

Challenges and ideas for the absorption of the **relic neutrino**

PTOLEMY collaboration meeting
6-8 November

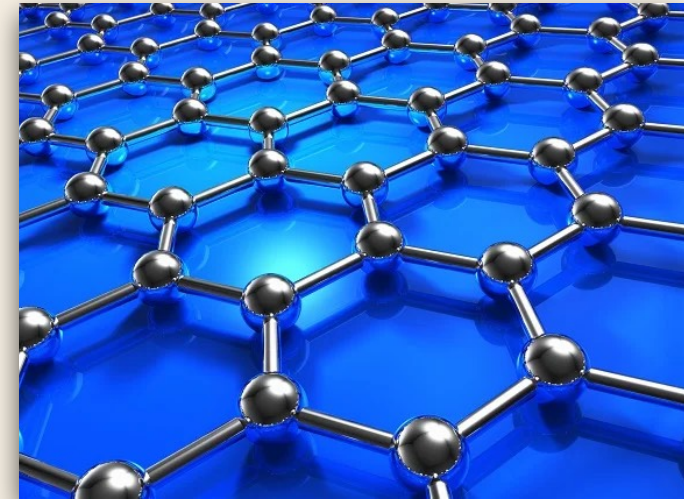
Andrea Casale



SAPIENZA
UNIVERSITÀ DI ROMA

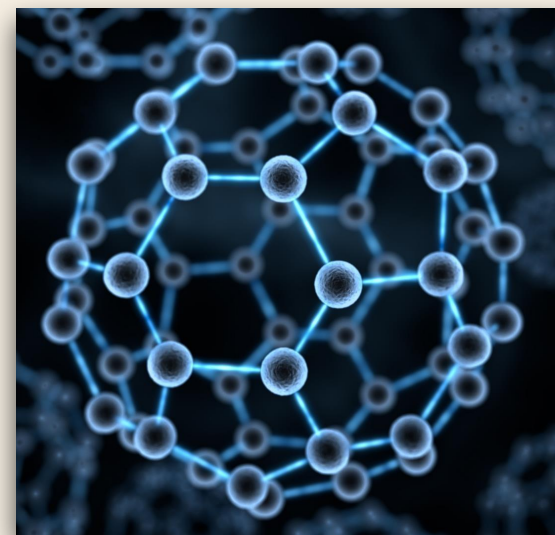
Overview

- **Graphene** and relic neutrinos don't seem to get along



- How would the electron spectra vary if we changed the **substrate**?

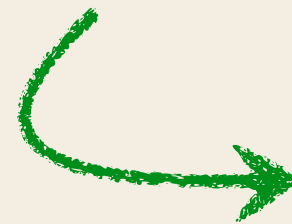
- First results from **fullerenes**



Relic neutrinos

Why is it important to detect relic neutrinos?

- Decoupled from ordinary matter just **1 second** after the Big Bang

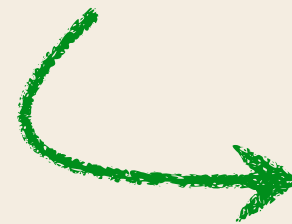


They carry invaluable information about the early Universe

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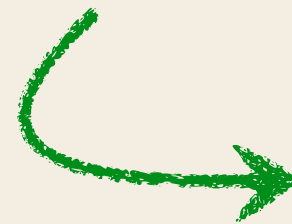
Why is it so difficult?

- 1) Mainly interact through **weak** interactions
- 2) Very **small masses**
- 3) Kinetic energies around 10^{-4} to 10^{-6} eV

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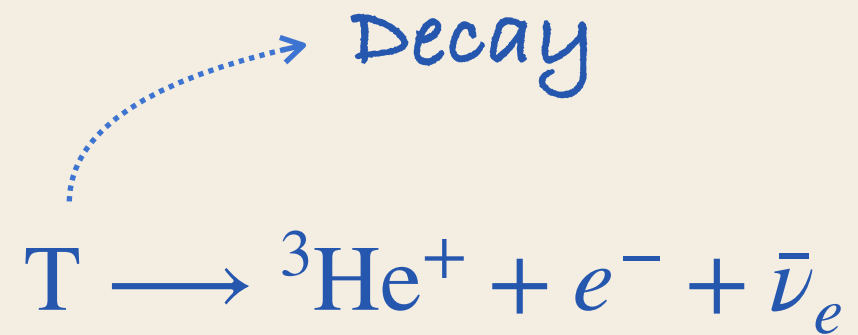
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Weinberg: **neutrino absorption!**

[Weinberg, 1962 Phys. Rev. 128 1457]

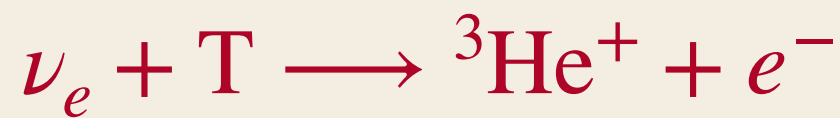
CNB detection in vacuum



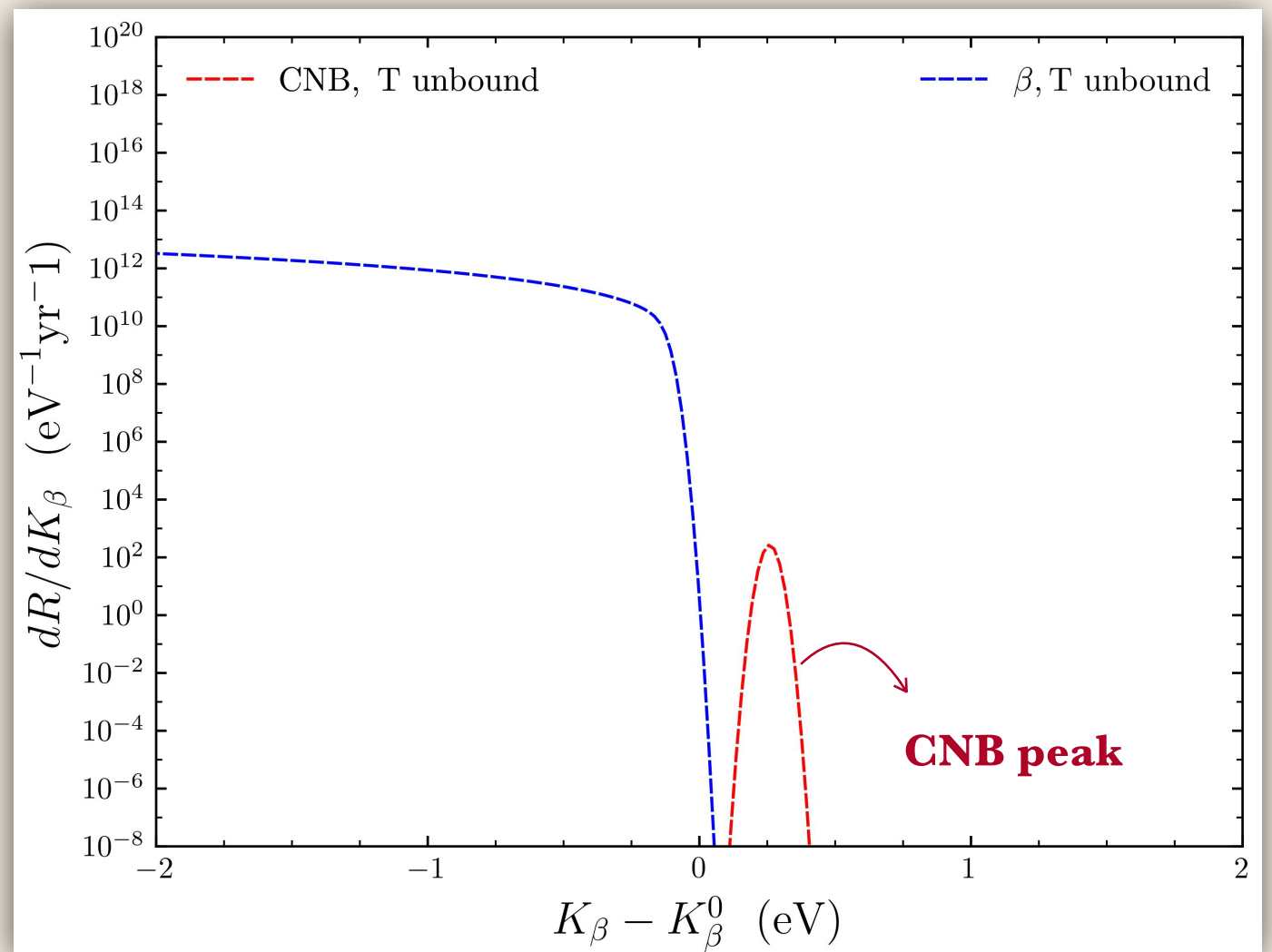
Neutrino absorption

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Decay

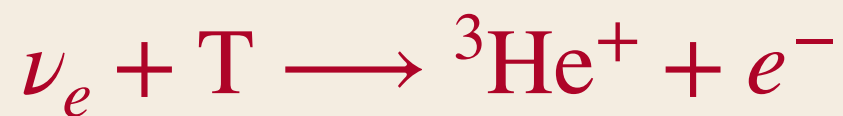


Neutrino absorption



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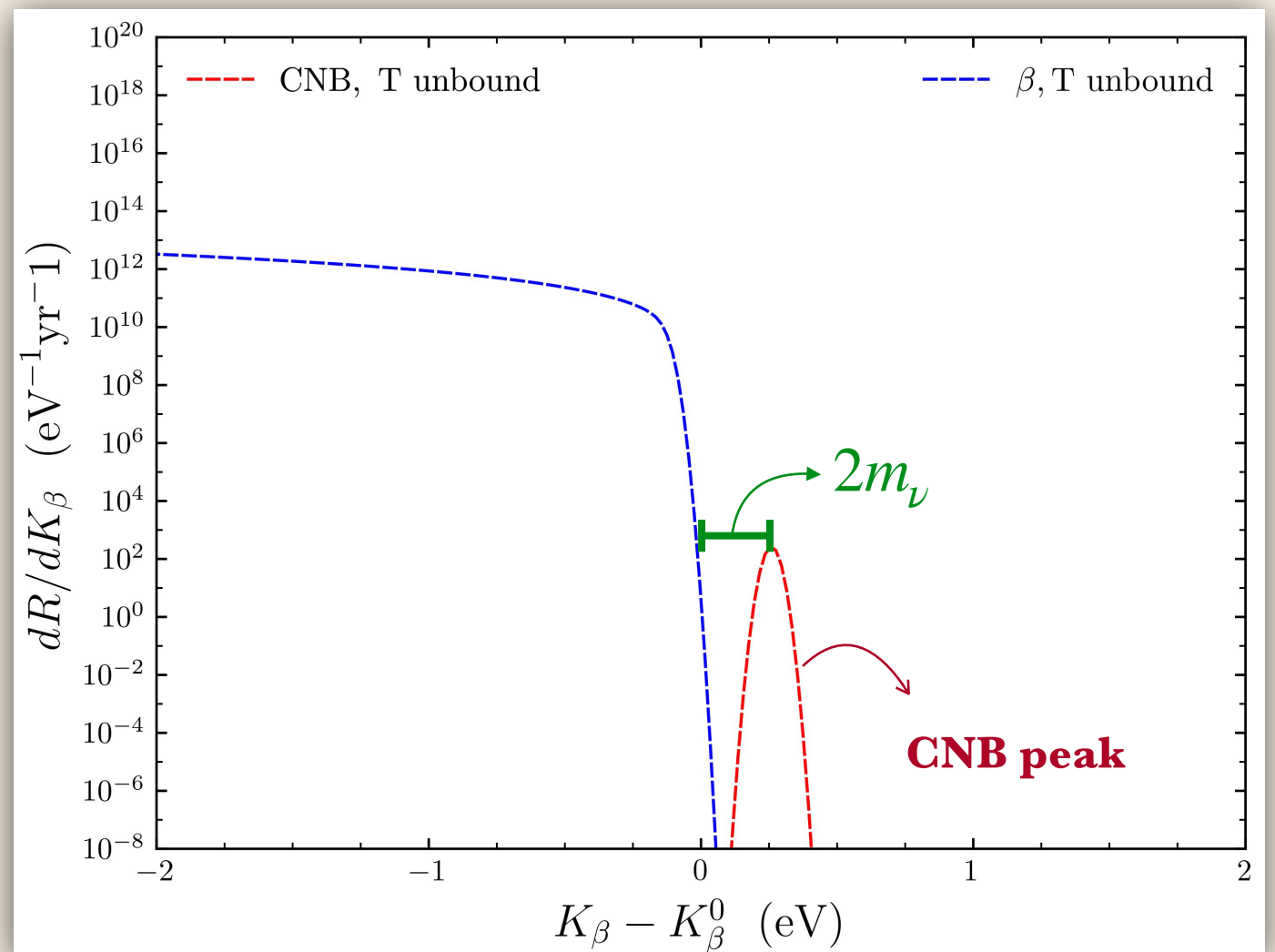
Decay



Neutrino absorption

• What do we need?

- 1) Enough **events** per year
- 2) Good **energy resolution**

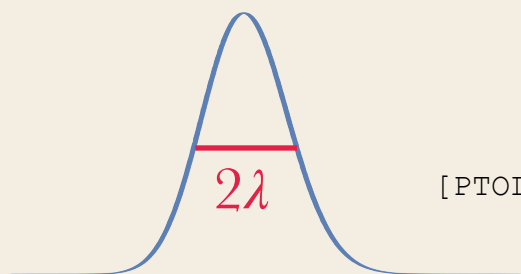


PTOLEMY with graphene

- What does graphene bring on the table? (potentially)
 1. **100 g** of tritium
 2. Energy resolution of **50 meV**

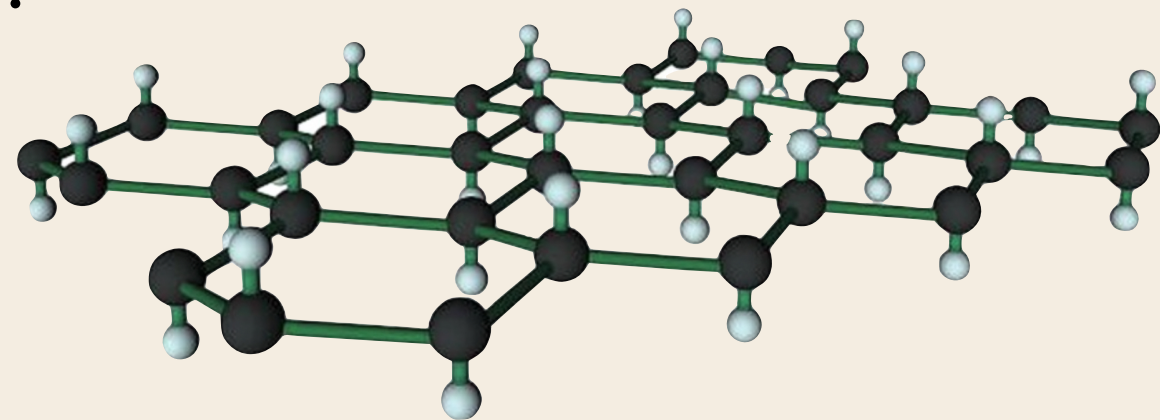
PTOLEMY with graphene

- What does graphene bring on the table? (potentially)
 1. **100 g** of tritium
 2. Energy resolution of **50 meV**
- How to describe tritium **initial state**?

$$\Psi_T(\vec{x}) \propto e^{-\vec{x}^2/2\lambda^2}$$


Localization
 $\lambda \simeq 0.08 \text{ \AA}$

[PTOLEMY – PRD 2022, 2203.11228]

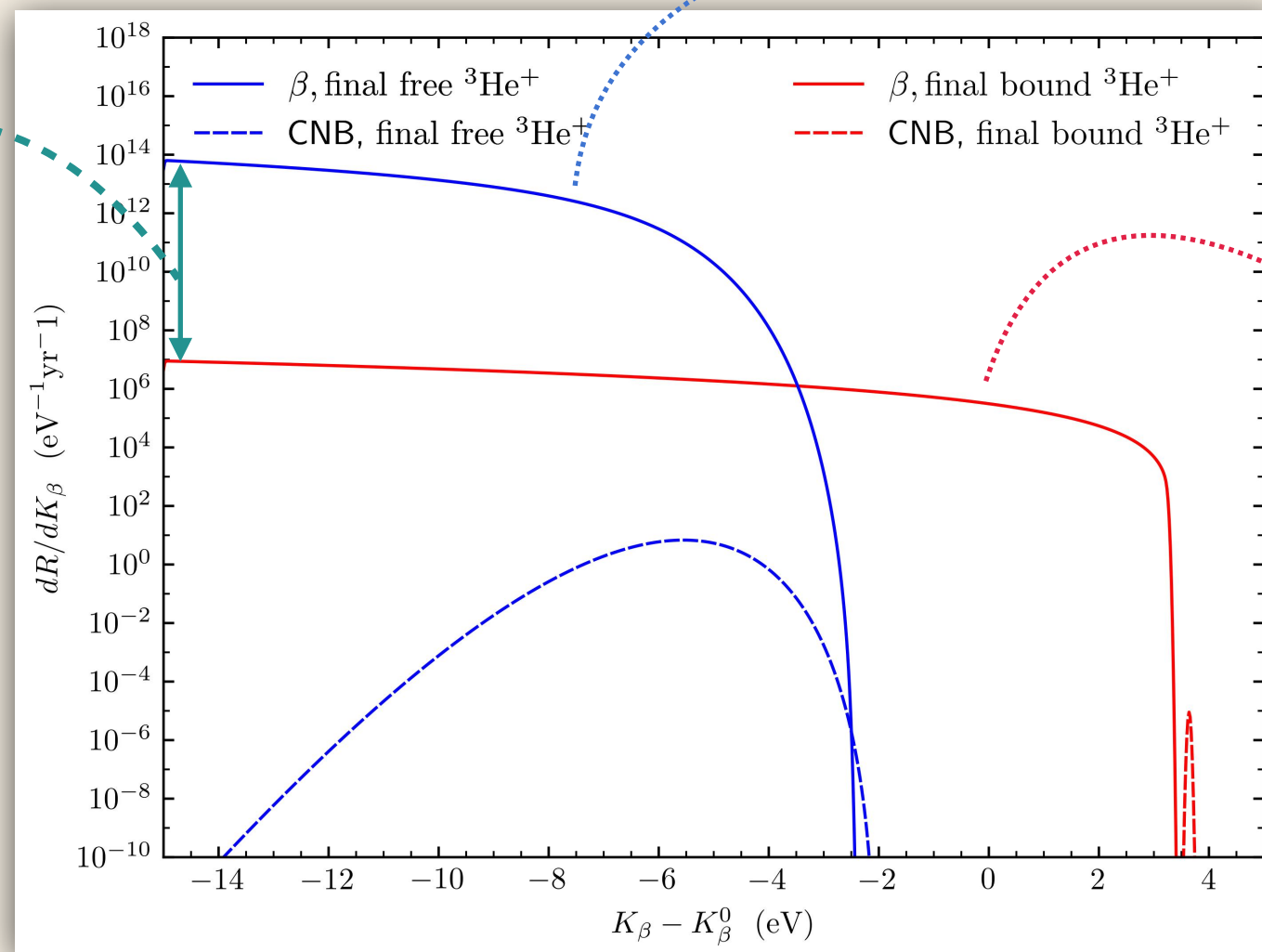


Results from graphene

- Final **bound states** are suppressed

$$d\Gamma_F \propto e^{-\lambda^2 |\vec{p}_\beta + \vec{p}_{\text{He}}|^2}$$

Suppression
of $\sim 10^{-7}$

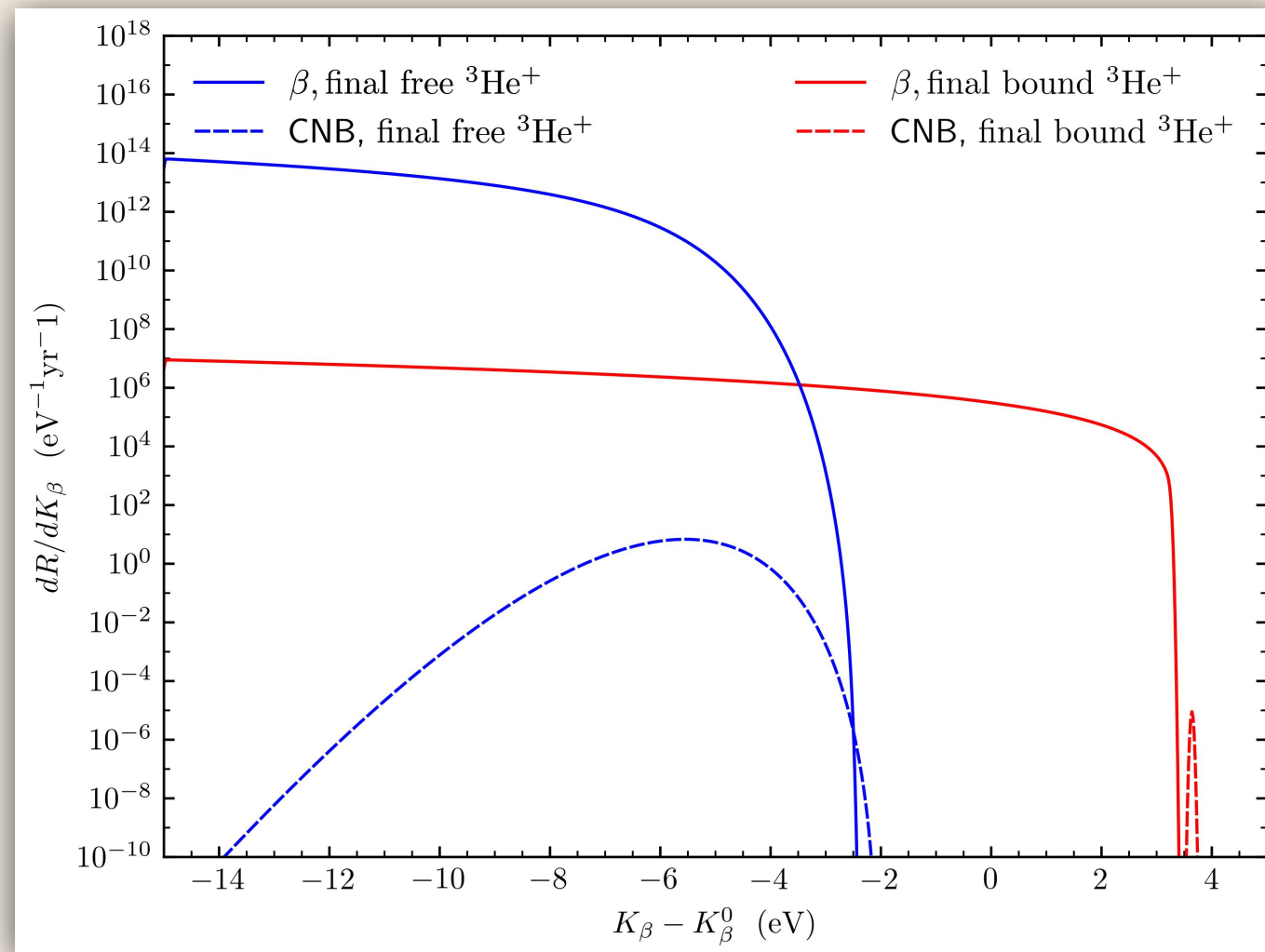


$$d\Gamma_B \propto e^{-\frac{\lambda^2 p_\beta^2}{2}}$$

$\lambda p_\beta \simeq 6$
at endpoint

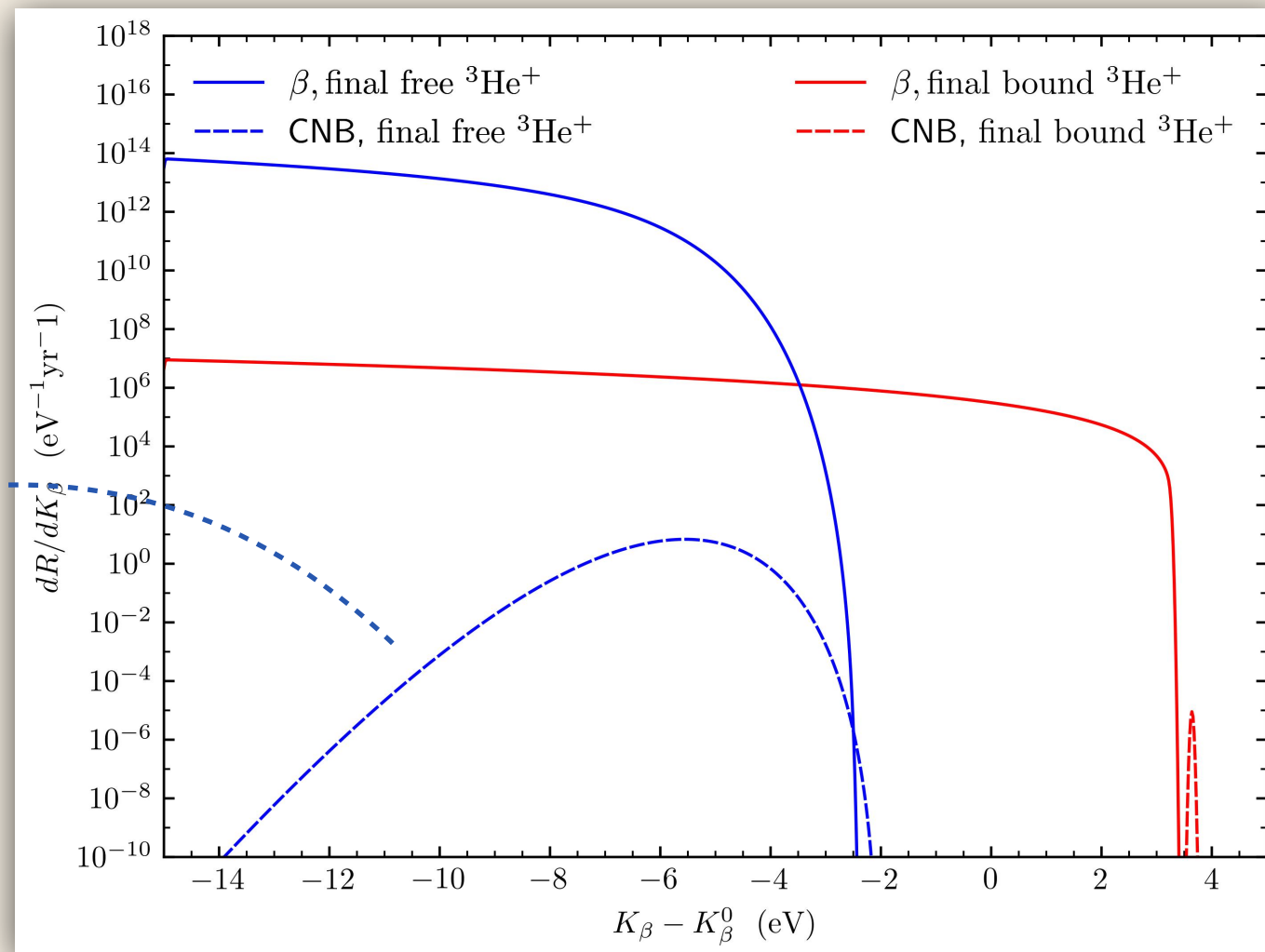
Results from graphene

- How good is graphene to **detect CNB**?



Results from graphene

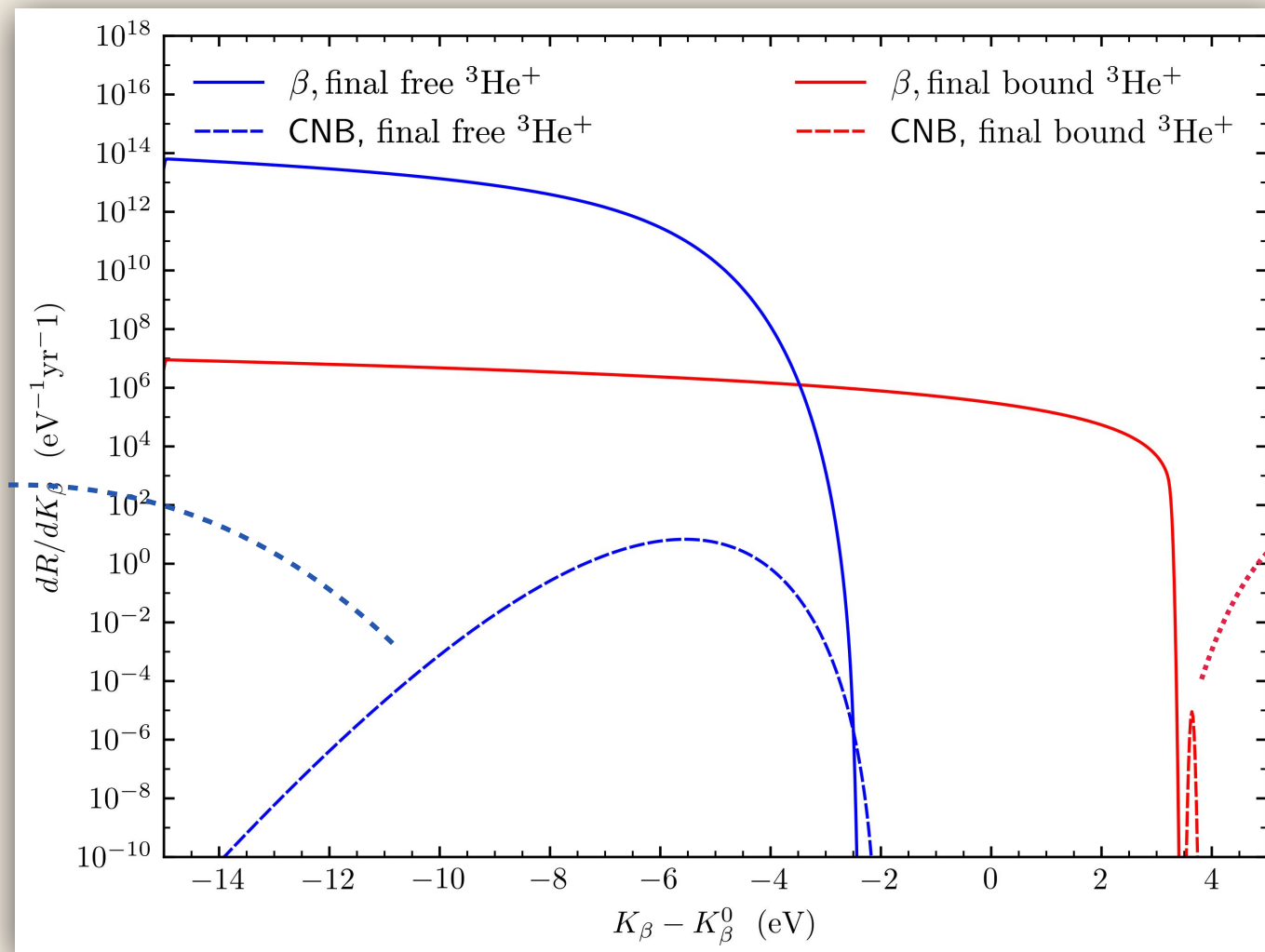
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Bad news:
Obscured CNB peak

Results from graphene

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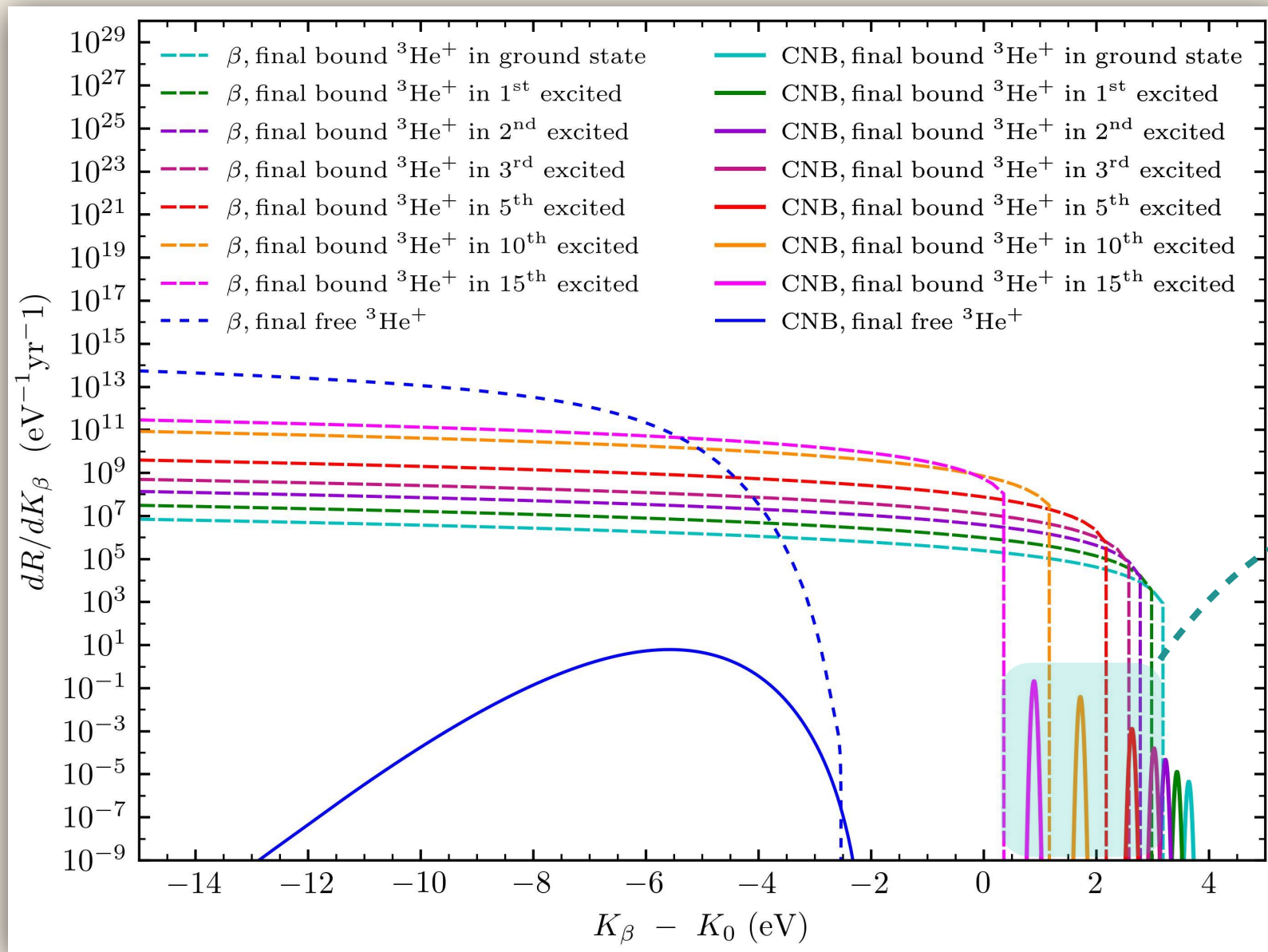


Bad news:
Obscured CNB peak

Bad news:
Suppressed CNB peak

Results from graphene

- What about final **excited bound states**?



Stronger peaks,
but **obscured!**

Need to change substrate

- What would change if we used **another substrate**?



Tritium would be
localized differently

Need to change substrate

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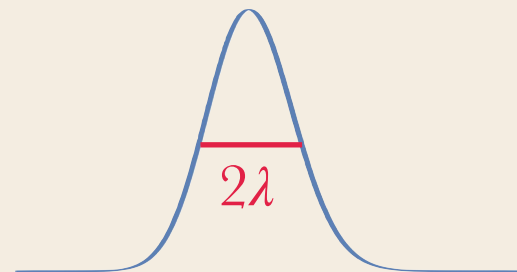


Tritium would be localized differently

- Different substrate



Different value of λ



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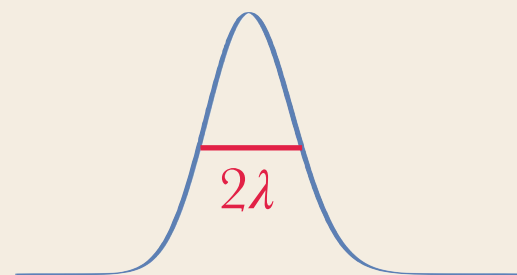


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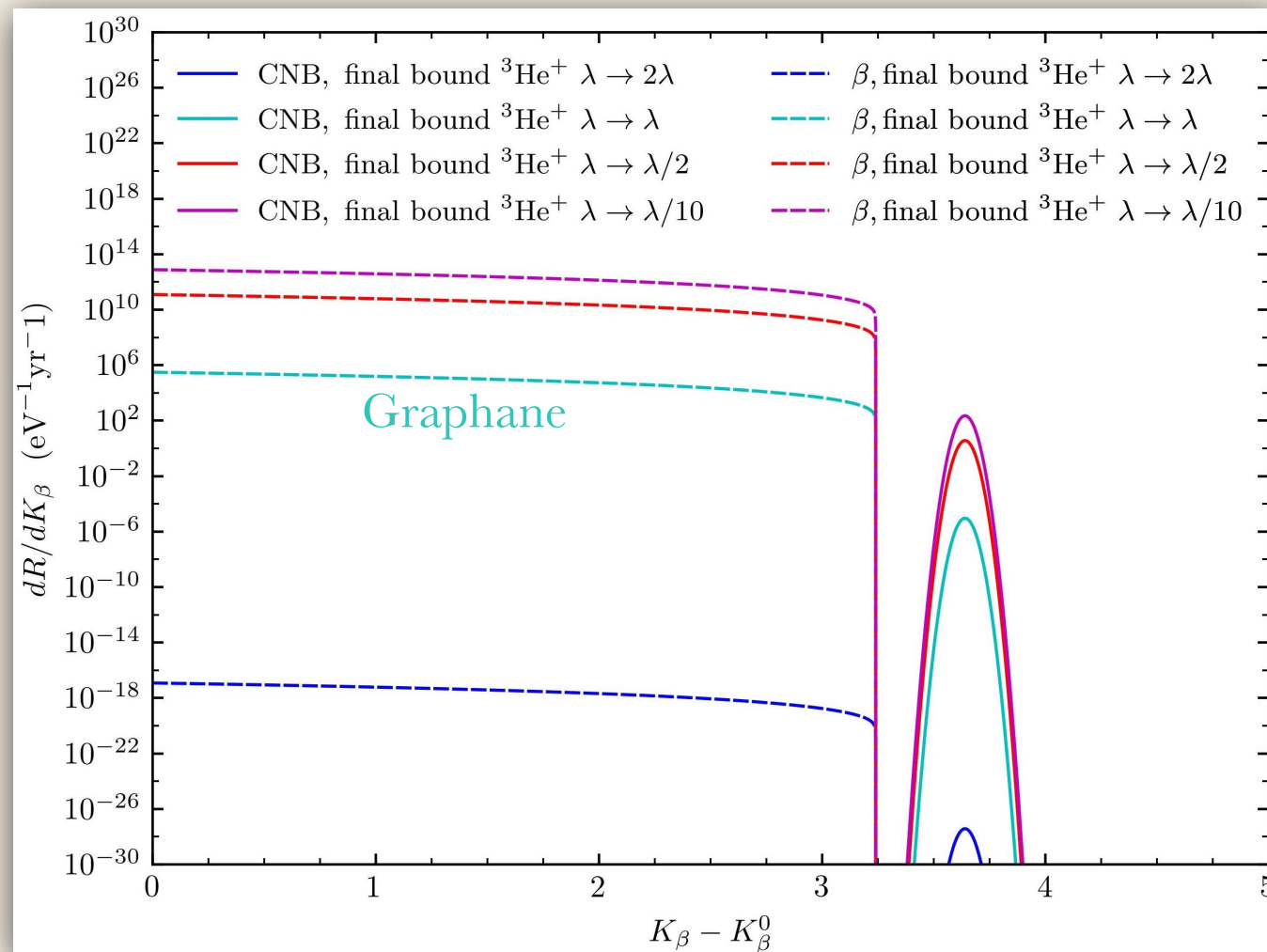


Different value of λ

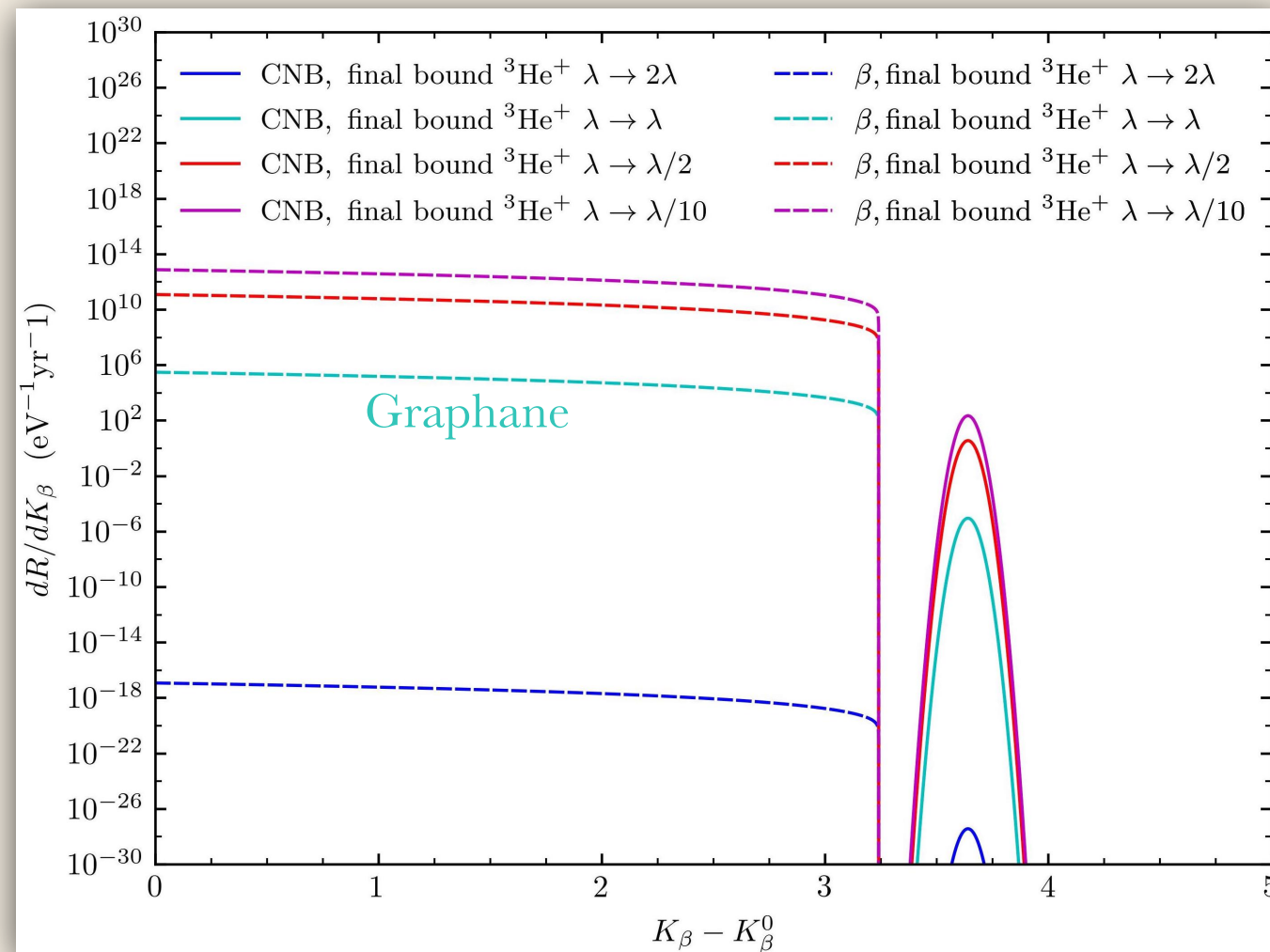


- Let's see how electron spectra change **varying λ**

Bound states varying λ



Bound states varying λ

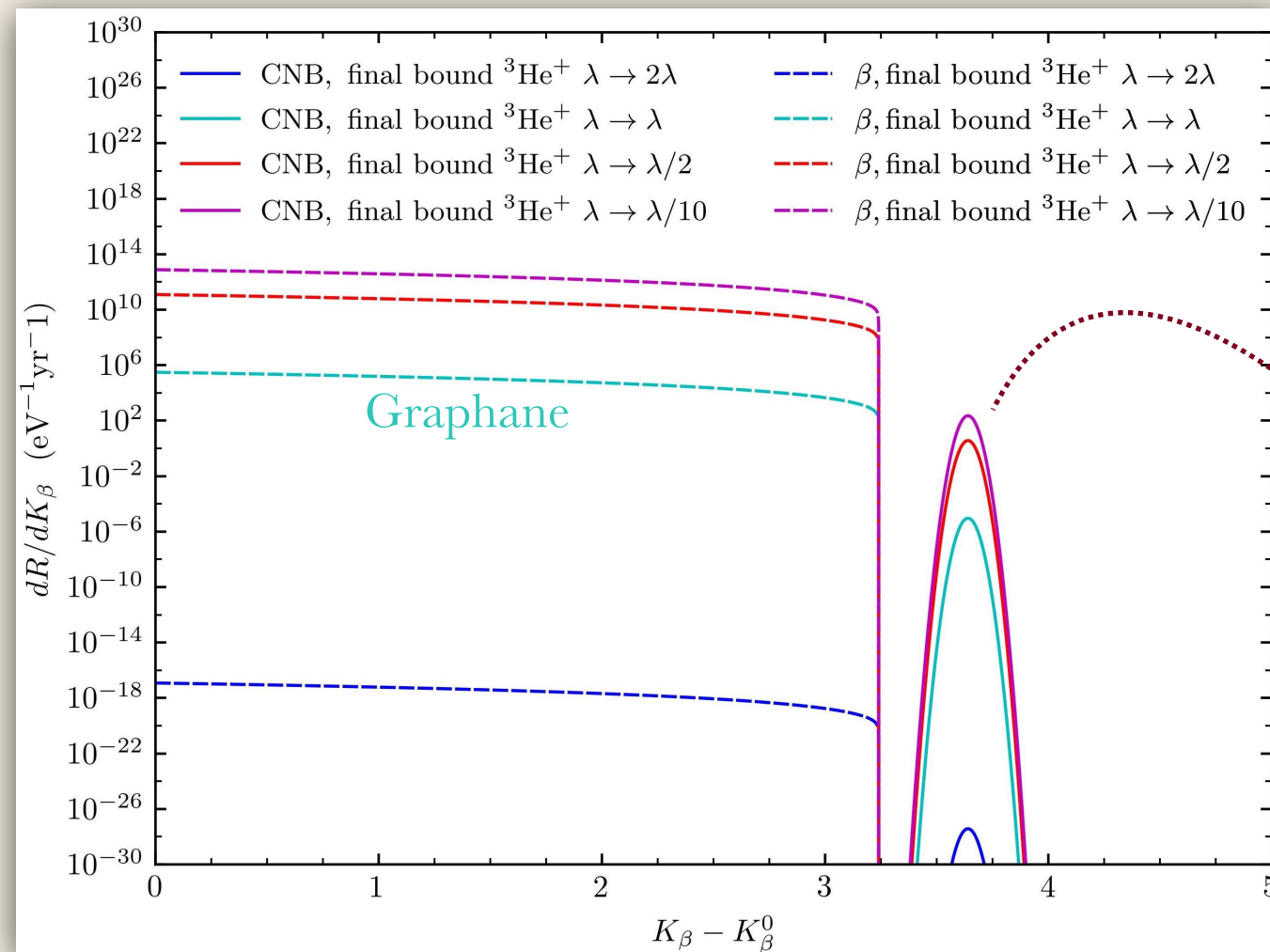


Delocalization brings
suppression



$$d\Gamma_B \propto e^{-\frac{\lambda^2 p_\beta^2}{2}}$$

Bound states varying λ



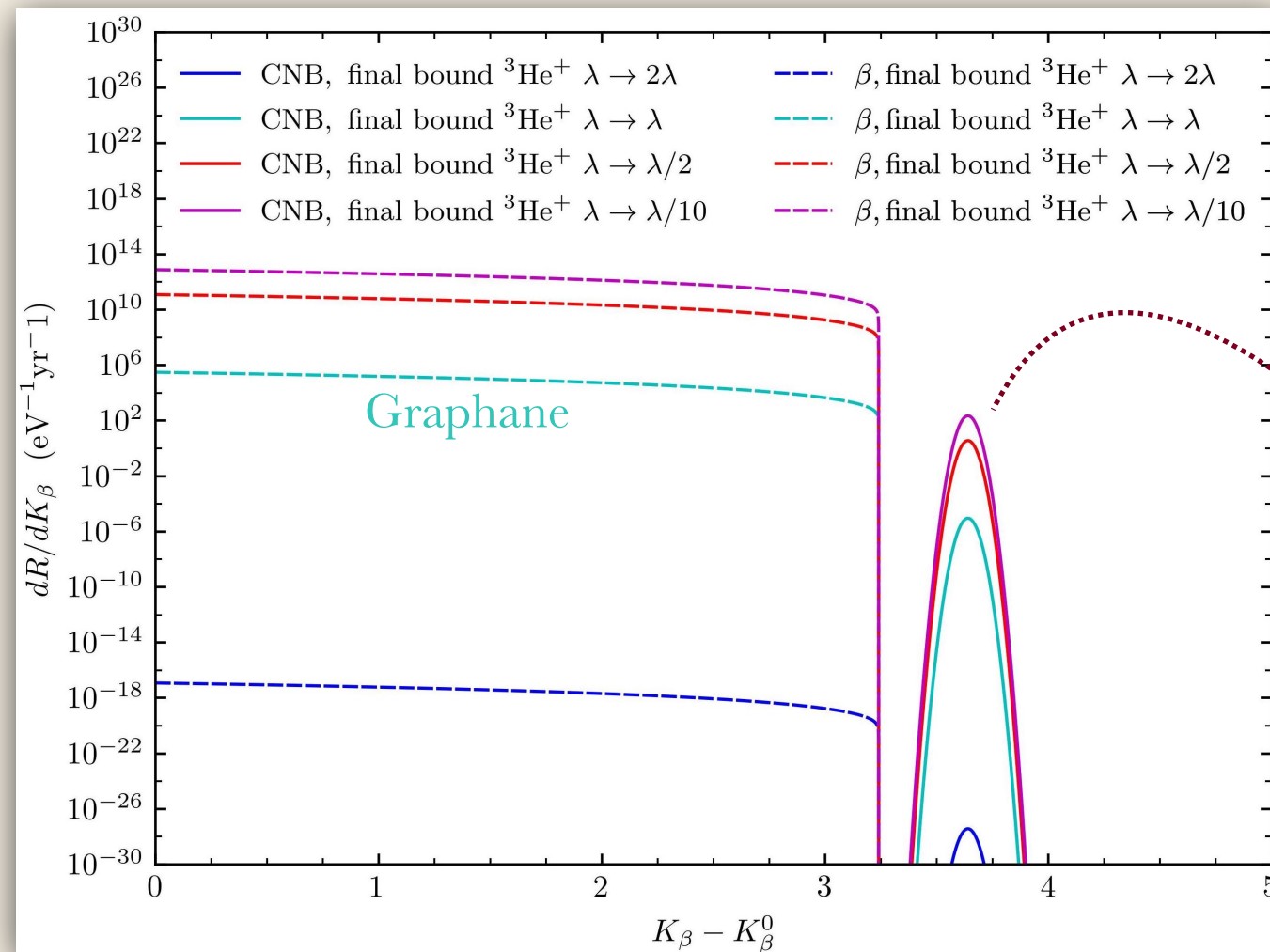
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$\mathcal{O}(100)$ CNB events
if $\lambda \rightarrow \lambda/10$

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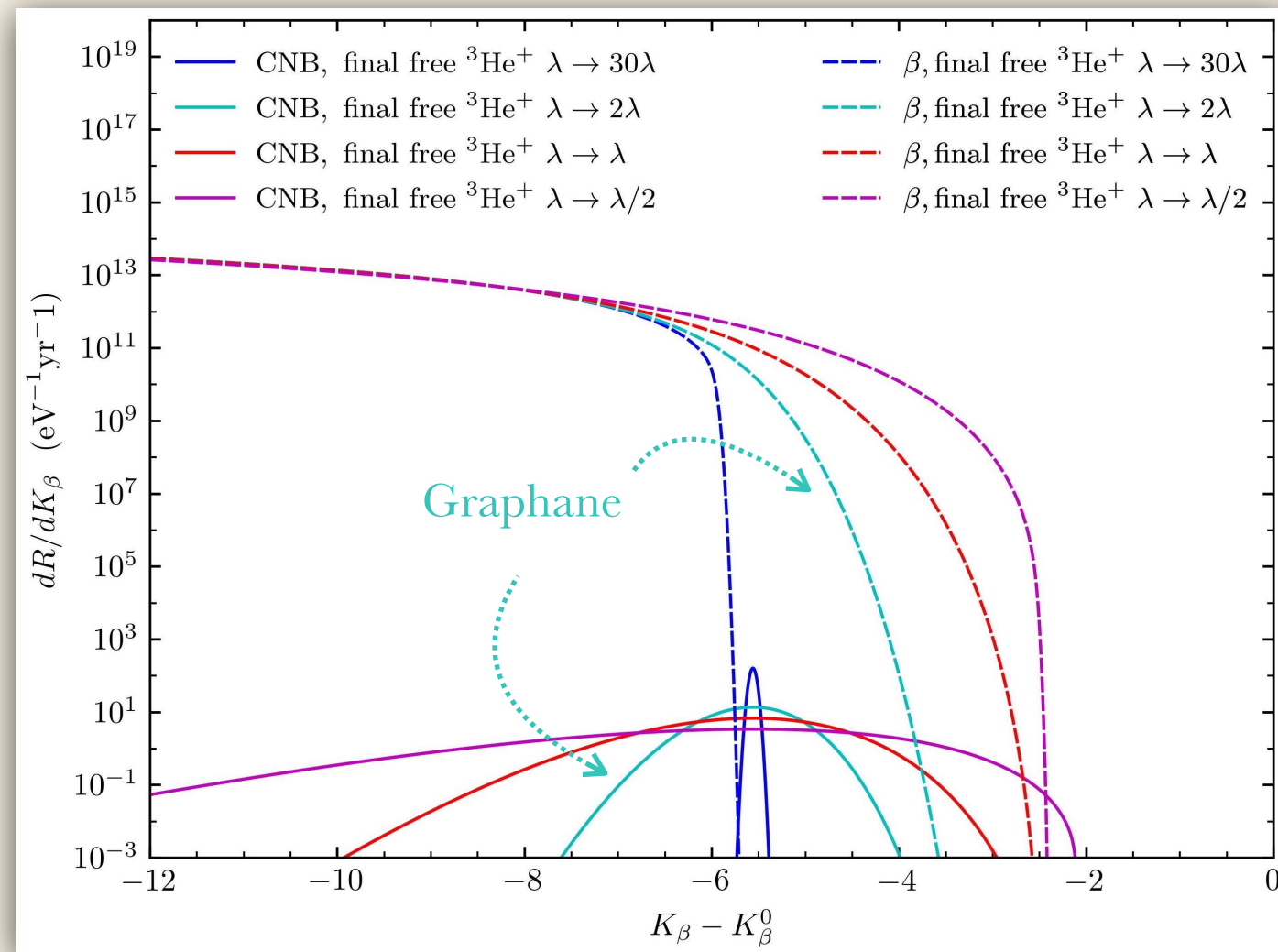
Strategy n.1: decrease λ



Very difficult in
condensed matter physics

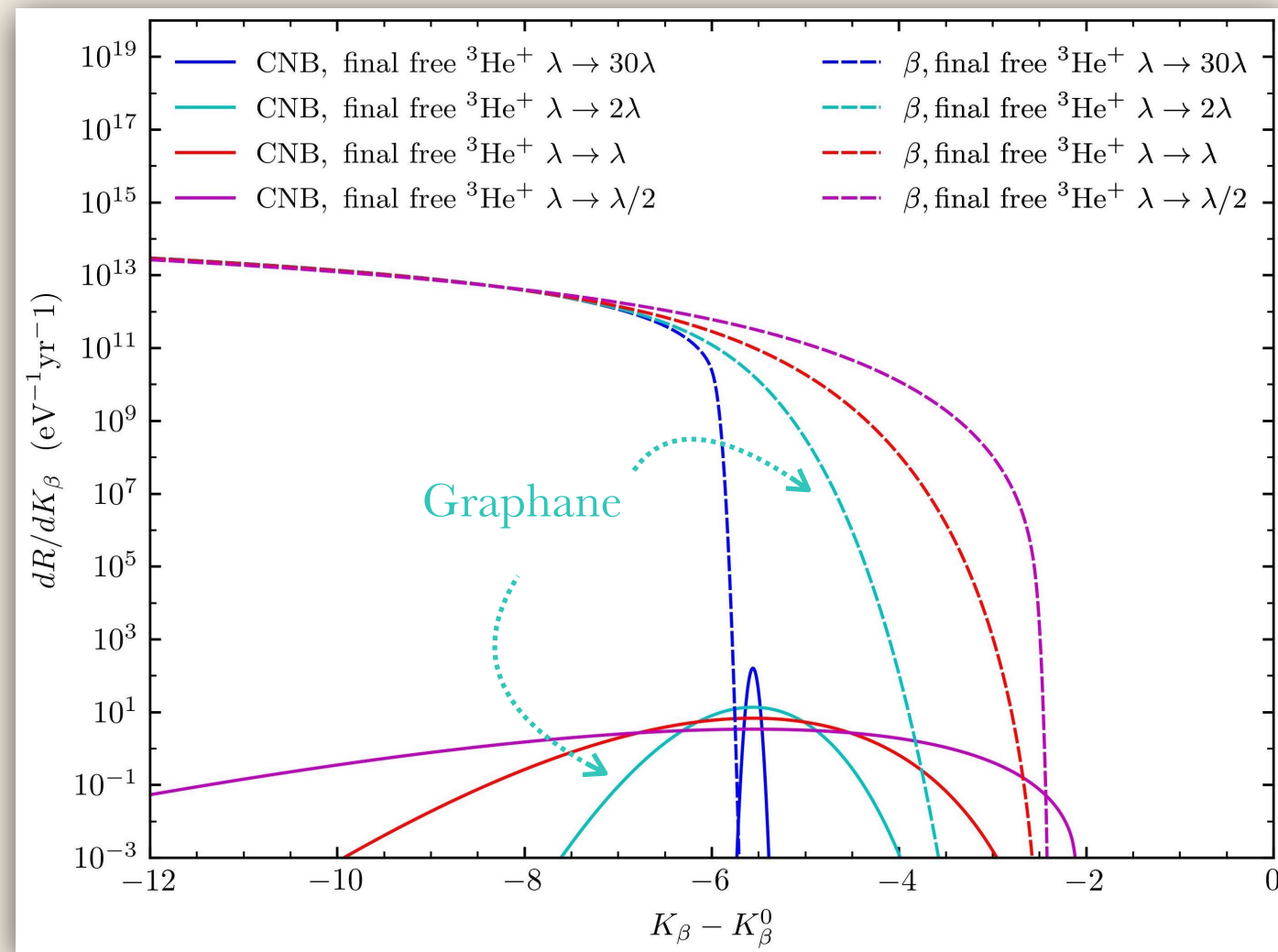
Free states varying λ

- Distorsion on the rates as λ is decreased



Free states varying λ

- Distorsion on the rates as λ is **decreased**

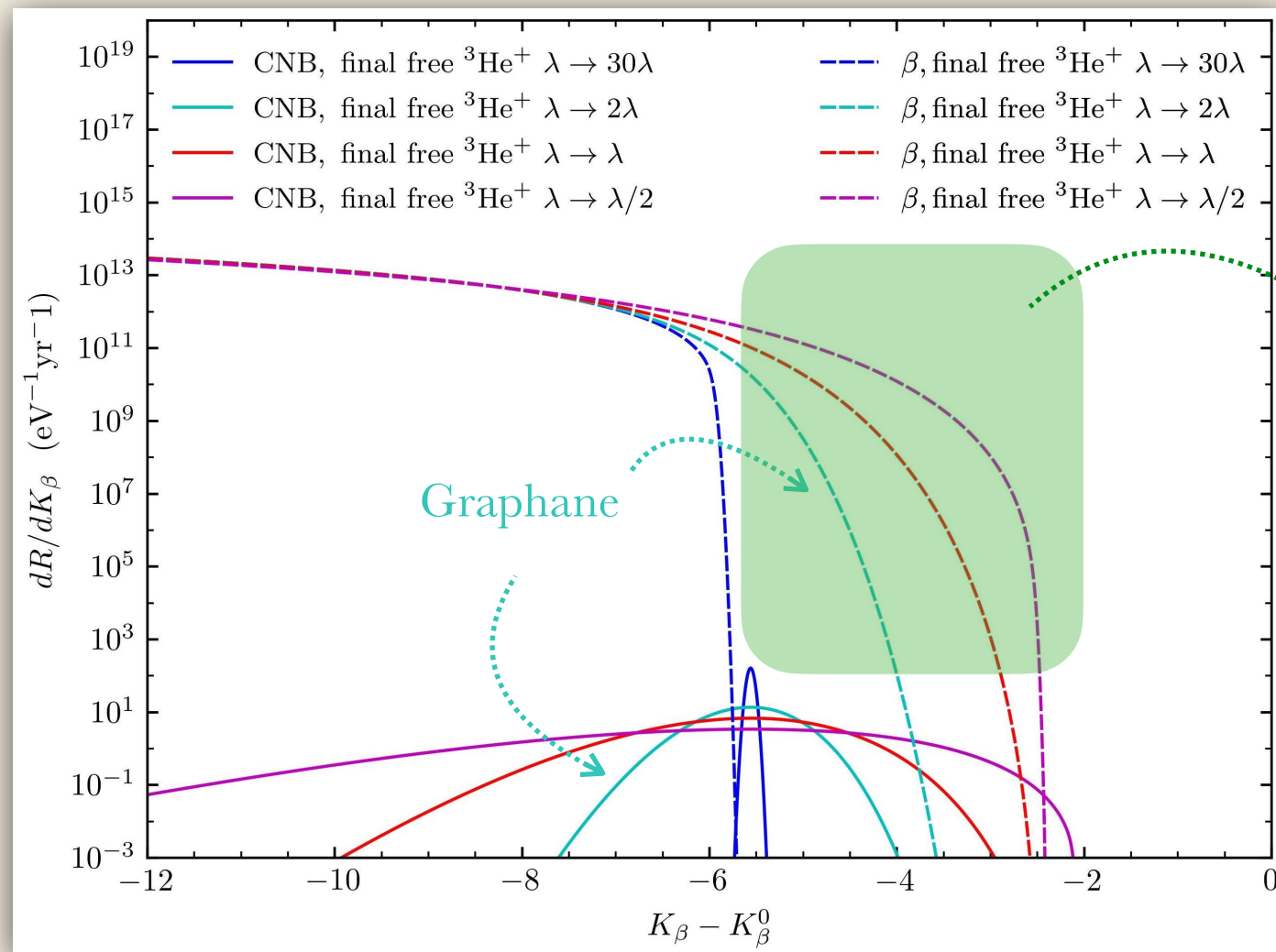


Heisenberg
uncertainty principle

$$\Delta K_\beta \simeq \frac{p_\beta}{m_{^3\text{He}^+} \Delta x_T}$$

Free states varying λ

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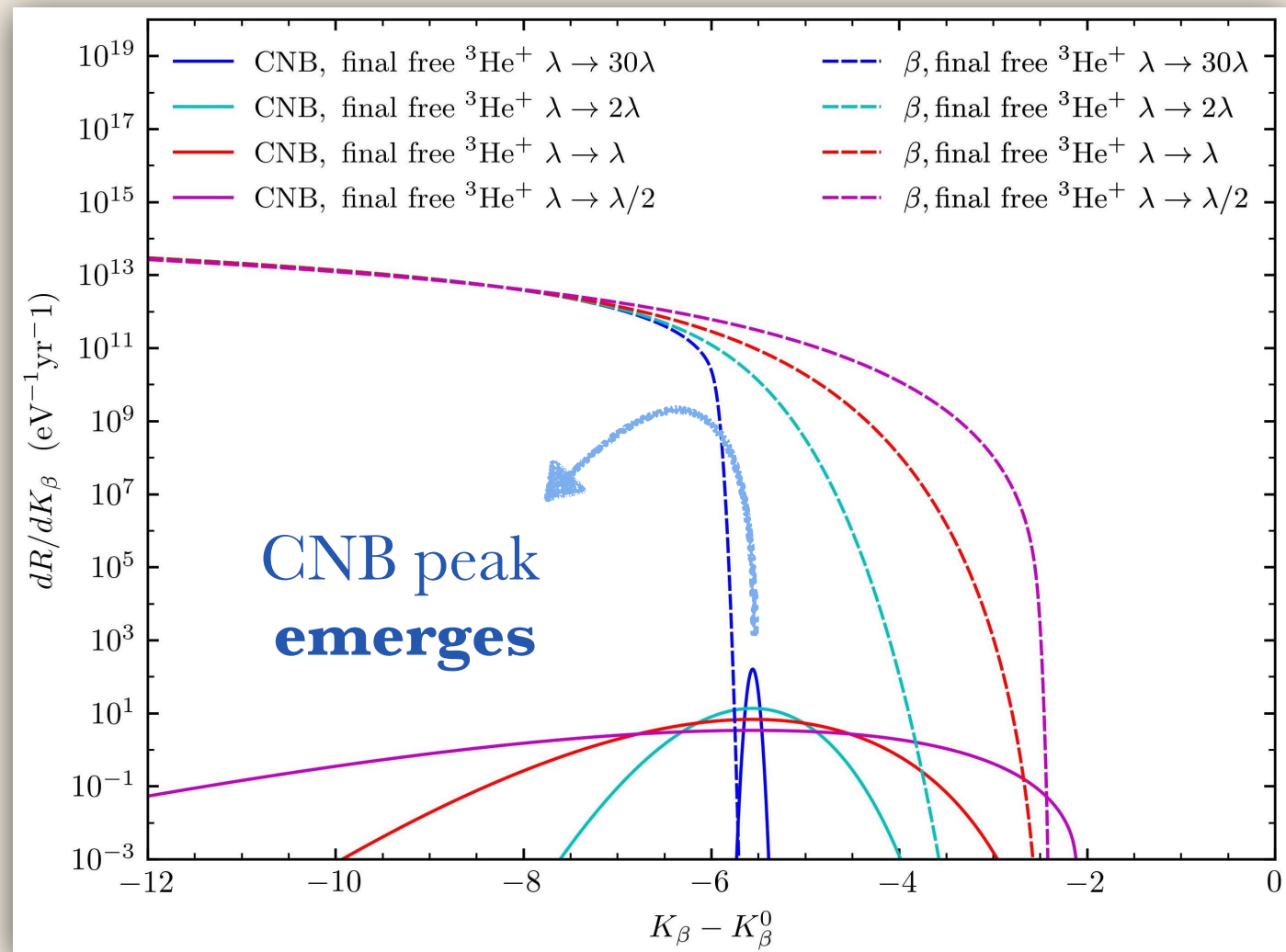
Beta decays obscure
CNB signals beneath

Free states varying λ

- What would happen if we **increased** λ ?



Quantum uncertainty decreases

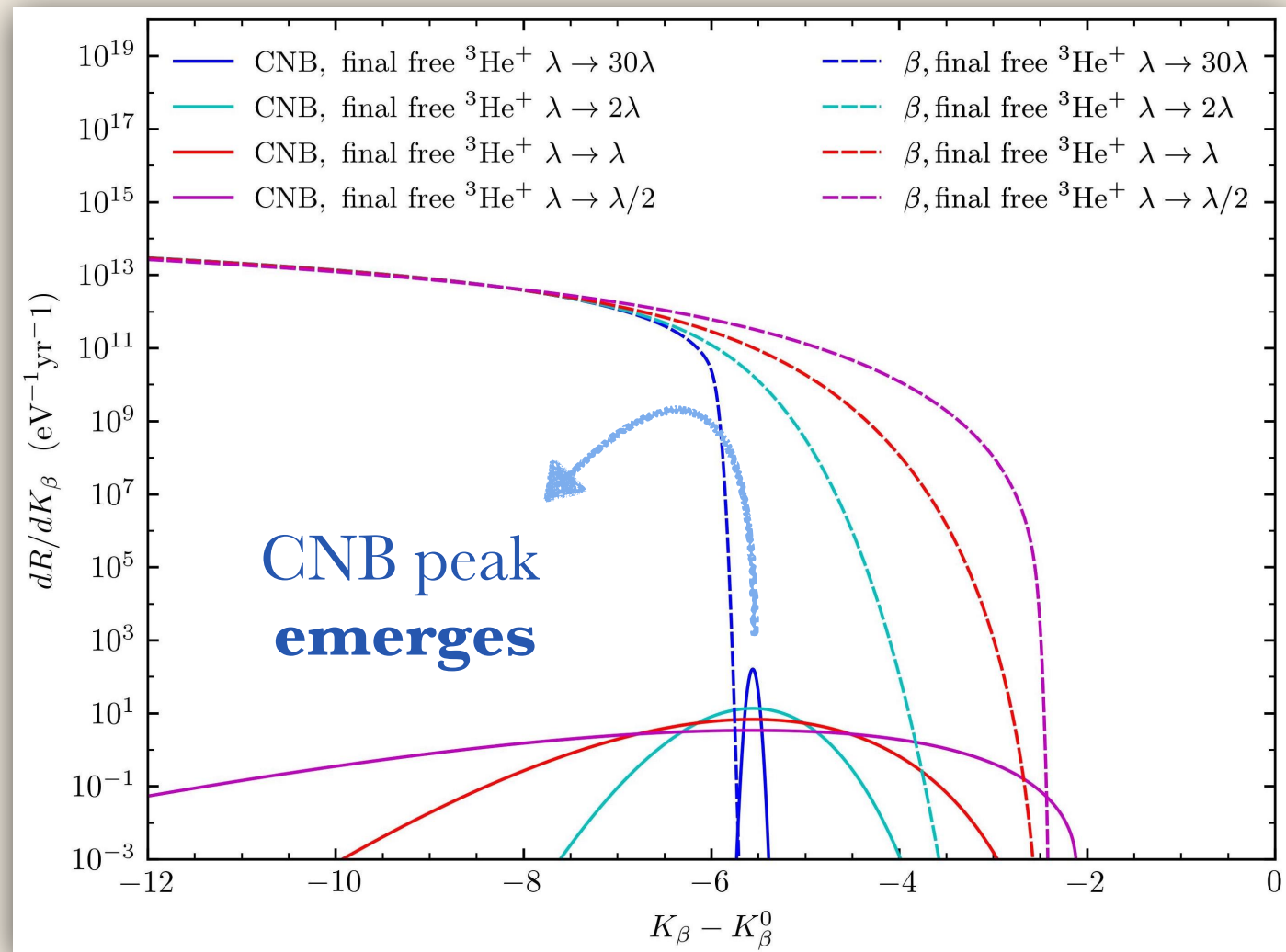


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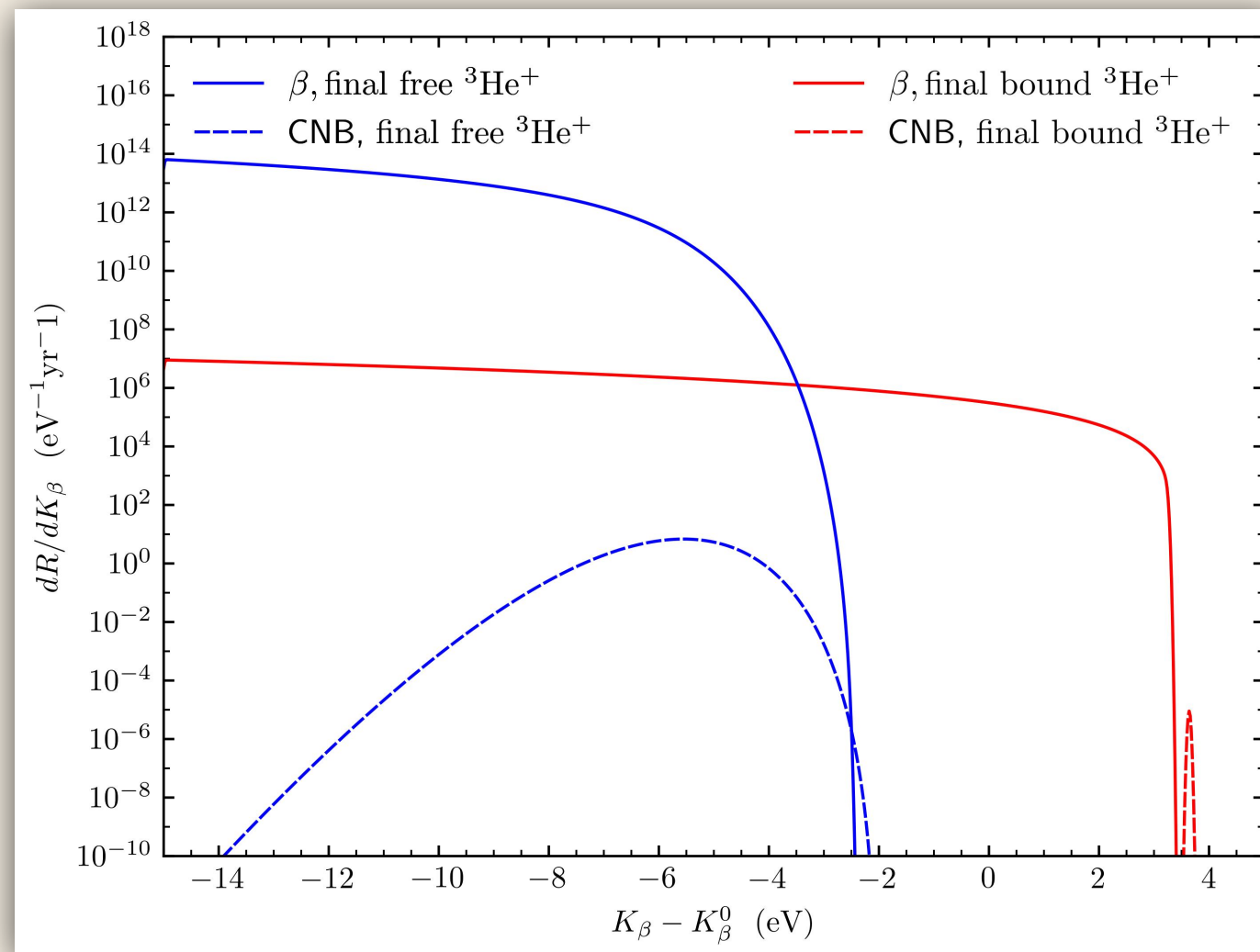
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Strategy n.2: increase λ

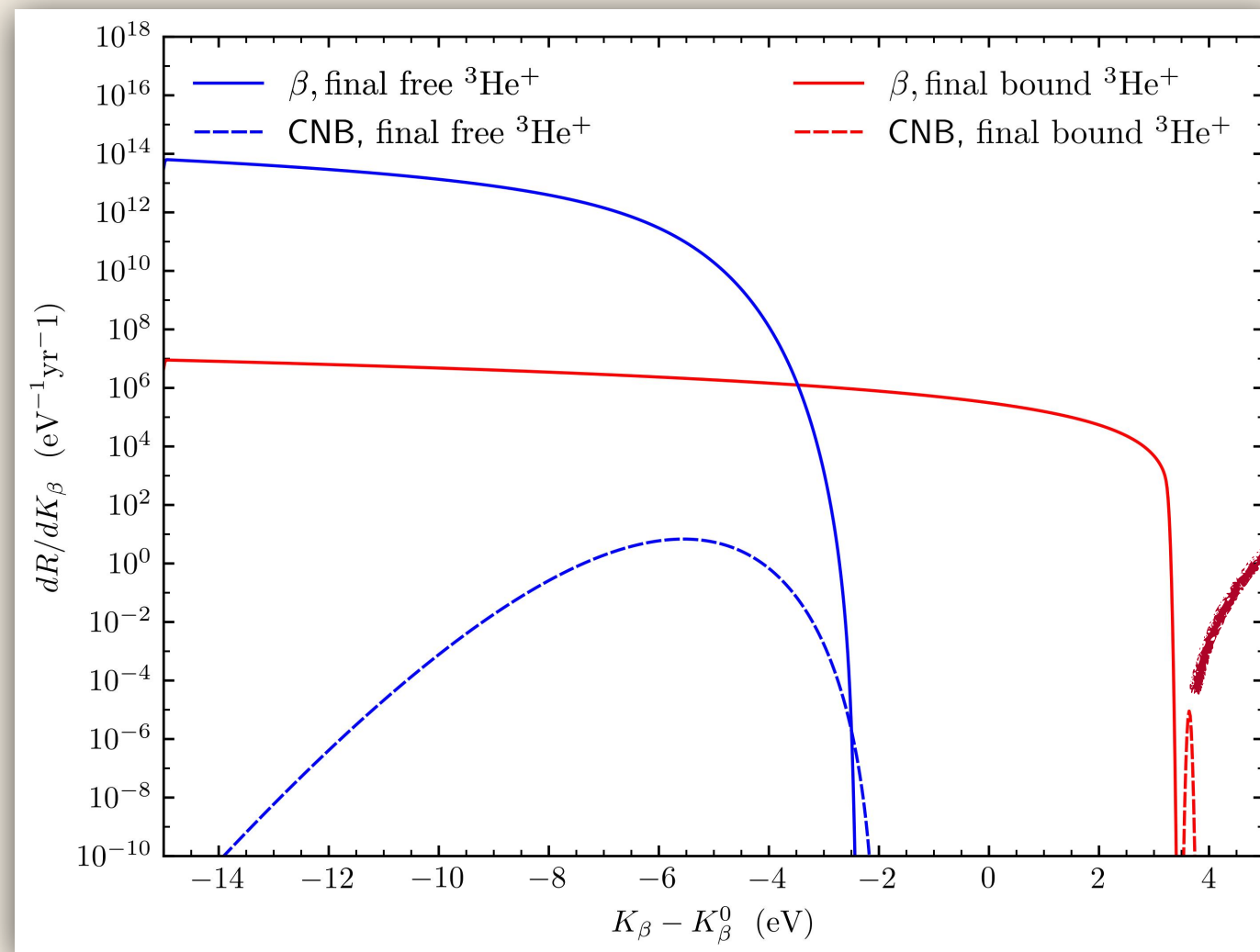
Moral of the story

- How to make CNB detection **possible**?



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Strategy n. 1:
Localize tritium to
increase CNB peak
intensity

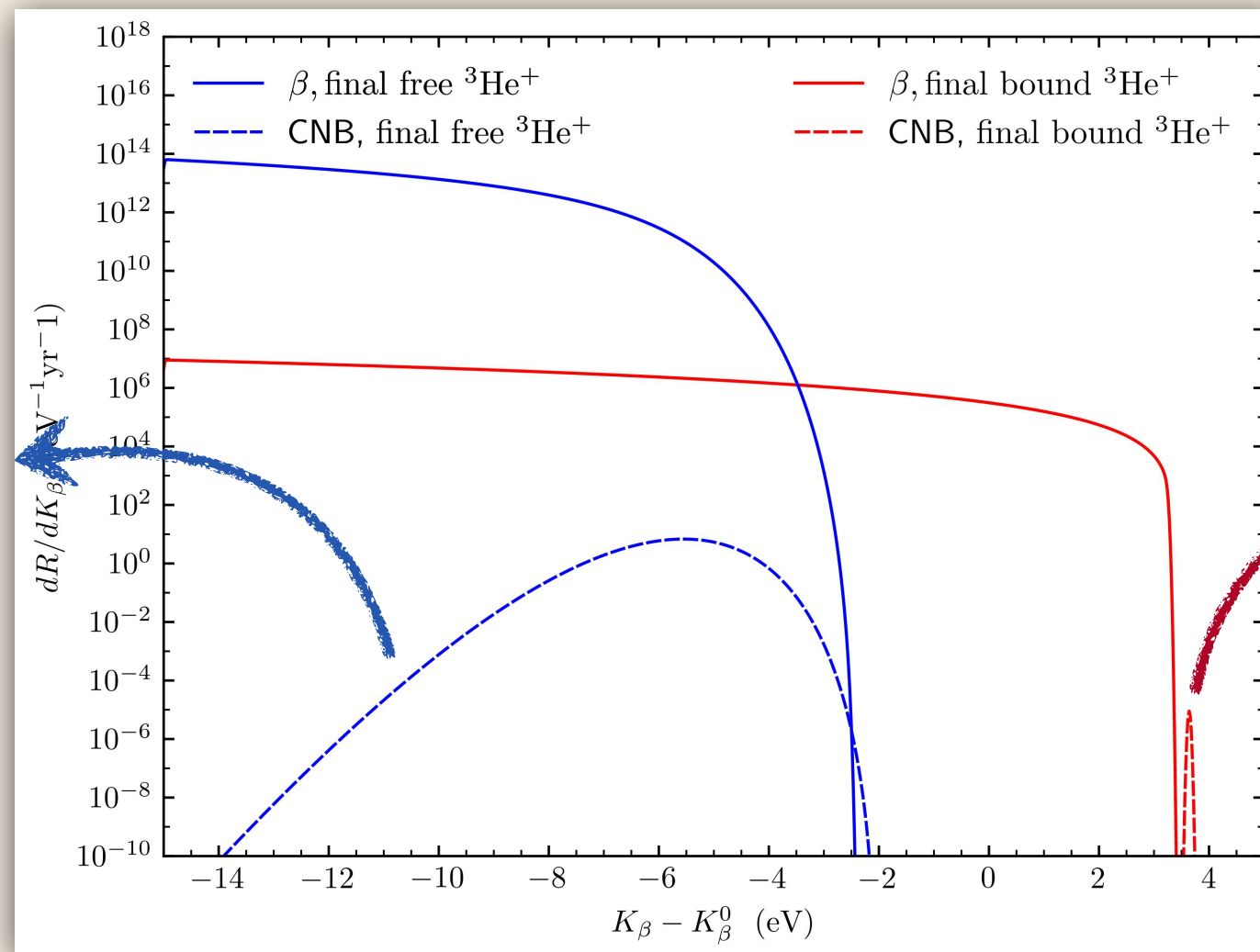
Moral of the story

- How to make CNB detection **possible**?

Strategy n. 2:

Delocalize tritium in order to:

1. Make CNB peak emerge from beta decay events



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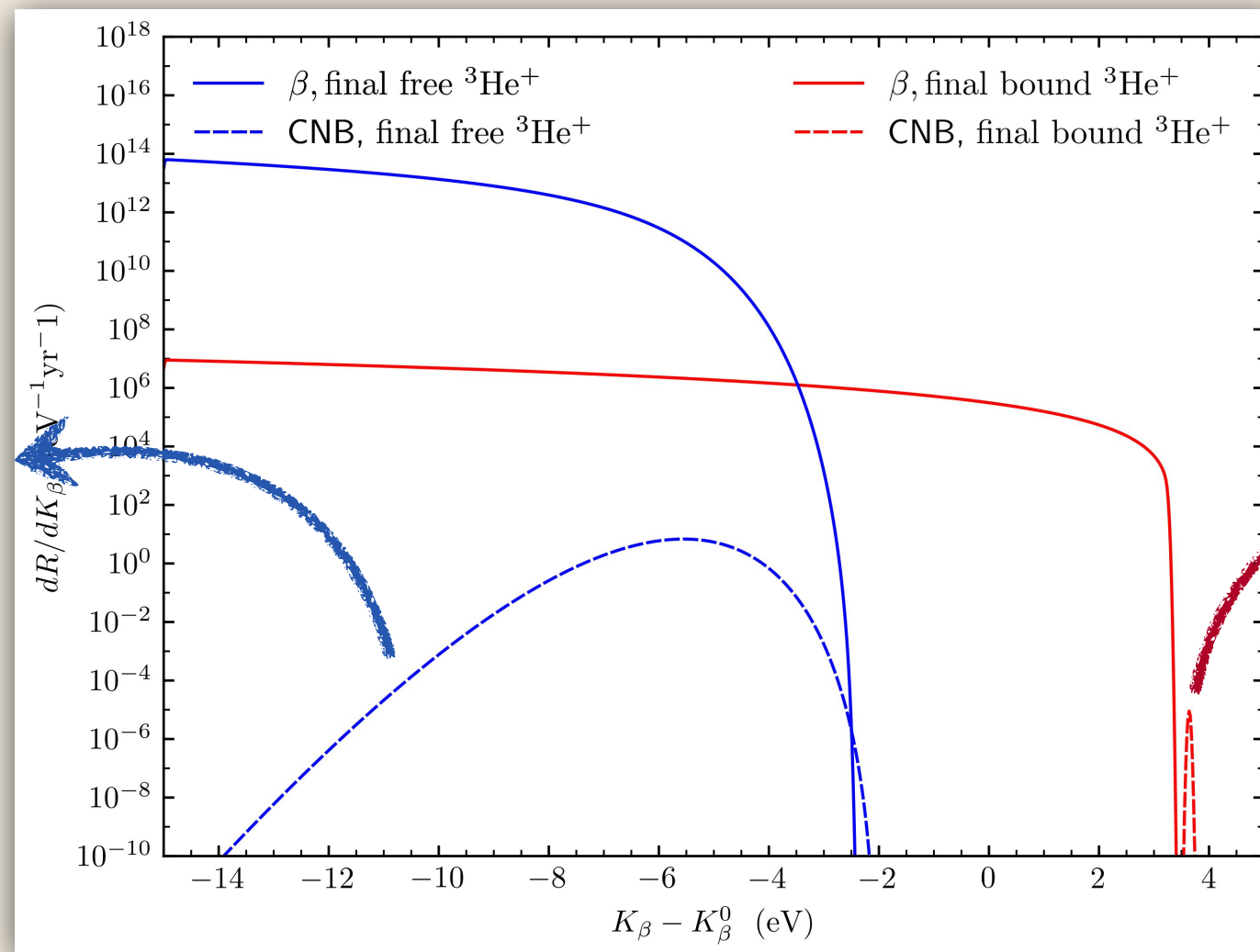
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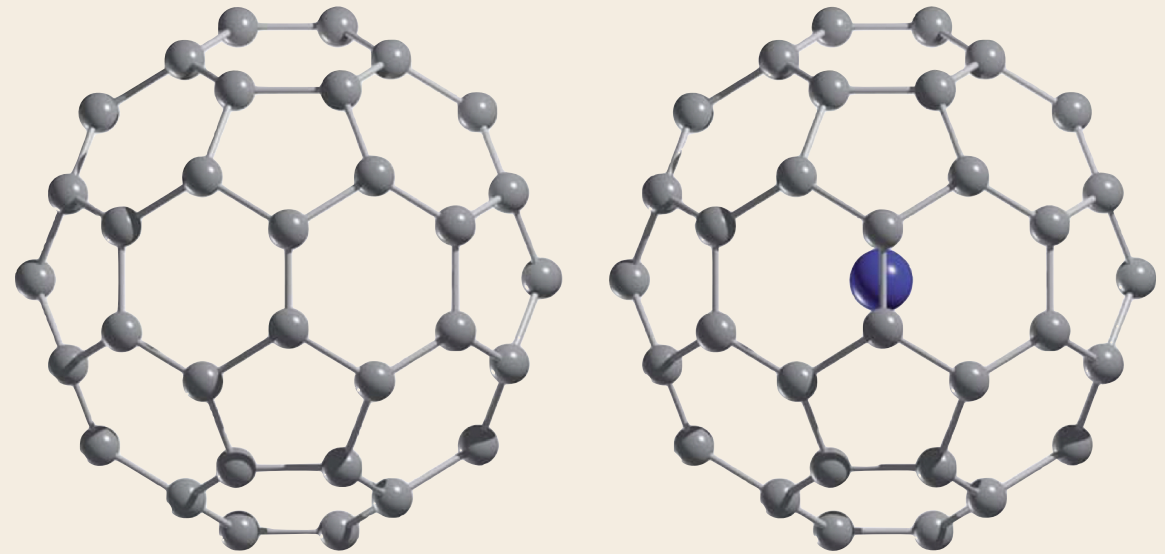
1. Make CNB peak emerge from beta decay events
2. Make bound events hugely suppressed



Strategy n. 1:
Localize tritium to increase CNB peak intensity

Fullerenes

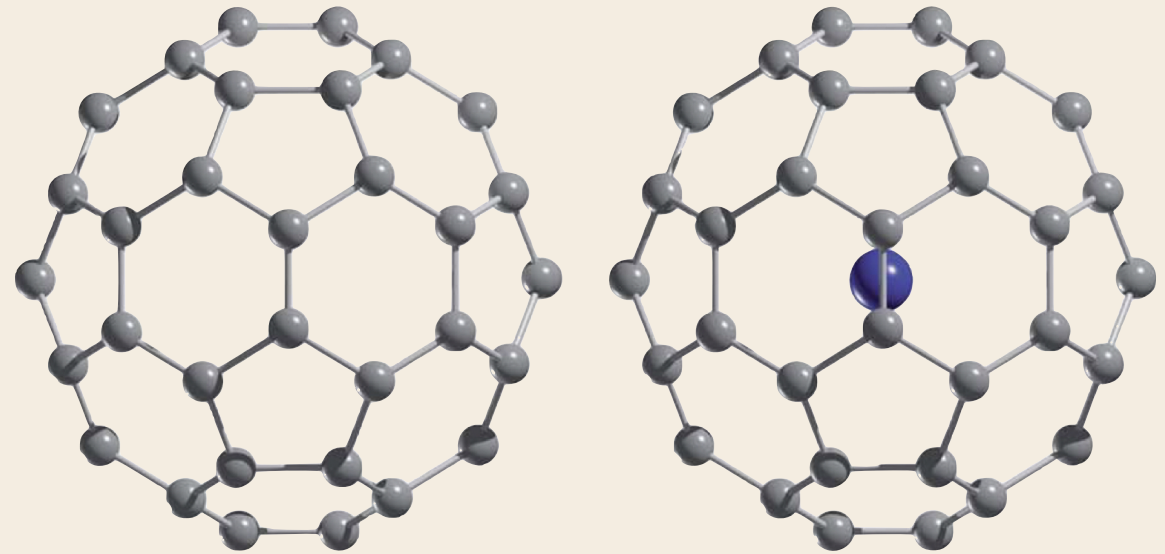
- We studied the C_{60} molecule



[Jalife et al., Chem. Sci., 2020, 11, 6642-6652]

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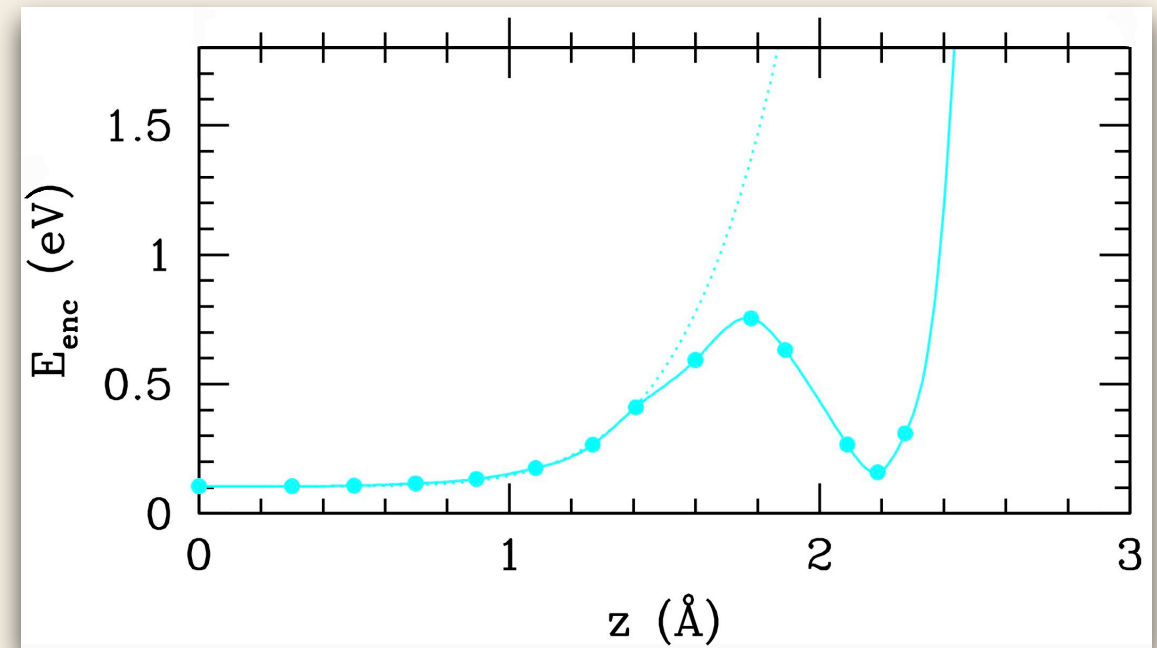
[Jalife et al., Chem. Sci., 2020, 11, 6642-6652]

- **Assumptions:**

1) Spherical symmetry

$$V(r) = a_6 r^6 + a_8 r^8$$

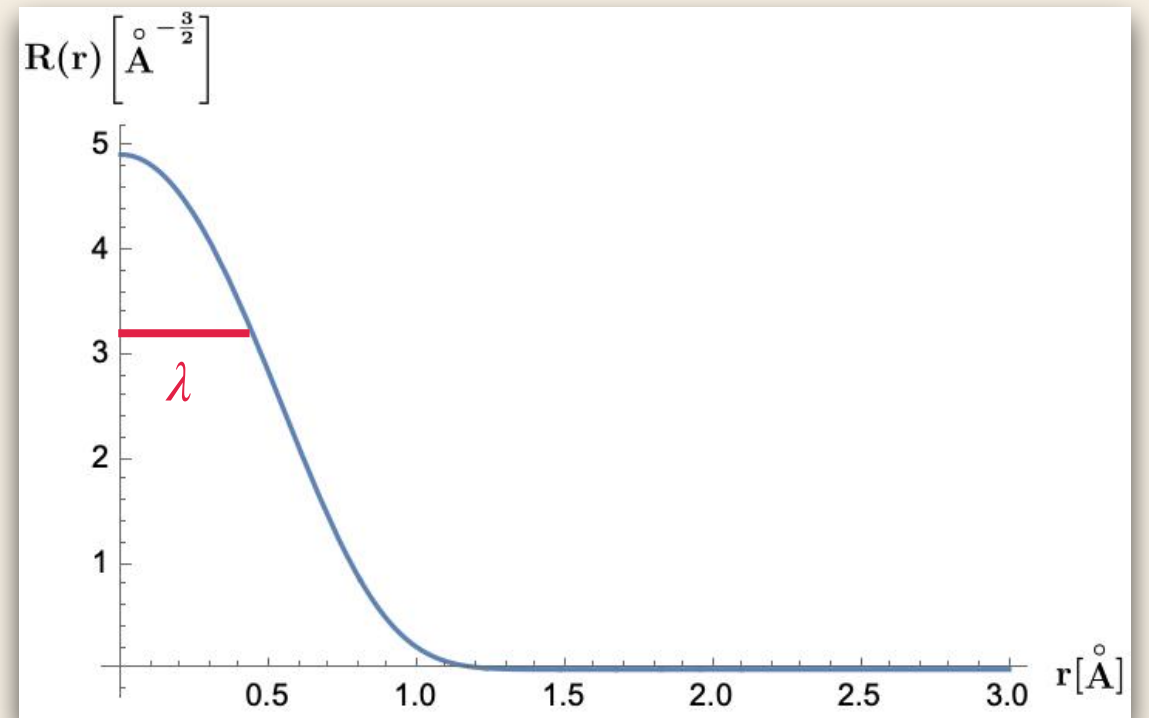
2) Binding energy of 1 eV



[Tozzini, Menichetti - Private communication]

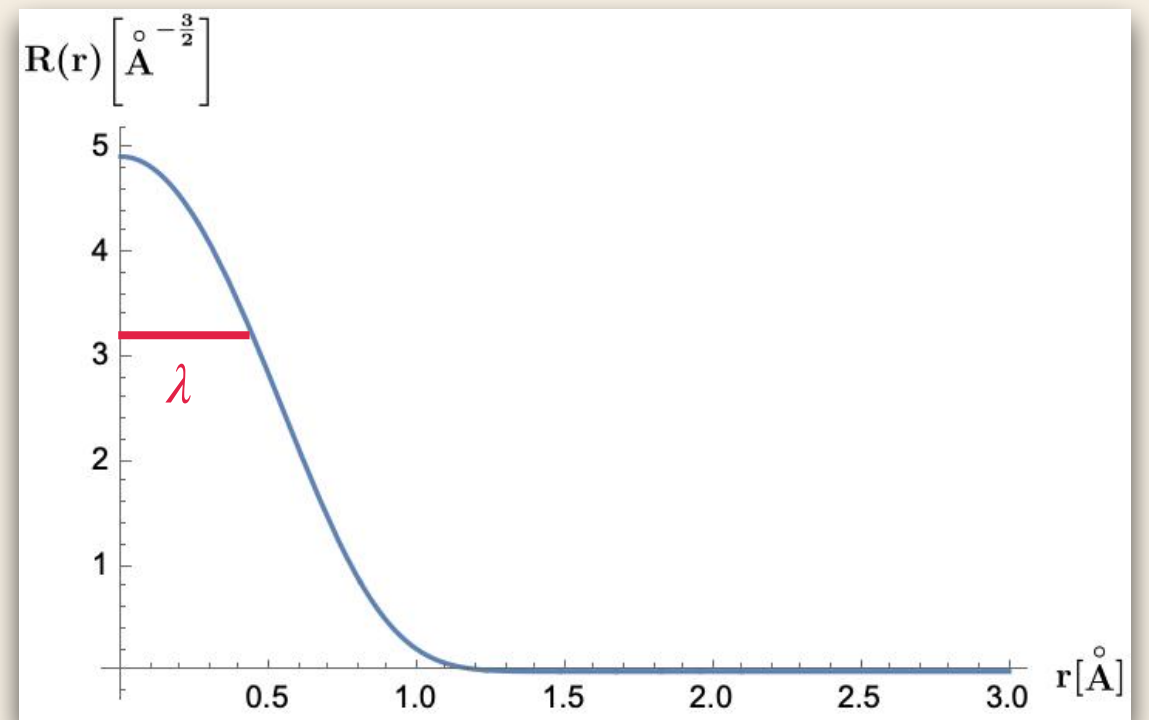
Effects of C_{60}

- **T** is more **delocalized**: $\lambda \simeq 0.44 \text{ \AA}$
↑
(with graphane $\lambda \simeq 0.08 \text{ \AA}$)



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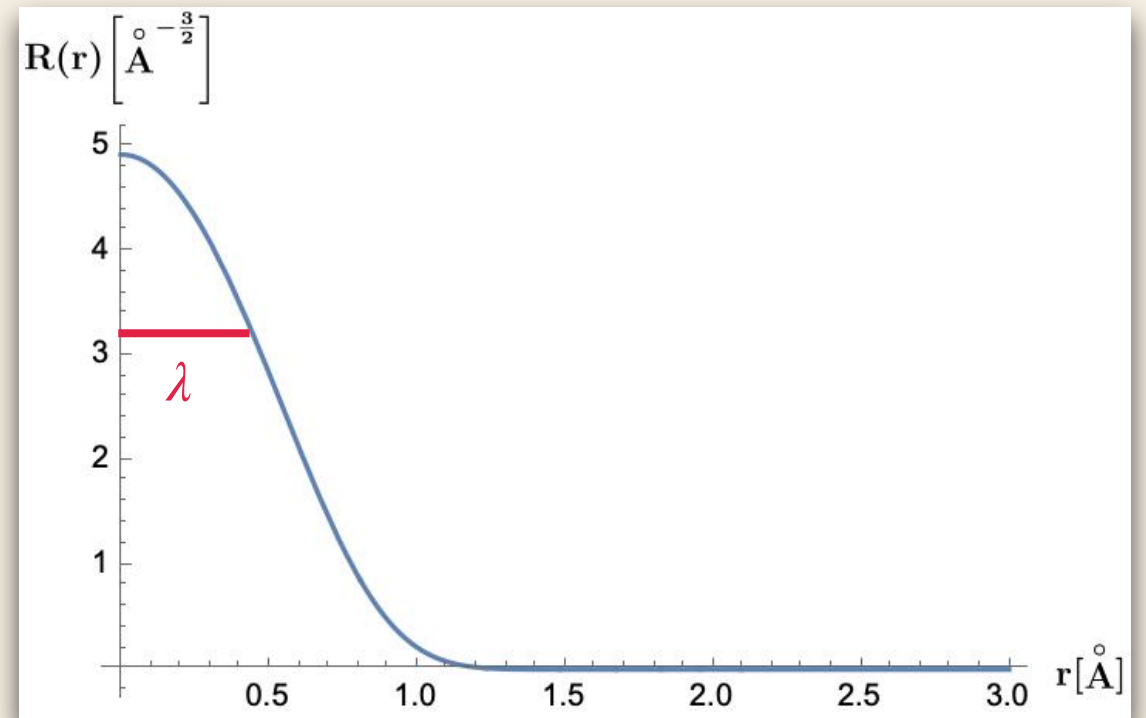
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- Final **bound** ${}^3\text{He}^+$: events are even more **suppressed**: $\lambda p_\beta \simeq 31$

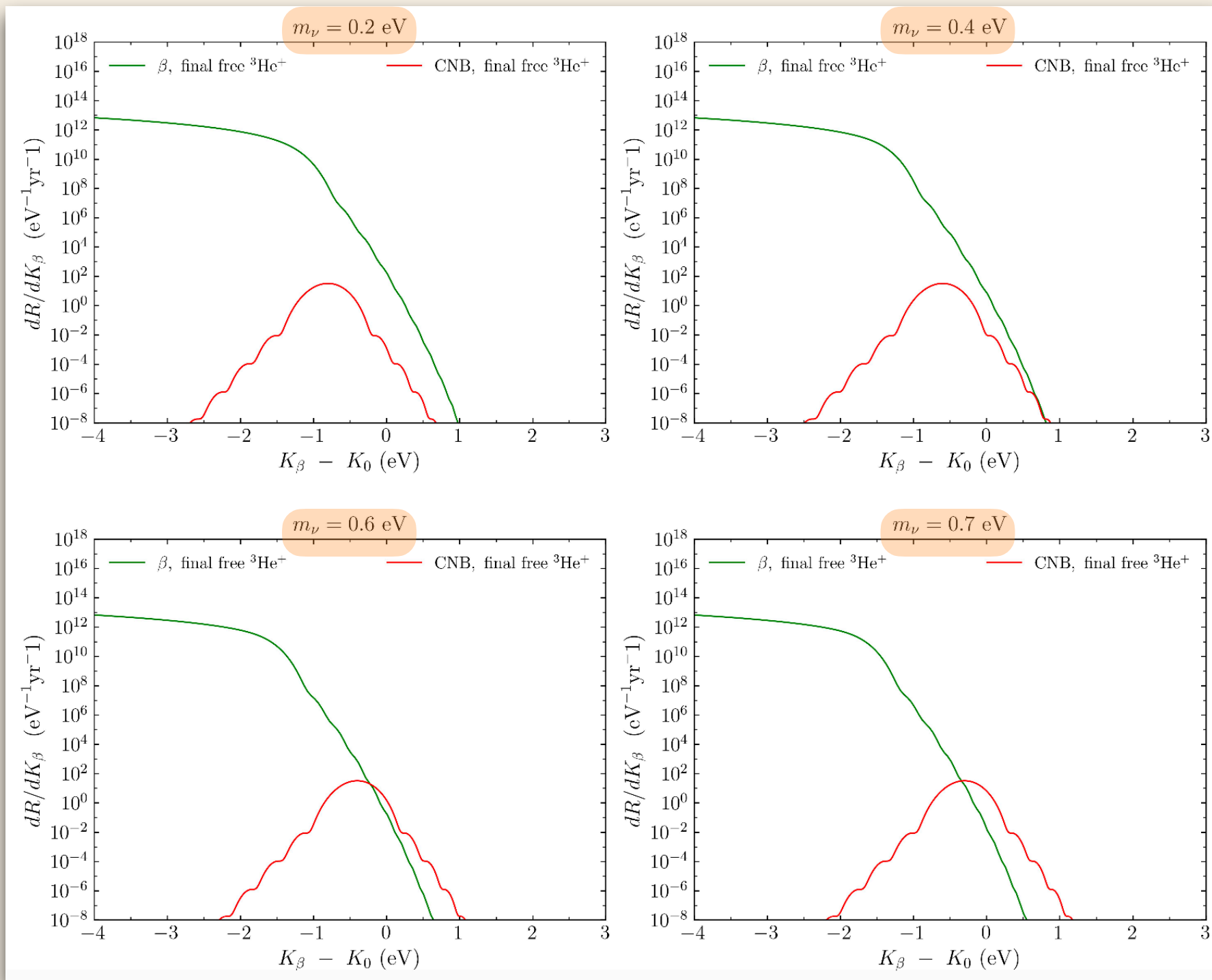
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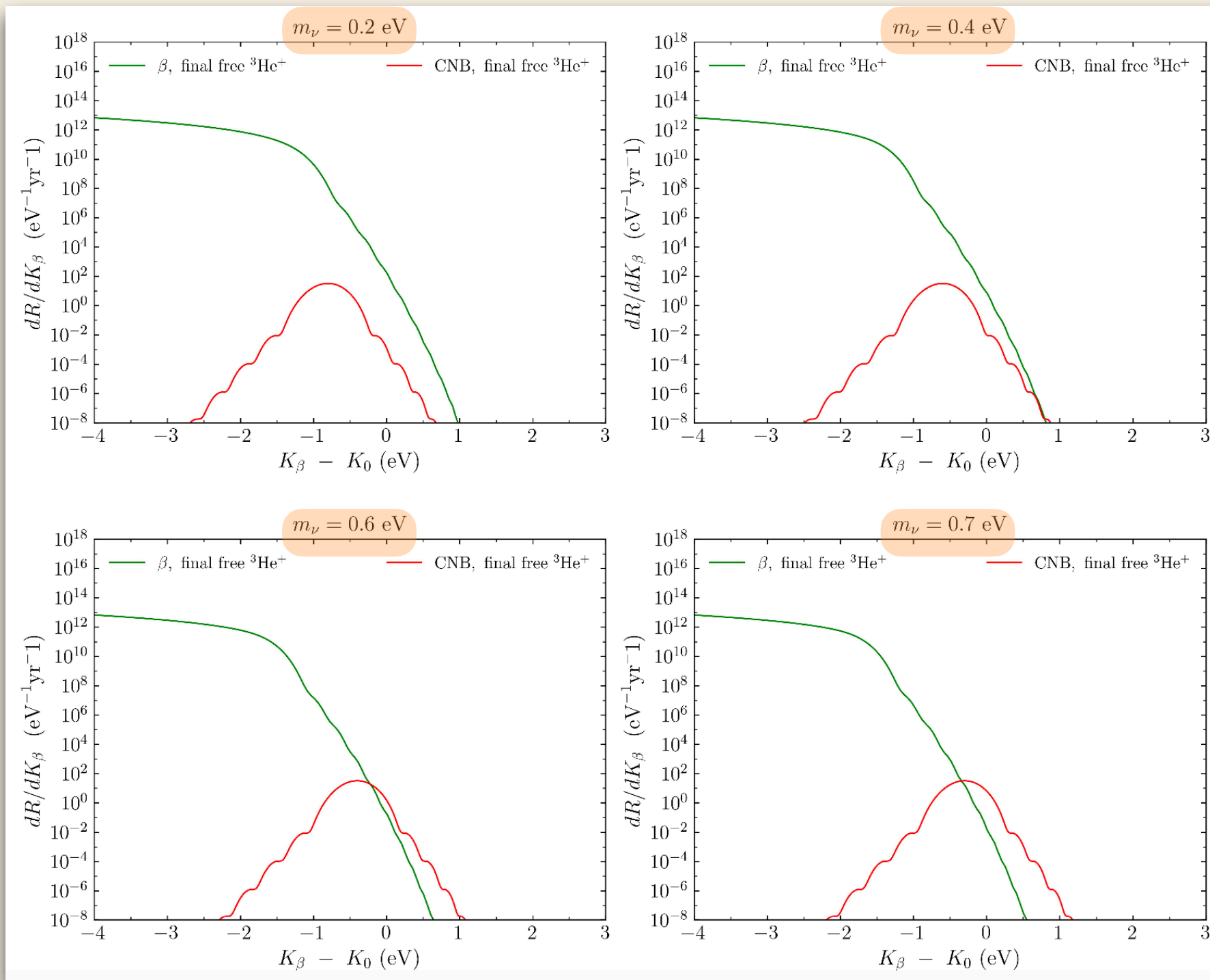


- Final **bound** ${}^3\text{He}^+$: events are even more **suppressed**: $\lambda p_\beta \simeq 31$
- Final **free** ${}^3\text{He}^+$: does the CNB peak emerge from background of beta decay events?

Results from C_{60}

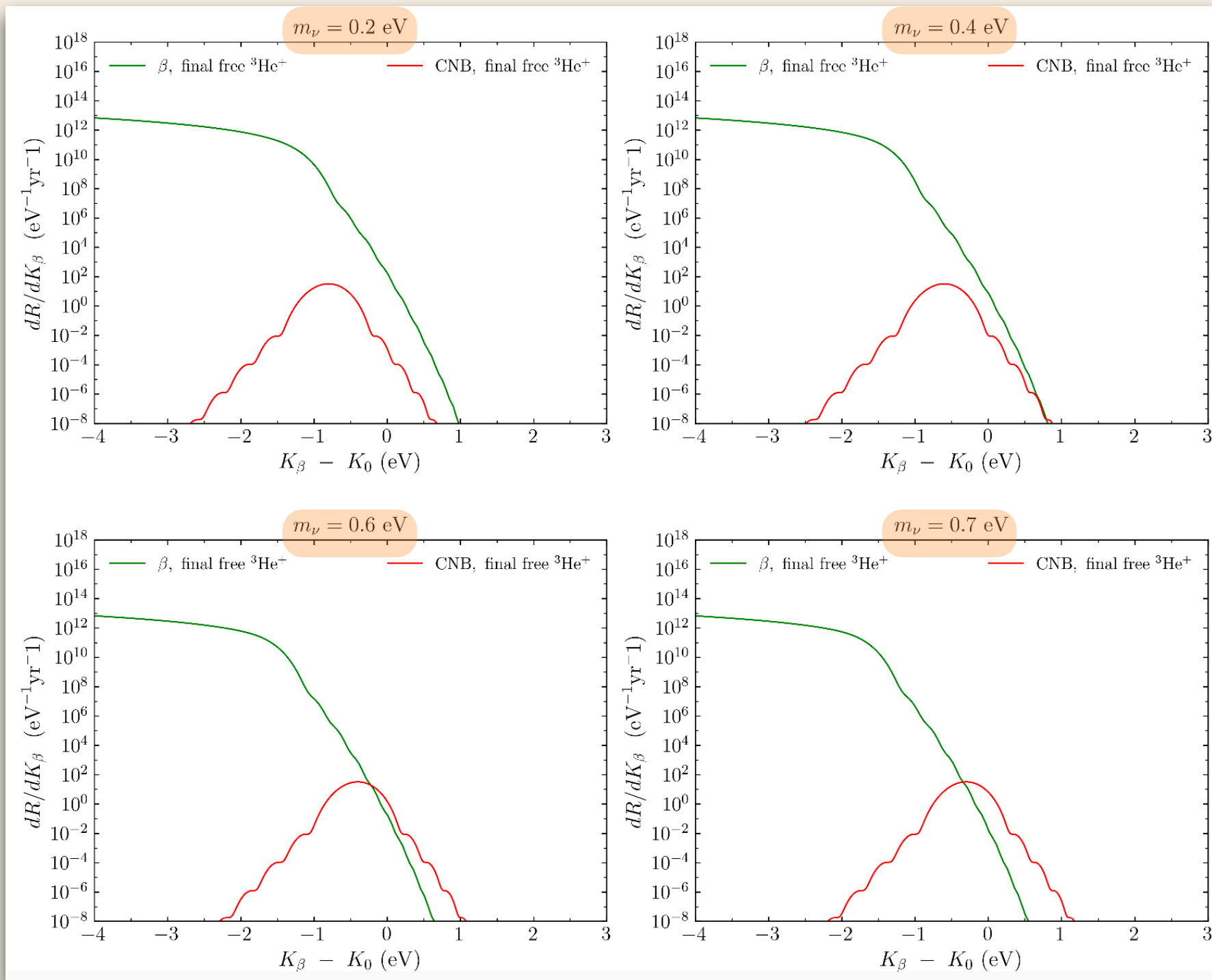


Results from C_{60}



CNB peak becomes more visible as m_ν increases...

Results from C_{60}



CNB peak becomes more visible as m_ν increases...

... but emerges only for $m_\nu \gtrsim 0.6$ eV

What if we expanded C_{60} ?

- C_{60} doesn't delocalize tritium enough



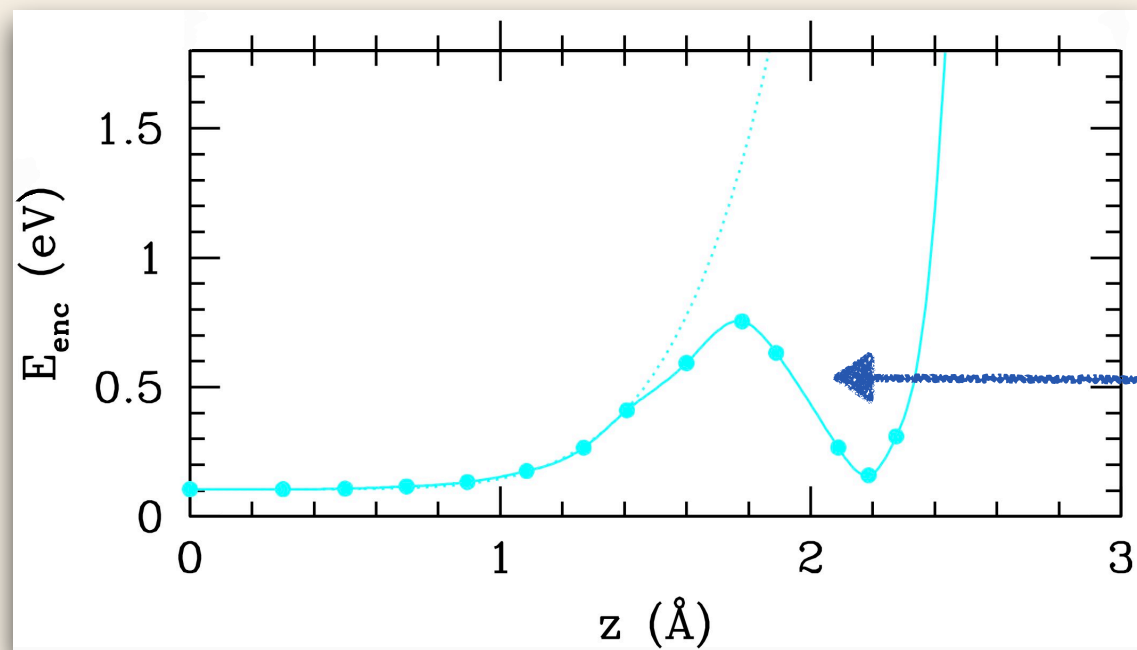
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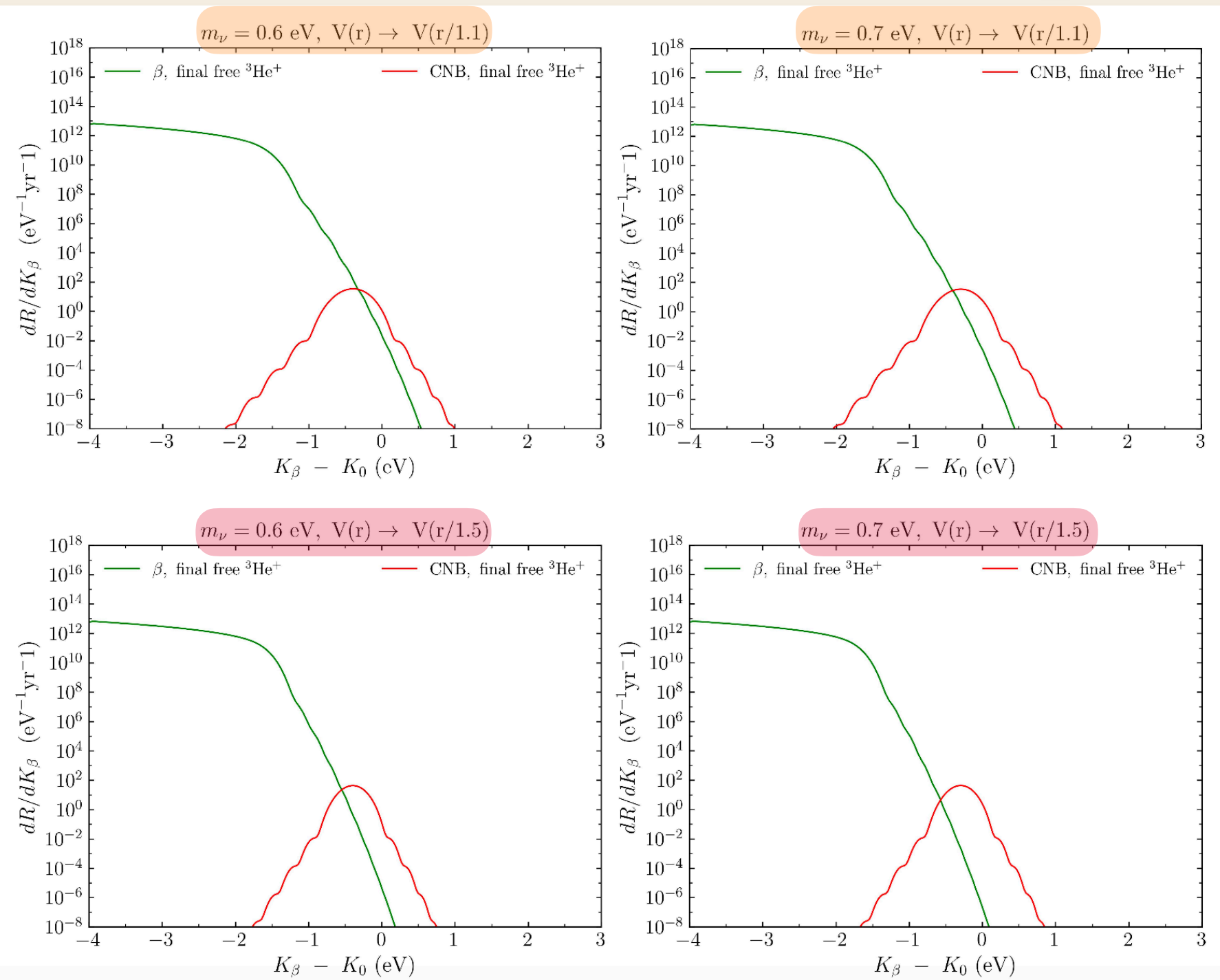
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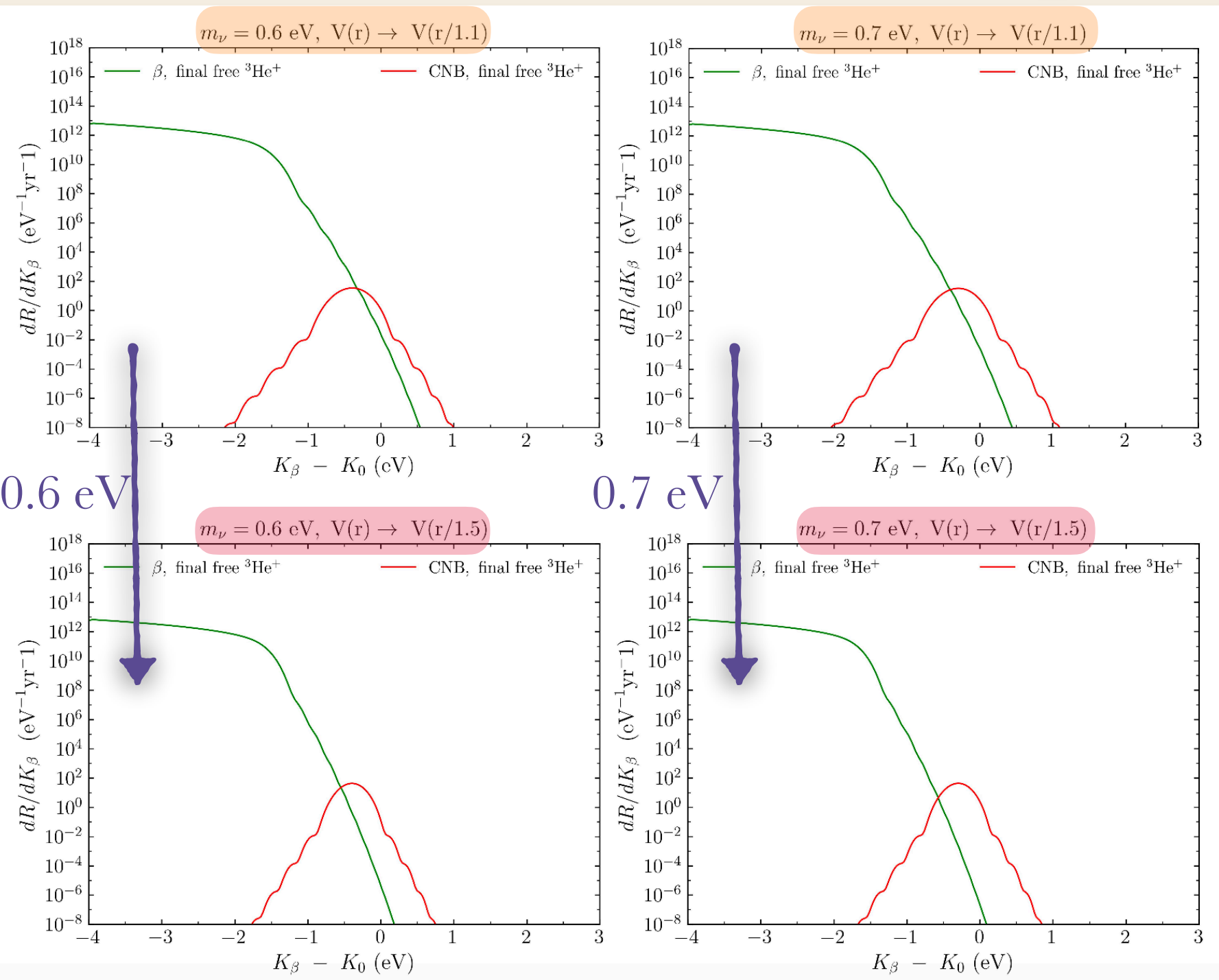
In the lab, this could be
achieved by flattening
the potential hill

Results from expanded C_{60}

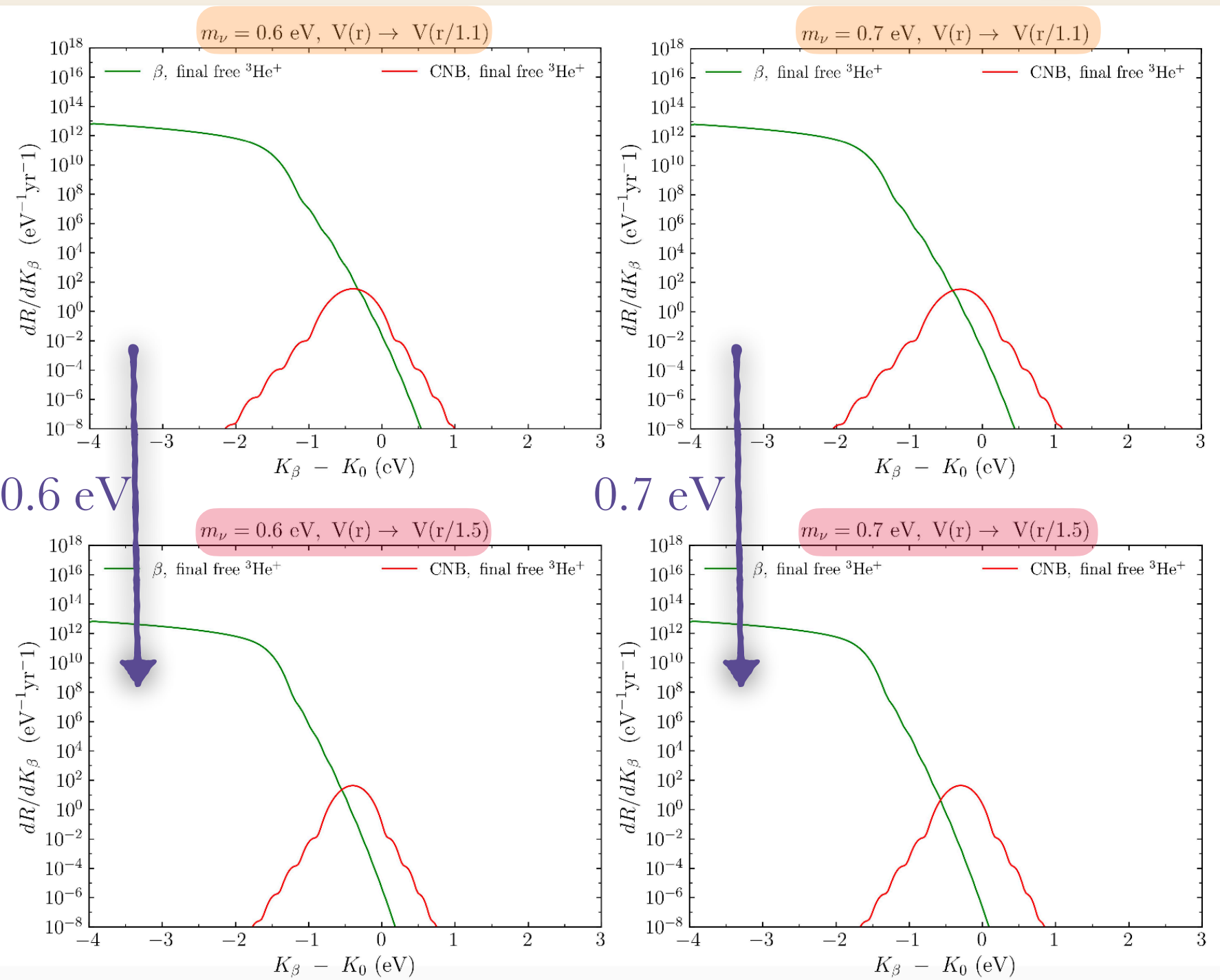


Results from expanded C_{60}

Quantum uncertainty
↓
decreases with
increasing radius:



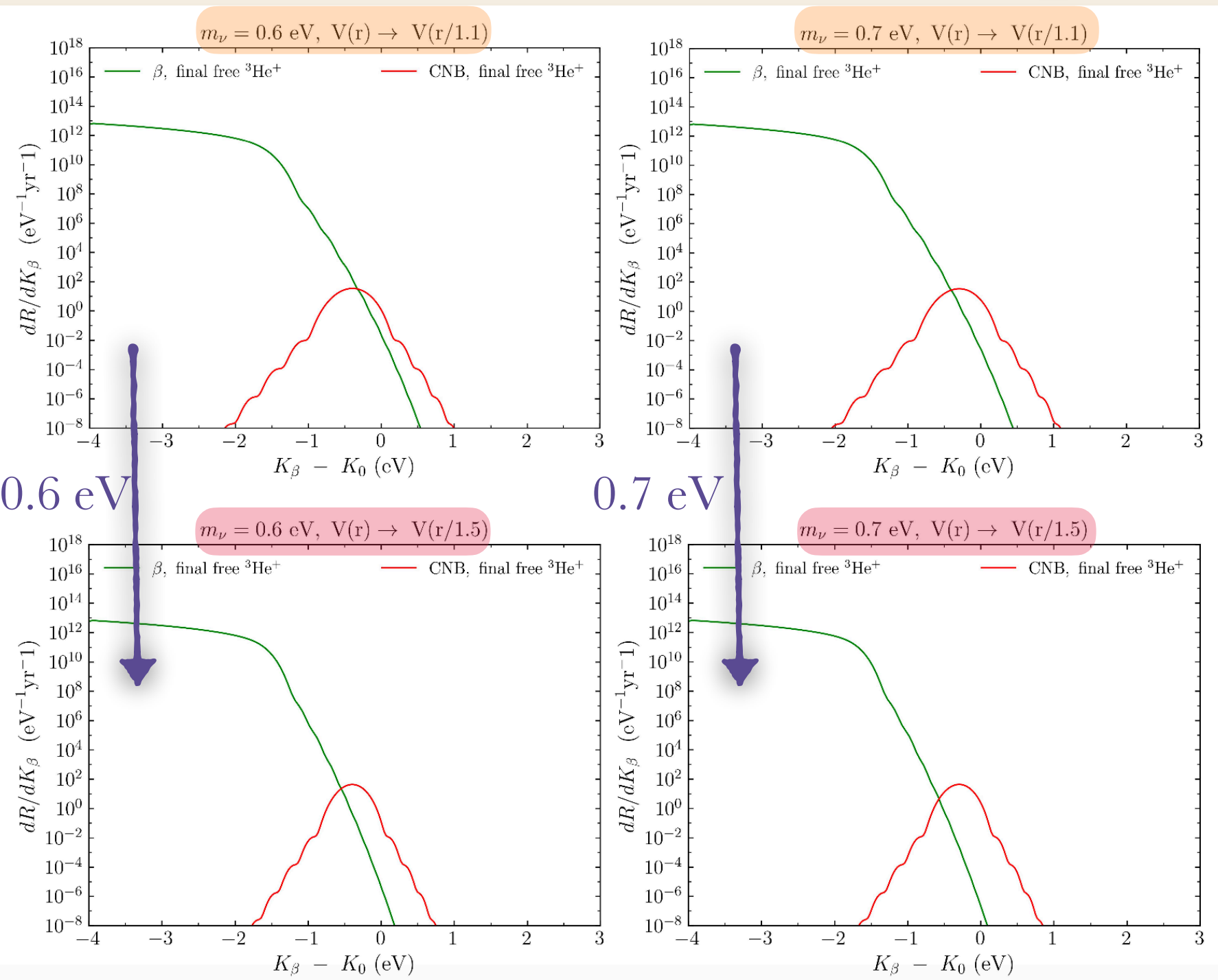
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1. Green curves become steeper: peak more visible

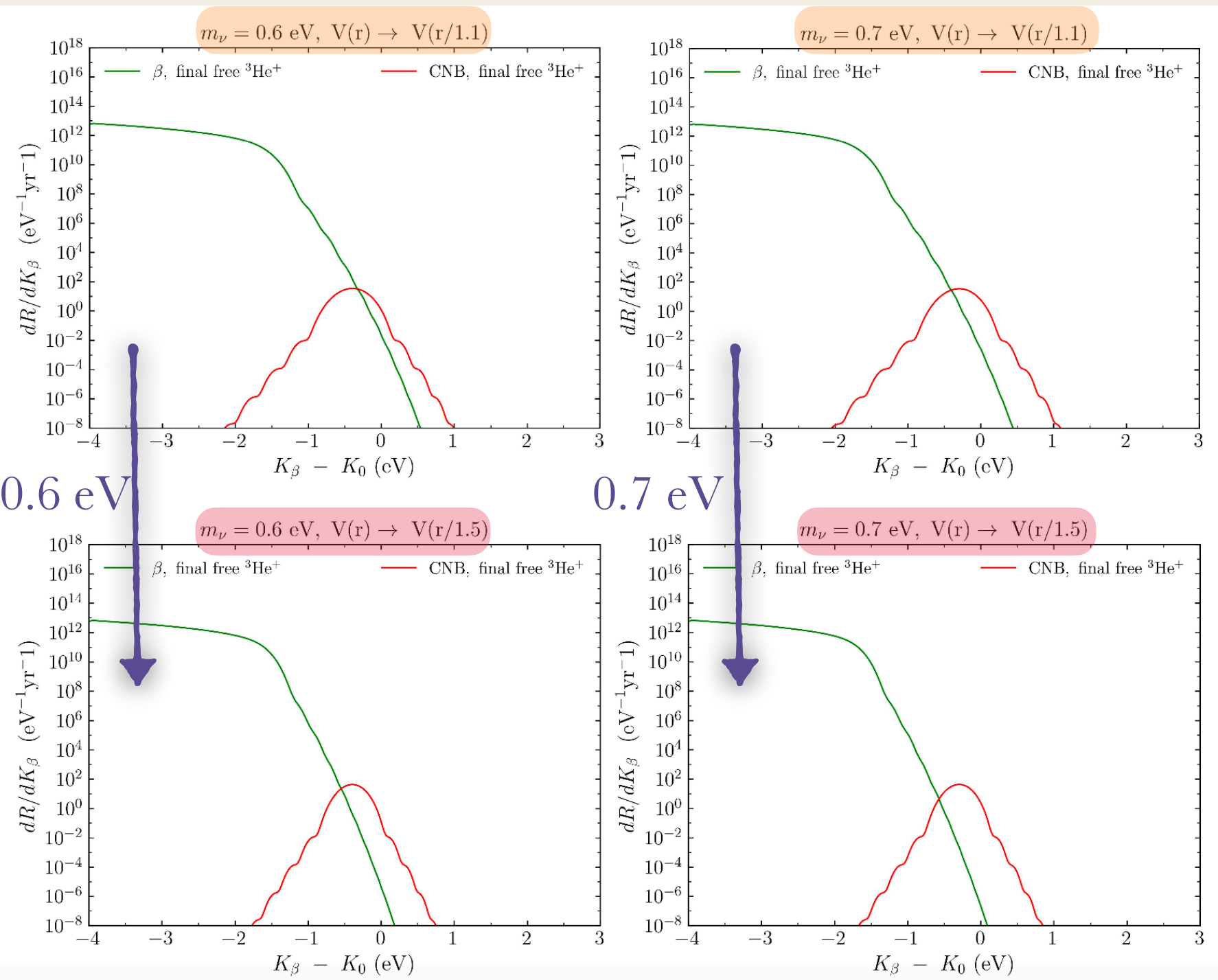
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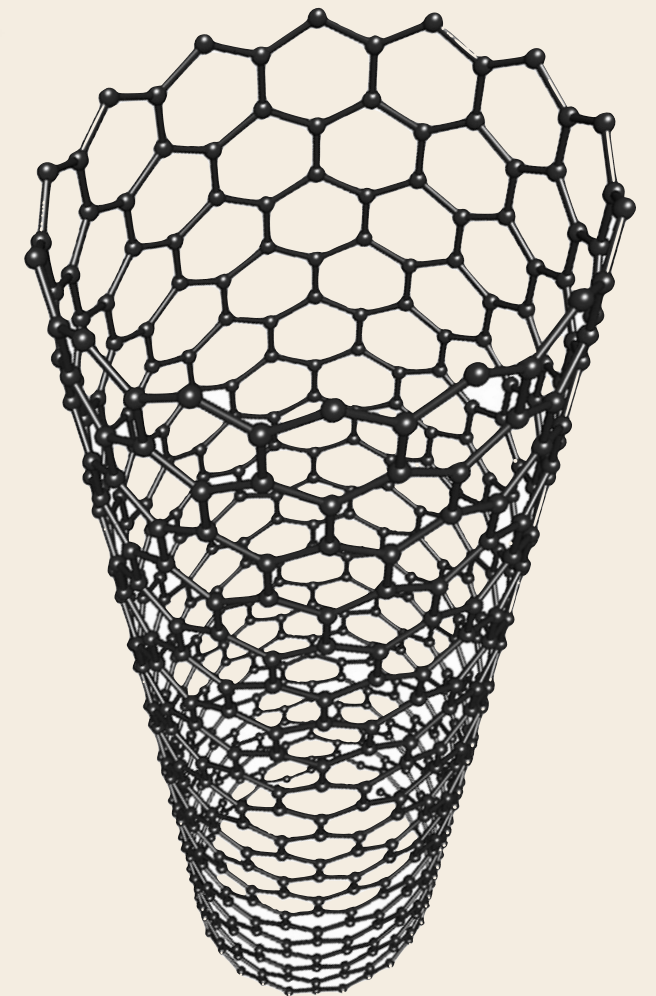
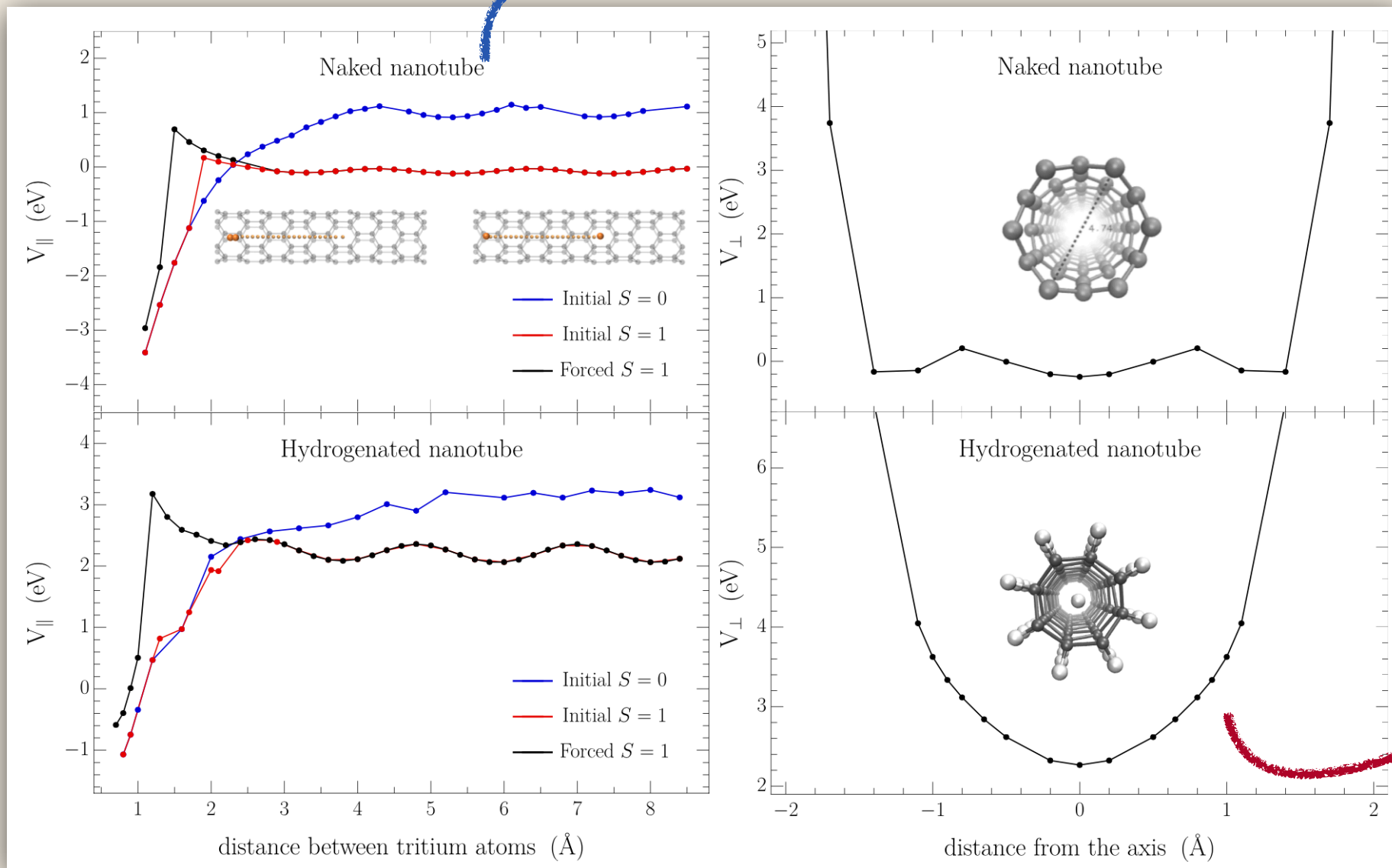
Only partially visible



Other ideas?

- **Carbon nanotubes**

Free along axis



Bound in the other directions

[PTOLEMY – PRD 2022, 2203.11228]



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- Neither **graphene** nor the C_{60} molecule seem to be ideal candidates to observe relic neutrinos





Further research is needed to determine the **optimal substrate** for the intended goal



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Thank you for your attention!