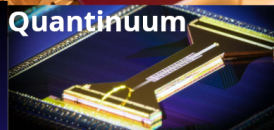
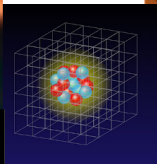
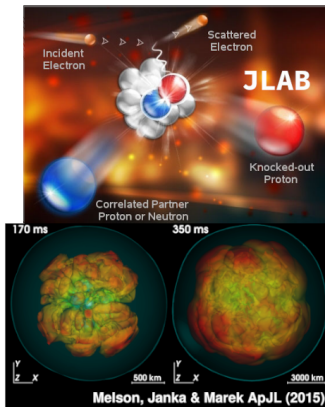


Quantum Computing for Nuclear Physics

Alessandro Roggero



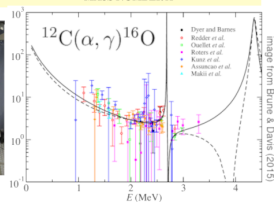
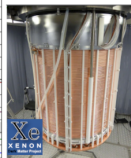
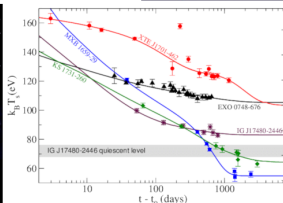
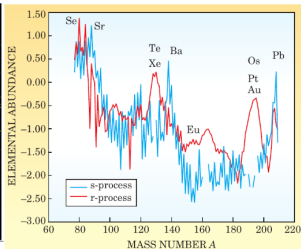
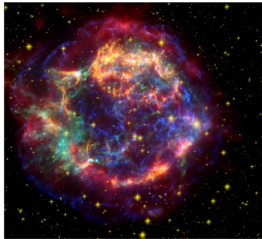
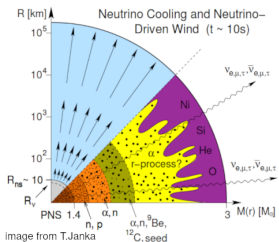
INFN2024 - Trento

27 Feb, 2024

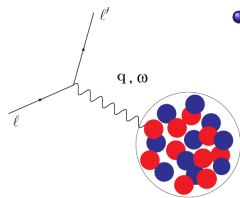


The need for ab-initio many-body dynamics in NP

- ν scattering for supernovae explosion and NS cooling
- capture reactions for crust heating and nucleosynthesis
- cross sections for dark-matter discovery and neutrino physics
- transport properties of neutron star matter for X-ray emission



Inclusive cross section and the response function

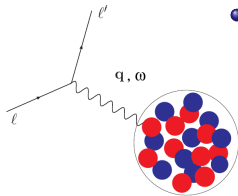


- cross section determined by the response function

$$R_O(\omega) = \sum_f \left| \langle f | \hat{O} | \Psi_0 \rangle \right|^2 \delta(\omega - E_f + E_0)$$

- excitation operator \hat{O} specifies the vertex

Inclusive cross section and the response function



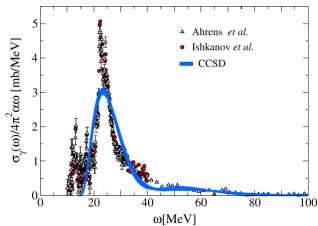
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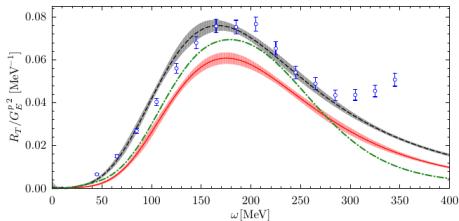
Extremely challenging classically for strongly correlated quantum systems

- dipole response of ^{16}O



Bacca et al. PRL(2013) LIT+CC

- quasi-elastic EM response of ^{12}C

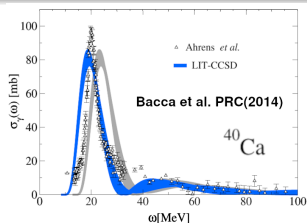


Lovato et al. PRL(2016) GFMC

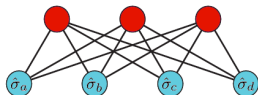
Prospects for classical simulations of nuclear dynamics

Quantum MC + Laplace/STA

- useful for quasi-elastic regime
- not yet accurate enough to go beyond $A = 12$ (sign-problem)



Machine Learning ideas could help



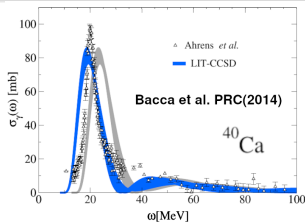
Coupled Cluster + Lorentz/Gauss

- useful for low energy regime
- accuracy limited by inversion

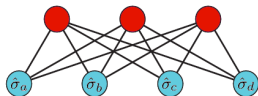
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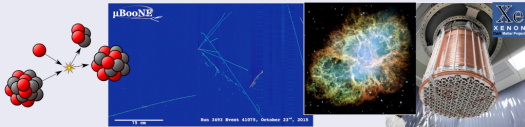


Coupled Cluster + Lorentz/Gauss

- useful for low energy regime
- accuracy limited by inversion

Some problems will still remain out of reach

- large open-shell nuclei
- exclusive cross-sections
- out of equilibrium



Quantum Computing and Quantum Simulations

R.Feynman(1982) we can use a controllable quantum system to simulate the behaviour of another quantum system

**Quantum System
we have control over**

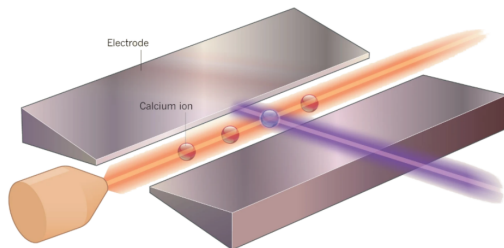


figure from E.Zohar

**Quantum System
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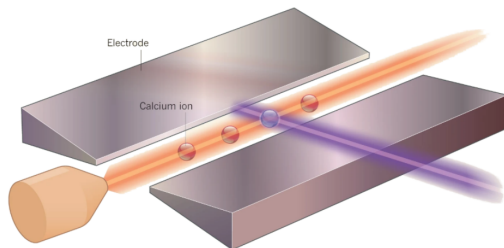
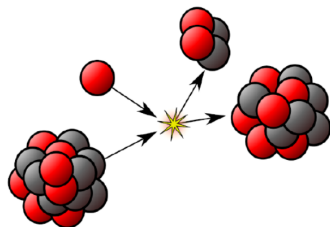


figure from E.Zohar

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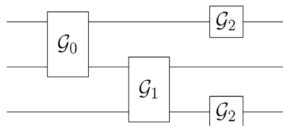
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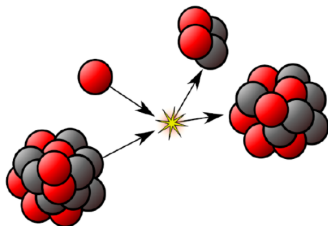
Quantum System
we have control over



Blume-Kohout et al. (2013)



Quantum System
we want to simulate



Black box model for a quantum computer



Blume-Kohout et al. (2013)

Box contains N qubits (2-level sys.)
together with a set of buttons

- initial state preparation ρ
- projective measurement \mathcal{M}
- quantum operations G_k

Black box model for a quantum computer



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Solovay–Kitaev Theorem

We can build a **universal** black box
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$$|\Psi(0)\rangle \rightarrow |\Psi(t)\rangle = e^{-iHt} |\Psi(0)\rangle$$

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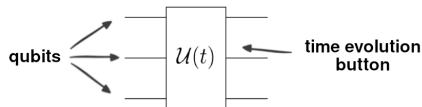
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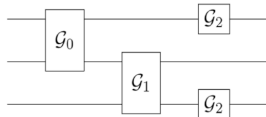
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Lloyd (1996) We can simulate time evolution of **local** Hamiltonians

- 1 discretize the physical problem
- 2 map physical states to bb states
- 3 push correct button sequence

$$|\Psi(0)\rangle \rightarrow |\Psi(t)\rangle = e^{-iHt}|\Psi(0)\rangle$$



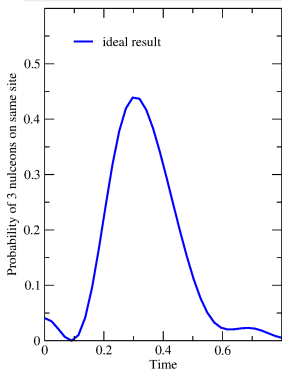
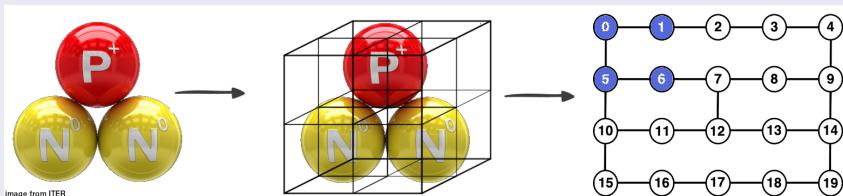
First programmable quantum devices are here



some figures from M.Savage

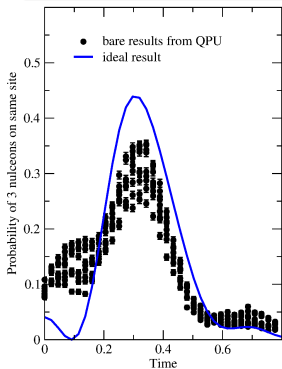
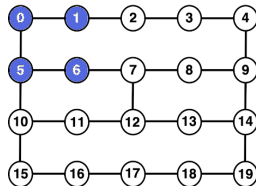
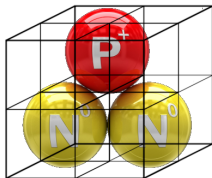
Real time dynamics on current generation devices

AR, Li, Carlson, Gupta, Perdue PRD(2020)



Real time dynamics on current generation devices

AR, Li, Carlson, Gupta, Perdue PRD(2020)



Error sources

- decoherence (environment)
- imperfect calibration



Blume-Kohout et al. (2013)

Real time dynamics on current generation devices

AR, Li, Carlson, Gupta, Perdue PRD(2020)

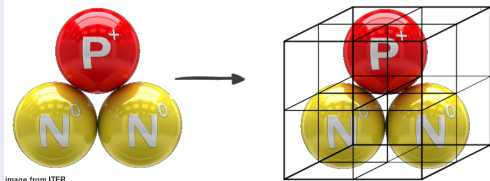
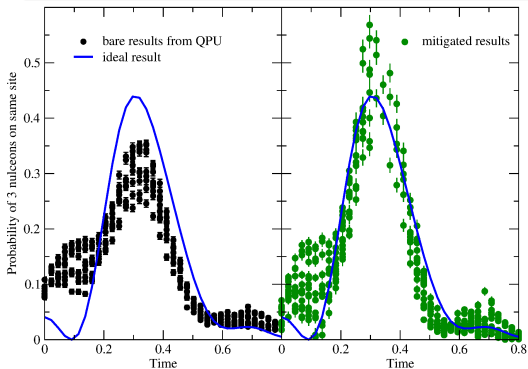
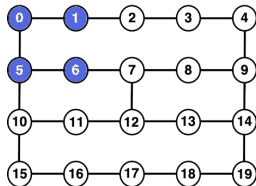
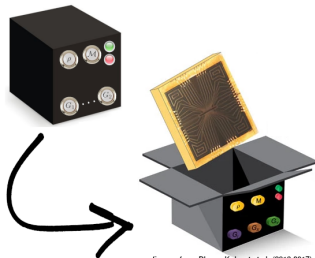


image from ITER



• Error mitigation is crucial



figures from Blume-Kohout et al. (2013,2017)

Fourier moments on (more) current generation devices

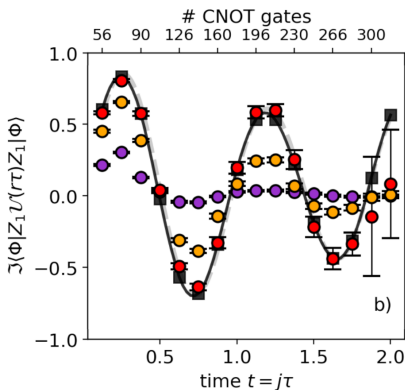
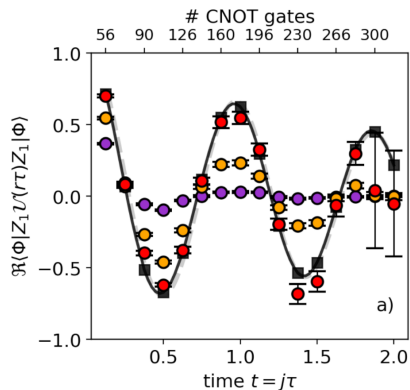
Both devices and error mitigation have come a long way in last few years

$$R(\omega) \approx \sum_k c_k(\omega) M(t_k) \quad \text{with} \quad M(t) = \langle \Psi_0 | O e^{-iHt} O | \Psi_0 \rangle$$

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Kiss, Grossi, AR arXiv:2401.13048 (2024)

Exclusive cross sections in neutrino oscillation experiments



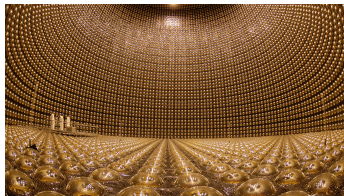
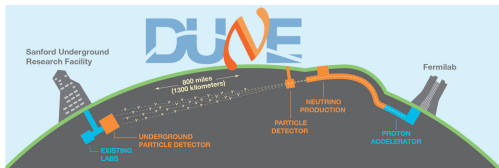
Goals for ν oscillation exp.

- neutrino masses
- accurate mixing angles
- CP violating phase

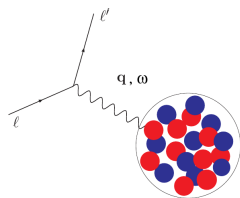
$$P(\nu_\alpha \rightarrow \nu_\alpha) = 1 - \sin^2(2\theta)\sin^2\left(\frac{\Delta m^2 L}{4E_\nu}\right)$$

- need to use measured reaction products to constrain E_ν of the event

DUNE, MiniBooNE, T2K, Minerva, NO ν A, ...



Towards exclusive scattering using quantum computing

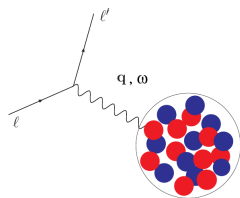


- response $R(\omega) \Leftrightarrow$ probability for events at fixed ω
- exclusive x-sec \rightarrow events with specific final states

IDEA: prepare the following state on QC

$$|\Phi\rangle = \sum_{\omega} \sqrt{R(\omega)} |\omega\rangle \otimes |\psi_{\omega}\rangle$$

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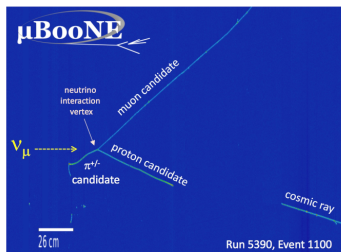
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Blume-Kohout et al. (2013)



AR & Carlson PRC(2019)

Prospects of impact of QC on Nuclear Physics

AR, Li, Carlson, Gupta, Perdue PRD(2020)

Cost estimates for realistic response in medium mass nuclei

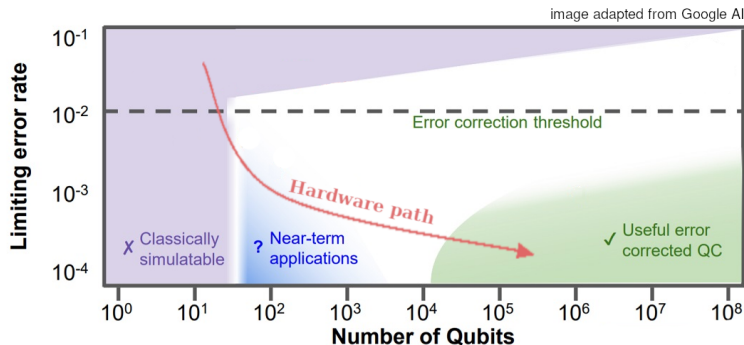
We need ≈ 4000 qubits and push the gate buttons $\approx 10^6 - 10^8$ times

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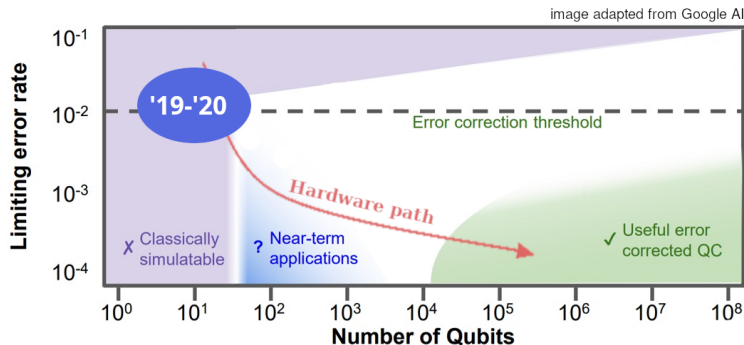


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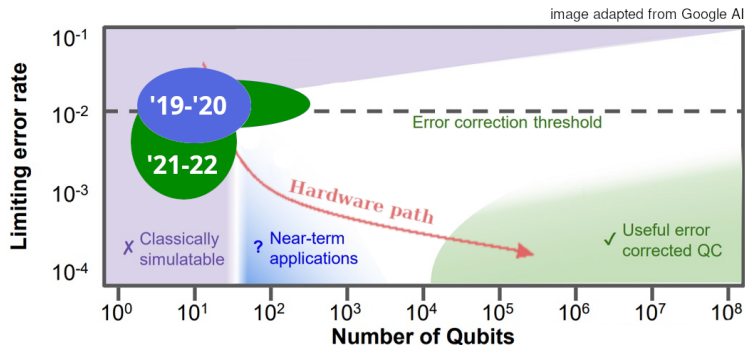


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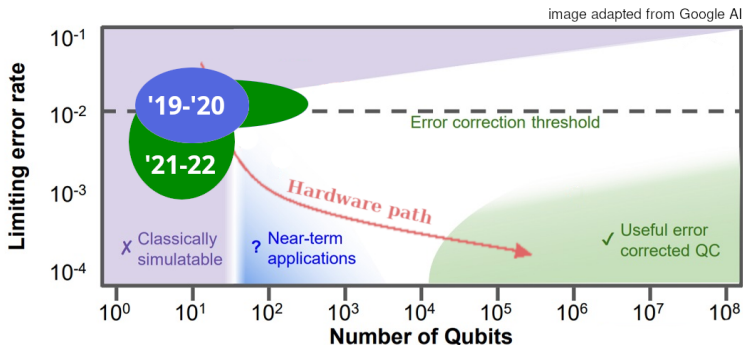


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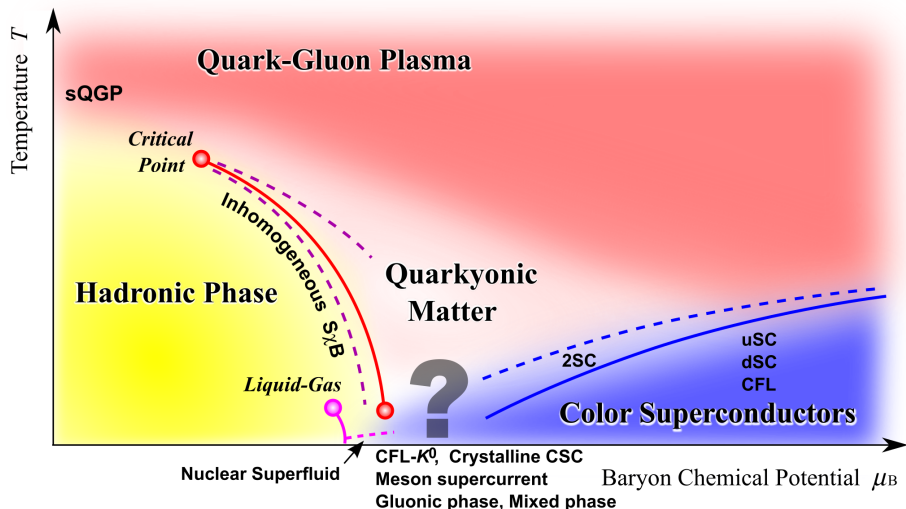
We need ≈ 4000 qubits and push the gate buttons $\approx 10^6 - 10^8$ times



- Still possible to optimize further (other encodings need ≈ 500 qubits)
- Insights for classical methods could come before we have a large QC!

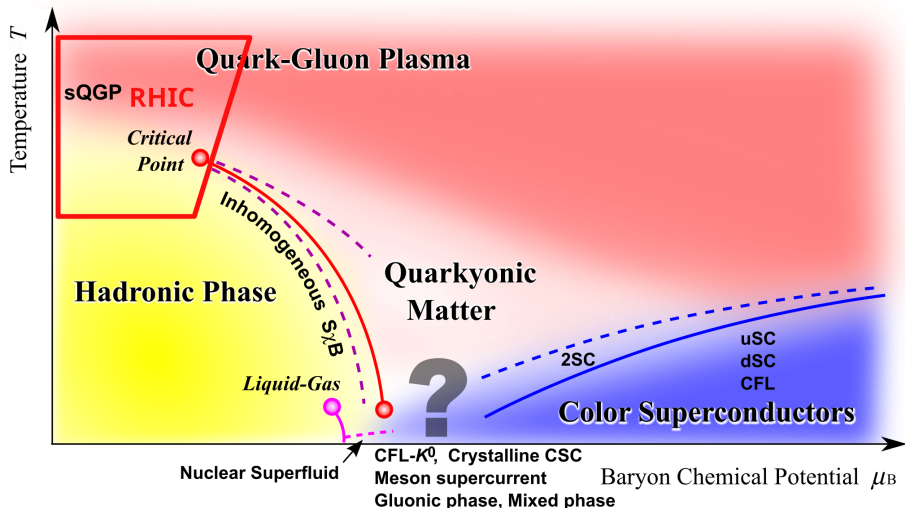
The QCD phase diagram

figure from Fukushima & Hatsuda (2011)



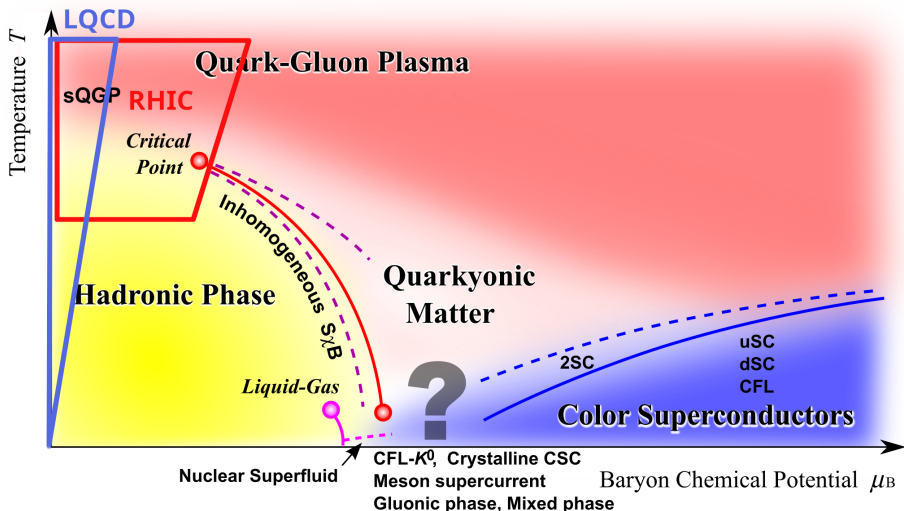
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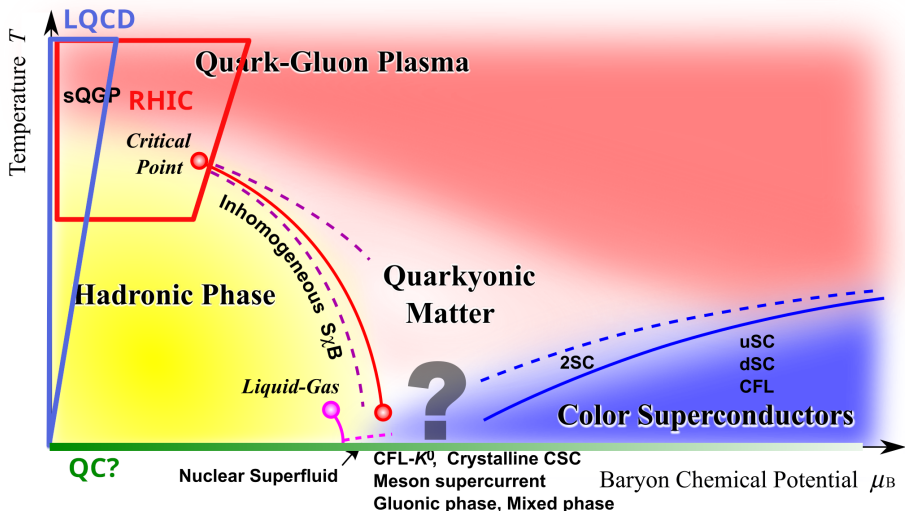
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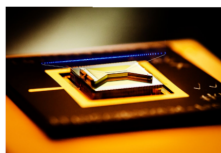
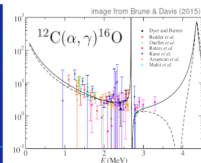
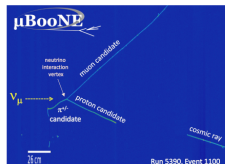
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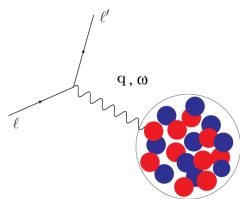


Summary & Conclusions

- Advances in theory and computing are opening the way to ab-initio calculation of equilibrium properties in the medium-mass region
- New ideas are needed to study nuclear dynamics in large open-shell nuclei, out-of-equilibrium processes and QCD at finite μ
- Quantum Computing has the potential to bridge this gap and increasingly better experimental test-beds are being built
- Error mitigation techniques will be critical to make the best use of these noisy near-term devices
- Early impact of QC on nuclear physics might come as insights into classical many-body methods and the role of entanglement



Towards exclusive scattering using quantum computing



- response $R(\omega) \Leftrightarrow$ probability for events at fixed ω
- exclusive x-sec \rightarrow events with specific final states

IDEA: prepare the following state on QC

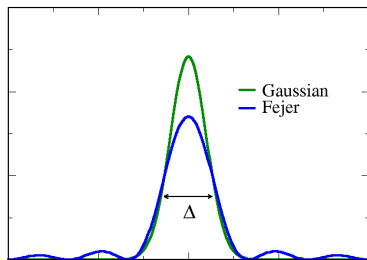
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- measurement of first register returns ω with probability $R(\omega)$!
- after measurement, the second register contains final states at ω !

Difficult to prepare $|\Phi\rangle$ but we can prepare instead the following state

$$|\Phi_{\Delta}\rangle = \sum_{\omega} \sqrt{R_{\Delta}(\omega)} |\omega\rangle \otimes |\psi_{\omega}\rangle$$

with R_{Δ} is an integral transform of the response with energy resolution Δ



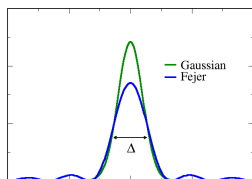
AR & Carlson PRC(2019), AR PRA(2020)

Nuclear dynamics with quantum (inspired) computing?

We can prepare the following state

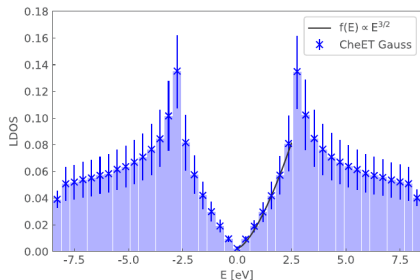
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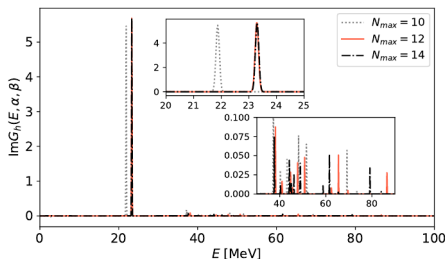


AR & Carlson PRC(2019), AR PRA(2020)

- Gaussian approach uses the fact that Chebyshev polynomials can be evaluated efficiently on quantum computers (Berry, Childs, Low, Chuang, ...)



Sobczyk, AR PRE(2022)



Sobczyk, Bacca, Hagen, Papenbrock PRC(2022)