

Hadronic contribution to to the muon $g - 2$: theoretical challenges with the MUonE experiment

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QCD@Work, Trani, 18-21 June 2024

$$\vec{\mu}_\mu = -g_\mu \frac{e\hbar}{2m_\mu} \vec{s}$$

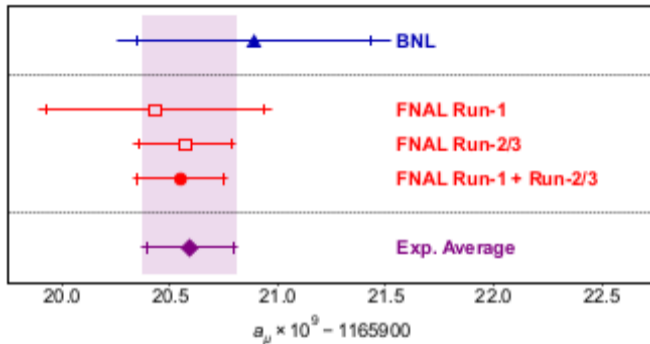
- in QED without quantum fluctuations

$$g_\mu = 2$$

- with quantum fluctuations: $g_\mu \neq 2$ at the 0.1% level

$$\mathbf{a}_\mu \equiv \frac{\mathbf{g}_\mu - 2}{2}$$

Experimental status



Muon $g - 2$ Coll., Phys. Rev. Lett. 126 (2021) 120801; Phys. Rev. Lett. 131 (2023) 161802; arXiv:2402.15410

present world average: $a_\mu^{\text{exp}} = 116592059(22) \cdot 10^{-11}$ (0.19 ppm)

M. Knecht, MITP Workshop 3-7/06/2024

$\Rightarrow \sim 0.14$ ppm in the (very) near future

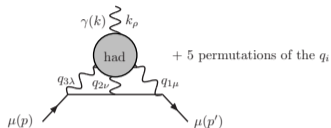
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- **QCD**: the largest source of uncertainty, due to non-perturbative effects

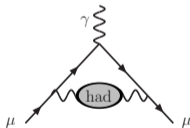
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- **QCD**: the largest source of uncertainty, due to non-perturbative effects
- **possible New Physics?**

- Hadronic Light-by-Light (HLxL)



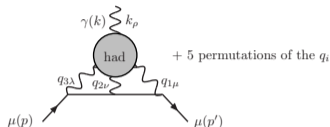
F. Jegerlehner, arXiv:0902.3360

- Hadronic Vacuum Polarization (HVP)



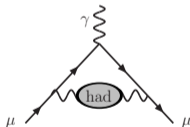
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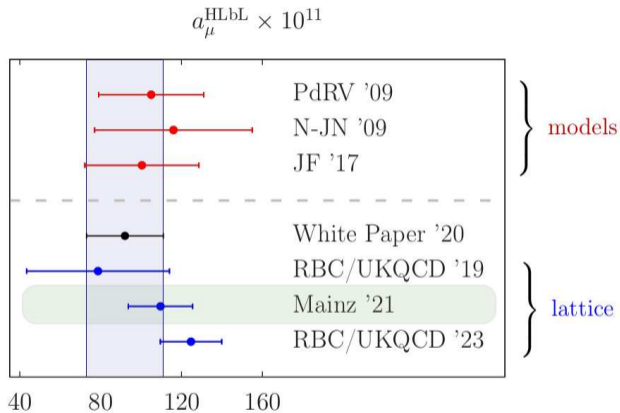


F. Jegerlehner, arXiv:0902.3360

- **two approaches for both contributions:**

- first principle calculations with LQCD
- dispersion relations

HLxL estimates



M. Knecht, MITP Workshop 3-7/06/2024

$$a_{\mu}^{\text{HLxL}} = 91(19) \cdot 10^{-11} \text{ (WP 2020) T. Aoyama et al., Phys. Rept. 887 (2020) 1}$$

The dispersive approach for HVP in a nutshell

$$a_{\mu}^{\text{HLO}} = \left(\frac{\alpha m_{\mu}}{3\pi}\right)^2 \int_{m_{\pi}^2}^{\infty} ds \frac{K(s)R(s)}{s^2}$$

$$K(s) = \int_0^1 dx \frac{x^2(1-x)}{x^2 + (1-x)(s/m_{\mu}^2)}$$

$$R(s) = \frac{\sigma^0(e^+e^- \rightarrow \text{hadrons} + \gamma)}{\sigma_{\text{pt}}}$$

$$\sigma_{\text{pt}} = \frac{4\pi\alpha^2}{3s}$$

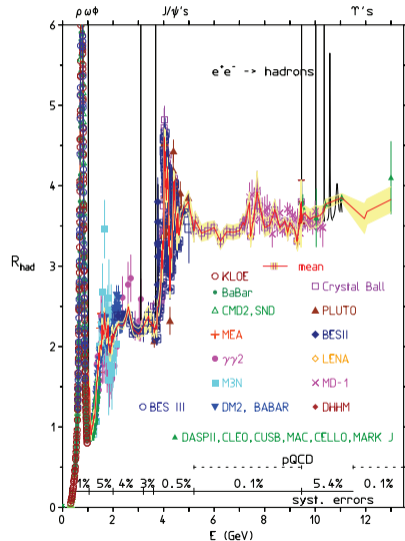
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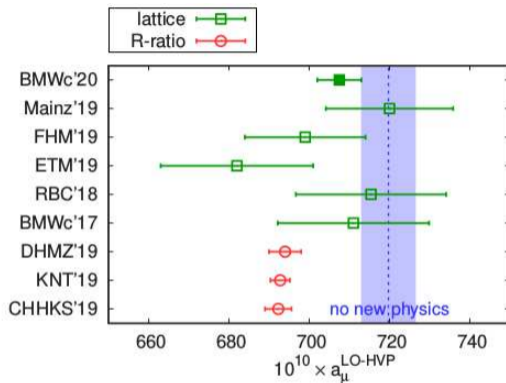
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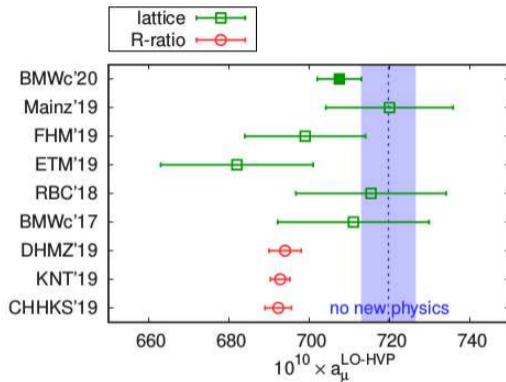
$$\sigma_{\text{pt}} = \frac{4\pi\alpha^2}{3s}$$





M. Knecht, MITP Workshop 3-7/06/2024

$$a_{\mu}^{\text{HVP-LO}} = 6931(40) \cdot 10^{-11} \text{ (WP 2020, without BMWc) } \quad \text{T. Aoyama et al., Phys. Rept. 887 (2020) 1}$$



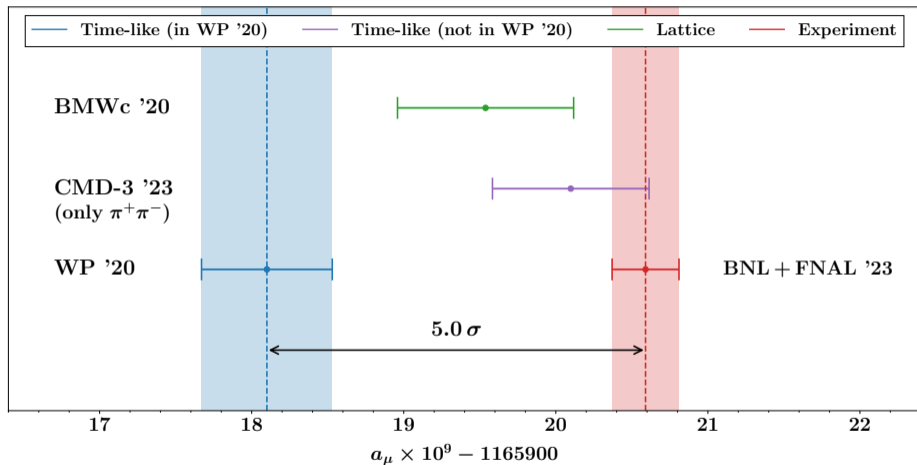
M. Knecht, MITP Workshop 3-7/06/2024

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- the new CMD-3 result on pion form-factor introduced an additional puzzle

F.V. Ignatov et al, arXiv:2302.08834

Summary of the comparison data-theory



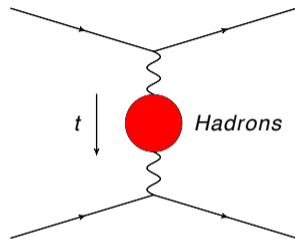
courtesy of A. Gurgone



- ★ G. Abbiendi, C.M. Carloni Calame, U. Marconi, C. Matteuzzi, G. Montagna, O. Nicosini, M. Passera, F. Piccinini, R. Tenchini, L. Trentadue, G. Venanzoni,
Measuring the leading hadronic contribution to the muon $g-2$ via μe scattering
Eur. Phys. J. C **77** (2017) no.3, 139 - arXiv:1609.08987 [hep-ph]
- ★ C. M. Carloni Calame, M. Passera, L. Trentadue and G. Venanzoni,
A new approach to evaluate the leading hadronic corrections to the muon $g-2$
Phys. Lett. B **746** (2015) 325 - arXiv:1504.02228 [hep-ph]

$$a_{\mu}^{\text{HLO}} = \frac{\alpha}{\pi} \int_0^1 dx (1-x) \Delta\alpha_{\text{had}}[t(x)]$$
$$t(x) = \frac{x^2 m_{\mu}^2}{x-1} < 0$$

e.g. Lautrup, Peterman, De Rafael, Phys. Rept. 3 (1972) 193



- ★ $\Delta\alpha_{\text{had}}(t)$ can be directly measured in a (single) experiment involving a space-like scattering process and a_{μ}^{HLO} obtained through numerical integration

Carlioni Calame, Passera, Trentadue, Venanzoni PLB 746 (2015) 325

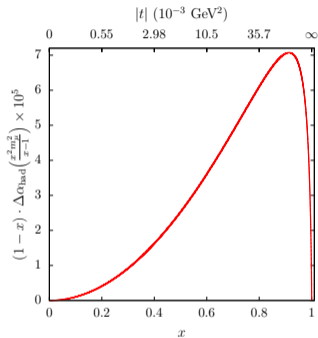
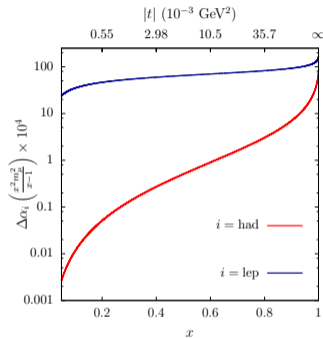
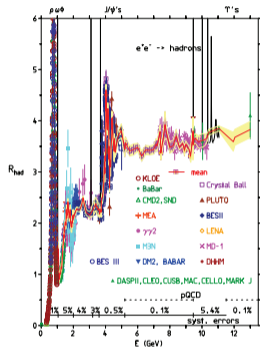
- ★ A data-driven, inclusive evaluation of a_{μ}^{HLO} , but with **space-like data**

From time-like to space-like evaluation of a_μ^{HLO}

Time-like



Space-like



Smooth function

→ **Time-like:** combination of many experimental data sets, control of RCs better than $\mathcal{O}(1\%)$ on hadronic channels required

→ **Space-like:** in principle, one single experiment, *it's a one-loop effect, very high accuracy needed*

Main challenge: precision on shapes of differential distributions at the 10ppm level

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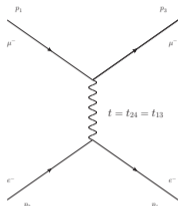
- **Radiative corrections to the signal**
- **Predictions for Background processes**

Main challenge: precision on shapes of differential distributions at the 10ppm level

Main sources of systematics on the theory side

- **Radiative corrections to the signal**
- **Predictions for Background processes**

High precision Monte Carlo simulation tools required



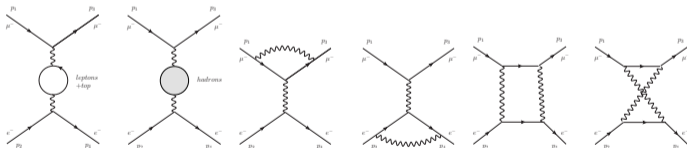
- analytical expression for tree level

$$\frac{d\sigma}{dt} = \frac{4\pi\alpha^2}{\lambda(s, m_\mu^2, m_e^2)} \left[\frac{(s - m_\mu^2 - m_e^2)^2}{t^2} + \frac{s}{t} + \frac{1}{2} \right]$$

- VP gauge invariant subset of NLO rad. corr.

- factorized over tree-level: $\alpha \rightarrow \alpha(t)$

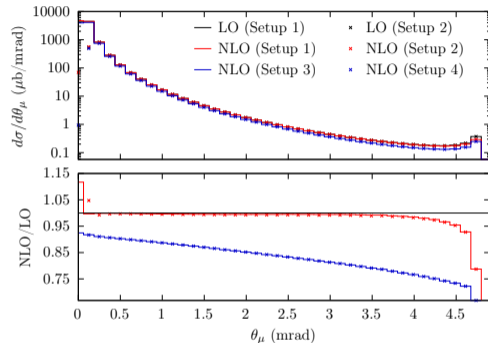
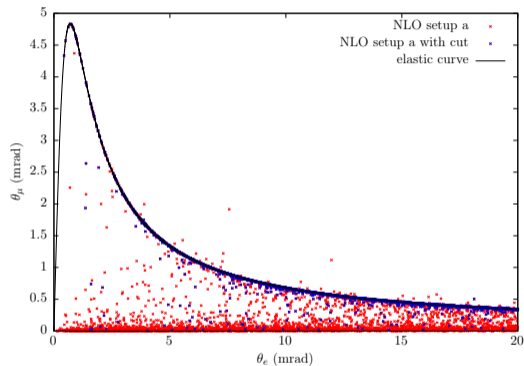
- QED NLO virtual diagrams and real emission diagrams with exact finite m_e and m_μ effects



- tree-level **Z-exchange important** at the 10^{-5} level ($\sim tG_\mu/4\pi\alpha\sqrt{2}$ in the Fermi theory)

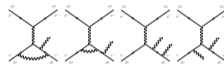
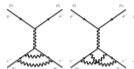
- SM weak RCs at most at a few 10^{-6} level, negligible

First realistic description of scattering events



- many points fall out of the $2 \rightarrow 2$ correlation curve $\theta_\mu - \theta_e$ because of the radiative events
- NLO QED radiative corrections at the % level, enhanced by exclusive event selections

- exact calculation of corrections along one lepton line with all finite mass effects



- two independent calculations, with different IR singularities handling procedures (slicing and subtraction)

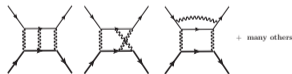
Carloni Calame et al., JHEP 11 (2020) 028,

P. Banerjee, T. Engel, A. Signer, Y. Ulrich, SciPost Phys. 9 (2020) 027

- implemented in **Mesmer** and **McMuLe**, perfect numerical agreement

- NNLO with finite mass effects and approximate up-down interference in Mesmer**

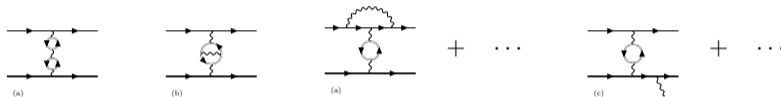
- interference of LO $\mu e \rightarrow \mu e$ amplitude with



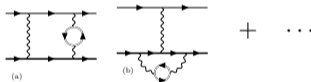
- ↪ NNLO double-virtual amplitudes where at least 2 photons connect the e and μ lines are approximated according to the Yennie-Frautschi-Suura ('61) formalism to catch the IR divergent structure

- **complete calculation of the amplitude** $f^+ f^- \rightarrow F^+ F^-$ **with** $m_f = 0, m_F \neq 0$ R. Bonciani et al., PRL 128 (2022)
- “**massification**” to recover the leading m_e terms, i.e. neglecting powers of m_e^2/Q^2
T. Engel, C. Grendiger, A. Signer and Y. Ulrich, JHEP 02 (2019) 118
Y. Ulrich, PoS RADCOR2023 (2024) 077
- **FKS^ℓ subtraction scheme**
T. Engel, A. Signer, Y. Ulrich, JHEP 01 (2020) 085
- **Next-to-soft stabilisation**, to obtain numerical stability in real-virtual corrections with soft and/or collinear photon configurations
T. Engel, A. Signer, Y. Ulrich, JHEP 04 (2022) 097; T. Engel, JHEP 07 (2023) 177
- with the above ingredients
 - **NNLO calculation neglecting terms of $\mathcal{O}(m_e^2/Q^2)$ in McMuLe**
A. Broggio et al., JHEP 01 (2023) 112

- any lepton (and hadron) in the VP blobs
- interfered with $\mu e \rightarrow \mu e$ or $\mu e \rightarrow \mu e \gamma$ amplitudes



- interfered with $\mu e \rightarrow \mu e$ amplitude



- 2-loop integral evaluated with **dispersion relation techniques** in **Mesmer**

used e.g. in the past for Bhabha: Actis et al., Phys. Rev. Lett. 100 (2008) 131602; Carloni Calame et al., JHEP 07 (2011) 126

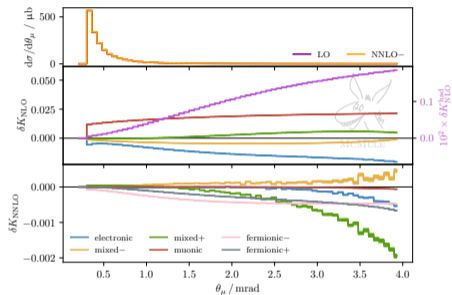
$$\frac{g_{\mu\nu}}{q^2 + i\epsilon} \rightarrow g_{\mu\nu} \frac{\alpha}{3\pi} \int_{4m_\ell^2}^{\infty} \frac{dz}{z} \frac{R_\ell(z)}{q^2 - z + i\epsilon} = g_{\mu\nu} \frac{\alpha}{3\pi} \int_{4m_\ell^2}^{\infty} \frac{dz}{z} \frac{1}{q^2 - z + i\epsilon} \left(1 + \frac{4m_\ell^2}{2z}\right) \sqrt{1 - \frac{4m_\ell^2}{z}}$$

- 2-loop integral evaluated (also) with **hyperspherical method** in **McMule**

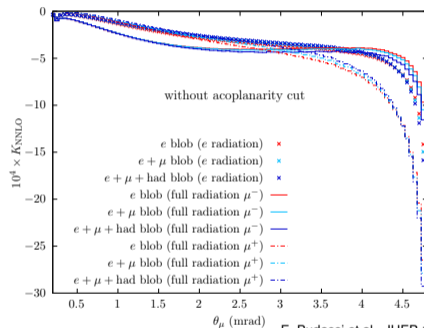
M. Fael, JHEP02 (2019) 027

NNLO order of magnitude

McMule



Mesmer

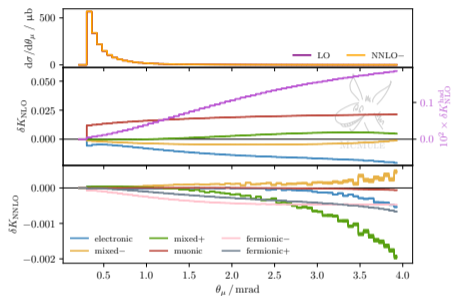


E. Budassi et al., JHEP 11 (2021) 098

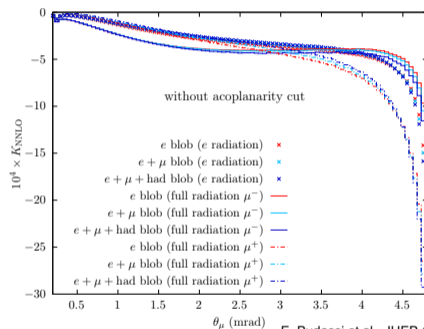
A. Broggio et al., JHEP 01 (2023) 112

- **NNLO corrections at the $10^{-4} - 10^{-3}$ level**

McMule



Mesmer

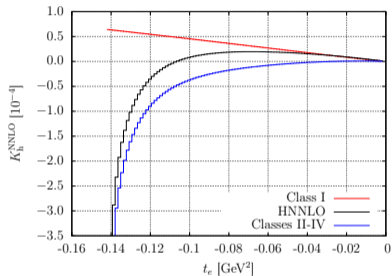
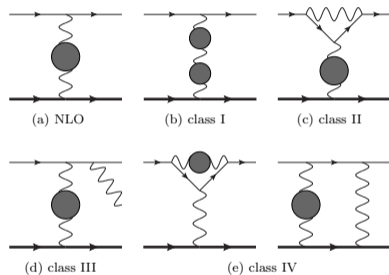


E. Budassi et al., JHEP 11 (2021) 098

A. Broggio et al., JHEP 01 (2023) 112

- **NNLO corrections at the $10^{-4} - 10^{-3}$ level**
- **eventually fixed order calculations need to be matched to resummation of higher order corrections, through PS techniques (e.g. BaBaYaga) or YFS techniques (e.g. KKMC/SHERPA)**

- using the dispersion relation approach

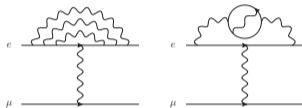


Fael, Passera, Phys. Rev. Lett. 122 (2019) 192001

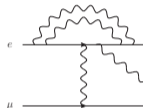
- corrections of the order of 10^{-4}
- hyperspherical integration method to calculate hadronic NNLO corrections, where the hadronic vacuum polarization is employed in the space-like region (used in **McMuLe**)

M. Fael, JHEP02 (2019) 027

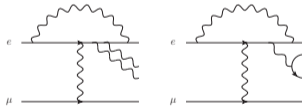
- All virtual (three loops)



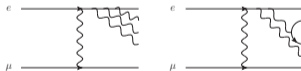
- Single real emission (two loops)



- Double real emission (one loops)



- Triple real



- **this contribution will allow improved perturbative predictions and more reliable theoretical uncertainty estimates**

- **the three-loop form factor with finite fermion mass is now available**

M. Fael, F. Lange, K. Schönwald, M. Steinhauser, Phys. Rev. Lett 128 (2022) 172003

M. Fael, F. Lange, K. Schönwald, M. Steinhauser, Phys. Rev.D 106 (2022) 034029

M. Fael, F. Lange, K. Schönwald, M. Steinhauser, Phys. Rev.D 107 (2023) 094017

- **All order subtraction scheme FKS^ℓ available**

T. Engel, A. Signer, Y. Ulrich, JHEP 01 (2020) 085

- **very recent generalisation of the LBK theorem to multi-photon emission \implies extension of next-to-soft stabilisation to multiple radiation**

T. Engel, JHEP 03 (2024) 004

- **real-virtual-virtual corrections recently recalculated with $m_e \rightarrow 0$**

S. Badger, J. Kryś, R. Moodle, S. Zoia, JHEP 11 (2023) 041

V.S. Fadin, R.N. Lee, JHEP 11 (2023) 148

Fixed target experiment \Rightarrow bound electron effects

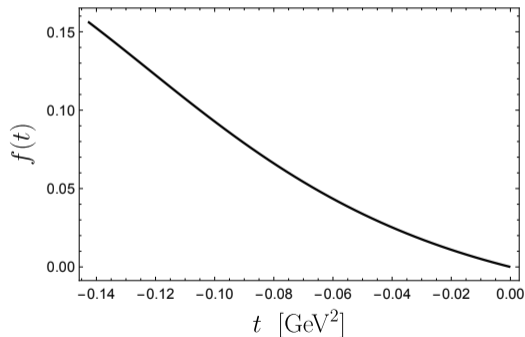
- **very recently estimated**

R. Plestid and M.B. Wise, arXiv:2403.12184

- for C

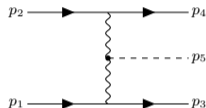
$$\frac{1}{\sigma} \frac{d\sigma}{dt} = \frac{1}{\sigma^0} \frac{d\sigma^0}{dt} (1 - K f(t))$$

- $K = 4.5 \cdot 10^{-4}$, scaling as $1/Z_A$



Backgrounds

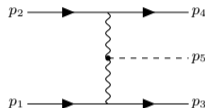
- **pion pair production forbidden** kinematically with the available \sqrt{s}
- **single π^0 production possible**



- π^0 **production** calculated and shown to be **well below** 10^{-5} w.r.t. $\mu e \rightarrow \mu e$

E. Budassi et al., PLB 829 (2022) 137138

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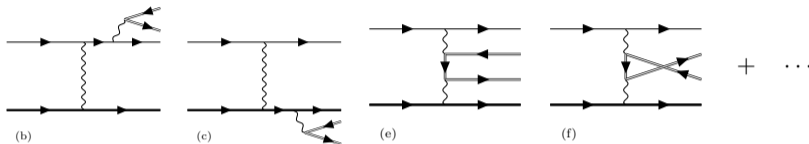
- π^0 **production** calculated and shown to be **well below** 10^{-5} w.r.t. $\mu e \rightarrow \mu e$

E. Budassi et al., PLB 829 (2022) 137138

- **lepton pair production**

- $\mu^\pm e^- \rightarrow \mu^\pm e^- \ell^+ \ell^-$
- $\mu^\pm N \rightarrow \mu^\pm N \ell^+ \ell^-$

- it also contributes at NNLO accuracy



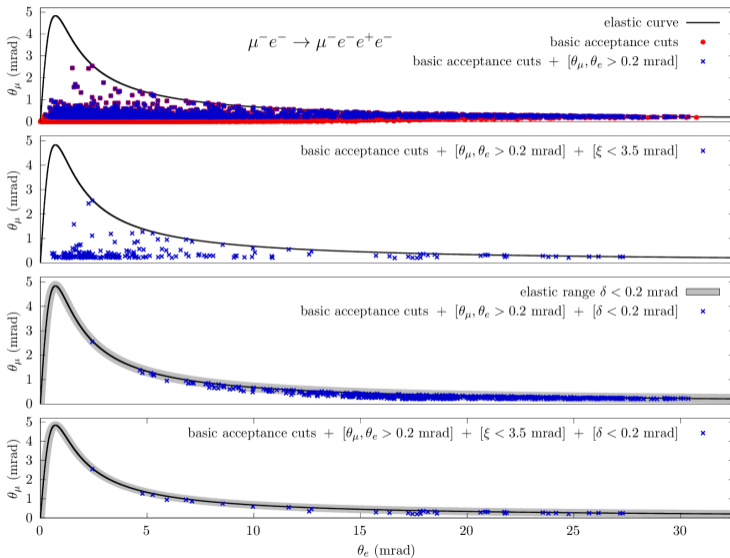
- the emission of an extra electron pair $\mu e \rightarrow \mu e e^+ e^-$ is potentially a dramatically large background, **because of the presence of “peripheral” diagrams** which develop powers of collinear logarithms upon integration

G. Racah, Il Nuovo Cimento 14 (1937) 83-113; L.D. Landau, E.M. Lifschitz, Phys. Z. Sowjetunion 6 (1934) 244; H.J. Bhabha, Proc. Roy. Soc. Lond. A152 (1935) 559;

R.N. Lee, A.A. Lyubyskin, V.A. Smirnov, Phys. Lett. B 848 (2024) 138408

- $\mu^\pm e^- \rightarrow \mu^\pm e^- \ell^+ \ell^-$ **calculated with finite mass effects and implemented in Mesmer**

simulation of $5 \cdot 10^5$ points of $\mu^\pm e^- \rightarrow \mu^\pm e^- \ell^+ \ell^-$



Real pair emission from scattering on nucleus: $\mu^\pm N \rightarrow \mu^\pm N \ell^+ \ell^-$

G. Abbiendi et al., Phys. Lett B854 (2024) 138720

- **it can mimic the signal if one particle is not reconstructed or two tracks overlap within resolution**
- **cross section scaling $\sim Z^2$**

- **GEANT4: “for the process of e^+e^- pair production the muon deflection is neglected”**

A.G. Bogdanov et al., IEEE transactions on nuclear science, 53, n. 2, April 2006

⇒ **a dedicated calculation implemented in the Monte Carlo generator Mesmer**

- **approximation: scattering on the external nucleus field**
- **finite extension of the nucleus through a form factor**

$$F_Z(q) = \frac{1}{Ze} \int_0^\infty dr r^2 \rho_Z(r) \frac{\sin(qr)}{qr}$$

- q : momentum transferred to the nucleus
- ρ_Z : nuclear charged density
- **different models for charge density**

J. Heeck, R. Szafron, Y. Uesaka, PRD 105 (2022) 053006

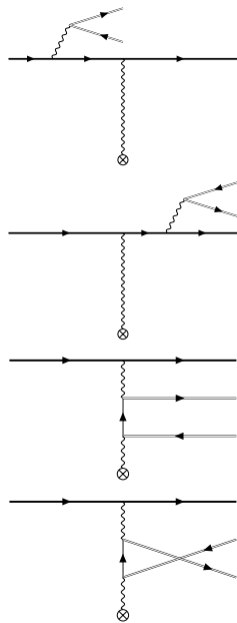
- $F_Z(q) = 1$ (conservative)
- 1 parameter Fermi model (1pF)

$$\rho_Z(r) = \frac{\rho_0}{1 + \exp \frac{r-c}{z}}$$

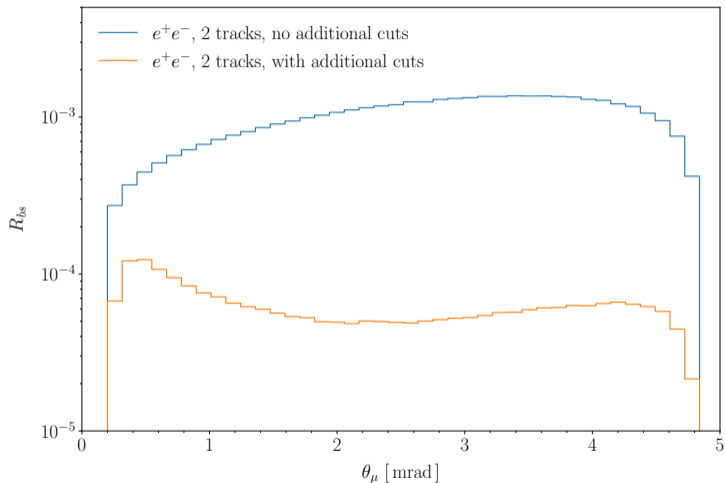
- Fourier Bessel expansion (FB)

$$\begin{aligned} \rho_Z(r) &= \sum_k^n a_k j_0 \left(\frac{k\pi r}{R} \right), & r \leq R \\ &= 0 & > R \end{aligned}$$

- **modified-harmonic oscillator model**



Background/signal ratio



G. Abbiendi, E. Budassi, C.M. Carloni Calame, A. Gurgone, F.P., Phys.Lett.B 854 (2024) 138720

Possible New Physics contamination in the $\Delta\alpha(t)$ determination?

A. Masiero, P. Paradisi and M. Passera, Phys. Rev. D102 (2020) 075013

P.S.B. Dev, W. Rodejohann, X.-J. Xu and Y. Zhang, JHEP 05 (2020) 053

- Effects of **heavy** ($M_{NP} \gg 1$ GeV) NP mediators investigated through EFT with dim-6 operators
 - excluded (at the 10^{-5} level) by existing data
- Effects of **light** ($M_{NP} \leq 1$ GeV) NP mediators investigated with spin-dependent general models
 - spin-0 NP mediators (ALPs)
 - spin-1 NP mediators (Dark Photons, light Z' vector bosons)
 - excluded (at the 10^{-5} level) by existing data

HVP determination with MUonE data will be robust against New Physics

- interesting proposals for NP searches at MUonE (new light mediators) in $2 \rightarrow 3$ processes

- invisibly decaying light Z' in $\mu e \rightarrow \mu e Z'$

Asai et al., Phys. Rev. D106 (2022) 5

- a relevant background can be $\mu e \rightarrow \mu e \pi^0$, in addition to $\mu e \rightarrow \mu e \gamma$

- long-lived mediators with displaced vertex signatures $\mu e \rightarrow \mu e A' \rightarrow \mu e e^+ e^-$

Galon et al., Phys.Rev.D 107 (2023) 095003

- through scattering off the target nuclei $\mu N \rightarrow \mu N X \rightarrow \mu N e^+ e^-$

Grilli di Cortona and E. Nardi, Phys. Rev. D105 (2022) L111701

- **Given its precision requirements, MUonE represents a challenge for**
 - QED corrections
 - background calculation

- **at present we have two independent Monte Carlo tools, Mesmer and McMuLe featuring**
 - NLO QED corrections
 - NNLO QED corrections from single lepton legs
 - YFS inspired approximation to the full NNLO QED in **Mesmer**
 - full NNLO QED with electron “massification” in **McMuLe**
 - pair production in **Mesmer**
 - $\mu^\pm e^- \rightarrow \mu^\pm e^- \ell^+ \ell^-$
 - $\mu^\pm N \rightarrow \mu^\pm N \ell^+ \ell^-$

- **efforts for N³LO started**

- **work in progress for matching with higher order QED corrections**

- **MUonE theory workshops**
 - Theory Kickoff Workshop, Padova, 4-5 September 2017
 - MITP Workshop, Mainz 19-23 February 2018
 - 2nd Workstop/ThinkStart, Zürich, 4-7 February 2019
 - N³LO kick-off workstop/thinkstart IPPP Durham, 3-5 August 2022
 - MITP Workshop, Mainz 14-18 November 2022
 - MITP Workshop, Mainz 03-07 June 2024
- **Five General MUonE Collaboration Meetings**

A collection of references on calculation developments

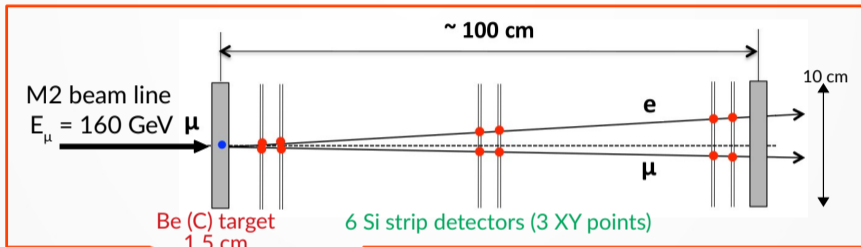
- ↪ Carloni Calame et al., PLB 746 (2015), 325
- ↪ Abbiendi et al., EPJ C77 (2017), 139
- ↪ Mastrolia et al., JHEP 11 (2017) 198
- ↪ Di Vita et al., JHEP 09 (2018) 016
- ↪ Alacevich et al., JHEP 02 (2019) 155
- ↪ Fael and Passera, PRL 122 (2019) 19, 192001
- ↪ Fael, JHEP 02 (2019) 027
- ↪ Engel et al., JHEP 02 (2019) 118
- ↪ Engel et al., JHEP 01 (2020) 085
- ↪ Carloni Calame et al., JHEP 11 (2020) 028
- ↪ Banerjee et al., SciPost Phys. 9 (2020), 027
- ↪ Banerjee et al., EPJC 80 (2020) 6, 591
- ↪ Budassi et al., JHEP 11 (2021) 098
- ↪ Balzani et al., PLB 834 (2022) 137462
- ↪ Bonciani et al., PRL 128 (2022) 2, 022002
- ↪ Budassi et al., PLB 829 (2022) 137138
- ↪ Engel et al., JHEP 04 (2022) 097
- ↪ Fael et al., PRL 128 (2022) 172003
- ↪ Fael et al., PRD 106 (2022) 034029
- ↪ Broggio et al., JHEP 01 (2023) 112
- ↪ Fael et al., PRD 107 (2023) 094017
- ↪ Engel, JHEP 07 (2023) 177
- ↪ Badger et al., JHEP 11 (2023) 041
- ↪ Fadin and Lee., JHEP 11 (2023) 148
- ↪ Ahmed et al., JHEP 01 (2024) 010
- ↪ Engel, JHEP 03 (2024) 004
- ↪ Abbiendi et al., PLB 854 (2024) 138720
- ↪ Plestid and Wise, arXiv:2403.12184

THANK YOU!

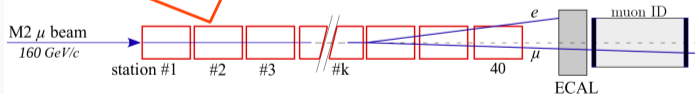
Few slides from R. Pilato for an exp. update

MITP Workshop, 03-07/06/2024, Mainz, Germany

The experimental apparatus



BMS



After LS3:
full apparatus with 40 stations

Achievable accuracy



40 stations
(60 cm Be) + 3 years of data taking =
($\sim 4 \times 10^{12}$ events
 $E_e > 1$ GeV)

$\sim 0.3\%$ statistical
accuracy on a^{HLO}

↓
Competitive with the latest
theoretical predictions

Main challenge:
keep systematic accuracy at the
same level of the statistical one



Systematic uncertainty
of 10 ppm in the signal region

Main systematic effects:

- Longitudinal alignment ($< 10 \mu\text{m}$)
- Knowledge of the beam energy (few MeV)
- Multiple scattering ($< 1\%$)
- Angular intrinsic resolution
- Non-uniform detector response

Staged approach towards the full experiment



- 2017: dedicated test beam to study multiple scattering.
- 2018: test beam to study elastic scattering properties and event selection.
- 2021: first joint test CMS-MUonE with a few 2S modules prototypes (parasitic).
- 2022:
 - test with 1 tracking station.
 - test the calorimeter.
- 2023: test with 2 tracking stations + calorimeter.
- 2025: run with a scaled version of the complete apparatus:
 - 3 tracking stations;
 - Calorimeter;
 - Muon ID;
 - Beam Momentum Spectrometer (BMS).

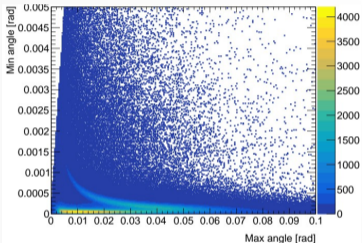
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TB 2023

μ -e elastic scattering event selection

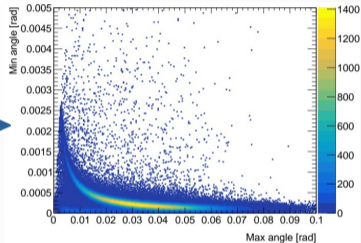


- Single μ_{in} candidate.
- μ_{out}, e_{out} pair candidate.



Initial selection

- Loose χ^2_{vtx} cut.
- $|z_{vtx} - z_{target}| < 3$ cm.
- Acoplanarity cut (elastic events are planar).



Work in progress:

- Exploit dedicated MC generators to study the backgrounds.
- Study the main sources of systematic error using tracker data:
 - Angular intrinsic resolution;
 - Beam energy scale.

- MUonE recently submitted a proposal for a phase 1 of the experiment to the SPSC, concerning a small scale version of the final apparatus.
- If approved, MUonE will request 4 weeks of data taking in 2025.

