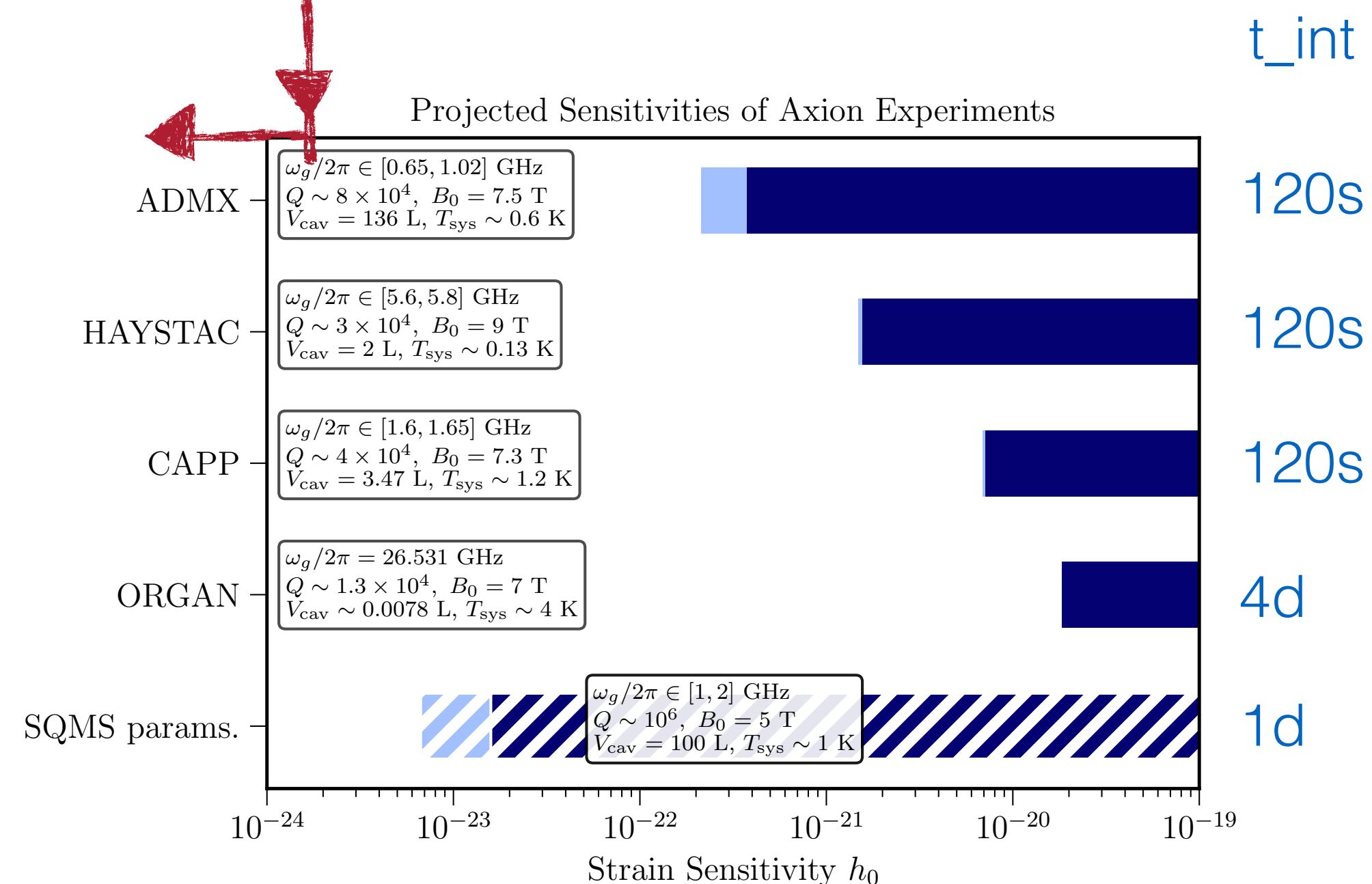


- **GW:**
 - Typical quadruple structure
 - Preferred mode: TM 020
 - Current direction dependent on GW



- **Axions:**
 - Preferred mode: TM 010
 - Current dependent on B-field direction
 - Little overlap with GW mode

[arXiv:2112.11465]

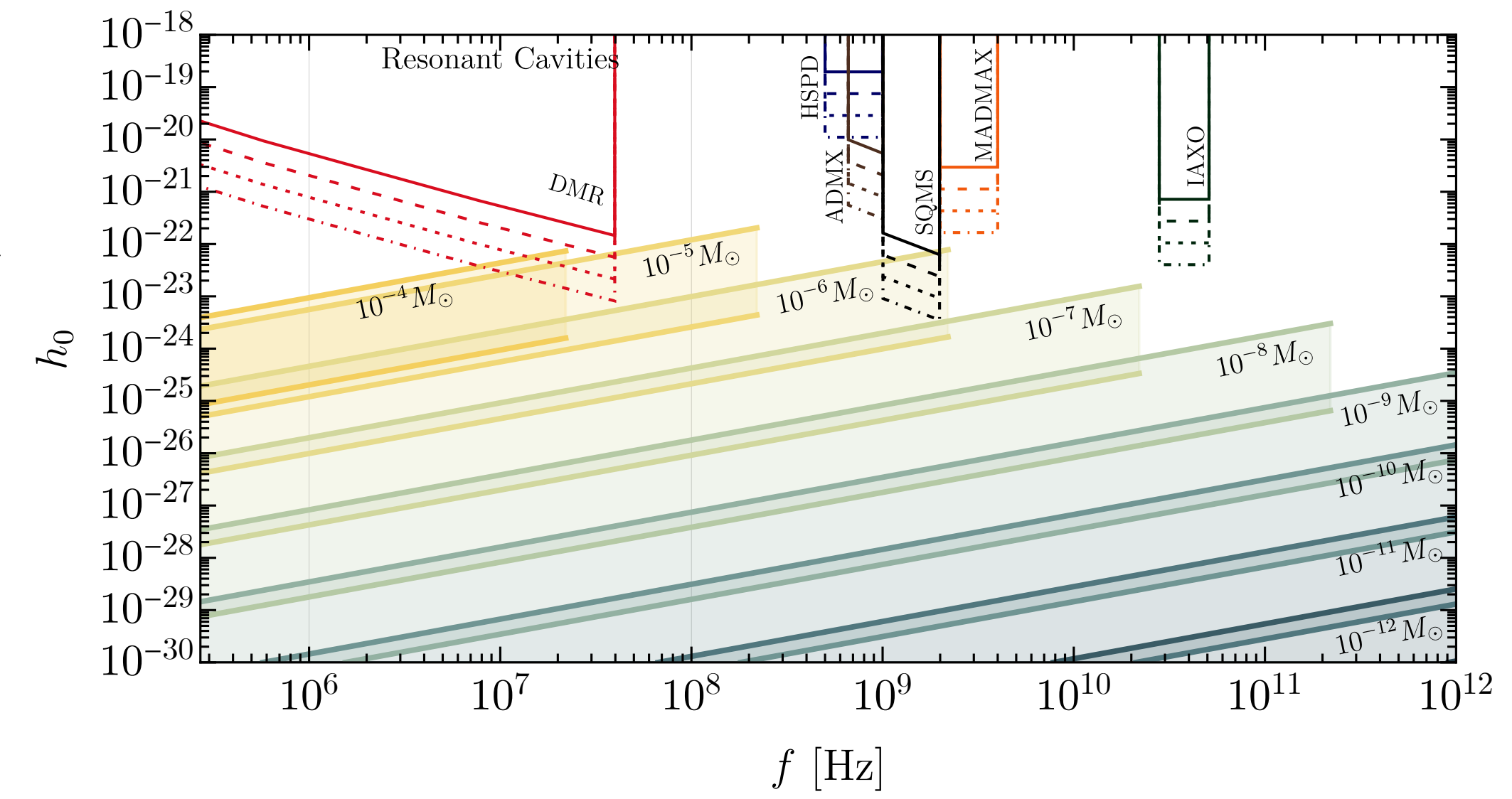


[Detecting high-frequency gravitational waves with microwave cavities
Asher Berlin, Diego Blas, Raffaele Tito D'Agnolo, Sebastian A.R. Ellis
arXiv:2112.11465]

High Frequency Gravitational Waves

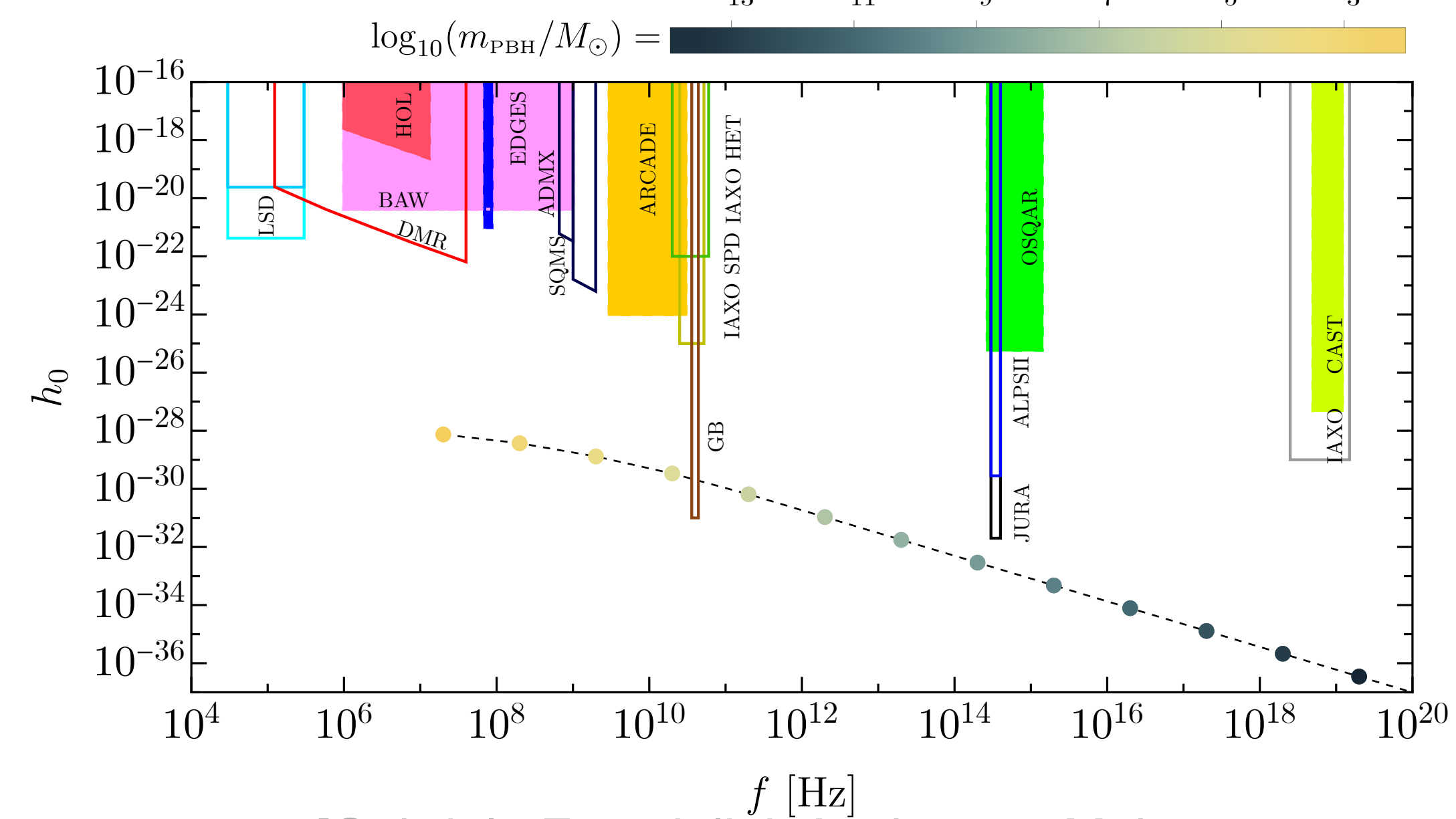
• Several well motivated beyond the standard model sources:

- Primordial black hole mergers
 - Chirp signals
- GW from boson clouds around BHs
 - (BH super radiance)
 - Monochromatic over long timescales
- Stochastic GW background
 - Even lower strains ...



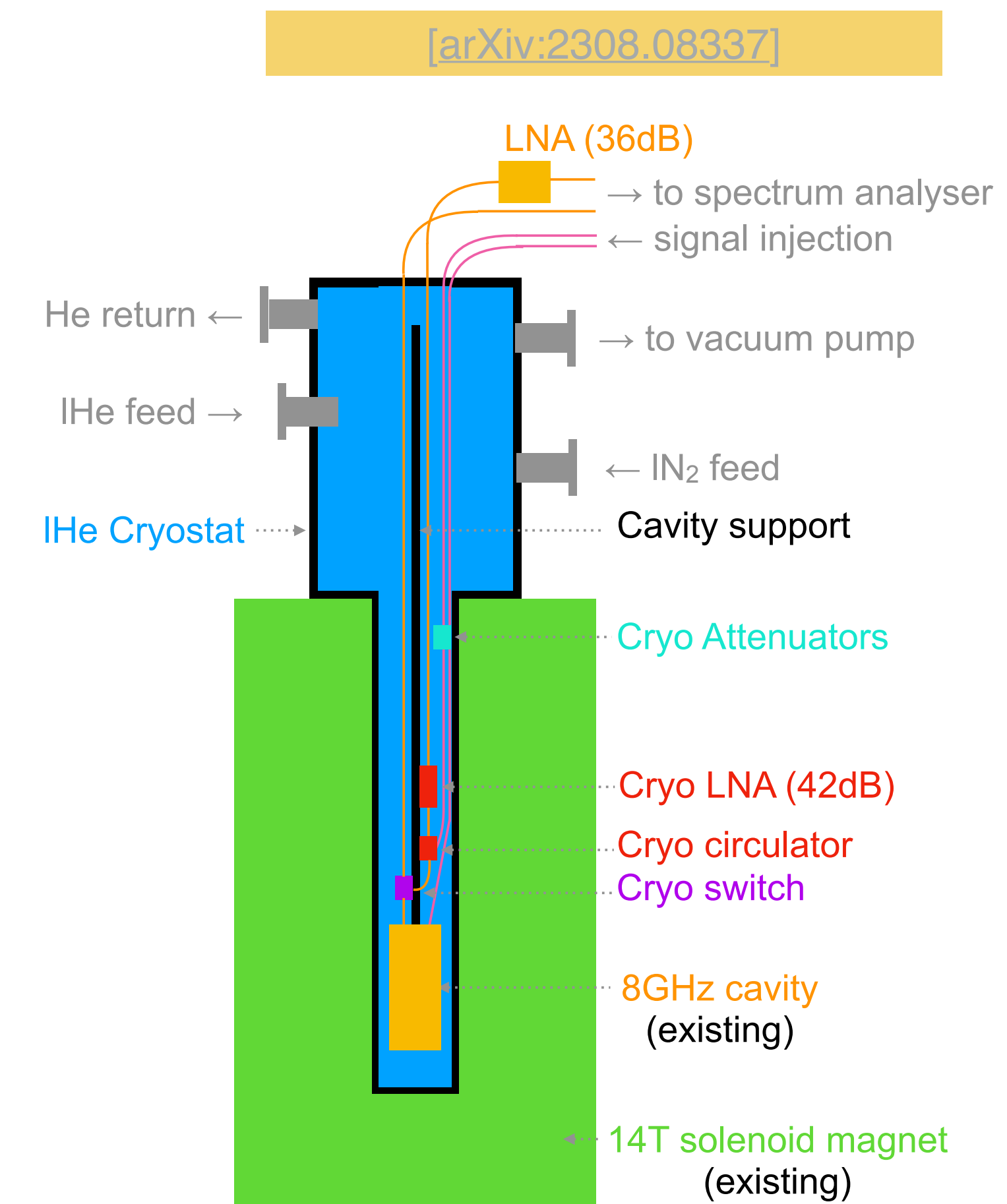
• Displayed expected experimental sensitivities for PBHs:

- Assuming GW signal long enough to ring up cavity
- E.g.: given for ADMX, SQMS @ $m_{PBH} \approx 10^{-10} M_{\odot}$



[Gabriele Franciolini, Anshuman Maharana, Francesco Muia; arXiv:2205.02153v1]

- **Supax:** superconducting axion search @ Mainz
 - First results on dark photons (~commissioning) [[arXiv:2308.08337](https://arxiv.org/abs/2308.08337)]
- **Goals:**
 - Study of new **SC materials** for resonant cavity experiments
 - Study of **cavity geometries** optimised for **GW** searches
 - Together with Mainz theory section (P. Schwaller)



[arXiv:2308.08337]

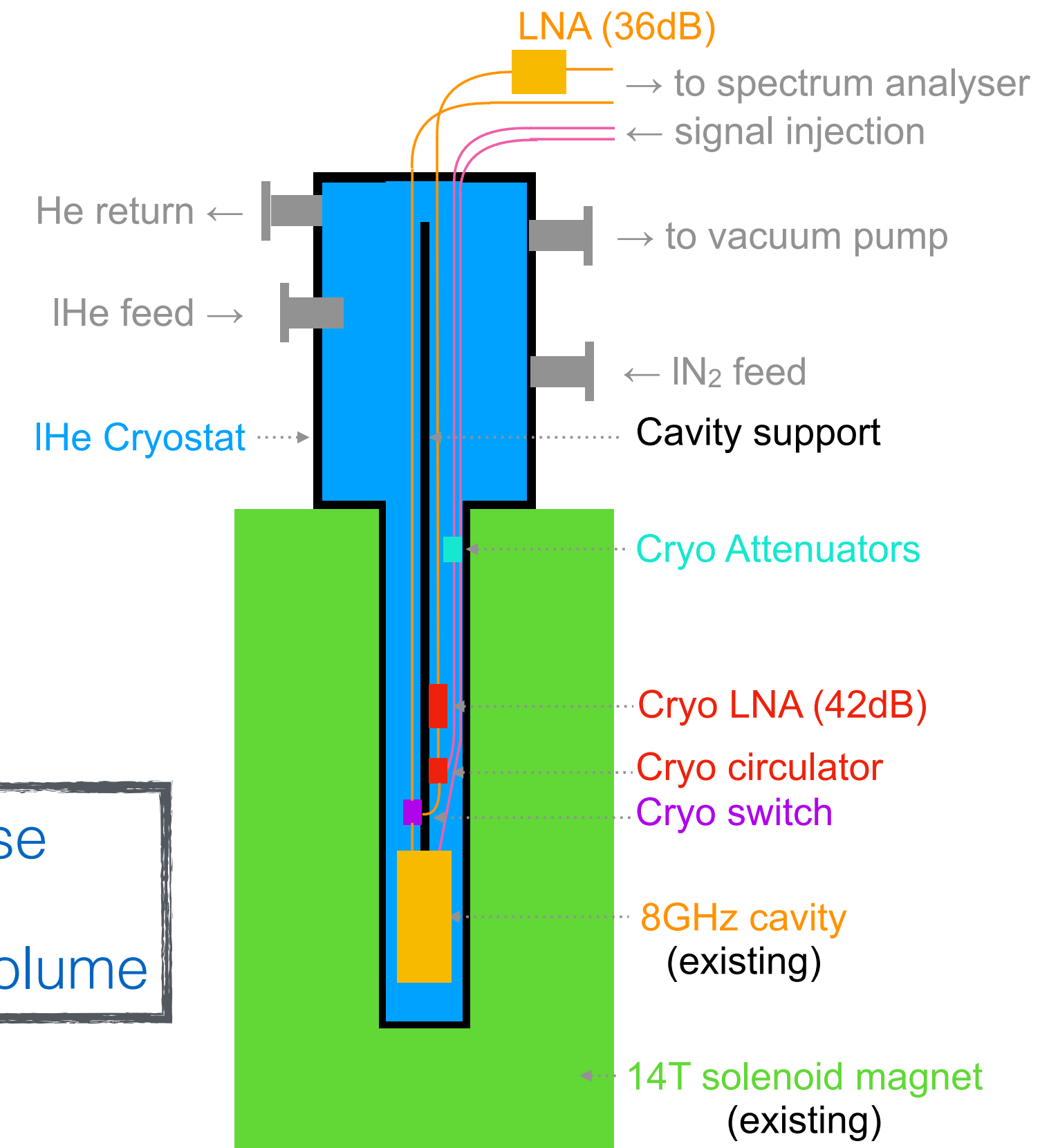
Metamaterials

Geometries

$$P_{sig} = \frac{1}{2} Q \omega_g^3 V^{5/3} (\eta_n h_0 B_0)^2 \frac{1}{\mu_0 c^2}$$

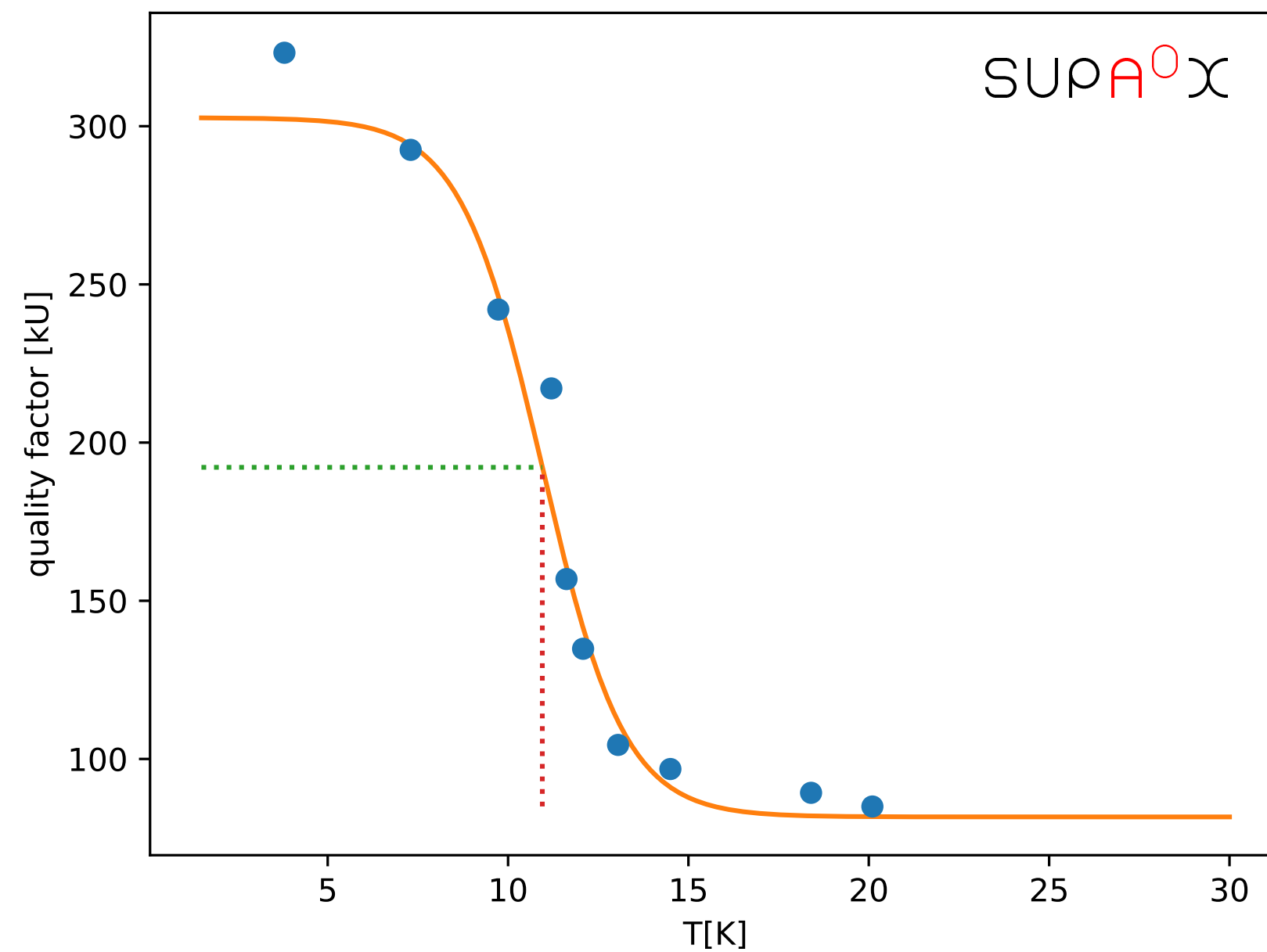
- Depends on cavity material:
 - High purity copper: $\sim 5 \cdot 10^4$
- Superconducting: difficult in high magnetic field!
 - Target: 10^6
 - Achieved: $3 \cdot 10^5$ (non tunable)
 - HTS [arXiv: 2002.08769](https://arxiv.org/abs/2002.08769)
 - Di-electric [arXiv: 2208.12670](https://arxiv.org/abs/2208.12670)
 - Materials under study: Nb₃Sn, HTS materials (YBCO)
 - New: **NbN**

- Up to 14T magnets in use
 - Up to 20T envisioned
- Larger fields - smaller volume



- **Supax:** new superconducting material for RF cavities:
 - **NbN**
 - $Q_0 = 3.1 \cdot 10^5$ @ 8.4 GHz, 4 K
 - Measurements within B-field currently ongoing


Cu cavity, coated with NbN at university of Siegen



How to become more sensitive?

- Current efforts focus on **improving single cavity** sensitivity
- But what about **combining various setups**?
- Phase aligned combination voltages from of N cavities
 - RF amplitude (voltage):

$$V_{comb} = \frac{it\omega}{\sqrt{N}} \sum_i V_i e^{i\phi_i} \propto \sqrt{N} V_0$$



 $V_i = V, \phi_i = \phi$

- Hence the **signal power scales linearly in N!**
 - Assumed single setup
 - 14T B-field, about 10cm diam., 30cm long
 - 3 spherical cavities @ 5GHz, SC, high Q
 - 1s integration time

Disclaimer

This is not a fully fledged proposal in all glory detail
 Rather intended as basis for discussions

Setup	Supax	GravNet
Shape	cyl.	spher.
f_0 [GHz]	8.3	5.0
Volume [l]	0.128	0.21
Q_0	39600	10^6
η	0.08	0.6
T_{sys} [K]	5	0.1
B [T]		14
int. time		1 s
n cavities	1	3
noise power [W]	$1.5 \cdot 10^{-21} W$	$6.2 \cdot 10^{-23} W$
$h_0(P_{sig} = P_{noise})$	$7.1 \cdot 10^{-21}$	$5.2 \cdot 10^{-23}$

- How sensitive can we get with **10 setups**, scattered around the globe

- Assumptions:

- Sampling of Waveform -> offline combination of phase aligned IQ data
- Setups as shown before
 - Effective signal power increased by factor 10
 - Strain sensitivity increased by factor $\sqrt{10} \approx 3$

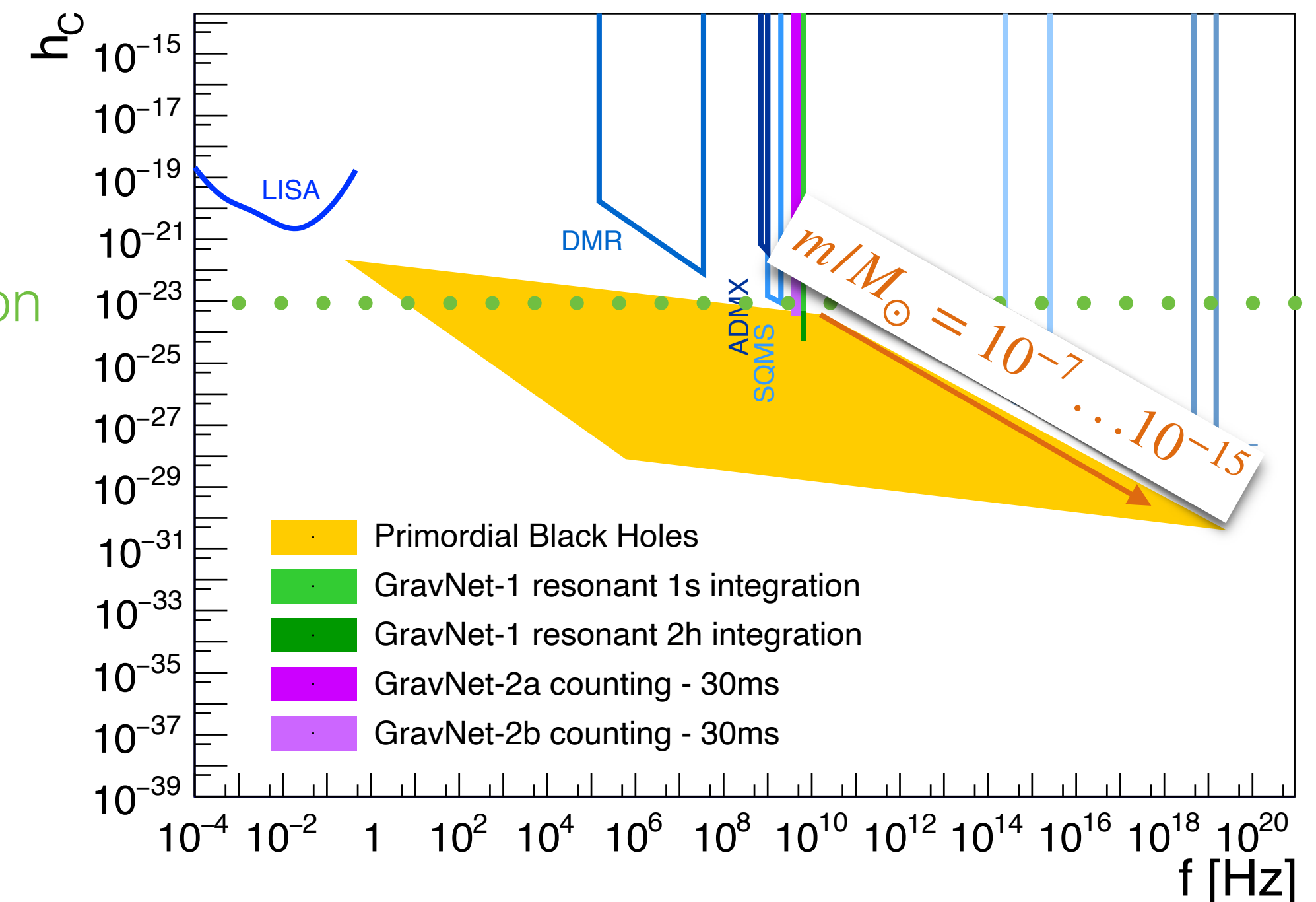
$$h_0 < 10^{-23}, \text{ 1 second integration time}$$

- Phase alignment for distributed setups:

- If signal seen in 3 cavities:
 - Direction of GW can be reconstructed
- Otherwise:
 - Scan through all possible directions and repeat combinations

- No frequency tuning needed:
 - PBH signals are fast transients
 - Single frequency sufficiency

1s integration



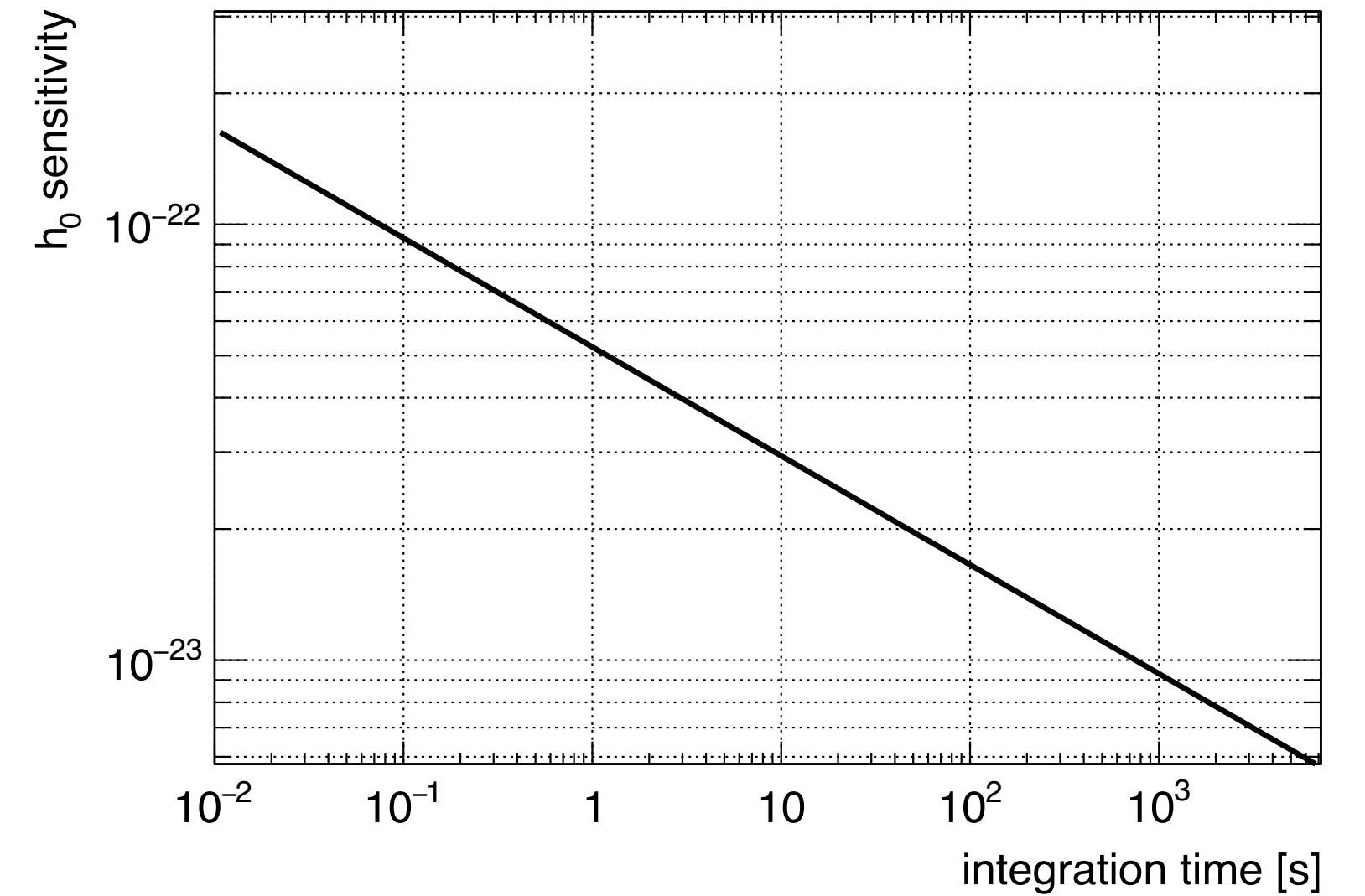
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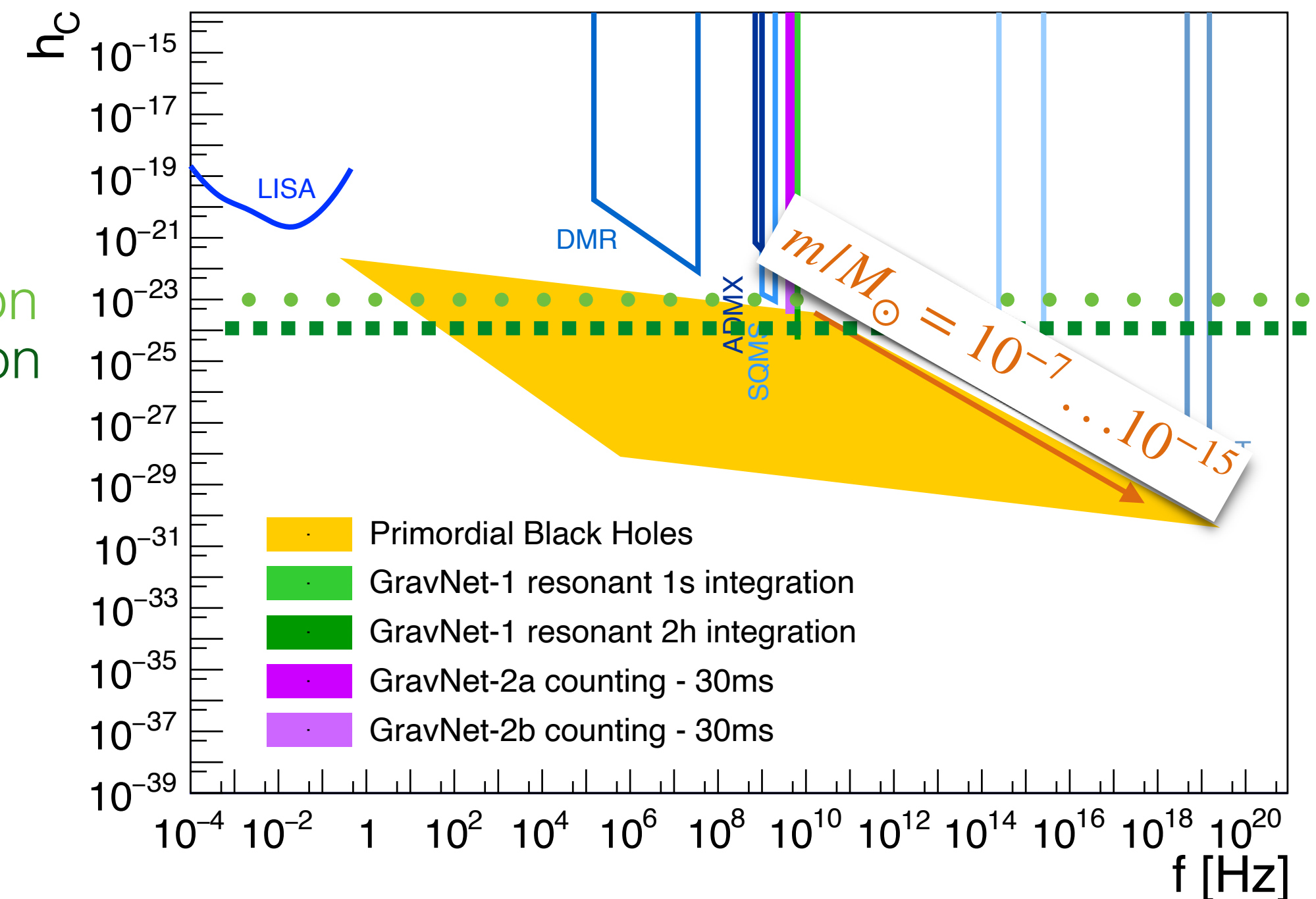
- Longer integration times

- Sensitivity gain with integration time $t^{1/4}$

$$h_0 < 10^{-24}, \text{ 2h integration time}$$



1s integration
2h integration



- GW strain: largest if merging is imminent (closest to innermost stable circular orbit)

- Frequency drift large

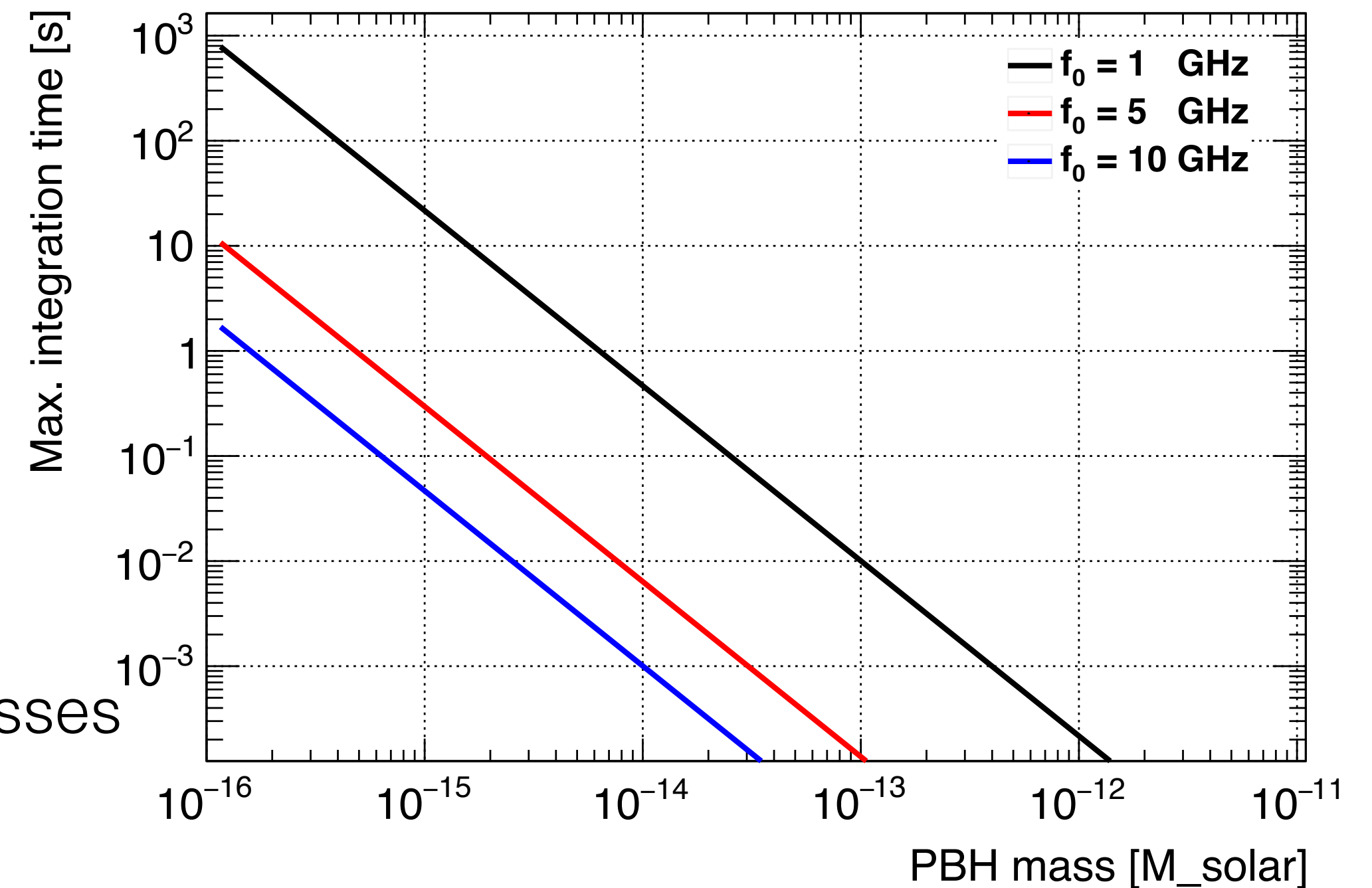
$$\dot{f} = \frac{96}{5} \pi^{8/3} m_c^{5/3} f^{11/3} \simeq 4.62 \times 10^{11} \text{ Hz}^2 \left(\frac{m_{\text{PBH}}}{10^{-9} M_\odot} \right)^{5/3} \left(\frac{f}{\text{GHz}} \right)^{11/3}$$

- To resonantly excite a cavity:

- GW frequency must stay within resonator bandwidth

- $\omega/Q \approx 10^{10} \text{ Hz} / 10^6 = 10 \text{ kHz}$

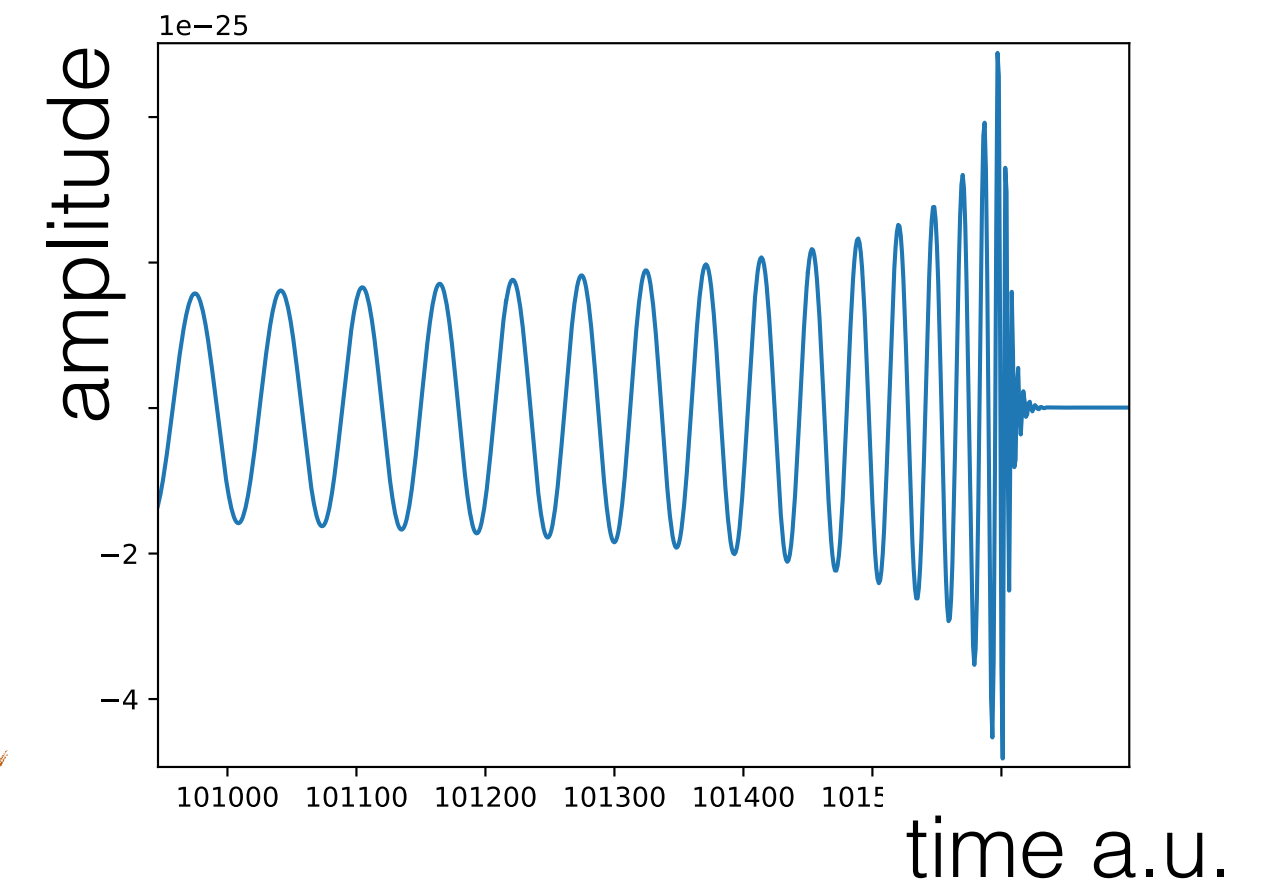
- Very short integration times O(ms) or below for larger PBH masses



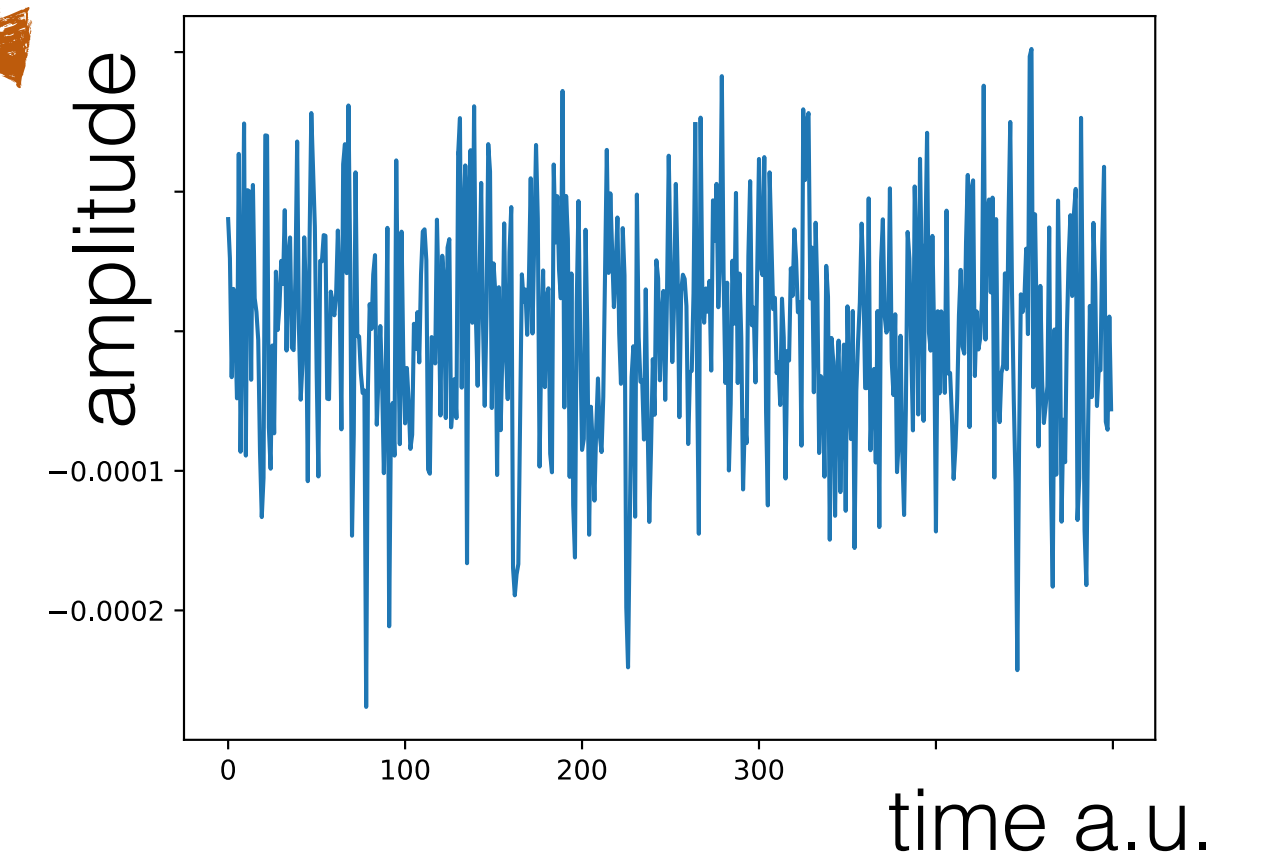
- No improvement with longer integration times!

- Alternative?

- Similar approach as for low frequency BH mergers:
 - Analysis in **time domain**
 - Data rates: $\sim 100\text{MB/s}$ per channel for 10MHz bandwidth
- Simultaneous fit of expected signal shape in all data streams
 - Exploiting all available information
 - + Increased sensitivity compared to time domain analysis
 - - Significant increase in storage & CPU requirement
 - **Sensitive to short transient** signals



Fit template



- Recent progress in R&D for single RF photon counters

- Several technologies under study

- Current Biased Josephson Junctions
- Kerr Josephon Parametric amplifiers
- Transmon Q-Bit readout

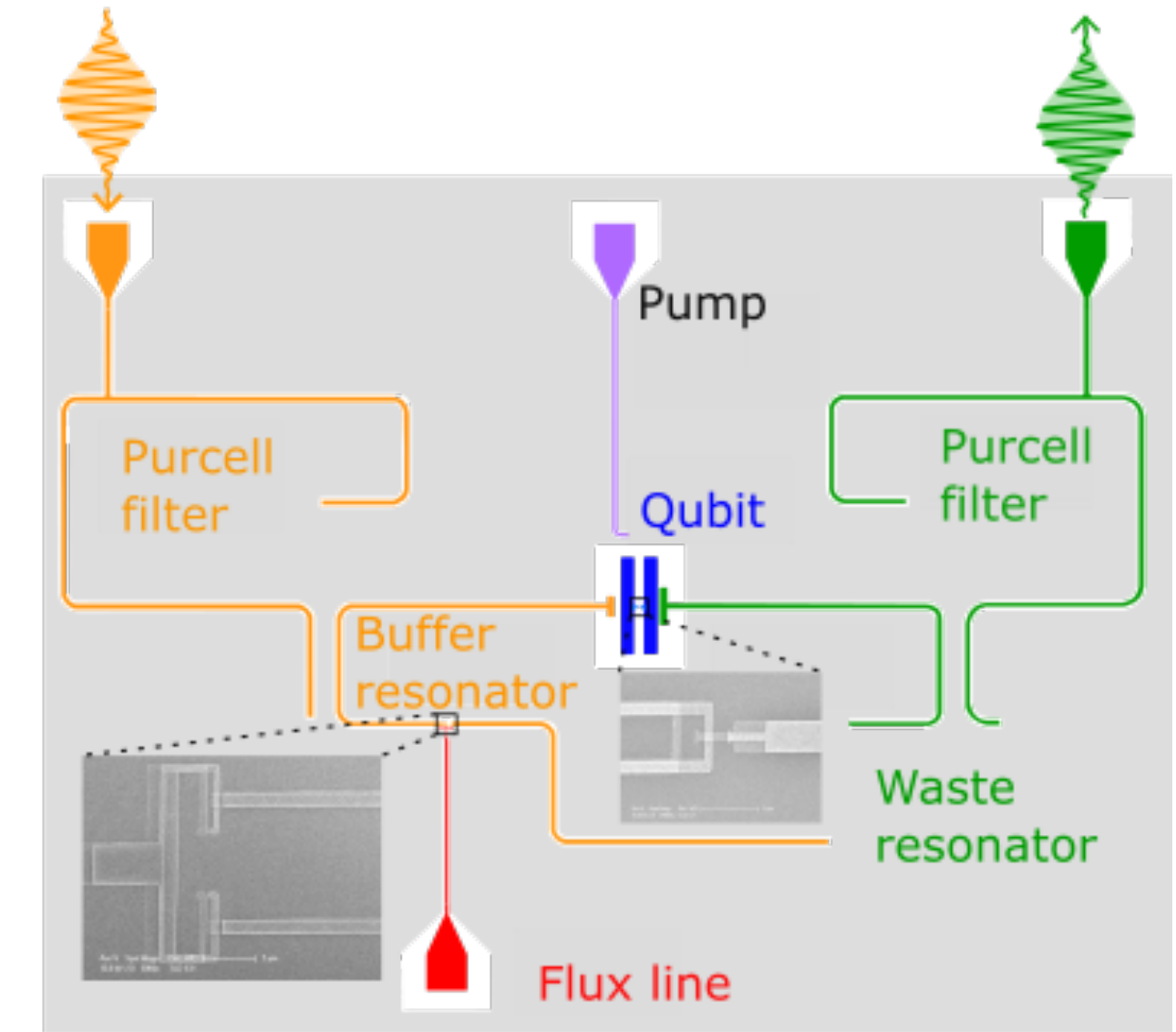
[arXiv:2302.07556]

[arXiv:2308.07084]

[arXiv:2307.03614]



- Shown **single photon efficiency: 43% @ 90 Hz dark count rate**
 - Big R&D effort ongoing [ERC syn.: “Dark Quantum”]



[arXiv:2307.03614]

- Measurement boils down to a **coincidence measurement** !

- Coincidence window and needed number of coincident detectors optimised depending on

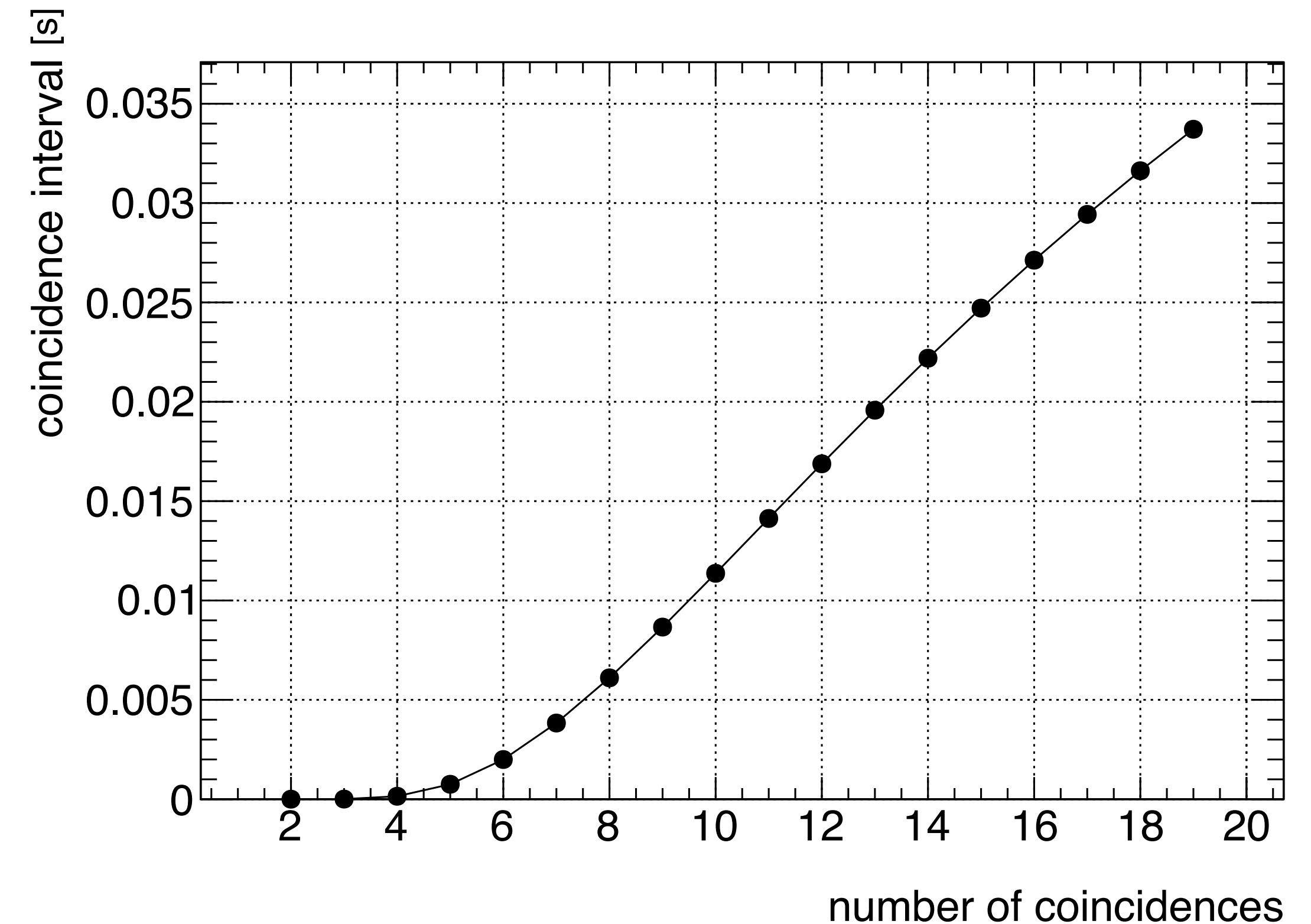
- Background rate (thermal, detector noise)
- Signal Rate

- Background rate:

- Average thermal power in cavity @ 0.1K $\sim 4 \times 10^{-23}$ W, corresponding to 10 photons / s @ 5 GHz
- Could be lowered going to lower temperatures
- Assuming advances in the near future on the single photon sensors:
 - Detector dark count rate will drop significantly -> negligible

- Parameter used for Calculation:

- Allowed accidental coincidence rate: $\leq 1/\text{year}$
- Background rate: 10 Hz
- N detectors: 20



Photon Counting - Signal efficiency

- Overall signal efficiency dependent on detector efficiency, coincidence window and signal photon flux:

- $\epsilon_{single} = \epsilon_{det} \Delta t_{coincidence} \Phi_{sig}$ Φ_{sig} = signal photon flux

- $\epsilon_{tot} = \sum_{i>k} \binom{N}{k} p^k (1-p)^{N-k}$, $p = \epsilon_{single}$, k = number of required coincidences, N = number of detectors

- Parameter used for Calculation:

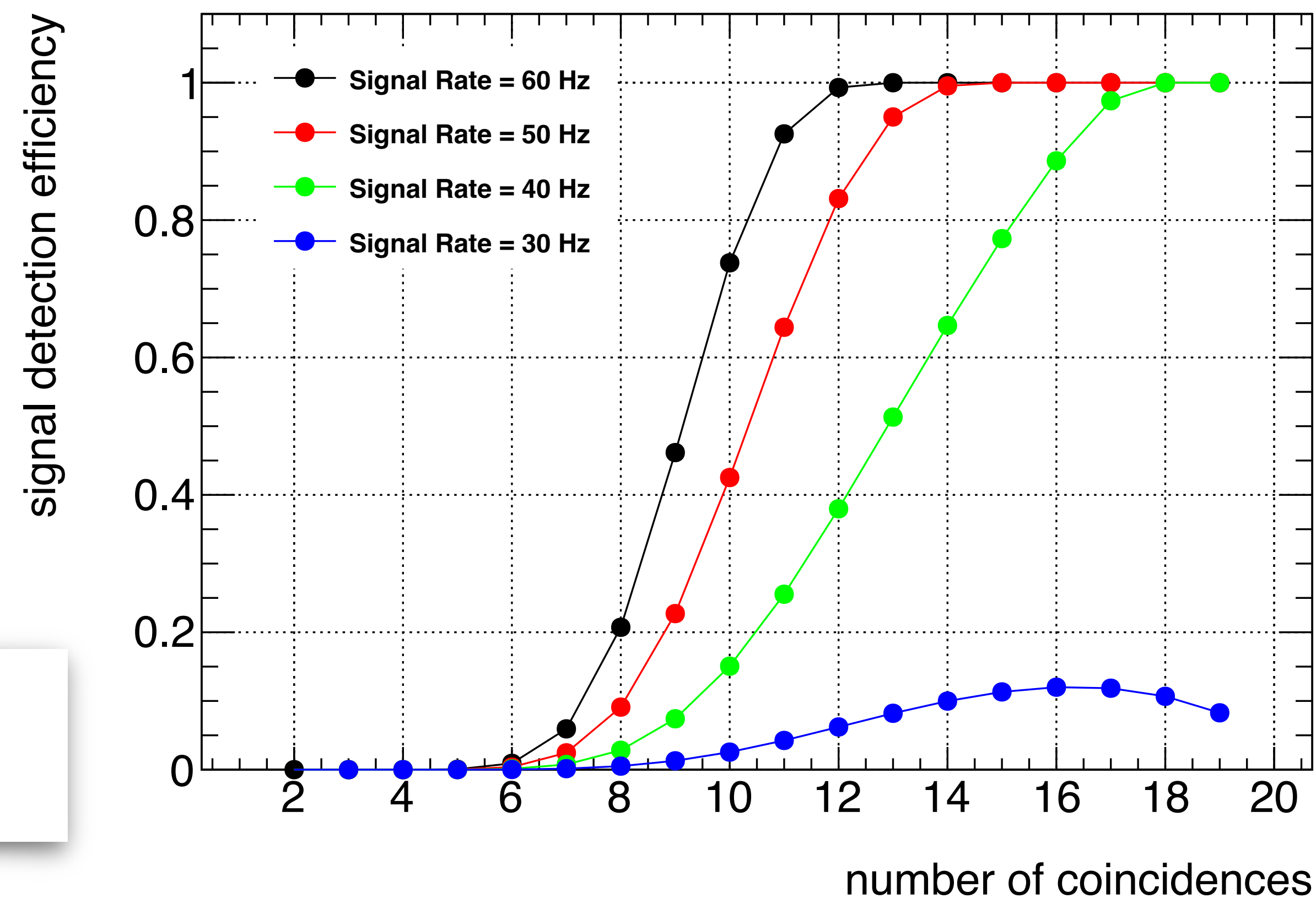
- Allowed accidental coincidence rate: $\leq 1/\text{year}$

- Background rate: 10 Hz

- N detectors: 20

- ϵ_{det} : 0.5

• With **20 detectors** a photon flux of **40 Hz** can be detected with an efficiency of 1 within a coincidence interval of **32ms**



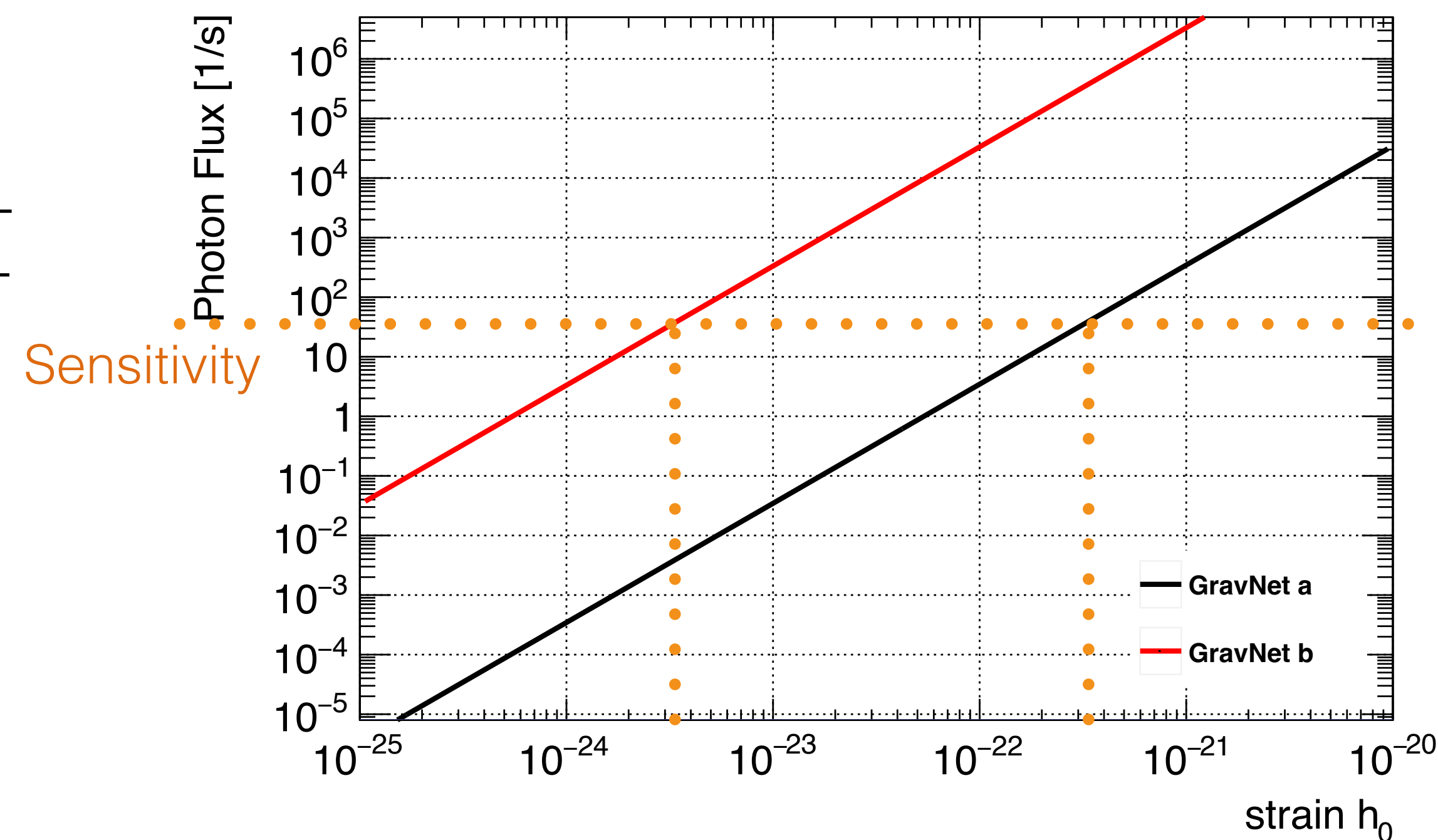
Photon Counting - Sensitivity on GW

• With 20 detectors a photon flux of 40 Hz can be detected with an efficiency of 1 within a coincidence interval of 32ms

• Signal photon flux depends on conversion region:

- a) Magnet dimensions as before (9cm diameter), $B = 14\text{T}$
- b) Assuming large NMR magnet (80cm diameter), $B = 9\text{T}$

Setup	GravNet-a	GravNet-b
radius	40 mm	40 cm
length	12cm	50 cm
Volume [m^3]	6×10^{-4}	0.25
Q_0	10^6	10^5
T_{sys} [K]	0.1	0.1
B [T]	14	9



Global network of HFGW detectors will be able to reach into the interesting region for PBH with existing technologies!

• Achievable sensitivity:

• $h_0 < 3 \times 10^{-22} \dots 3 \times 10^{-24}$

• With coincidence time of 32ms!

Significant room for improvements:
more detectors, larger volumes, higher detector efficiency

- To increase the sensitivity of halo scope style experiments we suggest to build a **global network of detectors**
 - Remember: SNR scales linear with number of detectors!
- **Integrating measurement:**
 - Sample RF data, combine phase aligned, integrate
- Typical integration times too long to be sensitive to BH merges!

- Single frequency sufficient to hunt for PBH mergers!
- Could even combine measurements at different frequencies

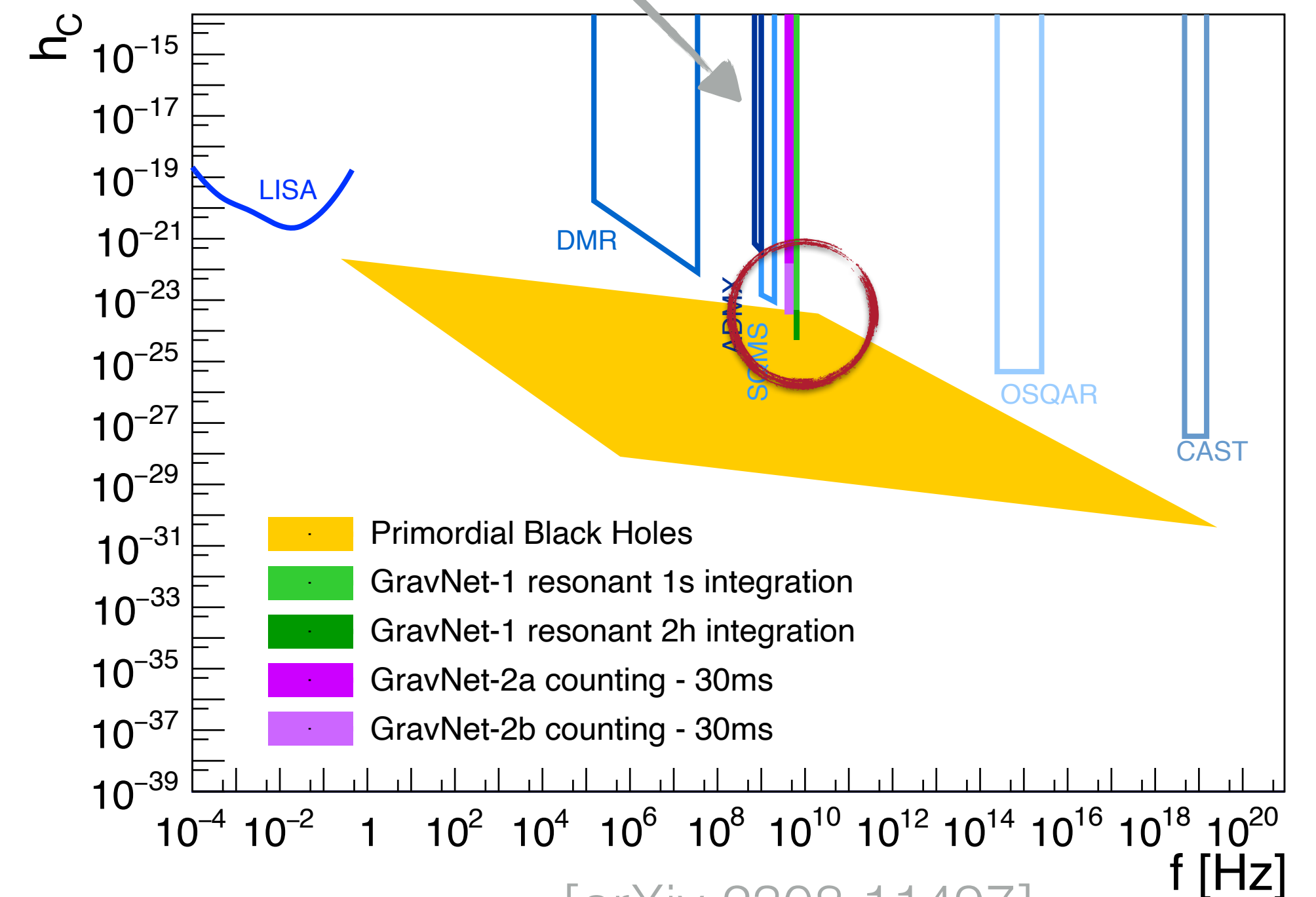
- **Photon counting style experiments:**
 - Recent advancements in single RF photon detection allows to use coincidences of several detectors
- Using 20 independent detectors:

• Sensitivity: $h_0 < 3 \times 10^{-22}$ 3×10^{-24}



Requires large meta material cavities
(high frequency @ large volume)

$t_{\text{int}} > O(100\text{s})$ [[arXiv:2112.11465](https://arxiv.org/abs/2112.11465)]



[[arXiv:2308.11497](https://arxiv.org/abs/2308.11497)]

GravNet is an idea up for discussion

- Many advantages in **combining efforts searching for UHFGWs** in coordinated way
- GravNet would significantly improve the sensitivity on high frequency gravitational waves
- Based on commercial magnet systems, which is comparatively cheap
- Worldwide collaboration would share costs automatically with local lab-based experiments
- Easy exchange of R&D results and integration at all locations
- Sensitivity to the PBH parameter space with existing technologies!

