

**Study of the $e^+e^- \rightarrow \pi^+\pi^-\psi(2S)$ reaction
at $\sqrt{s} > 4.6$ GeV and
search for the charged $Z_c(4430)$ exotic state**

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Preamble

What and Why

The $e^+e^- \rightarrow \pi^+\pi^-\psi(2S)$ reaction offers the possibility to probe the **XYZ sector**,

via the investigation of 2 exotic states

The **Y(4660)** via the $e^+e^- \rightarrow [\pi^+\pi^-/f_0(980)]\psi(2S)$

$\psi(4660)$, **observed by BaBar**^[1], **BELLE**^[2], and **BESIII**^[3] hypothesised to be a **baryonium**^[4], a **molecule**^[5], or a **tetraquark**^[6]

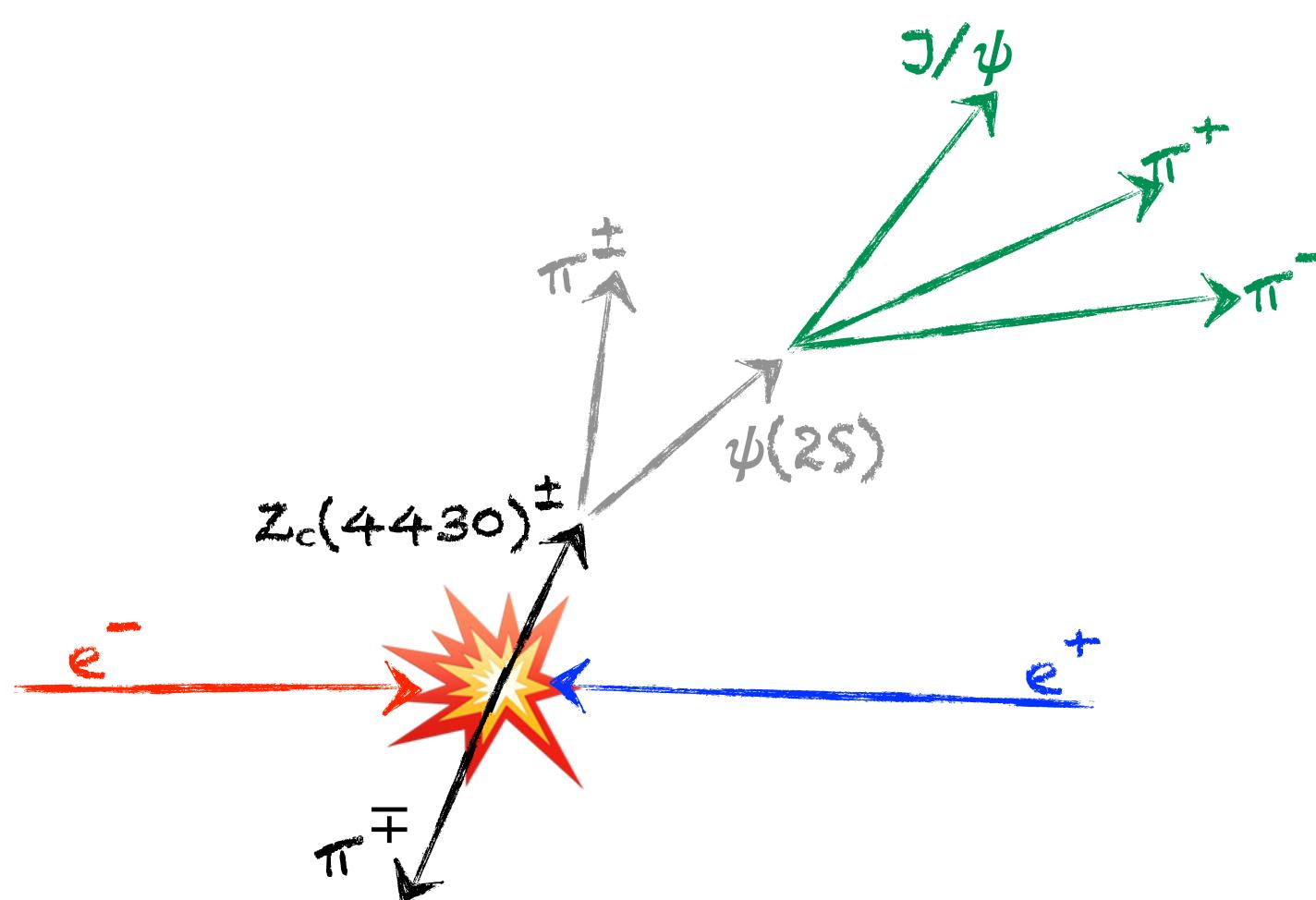
Study of the exotic $Z_c(4430)$ state through the $e^+e^- \rightarrow \pi^\pm Z_c(4430) \rightarrow \pi^\pm\pi^-\psi(2S)$

$Z_c^+(4430)$ was **observed** and studied in the B -decays in the $\pi\psi(2S)$ invariant mass **by BELLE**^[7] (and **by LHCb**^[8])

Motivation

In Refs. [9, 10], the $Z_c(3900)^\pm$ state is seen both in $\pi\psi(2S)$ and $\pi J/\psi$, and in relation with the $Y(4260)$ resonance

Ref. [10] finds $R = \sigma(\pi^\pm Z_c(3900)^\mp \rightarrow \pi^\pm\pi^-\psi(2S))/\sigma(\pi^\pm\pi^-\psi(2S)) \sim 22\%$, neglecting the the J/ψ to $\psi(2S)$ PHSP change, ~100 events are expected around $Y(4660)$



[1] Phys. Rev. D **89**, 111103

[2] Phys. Rev. D **91**, 112007

[3] Phys. Rev. D **104**, 052012

[4] J. Phys. G **35**, 075008 (2008)

[5] Phys. Lett. B **665**, 26-29

[6] Phys. Rev. D **89**, 114010

[7] Phys. Rev. D **88**, 074026

[8] Phys. Rev. Lett. **112**, 222002

[9] Phys. Rev. D **96**, 032004

[10] Phys. Rev. Lett. **110**, 252001

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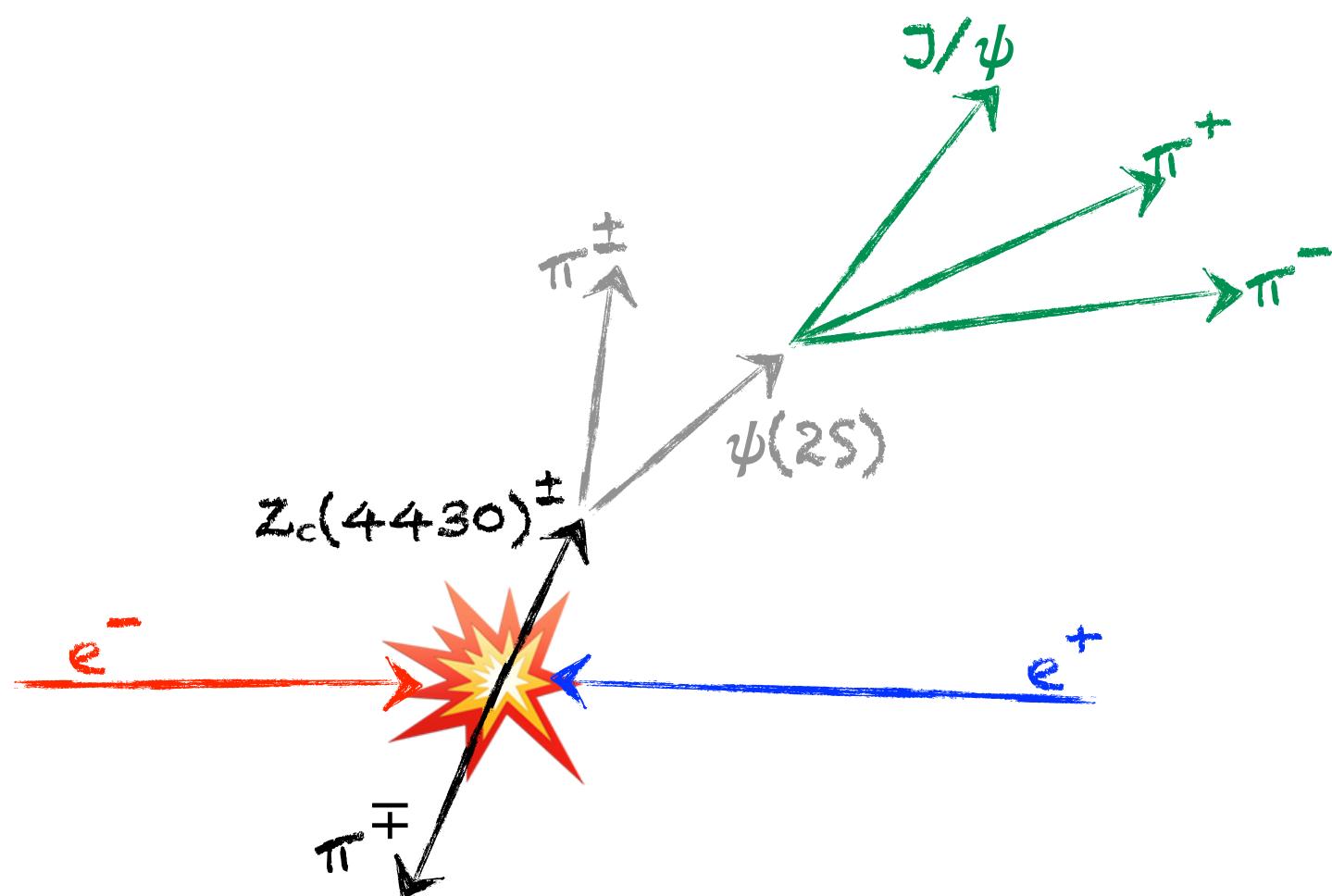
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How

The study will make use of the 12 datasets @ $\sqrt{s} > 4.6$ GeV

No $Z_c(4430)$ signal was observed in the **mono-energetic datasets**^[11], so the main idea is to merge all the data @ $\sqrt{s} > 4.6$ GeV to use the whole statistics



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Preamble

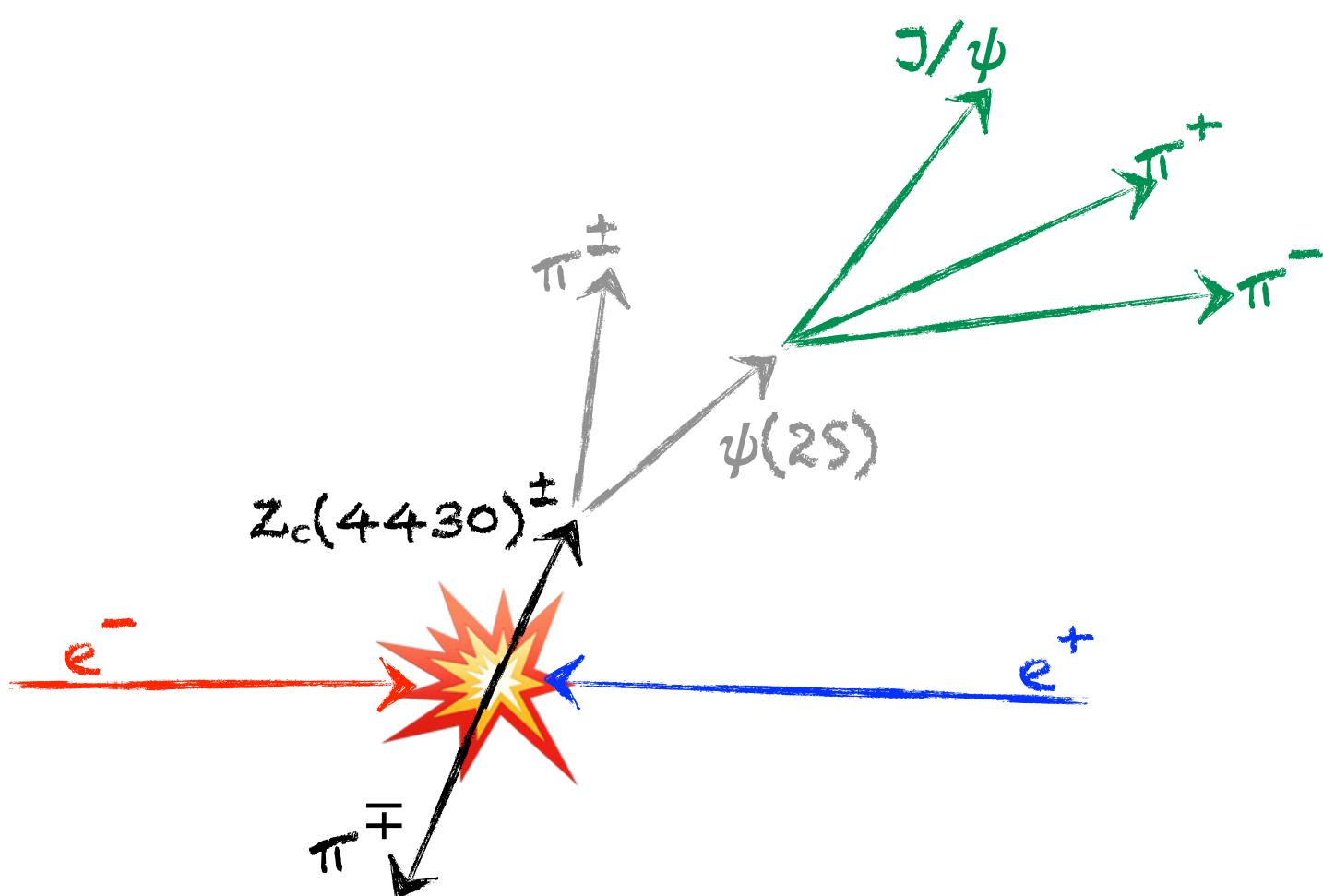
Datasets

Dataset	E_{CoM} (MeV)	\mathcal{L} (pb $^{-1}$)	Boss Version
4610	$4611.86 \pm 0.12 \pm 0.30$	$103.65 \pm 0.05 \pm 0.55$	7.0.6
4620	$4628.00 \pm 0.06 \pm 0.32$	$521.53 \pm 0.11 \pm 2.76$	
4640	$4640.91 \pm 0.06 \pm 0.38$	$551.65 \pm 0.12 \pm 2.92$	
4660	$4661.24 \pm 0.06 \pm 0.29$	$529.43 \pm 0.12 \pm 2.81$	
4680	$4681.92 \pm 0.08 \pm 0.29$	$1667.39 \pm 0.21 \pm 8.84$	
4700	$4698.82 \pm 0.10 \pm 0.36$	$535.54 \pm 0.12 \pm 2.84$	
4740	$4739.70 \pm 0.20 \pm 0.30$	$163.87 \pm 0.07 \pm 0.87$	7.0.7
4750	$4750.05 \pm 0.12 \pm 0.29$	$366.55 \pm 0.10 \pm 1.94$	
4780	$4780.54 \pm 0.12 \pm 0.30$	$511.47 \pm 0.12 \pm 2.71$	
4840	$4843.07 \pm 0.20 \pm 0.31$	$525.16 \pm 0.12 \pm 2.78$	
4914	$4918.02 \pm 0.34 \pm 0.34$	$207.82 \pm 0.08 \pm 1.10$	
4946	$4950.93 \pm 0.36 \pm 0.38$	$159.28 \pm 0.07 \pm 0.84$	

How

The study will make use of the 12 datasets
 $\text{@}\sqrt{s} > 4.6 \text{ GeV}$

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mono-energetic datasets^[11], so the main idea is
 to merge all the data $\text{@}\sqrt{s} > 4.6 \text{ GeV}$
 to use the whole statistics



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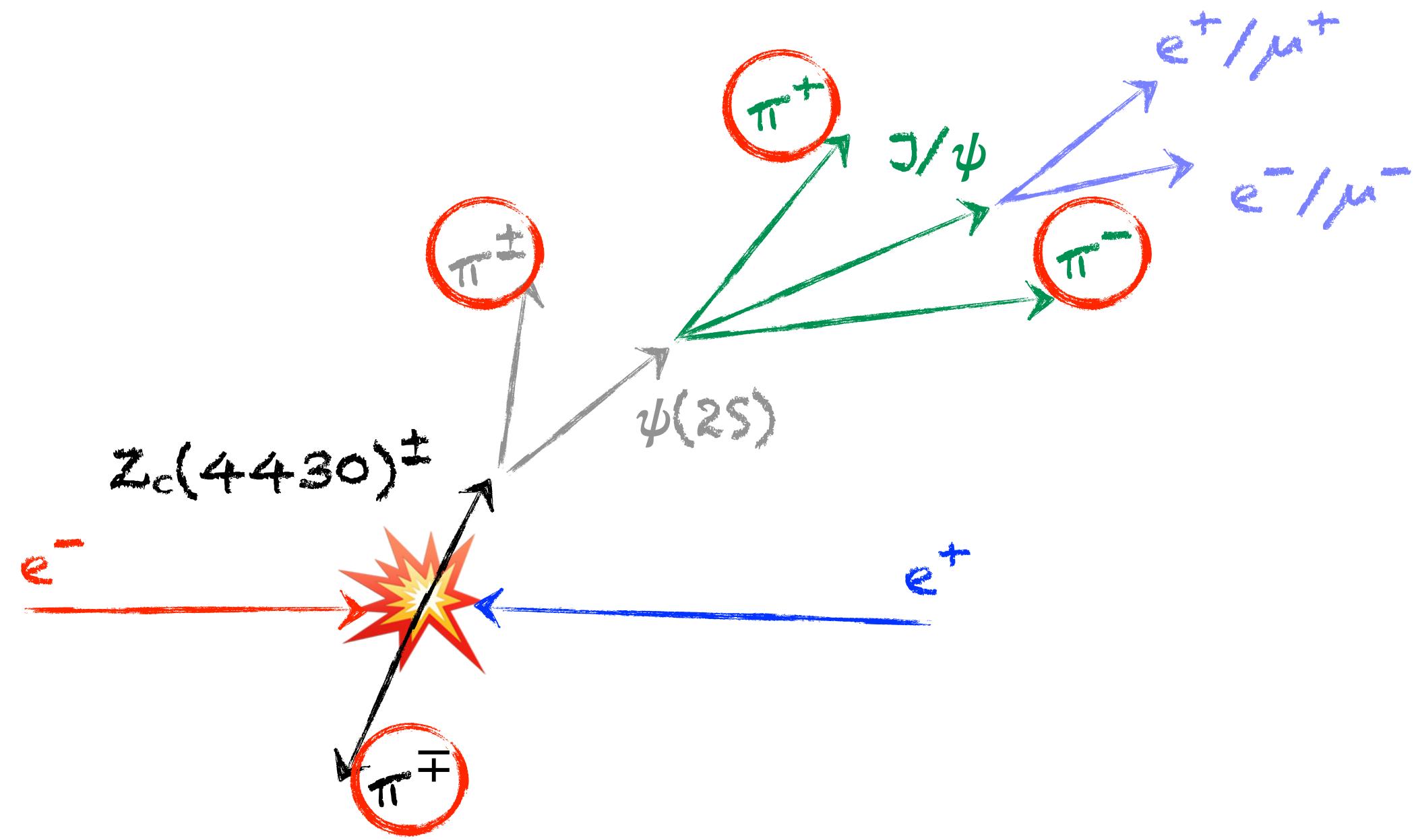
^[9] Phys. Rev. D **96**, 032004

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Event Selection

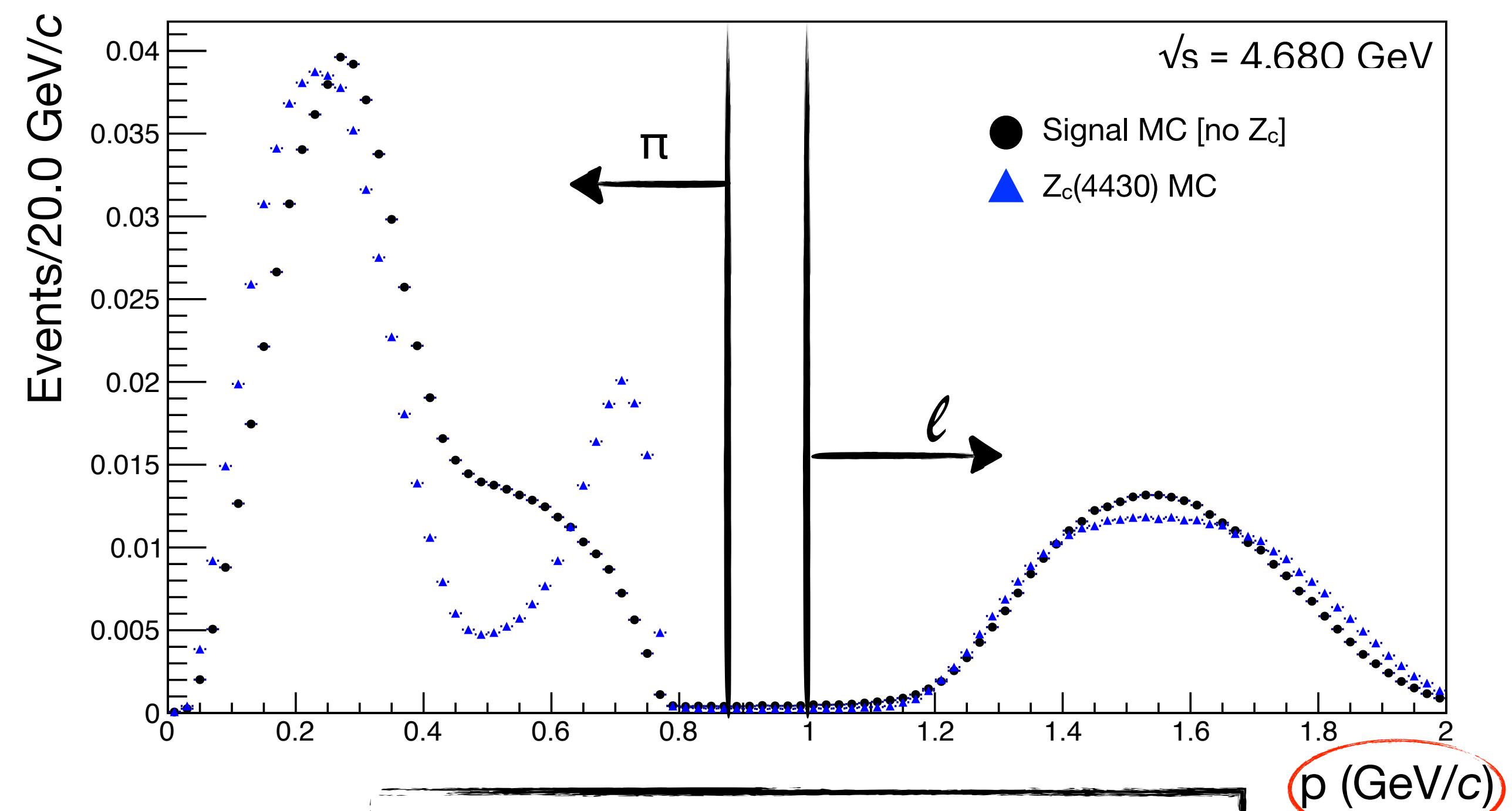
Signal MC sample
300k events



2 good charged topologies

$2\ell 4\pi$

$2\ell 3\pi$



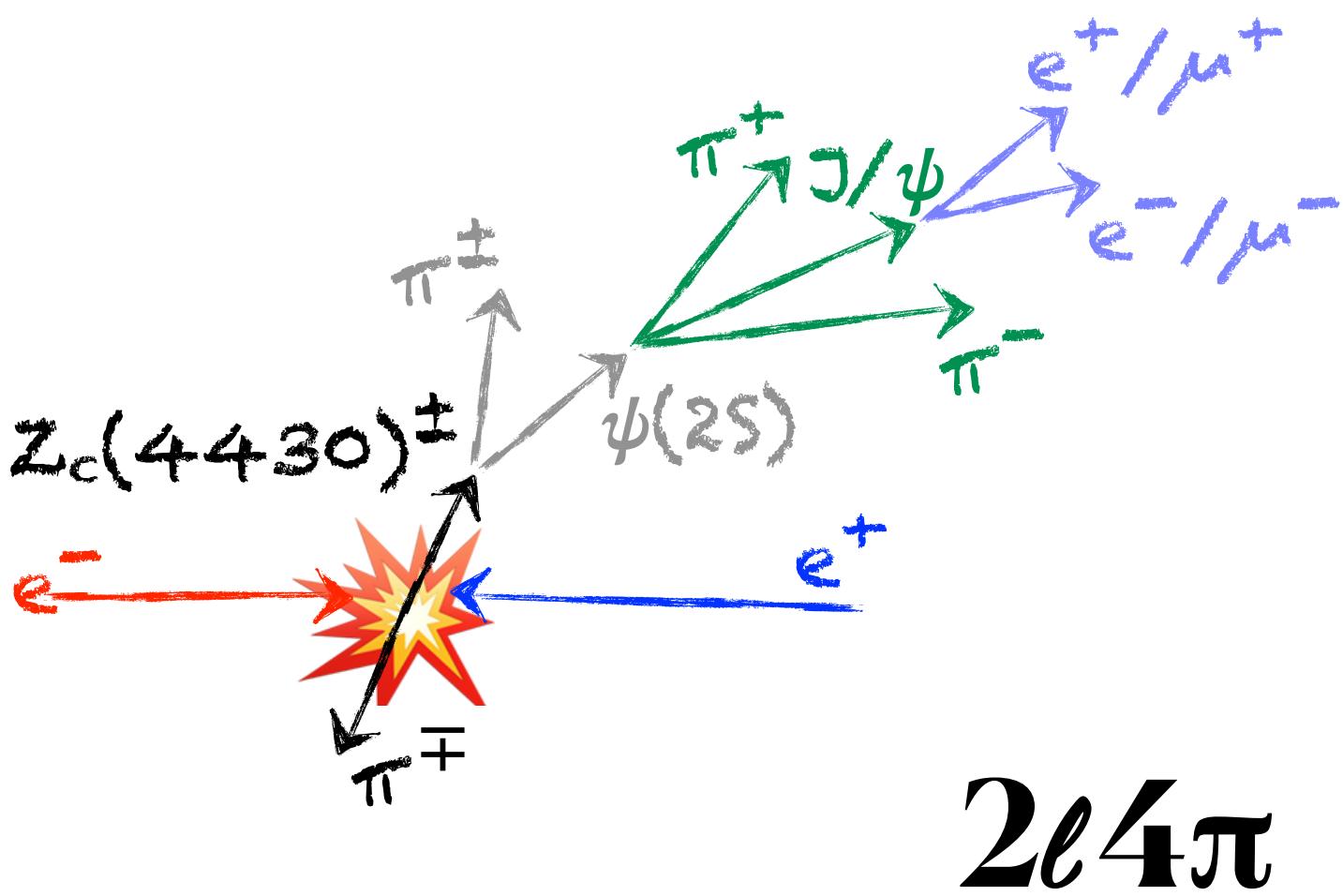
Channel ID

Pions
 $p < 0.85 \text{ GeV}$

Leptons
 $p > 1.00 \text{ GeV}$
 $E/p(e) > 0.7$
 $E/p(\mu) < 0.6$

Event Selection

Topology-dependent Kinematic Fits



6-constraint (6C) kinematic fit

1C on the $M_{J/\psi}$
1C on the $M_{\psi(2S)}$
4C on the $p_{T\text{tot}} = (\sqrt{s} * \sin(0.011), 0, 0, M_{\sqrt{s}})$

The $\pi\pi$ couples are selected via the best χ^2

2ℓ3π

2-constraint (2C) kinematic fit

1C on the $M_{J/\psi}$
1C on the $M_{\psi(2S)}$
 $[p_{T\text{tot}} = (\sqrt{s} * \sin(0.011), 0, 0, M_{\sqrt{s}})]$

$\pi\pi$ and $\pi\pi_{\text{Miss}}^*$ couples are selected by
minimising $M_{\psi(2S)}^{\text{Reco}} - M_{\psi(2S)}^{\text{PDG}}$

* π_{Miss} either from prompt production or from $\psi(2S)$ decay, but not from $Z_c(4430)$

Background Rejection

Inclusive MC sample
10x \mathcal{L} data

Index (i)	Decay tree	N_{Evts}	$\sum_i^{\text{Tot}} N_{Evts}$
1	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow \mu^+\mu^-$	3389	3389
2	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow e^+e^-$	2983	6372
3	$e^+e^- \rightarrow \pi^+\pi^-\psi'\gamma^I, \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow \mu^+\mu^-$	2875	9247
4	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow \mu^+\mu^-$	2528	11775
5	$e^+e^- \rightarrow \pi^+\pi^-\psi'\gamma^I, \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow e^+e^-$	2499	14274
6	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow e^+e^-$	2313	16587
7	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow \mu^+\mu^-$	1346	17933
8	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow e^+e^-$	1249	19182
9	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow \mu^+\mu^-$	1037	20219
10	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow e^+e^-$	907	21126
11	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow \mu^+\mu^-$	307	21433
12	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow e^+e^-$	289	21722
13	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow \mu^+\mu^-$	276	21998
14	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow e^+e^-$	245	22243
15	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow \mu^+\mu^-$	240	22483
16	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow e^+e^-$	197	22680
17	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow \mu^+\mu^-$	188	22868
18	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow \mu^+\mu^-$	161	23029
19	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow e^+e^-$	156	23185
20	$e^+e^- \rightarrow \pi^+\pi^+\pi^+\pi^-\pi^-\pi^-$	144	23329
21	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow \mu^+\mu^-$	132	23461
22	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow e^+e^-$	109	23570
23	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow \mu^+\mu^-$	104	23674
24	$e^+e^- \rightarrow \pi^+\pi^+\pi^+\pi^-\pi^-\pi^-\gamma^I$	103	23777
25	$e^+e^- \rightarrow \pi^+\pi^-\psi', \psi' \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow \mu^+\mu^-$	96	23873
26

From 1.3 billion inclusive MC events, **28136** survive, with a survival rate of $\sim O(10\text{ppm})$

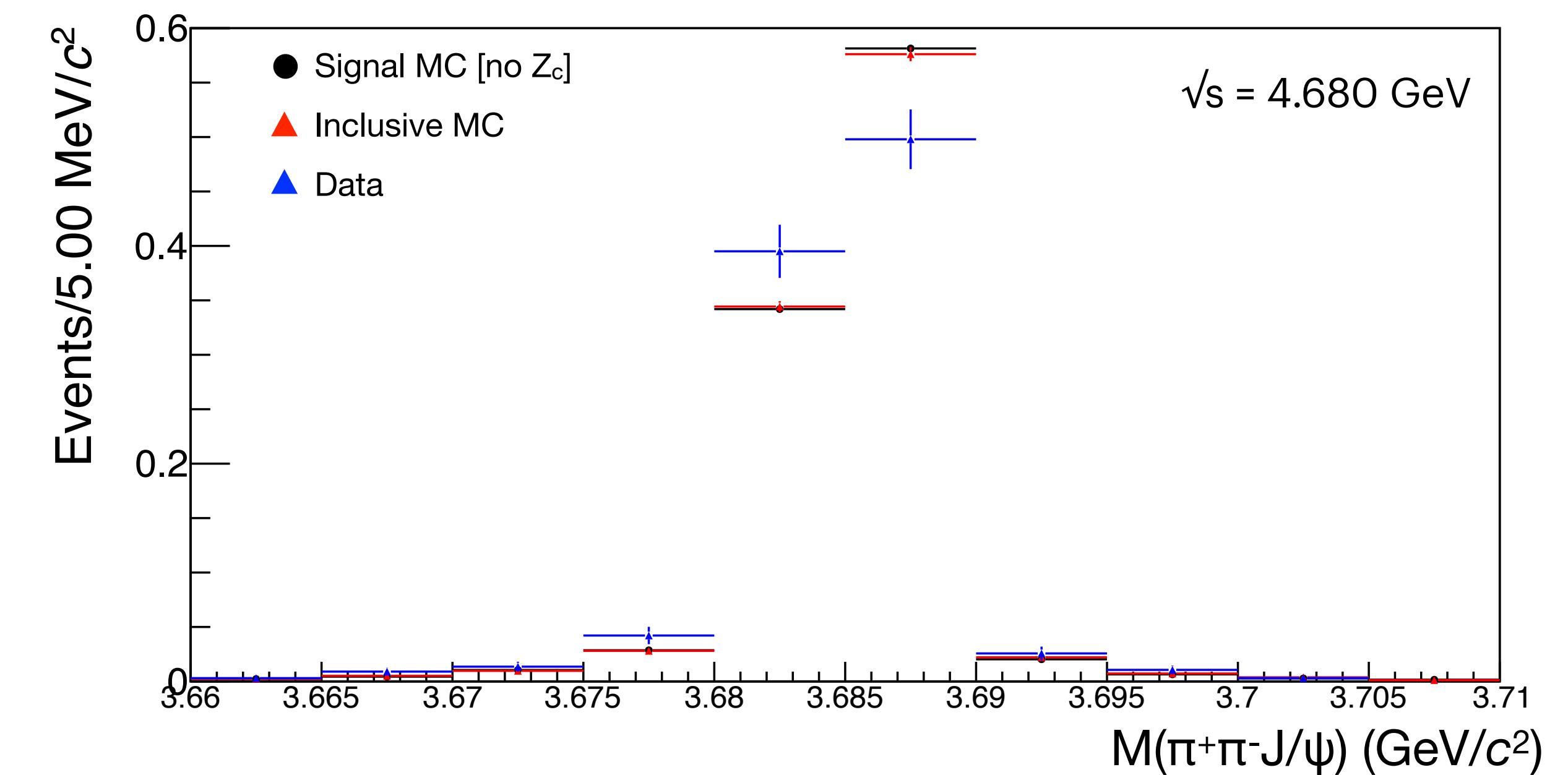
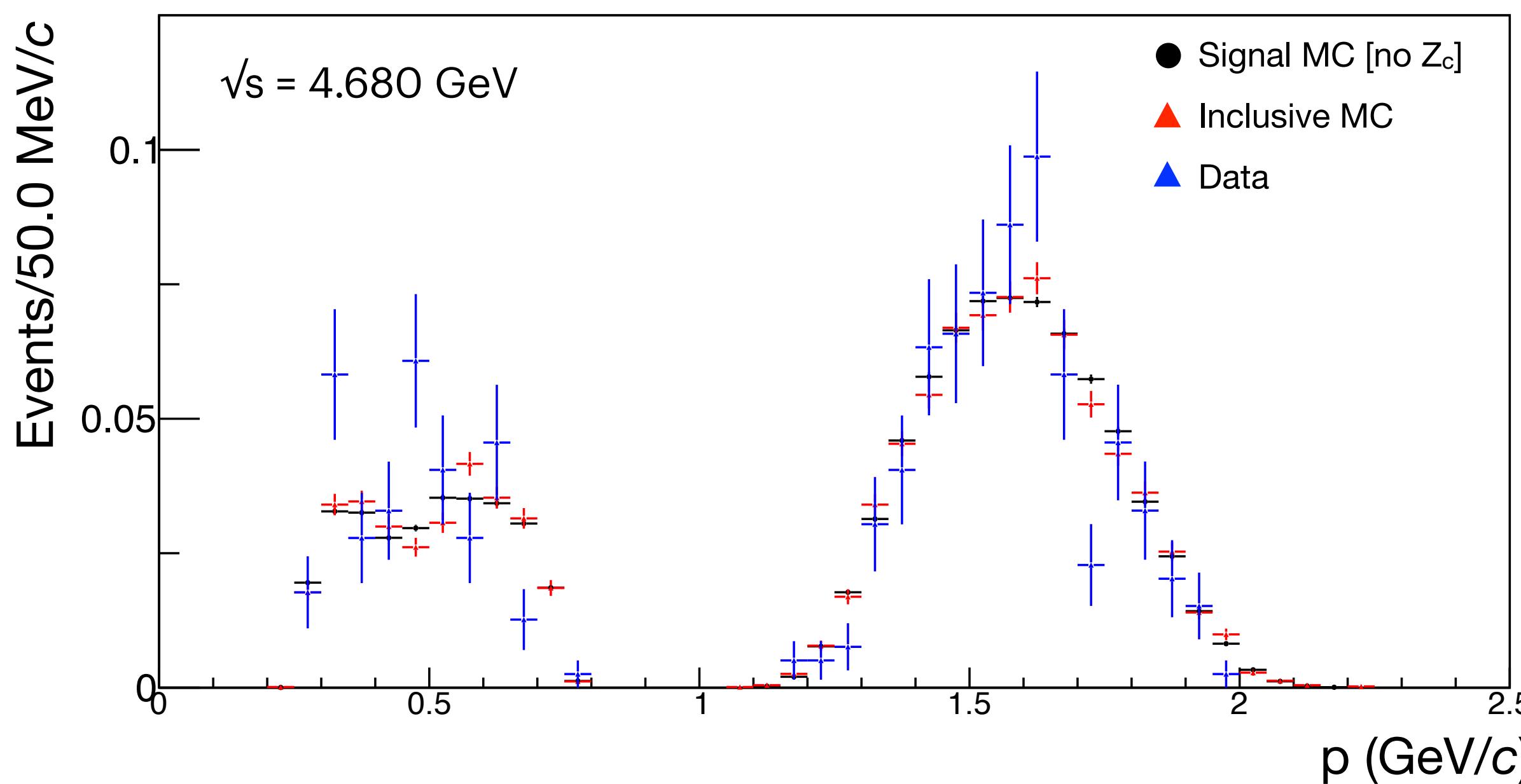
Virtually **only the hadron component** is surviving after the selection criteria

Out of 28136 total **IncMC events**, the events are from

- > 90% Non-resonant **$\pi\pi\psi(2S)$ signal**
- < 10% **Multi- π states**

After Selection Comparison

Inclusive MC / Signal MC [no Z_c] / Data



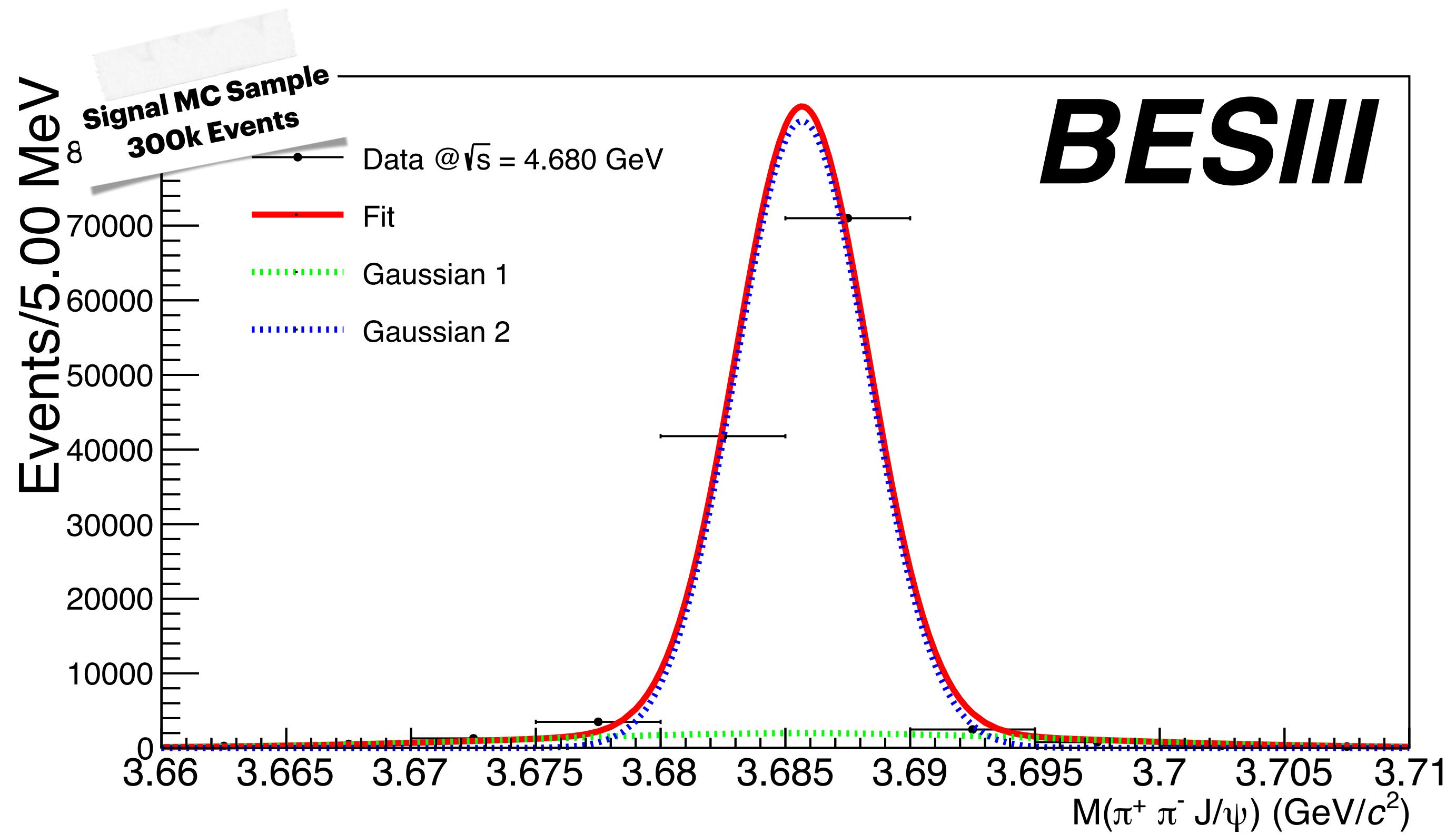
Extraction of the $\sigma(e^+e^- \rightarrow \pi^+\pi^-\Psi(2S))$

Study of $e^+e^- \rightarrow \pi^+\pi^-\Psi(2S)$ at $\sqrt{s} > 4.6$ GeV and search for the $Z_c(4430)^\pm$ - Marco Scodellaggio



Extraction of the $\sigma(e^+e^- \rightarrow \pi^+\pi^-\psi(2S))$

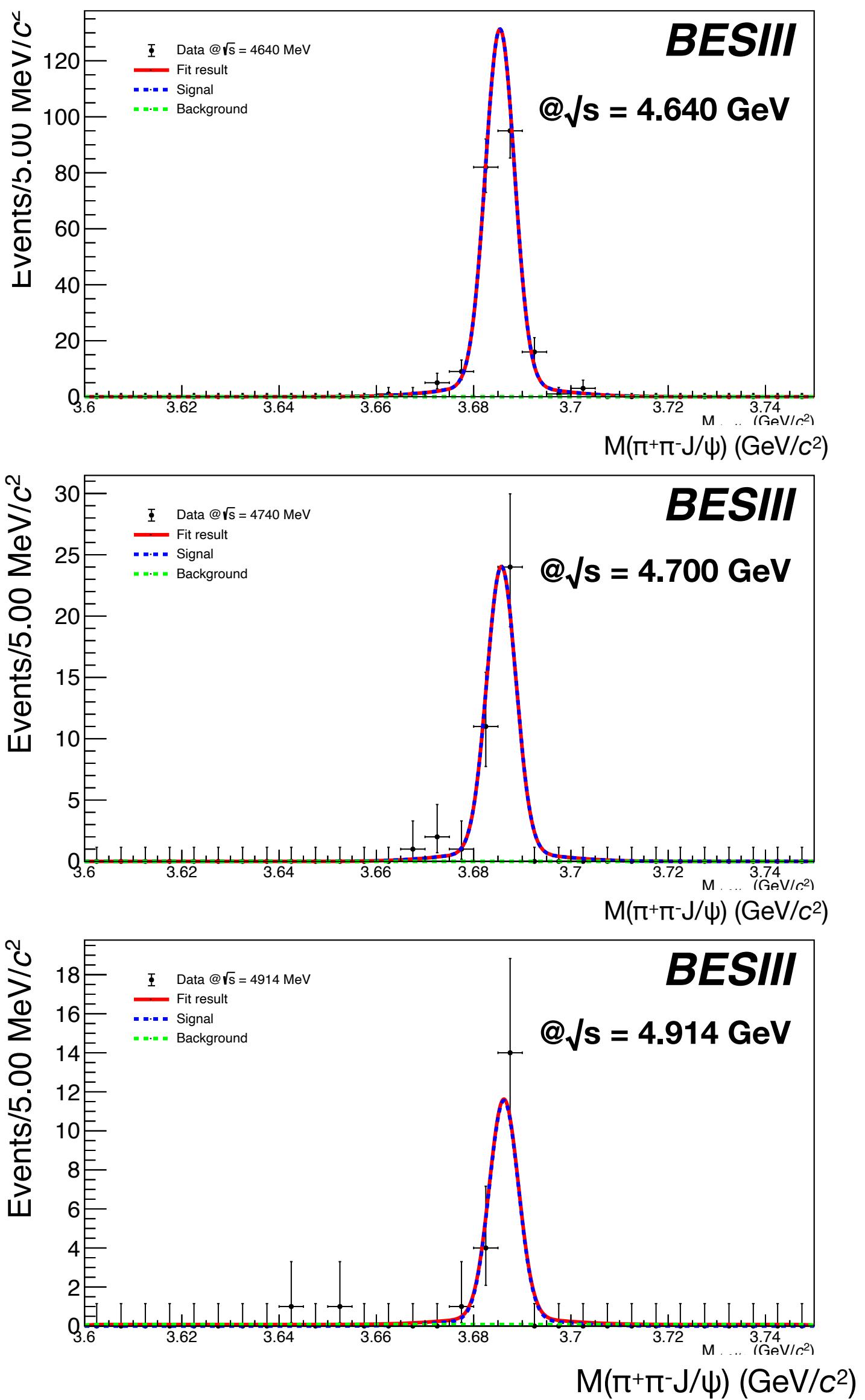
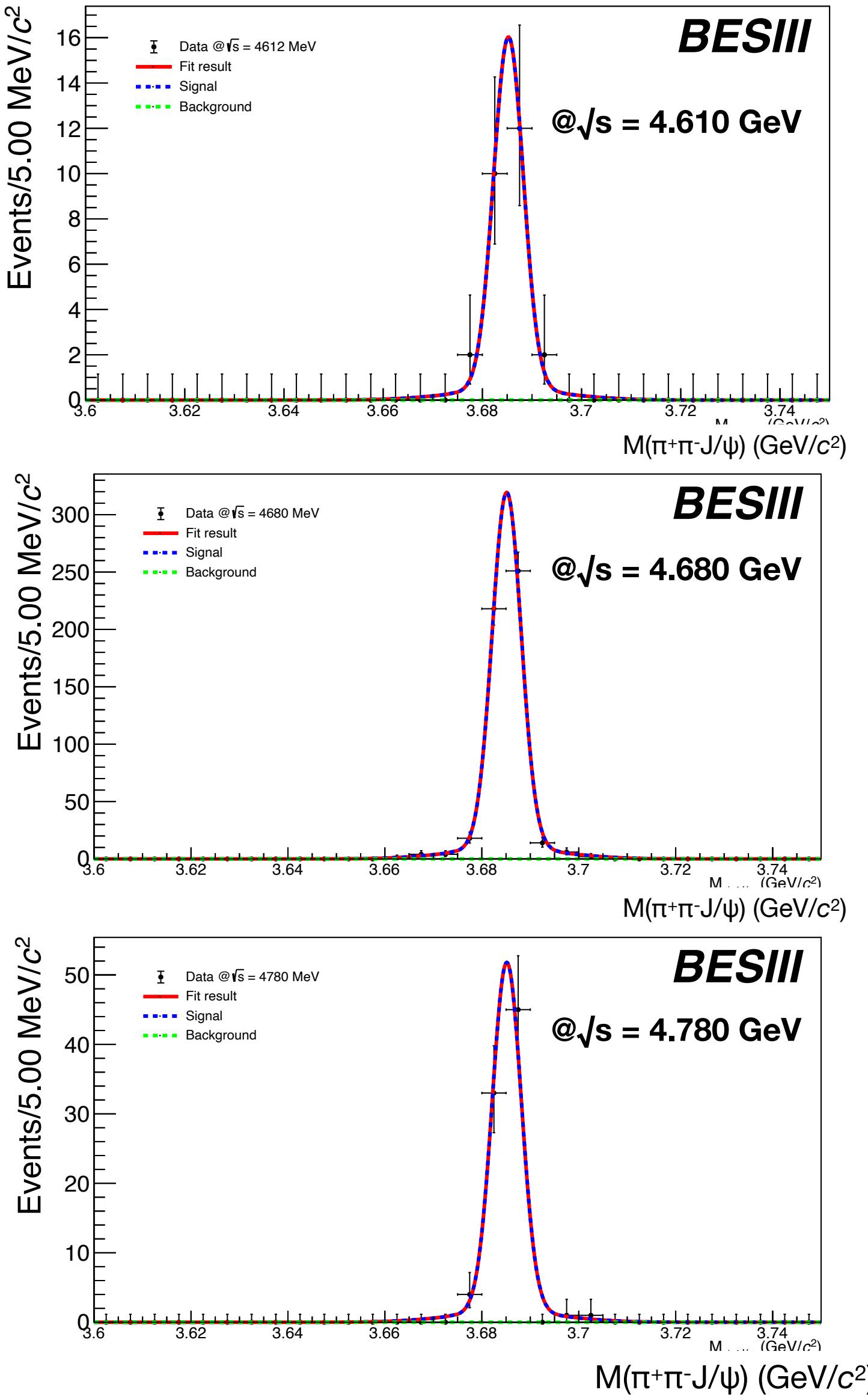
Signal Shape & Efficiency



For **each \sqrt{s}** , the **signal** is modelled via
a signal MC sample with a **sum of**
Gaussian and Crystal Ball functions

$\langle \text{Efficiency} \rangle \sim 36\%_{\text{Conexc}} (34\%_{\text{KKMC}})$

Extraction of the $\sigma(e^+e^- \rightarrow \pi^+\pi^-\psi(2S))$



Data Fits

For **each \sqrt{s}** , the $\pi\pi\psi(2S)$ contribution is extracted by **fitting the $M(\pi\pi J/\psi)$** invariant spectrum

The **signal** is modelled with a **sum of Gaussian and Crystal Ball**

A **polynomial** function is used to describe the **background**

Extraction of the $\sigma(e^+e^- \rightarrow \pi^+\pi^-\psi(2S))$

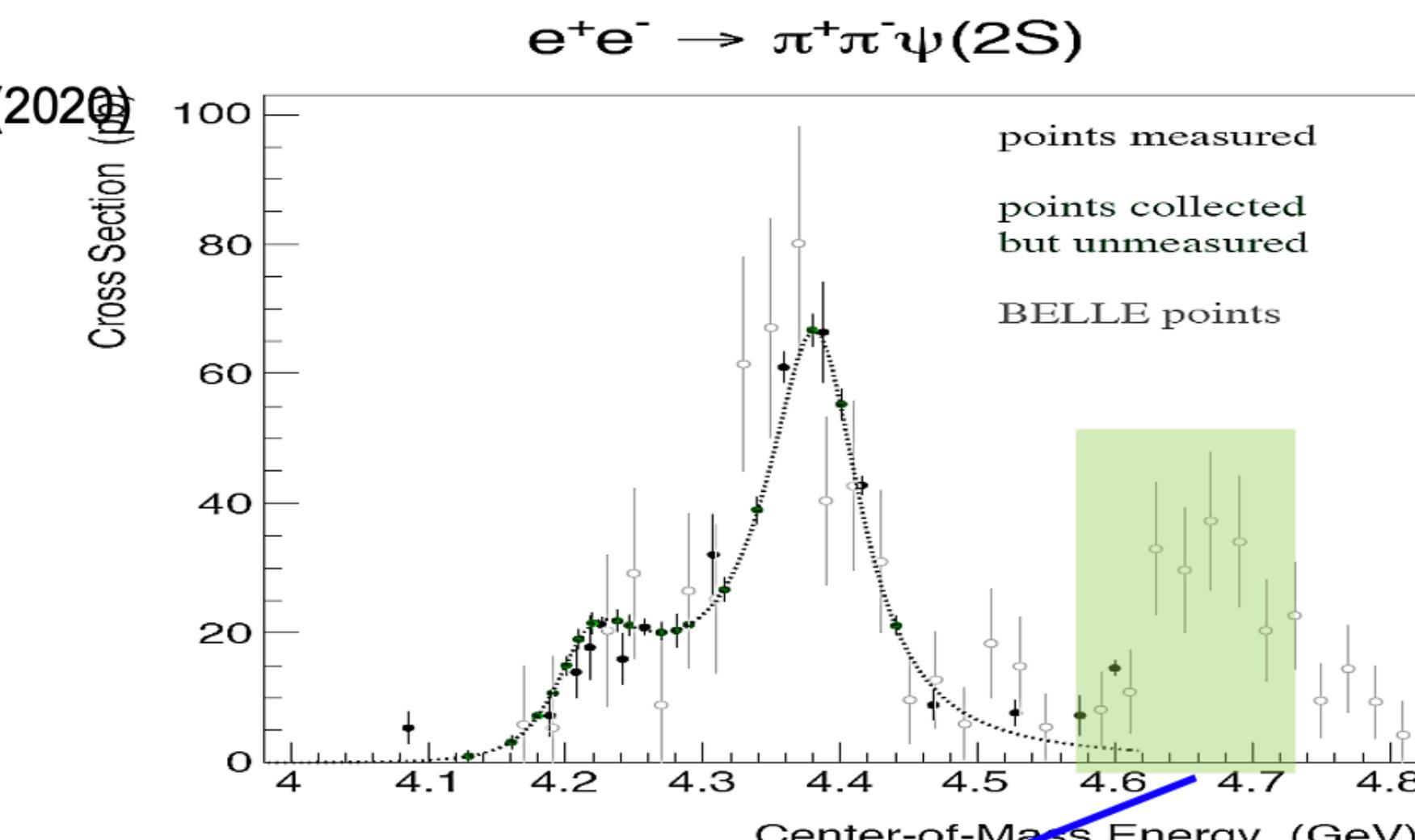
The Energy and Luminosity Update on BEPCII

Urgency from HEP

Future Physics Program of BESIII, Chin. Phys. C 44, 040001 (2020)

Table 7.1: List of data samples collected by BESIII/BEPCII up to 2019, and the proposed samples for the remainder of the physics program. The most right column shows the number of required data taking days in current (T_C) or upgraded (T_U) machine. The machine upgrades include top-up implementation and beam current increase.

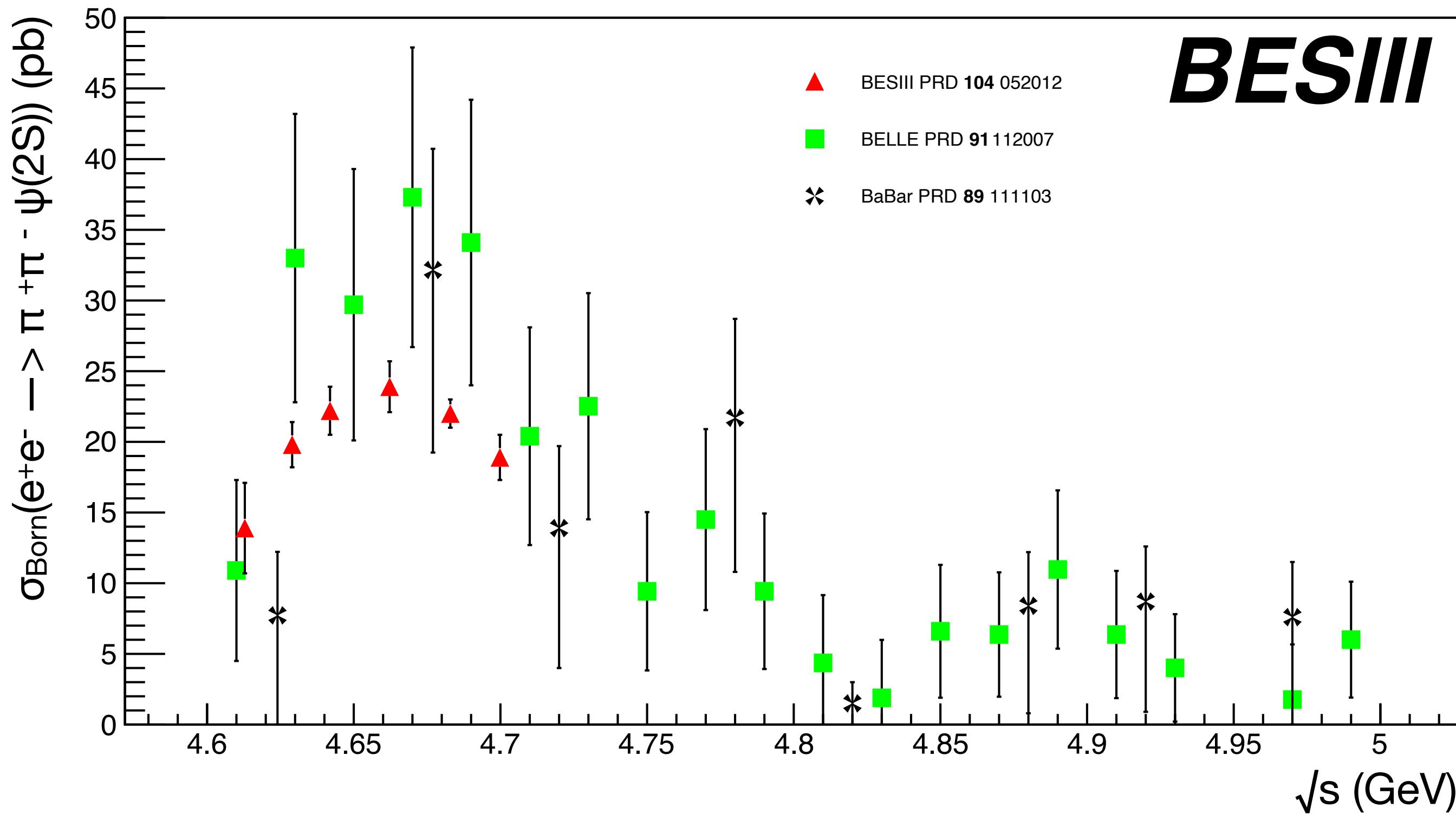
Energy	Physics motivations	Current data	Expected final data	T_C / T_U
1.8 - 2.0 GeV	R values Nucleon cross-sections	N/A	0.1 fb^{-1} (fine scan)	60/50 days
2.0 - 3.1 GeV	R values Cross-sections	Fine scan (20 energy points)	Complete scan (additional points)	250/180 days
J/ψ peak	Light hadron & Glueball J/ψ decays	3.2 fb^{-1} (10 billion)	3.2 fb^{-1} (10 billion)	N/A
$\psi(3686)$ peak	Light hadron & Glueball Charmonium decays	0.67 fb^{-1} (0.45 billion)	4.5 fb^{-1} (3.0 billion)	150/90 days
$\psi(3770)$ peak	D^0/D^\pm decays	2.9 fb^{-1}	20.0 fb^{-1}	610/360 days
3.8 - 4.6 GeV	R values $X\bar{Y}\bar{Z}$ /Open charm	Fine scan (105 energy points)	No requirement	N/A
4.180 GeV	D_s decay $X\bar{Y}\bar{Z}$ /Open charm	3.2 fb^{-1}	6 fb^{-1}	140/50 days
4.0 - 4.6 GeV	$X\bar{Y}\bar{Z}$ /Open charm Higher charmonia cross-sections	16.0 fb^{-1} at different \sqrt{s}	30 fb^{-1} at different \sqrt{s}	770/310 days
4.6 - 4.9 GeV	Charmed baryon/ $X\bar{Y}\bar{Z}$ cross-sections	0.56 fb^{-1}	15 fb^{-1}	1490/600 days
4.74 GeV	$\Sigma_c^+\Lambda_c^-$ cross-section	N/A	1.0 fb^{-1}	100/40 days
4.91 GeV	$\Sigma_c\Sigma_c$ cross-section	N/A	1.0 fb^{-1}	120/50 days
4.95 GeV	Ξ_c decays	N/A	1.0 fb^{-1}	130/50 days



The Progress on the BEPCII Upgrade, LIU Y. D.

Extraction of the $\sigma(e^+e^- \rightarrow \pi^+\pi^-\psi(2S))$

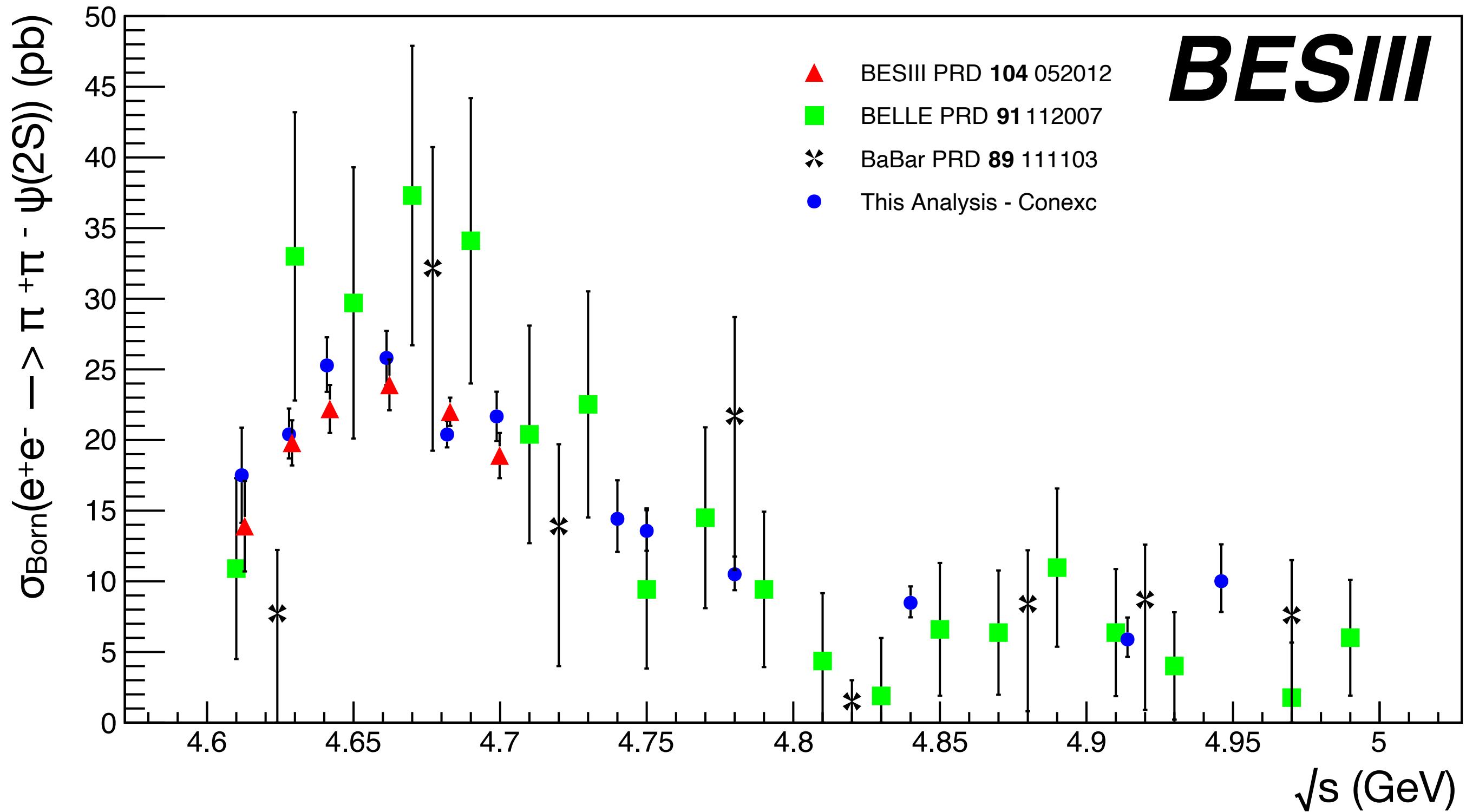
$\pi\pi\psi(2S)$ cross-section



[11] Phys. Rev. D **104**, 052012

Extraction of the $\sigma(e^+e^- \rightarrow \pi^+\pi^-\psi(2S))$

$\pi\pi\psi(2S)$ cross-section



$$\sigma_{\text{Born}} = \frac{N_{\text{Obs}}}{\mathcal{L}(1 + \delta) \frac{1}{|1 - \Pi^2|} \epsilon \mathcal{B}}$$

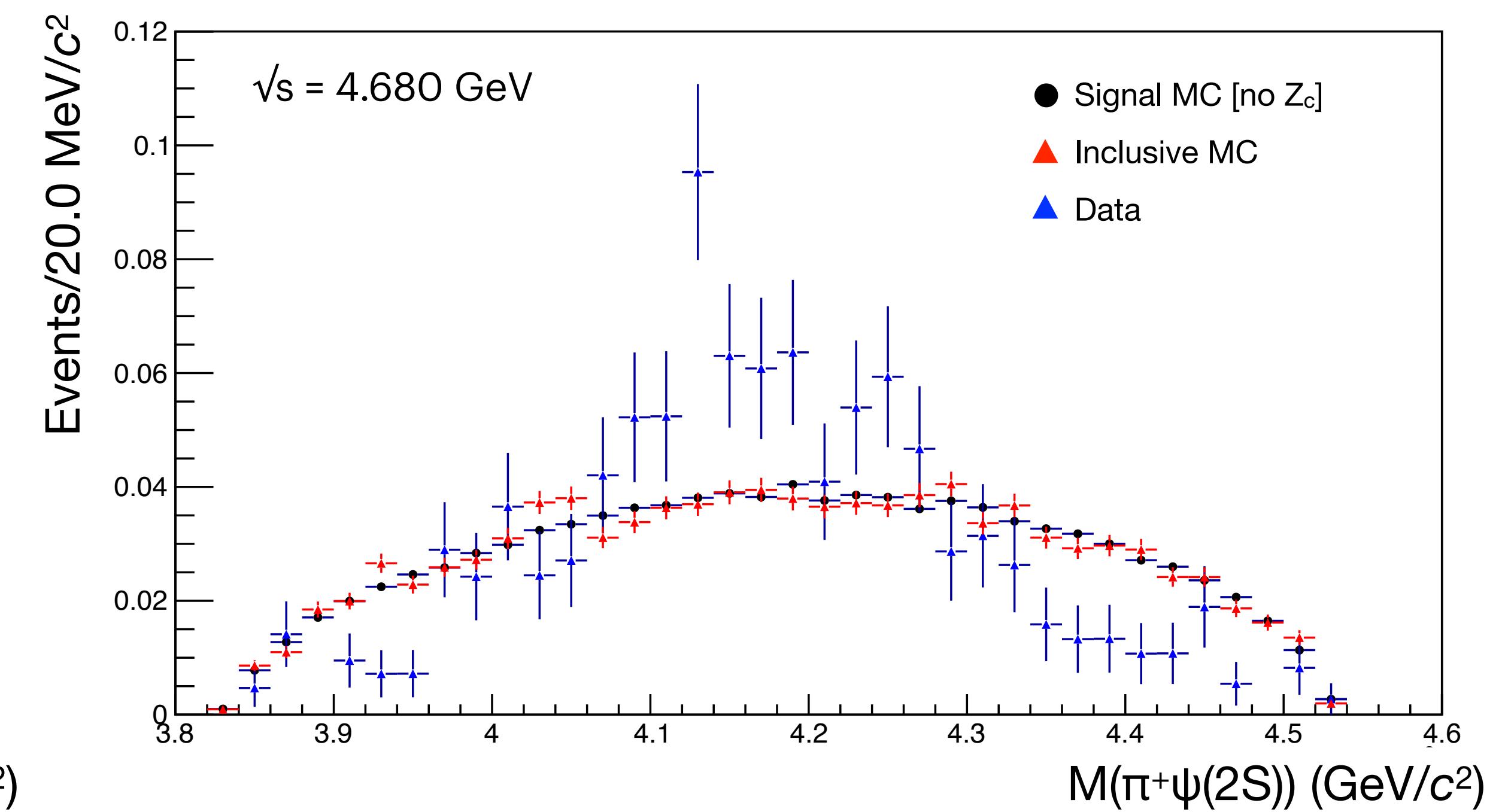
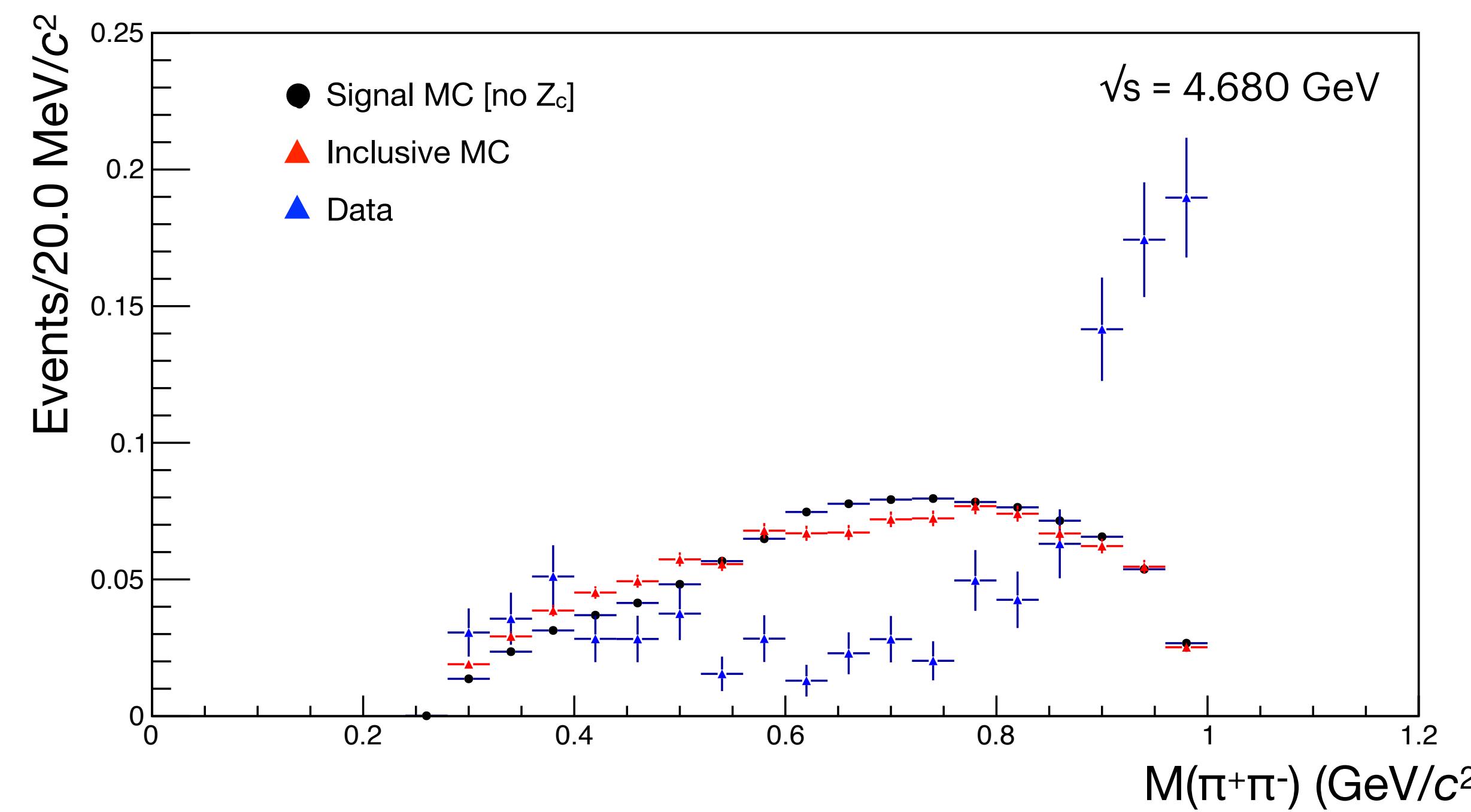
The observed **cross-section** is **compatible** with the previous result of **Ref. [11]**

Results from BELLE and BaBar are reported too, further **confirming the compatibility** of this thesis' results with the published literature

[11] Phys. Rev. D 104, 052012

Study of the invariant masses profiles

Inclusive MC / Non-resonant MC/ Data

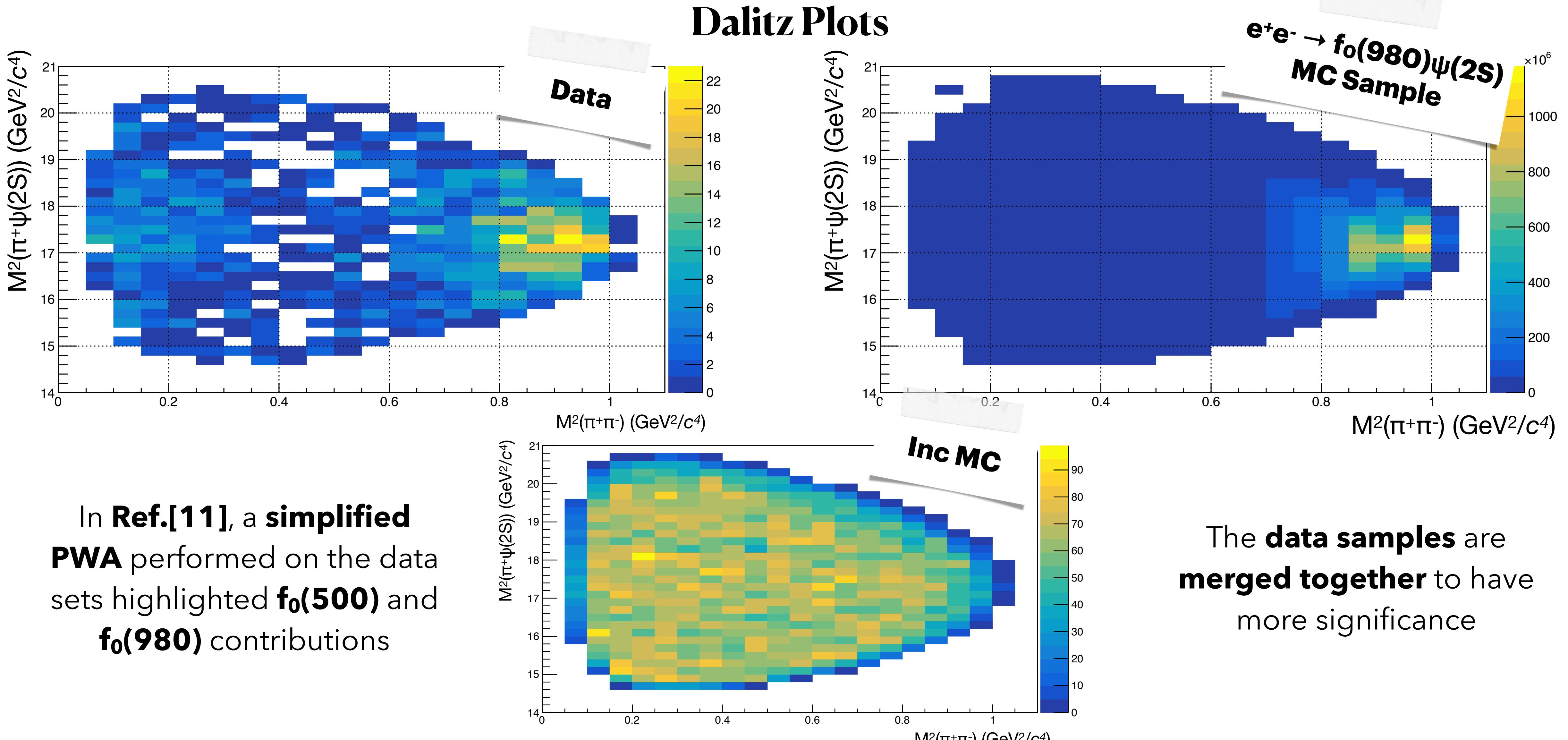


Study of the Intermediate States

Study of $e^+e^- \rightarrow \pi^+\pi^-\Psi(2S)$ at $\sqrt{s} > 4.6$ GeV and search for the $Z_c(4430)^\pm$ - Marco Scodellaggio

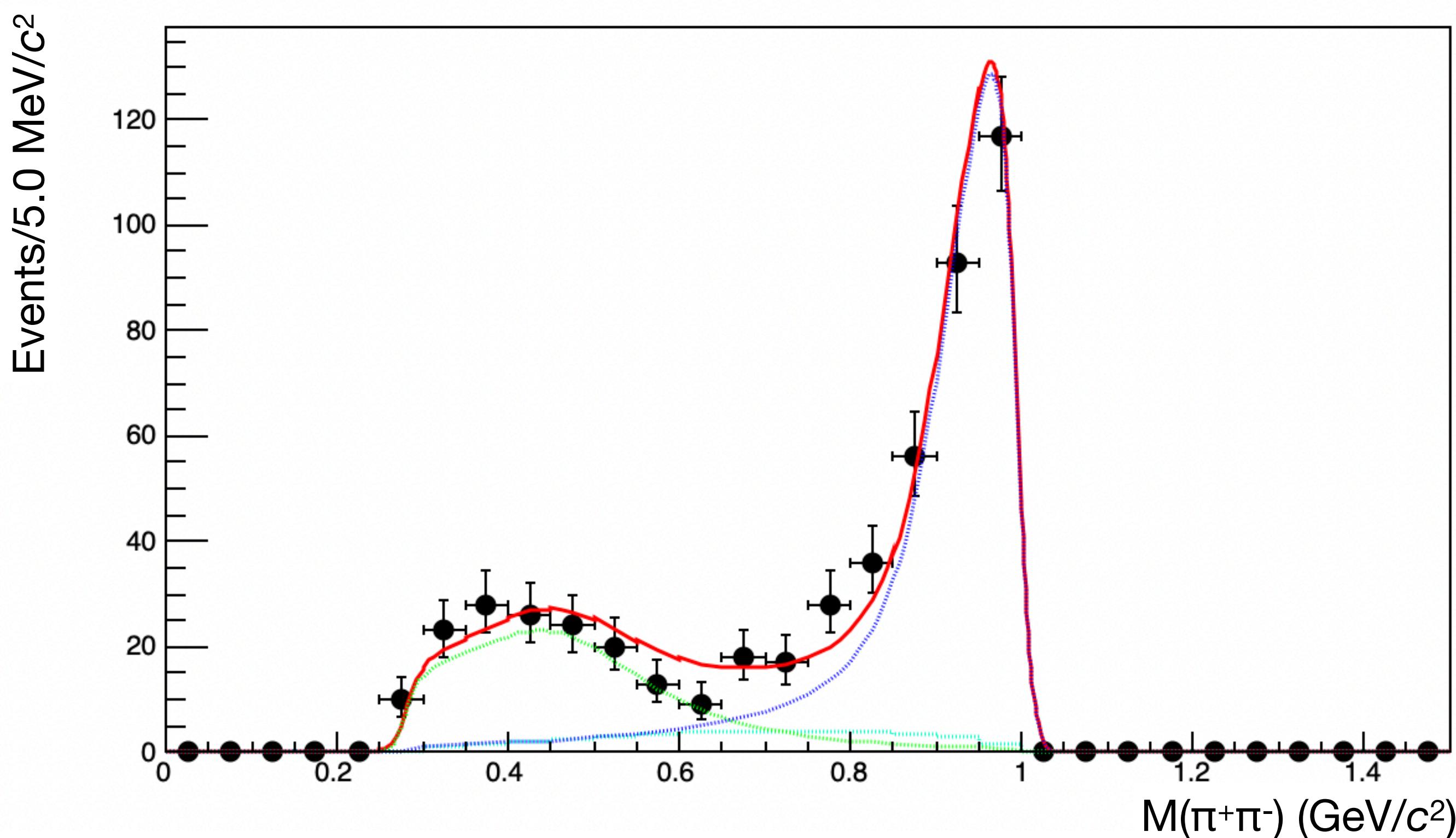


Study of the Intermediate States



Extraction of the $\sigma(f_0(980)\psi(2S))$

$f_0(980)$ contribution



For **each \sqrt{s}** , the **$f_0(980)$** contribution is extracted by fitting the $M(\pi\pi)$ and $M(\pi\psi(2S))$ invariant distributions

The signal is a **Flatté smeared by a Gauss(0, σ) multiplied by a threshold** function

$$BW(s) = \frac{1}{s - M^2 + i(g_1\rho_{\pi\pi}(s) + g_2\rho_{KK}(s))}$$

The **$f_0(500)$** contribution is modelled with

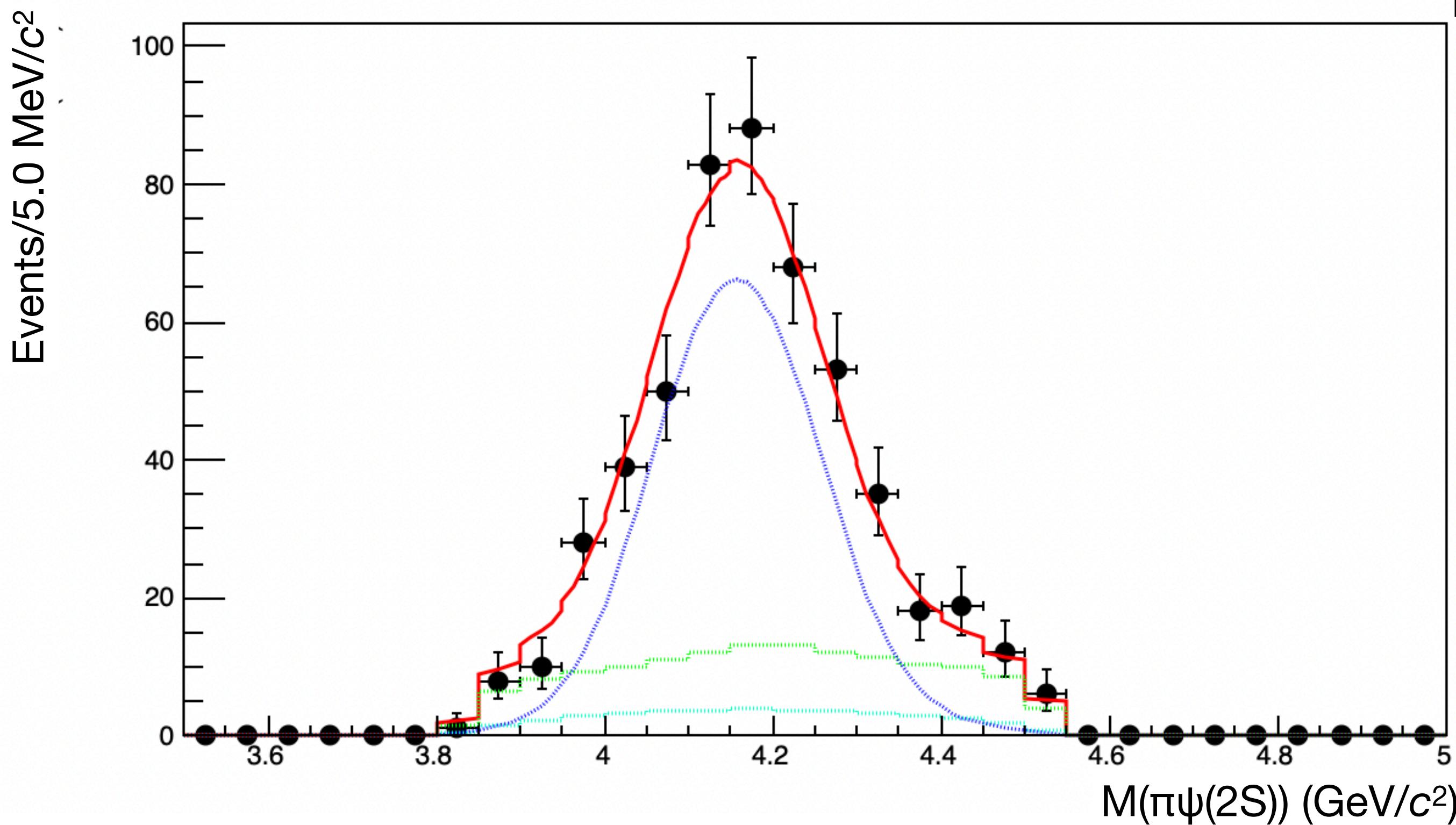
$$BW(s) = \frac{1}{s - M_0^2 + i\sqrt{s}\Gamma}$$

with an energy-dependent width à la E791...

$$\Gamma(s) = \sqrt{1 - \frac{4m_{\pi^\pm}^2}{s}}\Gamma$$

Extraction of the $\sigma(f_0(980)\psi(2S))$

$f_0(980)$ contribution



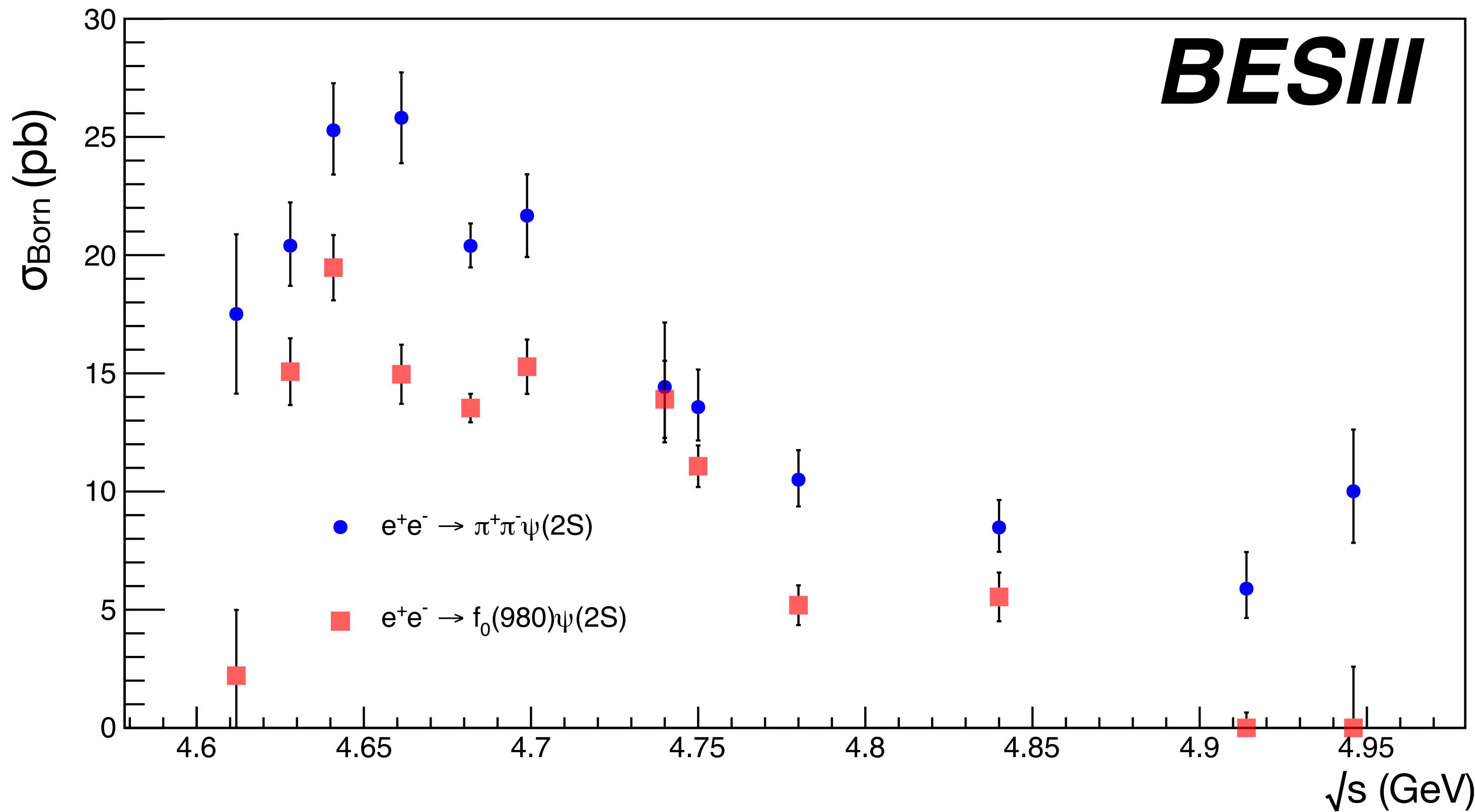
For **each \sqrt{s}** , the **$f_0(980)$** contribution is extracted by fitting the $M(\pi\pi)$ and $M(\pi\psi(2S))$ invariant distributions

The signal is a **MS shape smeared by a Gauss(0, σ)**

The **$f_0(500)$** and **PHSP** contributions are modelled too by a **MS shape**

Extraction of the $\sigma(f_0(980)\psi(2S))$

$f_0(980)$ contribution



No particular structures
can be recognised

Within the statistical uncertainty,
 $\sigma_{\text{Born}} \times \mathbf{B}$ is **flat** wrt $\sigma_{\text{Born}}(\pi\pi\psi(2S))$

The hypothesis of the **Y(4660)** being
an **$f_0(980)$ - $\psi(2S)$ molecule**^[12]
cannot be confirmed

[12] Phys. Lett. B 665, 26-29 (2008)

Systematic Uncertainties on the Cross-sections

- *Luminosity*: 1% as from Ref. [13]
- *Vacuum polarisation*: 0.5% from Ref. [14]
- *ISR radiative corrections*: Difference in the $(1 + \delta)$ between the last two iterations
- *Tracking efficiency*: 1.0% per track^[10], 2.0% (leptons) and 3.5% (average of 2 pion-topologies)
- *Intermediate states branching fractions*: from PDG
- *Lepton separation, trigger efficiency, and FSR*: 1.0% from Ref. [11]

[10] Phys. Rev. Lett **110**, 252001

[11] Phys. Rev. D **104**, 052012

[13] Chin. Phys. C **46**, 11, 113003

[14] Sov. J. Nucl. Phys. **41**, 466-472

Final Born Cross-sections Results

E_{CoM} (MeV)	$\sigma_{\text{Born}}^{e^+e^- \rightarrow \pi^+\pi^-\psi(2S)}$	$\sigma_{\text{Born}}^{e^+e^- \rightarrow f_0(980)\psi(2S)} \times \mathcal{B}(f_0(980) \rightarrow \pi^+\pi^-)$
4.612	$17.51 \pm 3.37 \pm 0.68$	$2.21 \pm 2.78 \pm 0.09$
4.626	$20.40^{+1.83}_{-1.70} \pm 0.80$	$15.07 \pm 1.41 \pm 0.58$
4.640	$25.28^{+1.99}_{-1.87} \pm 0.99$	$19.47 \pm 1.38 \pm 0.75$
4.660	$25.81 \pm 1.92 \pm 1.01$	$14.96 \pm 1.25 \pm 0.58$
4.680	$20.39^{+0.95}_{-0.91} \pm 0.80$	$13.53 \pm 0.60 \pm 0.53$
4.700	$21.67^{+1.75}_{-1.75} \pm 0.85$	$15.28 \pm 1.15 \pm 0.59$
4.740	$14.42^{+2.73}_{-2.34} \pm 0.57$	$13.90 \pm 1.63 \pm 0.54$
4.750	$13.57^{+1.59}_{-1.41} \pm 0.54$	$11.07 \pm 0.88 \pm 0.43$
4.780	$10.50^{+1.25}_{-1.13} \pm 0.42$	$5.19 \pm 0.84 \pm 0.21$
4.840	$8.48^{+1.16}_{-1.03} \pm 0.34$	$5.54 \pm 1.03 \pm 0.22$
4.914	$5.89^{+1.55}_{-1.24} \pm 0.24$	$0.00 \pm 0.65 \pm 0.00$
4.946	$10.01^{+2.61}_{-2.18} \pm 0.39$	$0.00 \pm 2.59 \pm 0.00$

Analysis of the $\pi^\pm\psi(2S)$ Invariant Mass and Search for the $Z_c(4430)^\pm$

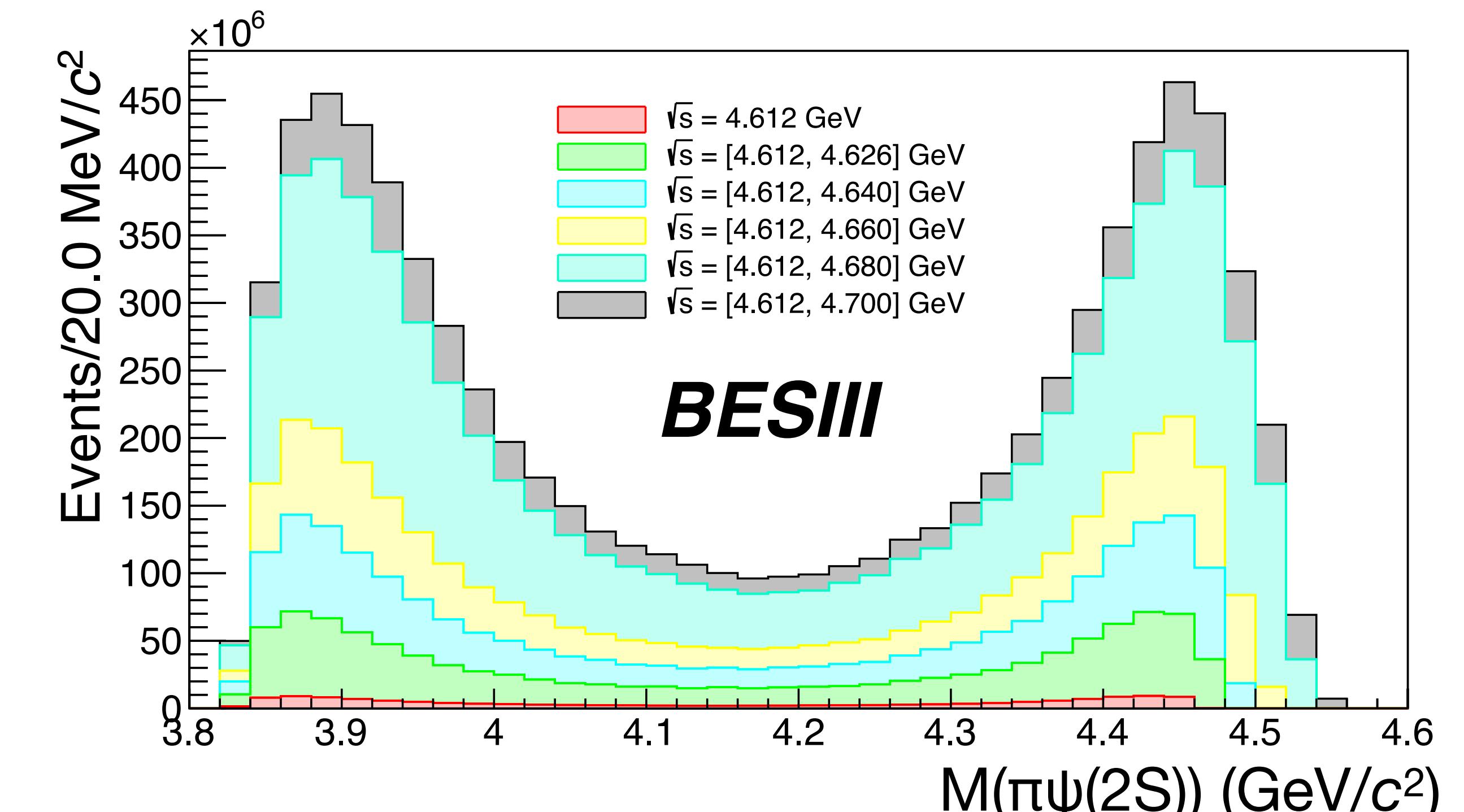
Study of $e^+e^- \rightarrow \pi^\pm\pi^\mp\psi(2S)$ at $\sqrt{s} > 4.6$ GeV and search for the $Z_c(4430)^\pm$ - Marco Scodellaggio



Analysis of the $\pi^\pm\psi(2S)$ Invariant Mass and Search for the $Z_c(4430)^\pm$

Signal MC Shape Extraction

\sqrt{s} [GeV]	$w_{\text{Normalised}} = (\sigma \times \mathcal{L}) / (\sigma \times \mathcal{L}) _{4.680}$
4.612	0.05
4.626	0.31
4.640	0.41
4.660	0.40
4.680	1.00
4.700	0.34
4.740	0.07
4.750	0.15
4.780	0.16
4.840	0.13
4.914	0.04
4.946	0.05



Signal function
MC Signal Shape

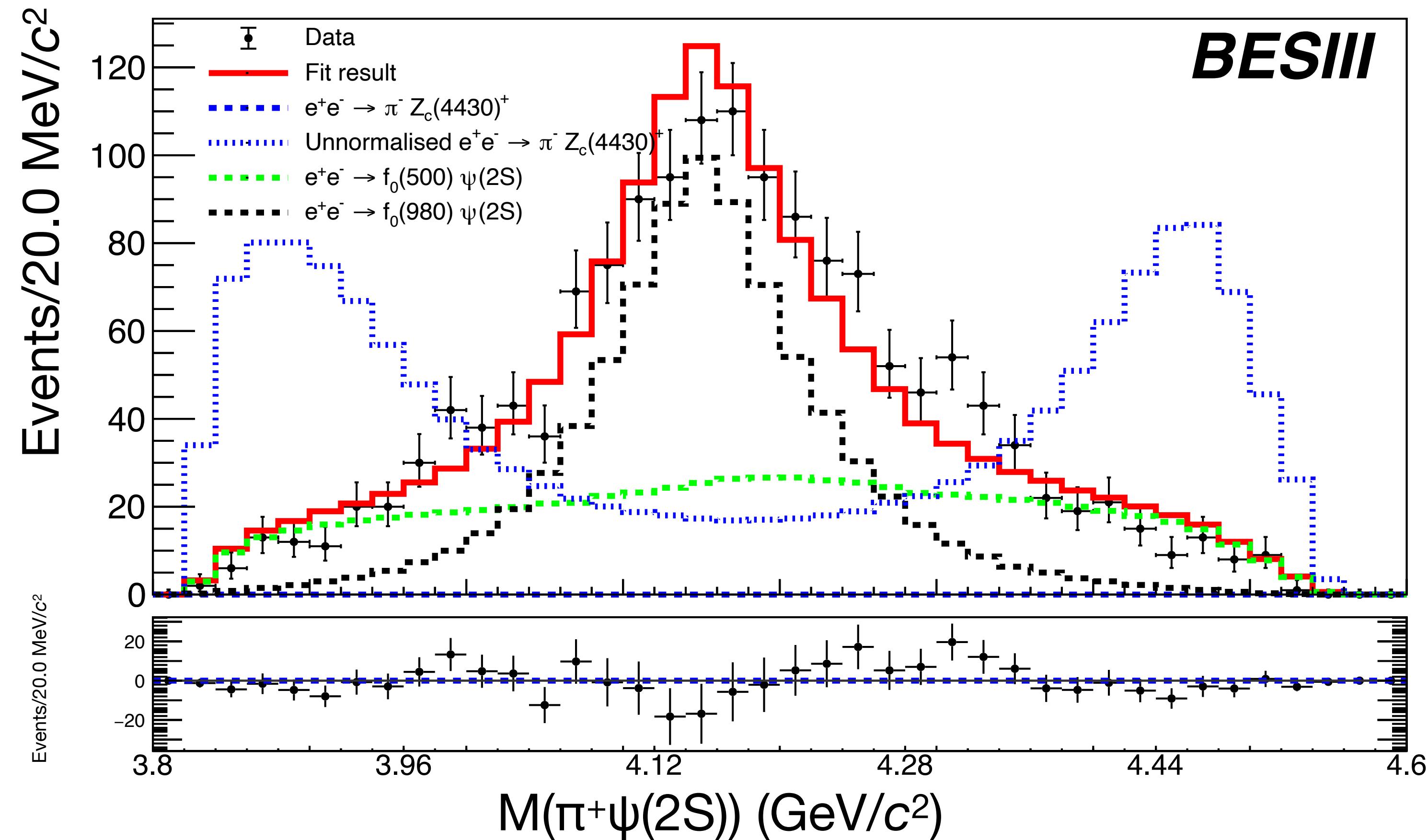
**Z_c Signal MC sample
300k events**

Analysis of the $\pi^\pm\psi(2S)$ Invariant Mass and Search for the $Z_c(4430)^\pm$

In accordance with Ref.[11] and the Dalitz plots only f_0 contributions are considered

Yield is 0 ± 4 , hence no evident $Z_c(4430)$ contribution is present

Bayesian U.L.
@90% C.L. is set



Analysis of the $\pi^\pm\psi(2S)$ Invariant Mass and Search for the $Z_c(4430)^\pm$

Production Ratio Estimation

Bayesian U.L. @90%
 $N(Z_c(4430)) < 17$

$$R = \frac{\sigma_{\text{Born}}(e^+e^- \rightarrow \pi^\pm Z_c(4430)^\mp \rightarrow \pi^+\pi^-\psi(2S))}{\sigma_{\text{Born}}(e^+e^- \rightarrow \pi^+\pi^-\psi(2S))} < 1.1 \%$$

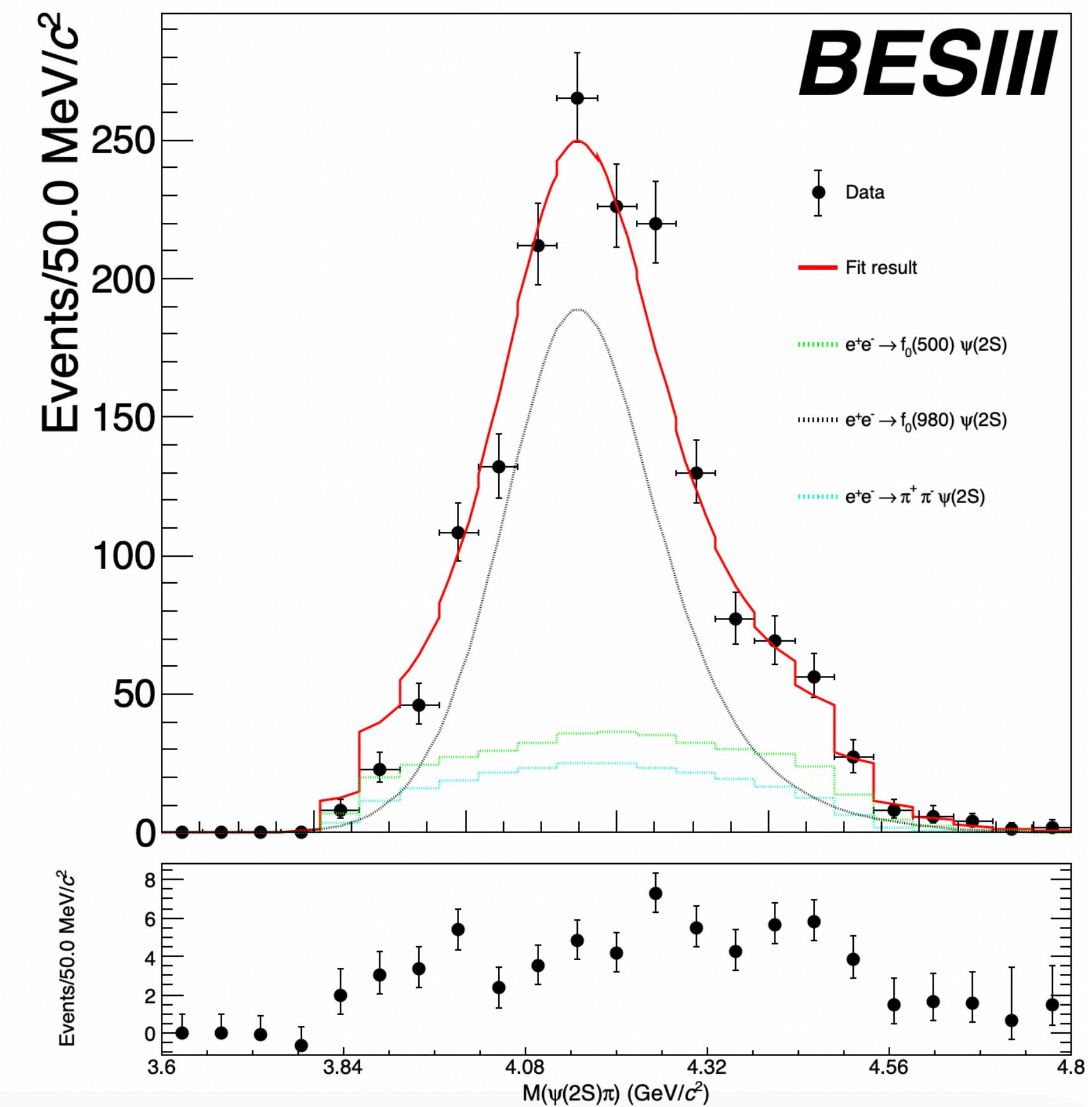
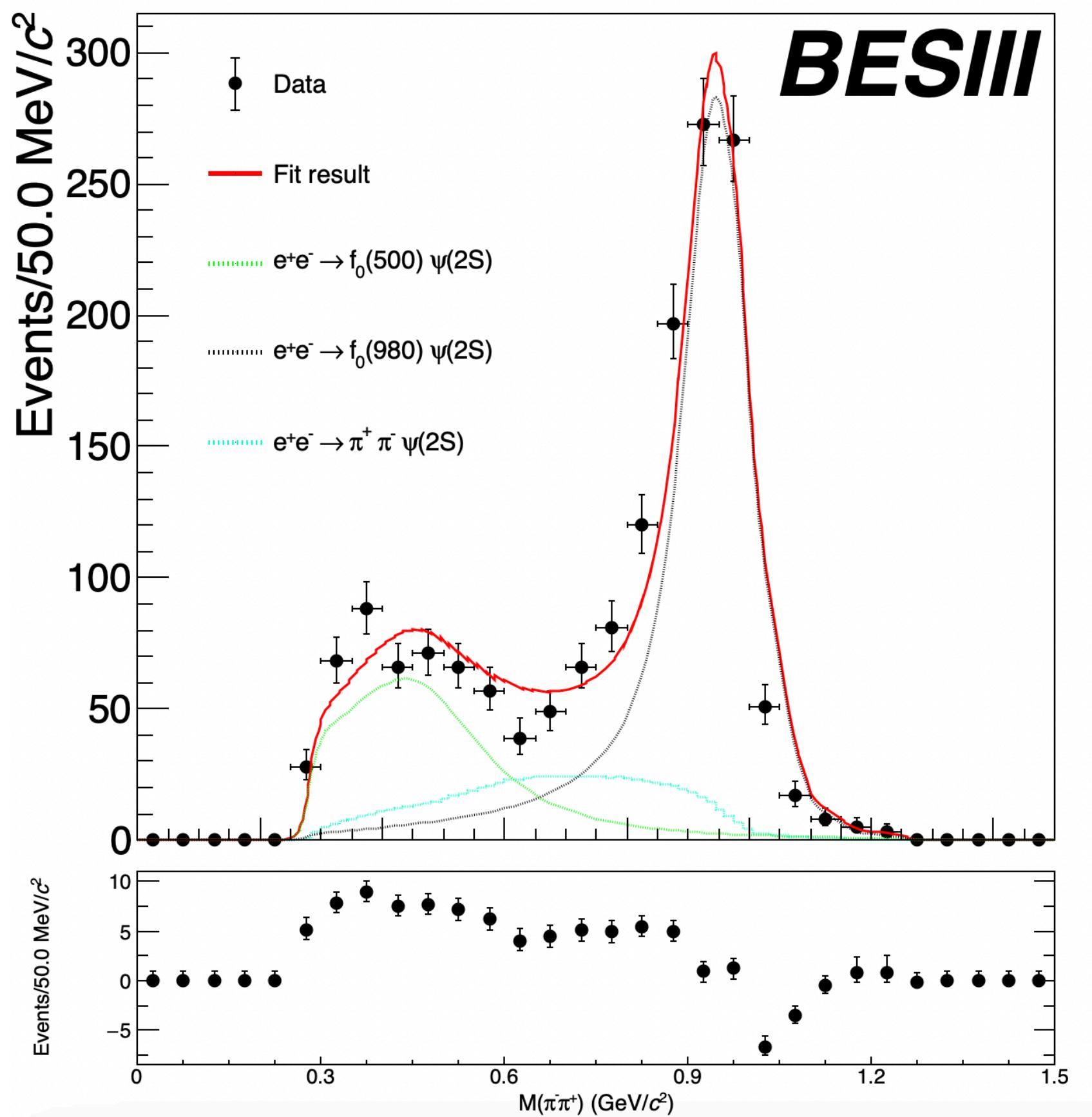
When **compared with the paper**^[10] used as motivation for this analysis, the $Z_c(4430)^\pm$ state **production** in the $e^+e^- \rightarrow \pi^+\pi^-\psi(2S)$ channel is **suppressed by** at least **20 times with respect to** that of the $Z_c(3900)^\pm$ hadron in $e^+e^- \rightarrow \pi^+\pi^+J/\psi$

Analysis of the $\pi^\pm\psi(2S)$ Invariant Mass and Search for the $Z_c(4430)^\pm$

Drawing from the $f_0(980)$ study,
the the **M($\pi\pi$)** and **M($\pi\psi(2S)$)**
invariant distributions are **fitted**
without $Z_c(4430)$ contribution

The two f_0 states are described by
analytical shapes, with the $f_0(980)$
being a weighted sum of 12 Flattés

All the other shapes are taken from
MC simulation

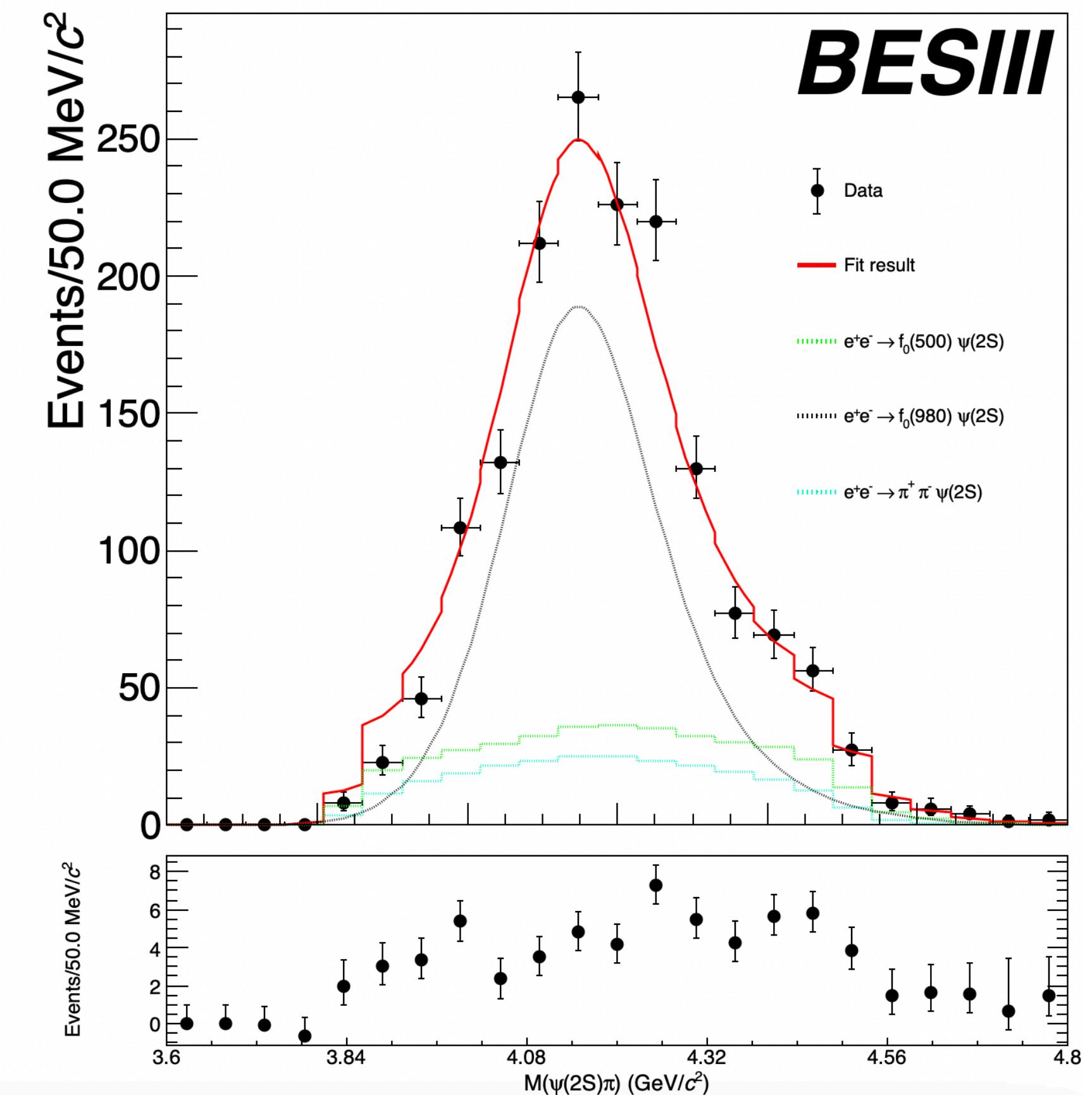
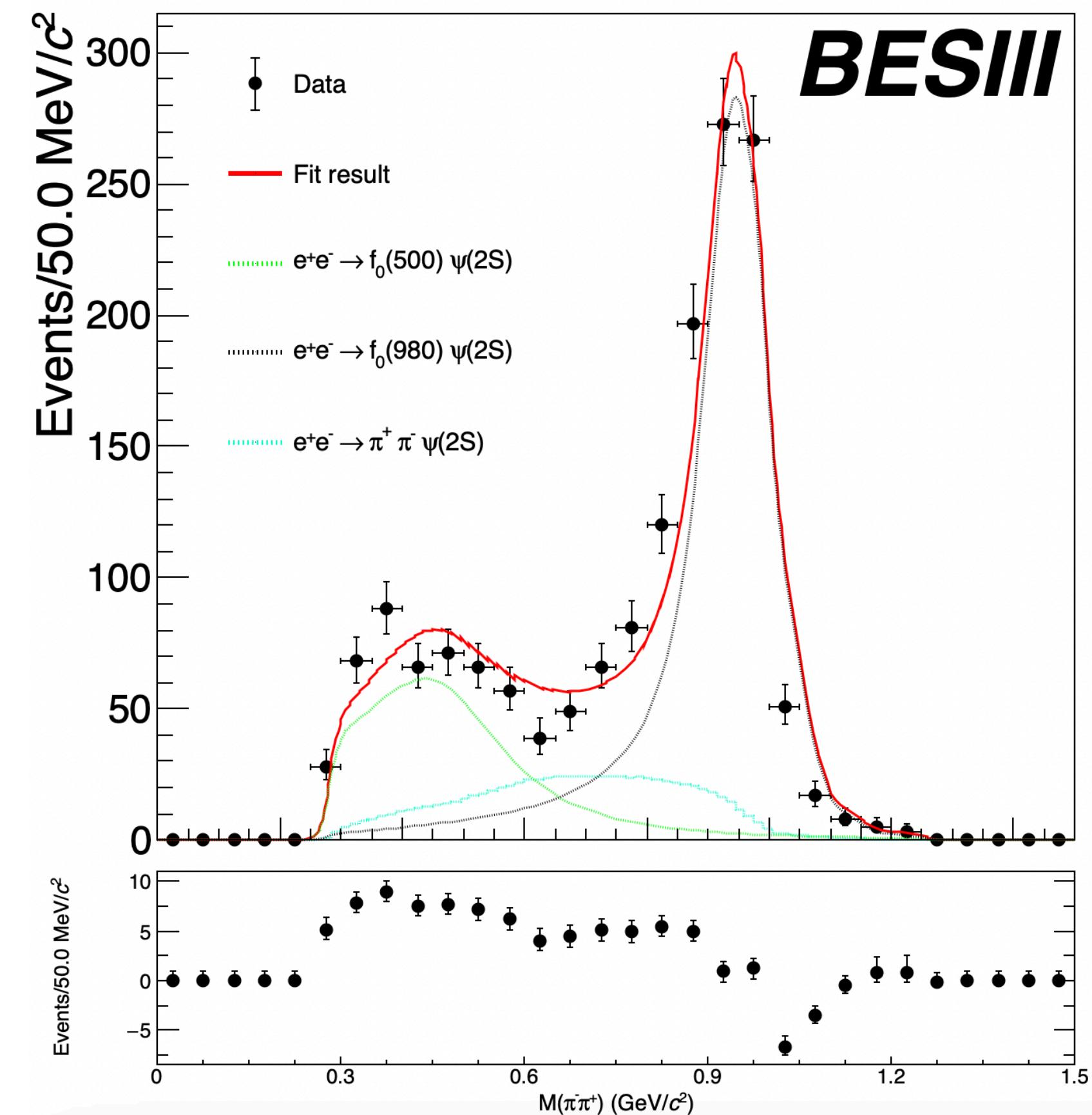


Analysis of the $\pi^\pm\psi(2S)$ Invariant Mass and Search for the $Z_c(4430)^\pm$

Drawing from the $f_0(980)$ study,
the the **M($\pi\pi$)** and **M($\pi\psi(2S)$)**
invariant distributions are **fitted**
without $Z_c(4430)$ contribution

Adding $Z_c(4430)$ contribution does
not improve the fit significantly

	Value
$N(f_0(980))$	988 ± 29
$N(f_0(500))$	384 ± 29
N(PHSP)	248 ± 41



NB
Constrained to total number of events

Conclusions and Outlook

- ★ The results found in this analysis **confirm Ref.[11]** and clearly **highlight the f_0 contributions** to the $\pi^+\pi^-\Psi(2S)$ cross-section
- ★ A search for the $Z_c(4430)$ exotic state @ $\sqrt{s} < 4.7$ GeV is performed via the $e^+e^- \rightarrow \pi^+\pi^-\Psi(2S)$ reaction, but **no evident $Z_c(4430)$** is found

★ The $e^+e^- \rightarrow \pi^+\pi^-\Psi(2S)$ reaction is studied @ $\sqrt{s} > 4.7$ GeV and two different generators (ISR and VP corrections) are tested and found to be comparable

The $Z_c(4430)$ 2D-fit with all the datasets does not show any exotic contribution

MEMO is almost ready, with the caveat of the $Z_c(4430)$ fit to be finalised (i.e., Upper Limit)

**Thanks
for your
attention!**



Back-up Slides



DEC Cards

Z_cResonant

```
noPhotos  
Particle vpho 4.680 0  
  
Decay vpho  
 0.5000 dummy10_1 pi- PHSP;  
 0.5000 anti-dummy10_1 pi+ PHSP;  
Enddecay  
  
Decay dummy10_1  
 1.0000 pi+ psi(2S) PHSP;  
Enddecay  
  
Decay anti-dummy10_1  
 1.0000 pi- psi(2S) PHSP;  
Enddecay  
  
Decay psi(2S)  
 1.0000 J/psi pi+ pi- JPIPI;  
Enddecay  
  
Decay J/psi  
 0.5000 e+ e- PHOTOS VLL;  
 0.5000 mu+ mu- PHOTOS VLL;  
Enddecay  
  
End
```

Z_c(4430)
M_{Z_c} = 4478⁺¹⁵₋₁₈ MeV
σ_{Z_c} = 181 ± 31 MeV

Signal MC samples
300k events

BOSS Release
7.0.x

non-Resonant

```
Particle vpho 4.6812 0.0  
Decay vpho  
 1.0000 ConExc -2 100443 211 -211;  
Enddecay  
  
Decay vhdr  
 1.0000 psi(2S) pi+ pi- VVPIPI;  
Enddecay  
  
Decay psi(2S)  
1.000 J/psi pi+ pi- JPIPI;  
Enddecay  
  
Decay J/psi  
 0.5000 e+ e- PHOTOS VLL;  
 0.5000 mu+ mu- PHOTOS VLL;  
Enddecay  
  
End
```

Signal MC Studies

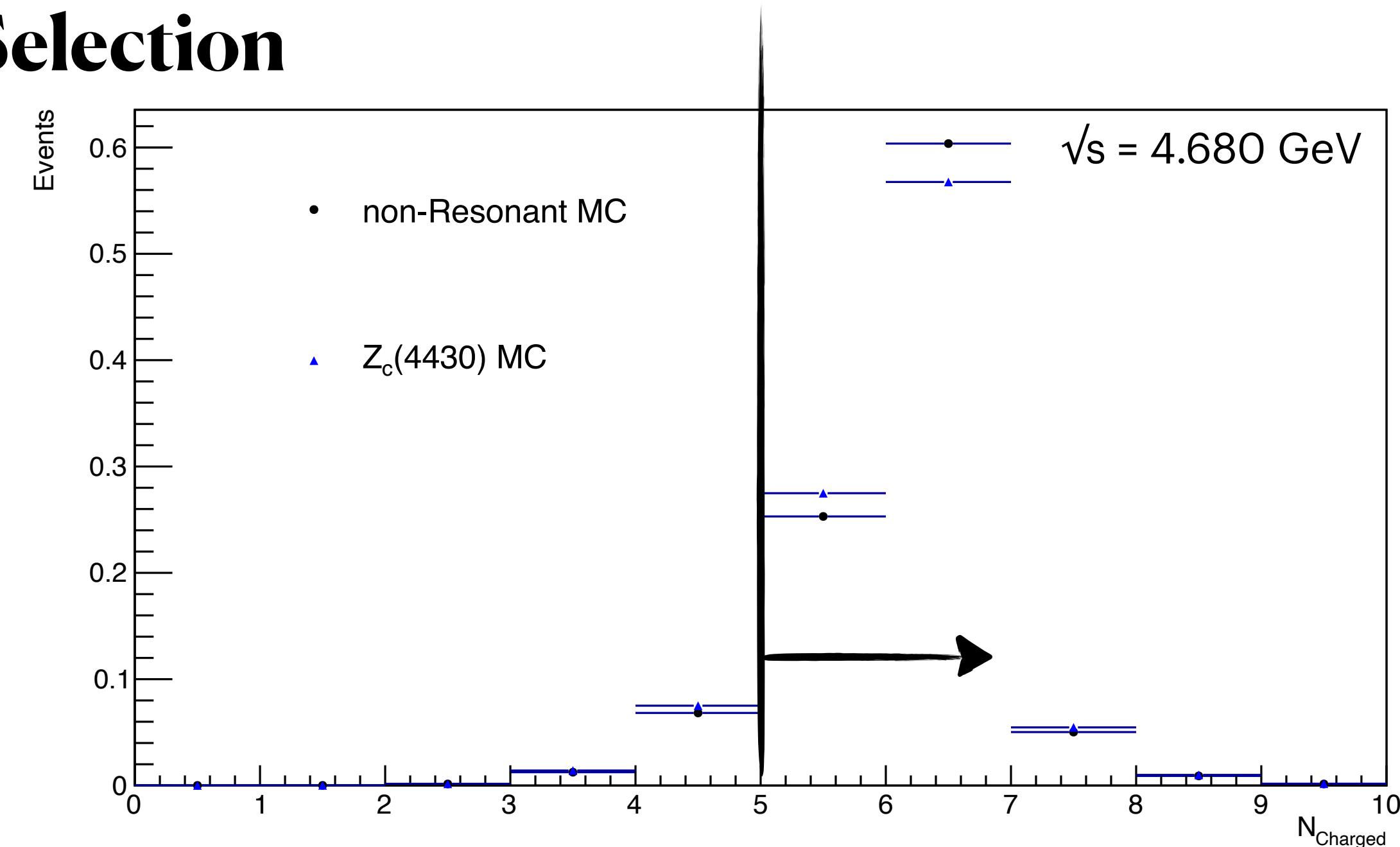
Signal MC sample
300k events

Event Selection

Goodness Cuts

Vertex: $R_{xy} < 1\text{cm}$ & $R_z < 10\text{ cm}$

Polar angle: $|\cos \theta| < 0.93$



Channel ID

charged tracks > 4

Signal MC Studies

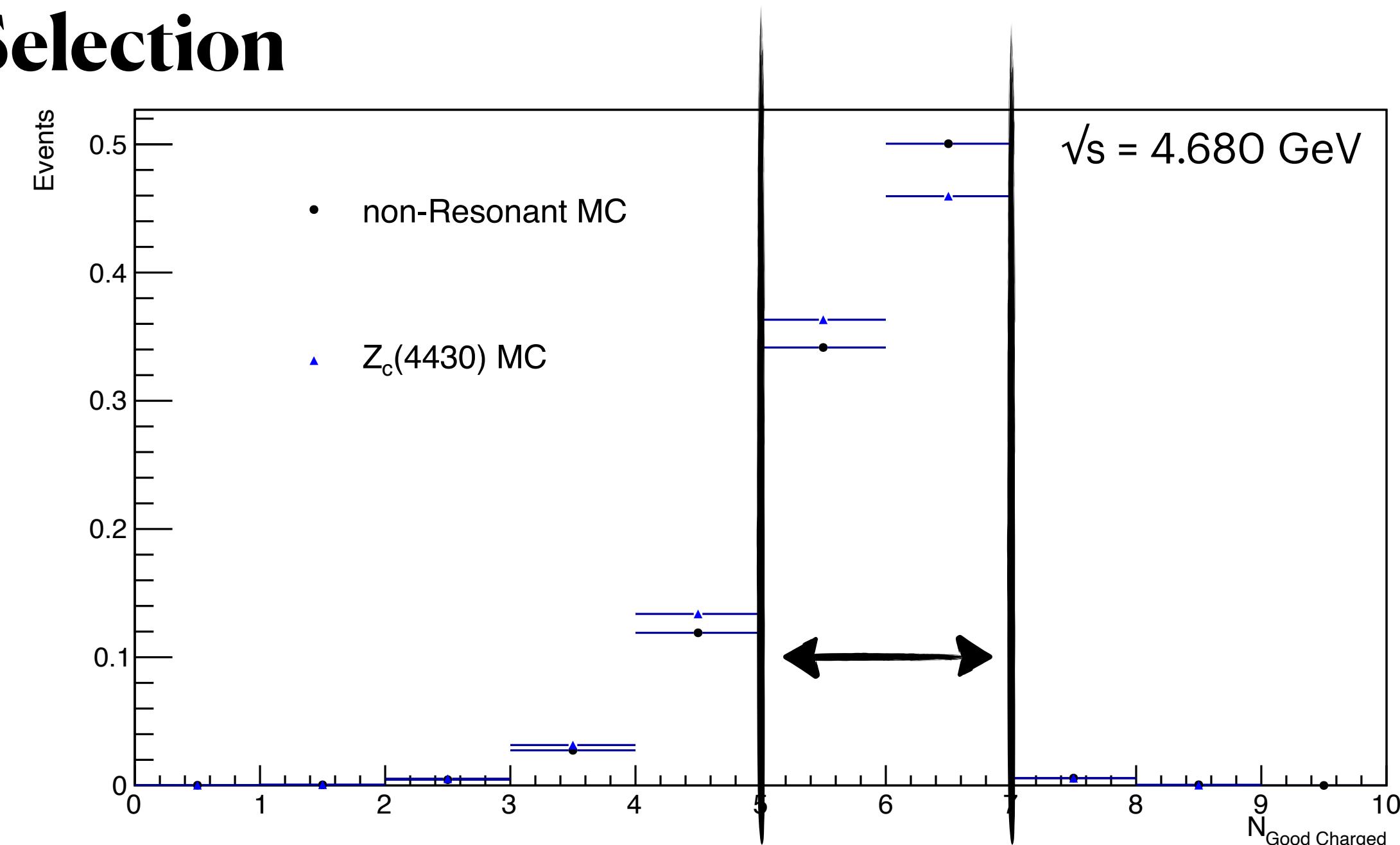
Signal MC sample
300k events

Event Selection

Goodness Cuts

Vertex: $R_{xy} < 1\text{cm}$ & $R_z < 10\text{ cm}$

Polar angle: $|\cos \theta| < 0.93$



Channel ID

charged tracks > 4

2 good charged topologies

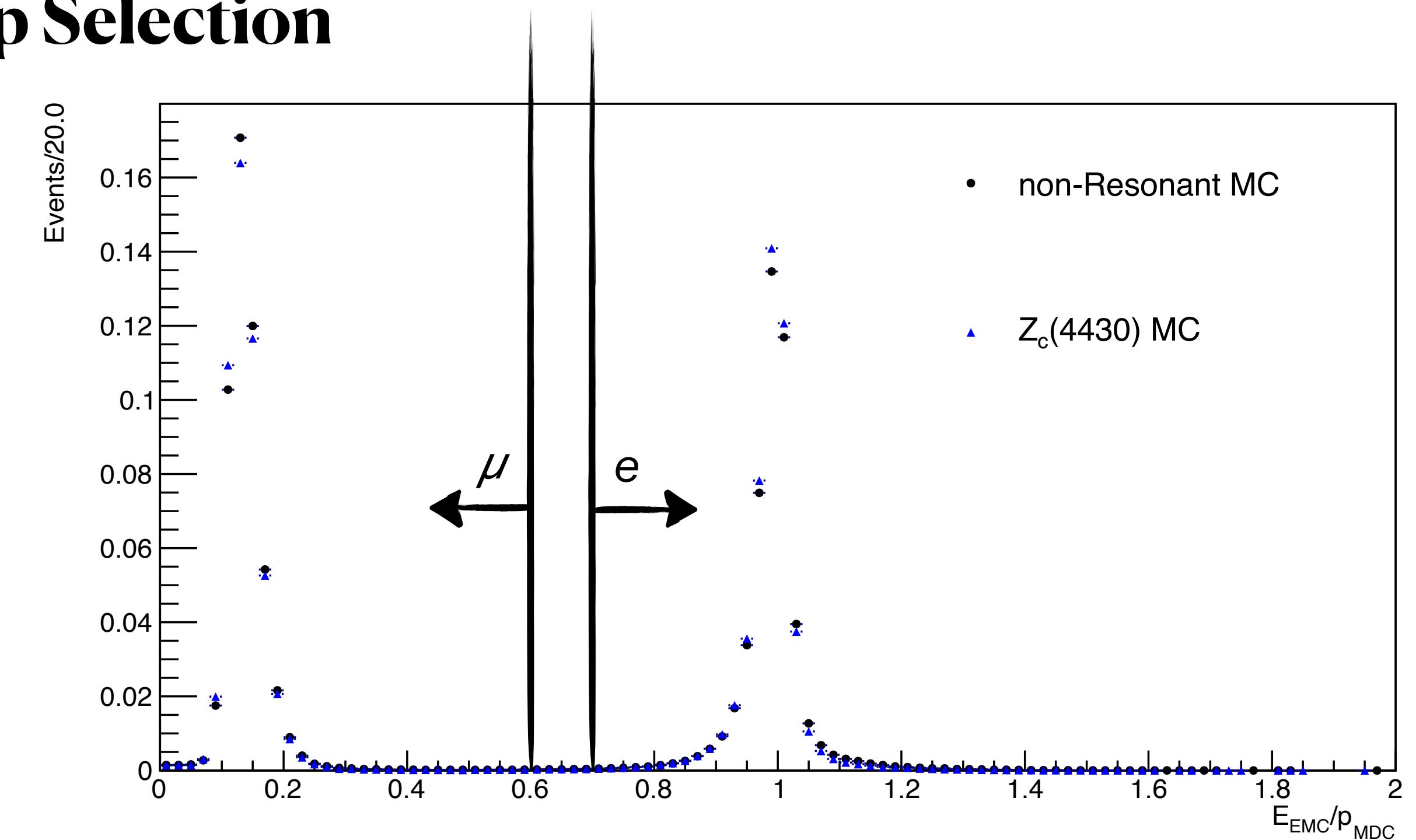
$2\ell 3\pi$

$2\ell 4\pi$

Signal MC Studies

Signal MC sample
300k events

E/p Selection



Goodness Cuts

Vertex: $R_{xy} < 1\text{cm}$ & $R_z < 10\text{ cm}$

Polar angle: $|\cos \theta| < 0.93$

Channel ID

charged tracks > 4

Leptons
 $p_T > 1\text{ GeV}$
 $E/p(e) > 0.7$
 $E/p(\mu) < 0.6$

Pions
 $p_T < 0.85\text{ GeV}$

2 good charged topologies
 $2\ell 3\pi$
 $2\ell 4\pi$

Signal MC Studies

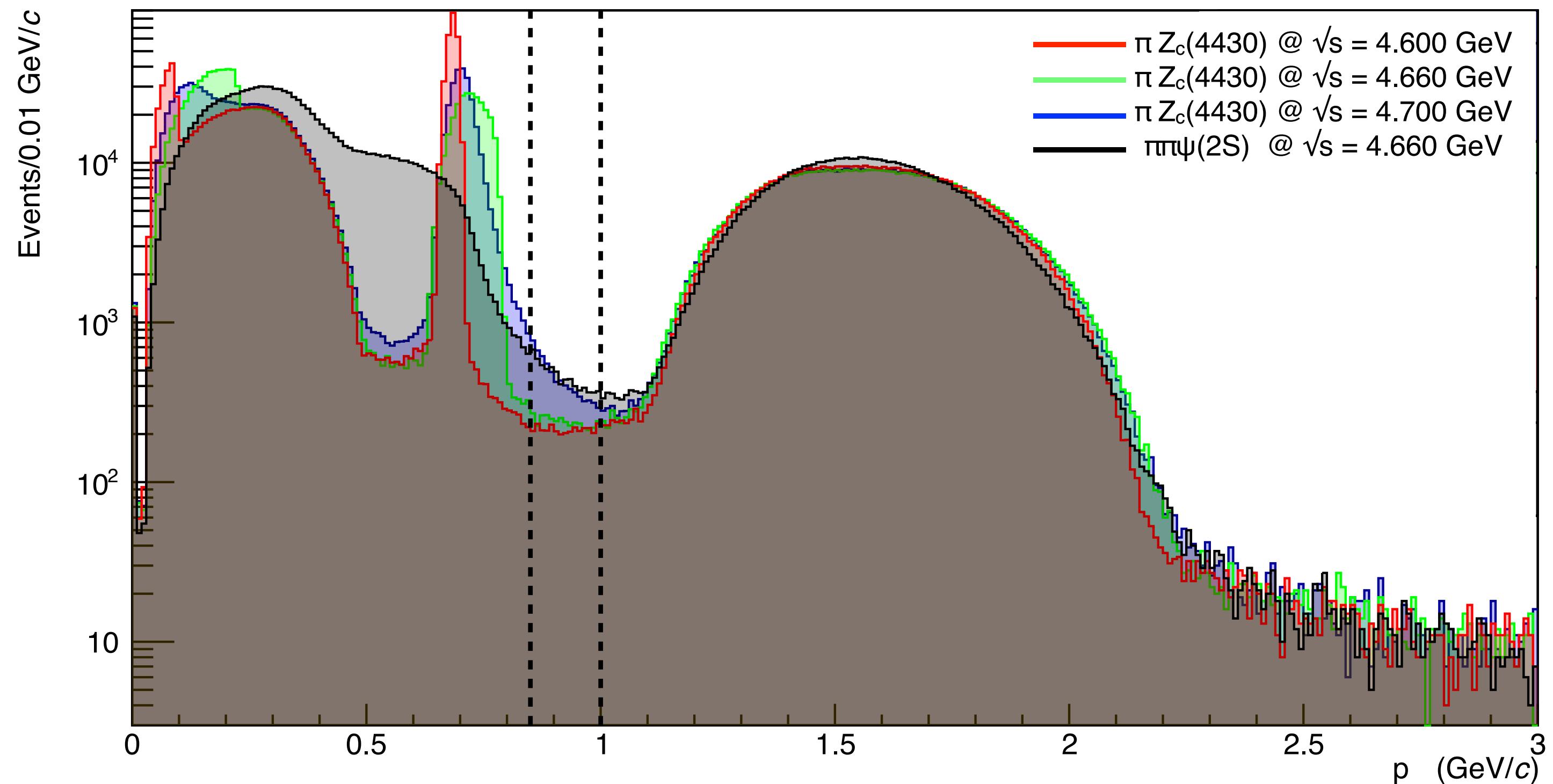
Charged Particles Momentum Comparison

Signal MC sample
300k events

Let's check it in more detail... the upper bound for p_π (< 0.85 GeV) can be improved?



$S(\text{Sig}_{\text{MC}} Z_c)/B(\text{Inc}_{\text{MC}})$ optimisation

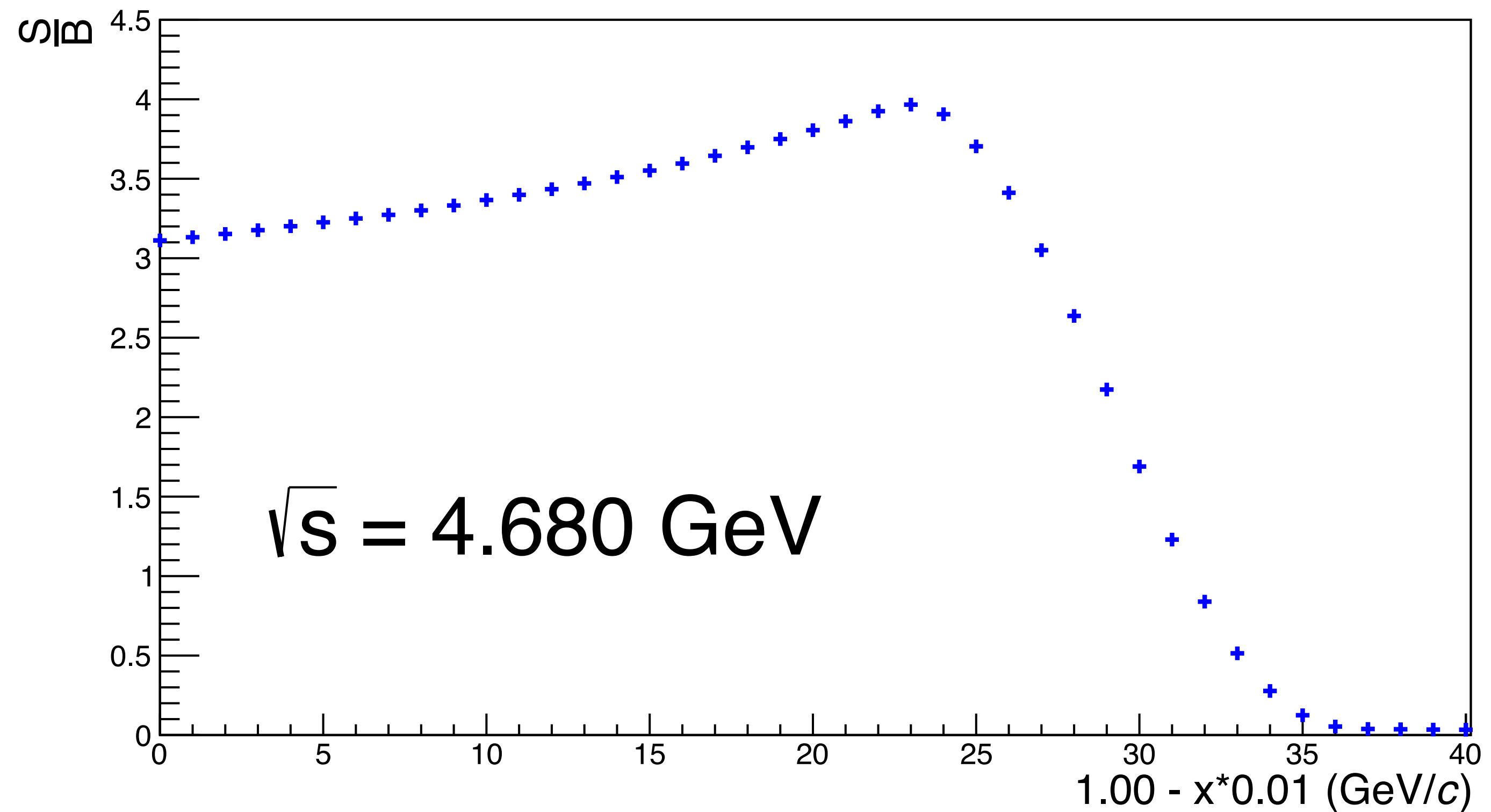


Event Selection

Charged Particles Momentum Optimisation

$S(\text{Sig}_{\text{MC}} Z_c)/B(\text{Inc}_{\text{MC}})$ optimisation
 $\forall \sqrt{s}$ and using only MC datasets

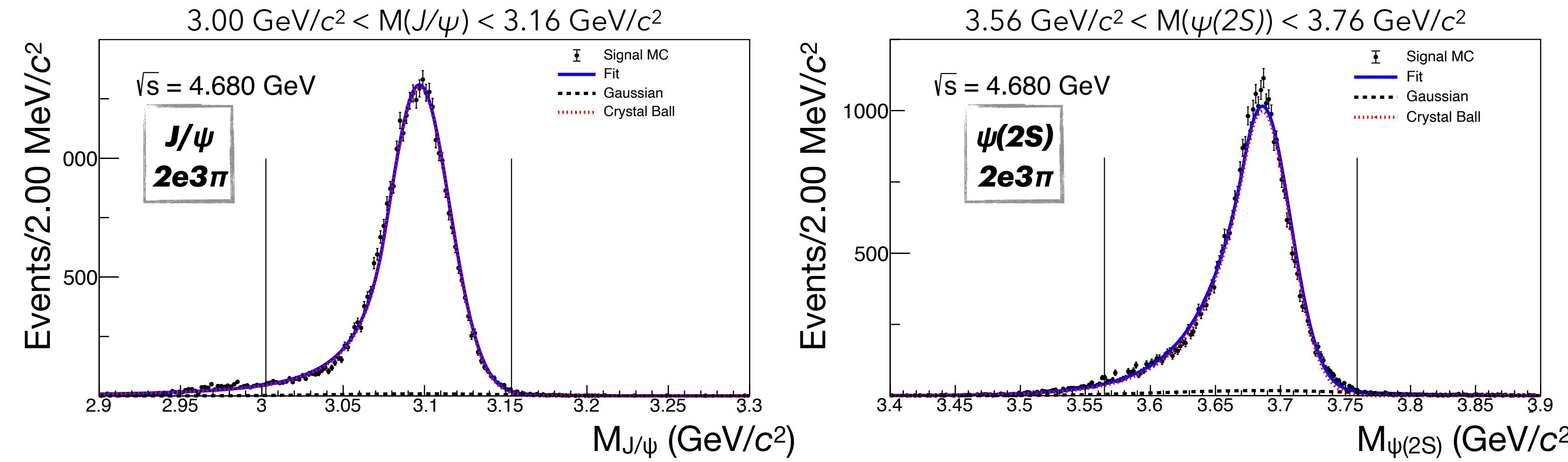
\sqrt{s}	p_{ch} [GeV/c]	\sqrt{s}	p_{ch} [GeV/c]
4.612	0.71	4.740	0.71
4.626	0.73	4.750	0.82
4.640	0.74	4.780	0.85
4.660	0.75	4.840	0.86
4.680	0.77	4.914	0.96
4.700	0.79	4.946	0.97



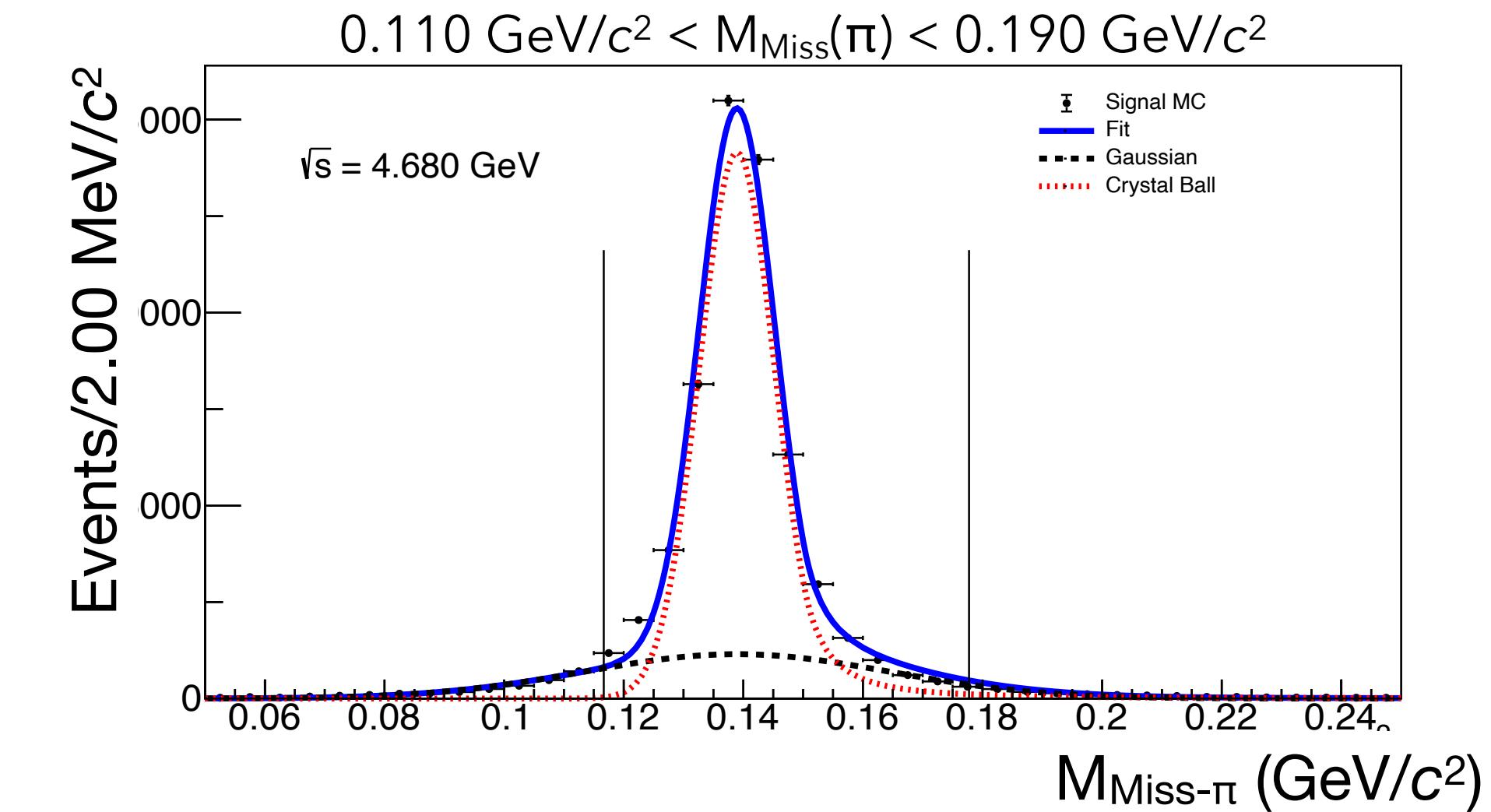
Event Selection

Signal Windows Definition

**Signal MC sample
300k Events**



An additional selection is applied on $M_{\text{Miss}}(\pi)$ for the $2\ell 3\pi$ topology



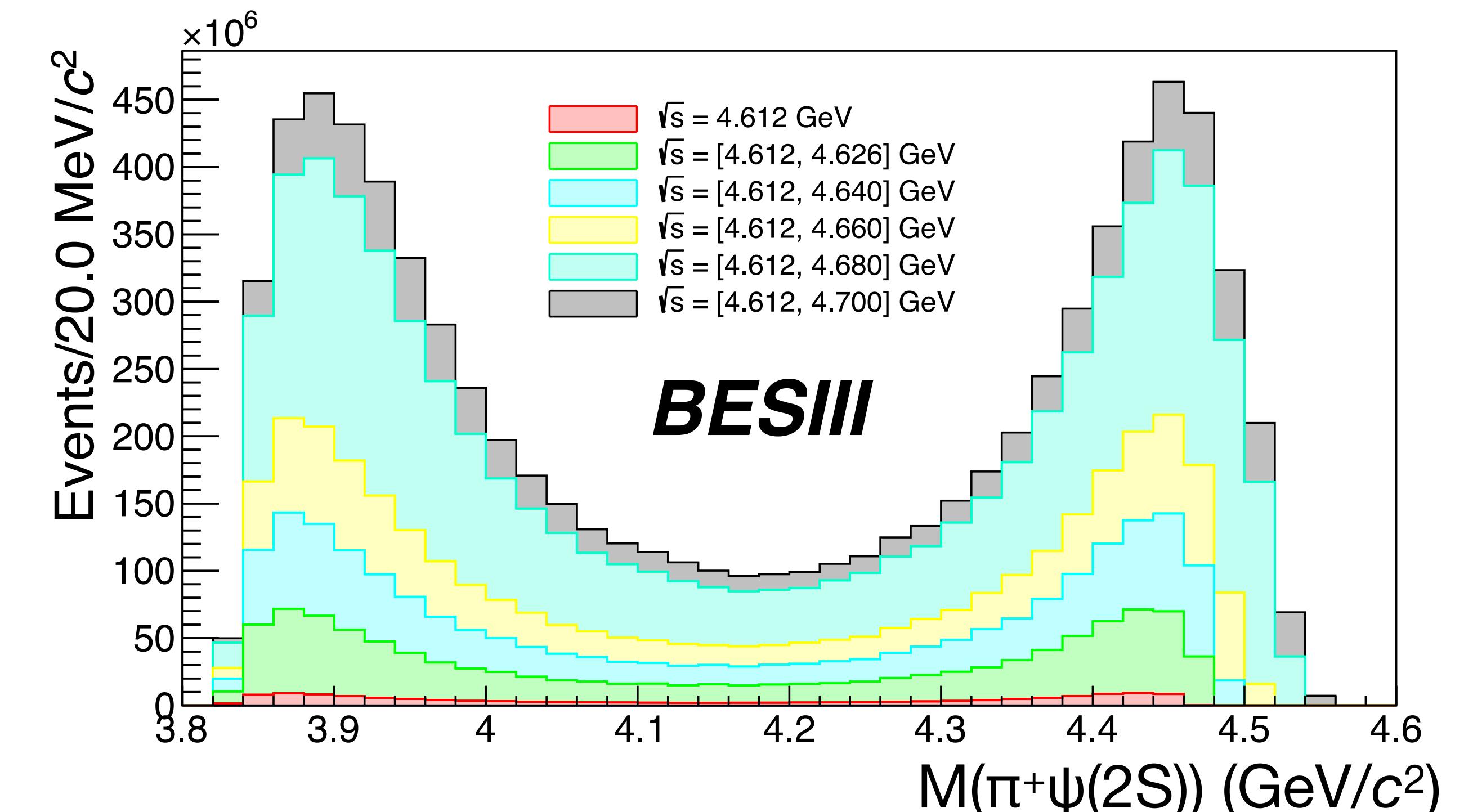
Selection performed on both the topologies on $M(J/\psi)$ and $M(\psi(2S))$

Analysis of the $\pi^\pm\psi(2S)$ Invariant Mass and Search for the $Z_c(4430)^\pm$

Signal MC Shape Extraction

Z_c Signal MC sample
300k events

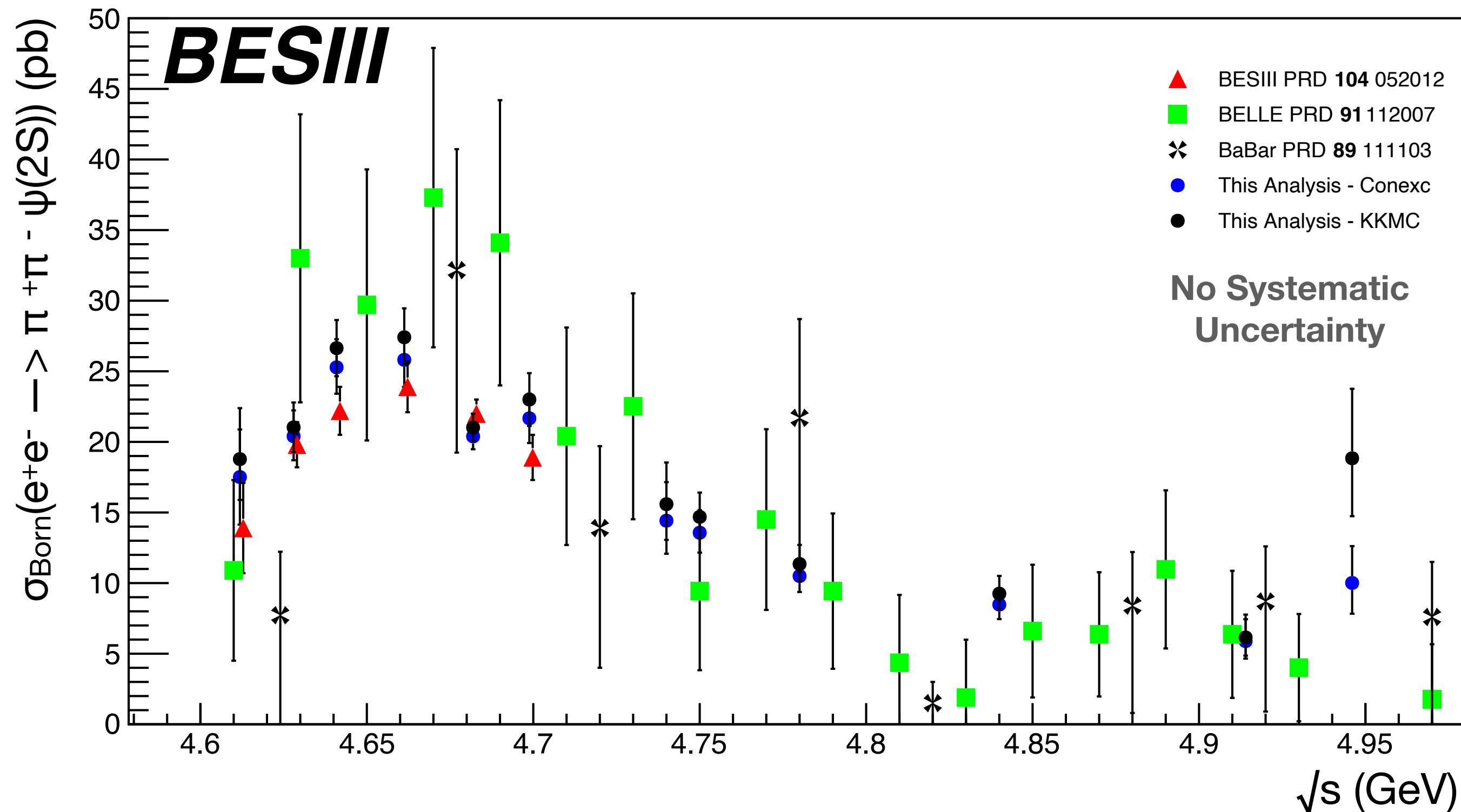
\sqrt{s} [GeV]	$W_{\text{Normalised}} = (\sigma \times \mathcal{L}) / (\sigma \times \mathcal{L}) _{4.680}$	Resolution [MeV/c ²]
4.612	0.04	—
4.626	0.28	2.33
4.640	0.32	0.77
4.660	0.35	0.69
4.680	1.00	0.67
4.700	0.27	0.74



Signal function
MC Signal Shape

Extraction of the $\sigma(e^+e^- \rightarrow \pi^+\pi^-\psi(2S))$

$\pi\pi\psi(2S)$ cross-section



$$\sigma_{\text{Born}} = \frac{N_{\text{Obs}}}{\mathcal{L}(1 + \delta) \frac{1}{|1 - \Pi^2|} \epsilon \mathcal{B}}$$

The observed **cross-section** is **compatible** with the previous result of **Ref. [11]**

Results from BELLE and BaBar are reported too, further **confirming the compatibility** of this thesis' results with the published literature

[11] Phys. Rev. D **104**, 052012

$\sigma(e^+e^- \rightarrow \pi^+\pi^-\psi(2S))$ vs $\sigma(f_0(980)\psi(2S))$

Number of Events

E_{CoM} (MeV)	$N_{e^+e^- \rightarrow \pi^+\pi^-\psi(2S)}$	$N_{e^+e^- \rightarrow f_0(980)\psi(2S)}$
4.612	26 ± 5	16 ± 4
4.626	156^{+14}_{-13}	107 ± 10
4.640	203^{+16}_{-15}	155 ± 11
4.660	202 ± 15	120 ± 10
4.680	518^{+24}_{-23}	337 ± 15
4.700	173 ± 14	120 ± 9
4.740	37^{+7}_{-6}	34 ± 4
4.750	77^{+9}_{-8}	63 ± 5
4.780	84^{+10}_{-9}	43 ± 7
4.840	66^{+9}_{-8}	43 ± 8
4.914	19^{+5}_{-4}	0 ± 2
4.946	23^{+6}_{-5}	0 ± 6

Systematic Uncertainties on the Cross-sections

$\pi\pi\psi(2S)$ cross-section

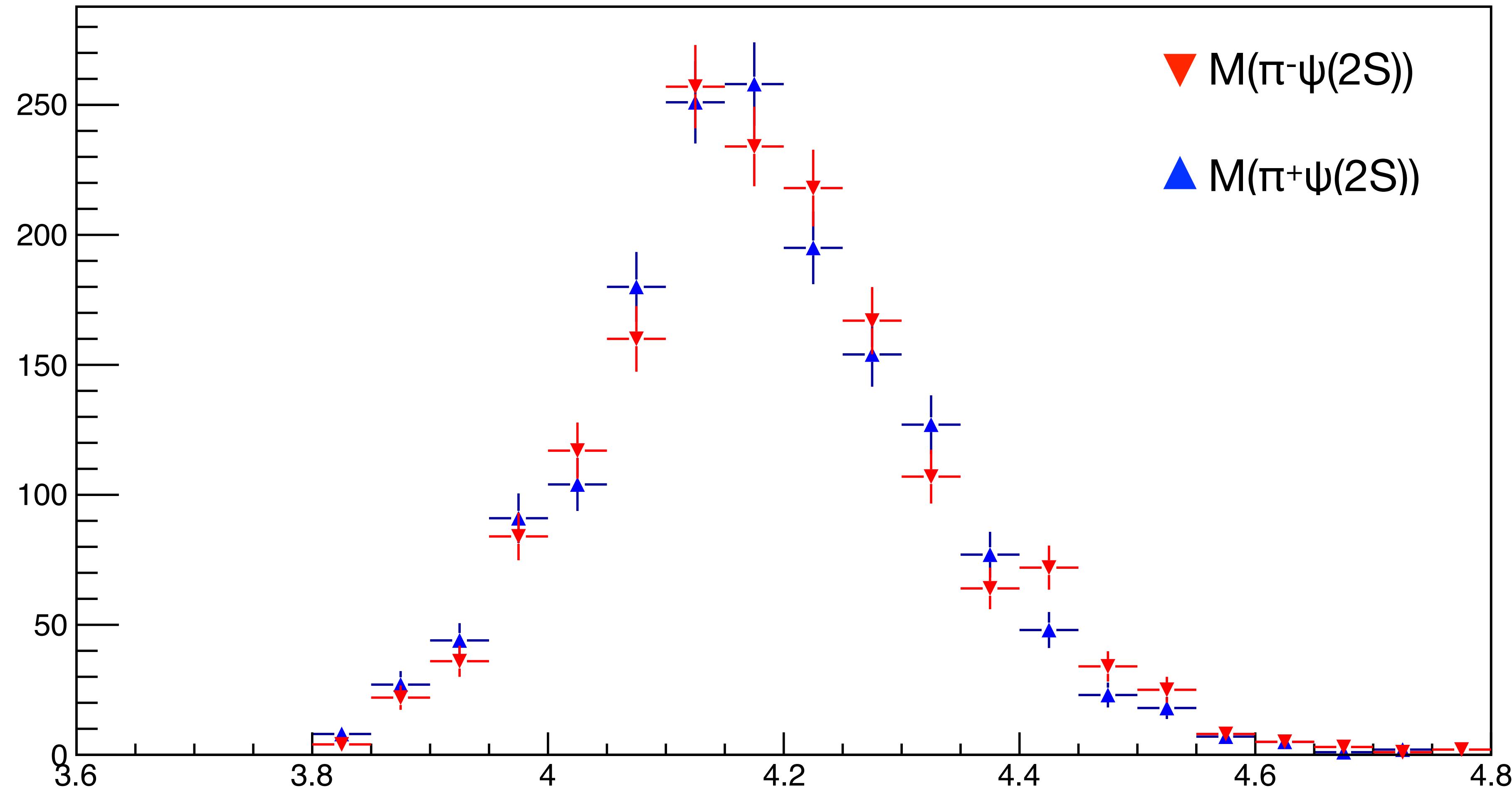
\sqrt{s} [GeV]	Lumi.	Vacuum Polarization	ISR Corrections	Tracking Efficiency	Other Sources	Final States \mathcal{B}	Total
4.612	0.18	0.09	0.00	0.61	0.18	0.16	0.68
4.626	0.20	0.10	0.00	0.71	0.20	0.18	0.80
4.640	0.25	0.13	0.00	0.88	0.25	0.22	0.99
4.660	0.26	0.13	0.00	0.90	0.26	0.23	1.01
4.680	0.20	0.10	0.02	0.71	0.20	0.19	0.80
4.700	0.22	0.11	0.07	0.76	0.22	0.20	0.85
4.740	0.14	0.07	0.03	0.50	0.14	0.15	0.57
4.750	0.14	0.07	0.01	0.47	0.14	0.14	0.54
4.780	0.10	0.05	0.01	0.37	0.10	0.12	0.42
4.840	0.08	0.04	0.01	0.30	0.08	0.10	0.34
4.914	0.06	0.03	0.01	0.21	0.06	0.07	0.24
4.946	0.10	0.05	0.00	0.35	0.10	0.10	0.39

Systematic Uncertainties on the Cross-sections

$f_0(980)\psi(2S)$ cross-section

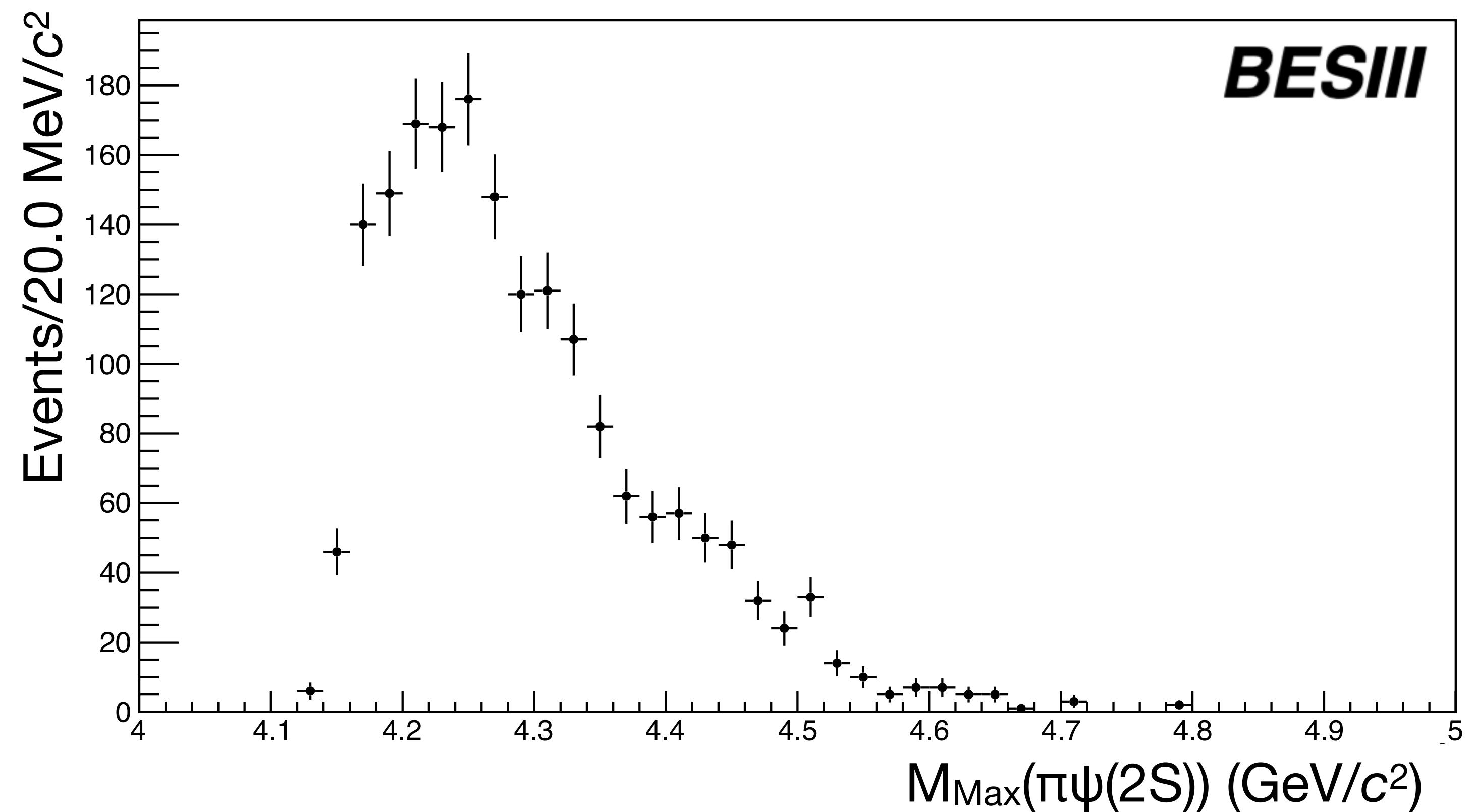
\sqrt{s} [GeV]	Lumi.	Vacuum Polarization	ISR Corrections	Tracking Efficiency	Other Sources	Final States \mathcal{B}	Total
4.612	0.02	0.01	0.00	0.08	0.02	0.02	0.09
4.626	0.15	0.08	0.00	0.53	0.15	0.10	0.58
4.640	0.19	0.10	0.00	0.68	0.19	0.14	0.75
4.660	0.15	0.07	0.01	0.52	0.15	0.12	0.58
4.680	0.14	0.07	0.01	0.47	0.14	0.11	0.53
4.700	0.15	0.08	0.00	0.53	0.15	0.12	0.59
4.740	0.14	0.07	0.00	0.49	0.14	0.12	0.54
4.750	0.11	0.06	0.02	0.39	0.11	0.10	0.43
4.780	0.05	0.03	0.00	0.18	0.05	0.06	0.21
4.840	0.06	0.03	0.00	0.19	0.06	0.05	0.22

$M(\pi^\pm\psi(2S))$ Comparison



Analysis of the $\pi^\pm\psi(2S)$ Invariant Mass and Search for the $Z_c(4430)^\pm$

Instead of looking at the whole $\pi\psi(2S)$ mass spectrum, could be worthwhile to check the $M_{Max}(\pi\psi(2S))$ as it was done for the $Z_c(3900)$



Analysis of the $\pi^\pm\psi(2S)$ Invariant Mass and Search for the $Z_c(4430)^\pm$

Drawing from the **$f_0(980)$** study,
the the $M(\pi\pi)$ and $M(\pi\psi(2S))$
invariant distributions are fitted

Fit is again inconclusive...
parameters have $\sim 100\%$
uncertainties

