

# Flavour News from my Homeoffice

*Andrzej J. Buras*  
*(Technical University Munich TUM-IAS)*

**QCD@Work 2024**

**(Trani, 17-21 June, 2024)**



# Overture

# News from the Homeoffice in Ottobrunn



# Trani Symphony

**1<sup>st</sup>  
Movement**

**: Standard Model Predictions for  
Rare K and B Decays without  
New Physics Infection**

**2<sup>nd</sup>  
Movement**

**: Z' at Work**

**3<sup>rd</sup>  
Movement**

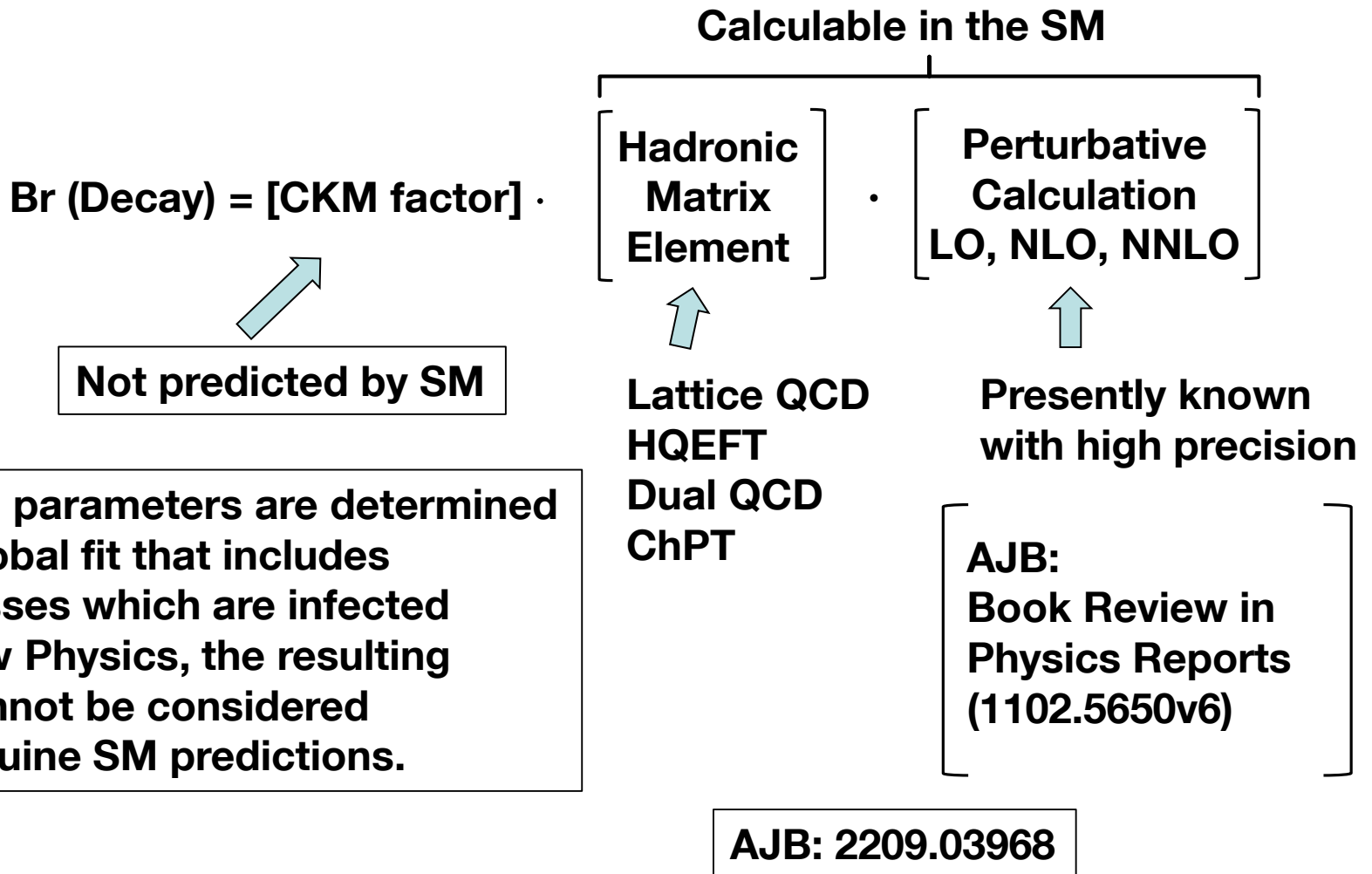
**: Disentangling New Physics in  $K \rightarrow \pi\nu\bar{\nu}$  and  
 $B \rightarrow K(K^*)\bar{\nu}\nu$  Decays**

**4<sup>th</sup>  
Movement**

**: More Flavour News**

**1st Movement:  
Standard Model Predictions  
for Rare K and B Decays  
without New Physics Infection**

# General Expression for Branching Ratios in the Standard Model



# Problems with SM Predictions for TH “clean” Rare K and B Decays

(AJB 2209.03968)

- 1.** In a global fit New Physics can infect them through CKM parameters.
- 2.** Tensions in the determination of  $|V_{cb}|$  from inclusive vs exclusive tree level decays. (Lower the precision and should be presently avoided)
- 3.** Hadronic uncertainties in some observables included in the fit are much larger than in many rare K and B decays. (Lower the precision and should be presently avoided)

# Suggested Strategy

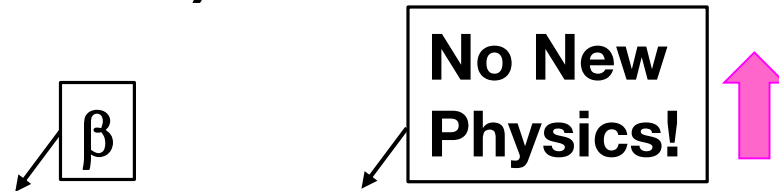
AJB	0303060
AJB+E.Venturini	2109.11032
"	2203.11960
AJB	2209.03968

## Step 1

Remove CKM dependence by calculating suitable ratios of branching ratios to  $\Delta M_d$ ,  $\Delta M_s$ ,  $|\varepsilon_k|$

⇒ CKM can be fully eliminated for all rare B decays. For K decays only the dependence on  $\beta$  remains. ( $\gamma$  dependence irrelevant!!)

## Step 2



Set  $\Delta M_d$ ,  $\Delta M_s$ ,  $\varepsilon_k$  and  $S_{\psi K_S}$  to experimental values ( $\Delta F=2$ )

⇒ Very precise predictions for rare decays branching ratios independent of CKM parameters!



## Step 3

Rapid test of New Physics infection  
in the  $\Delta F=2$  sector using  $|V_{cb}| - \gamma$  plots

BV1 + BV2  
+  
AJB 2204.10337

## Step 4

Determination of CKM parameters from  $\Delta F=2$  only.

Advantages over full global fits

- A.**  $\Delta F = 2$  sector appears to be free of NP infection:  
NP is not required.
- B.** The remaining observables outside the " $\Delta F = 2$  archipelago"  
that could be infected by NP can be predicted within the SM  
and the pulls can be better estimated.
- C.**  $|V_{cb}|$  and  $|V_{ub}|$  tensions can be avoided.

UT fitter  
CKM fitter  
PDG

Global Fitter



AJB

# Standard Model Predictions for Rare K and B Decays without $|V_{cb}|$ uncertainties and New Physics Infection

but with



E. Venturini

# $|V_{cb}|$ Tension

$$|V_{cb}|_{\text{inclusive}} = (41.97 \pm 0.48) \cdot 10^{-3} \quad \text{Finauri \& Gambino (2310.20234)}$$

$$|V_{cb}|_{\text{exclusive}} = (39.21 \pm 0.62) \cdot 10^{-3} \quad \text{(FLAG) (2022)}$$

(see also Bordone, Gubernari, van Dyk, Jung (1912.09335)  
Bordone, Capdevilla, Gambino (2107.00604))

Note: Changing  $|V_{cb}|$  :  $39 \cdot 10^{-3} \Rightarrow 42 \cdot 10^{-3}$

changes  $|V_{cb}|^2$  : by 16% ( $B_{s,d} \rightarrow \mu^+ \mu^-$ ,  $\Delta M_{s,d}$ )

$|V_{cb}|^3$  : by 25% ( $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ ,  $\epsilon_K$ )

$|V_{cb}|^4$  : by 35% ( $K_L \rightarrow \pi^0 \nu \bar{\nu}$ ,  $K_S \rightarrow \mu^+ \mu^-$ )

**$|V_{cb}|$  tension is a disaster for those who spent decades to calculate NLO and NNLO QCD Corrections to basically all important rare K and B decays.**

**Achieving the reduction of TH uncertainties to 1% - 2% level.**

**Similar disaster for Lattice QCD which for  $\Delta M_s$ ,  $\Delta M_d$ ,  $\varepsilon_K$  and weak decay constants achieved accuracy below 5%. Moreover experimental data are very precise for them.**

# Basic Strategy for Rare B and K Decays

AJB + E. Venturini (2109.11032)

**1.**

Use as basic parameters

$$\lambda, |\mathbf{V}_{cb}|, \beta, \gamma$$

**2.**

Construct  $|\mathbf{V}_{cb}|$  independent Ratios  $R_i(\beta, \gamma)$

**3.**

16 Ratios involving

$$\mathbf{B}_s \rightarrow \mu^+ \mu^-, \mathbf{B}_d \rightarrow \mu^+ \mu^-$$

$$\mathbf{B}^+ \rightarrow \mathbf{K}^+ \nu \bar{\nu}, \mathbf{B}^0 \rightarrow \mathbf{K}^{0*} \nu \bar{\nu}$$

$$\mathbf{K}^+ \rightarrow \pi^+ \nu \bar{\nu}, \mathbf{K}_L \rightarrow \pi^0 \nu \bar{\nu}, \mathbf{K}_s \rightarrow \mu^+ \mu^-$$

$$|\varepsilon_K|, \Delta M_d, \Delta M_s$$



Once  $\gamma$  and  $\beta$  will be precisely measured very good test of SM

Additional ratios with  $\mathbf{B} \rightarrow \mathbf{K}(\mathbf{K}^*)\mu^+\mu^-, \mathbf{B}_s \rightarrow \phi\mu^+\mu^-$  in 2209.03968

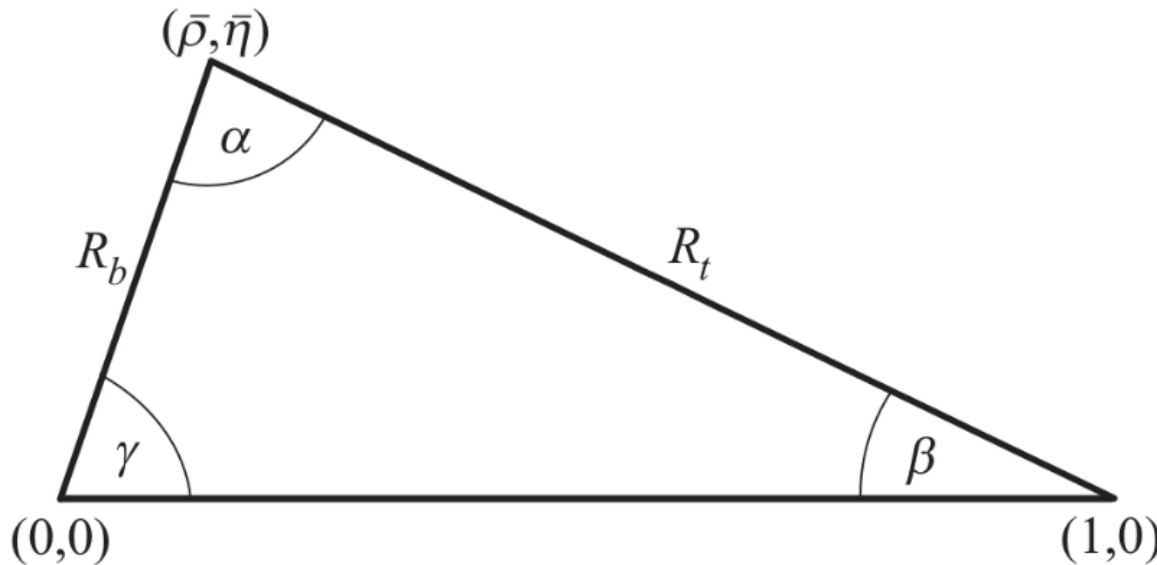
# Recommended Parametrization of CKM Matrix

50th Anniversary  
in 2023

$$\mathbf{V}_{us}, \mathbf{V}_{cb}, \beta, \gamma$$

AJB, Parodi, Stocchi  
(0207101)

$(\beta, \gamma)$   
**Strategy:**  
**Most efficient**  
**to find UT**



$$\bar{\rho} = \frac{\sin \beta \cos \gamma}{\sin (\beta + \gamma)}$$

$$\bar{\eta} = \frac{\sin \beta \sin \gamma}{\sin (\beta + \gamma)}$$

AJB: 2305.00021

# “Critical Exponents” of Flavour Physics

AJB + Venturini (2109.11032) (All decays TH clean)

$$\text{Br}(\text{K}^+ \rightarrow \pi^+ \nu \bar{\nu}) \sim |\mathbf{V}_{cb}|^{2.8} [\sin \gamma]^{1.4} \quad \text{Br}(\text{K}_L \rightarrow \pi^0 \nu \bar{\nu}) \sim |\mathbf{V}_{cb}|^4 [\sin \gamma]^2 [\sin \beta]^2$$

$$\text{Br}(\text{K}_s \rightarrow \mu^+ \mu^-)_{\text{SD}} \sim |\mathbf{V}_{cb}|^4 [\sin \gamma]^2 [\sin \beta]^2 \quad |\epsilon_K| \sim |\mathbf{V}_{cb}|^{3.4} [\sin \gamma]^{1.67} [\sin \beta]^{0.87}$$

$$\text{Br}(\text{B}_s \rightarrow \mu^+ \mu^-) \sim |\mathbf{V}_{cb}|^2 \quad \text{Br}(\text{B}_d \rightarrow \mu^+ \mu^-) \sim |\mathbf{V}_{cb}|^2 [\sin \gamma]^2$$

$$\text{Br}(\text{B}^+ \rightarrow \text{K}^+ \nu \bar{\nu}) \sim |\mathbf{V}_{cb}|^2 \quad \text{Br}(\text{B}^0 \rightarrow \text{K}^{0*} \nu \bar{\nu}) \sim |\mathbf{V}_{cb}|^2$$

$$\Delta \mathbf{M}_s \sim |\mathbf{V}_{cb}|^2 \quad \Delta \mathbf{M}_d \sim |\mathbf{V}_{cb}|^2 [\sin \gamma]^2$$

$$\mathbf{S}_{\psi \text{K}_s} = \sin 2\beta$$



# $|V_{cb}|$ Independent Ratios in the SM

AJB + E. Venturini (B-K Correlations)

$$R_1(\beta, \gamma) = \frac{\text{Br}(\text{K}^+ \rightarrow \pi^+ \nu \bar{\nu})}{[\bar{\text{Br}}(\text{B}_s \rightarrow \mu^+ \mu^-)]^{1.4}} = C_1 (\sin \gamma)^{1.4} (F_{B_s})^{-2.8}$$

$$R_2(\beta, \gamma) = \frac{\text{Br}(\text{K}^+ \rightarrow \pi^+ \nu \bar{\nu})}{[\bar{\text{Br}}(\text{B}_d \rightarrow \mu^+ \mu^-)]^{1.4}} = C_2 (\sin \gamma)^{-1.4} (F_{B_d})^{-2.8}$$

$$R_3(\beta, \gamma) = \frac{\text{Br}(\text{K}_L \rightarrow \pi^0 \nu \bar{\nu})}{[\bar{\text{Br}}(\text{B}_s \rightarrow \mu^+ \mu^-)]^2} = C_3 [\sin \beta \sin \gamma]^2 (F_{B_s})^{-4}$$

$$R_4(\beta, \gamma) = \frac{\text{Br}(\text{K}_L \rightarrow \pi^0 \nu \bar{\nu})}{[\bar{\text{Br}}(\text{B}_d \rightarrow \mu^+ \mu^-)]^2} = C_4 \left[ \frac{\sin \beta}{\sin \gamma} \right]^2 (F_{B_d})^{-4}$$

$V_{cb}$ -independent correlations between K and B Decays

$C_i = \text{CKM}$  independent known factors

# Important $V_{cb}$ – Independent Formulae

AJB + E. Venturini (2109.11032)

$$\frac{\text{Br}(\mathbf{K}^+ \rightarrow \pi^+ \nu \bar{\nu})}{|\varepsilon_{\mathbf{K}}|^{0.82}} = (1.31 \pm 0.05) \cdot 10^{-8} \left[ \frac{\sin 22.2}{\sin \beta} \right]^{0.71} \left[ \frac{\sin \gamma}{\sin 67^\circ} \right]^{0.015}$$

$$\frac{\text{Br}(\mathbf{K}_L \rightarrow \pi^0 \nu \bar{\nu})}{|\varepsilon_{\mathbf{K}}|^{1.18}} = (3.87 \pm 0.06) \cdot 10^{-8} \left[ \frac{\sin \beta}{\sin 22.2} \right]^{0.98} \left[ \frac{\sin \gamma}{\sin 67^\circ} \right]^{0.030}$$

$$\left\{ |\varepsilon_{\mathbf{K}}|_{\text{exp}}, \mathbf{S}_{\psi \mathbf{K}_s}^{\text{exp}} = \sin 2\beta \right\} \Rightarrow \left\{ \begin{array}{l} \text{Most accurate} \\ \text{Predictions to} \\ \text{date} \end{array} \right\}$$

**Note: practically  
 $\gamma$ -independent**

**14 additional  
ratios in  
2109.11032**

**Important reduction of TH uncertainties in  $\varepsilon_{\mathbf{K}}$   
(Brod, Gorbahn, Stamou, 1911.06822)**



# Standard Model

(2024)

SM:

$$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (8.6 \pm 0.4) \cdot 10^{-11}$$
$$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = (2.94 \pm 0.15) \cdot 10^{-11}$$

AJB + Venturini (2109.11032)

Relativ to  
1503.02693  
(AJB, Buttazzo,  
Girrbach-Noe,  
Knegjens)

Reduction of uncertainties:  
In  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  by factor 2.4  
 $K_L \rightarrow \pi^0 \nu \bar{\nu}$  by factor 4.0



## News from NA62 and KOTO

$$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (10.6 \pm 3.8) \cdot 10^{-11} \quad (\text{NA62})$$
$$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \leq 2.0 \cdot 10^{-9} \quad (\text{KOTO})$$

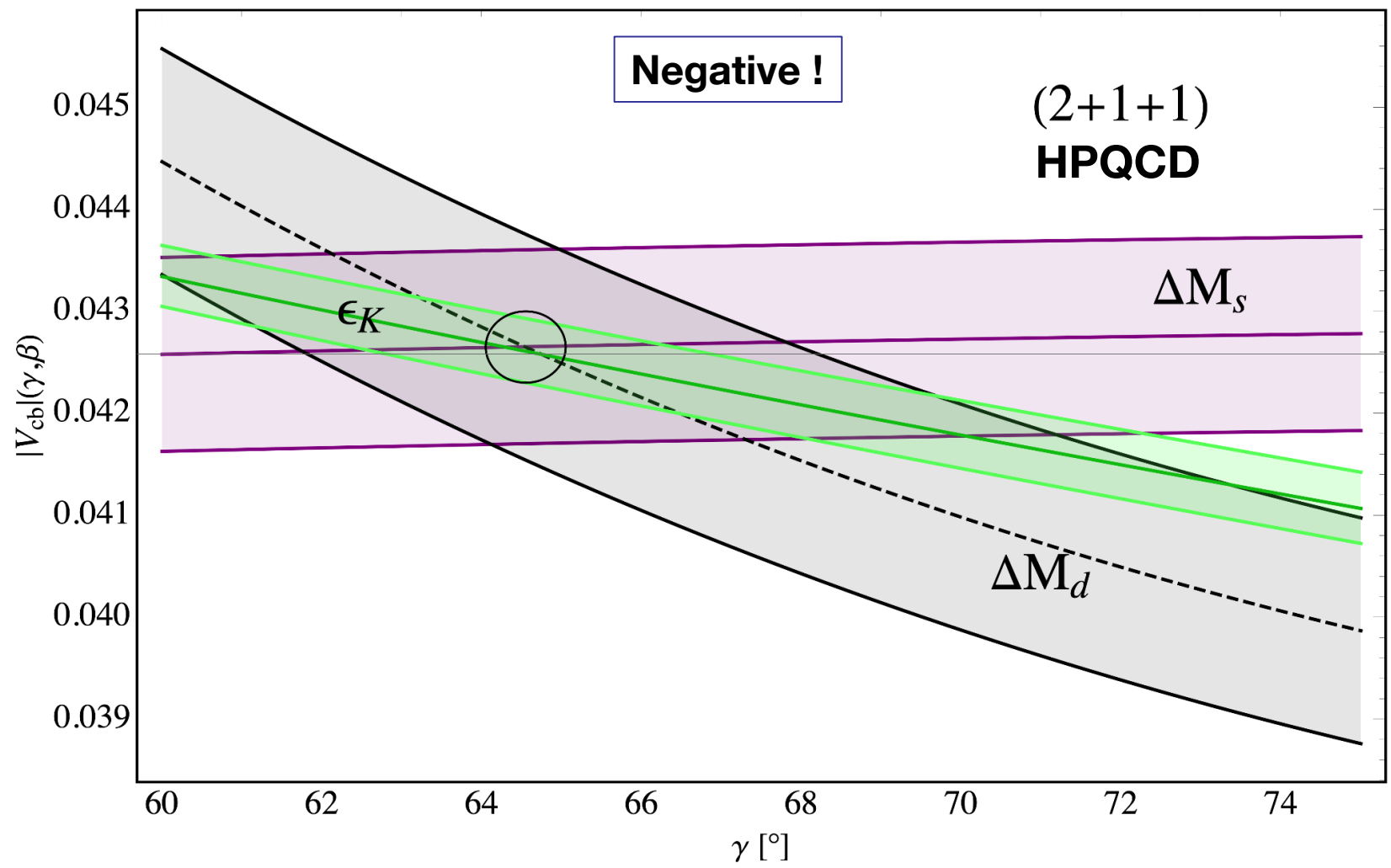
$$|V_{cb}| = 42.6(4) \cdot 10^{-3} \quad |V_{cb}|_{\text{inl}} = 42.0(5) \cdot 10^{-3}$$

$$\gamma = 64.6(16)^\circ \quad \gamma = 63.8(36)^\circ \quad \text{LHCb}$$

**$|V_{cb}| - \gamma$  Plot = Rapid Test**

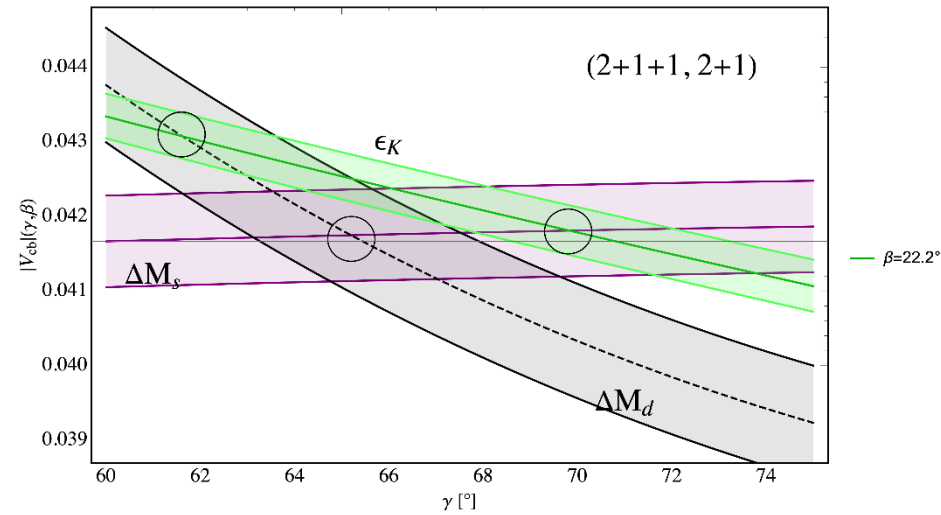
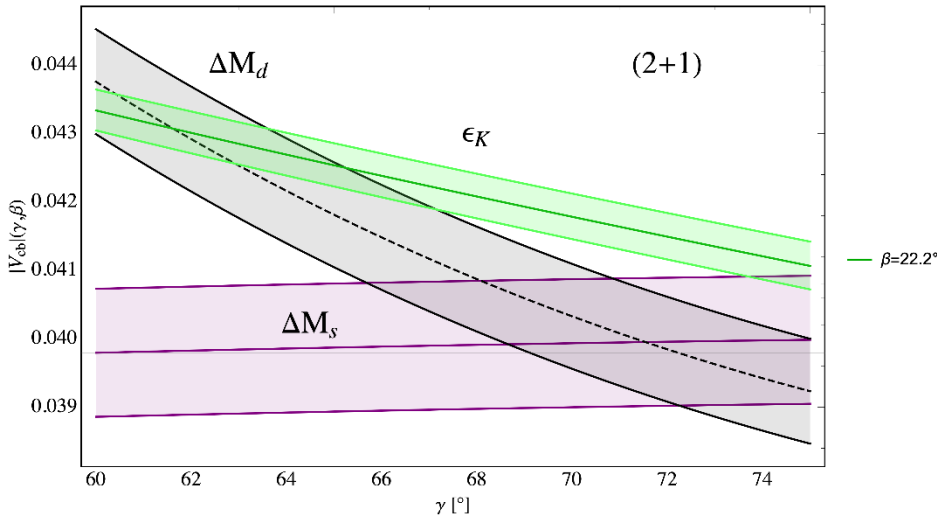
Perfect consistency between  $\Delta M_s$ ,  $\Delta M_d$ ,  $\epsilon_K$ ,  $S_{\psi K}$

AJB + Venturini 2203.11960



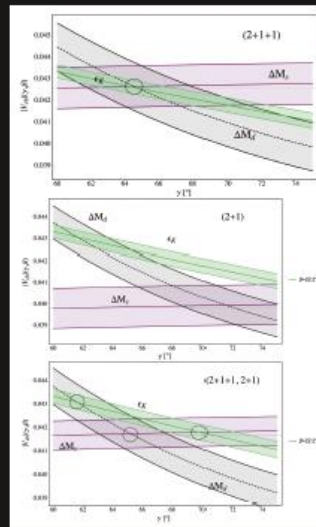
# Positive Tests

AJB + Venturini 2203.11960



**Precise Lattice QCD and higher order QCD calculations are necessary to make the rapid tests reliable!**

**Rapid Test: cover picture of EPJC Vol. 83 number 1, January 2023**

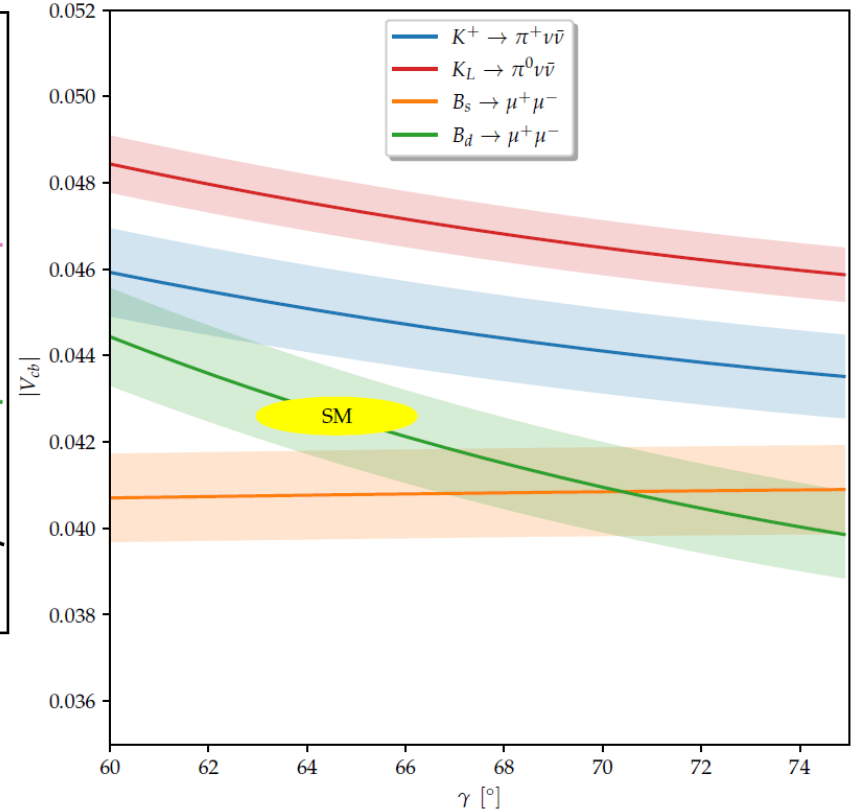
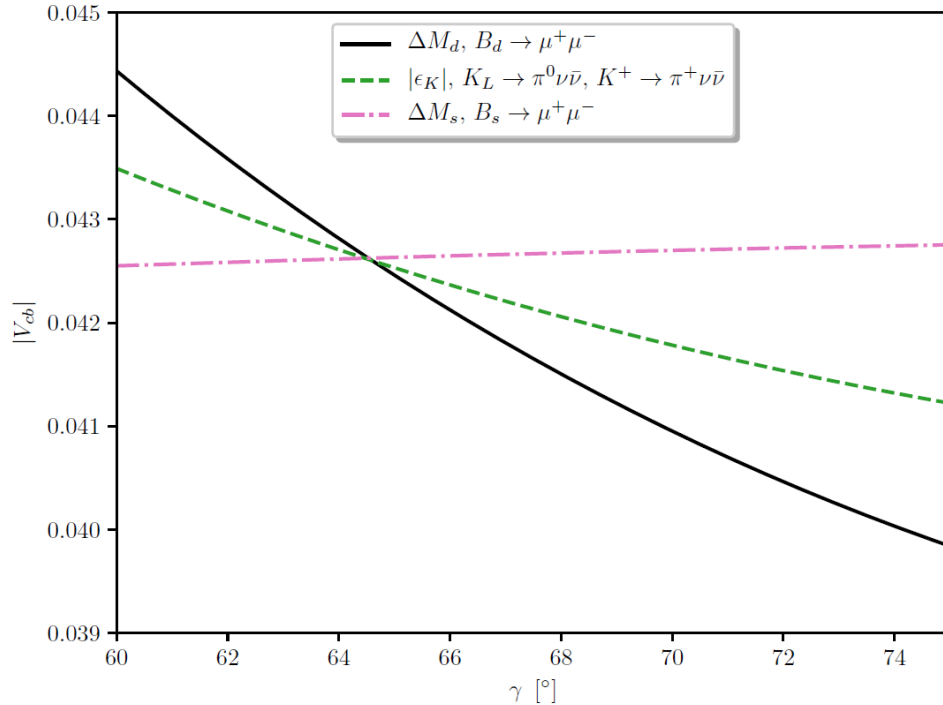


Three rapid tests of NP infection in the  $\Delta F=2$  sector as explained in the text. The values of  $|V_{cb}|$  extracted from  $\epsilon_K$ ,  $\Delta M_s$  and  $\Delta M_c$  as functions of  $\gamma$ .  $2+1+1$  flavours (top),  $2+1$  flavours (middle), average of  $2+1+1$  and  $2+1$  cases (bottom). The green band represents experimental  $S_{\psi K}$  constraint on  $\beta$

From Andrzej J. Buras on: Standard Model predictions for rare K and B decays without new physics infection. Eur. Phys. J. C 83, 66 (2023).



## $V_{cb} - \gamma$ Plot



**Superior over UT-triangle  
 plots:  $|V_{cb}|$  seen,  $\gamma$  better exposed  
 AJB 2204.10337**

**See CERN Courier July/Aug 2024  
 AJB**

# $R_i(\beta, \gamma)$ can now be predicted in the SM

AJB 2209.03968

$$\frac{\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})}{[\overline{\text{Br}}(B_s \rightarrow \mu^+ \mu^-)]^{1.4}} = 53.69 \pm 2.75$$

$$\frac{\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})}{[\text{Br}(B^+ \rightarrow K^+ \nu \bar{\nu})]^{1.4}} = (1.90 \pm 0.13) \cdot 10^{-3}$$

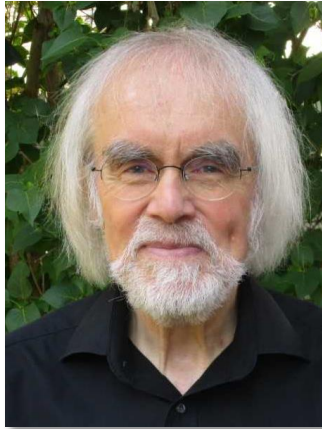
Many other results in 2209.03968



# **2nd Movement: Z' at Work**

# 10 Years Anniversary (Z', 331)

## AJB – Fulvia de Fazio – Jennifer Girrbaach-Noe Collaboration



**AJB**



**Fulvia**



**Jennifer**

1211.1896  
1211.1237  
1303.3723  
1311.6729  
1404.3824  
1405.3850

1512.02869  
1604.02344  
1912.09308  
2301.02649

Without Jennifer

10 papers

# Peculiar Pattern of Flavour Data

$\Delta\varepsilon_K^{\text{NP}} = 0$   
Indirect CP  
Violation

but

$\Delta\left(\frac{\varepsilon'}{\varepsilon}\right)^{\text{NP}} > 0$  (significant)  
Direct CP  
Violation

Direct CP  
Violation

Required  $\bar{s}d$  coupling from New Physics  
 $\Rightarrow$  Impact on  $\varepsilon_K$

$\Delta M_s, \Delta M_d$   
 $S_{\psi K_s}, S_{\psi\phi}$   
SM-Like

but

$\text{Br}(B^+ \rightarrow K^+ \mu^+ \mu^-)$  (pull -5.1  $\sigma$ )  
 $\text{Br}(B_s \rightarrow \phi \mu^+ \mu^-)$  (pull -4.8  $\sigma$ )

[1.1, 6]

Required  $\bar{b}s$  coupling from New Physics  
 $\Rightarrow$  Impact on  $\Delta M_s, S_{\psi\phi}, \dots$

Which NP scenario can reproduce this pattern ?

$$\varepsilon_K, \varepsilon'/\varepsilon, \Delta M_K, K^+ \rightarrow \pi^+ \nu \bar{\nu}, K_L \rightarrow \pi^0 \nu \bar{\nu}$$

**New heavy gauge boson  $Z'$ :  $\Delta_L^{sd}(Z') = |\Delta_L^{sd}(Z')| e^{i\varphi}$**

$$\begin{aligned} \varepsilon_K^{NP} &\sim \text{Im} \left( \Delta_L^{sd}(Z') \right)^2 \sim [\text{Re} \Delta_L^{sd}(Z')] [\text{Im} \Delta_L^{sd}(Z')] \\ (\varepsilon'/\varepsilon)^{NP} &\sim \text{Im} \Delta_L^{sd}(Z') \\ \Delta M_K^{NP} &\sim \left( \text{Re} \Delta_L^{sd}(Z') \right)^2 - \left( \text{Im} \Delta_L^{sd}(Z') \right)^2 \quad (K^0 - \bar{K}^0) \end{aligned}$$

**With  $\text{Re} \Delta_L^{sd}(Z') \ll \text{Im} \Delta_L^{sd}(Z')$**

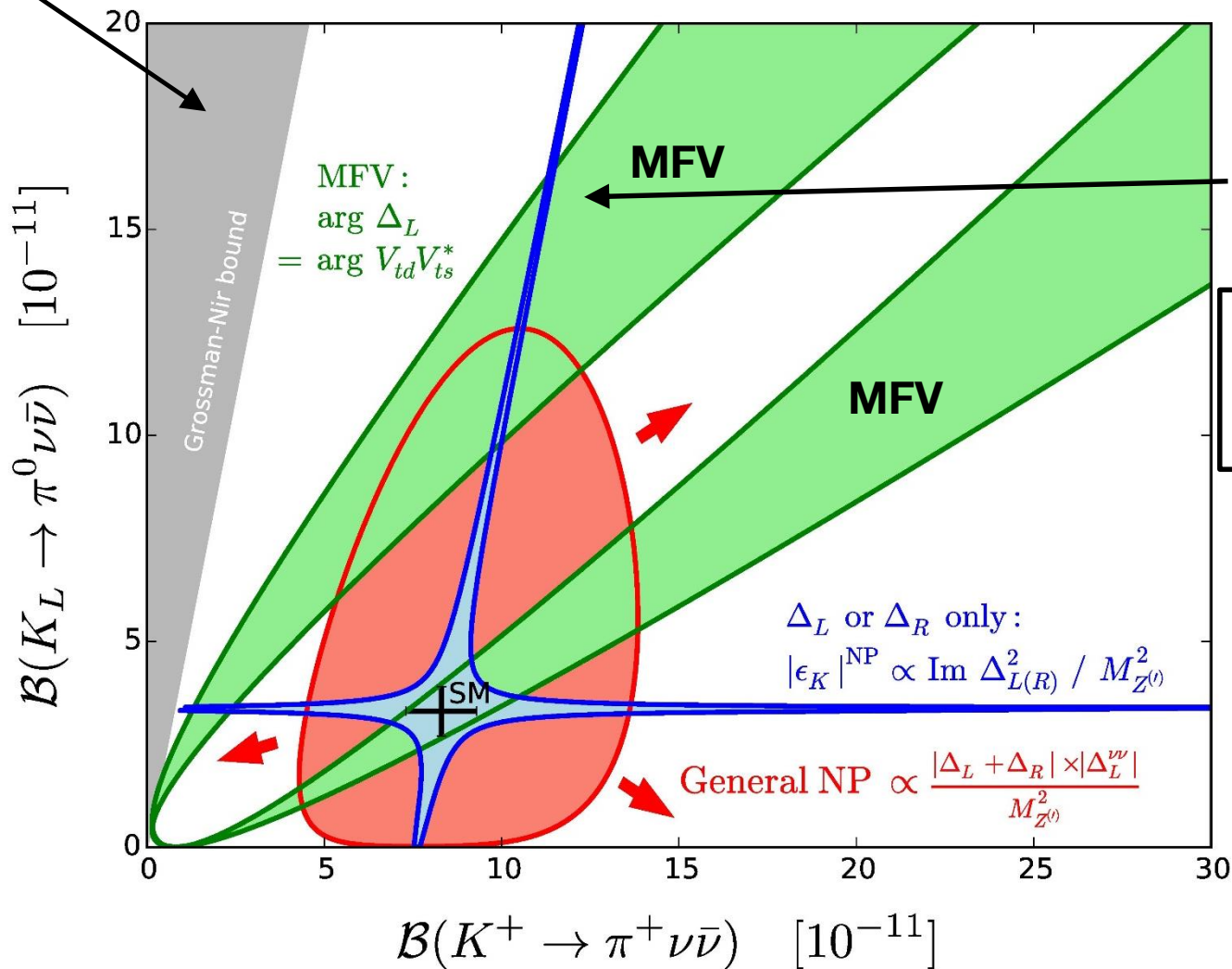
**(Imaginary coupling)**

**$\varepsilon_K^{NP} \simeq 0$   $(\varepsilon'/\varepsilon)^{NP}$  can be enhanced  
 $\Delta M_K$  can be suppressed + Interesting implications  
 (possibly required by Lattice QCD) for  $K \rightarrow \pi \nu \bar{\nu}$**

**Aebischer  
 AJB  
 Kumar  
 2302.00013**

GN  
bound

Buttazzo, AJB, Kneijens, 1507.08672



Monika Blanke

Based on the insights from Monika Blanke (0904.1545)

# Kaon Physics without New Physics in $\varepsilon_K$

$$R_{\nu\bar{\nu}}^+ = \frac{\mathcal{B}(K^+ \rightarrow \pi^+ \nu\bar{\nu})}{\mathcal{B}(K^+ \rightarrow \pi^+ \nu\bar{\nu})_{SM}}, \quad R_{\nu\bar{\nu}}^0 = \frac{\mathcal{B}(K_L \rightarrow \pi^0 \nu\bar{\nu})}{\mathcal{B}(K_L \rightarrow \pi^0 \nu\bar{\nu})_{SM}},$$

$$R_{\mu^+\mu^-}^S = \frac{\mathcal{B}(K_S \rightarrow \mu^+\mu^-)_{SD}}{\mathcal{B}(K_S \rightarrow \mu^+\mu^-)_{SM}^{SD}}, \quad R_{\pi^0\ell^+\ell^-}^0 = \frac{\mathcal{B}(K_L \rightarrow \pi^0\ell^+\ell^-)}{\mathcal{B}(K_L \rightarrow \pi^0\ell^+\ell^-)_{SM}},$$

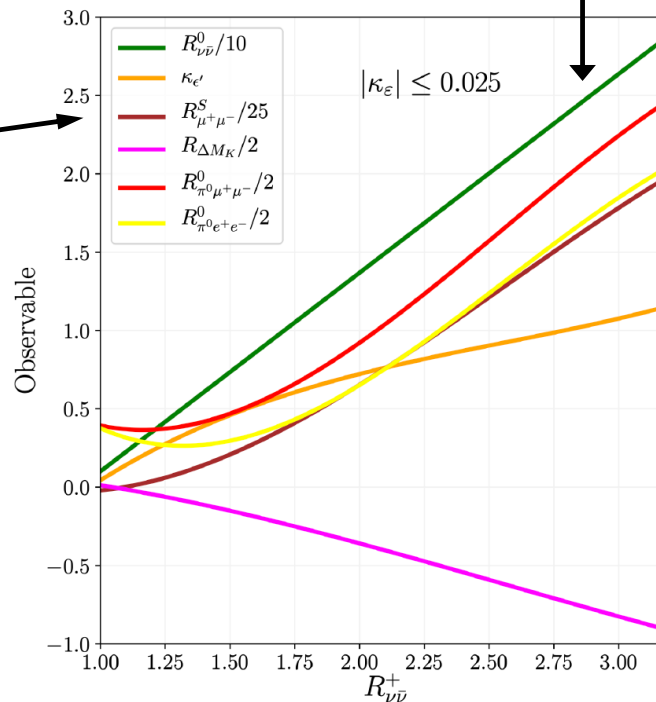
$$R_{\Delta M_K} = \frac{\Delta M_K^{BSM}}{\Delta M_K^{exp}}, \quad \Delta\left(\frac{\varepsilon'}{\varepsilon}\right) = \kappa_{\varepsilon'} \cdot 10^{-3}, \quad \Delta(\varepsilon_K) = \kappa_{\varepsilon} \cdot 10^{-3}$$

**MB branch**

$\kappa_{\varepsilon} \leq 0.02$

**Dery, Ghosh,  
Grossman, Schacht  
(2104.06427)**

**(Z' at work)**



**Aebischer, AJB, Kumar  
2302.00013**



J. Aebischer



J. Kumar

**Left-handed  
couplings**

# B Physics without NP in Quark Mixing

Fine tuning in  $\Delta M_q$   $q=d,s$

suppression factor

$$M_{12}(Z') \sim \left[ 1 + \left( \frac{\Delta_R^{bq}(Z')}{\Delta_L^{bq}(Z')} \right)^2 + 2K_{bq} \frac{\Delta_R^{bq}}{\Delta_L^{bq}} \right] \frac{\Delta_L^{bq}(Z')}{M_{Z'}^2}$$

$$K_{bq} = \frac{\langle \hat{Q}_1^{LR}(M_{Z'}) \rangle^{bq}}{\langle \hat{Q}_1^{VLL}(M_{Z'}) \rangle^{bq}} \approx -5$$

$$\Delta_R^{bq}(Z') \approx 0.1 \Delta_L^{bq}(Z')$$

AJB, De Fazio, Girrbach-Noe 1404.3824

AJB, Buttazzo, Girrbach-Noe 1408.0728

Crivellin, Hofer, Matias, Nierste, Pokorski, Rosiek 1504.07928

# Strong Suppression of $Z'$ to $B_s - \bar{B}_s$ Mixing

Requires

$$\Delta_R^{bs}(Z') \approx 0.1 \Delta_L^{bs}(Z')$$

Non-negligible  
RH couplings

## Implications for rare B-Decays

⊖ Suppression of  $B^+ \rightarrow K^+ \mu^+ \mu^-$ ,  $B_s \rightarrow \varphi \mu^+ \mu^-$ ,  $B \rightarrow K^* \mu^+ \mu^-$



⊕ Enhancement of  $B^+ \rightarrow K^+ \nu \bar{\nu}$ ,  $B^0 \rightarrow K^0 \nu \bar{\nu}$  up to 20%

AJB +



Peter Stangl

(2407.xxx)



# News from Belle II

(2311.14647)

$$\text{Br}(B^+ \rightarrow K^+ \nu \bar{\nu}) = (13 \pm 4) \cdot 10^{-6}$$
$$\text{Br}(B^+ \rightarrow K^+ \nu \bar{\nu})_{\text{SM}} = (4.92 \pm 0.30) \cdot 10^{-6}$$

\*)



AJB + Stangl (2024)

# News from CERN (LHCb, CMS, ATLAS)



$$\overline{\text{Br}}(B_s \rightarrow \mu^+ \mu^-) = (3.45 \pm 0.29) \cdot 10^{-9}$$

$$\overline{\text{Br}}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}} = (3.78 \pm 0.12) \cdot 10^{-9} \quad \text{AJB + Venturini (2022)}$$

\*) Many analyses:

Bause et al. (2309.00075)

Becirevic et al. (2301.06990, 2309.02246)

Dreiner et al. (2309.03727)

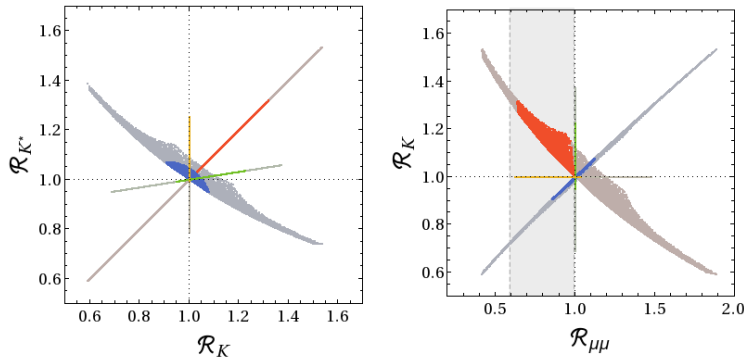
He et al. (2309.12741)

# Testing Z' Couplings

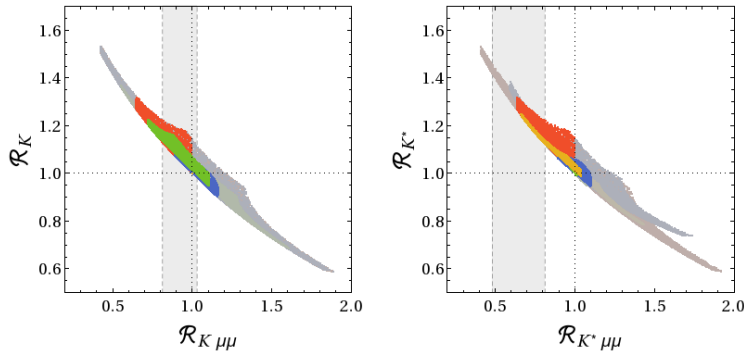
(1409.4557)

AJB, J. Girschbach-Noe, C. Niehoff, D. Straub

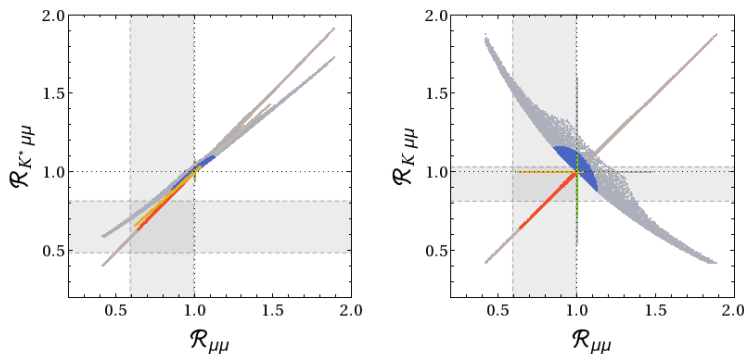
- Left-handed
- Right-handed
- Excluded



$$R_K = \frac{\text{Br}(B \rightarrow K\nu\bar{\nu})}{\text{Br}(B \rightarrow K\nu\bar{\nu})_{SM}}$$



$$R_{K^*} = \frac{\text{Br}(B \rightarrow K^*\nu\bar{\nu})}{\text{Br}(B \rightarrow K^*\nu\bar{\nu})_{SM}}$$



$$R_{\mu\mu} \leftrightarrow B_s \rightarrow \mu\bar{\mu}$$

$$R_{K\mu\mu} \leftrightarrow B^+ \rightarrow K^+ \mu\bar{\mu}$$

$$R_{K^*\mu\mu} \leftrightarrow B^0 \rightarrow K^{0*} \mu\bar{\mu}$$

# 3rd Movement:

**Distangling New Physics in  $K \rightarrow \pi\nu\bar{\nu}$  and  
 $B \rightarrow K(K^*)\bar{\nu}\nu$  Decays**

**AJB +**



**J. Harz**



**M. Mojahed**

**2405.06742**

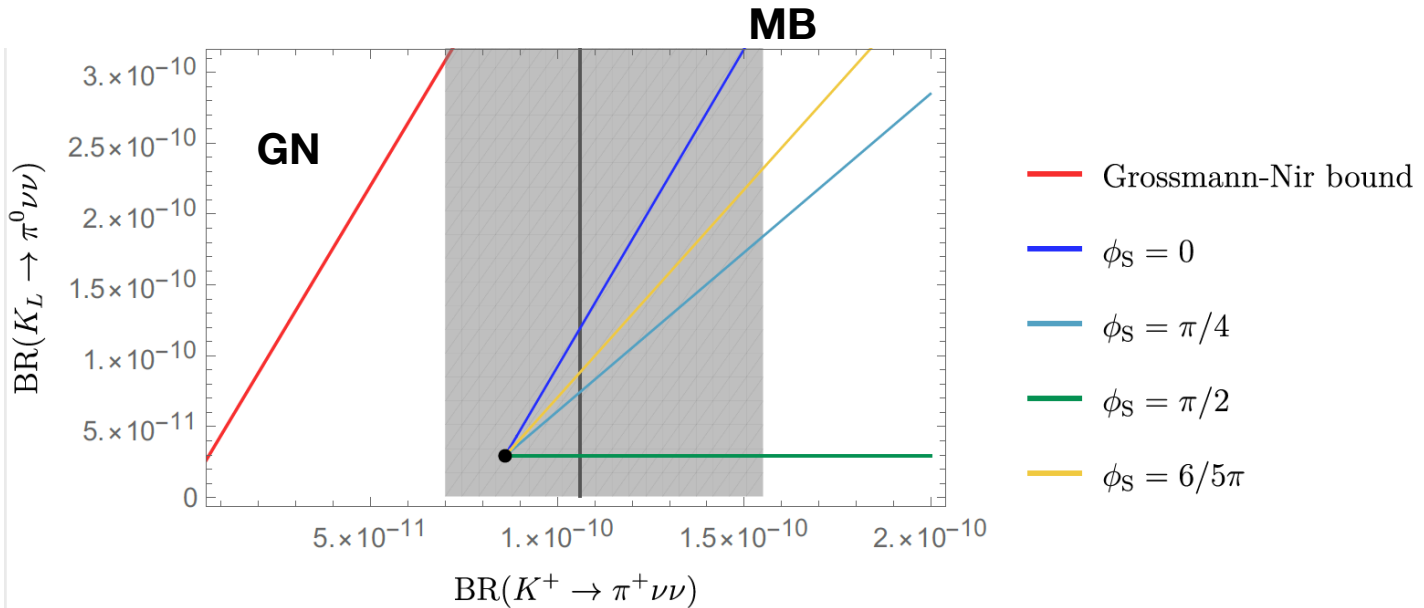
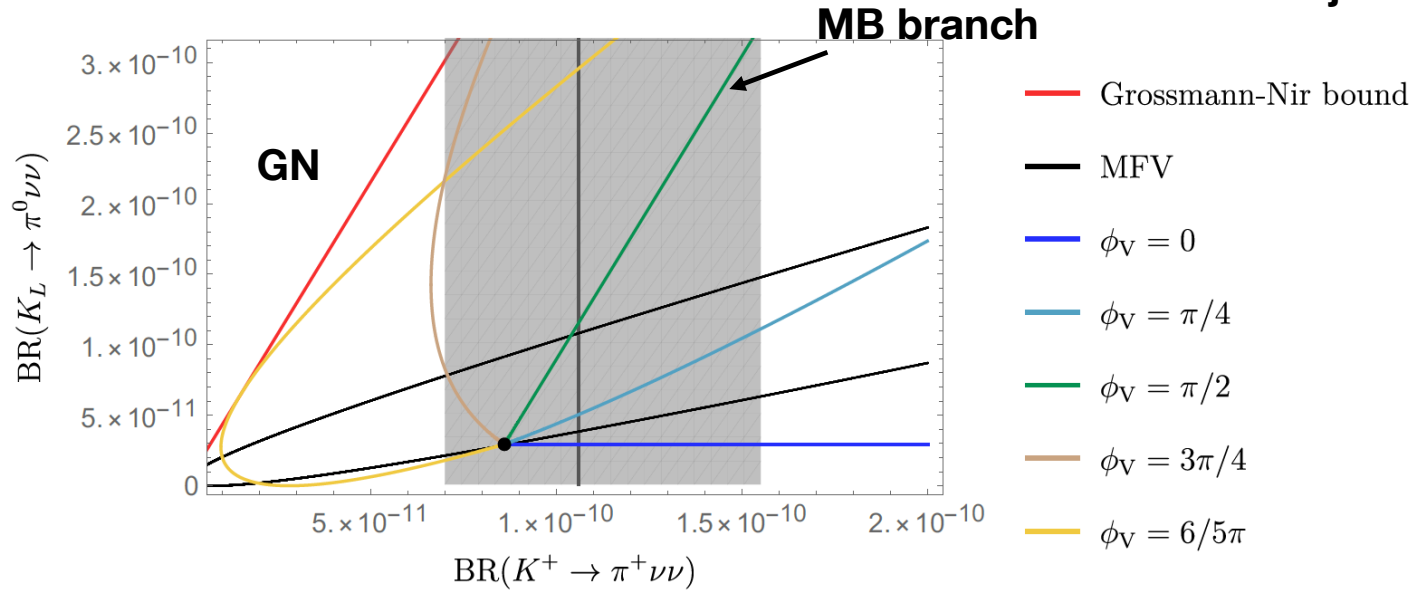
- Goal:** Disentangling different New Physics contributions to the rare decays  $K \rightarrow \pi + \cancel{E}$  and  $B \rightarrow K(K^*) + \cancel{E}$  through kinematic distributions in the missing energy  $\cancel{E}$
- Step 1:** WET with active or sterile neutrinos including Lepton Number violating operators with scalar and tensor currents
- Step 2:** Dark WET: new invisible particles in the final state: two dark scalars, two dark fermions, two dark vectors

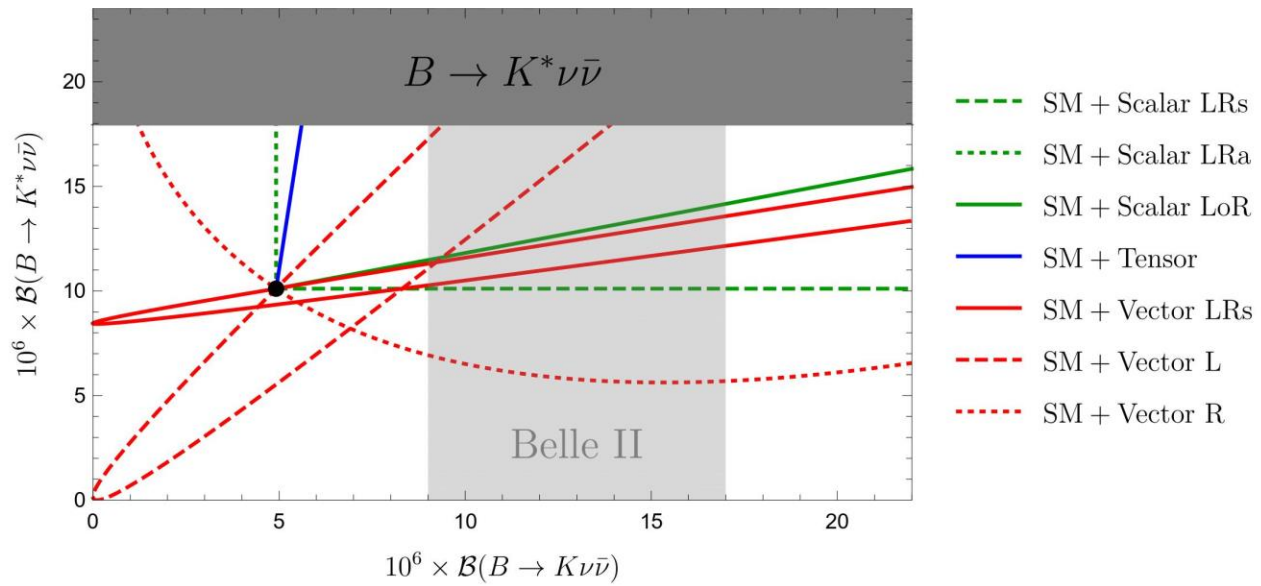
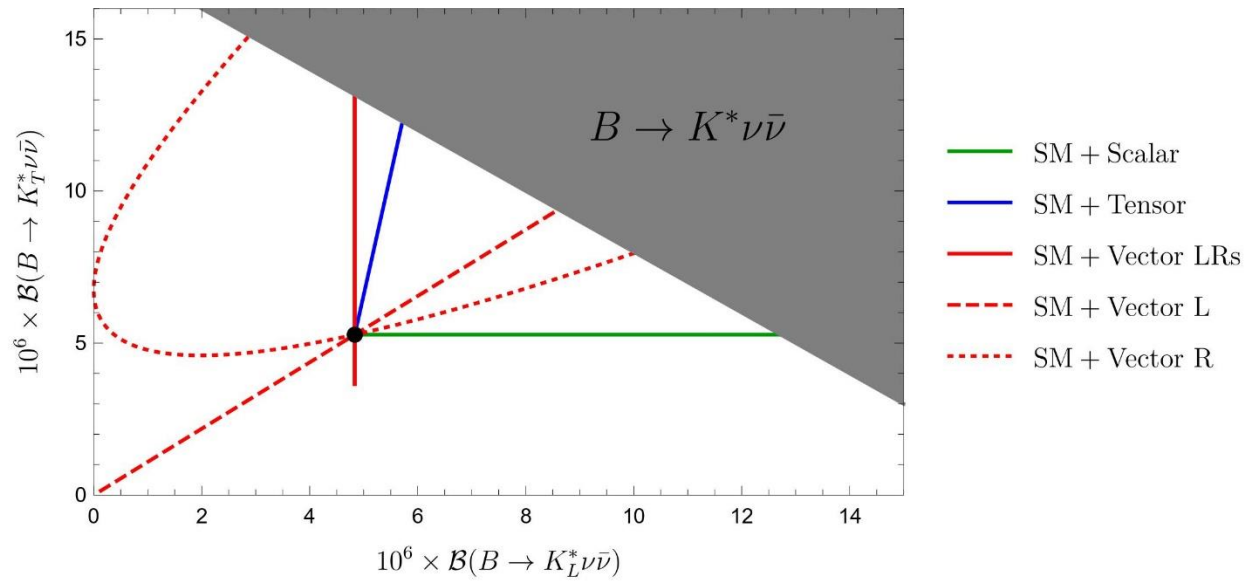
# Main Results

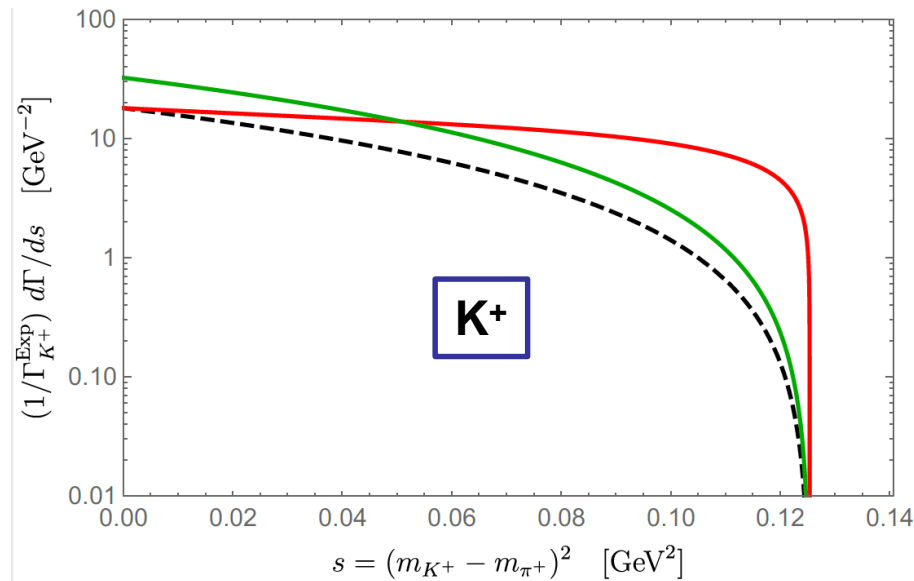
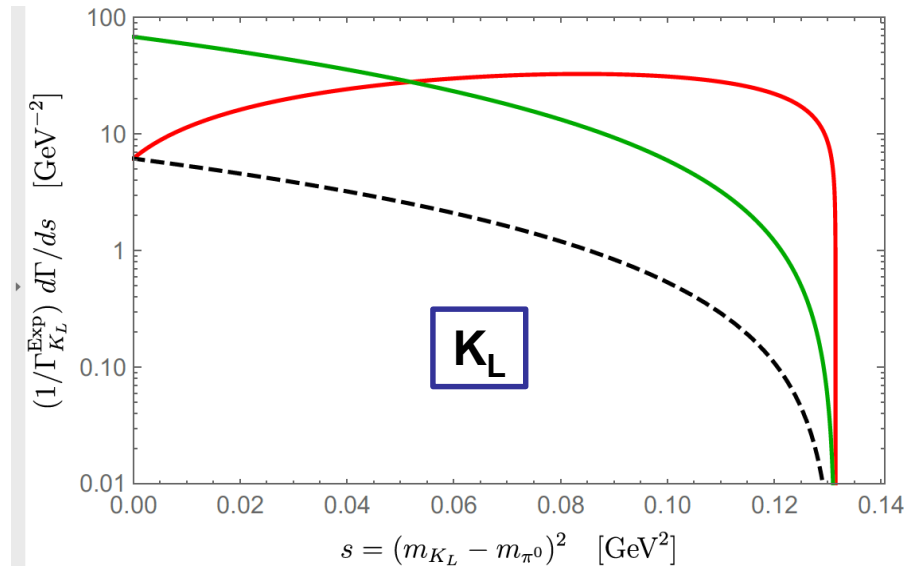
- A. Vector, scalar and tensor quark currents can be uniquely determined from experimental data of kinematic distributions**
  
- B. Measurements of kinematic distributions make it possible to disentangle the contributions of WET operators from most of the dark-sector operators**
  
- C. Sum Rules for vector currents in WET are also satisfied in some new dark-physics scenarios that mimic WET**

# $K_L \rightarrow \pi^0 \nu \bar{\nu} - K^+ \rightarrow \pi^+ \nu \bar{\nu}$ Correlation

AJB + J.Harz  
+ M. Mojahed









# **4th Movement More Flavour News**

# Dual QCD Approach for Weak Decays

Successful low energy approximation of QCD  
for  $K \rightarrow \pi\pi$   $K^0$ - $K^0$  mixing (Large N framework)

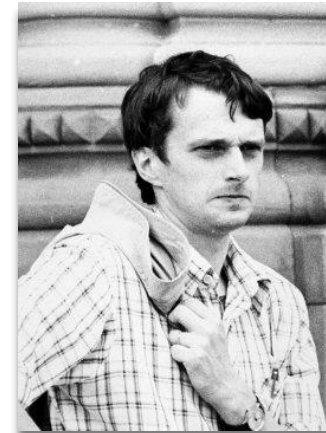
1986



W. Bardeen

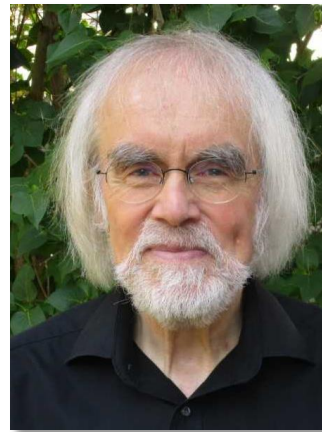


AJB



J.-M. Gérard

2024



# $\Delta I = 1/2$ Rule

$$R_{\text{exp}} = \frac{A(\text{K} \rightarrow (\pi\pi)_{I=0})}{A(\text{K} \rightarrow (\pi\pi)_{I=2})} = 22.4$$

Puzzle since  
1954 (Gell-Mann + Pais)

$$R_{\text{th}} = \sqrt{2} \quad (\text{without QCD})$$

1986  
2014

$$R = 16 \pm 2$$

Dual  
QCD

Bardeen, AJB, Gérard  
(Current-Current Operators)

2020

$$R = 19.19 \pm 4.8$$

RBC-UKQCD  
Lattice Collaboration

QCD dynamics dominate this rule  
but New Physics could still contribute

AJB  
F. de Fazio  
J. Girschbach-Noe  
(1404.3824)

$$\left(\varepsilon'/\varepsilon\right)_{\text{exp}} = \left(16.6 \pm 2.3\right) \cdot 10^{-4}$$

(NA48, KTeV) (2000)

$$\left(\varepsilon'/\varepsilon\right)_{\text{SM}} = \left(14 \pm 5\right) \cdot 10^{-4}$$

Chiral Perturbation Theory  
(Pich et al)

No Anomaly



$$\left(\varepsilon'/\varepsilon\right)_{\text{SM}} = \left(5 \pm 2\right) \cdot 10^{-4}$$

Hep-arxiv: 2101.00020

Insight from Dual QCD + NNLO QCD  
(AJB + Gérard)

Anomaly

$$\left(\varepsilon'/\varepsilon\right)_{\text{SM}} = \left(21.7 \pm 8.4\right) \cdot 10^{-4}$$

RBC – UKQCD

No Anomaly

Hopefully this controversy will be clarified in this decade

Reviews AJB: 2101.00020, 2203.12632  
2307.15737

# Good News on $\varepsilon'/\varepsilon$

$\varepsilon'/\varepsilon = \text{QCD Penguins} - \text{Electroweak Penguin}$

$$\left( \frac{\varepsilon'}{\varepsilon} \right)_{\text{SM}}^{\text{EWP}} = -(7 \pm 1) \cdot 10^{-4} \quad (\text{RBC} - \text{UKQCD} \text{ and } \text{DQCD})$$

Perfect Agreement!

Chiral Pert Th:  $\approx (-3.5 \pm 2.0) \cdot 10^{-4}$

Disagreements on QCD Penguin contribution.

Good news on  $\hat{B}_K$

$$\hat{B}_K = 0.73 \pm 0.02$$

Dual QCD (2014)

$$\hat{B}_K = 0.74 \pm 0.01$$

RBC-UKQCD (2024)

# Main Activities in the Homeoffice in Ottobrunn



AJB

# NLO QCD in WET and SMEFT (in Homeoffice)

**WET**

$$\mu \leq EW$$

$$SU(3)_c \otimes U(1)_{QED}$$

SM + New Physics Operators

$\Delta F = 1$  (Non-Leptonic)

J. Aebischer, C. Bobeth, AJB, J. Kumar,  
M. Misiak

(2107.10262) (2107.12391) ( $\epsilon'/\epsilon$ )

$\Delta F = 2$  (Non-Leptonic)

J. Aebischer, C. Bobeth, AJB, J. Kumar  
(2009.07276)

**SMEFT**

$$\mu \geq EW$$

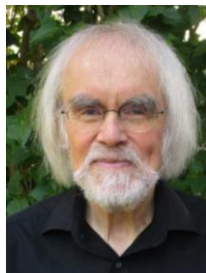
J. Aebischer, AJB, J. Kumar

$\Delta F = 2$  (Non-Leptonic)

(2203.11224) (2202.01225)



J. Aebischer



AJB



J. Kumar



Christoph Bobeth



M. Misiak

**New Physics  
(New Forces, New Particles)**

$$\Lambda_{\text{NP}} \gg \Lambda_{\text{SM}} \approx 0(100\text{GeV})$$

**Buchmüller, Wyler  
Warsaw Basis**

$\Lambda_{\text{NP}}$



**Standard Model Effective  
Field Theory (SMEFT)**

**Unbroken  $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$**

**SM particles, interactions + New Physics  
Contact Interactions  
(new operators)**

In full (D=6)  
generality  
1350 real  
parameters  
1149 complex  
phases

Renormalization  
Group Evolution

Energy  
Gap



$\Lambda_{\text{SM}}$



**$SU(3)_C \otimes U(1)_{\text{QED}}$**

**SM + New Physics Effects**

Jenkins, Manohar, Trott



In my view

**Top → Down**

approach  
requiring New  
Physics models  
more powerful  
than

**Bottom → Up**

Renormalization  
Group Evolution



**Scale of decaying mesons**

**Non-perturbative QCD**

**0(few GeV)**



# Messages to take to your Homeoffice

**1.**

$V_{cb}$  – independent ratios and  $V_{cb} - \gamma$  plots will play important roles in the search for New Physics

**2.**

The sextet

$$\begin{aligned} K^+ &\rightarrow \pi^+ \nu \bar{\nu}, K_L \rightarrow \pi^0 \nu \bar{\nu}, B \rightarrow K \nu \bar{\nu} \\ B &\rightarrow K^* \nu \bar{\nu}, B_s \rightarrow \mu^+ \mu^-, B_d \rightarrow \mu^+ \mu^- \end{aligned}$$

can reveal NP easier than

$$B \rightarrow K \mu^+ \mu^-, B \rightarrow K^* \mu^+ \mu^-$$

(smaller long-distance uncertainties)

**3.**

It is crucial that several lattice QCD groups calculate  $\Delta M_d$ ,  $\Delta M_s$ ,  $\varepsilon'/\varepsilon$ ,  $\Delta I = 1/2$  rule with 2 + 1 + 1 flavours

**Coming Years**

**: Flavour Precision Era**

**LHC Upgrade**  
**E = 14 TeV**  
**(CERN)**

**Precision**  
 **$B_{d,s}$  – Meson**  
**Decays**  
**LHCb, CMS**  
**ATLAS, Belle II**

★  
 $K^+ \rightarrow \pi^+ \nu \bar{\nu} (10^{-10})$  **(CERN)**  
 $K_L \rightarrow \pi^0 \nu \tilde{\nu} (3 \cdot 10^{-11})$  **J-PARC**  
**(Japan)**

**Lepton Flavour**  
**Violation**

$$\mu \rightarrow e \gamma$$

$$\mu \rightarrow e e e$$

$$\tau \rightarrow \mu \gamma, \tau \rightarrow 3 \mu$$

**Electric**  
**Dipole**  
**Moments**

★  
 $(g-2)_\mu$

**Improved**  
**Lattice**  
**Gauge Theory**  
**Calculations**

★  
 $\epsilon'/\epsilon$

★  
 $\Delta I = 1/2$  Rule,  
 $\Delta M_K$

**Neutrinos**

**2024-2046 : Expedition  
Attouniverse  $\rightarrow$  Zeptouniverse  
 $10^{-18}\text{m} \rightarrow 10^{-21}\text{m}$**

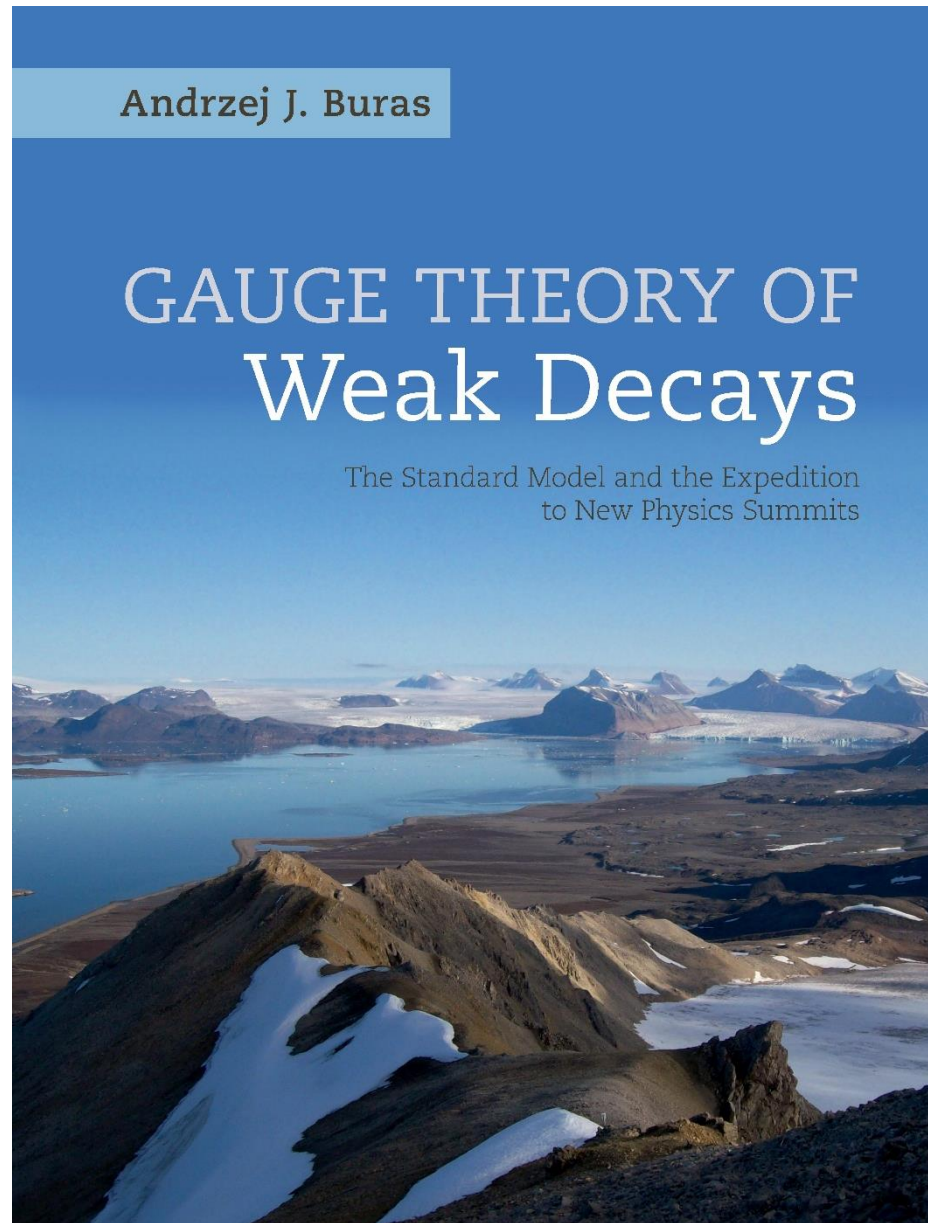
**Hopefully meeting  $Z'$ , Leptoquarks,  
Vector-Like Quarks and Leptons**

**Zeptouniverse  
Guide**

**Published  
July 2020**

**7**

**Exciting  
Years !**



**739 pages  
1350 references**

**Cambridge  
University  
Press**

# Flavour Physics (2024- )

Crevasses

New Physics Summits

SMEFT

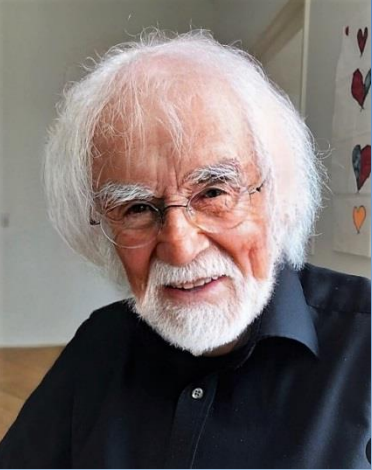
Energy gap

SM

Allan Buras



# Flavour Physics (2024- )



(2034)

Crevasses

Zeptouniverse

New Physics Summits

SMEFT

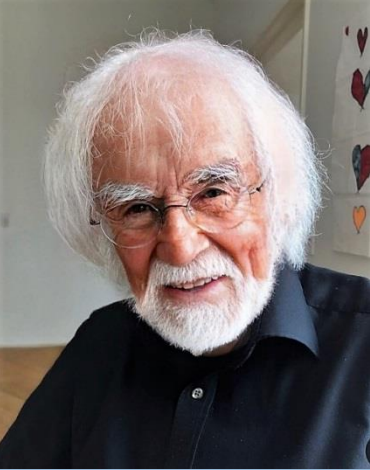
Energy gap

SM

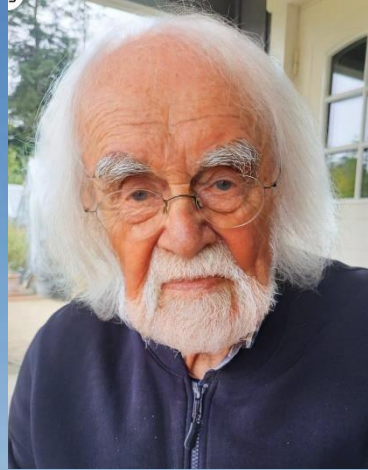
Allan Buras



# Flavour Physics (2024- )



(2034)

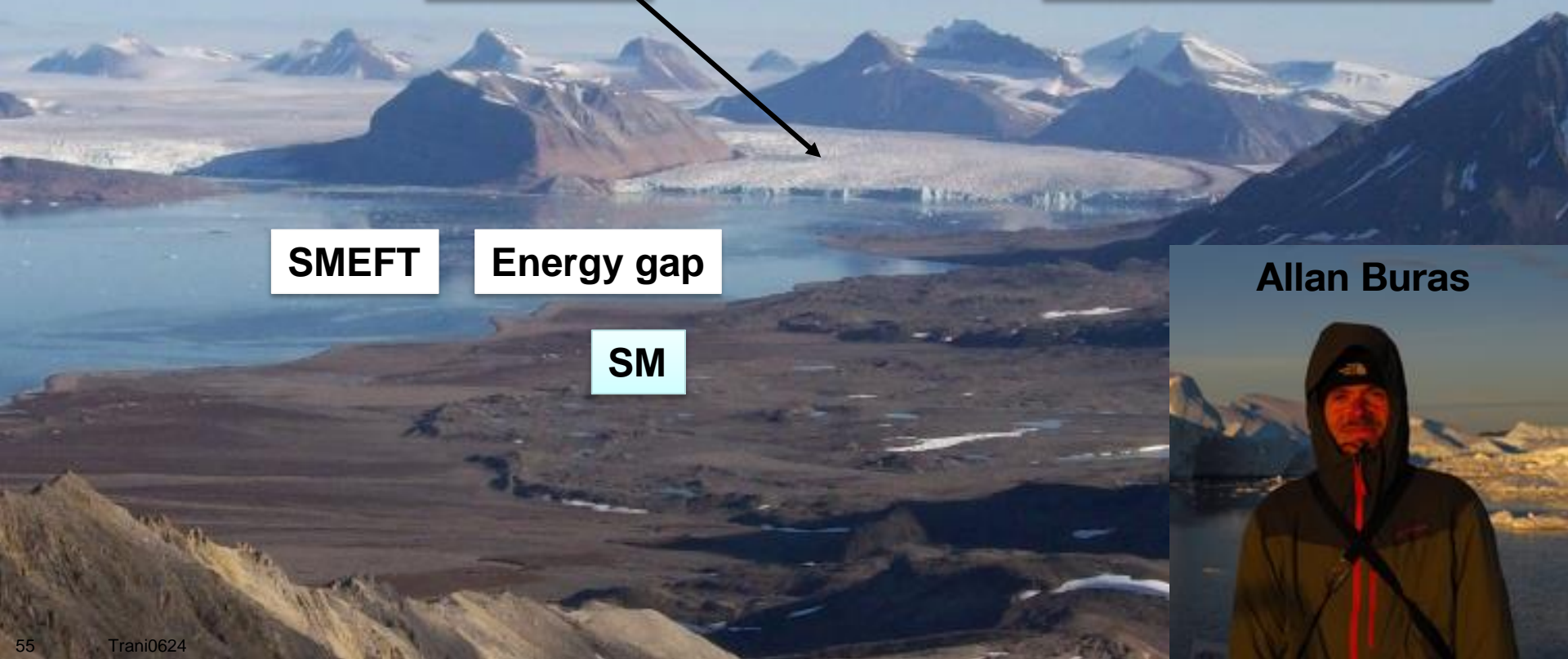


(2046)

Crevasses

Zeptouniverse

New Physics Summits



SMEFT

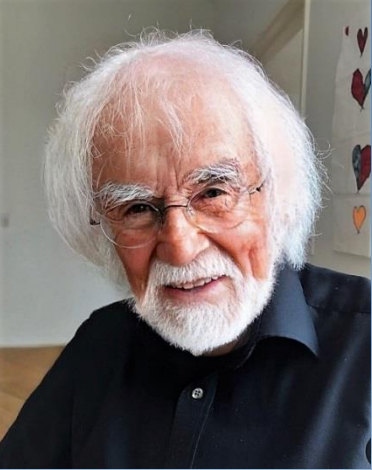
Energy gap

SM

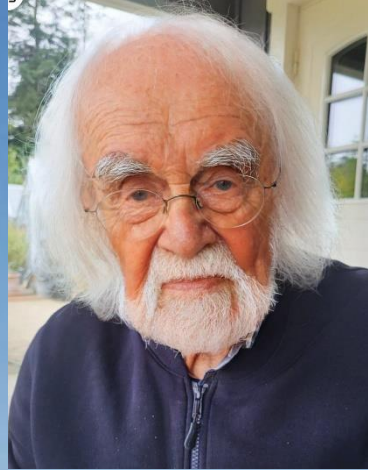
Allan Buras



# Flavour Physics (2024- )



(2034)



(2046)

Crevasses

Zeptouniverse

New Physics Summits



SMEFT

Energy gap

SM

Allan Buras



# Thank You !



# Backup

# Footprints of Majorana Neutrinos in Rare K and B Decays

AJB + Julia Harz

All existing calculations of  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  and  $K_L \rightarrow \pi^0 \nu \bar{\nu}$  assumed until recently that neutrinos are of Dirac type.

What if neutrinos are Majorana neutrinos?  
First pioneering studies:

1912.10433

T. Li, X.-D. Ma, M. A. Schmidt

2009.04494

F. Deppisch, K. Fridell, J. Harz



J. Harz

# Main Messages from these Studies

**1.**

**Lepton Number Violating operators**

$$\left(\bar{\mathbf{d}}_R^i \mathbf{d}_L^j\right)\left(\bar{\mathbf{v}}_\alpha^c \mathbf{v}_\beta\right) \quad \left(\bar{\mathbf{d}}_L^i \mathbf{d}_R^j\right)\left(\bar{\mathbf{v}}_\alpha^c \mathbf{v}_\beta\right) \quad (\text{LNV}) \quad (\Delta L = 2)$$

Enter  $L_{\text{eff}}$  as dim=7 operators.  $\mathbf{v} \equiv P_L \mathbf{v}$

$$\text{dim6} \quad \left(\bar{\mathbf{d}}_L^i \gamma^\mu \mathbf{d}_L^j\right)\left(\bar{\mathbf{v}}_\alpha^c \gamma^\mu \mathbf{v}_\beta\right) \quad \left(\bar{\mathbf{d}}_R^i \gamma^\mu \mathbf{d}_R^j\right)\left(\bar{\mathbf{v}}_\alpha^c \gamma^\mu \mathbf{v}_\beta\right) \quad (\text{LNC}) \quad (\Delta L = 0)$$

**2.**

**Difference between LNV and LNC seen in s-distributions,  
s = the invariant mass<sup>2</sup> of  $\mathbf{v}\bar{\mathbf{v}}$**

**3.**

**Scale  $\Lambda_{\text{NP}}^{\text{LNV}} \approx 20\text{TeV}$  can be probed**

**4.**

**All neutrino generations involved as opposed  
to neutrinoless double beta decay**

# Main Goals of AJB – JH Collaboration

AJB + Julia Harz

**A.** Closer look at the impact of Majorana neutrinos on the  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  -  $K_L \rightarrow \pi^0 \nu \bar{\nu}$  plane

**B.** Generalization to  $B \rightarrow K \nu \bar{\nu}$ ,  $B \rightarrow K^* \nu \bar{\nu}$ ,  $B \rightarrow X \nu \bar{\nu}$

**C.** Efficient strategies that would allow NA62, KOTO and Belle II to find possible footprints of Majorana neutrinos in their data.

**D.** Strategies valid in the presence of right-handed currents, LFUV and LFV

$$\Delta C_{\nu} = |C_{\nu}^{\text{NP}}| e^{i\phi_{\nu}} \quad C_s = |C_s| e^{i\phi_s}$$

# Present Anomalies

(2024)

$$B^+ \rightarrow K^+ \nu \bar{\nu}$$

+

B

Anomaly in  
Angular Distribution

$$B \rightarrow K^* \mu^+ \mu^- \quad (P_5')$$

-

B

$$B^+ \rightarrow K^+ \mu^+ \mu^-$$

$$B_s \rightarrow \phi \mu^+ \mu^-$$

-

B

Violation of  
 $\mu - \tau$  Universality  
 $R(D^*), R(D^*)$

+

B

$$B_s \rightarrow \mu^+ \mu^-$$

-

B

$$(g-2)_\mu \quad +$$

$$(g-2)_e \quad -$$

$$\Delta A_{CP} \quad -$$

C

$$\Delta M_K \quad -$$

K

Violation of  
CKM Unitarity

$$V_{us}, V_{ud}$$

$$\frac{\varepsilon'}{\varepsilon} \quad +$$

K

$$B_d^0 \rightarrow \pi^0 K_S$$

CPV – Anomaly

-

Neutrino  
Anomalies

# New Particles behind Anomalies

## Top candidates

Review:

Capdevilla, Crivellin, Matias  
2309.01311

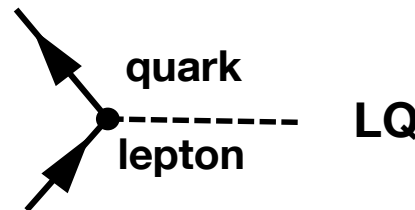
**Z' boson**

: heavy neutral gauge boson (Spin 1)

**Leptoquarks**

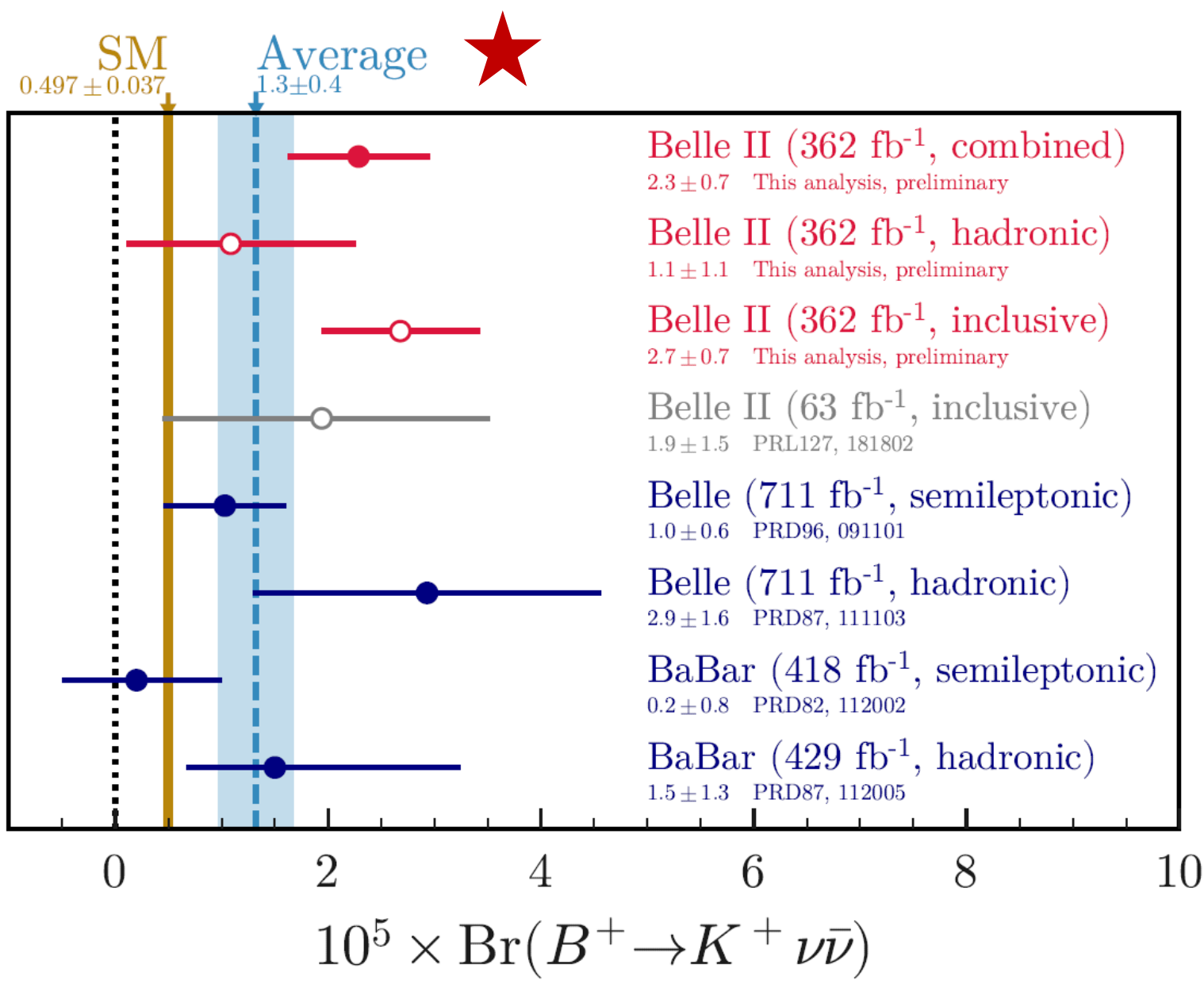
: Spin 0 or Spin 1  
(provide interactions between quarks and leptons)

**Dinosaurs of  
Flavour Physics?**



**Vector-like quarks**

: Left and right components transform identically under  $SU(2)_L$



# SM Relation for $\Delta M_s$ , $\Delta M_d$ , $|\varepsilon_K|$ , $\beta$

AJB: 2209.03968

$$R \equiv \frac{|\varepsilon_K|^{1.18}}{\Delta M_d \Delta M_s} = (8.22 \pm 0.18) \cdot 10^{-5} \left( \frac{\sin \beta}{\sin 22.2^\circ} \right)^{1.027} \text{ K ps}^2$$

$$K = \left( \frac{\hat{B}_K}{0.7625} \right)^{1.18} \left[ \frac{210.6 \text{ MeV}}{\sqrt{\hat{B}_{B_d} F_{B_d}}} \right]^2 \left[ \frac{256.1 \text{ MeV}}{\sqrt{\hat{B}_{B_s} F_{B_s}}} \right]^2$$

HPQCD

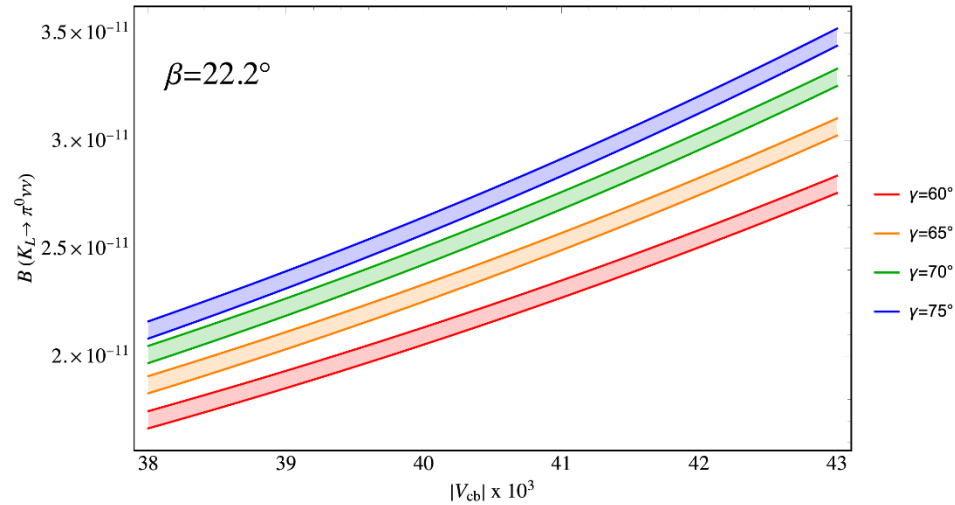
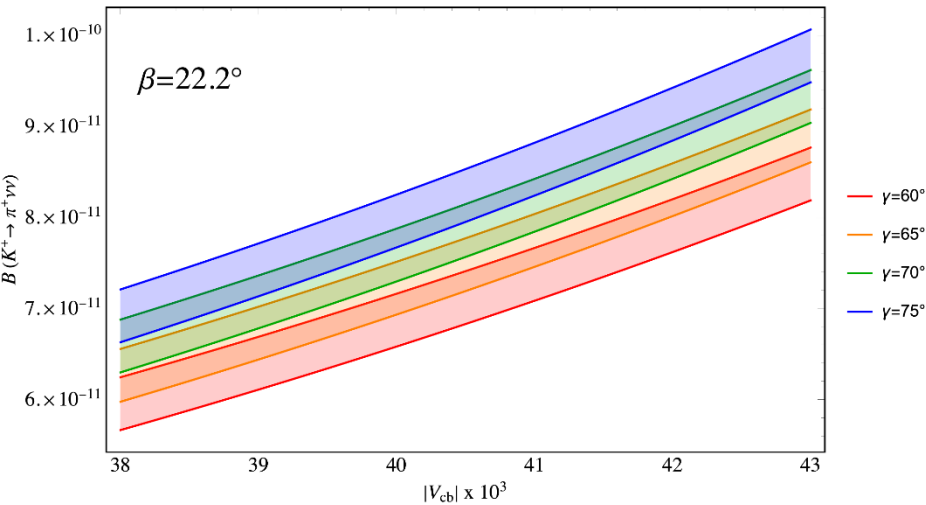
$$R_{\text{exp}} = (8.26 \pm 0.06) \cdot 10^{-5} \text{ ps}^2$$

$$K = 1.00 \pm 0.07$$



# $\text{Br}(\text{K}^+ \rightarrow \mu^+ \nu \bar{\nu})_{\text{SM}}$ and $\text{Br}(\text{K}_L \rightarrow \pi^0 \nu \bar{\nu})_{\text{SM}}$

AJB + E. Venturini (2109.11032)



$$\text{Br}(\text{K}^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{exp}} = \left( 10.6^{+4.0}_{-3.5} \right) \cdot 10^{-11}$$

NA62

$$\text{Br}(\text{K}_L \rightarrow \pi^0 \nu \bar{\nu})_{\text{exp}} \leq 3.0 \cdot 10^{-9}$$

KOTO

$$\text{Br}(\text{K}^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{SM}} = (8.60 \pm 0.42) \cdot 10^{-11}$$

$V_{\text{cb}}$  and  $\gamma$  independent



$$\text{Br}(\text{K}_L \rightarrow \pi^0 \nu \bar{\nu})_{\text{SM}} = (2.94 \pm 0.15) \cdot 10^{-11}$$

# The Story of $B_s \rightarrow \mu^+ \mu^-$ continues

(SM)

$$\overline{\text{Br}}(B_s \rightarrow \mu^+ \mu^-) = (3.78 \pm 0.12) \cdot 10^{-9}$$

AJB + Venturini  
2203.11960

$$\overline{\text{Br}}(B_s \rightarrow \mu^+ \mu^-) = (3.45 \pm 0.29) \cdot 10^{-9}$$

HFLAV  
(CMS, LHCb, ATLAS)

$$\overline{\text{Br}}(B_s \rightarrow \mu^+ \mu^-) = (3.47 \pm 0.14) \cdot 10^{-9}$$

UTfitter  
2212.1051

Theory  
SM

: Buchalla + AJB (1993, 1998)  
Misiak + Urban (1998) } NLO QCD

Bobeth, Gorbahn, Stamou (2013) NLO EW

Hermann, Misiak, Steinhauser (2013) NNLO QCD

Beneke, Bobeth, Szafron (2017, 2019) QED

# Searching for Majorana Footprints through LNC Sum Rules

## LNC Sum Rules

AJB, J. Girrbach-Noe, C. Niehoff, D. Straub  
(1409.4557)

$$(r_1^{\text{LNC}} = r_2^{\text{LNC}} = 1)$$

$$F_L = F_L^{\text{SM}} \left[ \frac{(\kappa_\eta - 2)R_K + 4R_{K^*}}{(\kappa_\eta + 2)R_{K^*}} \right] r_1^{\text{LNV}}$$

$$r_1^{\text{LNV}} \neq 1$$

$$r_2^{\text{LNV}} \neq 1$$

$$\text{Br}(B \rightarrow X_s v \bar{v}) = \text{Br}(B \rightarrow X_s v \bar{v})_{\text{SM}} \left[ \frac{\kappa_\eta R_K + 2R_{K^*}}{\kappa_\eta + 2} \right] r_2^{\text{LNV}}$$

$$R_K = \frac{\text{Br}(B \rightarrow K v \bar{v})}{B_{\text{SM}}(B \rightarrow K v \bar{v})}$$

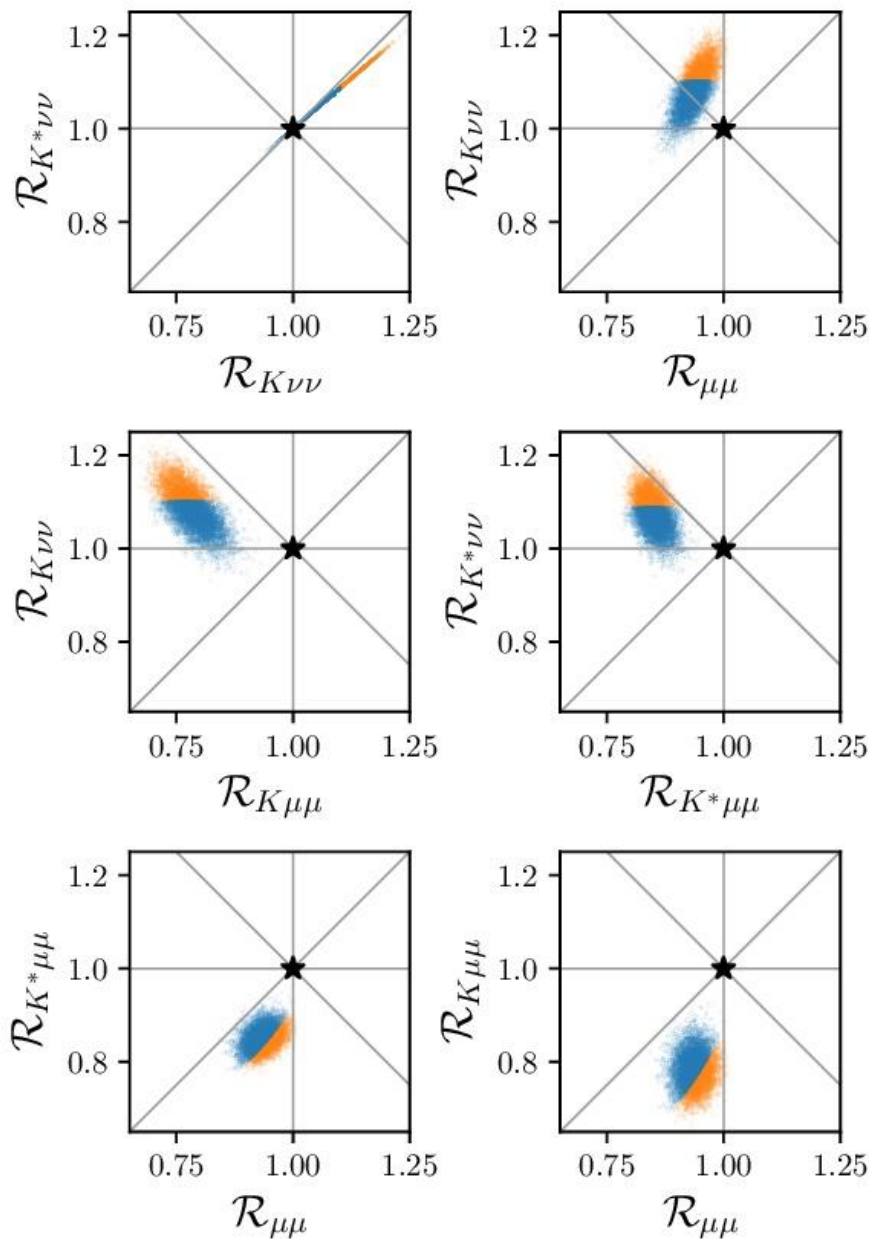
$$R_{K^*} = \frac{\text{Br}(B \rightarrow K^* v \bar{v})}{\text{Br}(B \rightarrow K^* v \bar{v})_{\text{SM}}}$$

$$\kappa_\eta = 1.33 \pm 0.05 \text{ (formfactor)}$$

$$F_L^{\text{SM}} = 0.49 \pm 0.04$$

**K\*** longitudinal polarization fraction

# Vector Z' Couplings to Leptons



$$\Delta \mathbf{C}_9(\Lambda_{\text{NP}}) \neq \mathbf{0}$$

$$\Delta \mathbf{C}_{10}(\Lambda_{\text{NP}}) = \mathbf{0}$$

**AJB + Stangl  
(2407.xxx)**

# Strong Suppression of $Z'$ to $\Delta F = 2$ Process

**K-System**

$$\text{Re}\Delta_L^{\text{sd}}(Z') \ll \text{Im}\Delta_L^{\text{sd}}(Z')$$

**Negligible  
RH couplings**

**$B_{s,d}$ -Systems**

$$\Delta_R^{\text{bq}}(Z') \approx 0.1 \Delta_L^{\text{bq}}(Z')$$

**Non-negligible  
RH couplings**