

# Cluster Effective Field Theory calculation of electromagnetic breakup reactions with the Lorentz Integral Transform method

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and Applications

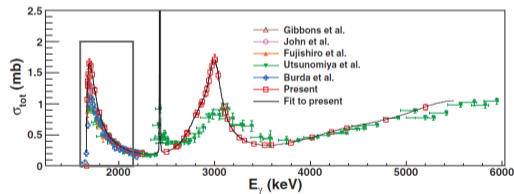
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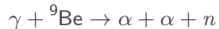


Study of the reaction of *astrophysical interest*  
in the **low-energy regime**:

- $^9\text{Be}$  3-body ( $\alpha\alpha n$ ) binding energy
- Cross section

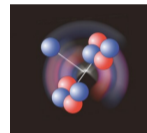


[Arnold *et al.* (2012)]



## MODEL

- Effective particles: **nucleons** and  $\alpha$ -particles
- Interaction: potential models from **Effective Field Theory (EFT)**  
(2-body and 3-body potentials) [Hammer *et al.* (2017)]



P. Mueller/Argonne National Lab

### Cluster-EFT approach: why?

${}^9\text{Be}$  binding  $B_3 \approx 1.573 \text{ MeV} \ll \alpha$  binding ( $\approx 20 \text{ MeV}$ ) ← SEPARATION OF SCALES  
 ↑  
 shallow binding

⇒  ${}^9\text{Be}$  is a 3-body *effective* clustering system in the low energy regime

⇒ EFT approach



## Two-Body Effective Potentials



Effective potential defined in momentum space and in the partial wave  $\ell$ :

$$\mathcal{V}_\ell(p, p') = \left[ \lambda_0 + \lambda_1 (p^2 + p'^2) \right] p^\ell p'^\ell g(p)g(p')$$

Regulator function:

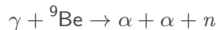
$$g(p) = e^{-\left(\frac{p}{\Lambda}\right)^{2m}} \quad m = 1, 2$$

- We calculate the T-matrix by solving the Lippmann-Schwinger equation
  - We compare the calculated low-energy T-matrix with its ERE

The LECs are fixed on the experimental values of the scattering length and the effective range

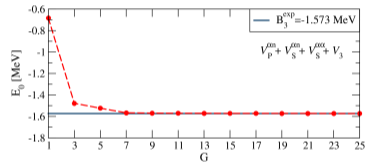
$$\lambda_i = \lambda_i(a_\ell^{\text{exp}}, r_\ell^{\text{exp}}, \Lambda)$$

The effective potentials  $\mathcal{V}_\ell^{\alpha n}(p, p')$  and  $\mathcal{V}_\ell^{\alpha\alpha}(p, p')$  reproduce the correct low-energy  $\alpha n$  and  $\alpha\alpha$  phase-shifts



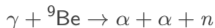
## METHOD

- Bound-state problem:  
the variational method with a **Non-Symmetrized Hyperspherical Harmonics (NSHH)** basis  
[Gattobigio *et al.* (2011), Deflorian *et al.* (2013)]

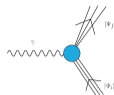


- Continuum problem:  
the **Lorentz Integral Transform (LIT)** method  
[Efros *et al.* (2007)]





$$\gamma : \hat{\epsilon}_{\mathbf{q},\lambda}, \omega = |\mathbf{q}|$$



Bacca et al (2014)

# RESULTS

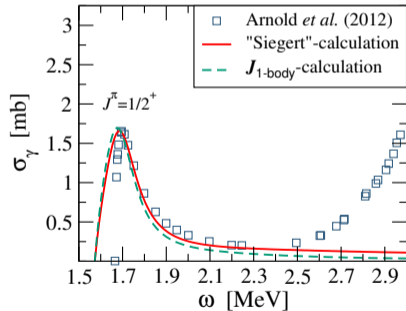
$$\sigma_\gamma \propto \mathcal{R}_\gamma(\omega) \sim \langle \Psi_f | \hat{\epsilon}_{\mathbf{q},\lambda} \cdot \mathbf{J}(\mathbf{q}) | \Psi_0 \rangle \leftarrow \text{Nuclear Current m.e.}$$

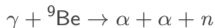
$$\mathbf{J} = \mathbf{J}_{1\text{-body}} + \mathbf{J}_{2\text{-body}} + \dots$$

We make two types of calculations (E1 contribution):

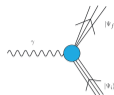
- 1 we use the **one-body current**  $\mathbf{J}_{1\text{-body}}$  [Filandri (2022)]
- 2 we calculate the **dipole operator m.e.**  $\langle \Psi_f | \hat{\epsilon}_{\mathbf{q},\lambda} \cdot \mathbf{D} | \Psi_0 \rangle$

**Why?** The **Siegert theorem**, at low energy, ensures that the dipole operator contains the contribution of the 1-body current and beyond  
 $\Rightarrow$  inclusion of  $\mathbf{J}_{2\text{-body}}$  and  $\mathbf{J}_{3\text{-body}}$  contribution to  $\sigma_\gamma$





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Bacca et al (2014)

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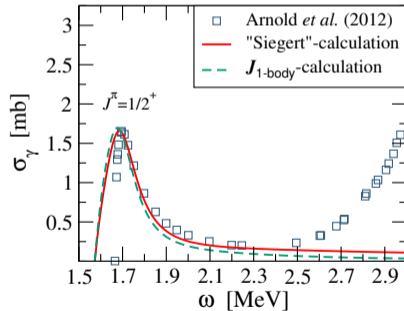
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Thank You!