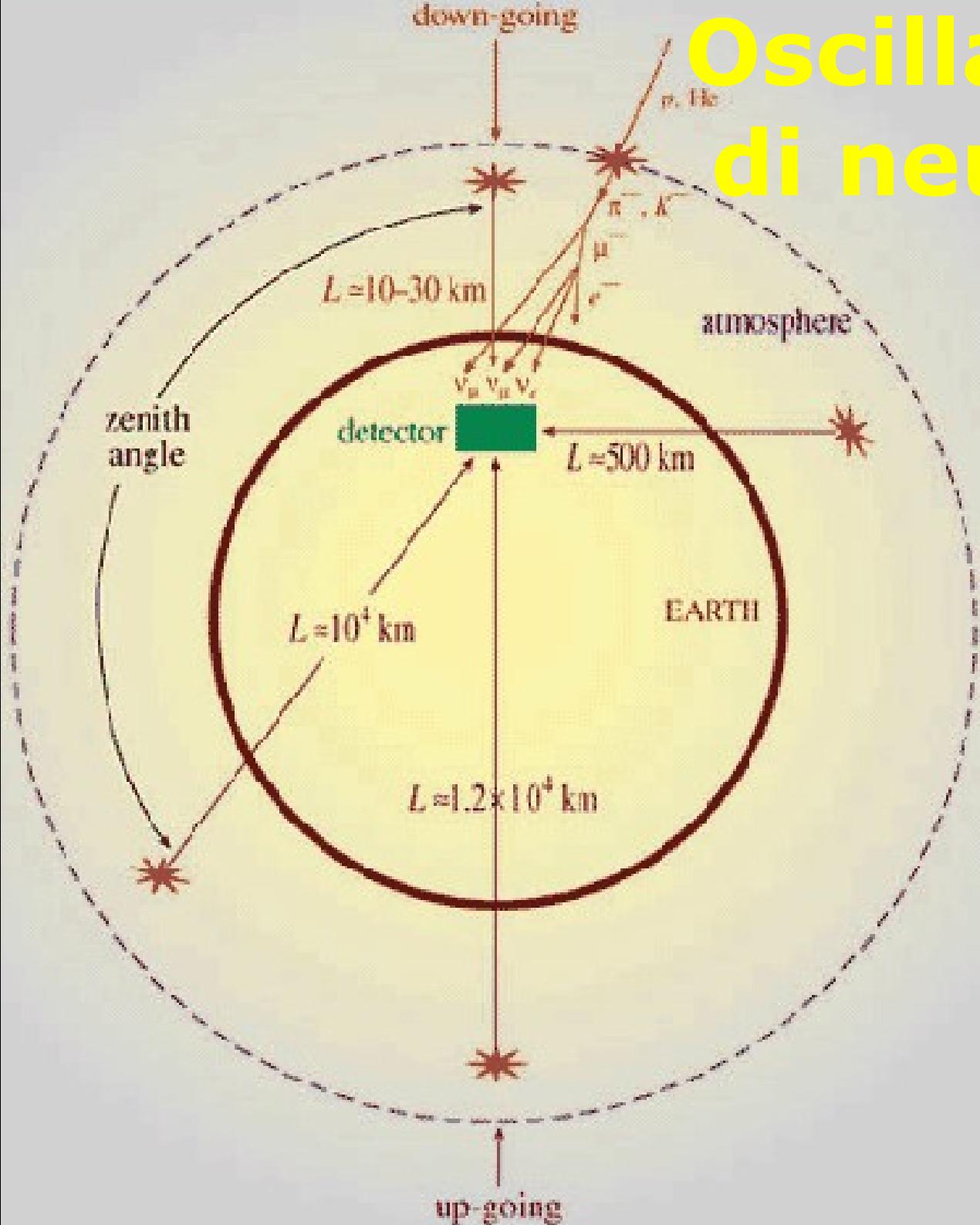


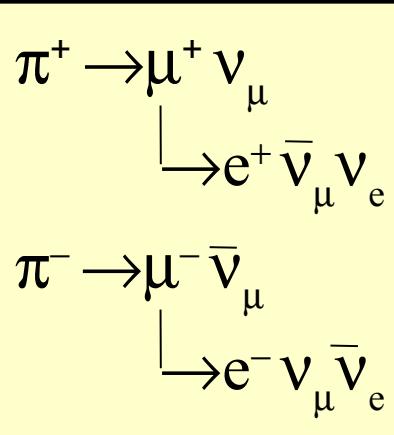
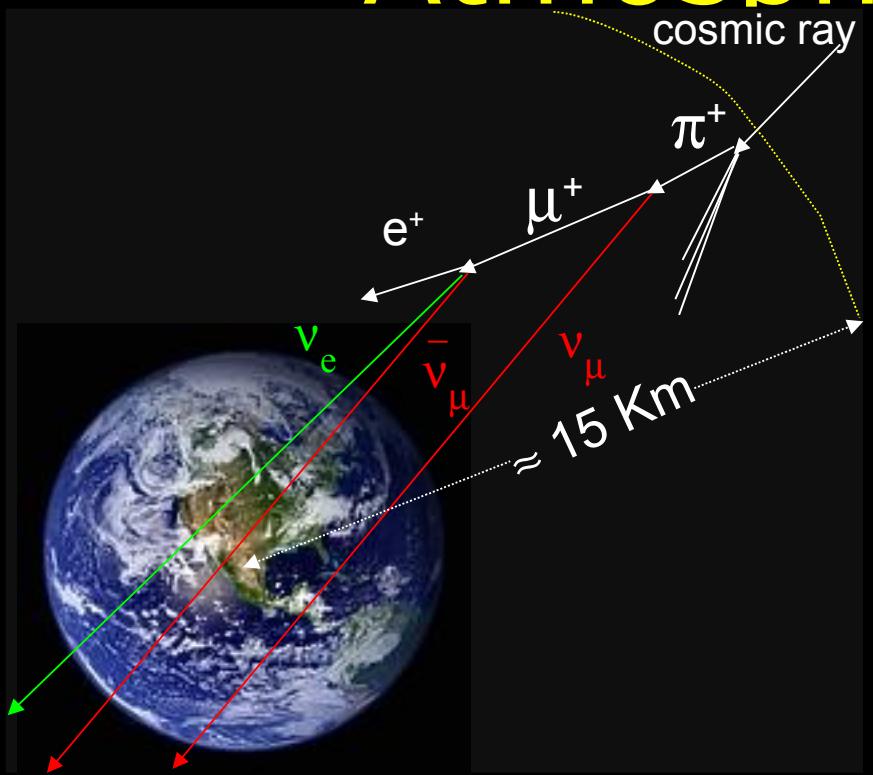
Oscillazioni di neutrini



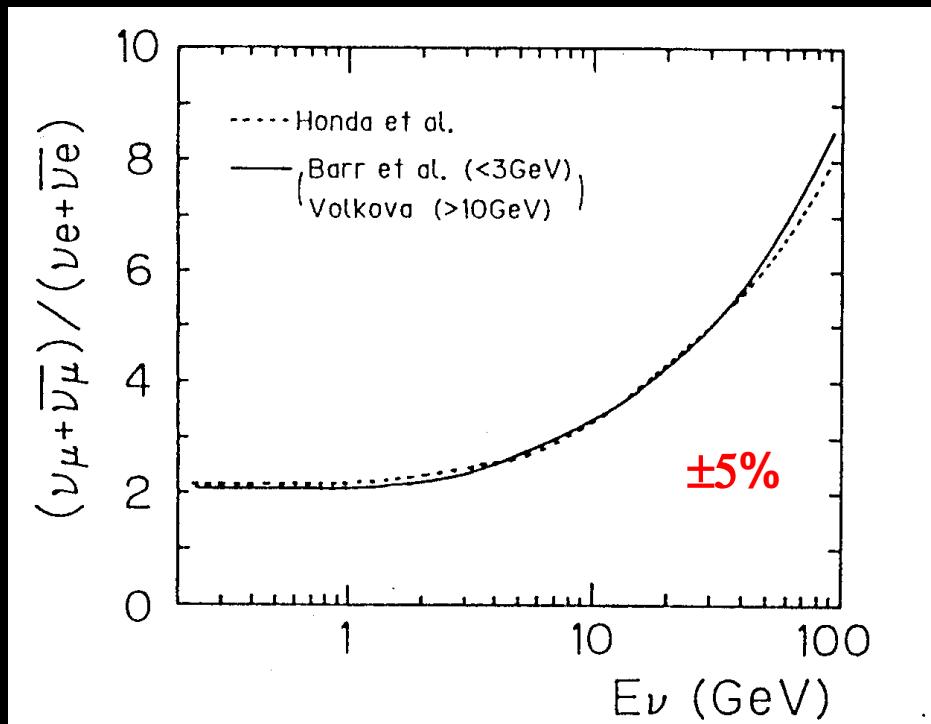
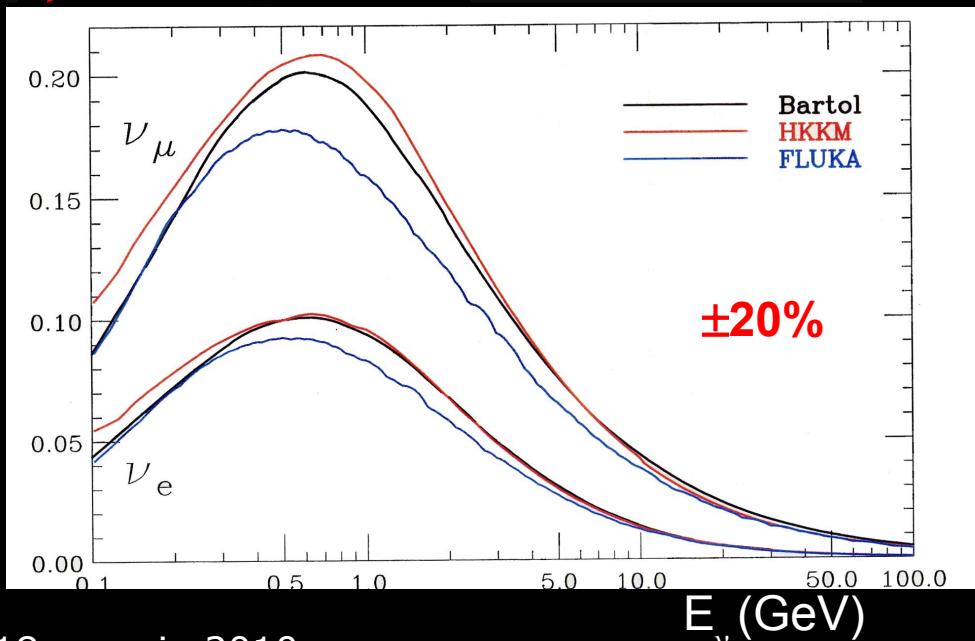
L. Ludovici
INFN/Roma

Pomeriggi Tematici
Roma, 12 maggio 2011

Atmospheric neutrinos



$$R(E) = \frac{(\nu_\mu + \bar{\nu}_\mu)}{(\nu_e + \bar{\nu}_e)} \xrightarrow{E \approx 1 \text{ GeV}} 2$$



ν_μ/ν_e Ratio (of Ratios)

Kamioka mines (3000t)

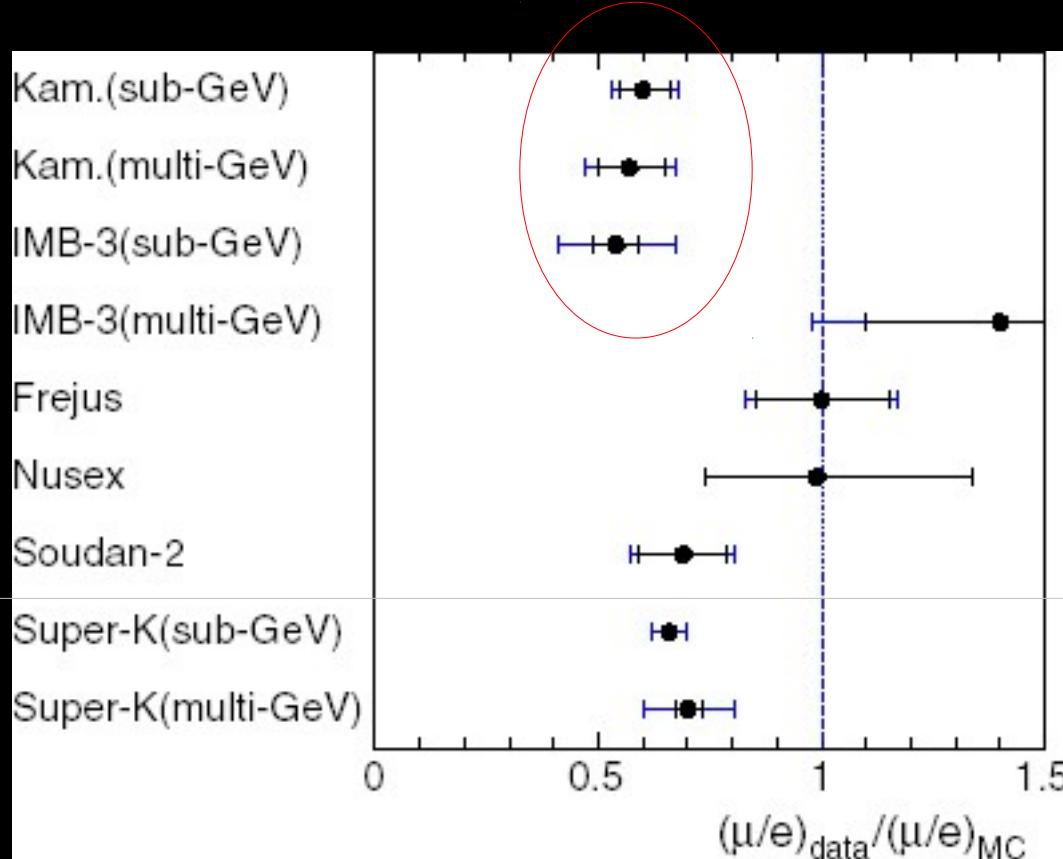
Morton salt mines (8000t)

Frejus (900t)

Mont Blanc (150t)

Soudan mines(960t)

Kamioka mines (50,000t)



Prime (contrastanti)
indicazioni

Prima indicazione del deficit di ν_μ dal rapporto ν_μ/ν_e (Kamiokande)

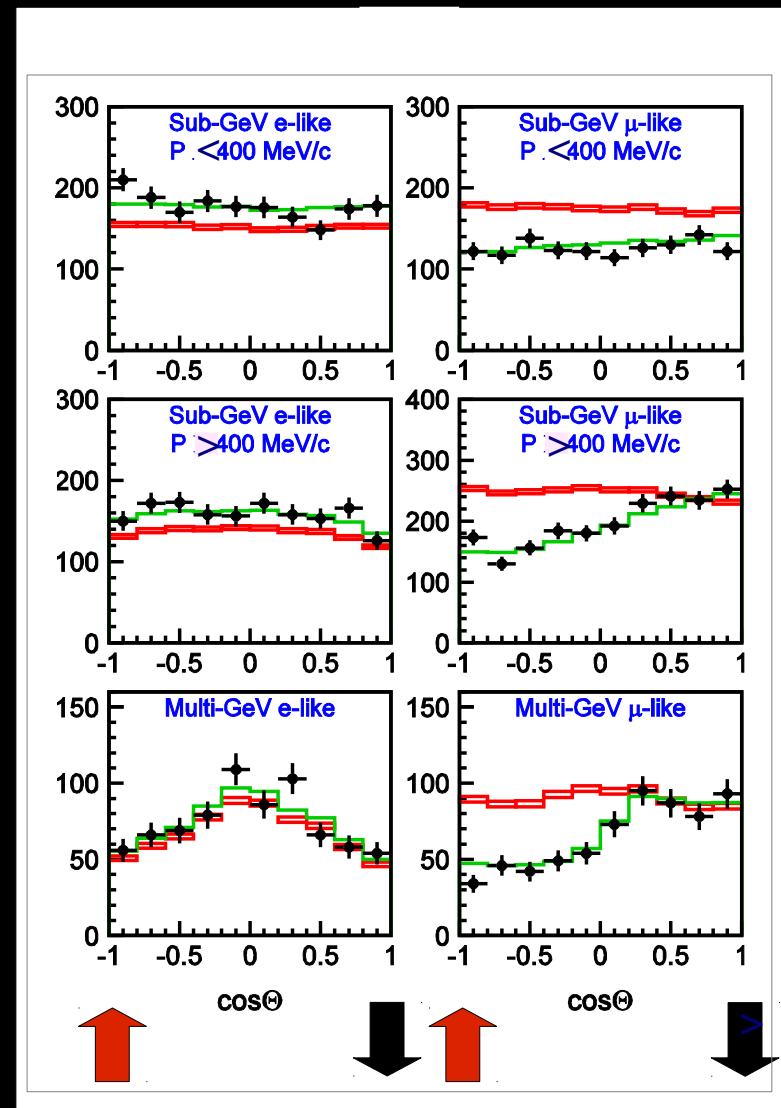
Indicazioni contrastanti negli anni '80



SK zenith angle dependence (1998)

“The data are consistent with two-flavor $\nu_\mu \rightarrow \nu_\tau$ oscillations with $\sin 2\theta > 0.82$ and $5 \cdot 10^{-4} < \Delta m^2 < 6 \cdot 10^{-3}$ eV 2 at the 90% confidence level.”

Phys.Rev.Lett. 81 (1998) 1562
(3500+ citations)



Neutrino Physics and oscillation

1930	ν existence postulated	Pauli
1934	ν interaction theory and name	Fermi
1938	Solar ν flux calculation	Bethe
1946	Idea of ν chlorine detector	Pontecorvo
1956	ν interactions observed	Reines & Cowan
1957	Idea of ν oscillation	Pontecorvo
1958	Left-handed ν	Goldhaber
1962	2 ν 's, ν_{μ}, ν_e	Lederman, Schwartz & Steinberger
1968	Solar neutrino deficit	Davis
1973	ν NC interactions observed	Gargamelle
1975	τ and the third ν	Perl
1986	Solar deficit again, atmospheric(?)	Kamiokande
1987	ν from SN1987A	Kamiokande, IMB
1989	3 light neutrino families	LEP Collaborations
1991	Solar deficit again	Gallex, SAGE
1998	Atmospheric ν oscillation	Super-Kamiokande
2002	Solar ν oscillation confirmed	SNO, KamLand
2005	Atmospheric ν oscillation confirmed	K2K

CHARM

(1976-1983)

CHARM2

(1983-93)

CHORUS

(1991-1998)

K2K

(1999-2004)

OPERA

(2007)

T2K

(2010)

Flavour Eigenstates

\mathbf{V}_e \mathbf{V}_μ \mathbf{V}_τ

$$\mathbf{U}\mathbf{U}^\dagger = \mathbf{U}^\dagger\mathbf{U} = \mathbf{1}$$

Mass Eigenstates

\mathbf{V}_1 \mathbf{V}_2 \mathbf{V}_3

$$| \nu_i \rangle = \sum_{\alpha=e,\mu,\tau} \mathbf{U}_{\alpha i} | \nu_\alpha \rangle$$

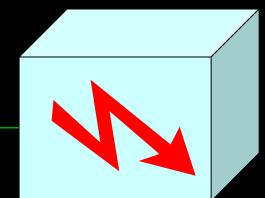
sorgente
di neutrini



autostato α
di sapore definito

propagazione

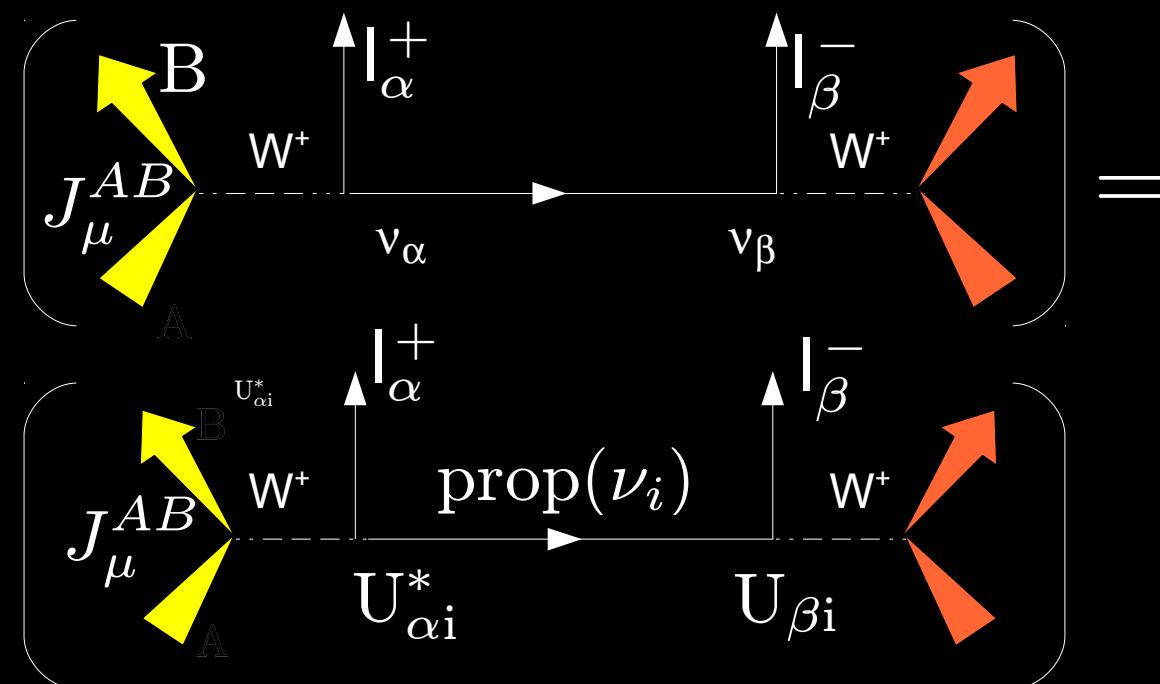
rivelatore



autostato β
di sapore definito

$$\pi^+ \rightarrow \mu^+ \nu$$

Amp



$$= \sum_i \text{Amp}$$

$$\nu_\tau N \rightarrow \tau^- N$$

Probabilità di oscillazione

$$\mathcal{P}_{\stackrel{(-)}{\nu_\alpha} \rightarrow \stackrel{(-)}{\nu_\beta}}(L, E) = \sum_k |\mathbf{U}_{\alpha k}|^2 |\mathbf{U}_{\beta k}|^2 + 2 \Re \sum_{k > j} \mathbf{W}_{kj}^{\alpha\beta} {}^{(*)} e^{-i \frac{\Delta m_{kj}^2}{2E}}$$

$$\mathbf{W}_{kj}^{\alpha\beta} = \mathbf{U}_{\alpha k}^* \mathbf{U}_{\beta k} \mathbf{U}_{\alpha j} \mathbf{U}_{\beta j}^*$$

$$\begin{aligned} \mathcal{P}_{\stackrel{(-)}{\nu_\alpha} \rightarrow \stackrel{(-)}{\nu_\beta}}(L, E) = & \sum_k |\mathbf{U}_{\alpha k}|^2 |\mathbf{U}_{\beta k}|^2 + 2 \sum_{k > j} \Re \{ \mathbf{W}_{kj}^{\alpha\beta} \} \cos \left(\frac{\Delta m_{kj}^2 L}{2E} \right) \\ & {}^{(+)}_(-) 2 \sum_{k > j} \Im \{ \mathbf{W}_{kj}^{\alpha\beta} \} \sin \left(\frac{\Delta m_{kj}^2 L}{2E} \right) \end{aligned}$$

$$\begin{aligned} \mathcal{P}_{\stackrel{(-)}{\nu_\alpha} \rightarrow \stackrel{(-)}{\nu_\beta}}(L, E) = & \delta_{\alpha\beta} + 4 \sum_{k > j} \Re \{ \mathbf{W}_{kj}^{\alpha\beta} \} \sin^2 \left(\frac{\Delta m_{kj}^2 L}{4E} \right) \\ & {}^{(+)}_(-) 2 \sum_{k > j} \Im \{ \mathbf{W}_{kj}^{\alpha\beta} \} \sin \left(\frac{\Delta m_{kj}^2 L}{2E} \right) \end{aligned}$$

Probabilità per due famiglie

$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \mathbf{U} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix} \quad \mathbf{U} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \quad \Delta m^2 = m_2^2 - m_1^2$$

$$\mathcal{P}_{\nu_\alpha \rightarrow \nu_\beta} = \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E} \right)$$

Importante storicamente e nella pratica degli esperimenti di oscillazione
Approssimazione delle formule generali valida in molti casi

Formule approssimate

Esperimenti a distanze terrestri, con $\Delta m_{12} L/E \ll 1$, sono descritti solo da 3 parametri: θ_{23} , Δm_{12} , θ_{13} e da formule simili a quelle per 2 famiglie:

$$P(\nu_e \rightarrow \nu_\mu) \approx \sin^2 \theta_{23} \sin^2 2\theta_{13} \sin^2 \Delta_{23} = \sin^2 2\theta_{\mu e} \sin^2 \Delta_{23}$$

$$P(\nu_\mu \rightarrow \nu_\tau) \approx \cos^4 \theta_{13} \sin^2 2\theta_{23} \sin^2 \Delta_{23} = \sin^2 2\theta_{\mu \tau} \sin^2 \Delta_{23}$$

$$P(\nu_e \rightarrow \nu_\tau) \approx \cos^2 \theta_{23} \sin^2 2\theta_{13} \sin^2 \Delta_{23} = \sin^2 2\theta_{e \tau} \sin^2 \Delta_{23}$$

$$P(\nu_\mu \rightarrow \nu_\mu) \approx 1 - (\sin^2 2\theta_{\mu \tau} + \sin^2 2\theta_{\mu e}) \sin^2 \Delta_{23}$$

$$P(\nu_e \rightarrow \nu_e) \approx 1 - \sin^2 2\theta_{13} \sin^2 \Delta_{23}$$

Angoli di mixing efficaci:

$$\sin^2 2\theta_{\mu e} = \sin^2 \theta_{23} \sin^2 2\theta_{13} \approx 0.5 \sin^2 2\theta_{13}$$

$$\sin^2 2\theta_{\mu \tau} = \cos^4 \theta_{13} \sin^2 2\theta_{23} \approx \sin^2 2\theta_{23}$$

$$\sin^2 2\theta_{e \tau} = \cos^2 \theta_{23} \sin^2 2\theta_{13} \approx 0.5 \sin^2 2\theta_{13}$$

Parametrizzazione della matrice di mixing

$$U = R_{23} R_{13}^C R_{12} D(\phi_2, \phi_3)$$

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & e^{-i\delta} s_{13} \\ 0 & 1 & 0 \\ -e^{i\delta} s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\phi_2} & 0 \\ 0 & 0 & e^{i\phi_3} \end{pmatrix}$$

atmosferici

“terra incognita”

solari

$\Delta L=2$

Still unmeasured:
CHOOZ limit:
 $\sin^2(2\theta_{13}) < 0.15$ (90% CL)

SK, K2K, MINOS

$\sin^2(2\theta_{23}) > 0.92$ (90% CL)

$\Delta m^2_{23} = 2.43 \pm 0.13 \times 10^{-3} \text{ eV}^2$

KAMLAND, SNO

$\sin^2(2\theta_{12}) = 0.87 \pm 0.03$

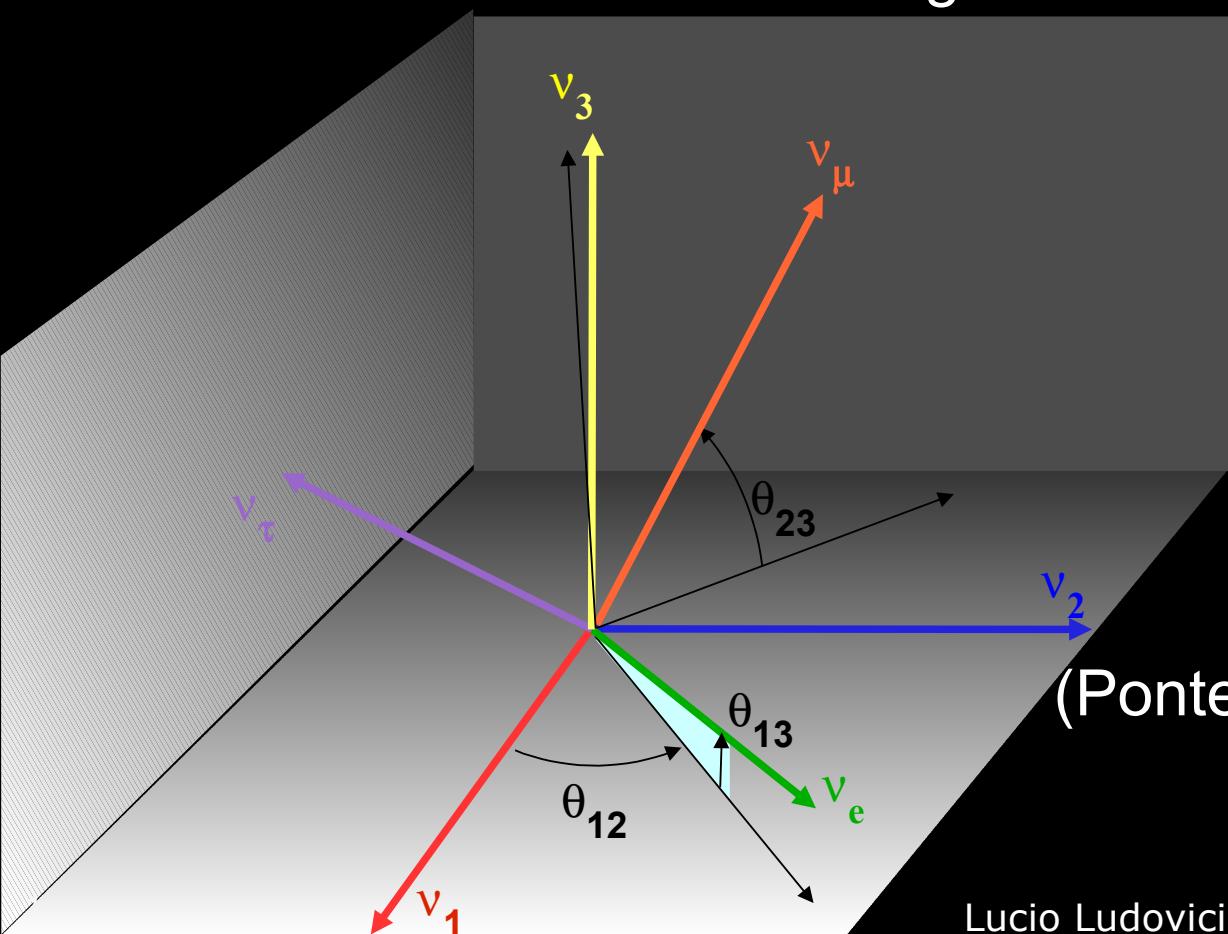
$\Delta m^2_{12} = 7.59 \pm 0.20 \times 10^{-5} \text{ eV}^2$

Parametrizzazione della matrice di mixing

$$U = R_{23} R_{13}^C R_{12} D(\phi_2, \phi_3)$$

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & e^{-i\delta} s_{13} \\ 0 & 1 & 0 \\ -e^{i\delta} s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\phi_2} & 0 \\ 0 & 0 & e^{i\phi_3} \end{pmatrix}$$

atmosferici “terra incognita” solari $\Delta L=2$



3 neutrini:
 θ_{12} θ_{23} θ_{13} δ
(+ $2\Delta m^2$ indipendenti)

Matrice PMNS
(Pontecorvo-Maki-Nakagawa-Sakata)

Violazione di CP leptonica

$$\mathcal{A}_{\alpha\beta}^{CP} = \frac{\mathcal{P}_{\nu_\alpha \rightarrow \nu_\beta} - \mathcal{P}_{\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta}}{\mathcal{P}_{\nu_\alpha \rightarrow \nu_\beta} + \mathcal{P}_{\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta}}$$

$$\mathcal{A}_{\alpha\beta}^{CP} = \frac{2 \sum_{k>j} \Im\{W_{kj}^{\alpha\beta}\} \sin\left(\frac{\Delta m_{kj}^2 L}{2E}\right)}{\delta_{\alpha\beta} - 4 \sum_{k>j} \Re\{W_{kj}^{\alpha\beta}\} \sin^2\left(\frac{\Delta m_{kj}^2 L}{4E}\right)}$$

Invariante di Jarlskog

$$J_{\alpha\beta;kj} = \Im\{U_{\alpha k}^* U_{\beta k} U_{\alpha j} U_{\beta j}^*\} = \pm J$$

Analogo all'area dei triangoli unitari in CKM: $J_{CKM} \approx 3 \cdot 10^{-5}$

$$J = \frac{1}{4} \sin 2\theta_{12} \sin 2\theta_{23} \cos^2 \theta_{13} \sin \theta_{13} \sin \delta \approx 0.23 \sin \theta_{13} \sin \delta$$

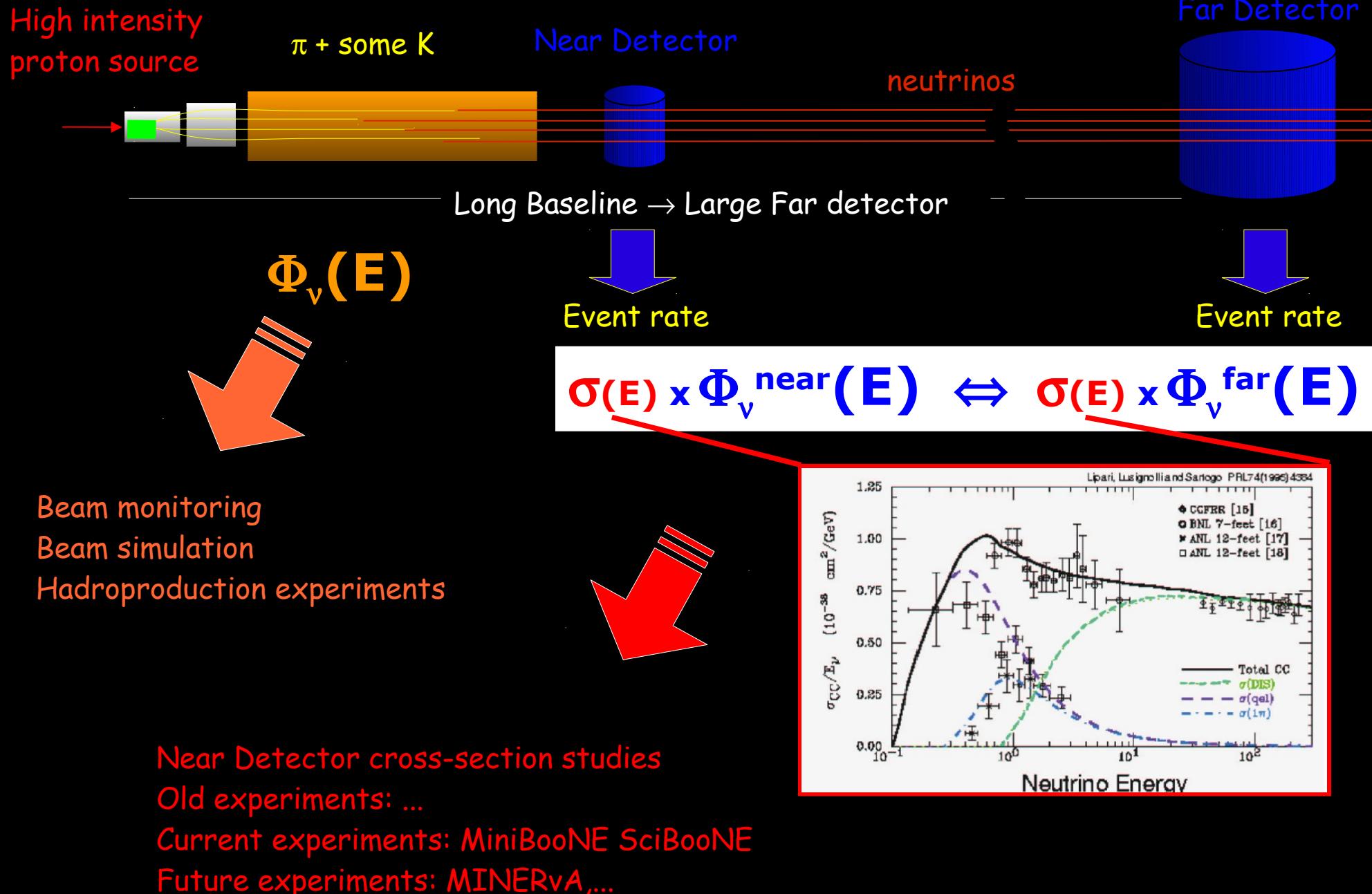
La possibilità di misurare CP è legata al valore di θ_{13}

Conferma agli acceleratori delle oscillazioni degli atmosferici

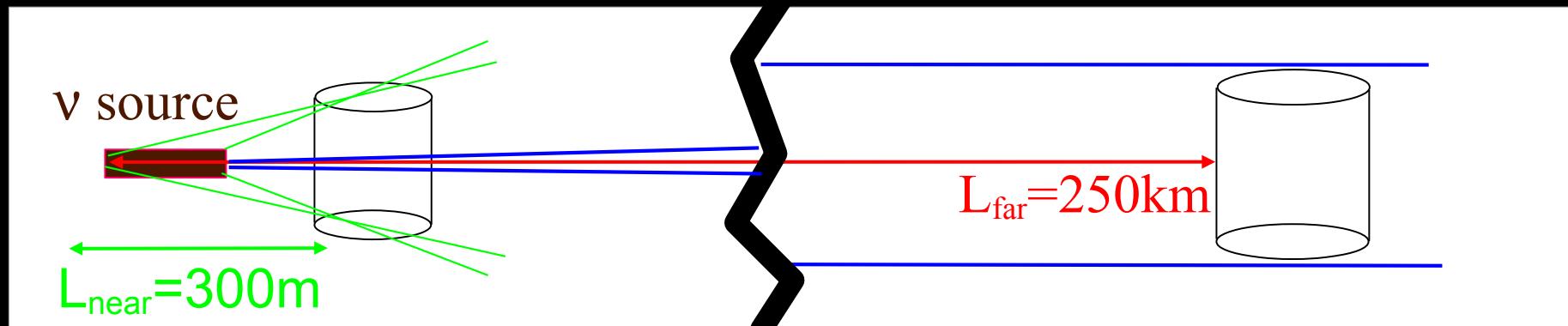
$$\Delta m^2 \text{ L/E}$$

Long Baseline

Experimental Strategy

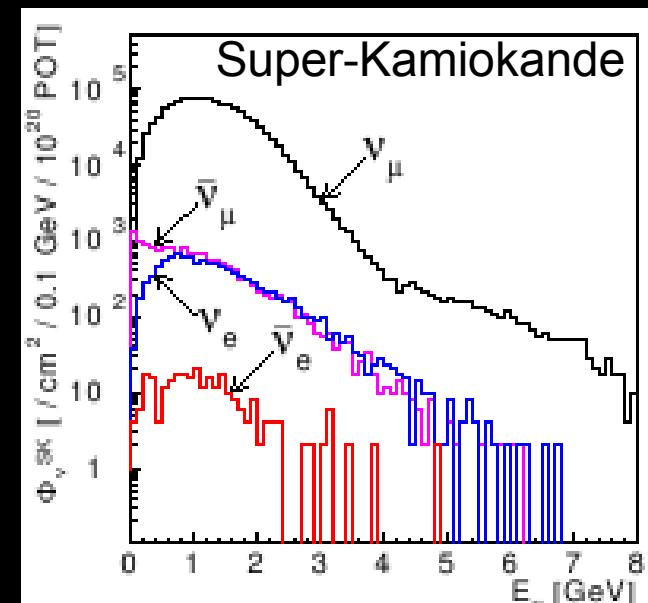
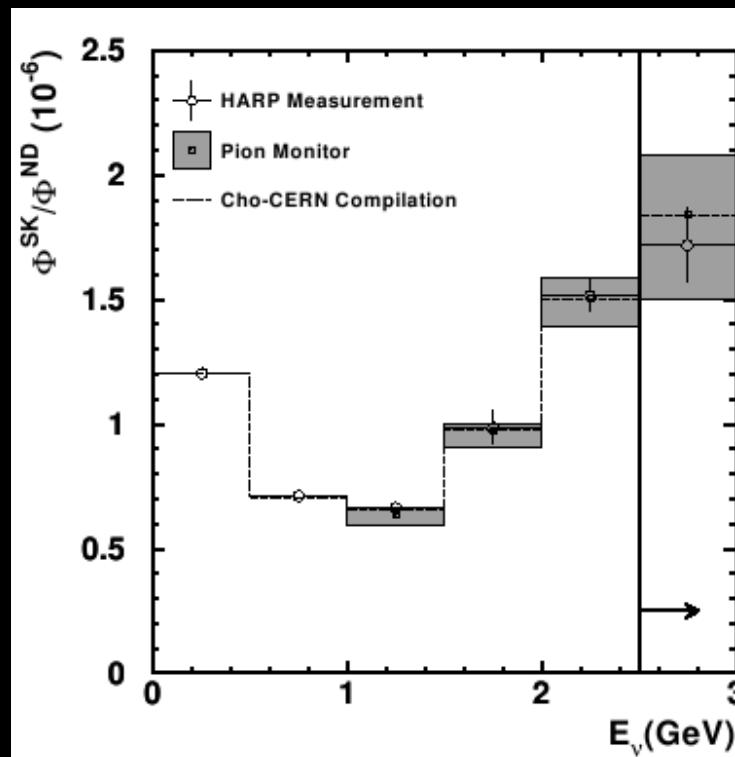
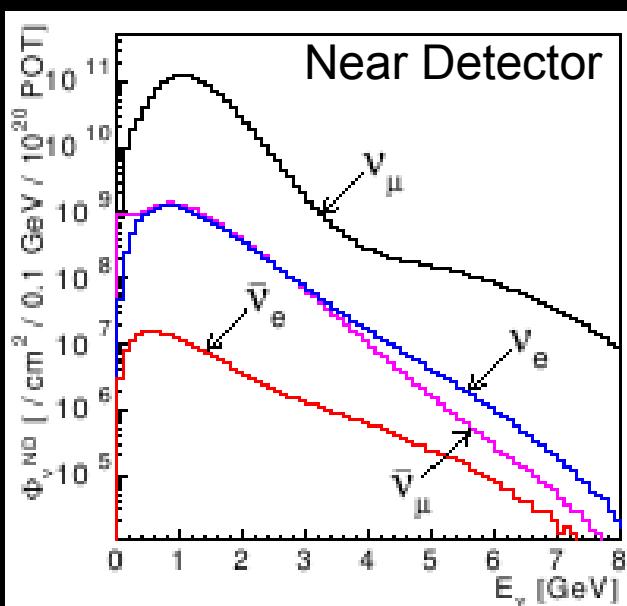


Far/Near Ratio

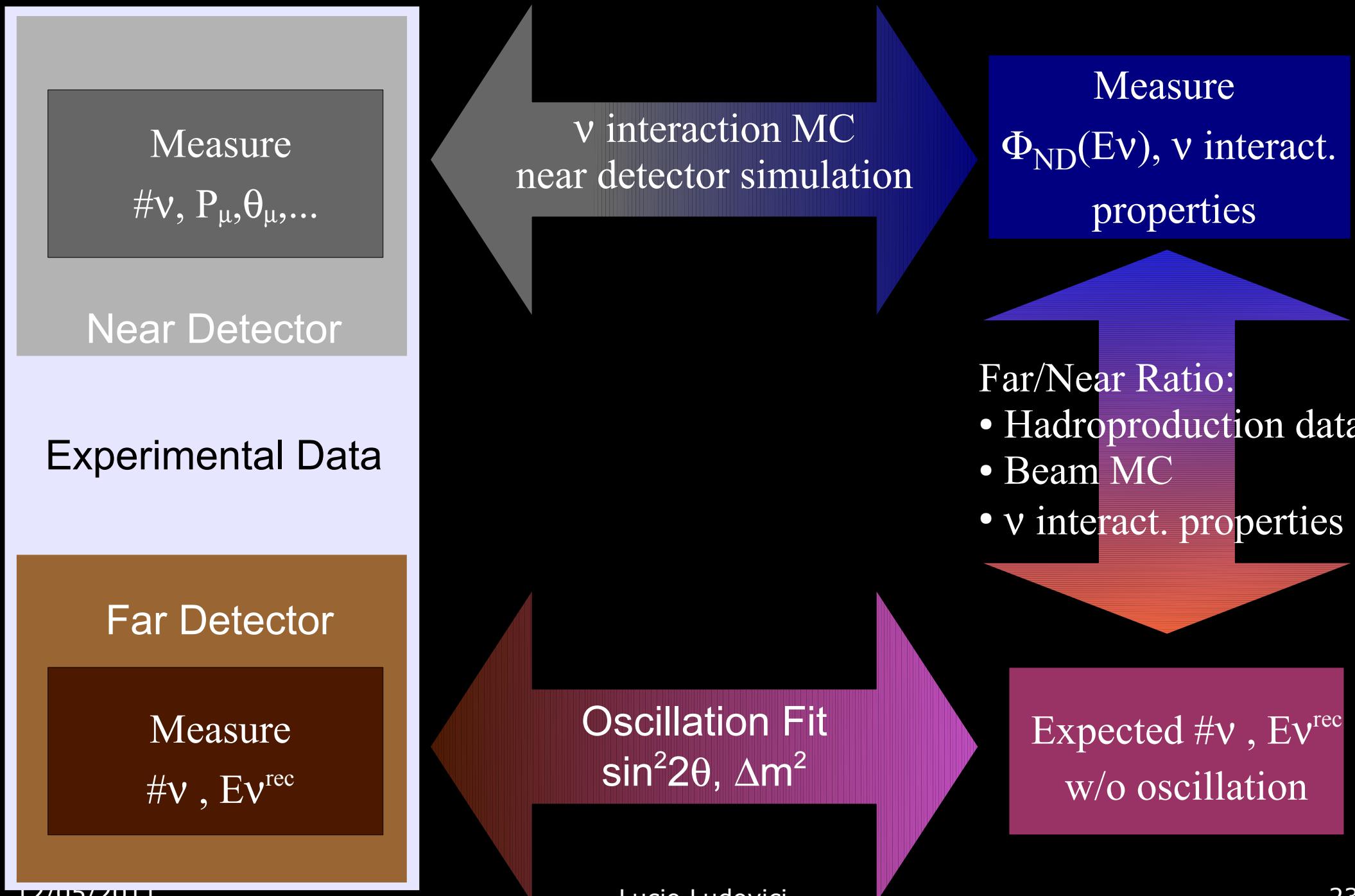


Extended neutrino source
Near vs Far solid angle

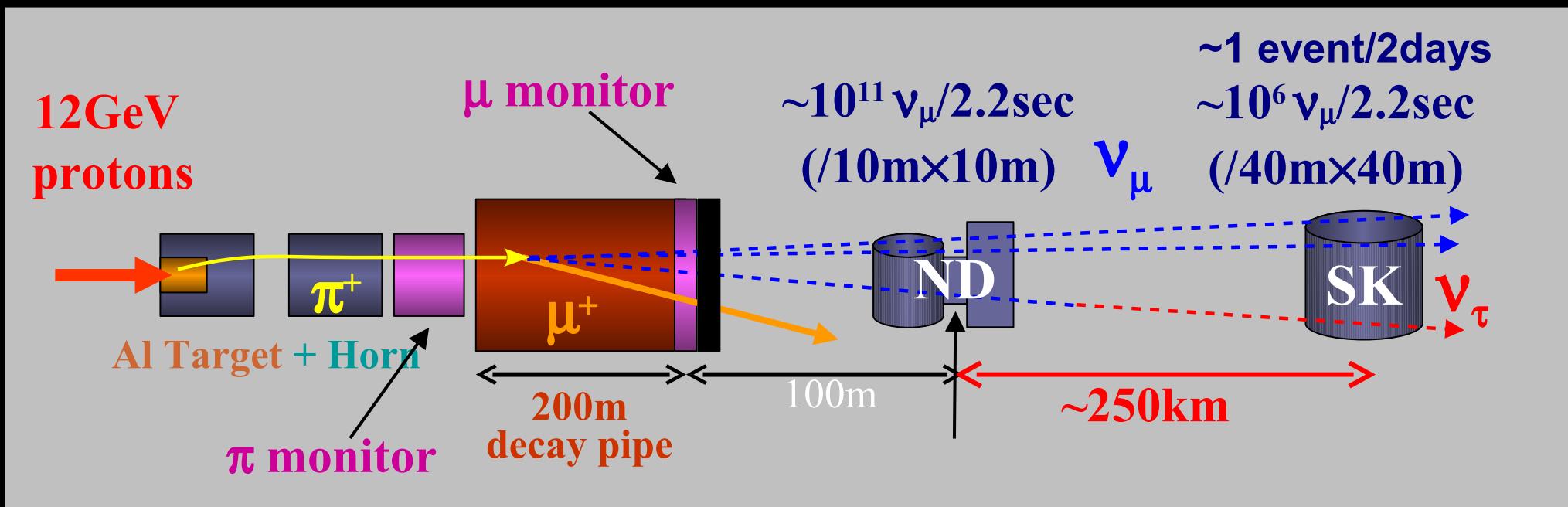
$$R_N/F(E_\nu) \neq (L_{\text{near}}/L_{\text{far}})^2 \sim 10^{-6}$$



Analysis Strategy



K2K Conceptual Layout

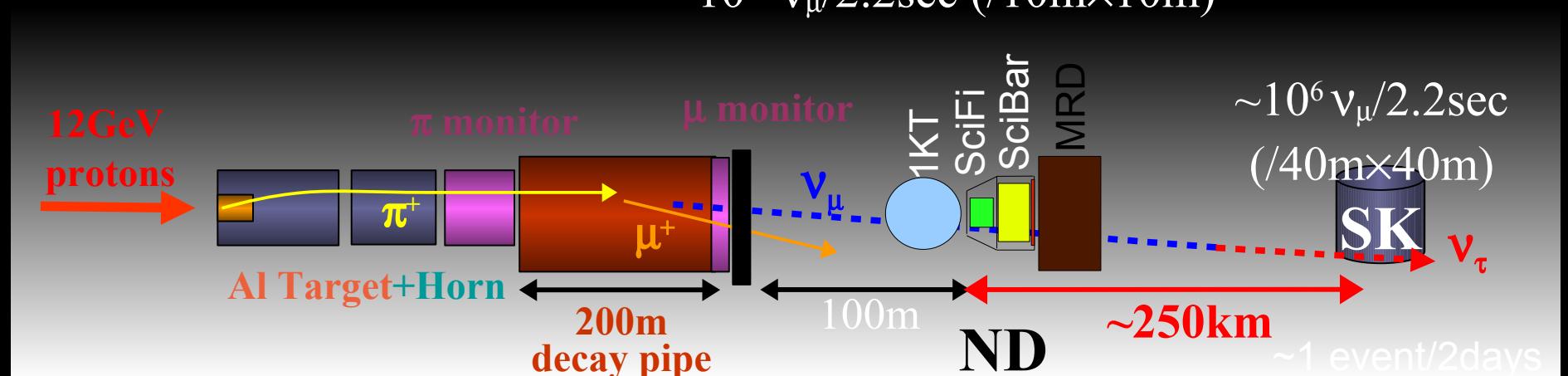


Signature of neutrino oscillation

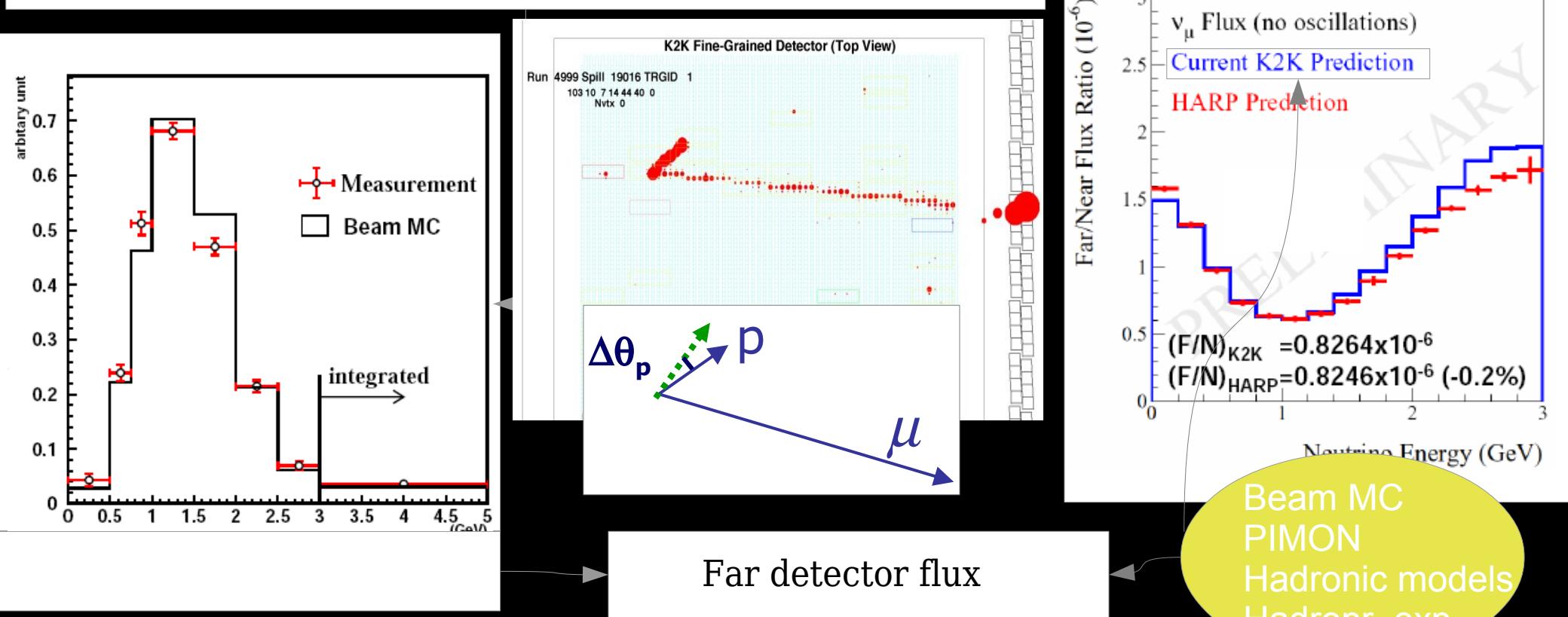
1. Reduction of ν_μ events
2. Distortion of ν_μ energy spectrum

K2K Layout and Strategy

$\sim 10^{11} \nu_\mu / 2.2 \text{sec}$ ($/10\text{m} \times 10\text{m}$)



Combined (1KT,SciFi,SciBar) fit of P_μ, θ_μ distributions





GPS

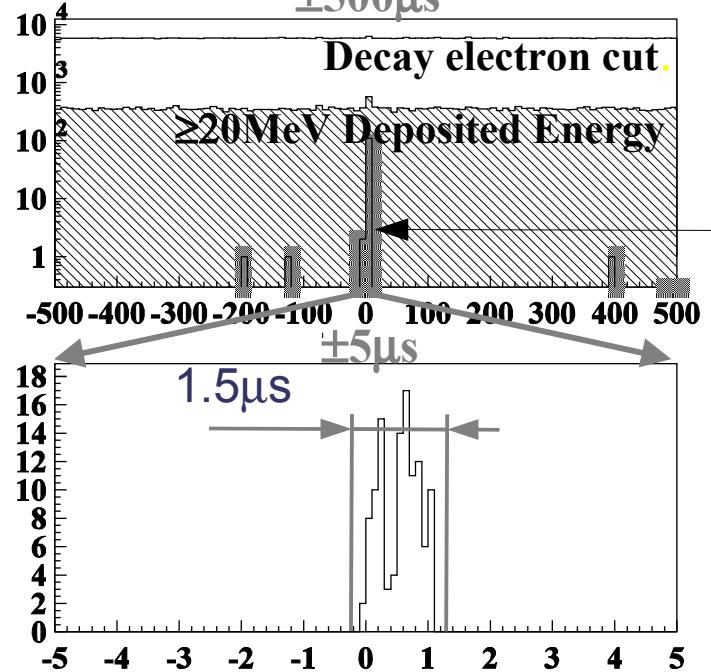
 T_{spill}

GPS

ToF=0.83ms

 $\pm 500\mu\text{s}$

Decay electron cut.

 $\geq 20\text{MeV Deposited Energy}$ 

K2K	DATA	MC
FC 22.5kt	112	155.9
1-Ring	67	99.0
1-R μ -like	58	90.8
1-R e-like	9	8.2
Multi Ring	45	56.8

$$E_{\nu}^{\text{rec}} = \frac{(m_N - V)E_{\mu} - m_{\mu}^2/2 + m_N V - V^2/2}{(m_N - V) - E_{\mu} + p_{\mu} \cos \theta_{\mu}}$$

+11.5 (7.4%)
-10.2 (6.5%)

Absolute Deficit
 3.1σ

Shape Distortion
 2.8σ

No Activity in Outer Detector
Event Vertex in Fiducial Volume
More than 30MeV Deposited Energy

No Oscillation
0.003%
 4.2σ

Best fit value (all region)

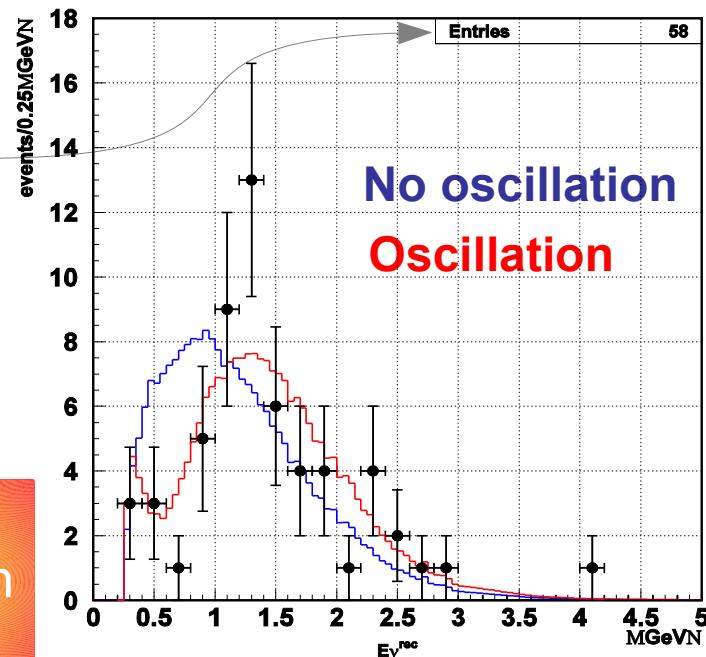
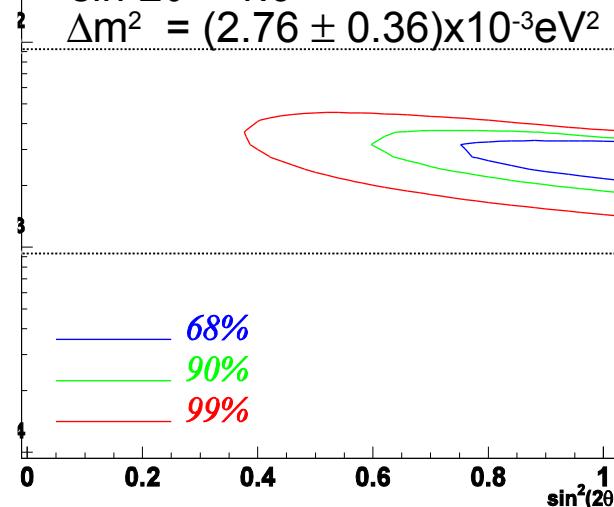
$$\sin^2 2\theta = 1.19 \pm 0.23$$

$$\Delta m^2 = (2.55 \pm 0.40) \times 10^{-3} \text{ eV}^2$$

(in physical region)

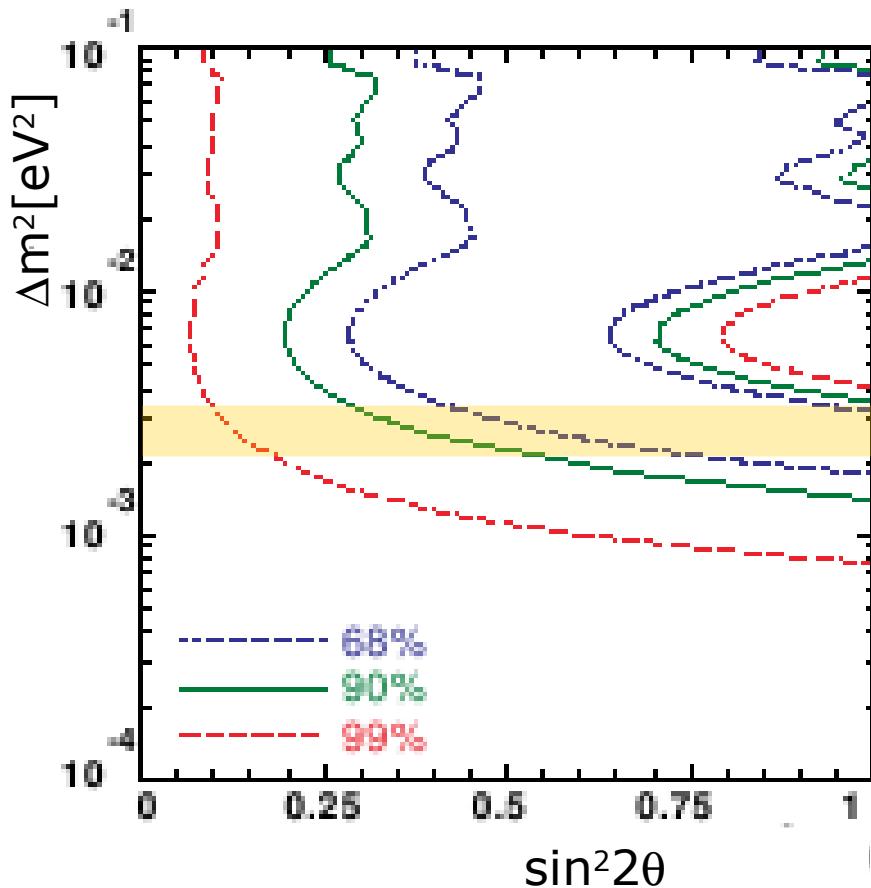
$$\sin^2 2\theta = 1.0$$

$$\Delta m^2 = (2.76 \pm 0.36) \times 10^{-3} \text{ eV}^2$$

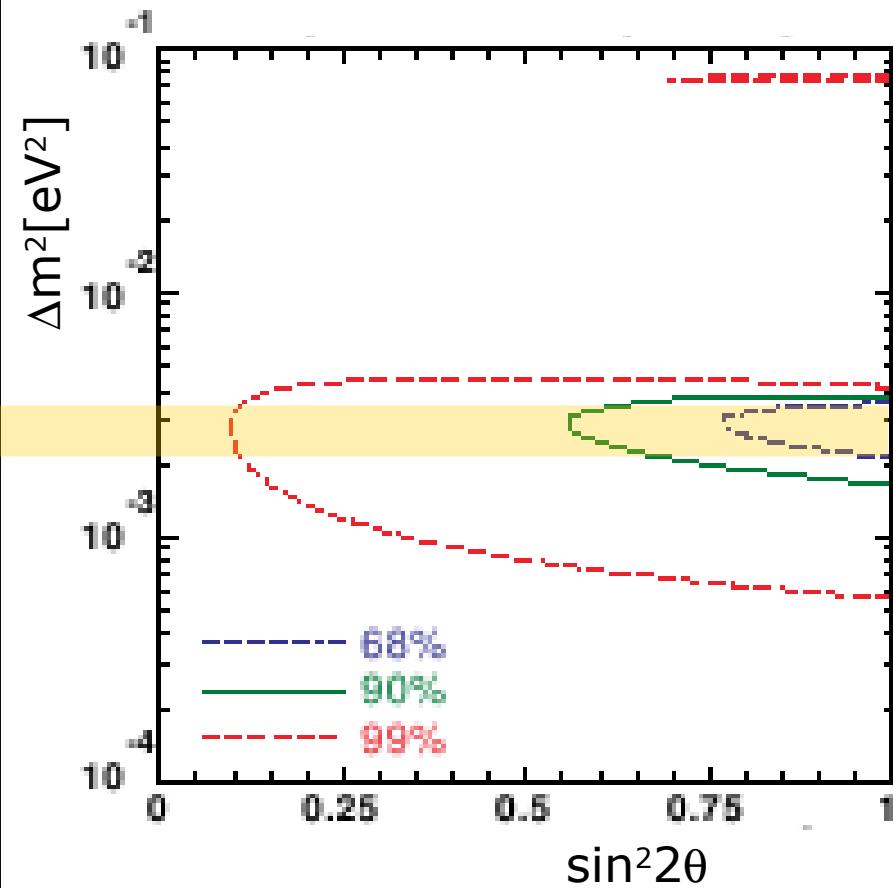


Disappearance & Shape

ABSOLUTE DEFICIT

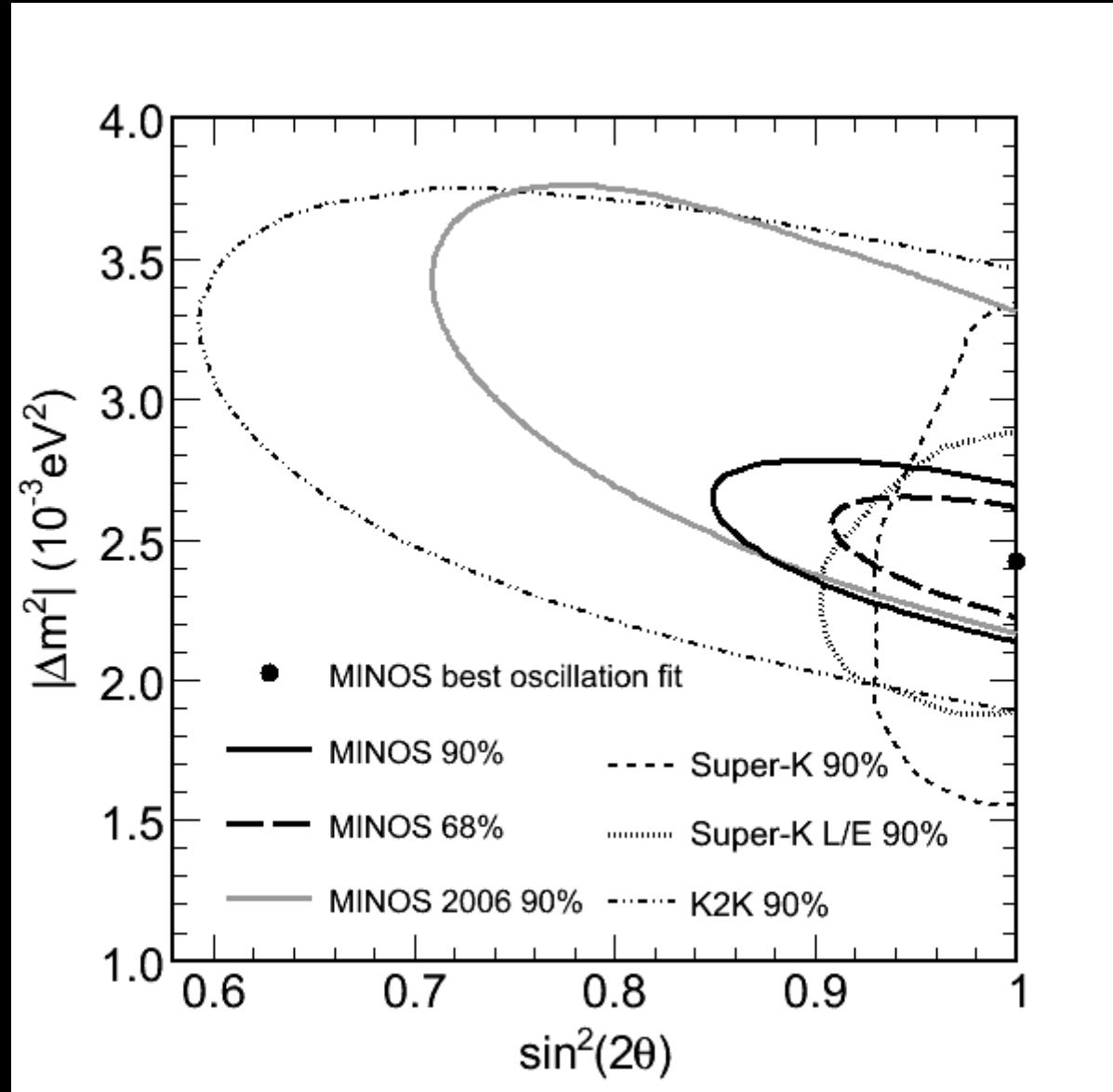


ENERGY SPECTRUM DISTORTION



Allowed regions from ν_μ disappearance and distortion of E_ν spectrum are consistents

Minos (Fermilab→Soudan)



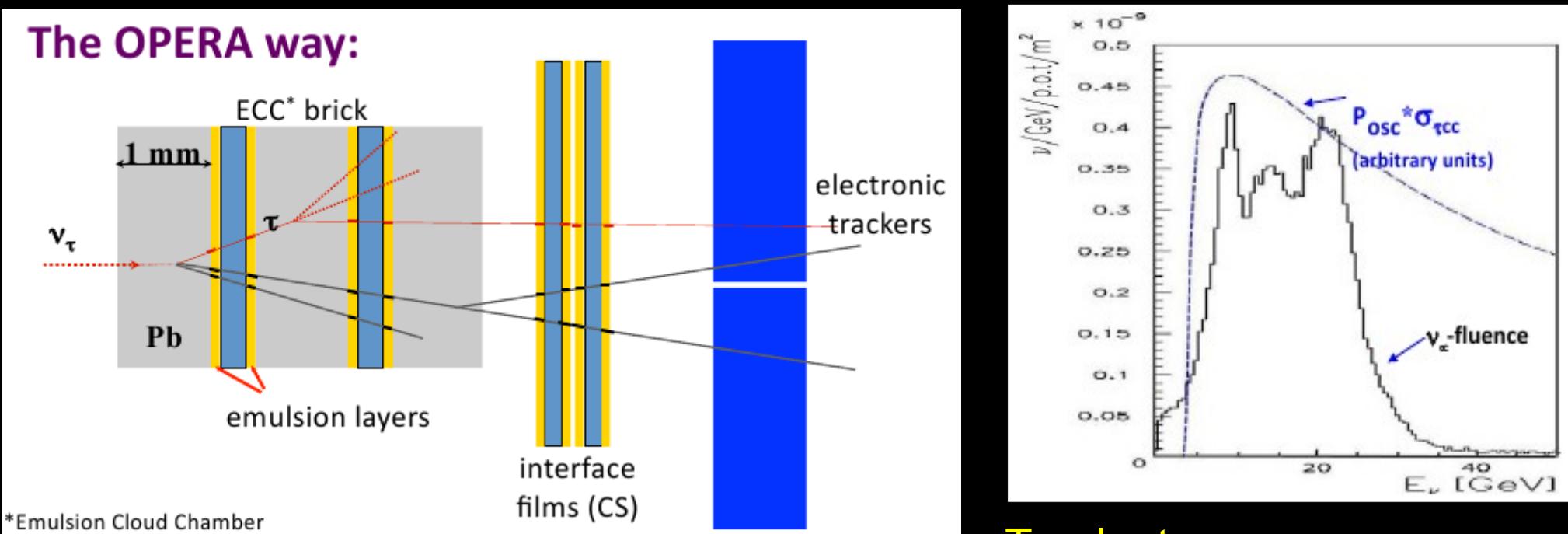
OPERA: $\nu_\mu \rightarrow \nu_\tau$ appearance

$$N_\tau \propto M_D \int \Phi_{\nu_\mu}(E) P_{\nu_\mu \rightarrow \nu_\tau}(E, \Delta m^2) \sigma_{\nu_\tau}(E) \epsilon(E) dE$$

Small interaction probability: large detector mass $\approx 1kT$

Small signal/background: high resolution $\approx 1\mu\text{m}$

Cross-section threshold: large energy $\approx 20\text{GeV}$

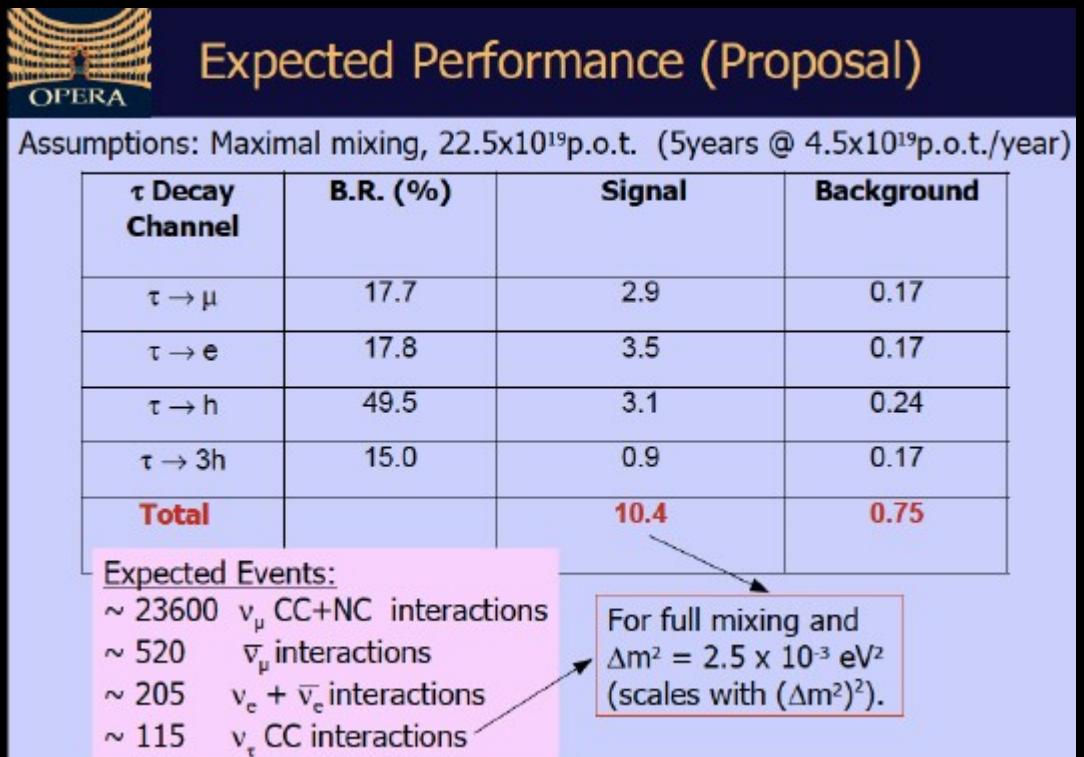
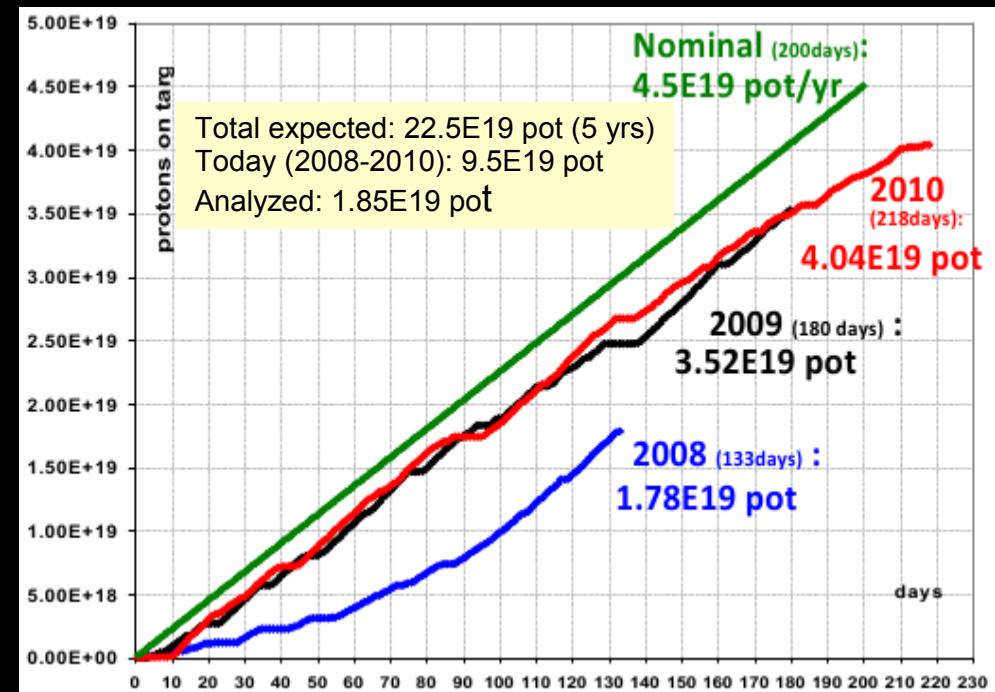


Tau lepton
Impact Parameter $c\tau \sim 87\mu\text{m}$
Track length $c\tau\gamma \sim 1\text{mm}$

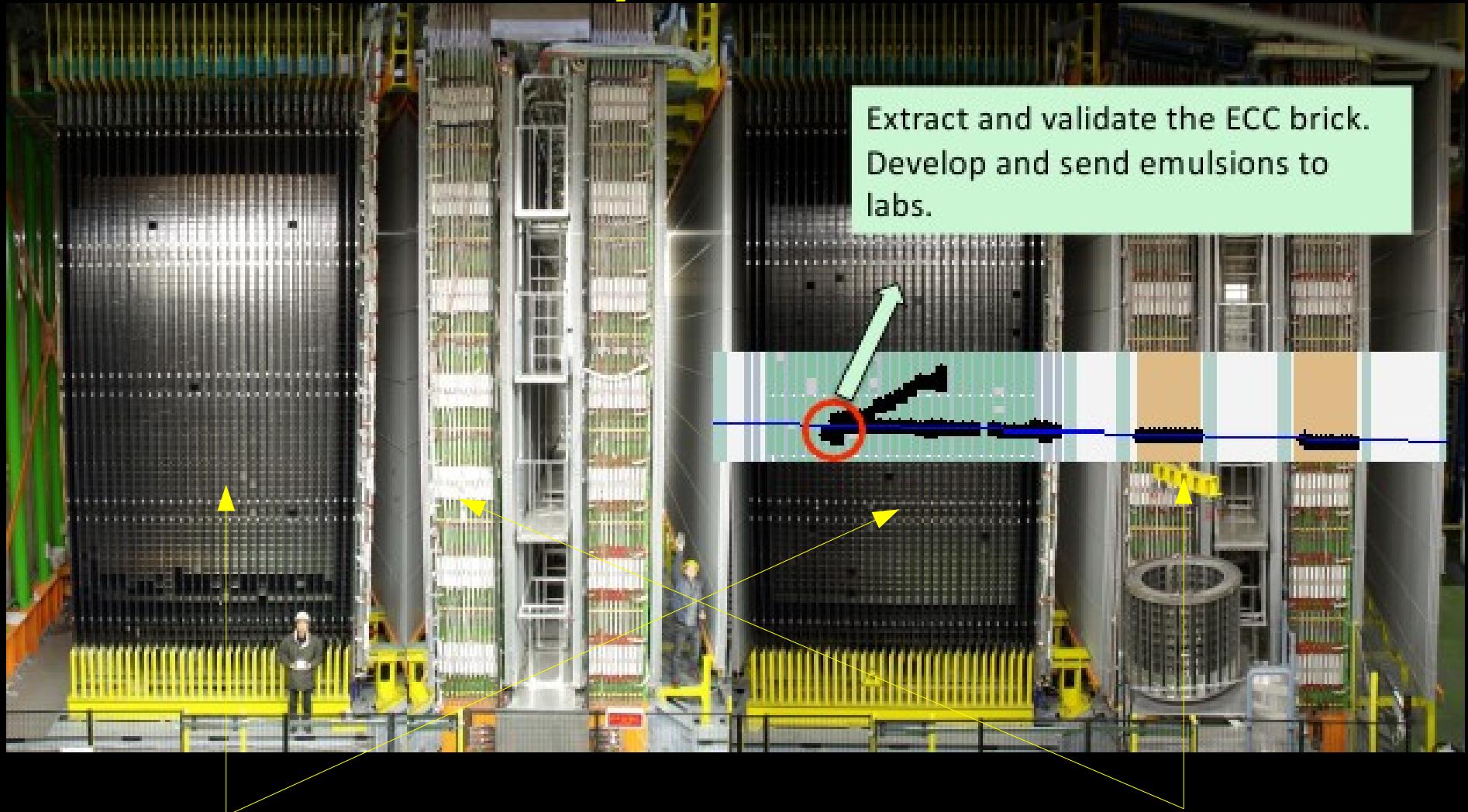
The CNGS beam



$\langle E_n \rangle$	17.7 GeV
L	730 km
$(N\nu_e + N\bar{\nu}_e)/N\nu_\mu$	0.87%
$N\nu_\mu/N\bar{\nu}_\mu$	2.1%
Prompt ν_τ	Negligible



OPERA Hybrid Detector



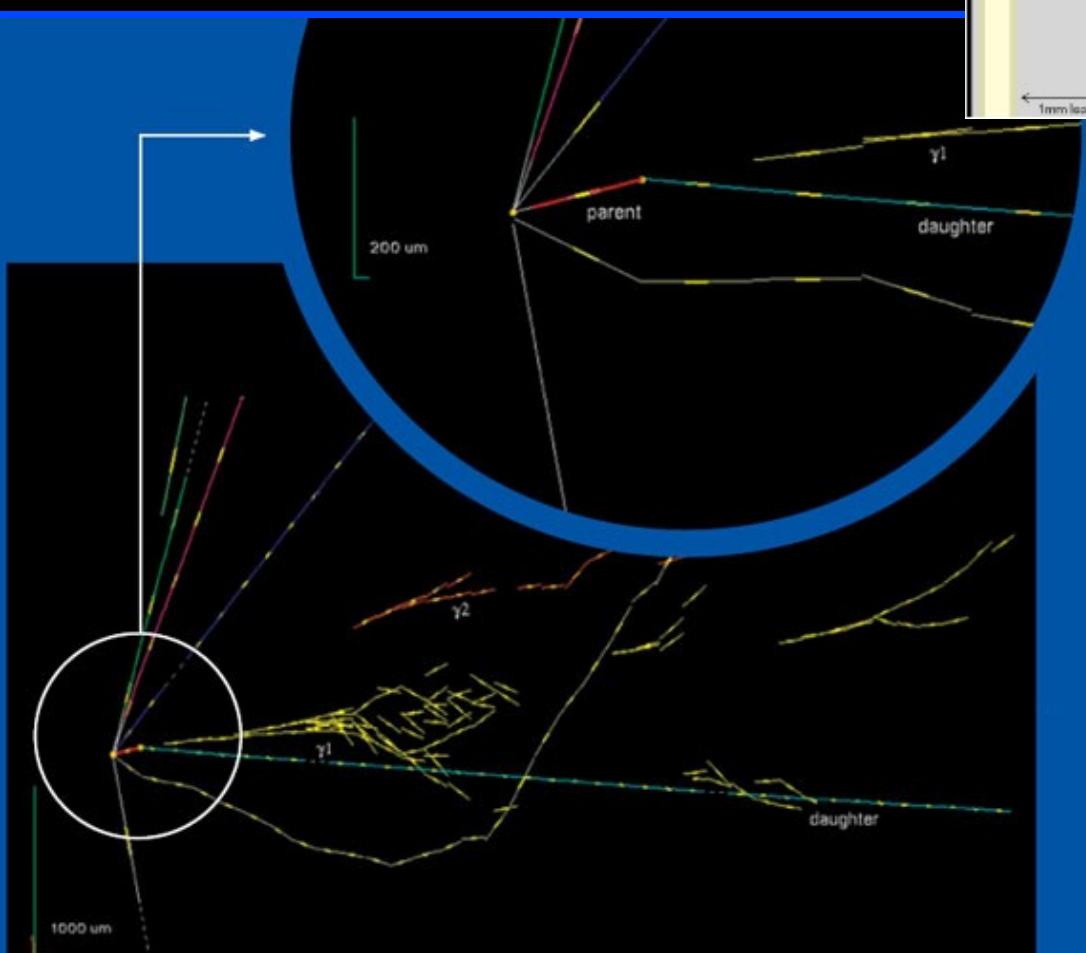
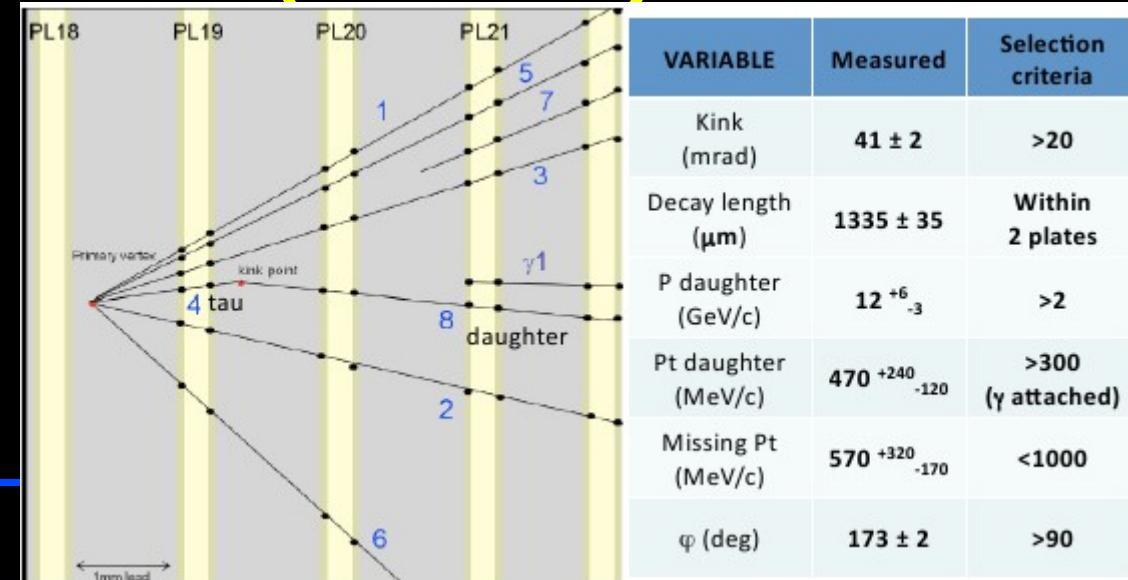
TARGETS

Target tracker (scintillators)
Lead/Emulsion Bricks (75,000x2)
Target mass~1.25 kt

MUON SPECTROMETERS

Iron + RPCs
Precision Tracker: 6 drift tubes planes

**Event number 9234119599,
22 August 2009, 19:27 (UTC)**

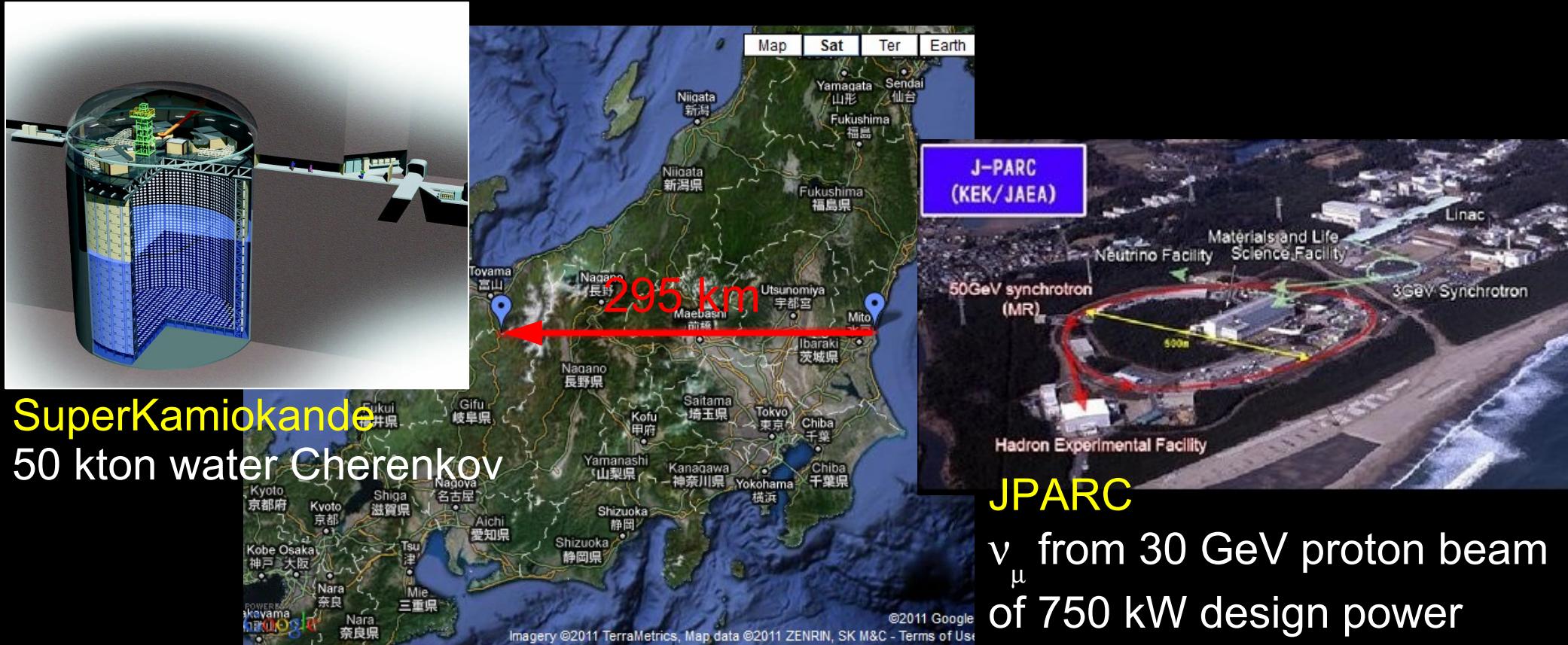


Probability of backg. fluctuation
(only 1 prong)

4.5%
(1.8%)

Statistical significance
 2.01σ
(2.36σ)

T2K (Tokai to Kamioka) experiment



Goals

1. ν_e appearance (θ_{13} “discovery”)
2. ν_μ disappearance ($\theta_{23}, \Delta m^2_{23}$ precise measurement)

Off-Axis neutrino Beams

BNL proposal E889 <http://minos.phy.bnl.gov/nwg/papers/E889>



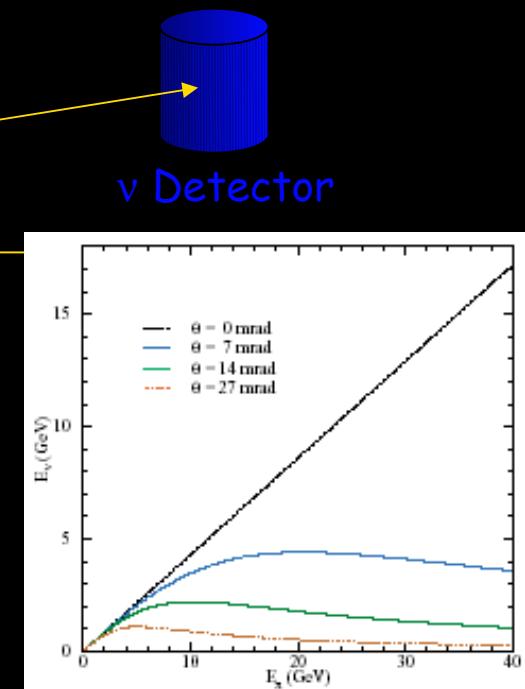
$$E_\nu = \frac{m_\pi^2 - m_\mu^2}{2(E_\pi - p_\pi \cos\theta)}$$

$$\Phi_\nu = \frac{1}{4\pi L^2} \frac{m_\pi^2}{(E_\pi - p_\pi \cos\theta)^2}$$

$E_\pi \gg m_\pi$, and $\theta \ll 1$

$$\frac{m_\pi^2 - m_\mu^2}{m_\pi^2 (1 + \gamma_\pi^2 \theta^2)} E_\pi$$

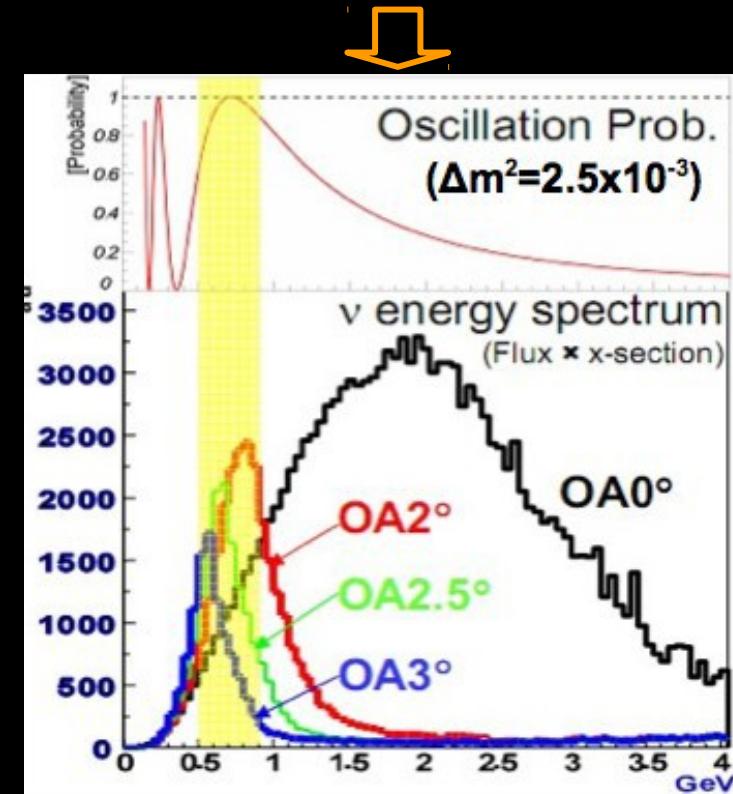
$$\frac{1}{\pi L^2} \left(\frac{E_\pi}{m_\pi} \right)^2 \frac{1}{(1 + \gamma_\pi^2 \theta^2)^2}$$



Much higher flux than old-style NBB.
Strong cut-off of HE tail: reduced NC π^0 bckg.
Reduced ν_e contamination.
Tune energy to maximise sensitivity:

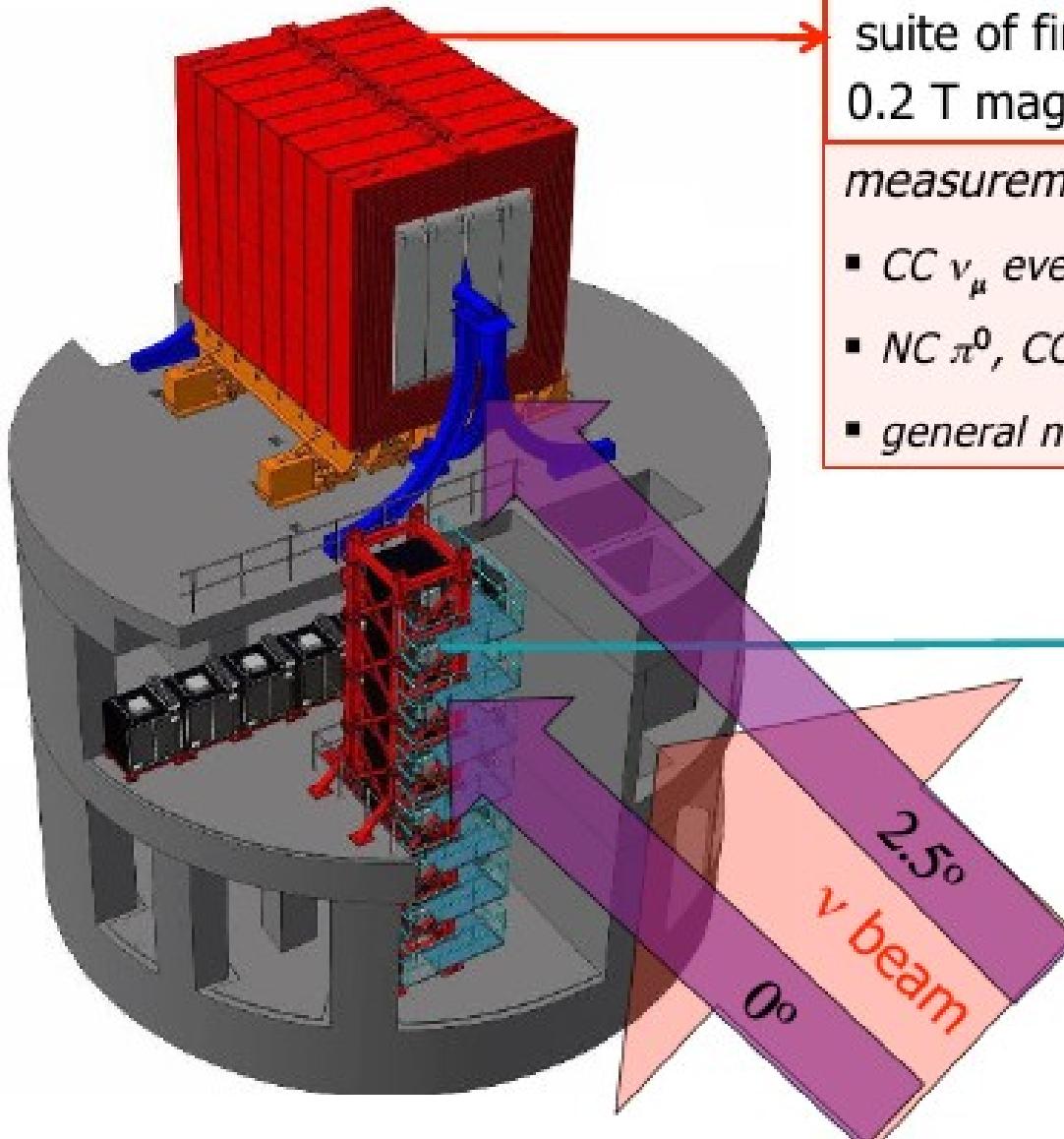
$$\Delta = 1.27 \cdot \Delta m^2 (eV^2) \cdot L(Km) / E(GeV)$$

Beam energy almost fixed by geometry



T2K Near Detector: ND280

ND280



Off-Axis (ND280)

suite of fine grain detectors/tracker in
0.2 T magnetic field (UA1/NOMAD magnet)

measurements of

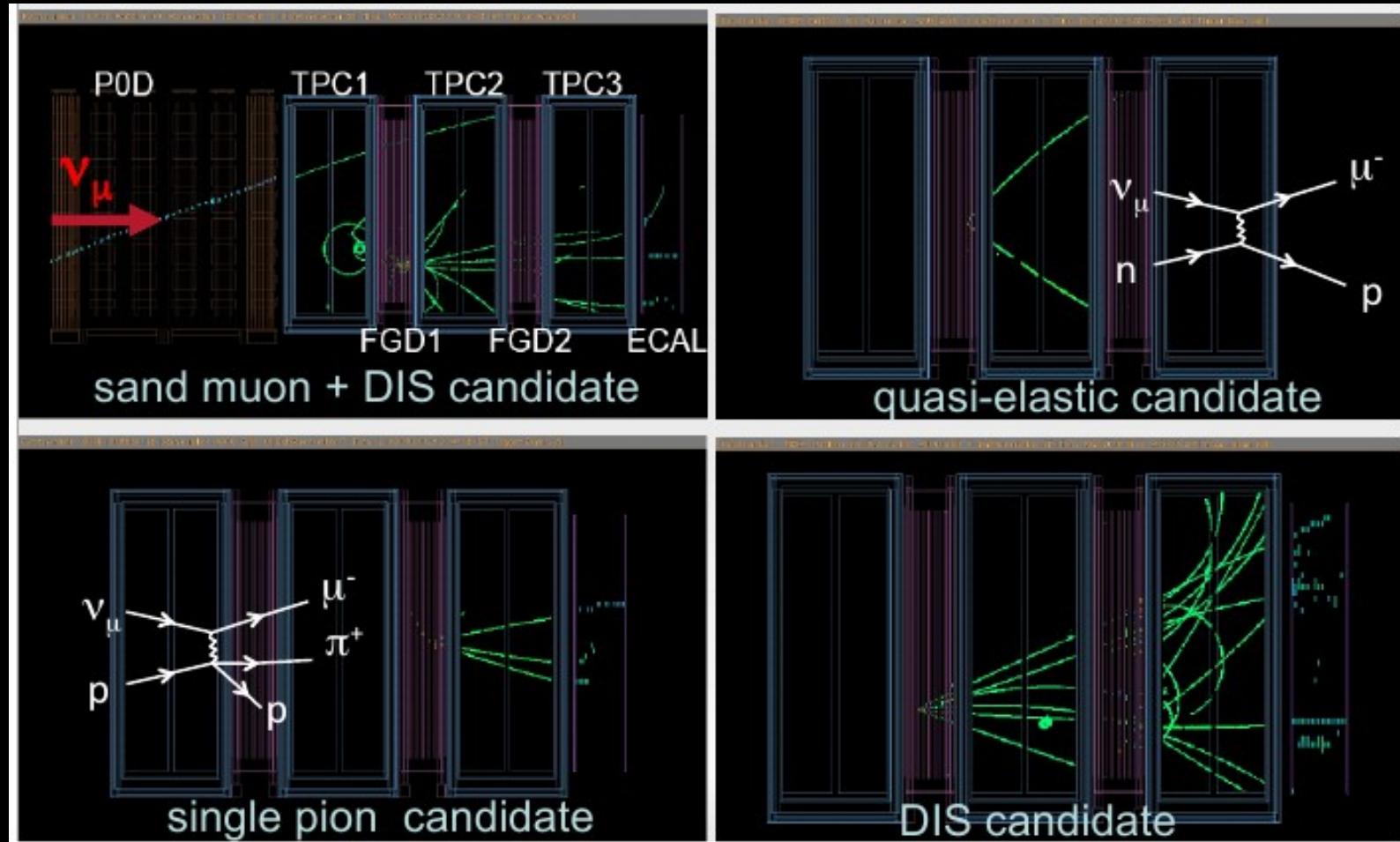
- $CC \nu_\mu$ events (normalization, E_ν -spectrum)
- $NC \pi^0$, $CC \nu_e$ events (backgrounds to ν_e appearance)
- general neutrino interaction properties

On-axis (INGRID)

scintillator-iron detectors

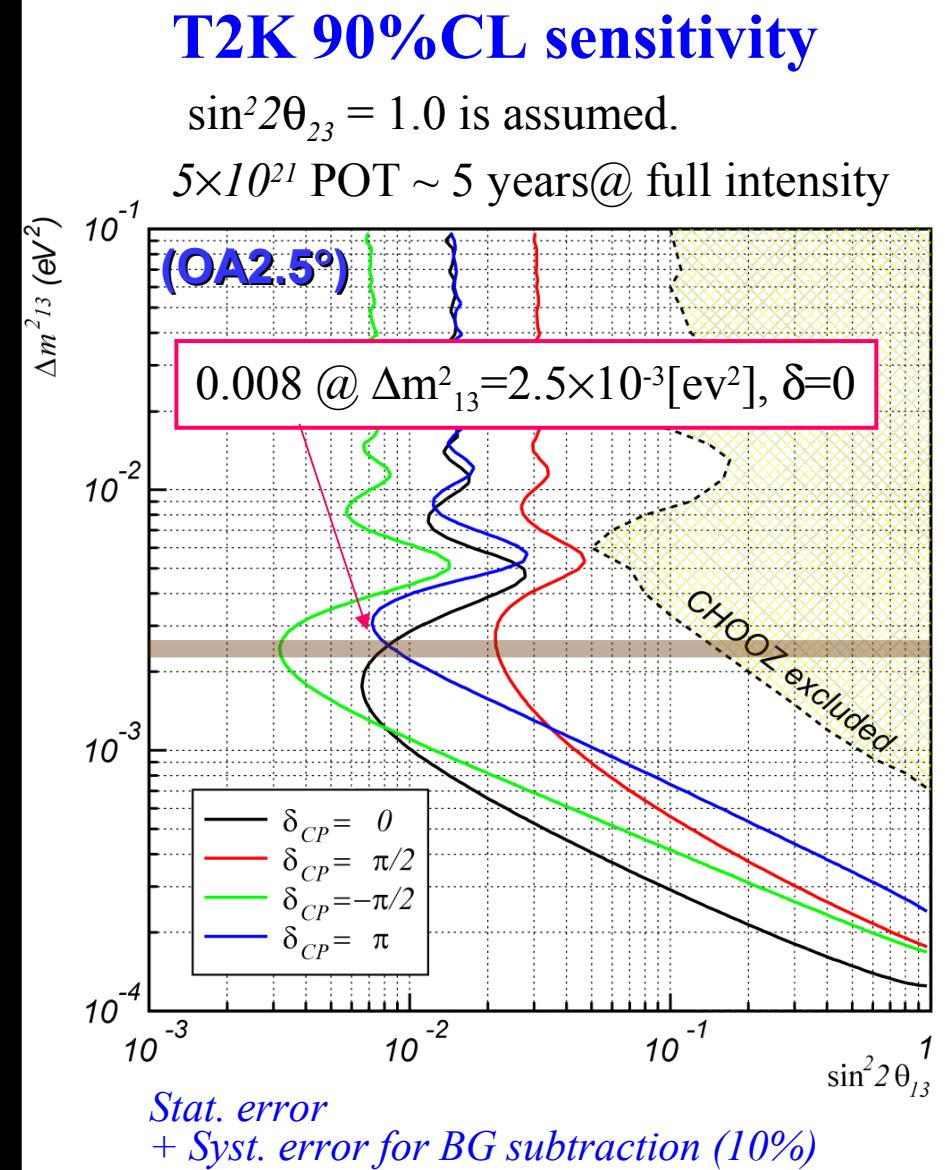
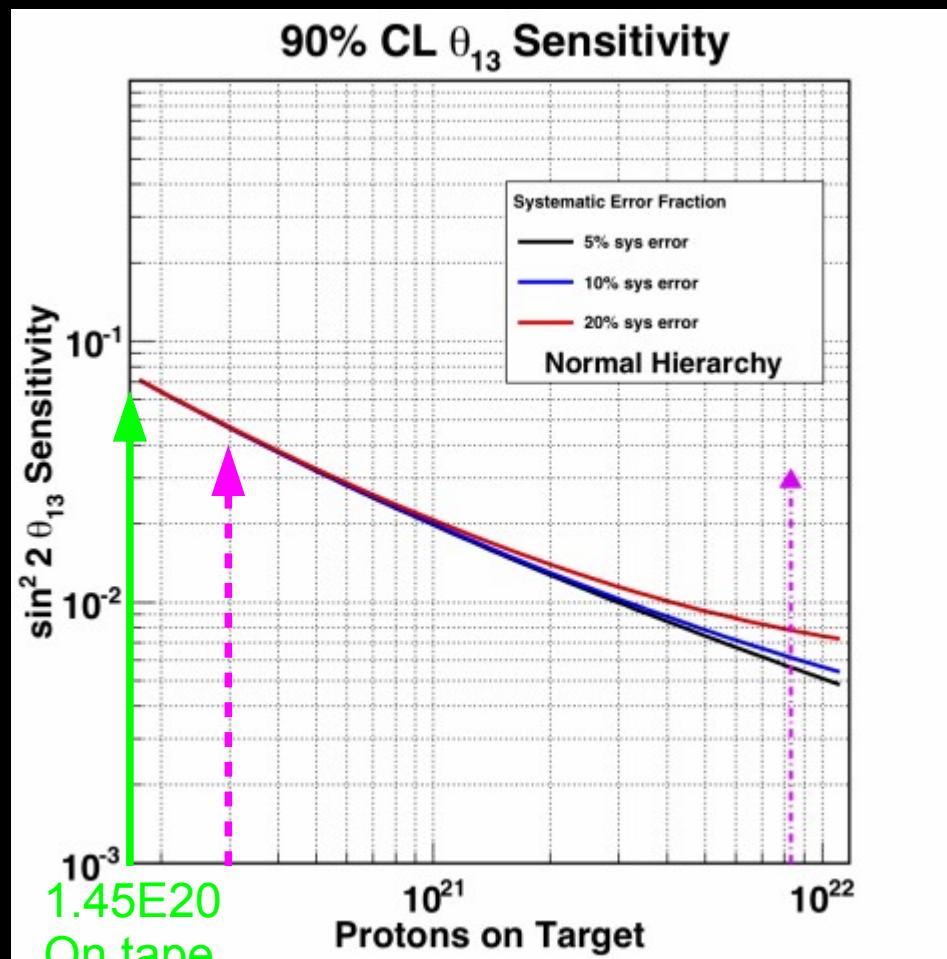
*measurement of beam direction
and profile*

ND280 events



T2K θ_{13} sensitivity

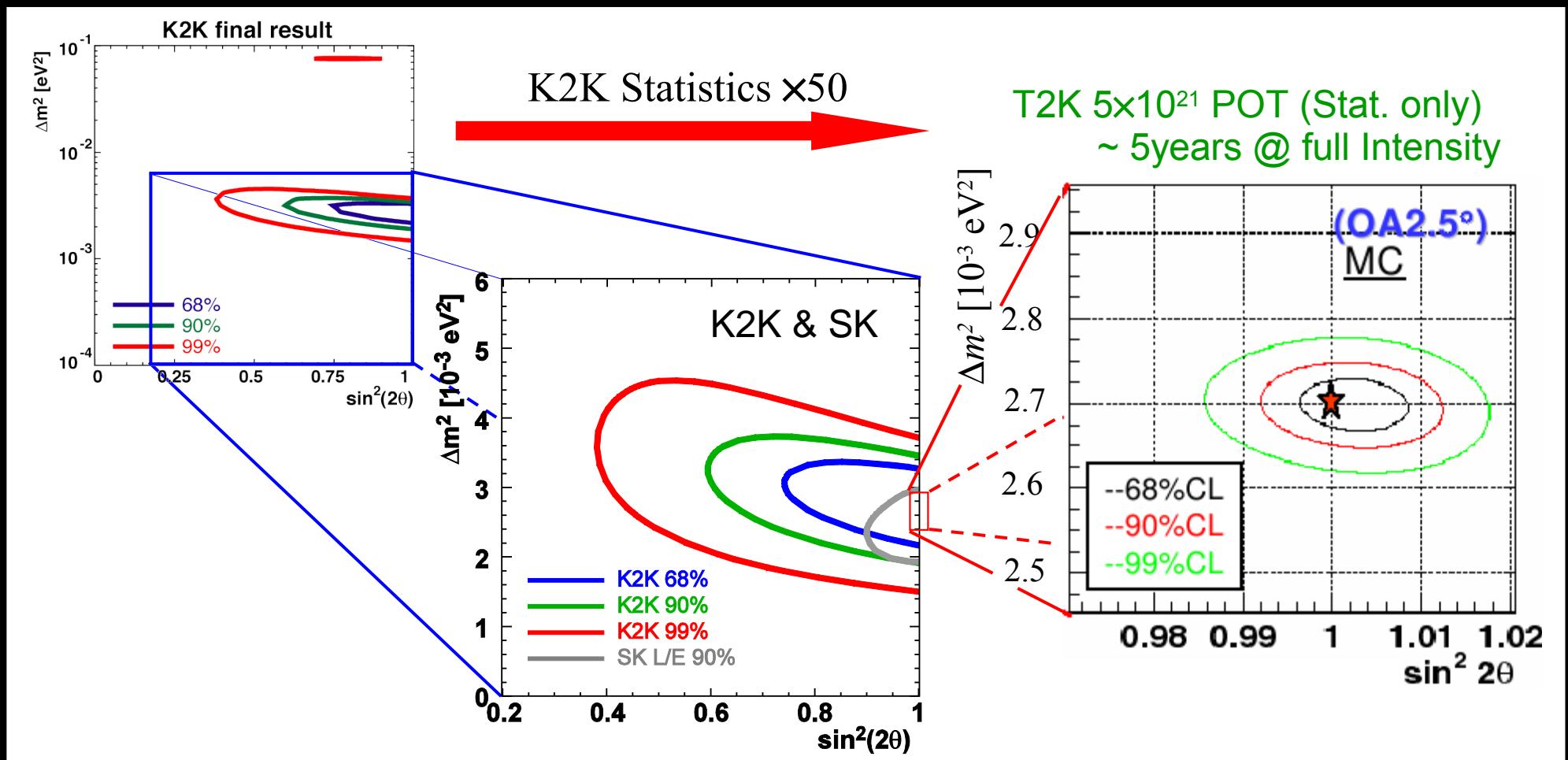
$$P(\nu_\mu \rightarrow \nu_e) \approx \sin^2 \theta_{23} \sin^2 2\theta_{13} \sin^2(1.27 \Delta m_{23}^2 L/E)$$



T2K ν_μ disappearance

$$P(\nu_\mu \rightarrow \nu_\mu) \approx 1 - \sin^2 2\theta_{23} \sin^2(1.27 \Delta m^2_{23} L/E)$$

Sensitivity: $\delta(\sin^2 2\theta_{23}) \sim 0.01$, $\delta(\Delta m^2_{23}) < 1 \times 10^{-4}$ [eV²]



T2K Preliminary Results

Jan-June 2010 (2010a): 3.23E19 pot
(w.r.t. 1.45E20 already on tape)

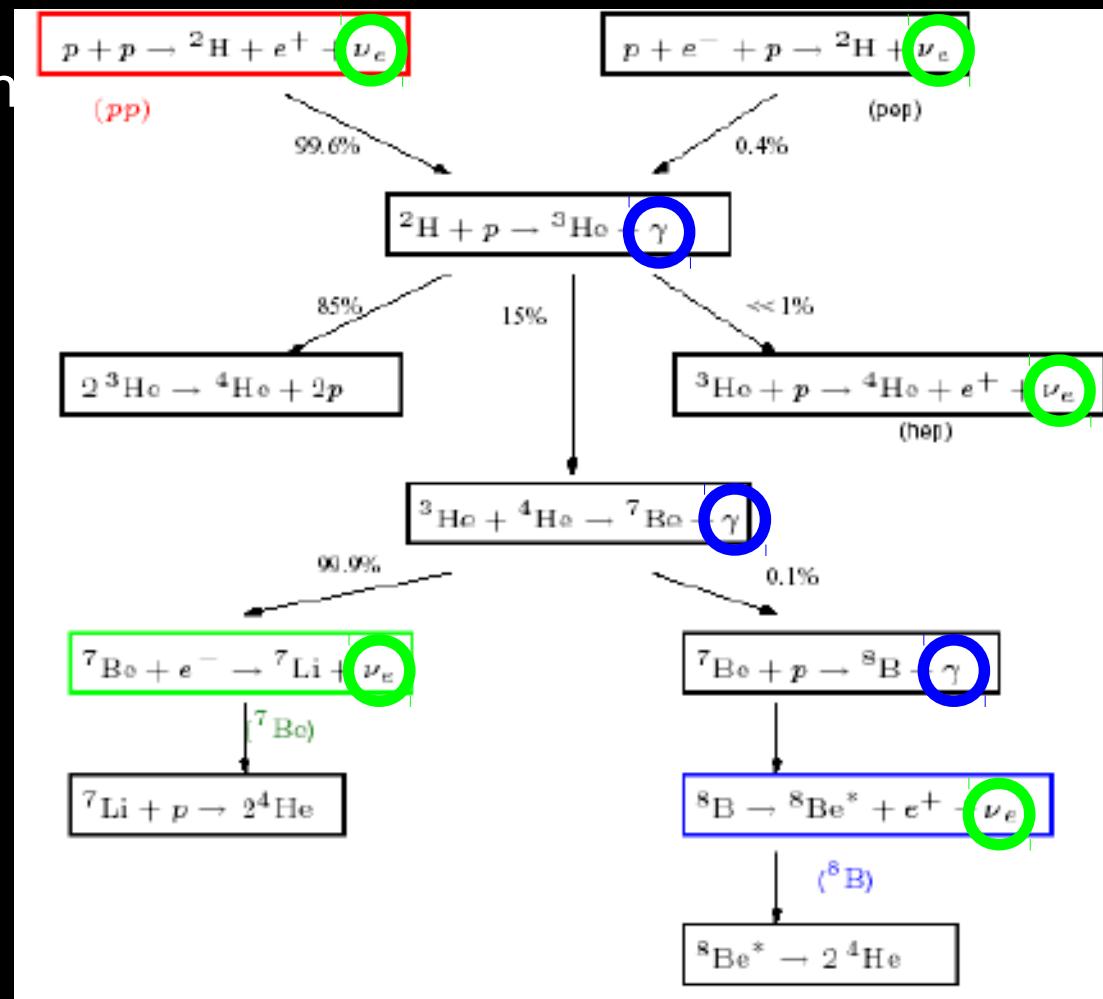
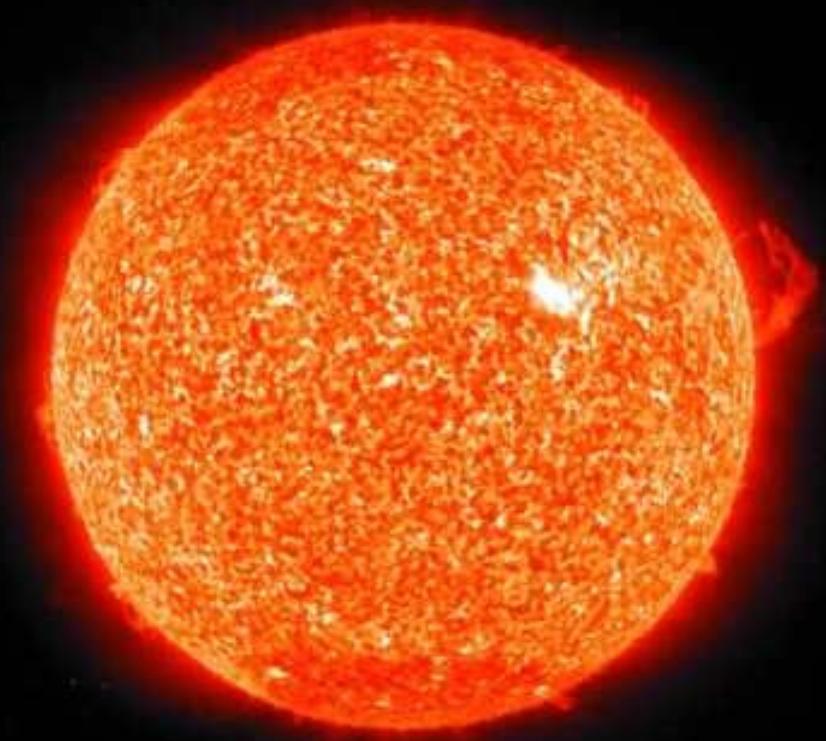
From $\pm 500 \mu\text{s}$ window around beam spills	Data	MC		BG (12 μs window)
		No oscillation	Oscillation $\Delta m^2 = 2.4 \times 10^{-3} (\text{eV}^2)$ $\sin^2 2\theta_{23} = 1.0$	
Fully-Contained	33	54.5	24.6	0.0094
Fiducial Volume, $E_{\text{vis}} > 30 \text{ MeV}$	23	36.8	16.7	0.0011
Single-ring μ -like ($P_\mu > 200 \text{ MeV}/c$)	8 (8)	24.6 (24.5 ± 3.9)	7.2 (7.1 ± 1.3)	-
Single-ring e-like ($P_e > 100 \text{ MeV}/c$)	2 (2)	1.9 (1.5 ± 0.7)	1.5 (1.3 ± 0.6)	-
Multi-ring	13	10.2	8.0	-

Consistent with oscillation parameters measured by SK, K2K,MINOS

observed ν_e candidates surviving all cuts: 1
expected background events ($\theta_{13}=0$): 0.30 ± 0.07

Neutrino from the Sun

The Standard Solar Model (SSM) predicts the power radiated by the Sun from fusion reactions in its core



98.5% of the Sun power comes from the pp reaction: $4 p \rightarrow 4\text{He} + 2e^+ + 2\nu_e + 26.7 \text{ MeV}$

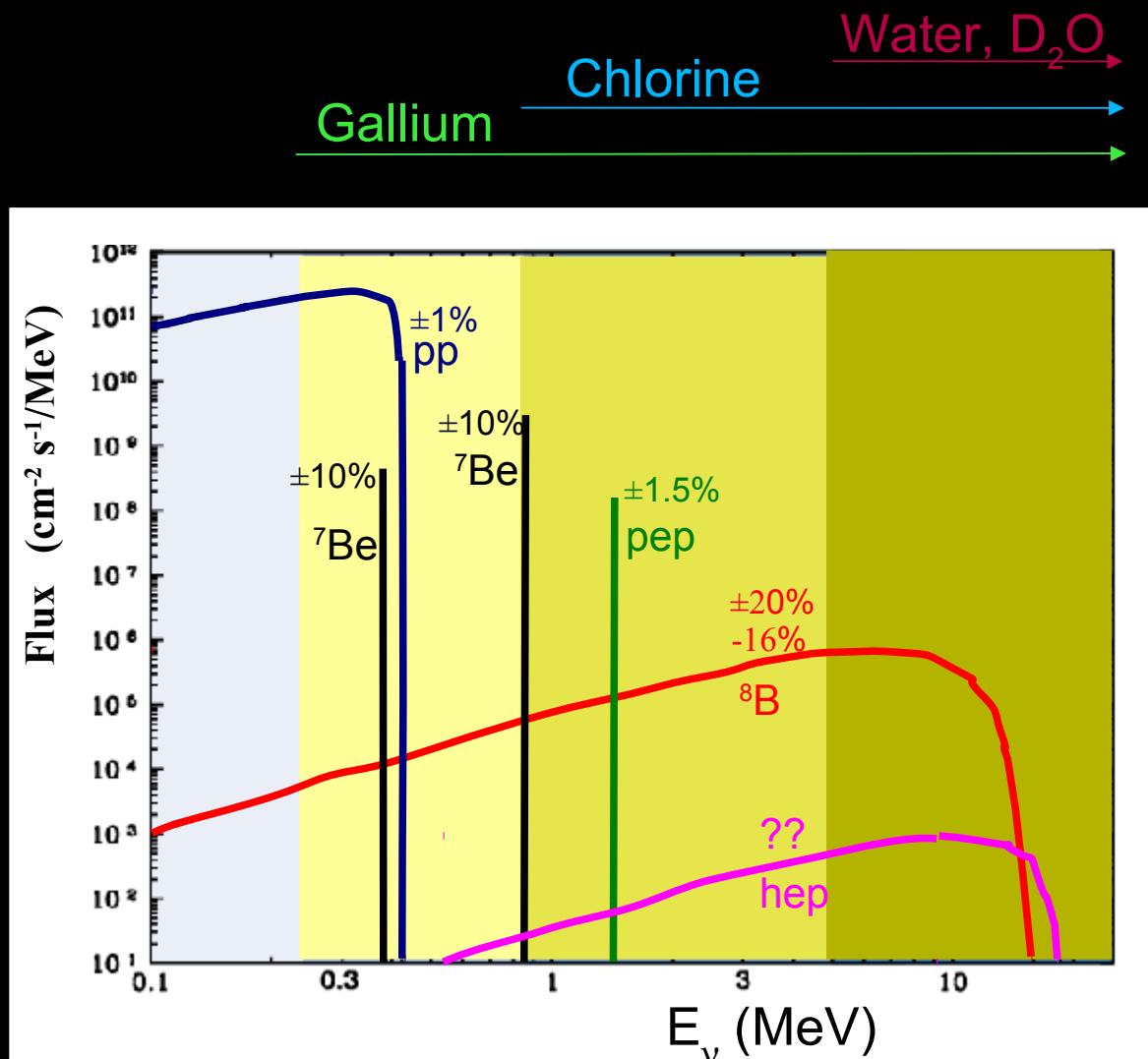
$$L_{\odot} = 3.9 \cdot 10^{26} \text{ Js}^{-1}$$

$$D = 1.5 \cdot 10^{11} \text{ m}$$

$$Q = 26.7 \text{ MeV} = 4.3 \cdot 10^{-12} \text{ J}$$

$$\Phi_{\odot} = 2L_{\odot}/Q \cdot (1/4\pi D^2) \approx 6.5 \cdot 10^{10} \text{ cm}^{-2} \text{ s}^{-1}$$

Spettro dei neutrini solari



Chlorine

Homestake



Gallium

SAGE, Gallex, GNO



Water

Kamiokande, SuperK

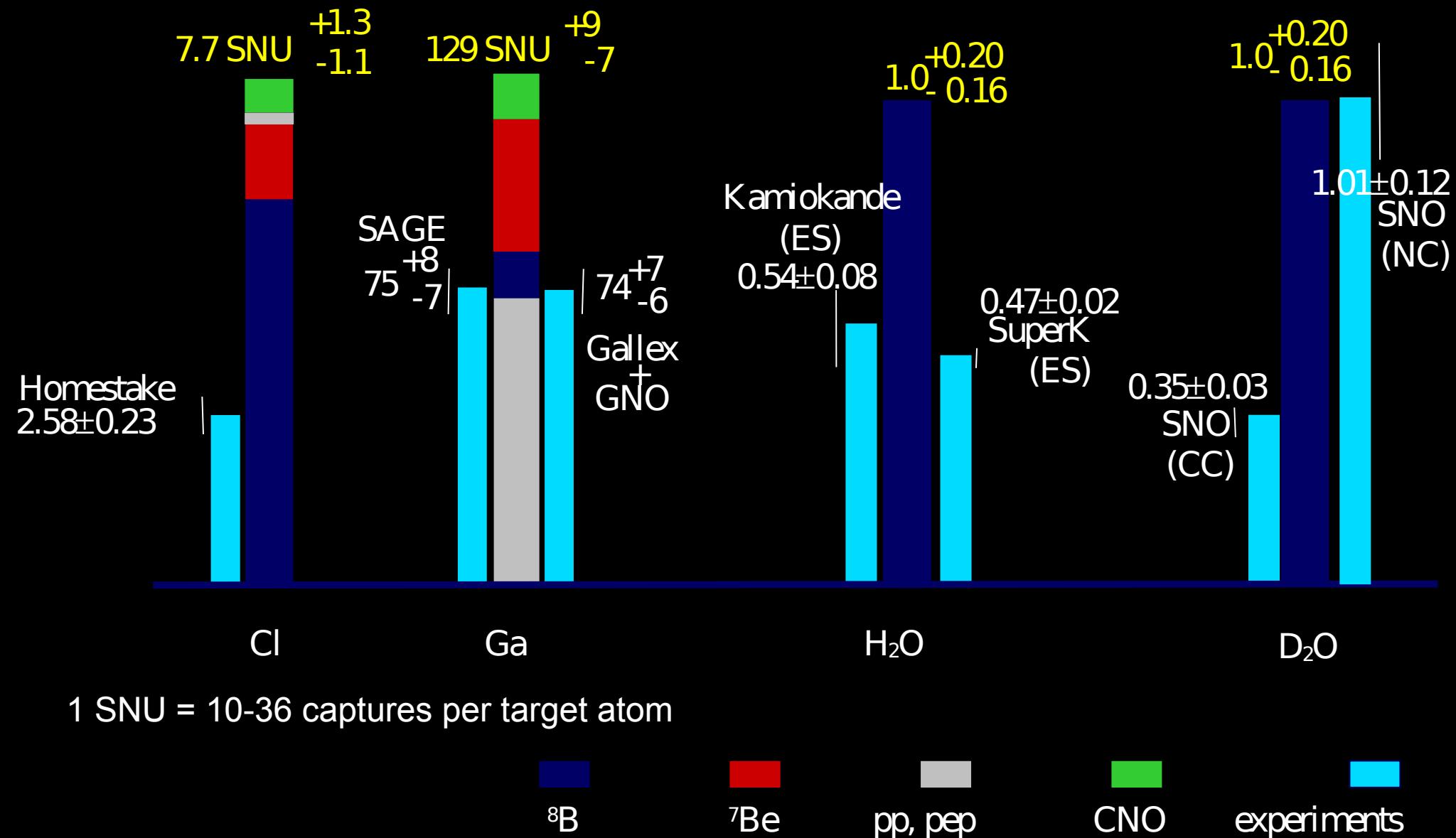


D₂O

SNO



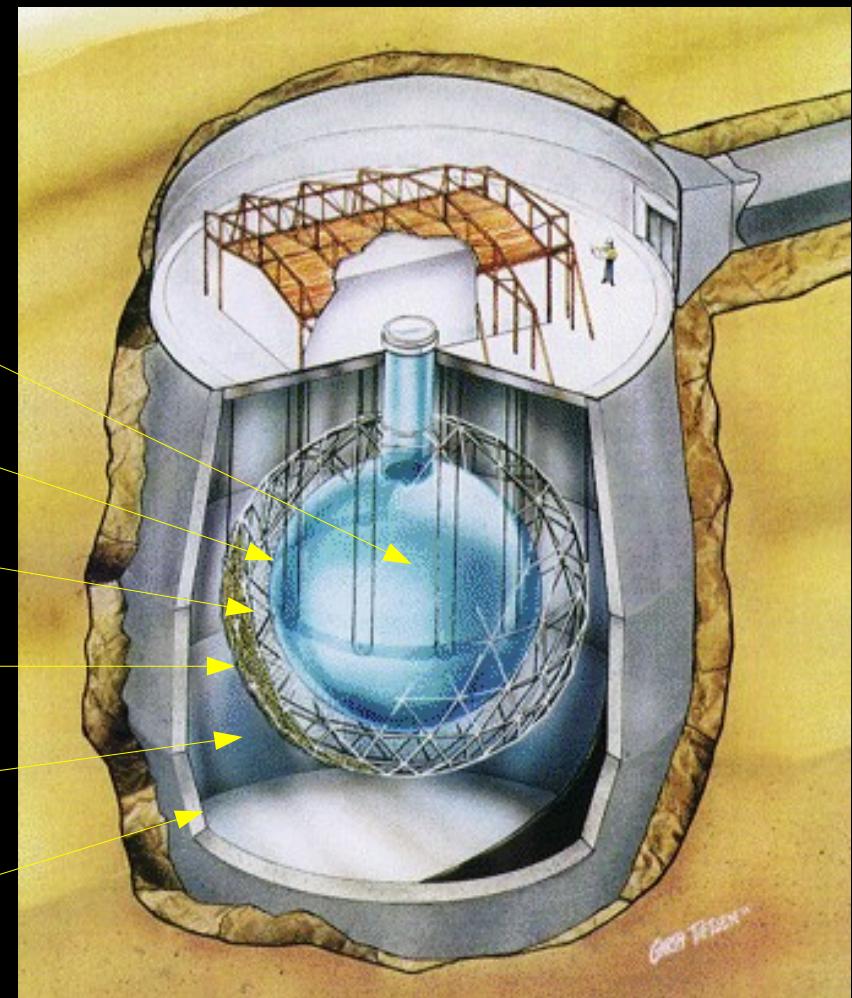
Misure del flusso dei neutrini solari



Sudbury Neutrino Observatory (SNO)



1000 tonnes D_2O
12 m Diameter Acrylic Vessel
1700 tonnes Inner Buffer H_2O
9500 PMTs, 60% coverage
5300 tonnes Outer Shield H_2O
Urylon Liner and Radon Seal

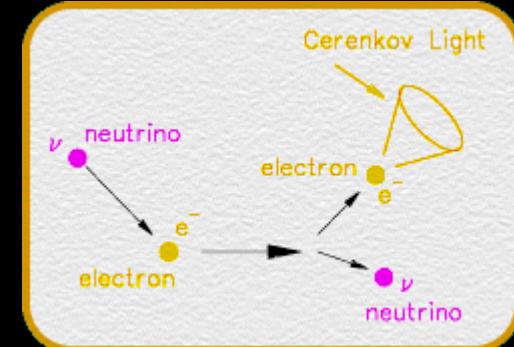


Neutrino interactions in SNO

ES

$$\nu_x + e^- \rightarrow \nu_x + e^-$$

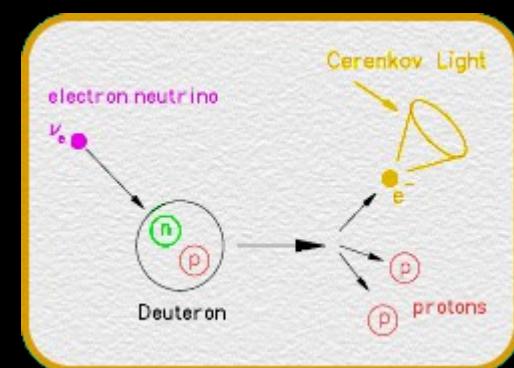
- ★ In SNO (D_2O) as in SK (H_2O)
- ★ Mainly ν_e but also ν_μ, ν_τ (1:6)
- ★ Strong Θ_V sensitivity



CC

$$\nu_e + d \rightarrow p + p + e^-$$

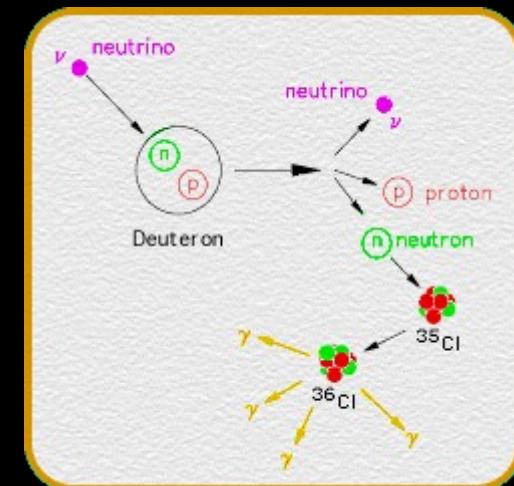
- ★ Good energy measurement
- ★ ν_e only
- ★ Weak directionality: $\propto 1 - 1/3 \cos(\Theta_V)$



NC

$$\nu_x + d \rightarrow n + p + \nu_x$$

- ★ Equally sensitive to all ν
- ★ Measure the total 8B flux



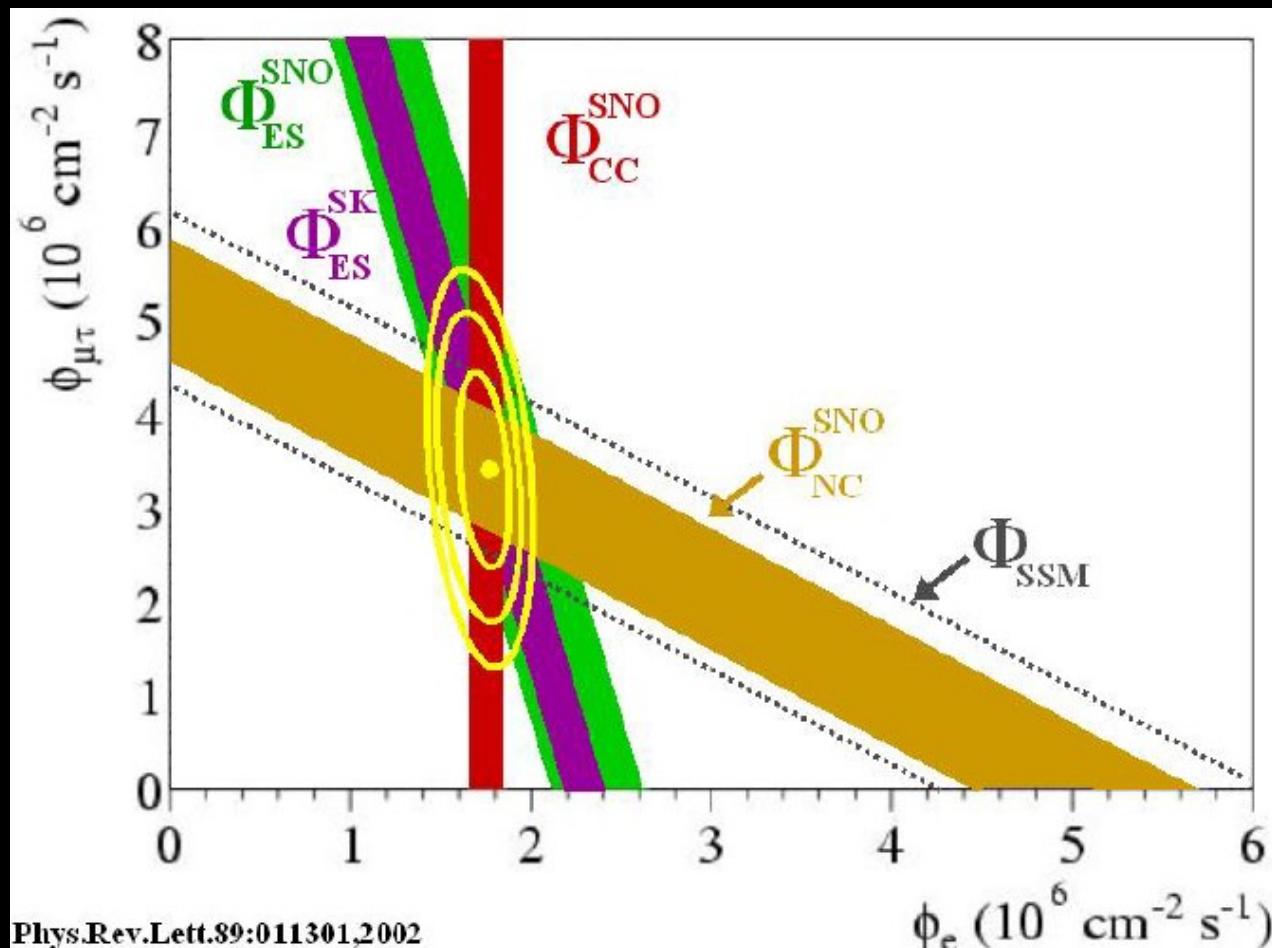
SNO: total flux as expected from SSM

- NC rate as expected from SSM (all neutrinos)
- CC rate (only ν_e) is 0.31 SSM
- ES rate is consistent with Super-Kamiokande and oscillation into ν_μ, ν_τ

$$\Phi_{CC} = 1.59^{+0.10}_{-0.11} \cdot 10^{-6} \text{ cm}^{-2} \text{ s}^{-1}$$

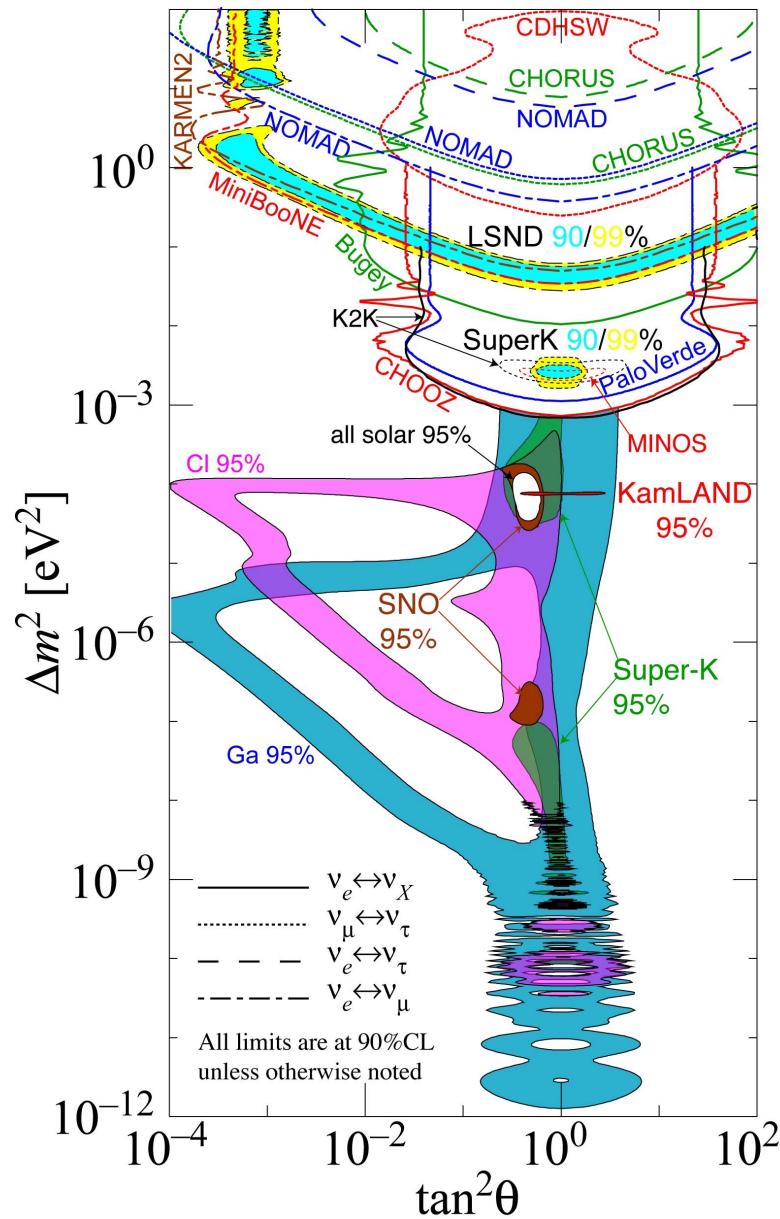
$$\Phi_{ES} = 2.21^{+0.33}_{-0.28} \cdot 10^{-6} \text{ cm}^{-2} \text{ s}^{-1}$$

$$\Phi_{ES} = 5.21 \pm 0.47 \cdot 10^{-6} \text{ cm}^{-2} \text{ s}^{-1}$$



Neutrino different from ν_e coming from the Sun ! (2002)

Oscillation data overview



<http://hitoshi.berkeley.edu/neutrino>

Decades of experimental and theoretical efforts !

That's all folks ?!

“There is nothing new to be discovered in physics now.
All that remains is more and more precise measurement.”

Kelvin, c. 1900