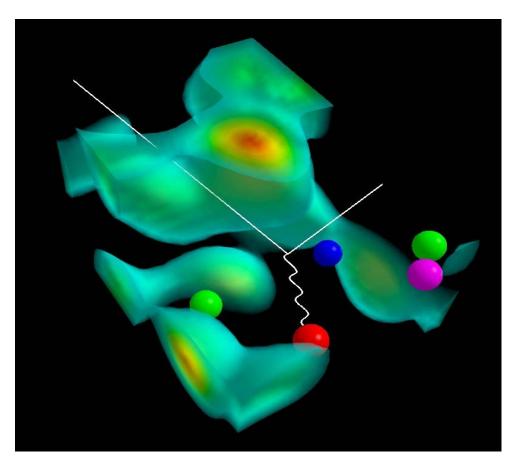
## **Strangeness in the Nucleon :** What have we learned?







**Australian Government Australian Research Council** 





#### **Anthony W. Thomas**



**PAVI11** Rome: September 5-9 2011



## Outline

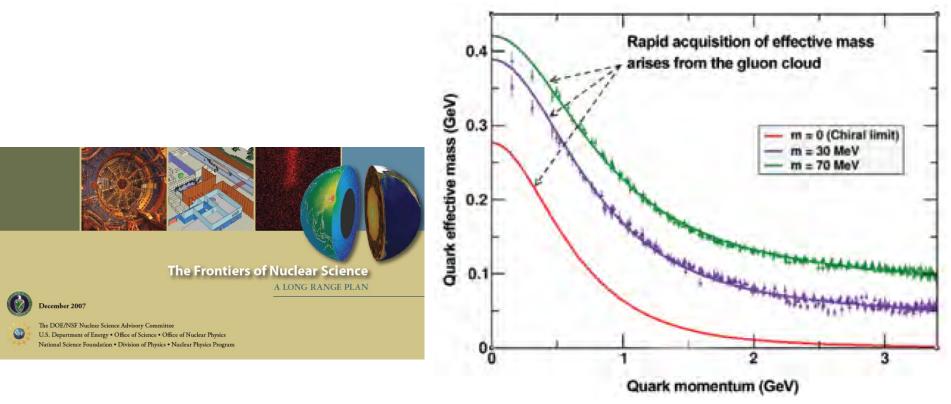
- Strange Vector Current
   "Lamb shift" for QCD
- Overview of lattice data
- Strange sigma commutator

   Implications for Dark Matter Searches
- The H-dibaryon re-incarnated?
- The s-quark as a heavy d-quark CSV
- Strange quark sea





## **Quark and Gluon Propagators**



**Figure 2.1:** Mass from nothing. In QCD a quark's effective mass depends on its momentum. The function describing this can be calculated and is depicted here. Numerical simulations of lattice QCD (data, at two different bare masses) have confirmed model predictions (solid curves) that the vast bulk of the constituent-mass of a light quark comes from a cloud of gluons, that are dragged along by the quark as it propagates. In this way, a quark that appears to be absolutely massless at high energies (m = 0, red curve) acquires a large constituent mass at low energies.





## **Strange Vector Current**





#### **Strange Vector Form Factors**

There have been a number of major steps forward recently, both theory and experiment :

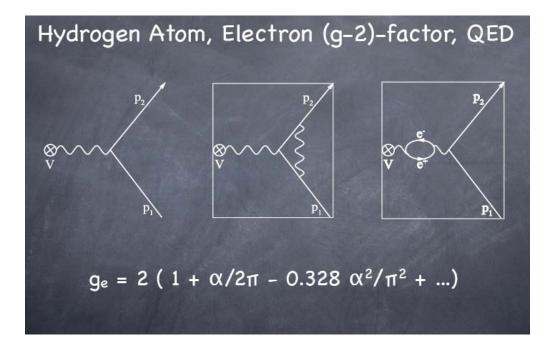
- > Calculation of  $G_{E,M}^{s}$  (Q<sup>2</sup>) :
  - Indirect: Adelaide-JLab
  - Direct: Kentucky
- Experimental determination of G<sub>E,M</sub><sup>s</sup> (Q<sup>2</sup>)
  - G0 and Happex
  - Mainz PVA4 (and earlier Bates)

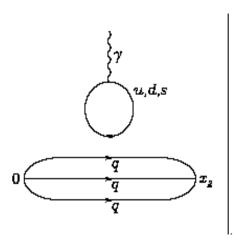




#### **Testing Non-Perturbative QCD**

• Strangeness contribution is a vacuum polarization effect, analogous to Lamb shift in QED





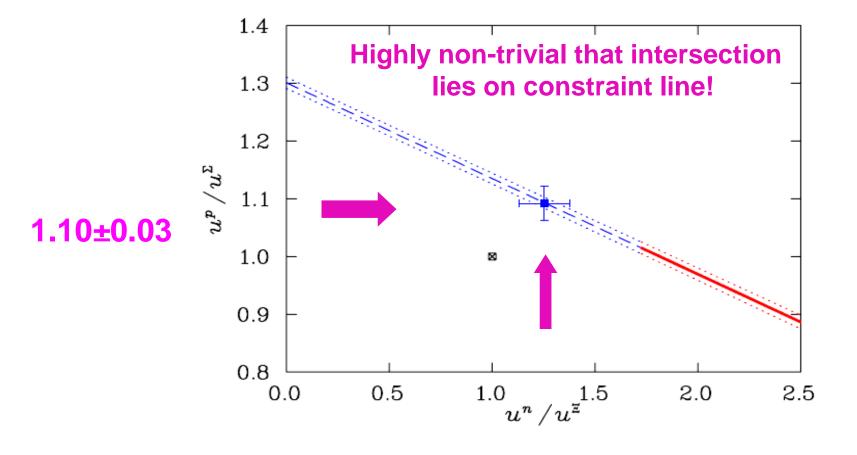
 Checking theoretical calculations versus data constitutes a fundamental test of non-perturbative QCD





## **Indirect Approach** u,d,s $\gamma$ Leinweber et al., Phys Rev D62 (2000) $p = 2/3 u^p - 1/3 d^p + O_N$ $n = -1/3 u^p + 2/3 d^p + O_N$ CS $2p + n = u^p + 3 O_N$ $(and p + 2n = d^p + 3 O_N)$ $\Sigma^{+} = 2/3 u^{\Sigma} - 1/3 s^{\Sigma} + O_{\Sigma}$ $\Sigma^{-} = -1/3 u^{\Sigma} - 1/3 s^{\Sigma} + O_{\Sigma}$ $\Sigma^+$ - $\Sigma^- = \mathbf{u}^\Sigma$ **HENCE**: $O_N = 1/3 [2p + n - (u^p / u^{\Sigma}) (\Sigma^+ - \Sigma^-)]$ Just these ratios from Lattice QCD PECIAL RESEARC $O_{N} = 1/3 [n + 2p - (u^{n} / u^{\Xi}) (\Xi^{0} - \Xi^{-})]$

#### **First Accurate Determination of G**<sub>M</sub><sup>s</sup> **from QCD**



1.25±0.12

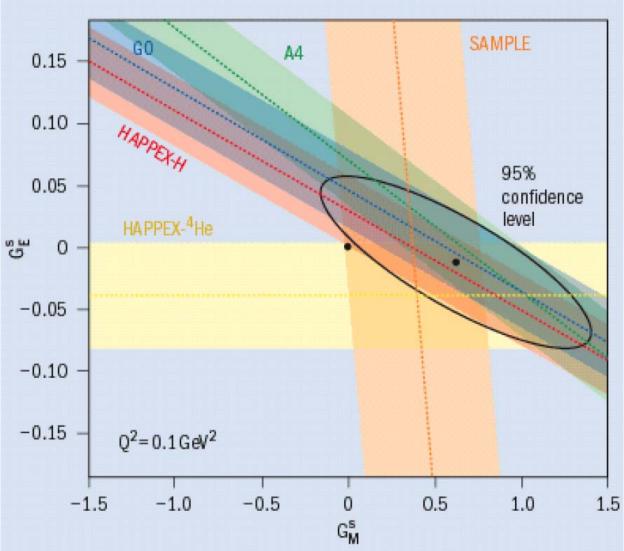
Yields :  $G_{M}^{s} = -0.046 \pm 0.019 \mu_{N}$ 



Leinweber et al., PRL 94 (2005) 212001



#### **Caveat Emptor – CERN Courier 2005**







## **State of the Art Magnetic Moments**

	QQCD	Valence	Full QCD	Expt.
р	2.69 (16)	2.94 (15)	2.86 (15)	2.79
n	-1.72 (10)	-1.83 (10)	-1.91 (10)	-1.91
Σ+	2.37 (11)	2.61 (10)	2.52 (10)	2.46 (10)
Σ-	-0.95 (05)	-1.08 (05)	-1.17 (05)	-1.16 (03)
Λ	-0.57 (03)	-0.61 (03)	-0.63 (03)	-0.613 (4)
Ξ <sup>0</sup>	-1.16 (04)	-1.26 (04)	-1.28 (04)	-1.25 (01)
Ξ	-0.65 (02)	-0.68 (02)	-0.70 (02)	-0.651 (03)
u <sup>Σ</sup>	1.66 (08)	1.85 (07)	1.85 (07)	1.81 (06)
u <sup>E</sup>	-0.51 (04)	-0.58 (04)	-0.58 (04)	-0.60 (01)

SUBAT <u>MIC</u>

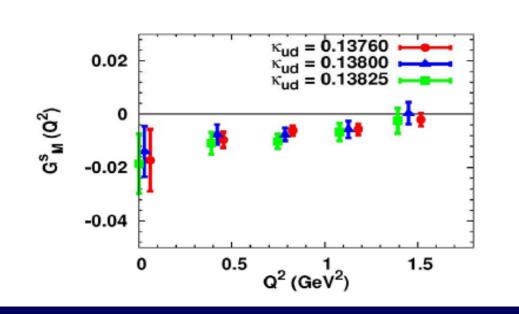
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#### Direct Calculation of $G_M^{s}(Q^2) - K$ .-F. Liu et al.

Strangeness Magnetic Form Factors with 3 Quark Masses  $(m_n = 0.6, 0.7, 0.8 \text{ GeV})$ ; T. Doi et al. ( $\chi$ QCD) arXiV:0903.3232



 $G_M^S(Q^2=0) = -0.017(25)(07) \mu_N$ 

c.f. - 0.046 ± 0.019 (Leinweber et al.)



N.B. Result of Doi et al. increases by factor ~1.8 when light quark mass takes physical value with m<sub>s</sub> fixed (Wang et al., hep-ph/0701082 : Phys Rev D75 (2008) )



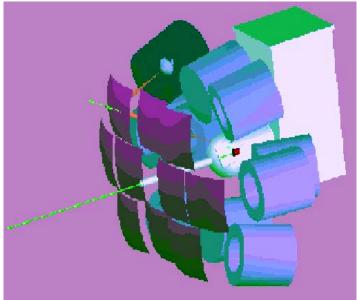
#### **Experiment: Parity Violating Electron Scattering**

$$A^{PV} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} = \begin{bmatrix} -G_F Q^2 \\ \pi \alpha \sqrt{2} \end{bmatrix} \underbrace{\varepsilon G_E^{p\gamma} (G_E^{p2}) + \tau G_M^{p\gamma} (G_M^{p2}) - \frac{1}{2} (1 - 4 \sin^2 \theta_W) \varepsilon' G_M^{p\gamma} (G_A^{p\gamma})}{\varepsilon (G_E^{p\gamma})^2 + \tau (G_M^{p\gamma})^2}$$
Neutral-weak form factors
Assume charge symmetry:
$$4G_{E,M}^{pZ} = (1 - 4 \sin^2 \theta_W) G_{E,M}^{p\gamma} - G_{E,M}^{n\gamma} - G_{E,M}^{s}$$
Proton weak charge
(tree level)
$$Strangeness$$





## **MIT-Bates & A4 at Mainz**



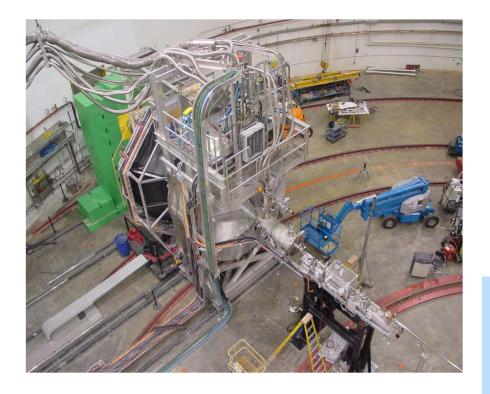


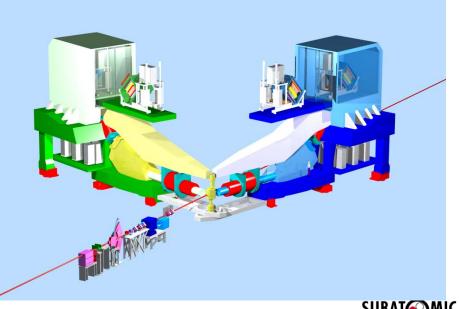






#### **G0 and HAPPEx at Jlab**

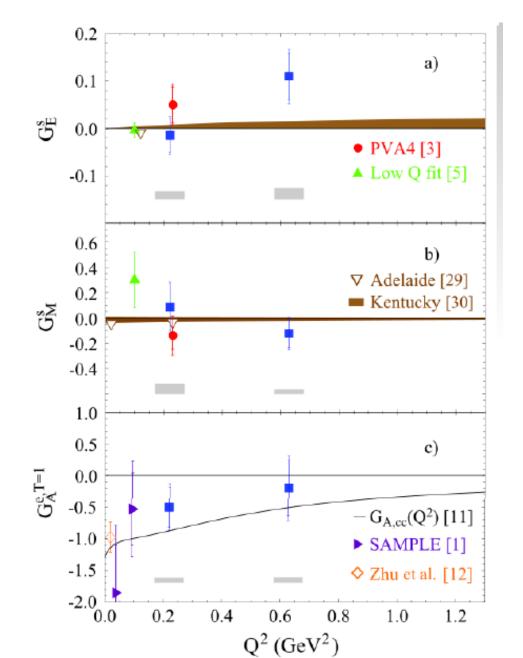








## **PVES Data by 2010**

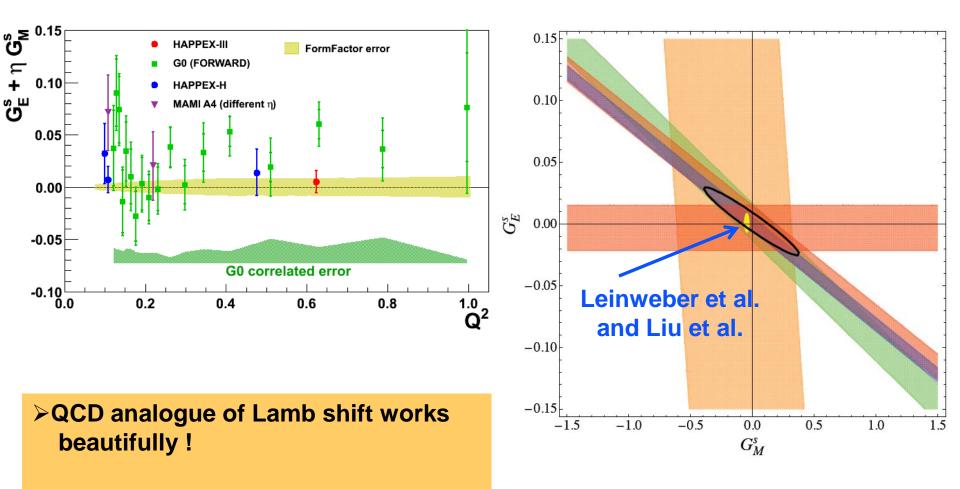






#### **Data Analysis**

 $Q^2 = 0.1 \text{ GeV}^2$ 





Young et al., PRL 99 (2007)122003 & Young arXiv 1004.5163 [nucl-th]

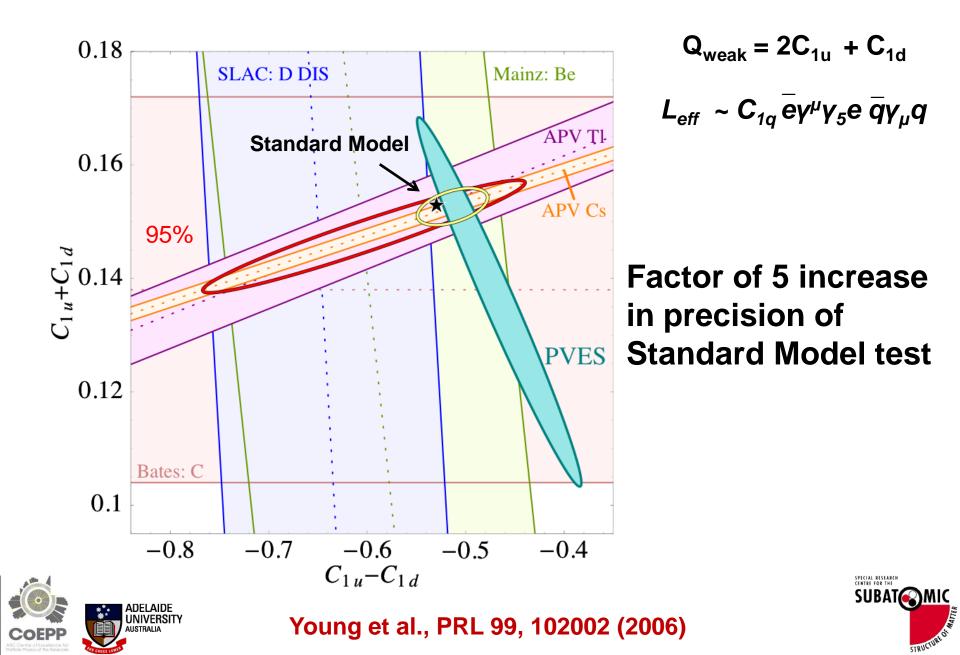






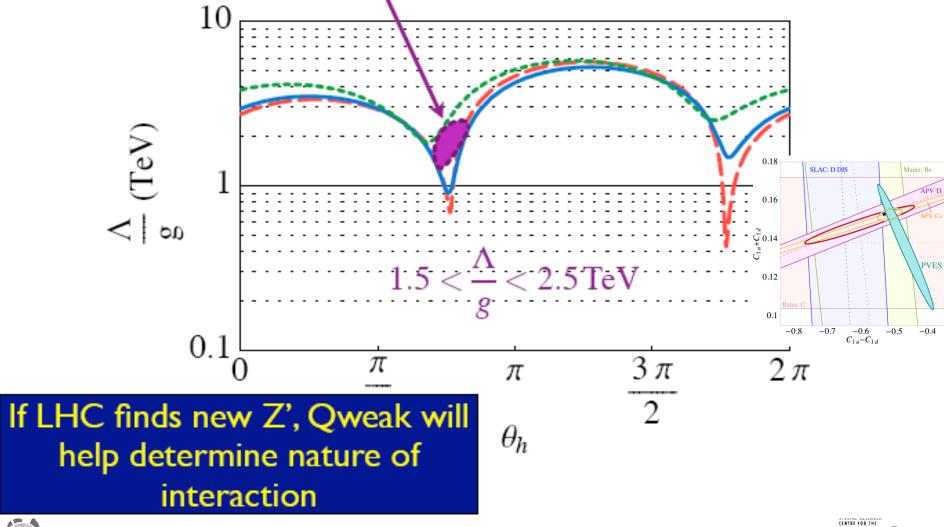


#### Major progress on C<sub>1q</sub> couplings



# **Potential for Q**weak **Discovery**

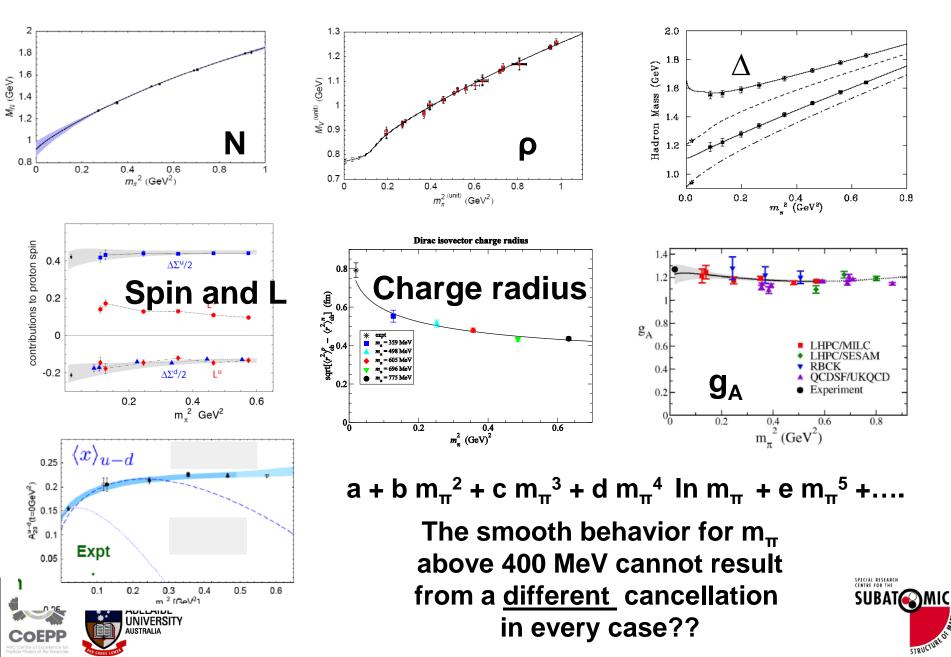
#### Assume Qweak takes central value of current measurements







## Why are the strange form factors so small?



#### Very simple lesson / universal feature of lattice data

• Meson loops are suppressed once the meson

```
mass exceeds ~0.4 GeV
```

- in this region observables either  $\sim c M or c/M$ , with M = M<sub>0</sub> + m<sub>q</sub>
- This corresponds to a remarkably small current

mass –  $m_q \sim 40 \text{ MeV}$ 

• Maybe scale intrinsic to instantons BUT certainly (as in FRR)

the finite size of hadron suppresses loops









# Strange scalar form factor

# (strange σ commutator)

## **Sigma Commutators**

These are a direct measure of the breaking

of chiral symmetry in QCD

•  $\sigma_{\pi N} = \langle N | m_1 (uu + dd) | N \rangle \sim 45-65 \text{ MeV}?$ 

(Gasser, Leutwyler, Sainio...)

• 
$$\sigma_s = \langle N | m_s \overline{s} s | N \rangle \sim 300 \text{ MeV}?$$

(Kaplan, Manohar, early lattice...)

These are the measure of the contribution of the

masses of the quarks to the nucleon mass



 $m_{I} = (m_{u} + m_{d})/2$ 



## **Can use lattice QCD to measure these**

• Feynman-Hellmann theorem:

$$- \sigma_{\pi N} = m_I \partial M_N / \partial m_I$$

$$- \sigma_{\rm s} = m_{\rm s} \partial M_{\rm N} / \partial m_{\rm s}$$

• Hence IF we have a reliable parametrization of

the mass of the nucleon vs  $m_{\pi}$  and  $m_{K}$  we can

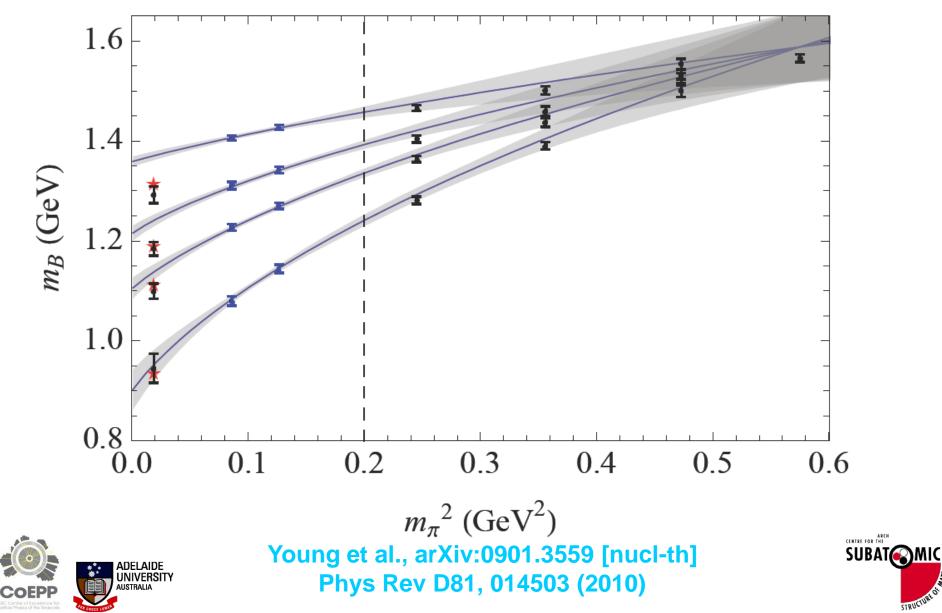
evaluate the  $\sigma$ -terms by differentiation





## **Octet Baryon Masses - LHPC Data**

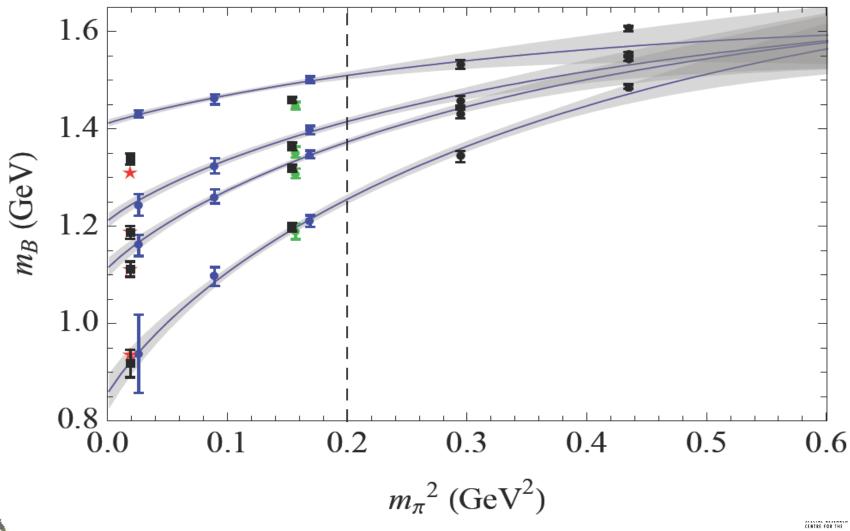
(lattice data: Walker-Loud et al., arXiv:0806.4549)



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## **PACS-CS** Data

(lattice data: Aoki et al., arXiv:0807.1661[hep-lat])







#### Summary of Results of Combined Fits (of 2008 LHPC & PACS-CS data)

	Mass (GeV)	Expt.		$\bar{\sigma}_{Bs}$
N	0.945(24)(4)(3)	0.939	0.050(9)(1)(3)	0.033(16)(4)(2)
$\Lambda$	1.103(13)(9)(3)	1.116	0.028(4)(1)(2)	0.144(15)(10)(2)
Σ	1.182(11)(2)(6)	1.193	0.0212(27)(1)(17)	0.187(15)(3)(4)
Ξ	1.301(12)(9)(1)	1.318	0.0100(10)(0)(4)	0.244(15)(12)(2)

$$\bar{\sigma}_{Bq} = (m_q/M_B)\partial M_B/\partial m_q$$

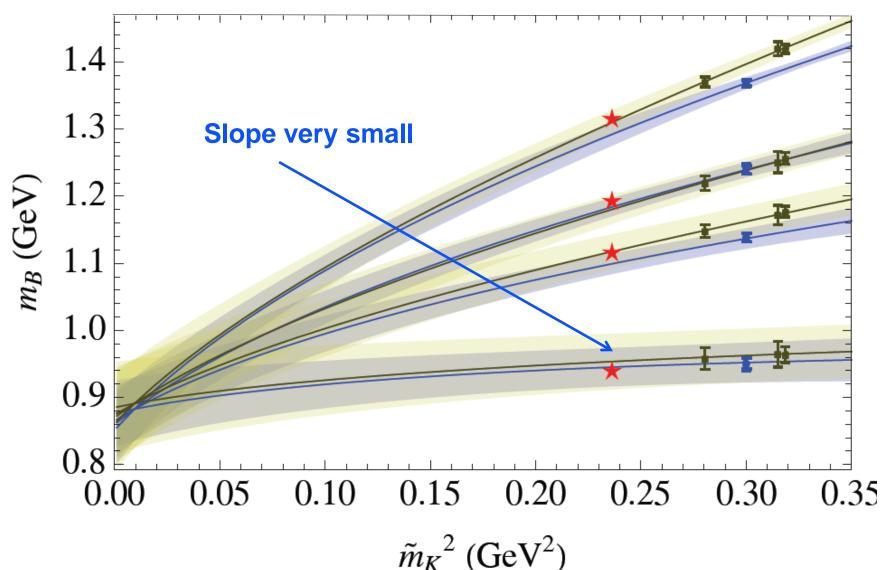
**Of particular interest:** 

 $\label{eq:starses} \begin{aligned} & \sigma \ commutator \ well \ determined : \sigma_{\pi N} = 47 \ (9) \ (1) \ (3) \ MeV \\ & \text{and strangeness sigma commutator } \underline{small} \\ & m_s \ \partial M_N / \ \partial \ m_s = 31 \ (15) \ (4) \ (2) \ MeV \\ & \text{NOT several 100 MeV } ! \end{aligned}$ 

Profound Consequences for Dark Matter Searches



#### **Dependence of Octet Masses on m**<sub>s</sub>

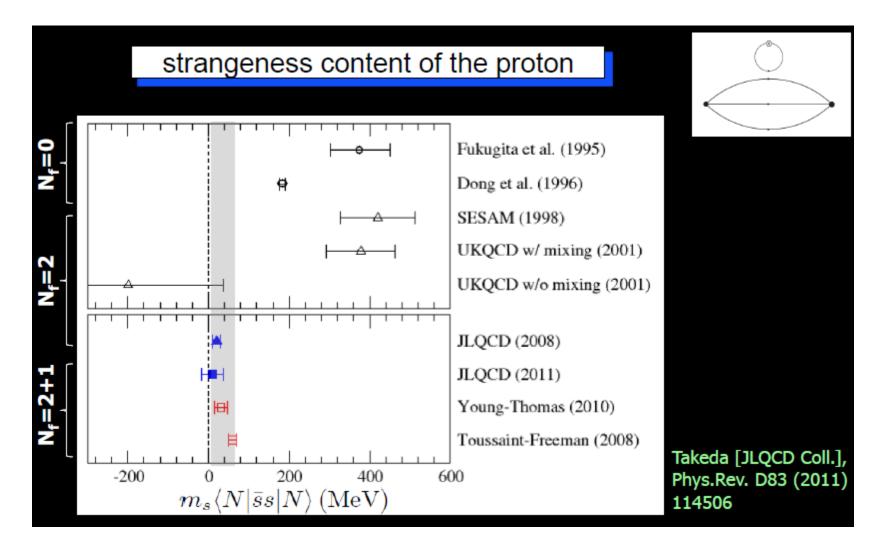




from Young, AIPCP (2011)



## New techniques – new answers





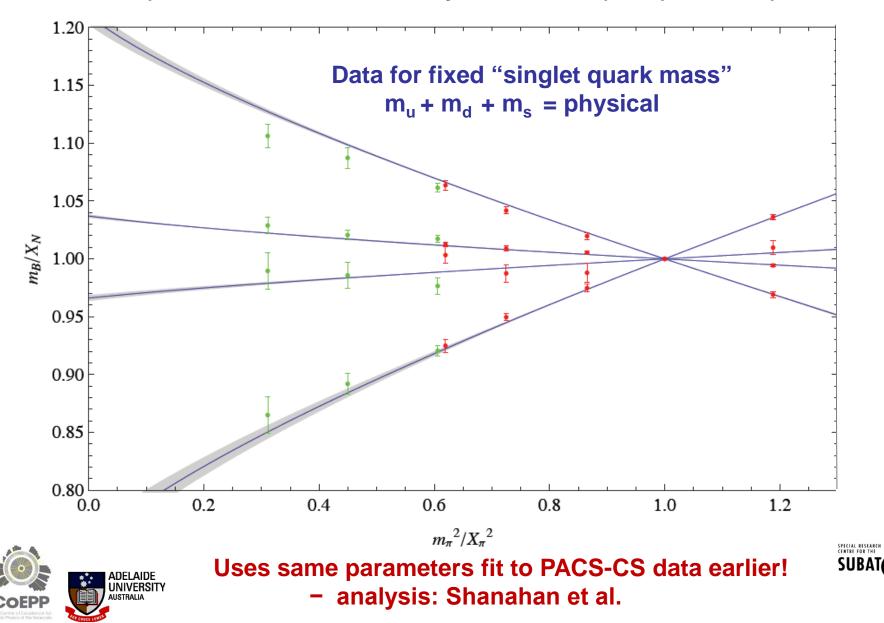
from Hatsuda PANIC 2011

adelaide University

STRALIA

#### Further check: Comparison with UKQCD data

(Data: Bietenholz et al., Phys.Lett. B690 (2010) 436-441 )



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#### Hadronic Uncertainties in the Elastic Scattering of Supersymmetric Dark Matter

John Ellis,<sup>1,\*</sup> Keith A. Olive,<sup>2,†</sup> and Christopher Savage<sup>2,‡</sup>

```
CERN-PH-TH/2008-005
UMN-TH-2631/08
FTPI-MINN-08/02
```

We find that the spin-independent cross section may vary by almost an order of magnitude for 48 MeV  $< \Sigma_{\pi N} < 80$  MeV, the  $\pm 2$ - $\sigma$  range according to the uncertainties in Table I. This uncertainty is already impacting the interpretations of experimental searches for cold dark matter. Propagating the  $\pm 2$ - $\sigma$  uncertainties in  $\Delta_s^{(p)}$ , the next most important parameter, we find a variation by a factor  $\sim 2$  in the spin-dependent cross section. Since the spinindependent cross section may now be on the verge of detectability in certain models, and the uncertainty in the cross section is far greater, we appeal for a greater, dedicated effort to reduce the experimental uncertainty in the  $\pi$ -nucleon  $\sigma$  term  $\Sigma_{\pi N}$ . This quantity is not just an object of curiosity for those interested in the structure of the nucleon and nonperturbative strong-interaction effects: it may also be key to understanding new physics beyond the Standard Model.

$$\mathcal{L} = \alpha_{2i} \bar{\chi} \gamma^{\mu} \gamma^{5} \chi \bar{q}_{i} \gamma_{\mu} \gamma^{5} q_{i} + \alpha_{3i} \bar{\chi} \chi \bar{q}_{i} q_{i} \right)^{\sigma \text{ terms}}$$

Neutralino (0.3 GeV / cc : WMAP )





#### What Ellis et al. really wanted...

Use naive SU(3) to extract  $\sigma_0$  from octet masses:

$$\sigma_0 = m_\ell \langle N | \bar{u}u + \bar{d}d - 2\bar{s}s | N \rangle$$

Then use difference from  $\,\sigma_{\pi N}\,$  to extract what is really needed, namely  $\sigma_s$ 

$$\sigma_{\ell} - \sigma_0 = 2 \frac{m_{\ell}}{m_s} \sigma_s$$

**Problem :** a small error in  $\sigma_0$  leads to a huge error

in  $\sigma_s$  – its much better to determine  $\sigma_s$  directly!





#### CMSSM Predictions for Dark Matter $\sigma$

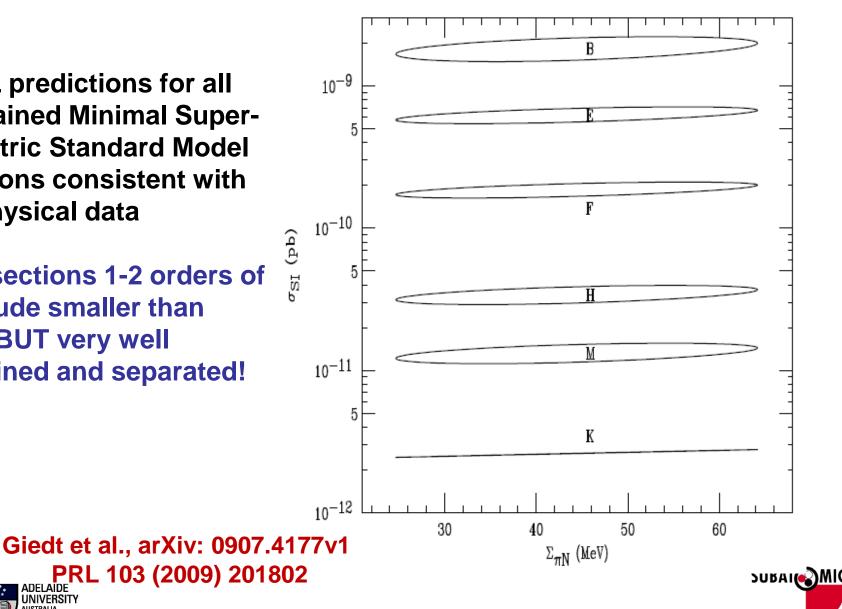
In response to request by Ellis, Olive & Savage.... Old Model C 2  $10^{-9}$ (d d) **Cross section accurately fixed** (e.g. "New model C") c.f. using N old relation to unknown  $\pi N$ sigma commutator 5 ("Old Model C") **New Model C** Giedt et al., arXiv: 0907.4177v1 2 PRL 103 (2009) 201802 30 60 70 40 50  $\Sigma_{\pi N}$  (MeV)



#### **CMSSM** Predictions for Dark Matter $\sigma$

95% CL predictions for all **Constrained Minimal Super-**Symmetric Standard Model extensions consistent with astrophysical data

**Cross sections 1-2 orders of** magnitude smaller than before BUT very well determined and separated!





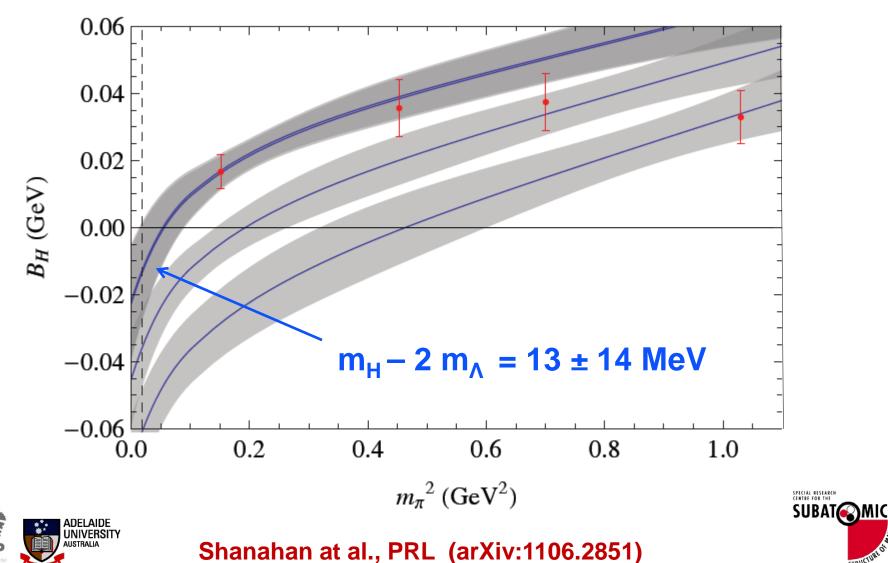
## **Latest Strange Twist**





## The H-di-baryon again

# Using data from NPLQCD & HAL: H bound at larger $m_l \rightarrow$ H-di-baryon almost bound at physical masses





Nuclear Physics A691 (2001) 242c-245c

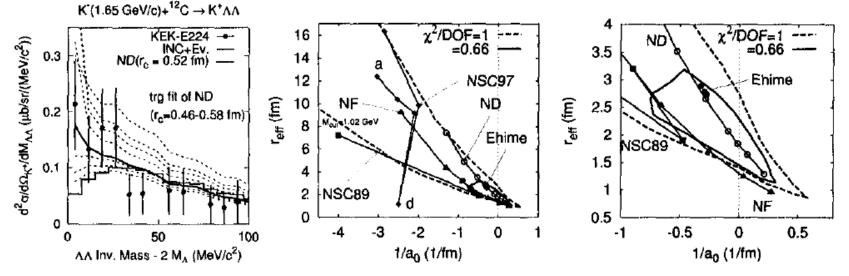


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www.elsevier.com/locate/npe

 $\Lambda - \Lambda$  correlation in  $(K^-, K^+)$  reaction — Is there a virtual pole ?

A. Ohnishi<sup>a</sup>, Y. Hirata<sup>a,b</sup>, Y. Nara<sup>b,c</sup>, S. Shinmura<sup>d</sup> and Y. Akaishi<sup>e</sup>



In this paper, we have studied the hyperon momentum distribution and correlation between  $\Lambda\Lambda$  in  $(K^-, K^+)$  reactions. Global understanding of  $K^+$  and  $\Lambda$  momentum distribution is achieved in a microscopic transport model. The correlation function analysis suggests that attractive  $\Lambda\Lambda$  interaction is necessary, and the best fit interaction makes  $\Lambda\Lambda$  system barely unbound. It may be possible that a virtual pole of  $\Lambda\Lambda$  system would exist. Higher statistics data is desired to determine  $\Lambda\Lambda$  interaction more precisely.



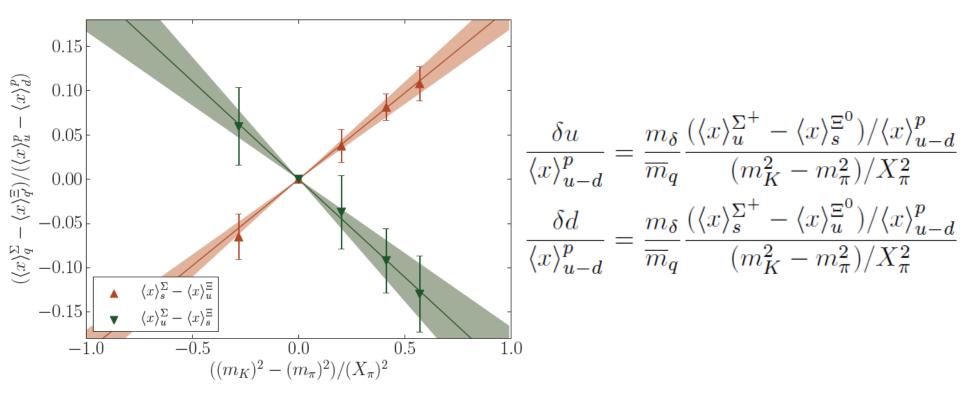
adelaide University

# Charge Symmetry Violation – s-quark as heavy d





### Lattice QCD – Octet Moments Probe CSV



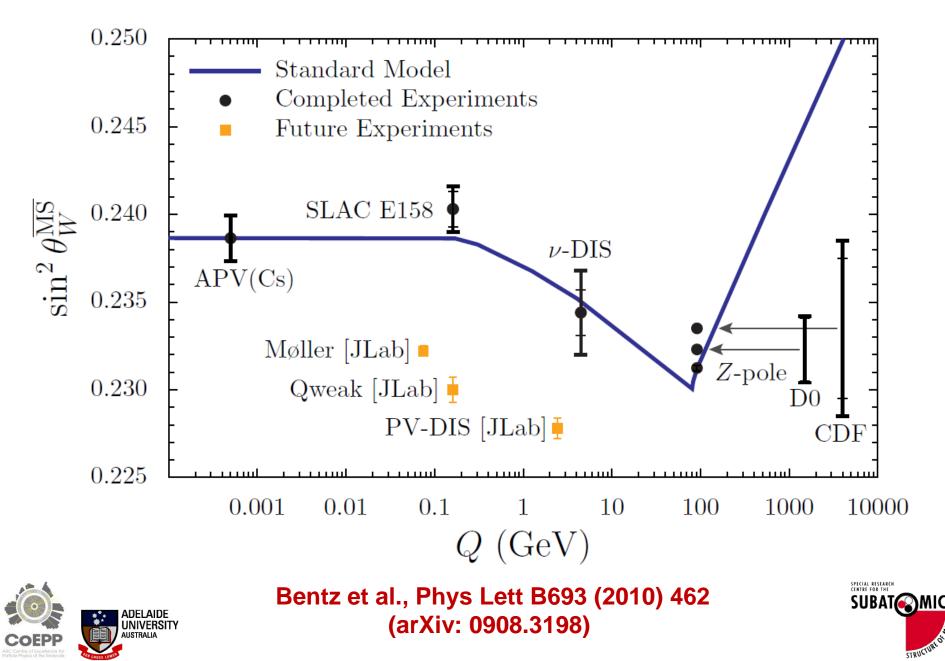
**Deduce:**  $\delta u = -0.0023(6), \quad \delta d = 0.0020(3)$ 

- in excellent agreement with phenomenological estimates of Rodionov *et al.*  $\delta u^- = -0.0014$  and  $\delta d^- = 0.0015$ 



Horsley et al., arXiv: 1012.0215 [hep-lat] Phys Rev D83 (2011) 051501(R)

### The Standard Model works... again



### **Summary of Corrections to NuTeV Analysis**

- Isovector EMC effect:  $\Delta R^{\rho^0} = -0.0019 \pm 0.0006$ 
  - using NuTeV functional
- **CSV:**  $\Delta R^{\text{CSV}} = -0.0026 \pm 0.0011$ 
  - again using NuTeV functional
- Strangeness:  $\Delta R^{s} = -0.0011 \pm 0.0014$ 
  - this is largest uncertainty (systematic error); desperate need for an accurate determination of s<sup>-</sup>(x), e.g. semi-inclusive DIS?
- Final result:  $\sin^2 \theta_W = 0.2221 \pm 0.0013 (\text{stat}) \pm 0.0020 (\text{syst})$

- c.f. Standard Model: 
$$\sin^2 heta_W = 0.2227 \pm 0.0004$$



Bentz et al., Phys Lett B693 (2010) 462 (arXiv: 0908.3198)



## **Strange Quark Sea – still mysterious**



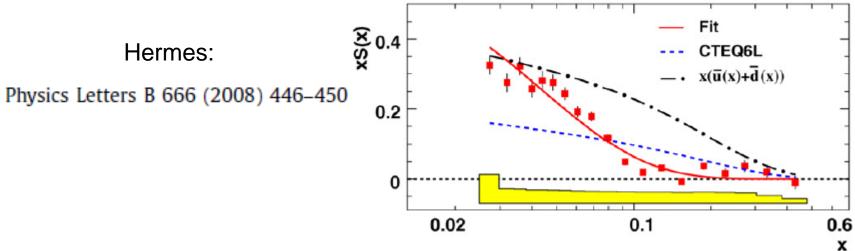


#### PHYSICAL REVIEW D **79**, 094502 (2009)

#### Moments of nucleon's parton distribution for the sea and valence quarks from lattice QCD

M. Deka,<sup>1,\*</sup> T. Streuer,<sup>2</sup> T. Doi,<sup>1</sup> S. J. Dong,<sup>1</sup> T. Draper,<sup>1</sup> K. F. Liu,<sup>1</sup> N. Mathur,<sup>3</sup> and A. W. Thomas<sup>4</sup>

We provide results for both the connected and disconnected insertions. The perturbatively renormalized  $\langle x \rangle$  for the strange quark at  $\mu = 2$  GeV is  $\langle x \rangle_{s+\bar{s}} = 0.027 \pm 0.006$  which is consistent with the experimental result.



Odd shape: interpreted (e.g.) by Chang and Peng (PRL 2011) as 5-q component of nucleon wave function



? LO analysis & model dependence? - needs more work!



## Summary

QCD yields excellent agreement with experiment

- success analogous to Lamb shift in QED

•  $\sigma_s$  evaluated using new techniques and order of

magnitude smaller than previously thought

- with dramatic consequences for Dark Matter searches

• Rumours of the death of the H-di-baryon may be

"much exaggerated" - likely just unbound!





## Summary (cont.)

- Can use lattice simulations with s acting as a heavy d-quark – to probe CSV
- Of critical importance to interpretation of NuTeV expt.
- Strange sea also needed there AND presents its own mysteries – e.g. apparentlyodd shape of s + s
- s s likely small (meson cloud picture recall kaon loops suppressed as general result of lattice studies)









#### Dynamical Symmetry Breaking in the Sea of the Nucleon

$$(S - \bar{S})^{(n)} = \int_0^1 dx \, x^n [s(x) - \bar{s}(x)] = V_\Lambda^{(n)} \cdot f_{\Lambda K}^{(n)} - V_K^{(n)} \cdot f_{K\Lambda}^{(n)}$$
$$f_{K\Lambda}^{(n)}|_{\text{LNA}} = \frac{27}{25} \, \frac{M^2 g_A^2}{(4\pi f_\pi)^2} \, (M_\Lambda - M)^2 (-1)^n \, \frac{m_K^{2n+2}}{\Delta M^{2n+4}} \log(m_K^2/\mu^2) \,,$$
$$n \text{th moment of } \bar{s} \text{ is of order } m_K^{2n+2} \, \log m_K^2$$

LNA contribution to the *n*th moment of *s* is of order  $m_K^2 \log m_K^2$ 

#### Compared with the first case: dbar-ubar asymmetry in the proton

$$f_{\pi N}^{(n)}|_{\text{LNA}} = [3M^2 g_A^2 / (4\pi f_\pi)^2] \times \begin{cases} (-1)^{n/2} [(n+4)/(2n+4)] (m_\pi/M)^{n+2} \log(m_\pi^2/\mu^2) & (n=0,2,4,\ldots) \\ (-1)^{(n+1)/2} [(n+5)/2] (m_\pi/M)^{n+3} \log(m_\pi^2/\mu^2) & (n=1,3,5,\ldots) \end{cases}$$



$$(\overline{D} - \overline{U})^{(n)} = -\frac{1}{3} V_{\pi}^{(n)} \cdot f_{\pi\Delta}^{(n)}$$



## **Strange Quark Asymmetry**

- Required in principle by chiral symmetry (s and s have different chiral behaviour\*)
- Experimental constraint primarily through opposite sign di-muon production with neutrinos (CCFR & NuTeV)

	$\langle x  s^-  angle$	$\Delta R^s$	$\Delta R^{\mathrm{total}}$	$\sin^2 \theta_W \pm \text{syst.}$
Mason $et \ al. \ [8]$	$0.00196 \pm 0.00143$	$-0.0018 \pm 0.0013$	$-0.0063 \pm 0.0018$	$0.2214 \pm 0.0020$
NNPDF [9]	$0.0005 \pm 0.0086$	$-0.0005 \pm 0.0078$	$-0.0050 \pm 0.0079$	$0.2227\pm large$
Alekhin et al. [31]	$0.0013 \pm 0.0009 \pm 0.0002$	$-0.0012 \pm 0.0008 \pm 0.0002$	$-0.0057 \pm 0.0015$	$0.2220 \pm 0.0017$
MSTW [32]	$0.0016\substack{+0.0011\\-0.0009}$	$-0.0014_{+0.0008}^{-0.0010}$	$-0.0059 \pm 0.0015$	$0.2218 \pm 0.0018$
CTEQ [33]	$0.0018\substack{+0.0016\\-0.0004}$	$-0.0016\substack{+0.0014\\-0.0004}$	$-0.0061\substack{+0.0019\\-0.0013}$	$0.2216\substack{+0.0021\\-0.0016}$
This work (Eq. $(10)$ )	$0.0\pm0.0020$	$0.0\pm0.0018$	$-0.0045 \pm 0.0022$	$0.2232 \pm 0.0024$



\* Signal & Thomas, Phys Lett B191 (1987) 205; ELAIDE IVERSITY Thomas et al., PRL 85 (2000) 2892



### **Separate Neutrino and Anti-Neutrino Ratios**

• Biggest criticism of this explanation was that NuTeV actually measured  $R^{\nu}$  and  $R^{\bar{\nu}}$ , separately: Claim we should compare directly with these.

• Have done this: 
$$\delta R^{\nu} = \frac{2\left(3\,g_{Lu}^2 + g_{Ru}^2\right)\left\langle x_A\,u_A^- - x_A\,d_A^-\right\rangle}{\left\langle 3\,x_A\,u_A + 3\,x_A\,d_A + x_A\,\bar{u}_A + x_A\,\bar{d}_A + 6\,x_A\,s_A\right\rangle}$$
$$\delta R^{\bar{\nu}} = \frac{-2\left(3\,g_{Rd}^2 + g_{Ld}^2\right)\left\langle x_A\,u_A^- - x_A\,d_A^-\right\rangle}{\left\langle x_A\,u_A + x_A\,d_A + 3\,x_A\,\bar{u}_A + 3\,x_A\,\bar{d}_A + 6\,x_A\,\bar{s}_A\right\rangle}$$

• Then  $R^{\nu}$  moves from  $0.3916 \pm 0.0013$  c.f. 0.3950 in the Standard Model to  $0.3933 \pm 0.0015$ ;

 $R^{ar{
u}}$  moves from  $0.4050\pm0.0027$  to  $0.4034\pm0.0028$ , c.f. 0.4066 in SM

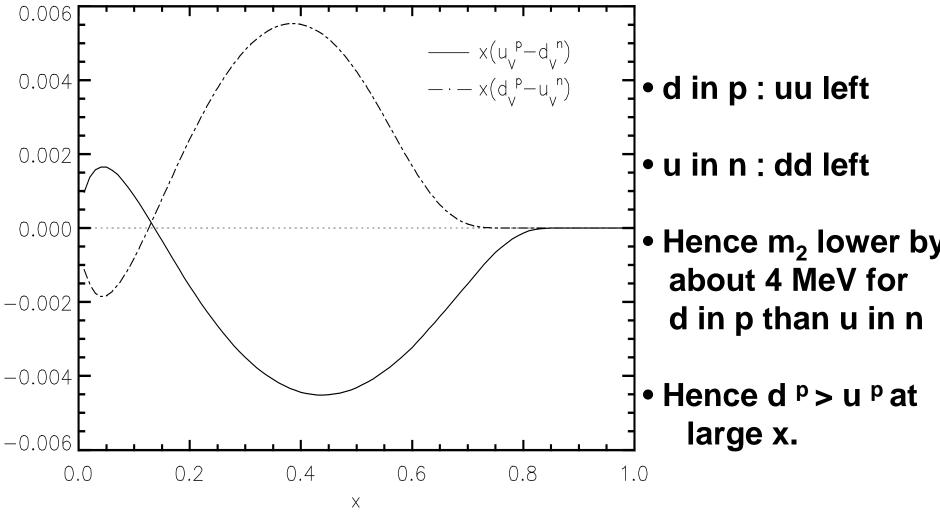
 This is tremendous improvement : χ<sup>2</sup> changes from 7.2 to 2.6 for the two ratios!



Bentz et al., Phys Lett B693 (2010) 462 ( arXiv: 0908.3198)



## **Application to Charge Symmetry Violation**



From: Rodionov et al., Mod Phys Lett A9 (1994) 1799



#### **Remarkably Similar to MRST Fit 10 Years Later**

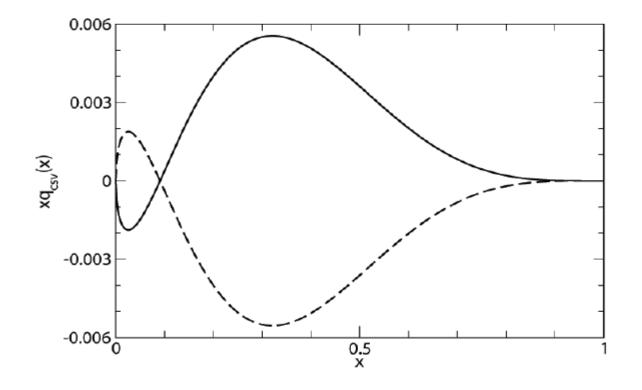


FIG. 5: The phenomenological valence quark CSV function from Ref. [23], corresponding to best fit value  $\kappa = -0.2$  defined in Eq. (35). Solid curve:  $x \delta d_{\rm v}$ ; dashed curve:  $x \delta u_{\rm v}$ .







