Neutrino mass sensitivity with the Ptolemy demonstrator: approach 1

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- sensitivity estimate for "bare" Tritium spectrum (i.e. in vacuum decay)
- effect on sensitivity of Heisenberg ZPF in the initial state for free ³He⁺ decay
- TODO: sensitivity from analysis of end-points of bound ³He⁺ decays





PTOLEMY demonstrator neutrino mass statistical sensitivity / 1



Simulated tritium spectrum in PTOLEMY demonstrator for

- 1 µg of ³H (\approx 50 cm² at 100% graphene loading) \rightarrow **A**_{3H}=**370 MBq**
- 3 year measurement (t_{M})
- EMF selection: $\boldsymbol{E}_{\min} = \boldsymbol{q}_{e}(\boldsymbol{V}_{3H} \boldsymbol{V}_{TES}) \rightarrow \boldsymbol{Q}' = \boldsymbol{Q}_{3H} \boldsymbol{E}_{\min}$
- rate on TES microcal array (MCA) A'≈ЗА_{зн}(Q'/Q_{зн})^{3/2}
- pile-up probability $f_{pp} = A' \tau_R / n_{pix}$ (TES τ_R time resolution)
- for $Q'=30 \text{ eV} \rightarrow A'=2.3 \text{ c/s} \rightarrow f_{pp}=10^{-5} \text{ for } n_{pix}=1 \text{ and } \tau_{R}=1 \text{ } \mu\text{s}$



PTOLEMY demonstrator statistical sensitivity

estimated by frequentist approach

- $N'_{ev} = \eta A' t_{M}$
- pitch angle acceptance $\eta=1$ (i.e. $0 < \theta_{\beta} \le 180^{\circ}$)
- no background

A.Nucciotti, et al., Astropart.Phys. 34 (2010) 80–89; https://doi.org/10.1016/j.astropartphys.2010.05.004

PTOLEMY demonstrator neutrino mass statistical sensitivity / 2

PTOLEMY demonstrator statistical sensitivity estimated by frequentist approach

- pitch angle acceptance η for $\theta_{\beta}=$ 30°, 45°, 60°, 90°, 180°
- geometrical TES efficiency (coverage): 0.5
- $N'_{ev} = 0.5 \ \eta \ A' \ t_{M}$
- $f_{pp} = 0.5 \eta A' \tau_{R} / n_{pix}$
- Δ*E*_{FWHM}=0.1eV



B

θβ

Systematic uncertainty because of unknown Heisenberg ZPF broadending

- ZPF broadening with 0.17 eV $\leq \Delta E \leq 0.75$ eV (5 values in the interval)
- ZPF broadening in "experimental spectra" vs. broadening in fit "model"
- perfectly known TES resolution $\Delta E_{FWHM} = 0.1 eV$

| • | pitch | angle | acceptance | η=1 |
|---|-------|-------|------------|-----|
|---|-------|-------|------------|-----|

| Potential | Source | κ , [eV/Å ²] | $\lambda, [\text{Å}]$ | $\Delta E, [eV]$ |
|---------------|--------------|---------------------------------|-----------------------|------------------|
| Chemisorption | [23] | 2.15 | 0.16 | 0.60 |
| | [21], GGA | 4.62 | 0.13 | 0.73 |
| | [21], vdW-DF | 4.9 | 0.13 | 0.75 |
| Physisorption | [24] | 0.08 | 0.37 | 0.26 |
| | [23] | 0.09 | 0.34 | 0.28 |
| | [21], GGA | 0.18 | 0.29 | 0.33 |
| | [21], vdW-DF | 0.13 | 0.32 | 0.2 |
| | [22], GGA | 0.04 | 0.43 | 0.22 |
| | [22], LDA | 0.01 | 0.55 | 0.17 |
| Migration | [26] | 0.283 | 0.264 | 0.37 |

https://doi.org/10.1103/PhysRevD.104.116004



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background due to bound state decays not included!



Systematic uncertainty because of unknown Heisenberg ZPF broadending

- ZPF broadening with 0.17 eV $\leq \Delta E \leq 0.75$ eV (5 values in the interval)
- complete ignorance
 - uncertain ZPF broadening in "experimental spectra", flat distributed in $[\Delta E(1-\alpha), \Delta E(1+\alpha)]$
 - fit "model" with only TES resolution
- perfectly known TES resolution $\Delta E_{FWHM} = 0.1 eV$
- pitch angle acceptance $\eta=1$

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Sensitivity estimates Including intial and final states

- Use complete composite spectrum with neutrino mass affecting all spectra end-points
- Inputs for simulation:
 - ZPF broadening in final free ³He⁺ decay known from theory
 - Resitdual theoretical uncertainties \rightarrow systematic uncertainties
 - known branching ratios between free and bound ³He⁺ decays
 - known end-points for final free and bound ³He⁺ decays
- Expected consequences
 - ZPF ΔE≈1 eV would limit statistical sensitivity
 - Background from higher end-point spectra would limit statistical sensitivity
 - Decay on final bound ³He⁺ in 1st excited has too low rate at end-point

