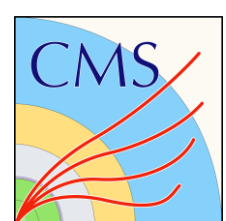


Jet substructure measurements with CMS

Kaustuv Datta (ETH Zürich)

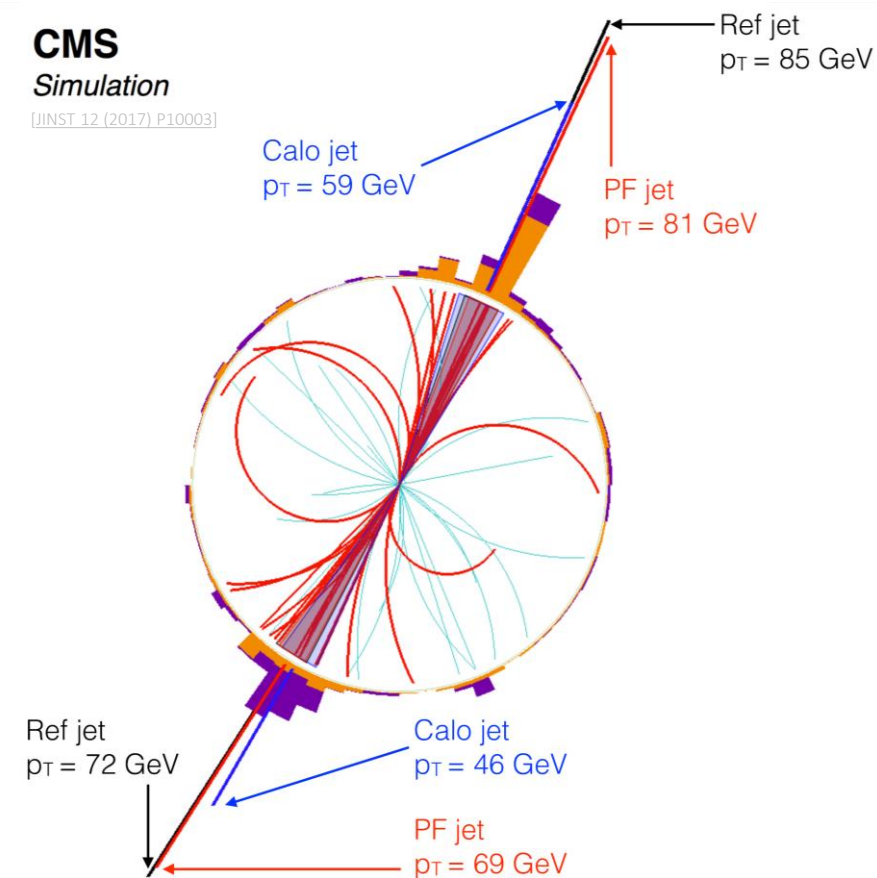
on behalf of the CMS Collaboration

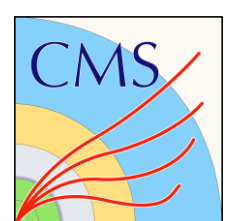
July 30, BOOST 2024



Outline

1. Introduction
2. Jet substructure measurements at CMS:
 - a. Measurement of the primary Lund jet plane density in proton-proton collisions at $\sqrt{s} = 13$ TeV; [JHEP 05 \(2024\) 116](#)
 - b. Measurement of energy correlators inside jets and determination of the strong coupling $\alpha_S(m_Z)$; [arXiv:2402.13864](#)
 - c. Girth and groomed radius of jets recoiling against isolated photons in lead-lead and proton-proton collisions at $\sqrt{s_{NN}} = 5.02$ TeV; [arXiv:2405.02737](#) (see Bharadwaj's [talk](#))
 - d. Unfolding the jet axis decorrelation in pp and PbPb collisions at $\sqrt{s_{NN}} = 5.02$ TeV with CMS; [CERN-CMS-NOTE-2024-004](#) (see Molly's [talk](#))
 - e. Jet fragmentation function and groomed substructure of bottom quark jets in proton-proton collisions at $\sqrt{s} = 5.02$ TeV; CMS-PAS-HIN-24-005 (see Lida's [talk](#))
 - f. Exploring small-angle emissions in D-tagged jets in proton-proton collisions at $\sqrt{s} = 5.02$ TeV; CMS-PAS-HIN-24-007 (see Jelena's [talk](#))
3. Summary





Introduction

(some) recent CMS measurements

- Jet substructure measurements a critical part of experimental programmes at LHC collaborations and beyond

→ experimental precision sufficient to compare unfolded measurements

to state-of-the-art in analytic calculations in perturbative QCD

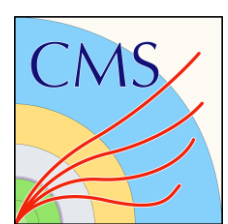
→ isolate modelling of different perturbative and non-perturbative contributions in a well-defined way

→ probe stages of jet formation, scaling properties of QCD

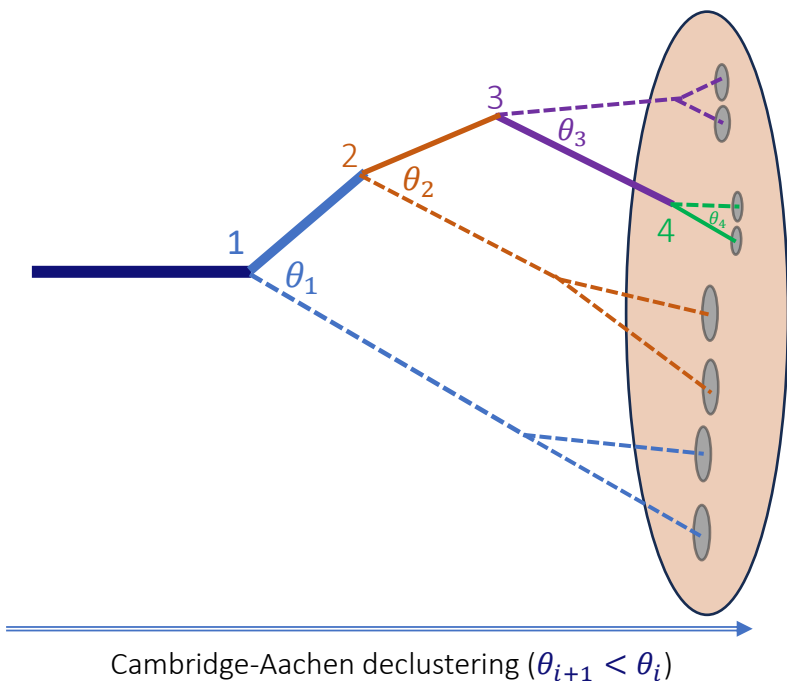
→ provide numerous handles for tuning Monte Carlo event generators, parton shower and hadronization models, custom underlying event tunes

→ reduction in uncertainties on other measurements/searches/ML taggers relying on accurate modelling of jet substructure

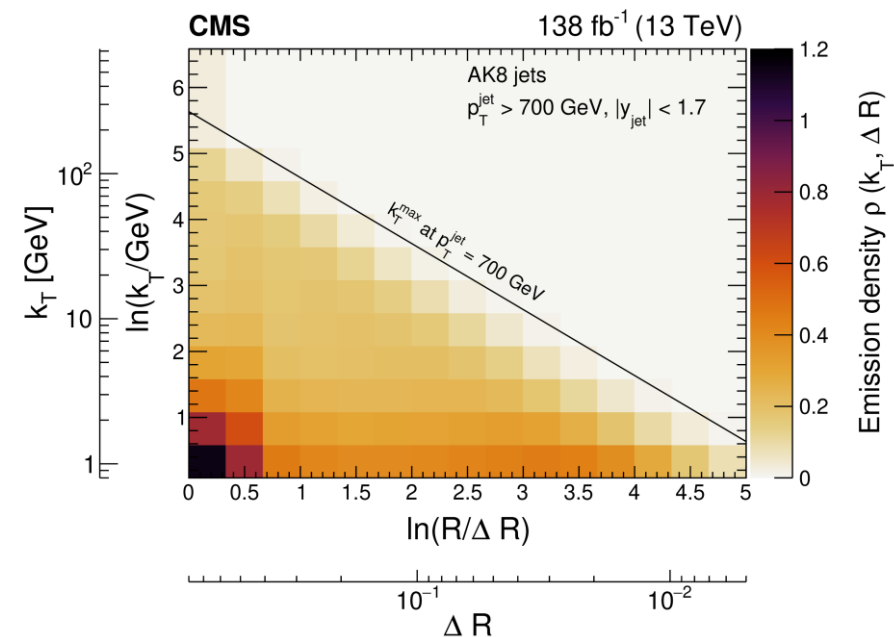
Reference, \sqrt{s}	Final state	Jets flavours, p_T (GeV)	Observables
1808.0734 13 TeV pp	$t\bar{t}$	q/g-jets (AK4), $p_T > 30$ g-jets (AK4), $p_T > 30$ b-jets (AK4), $p_T > 30$	Jet substructure and softdrop observables
1809.08602 5.02 TeV pp/PbPb	jets	q/g-jets (AK3), $p_T > 30$	Jet shapes
1911.038 13 TeV pp	$t\bar{t}$	top-jets (XC12), $p_T > 400$	XCone-groomed jet mass
2004.00602 5.02 TeV pp/PbPb	jets	q/g-jets (AK4), $p_T > 120$	Jet charge
2101.0472 5.02 TeV pp/PbPb	dijets	q/g-jets (AK4), $p_T > 50$	Jet shapes
2109.0334 13 TeV pp	dijets Z+jets	q/g-jets (AK4), $p_T > 30$ q-jets (AK4), $p_T > 30$	Generalised angularities
2210.08547 5.02 TeV pp/PbPb	jets	q/g-jets, b-jets (AK4), $p_T > 120$	Jet shapes
2211.01456 13 TeV pp	$t\bar{t}$	top-jets (XC12), $p_T > 400$	XCone-groomed jet mass
2312.16343 13 TeV pp	dijets	q/g-jets (AK4, AK8), $p_T > 700$	Lund plane
2312.17103 13 TeV pp	Jets	q/g-jets (AK4), $p_T > 550$	2D angular correlations
2402.13864 13 TeV pp	dijets	q/g-jets (AK4), $97 < p_T < 1784$	Energy correlators
2405.02737 5.02 TeV pp/PbPb	γ +jet	q/g-jets (AK2), $p_T > 40$	Groomed jet radius, girth

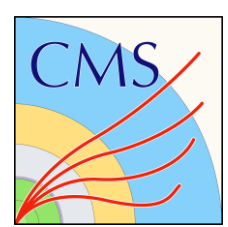


Measurement of the primary Lund jet plane density in proton-proton collisions at $\sqrt{s} = 13$ TeV



[JHEP 05 \(2024\) 116](#)





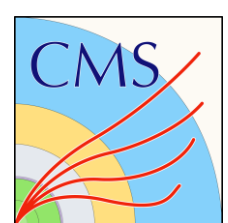
Building the primary Lund jet plane

F. Dreyer, G. Salam, G. Soyez, [JHEP 12 \(2018\) 064](#)

- Angle-ordered reclustering of particles in a jet using Cambridge-Aachen (C/A) algorithm
- Start with the full jet, work backwards through the C/A clustering tree
 - decluster object at step i , store kinematic coordinates characterizing the declustering $\{k_T^{(i)}, \Delta R^{(i)}, \dots\}$

$$\Delta R = \sqrt{(y_{softer} - y_{harder})^2 + (\phi_{softer} - \phi_{harder})^2}, \quad k_T = p_{T,softer} \Delta R$$

→ repeat along the harder of two branches until only 1 particle left on hard branch



Building the primary Lund jet plane

F. Dreyer, G. Salam, G. Soyez, [JHEP 12 \(2018\) 064](#)

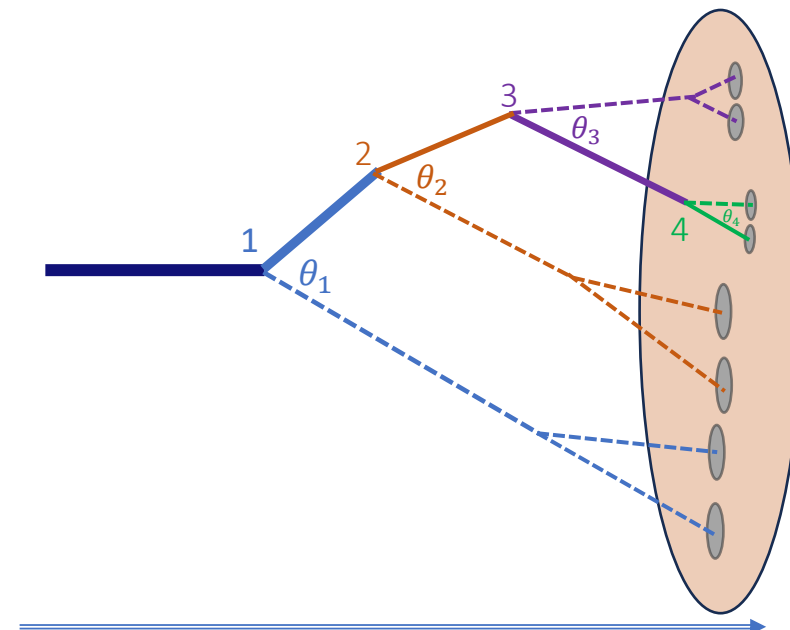
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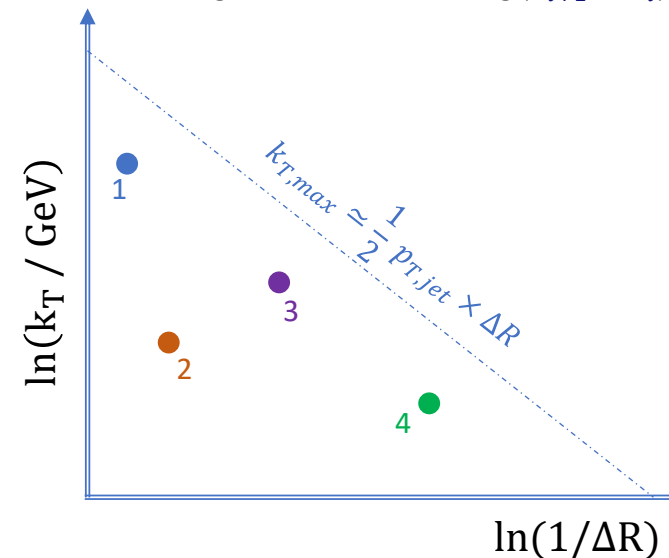
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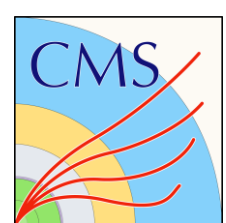
→ repeat along the harder of two branches until only 1 particle left on hard branch

- Ordered list of tuples of kinematic variables fills the primary Lund plane from left to right, (from larger to smaller splitting angles)
- See [Cristian's talk](#) on isolating a gluon-enriched phase space using the secondary LJP!
- Measurements by ATLAS [Phys. Rev. Lett. 124, 222002 \(2020\)](#) and ALICE [ALICE-PUBLIC-2021-002](#)



Cambridge-Aachen declustering ($\theta_{i+1} < \theta_i$)





Building the primary Lund jet plane

F. Dreyer, G. Salam, G. Soyez, *JHEP* 12 (2018) 064

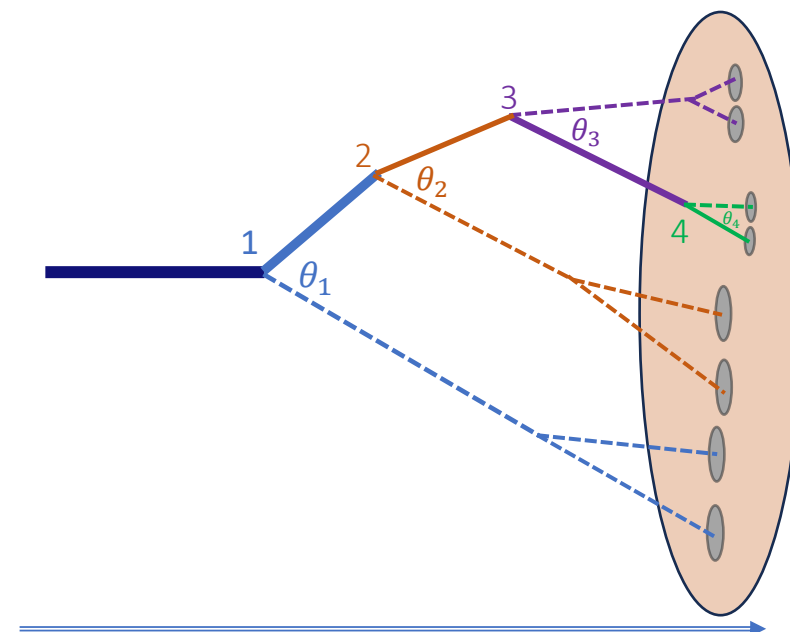
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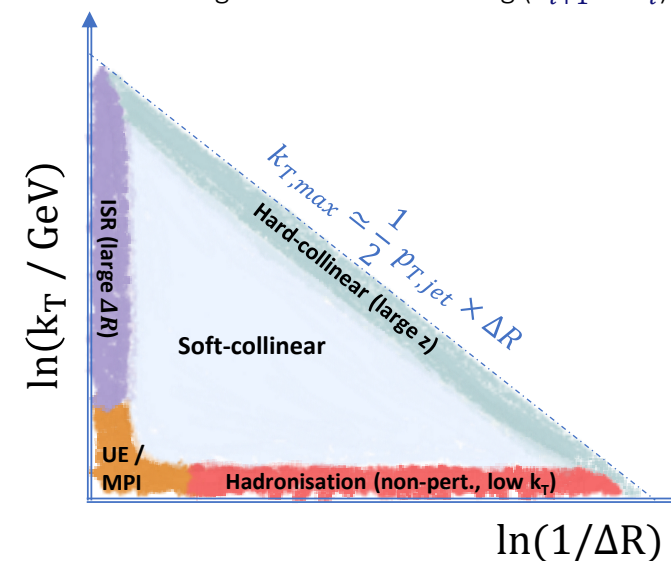
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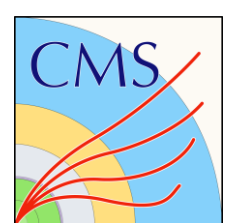
→ repeat along the harder of two branches until only 1 particle left on hard branch

- Different QCD mechanisms naturally localized to specific regions of the plane
 - test calculations explicitly for different regimes in slices of k_T and ΔR
 - study specific aspects of mismodeling in MC event generators and parton shower/hadronization models and UE tunes



Cambridge-Aachen declustering ($\theta_{i+1} < \theta_i$)

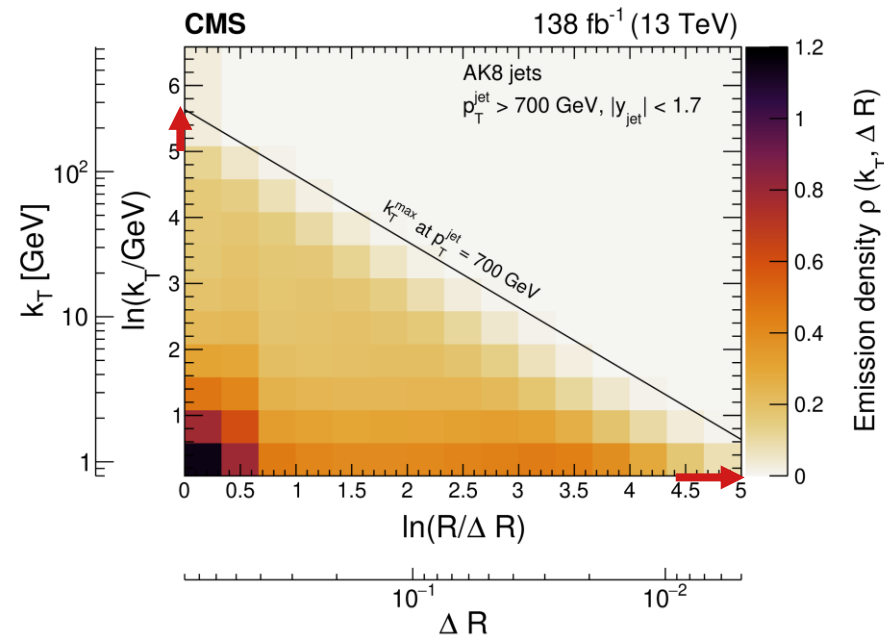
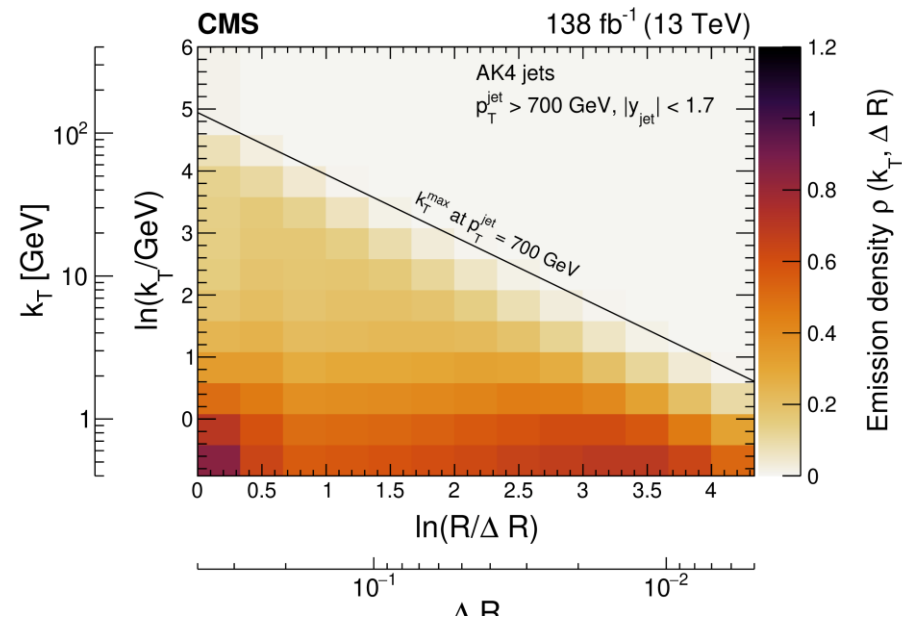


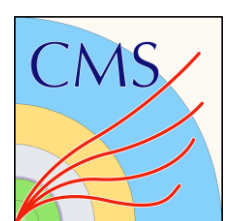


LJP: CMS measurement in Run 2

[JHEP 05 \(2024\) 116](#)

- Inclusive jet selection, with central, high p_T jets:
 - $p_T > 700$ GeV, $|y| < 1.7$
 - anti- k_T jets with $R = 0.4$ and 0.8 (larger PS for hard & wide-angle emissions)
range of the measurement:
 - $\sim 0.4(1) < k_T < \sim 300(700)$ GeV, $0.005 < \Delta R < 0.4(0.8)$
 - pileup (PU) mitigation using charged-hadron subtraction (CHS)
 - negligible background contributions from non-QCD processes,
 - only **charged** constituents/PF candidates:
 - improved angular & momentum resolution
 - PU contributions better controlled
- First measurements in large-radius jets; mitigates clustering effects in large swathes of the plane
- [HEPData](#) entry available for unfoldings



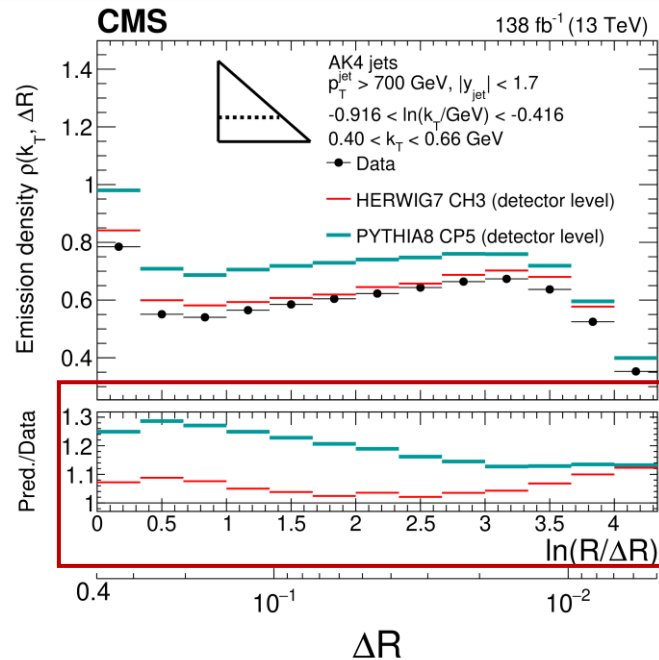
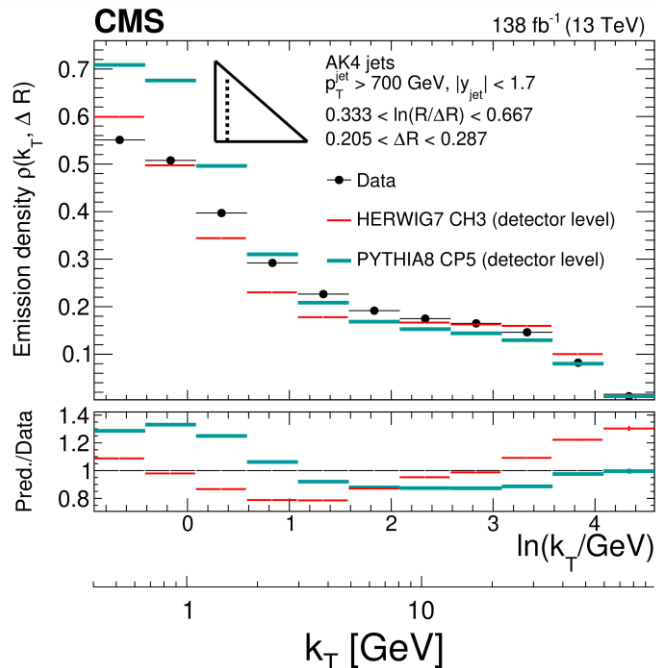
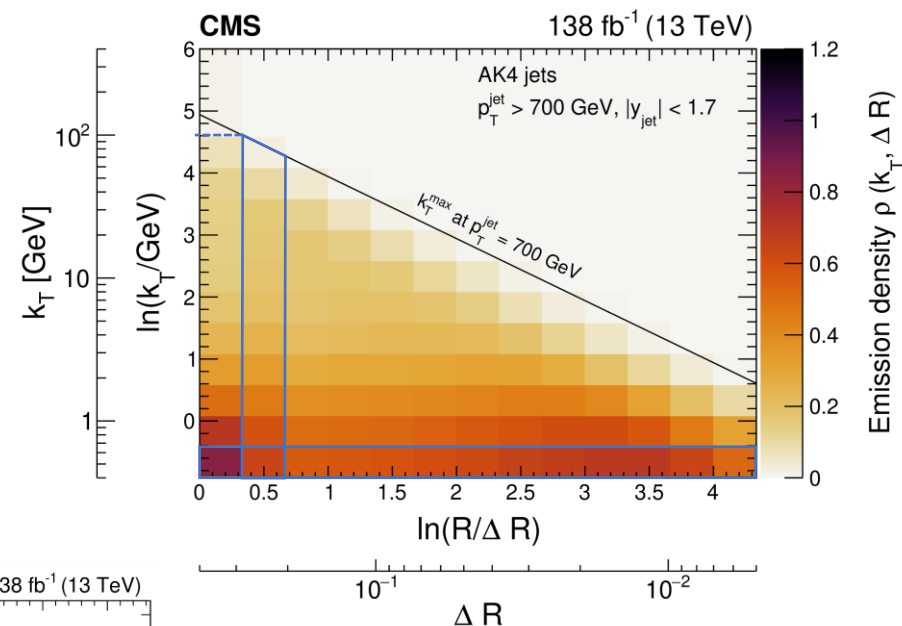


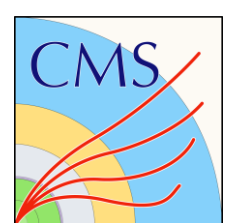
LJP: CMS measurement in Run 2

NB: 1-D slices are at the **detector level**, and LJP density after unfolding to the **particle level**

[JHEP 05 \(2024\) 116](#)

- Measurements are unfolded to particle level
 - **PYTHIA8 CP5** and **HERWIG7 CH3** generally envelope data at **detector level** except in low k_T slice
 - migration matrices and other corrections to detector level derived in nominal MC (**PYTHIA8** w. **CP5** tune),

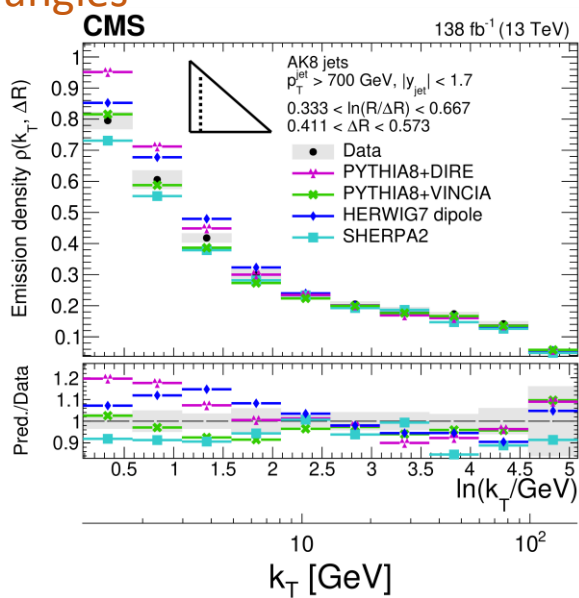
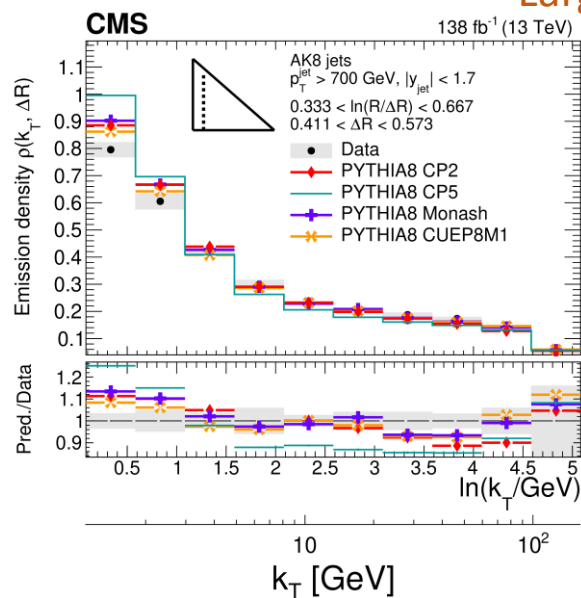




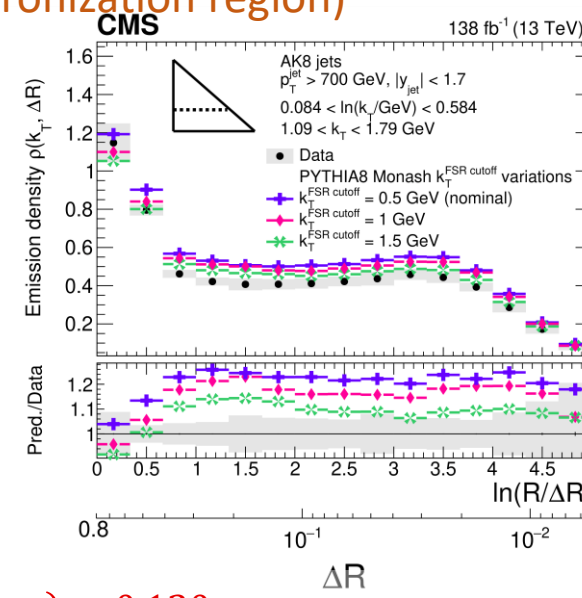
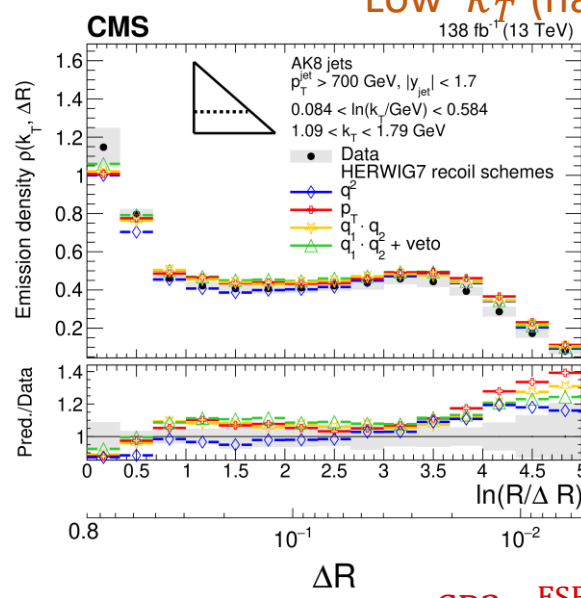
LJP: Handles on PS models and UE tunes

JHEP 05 (2024) 116

Large angles



Low k_T (hadronization region)



$$\text{CP2 } \alpha_S^{\text{FSR}}(m_Z) = 0.130$$

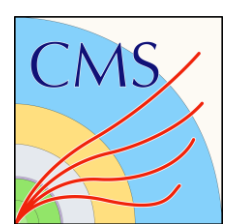
$$\text{CP5 } \alpha_S^{\text{FSR}}(m_Z) = 0.118$$

$$\text{Monash } \alpha_S^{\text{FSR}}(m_Z) = 0.1365$$

$$\text{CUPE8M1 } \alpha_S^{\text{FSR}}(m_Z) = 0.1365$$

- Extensive set of tune/parton shower model comparisons
 - PYTHIA8 tunes: CP5, CP2, Monash, CUPE8M1
 - dipole shower models: VINCIA, DIRE, HERWIG7 dipole, SHERPA
 - angle-ordered Herwig7.2 recoil schemes: q^2 , p_T , $q_1 \cdot q_2$, $q_1 \cdot q_2 + \text{veto}$
 - variations of k_T^{FSR} cutoff in Monash tune: 0.5, 1, 1.5 GeV
- Differences, all MC, $\sim 10\text{--}20\%$ vs. bulk of the distribution in unfolded data

- Higher values of $\alpha_S^{\text{FSR}}(m_Z)$ and k_T^{FSR} describe substructure better
- Angle-ordered showers in HERWIG7 more compatible with data vs. dipole shower across bulk of LJP; q^2 $q_1 \cdot q_2 + \text{veto}$ scheme better in (non-)perturbative region,



LJP: Constraining emission patterns in a jet

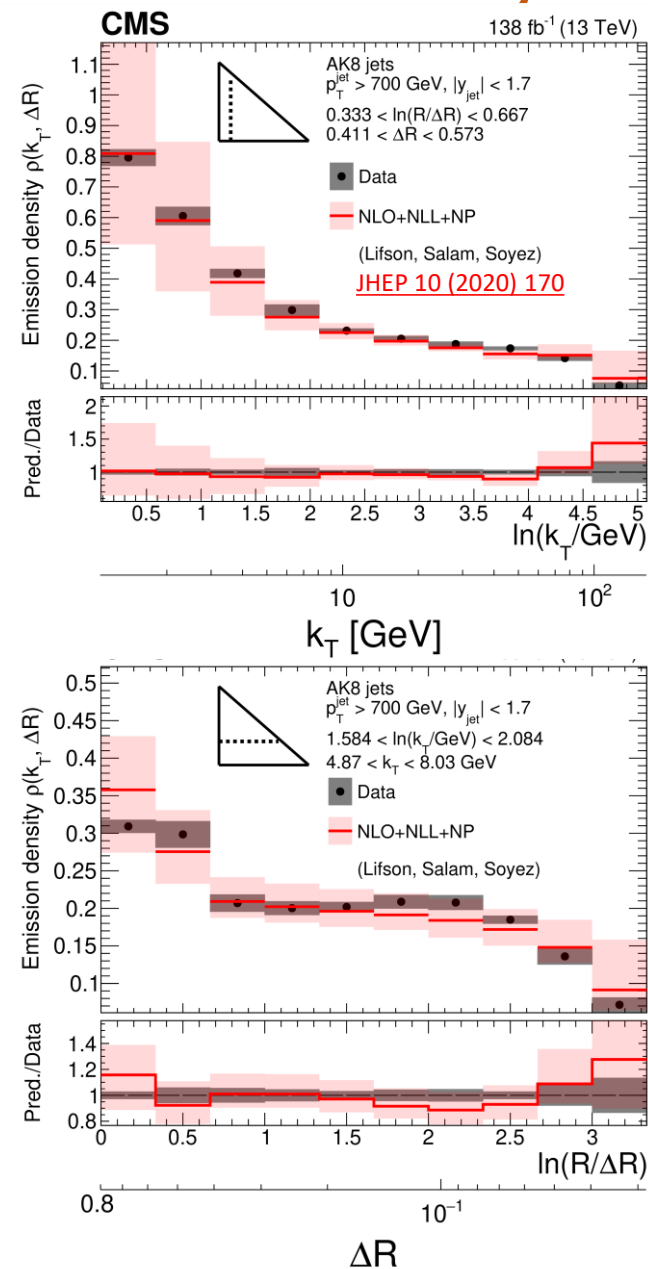
[JHEP 05 \(2024\) 116](#)

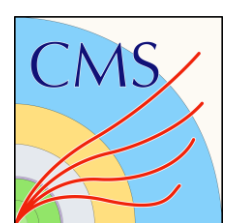
- Comparison to parton level pQCD predictions in measurement phase space

- NLL accuracy, matched to NLO, with NP corrections
- ρ scaled by avg. charged fraction (0.62)
- bin-by-bin correction to hadron level with MC
- theory uncertainties: from pQCD calculation and NP corrections
- resummation of non-global logs \leftrightarrow increased density at large ΔR
- effect of non-perturbative corrections \leftrightarrow at low k_T (< 5 GeV)

Analytical calculations of substructure consistent with unfolded data;

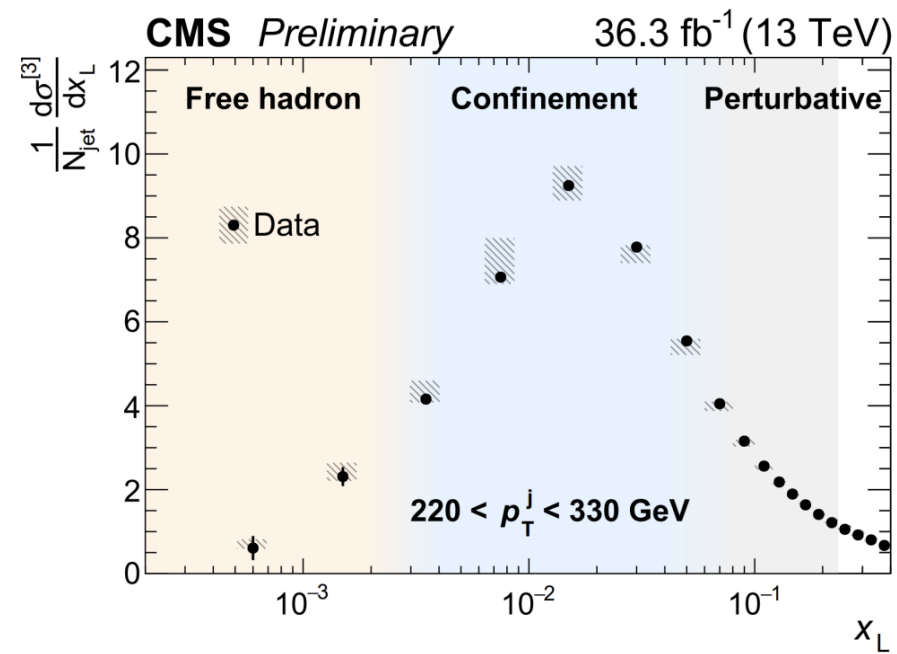
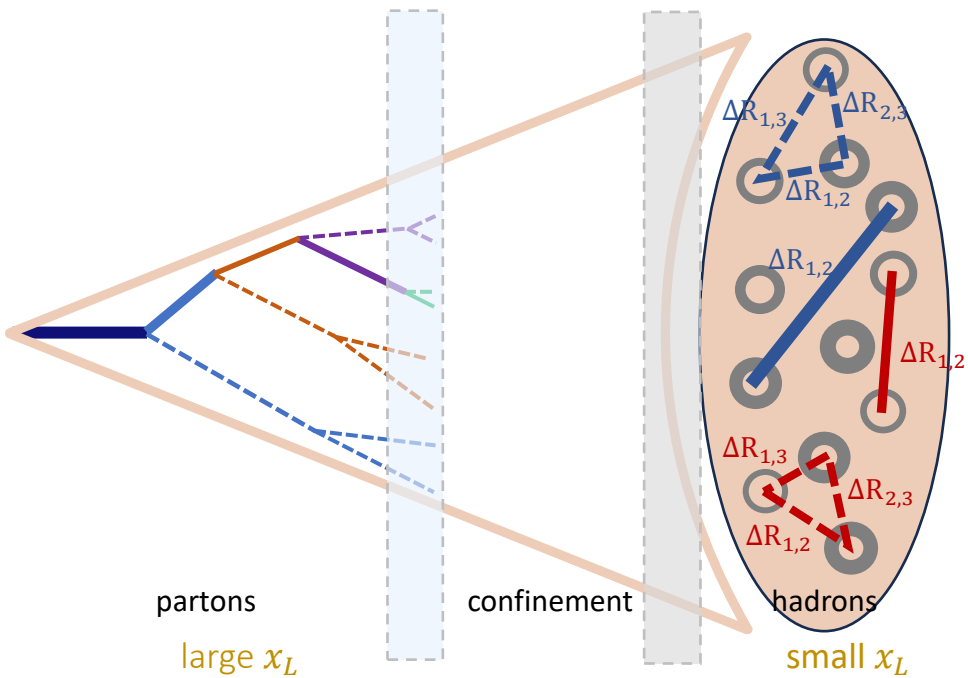
precision measurement \leftrightarrow our understanding of radiation in jets!

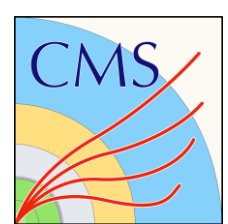




Measurement of energy correlators inside jets and determination $\alpha_S(m_Z)$

[arXiv:2402.13864](https://arxiv.org/abs/2402.13864)





Energy correlators in jets

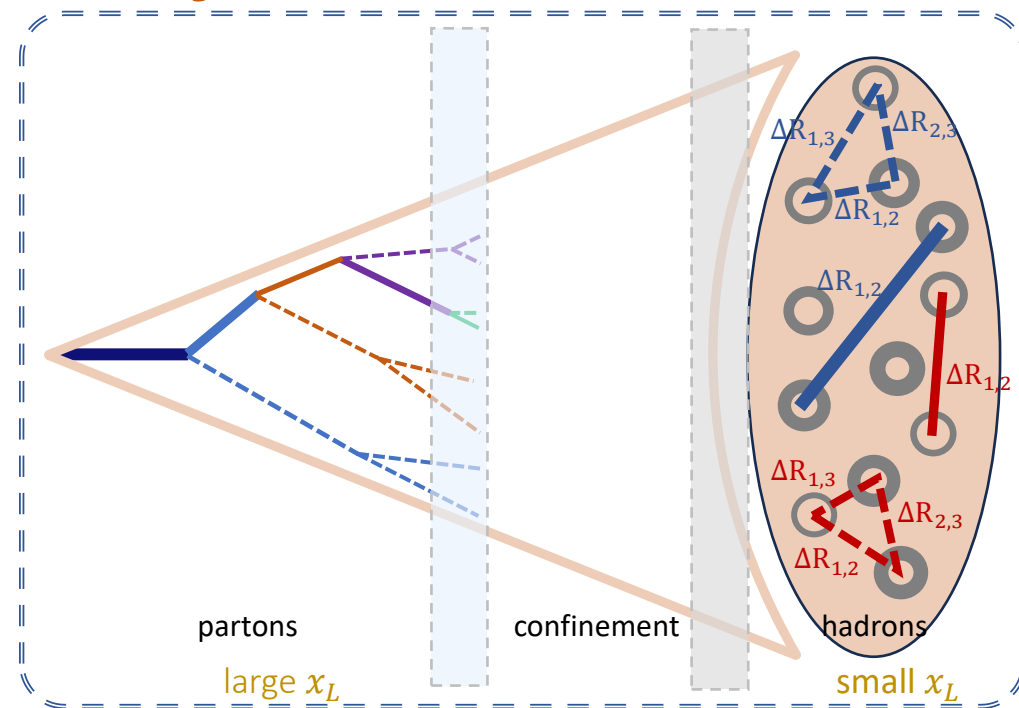
- Unravel dynamics of jet formation, probe scaling behaviour of QCD
- jet substructure ↔ study of correlation functions of energy flow operators in the collinear limit (plane of detector cells effectively at infinity)

$$\epsilon(\vec{n}) = \int_0^\infty dt \lim_{r \rightarrow \infty} r^2 n^i T_{0i}(t, r\vec{n})$$

→ $\langle \Psi | \epsilon(\hat{n}_1) \dots \epsilon(\hat{n}_N) | \Psi \rangle$, perturbatively calculable at higher orders

→ n-point energy correlators, projected onto axis of (largest) angular distance x_L :
energy weight

$$EnC = \frac{d\sigma^{[n]}}{dx_L} = \sum_n \sum_{1 \leq i_1 \dots i_N \leq n} \int d\sigma \frac{\prod_{a=1}^N E_{i_a}}{E^N} \delta(x_L - \max\{\Delta R_{i_1, i_2} \dots \Delta R_{i_{N-1}, i_N}\})$$



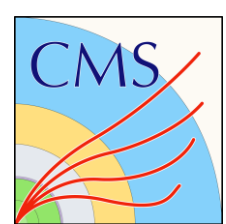
Hofman, Maldacena;
[JHEP 05 \(2008\) 012](#)

Dixon, Moutl, Zhu;
[Phys. Rev. D 100, 014009](#)

Chen, Moutl, Zhang, Zhu;
[Phys. Rev. D 102, 054012](#)

Chen, Luo, Moutl, Yang, Zhang, Zhu;
[JHEP 08 \(2020\) 028](#)

Lee, Meçaj, Moutl;
[arXiv:2205.03414](#)



Energy correlators in jets

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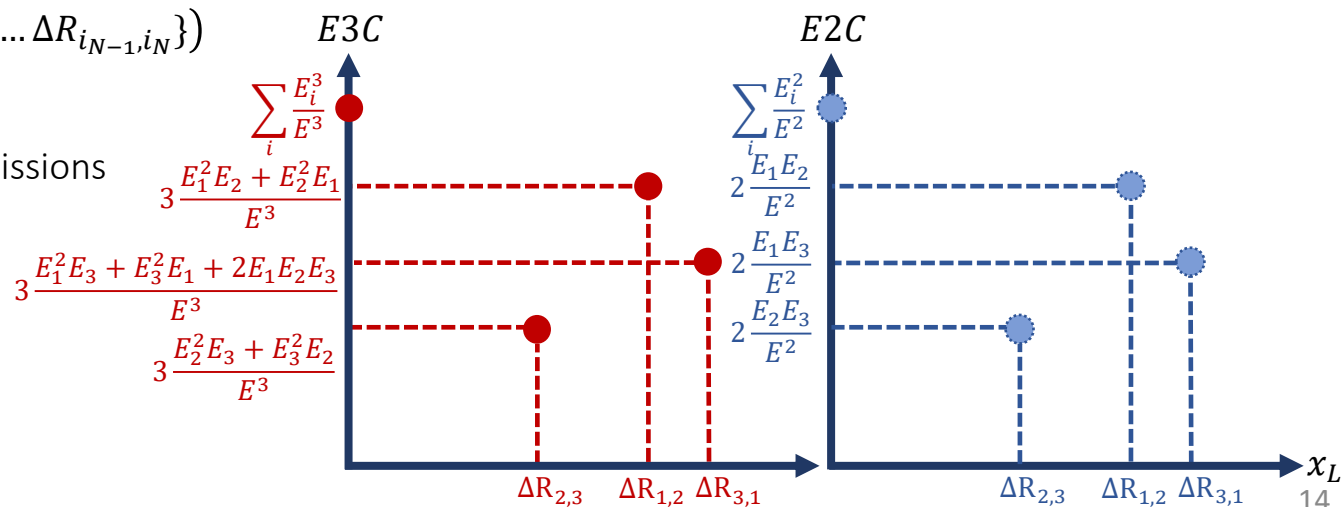
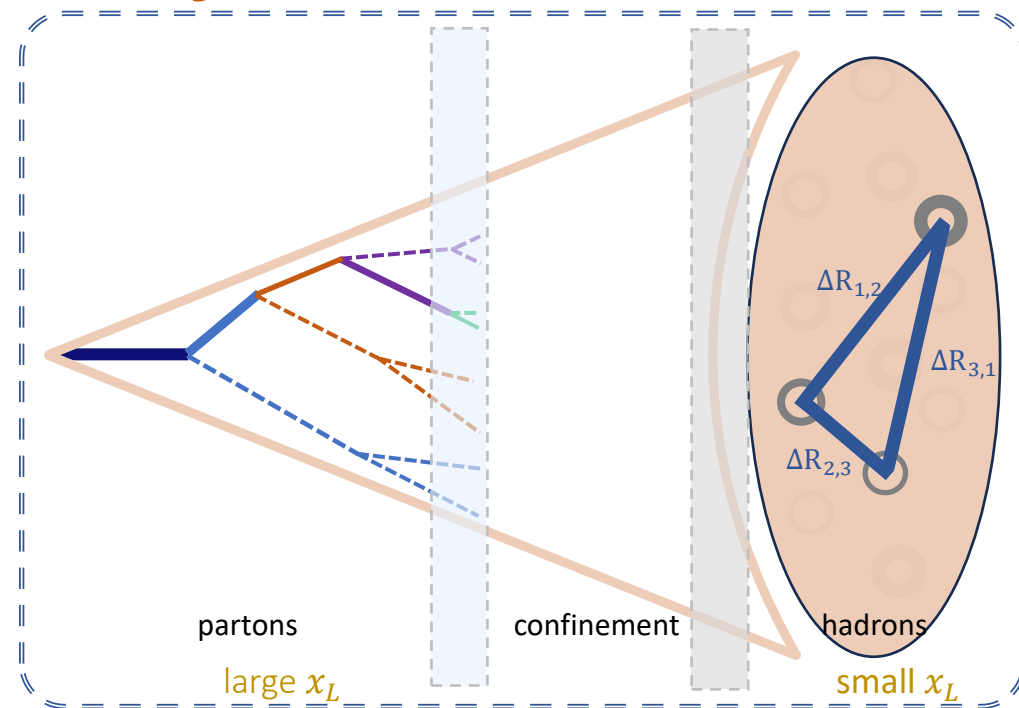
$$\epsilon(\vec{n}) = \int_0^\infty dt \lim_{r \rightarrow \infty} r^2 n^i T_{0i}(t, r\vec{n})$$

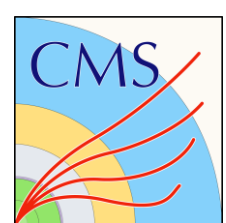
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- Multi-entry distributions for correlations between pairs/triplets of emissions
- Amenable to a novel extraction of the strong coupling





Energy correlators in jets

- Substructure measurements of α_s complicated by degeneracies between α_s and q/g fractions in jets (emission probabilities $\propto \alpha_s C_i$)

- Linear dependence on strong coupling at leading log:

$$E2C, E3C \sim c_0 + c_1 \alpha_s(Q) \ln(x_L) + O(\alpha_s^2) + (\dots),$$

→ different c_i 's for E2C and E3C, dependent on color factors C_i

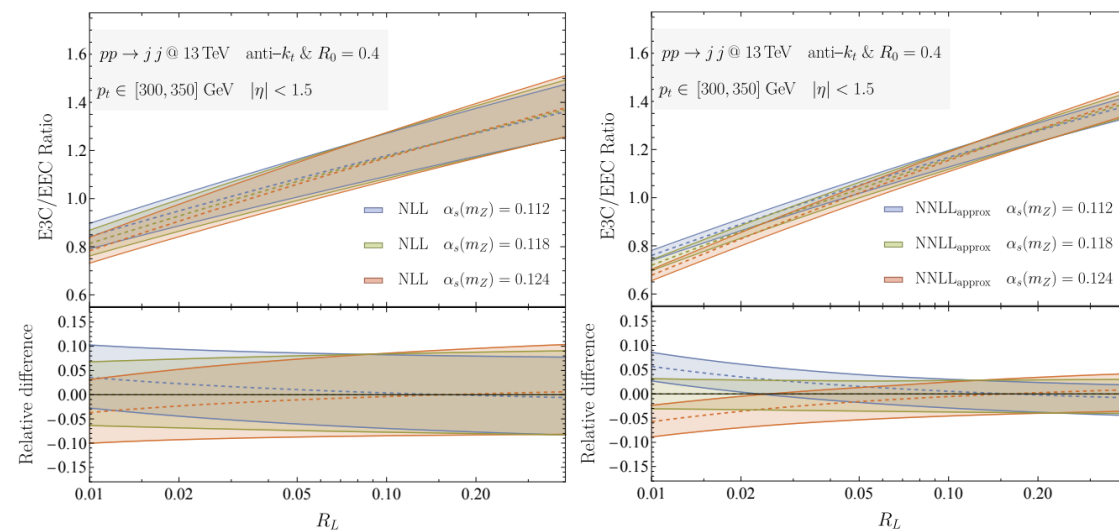
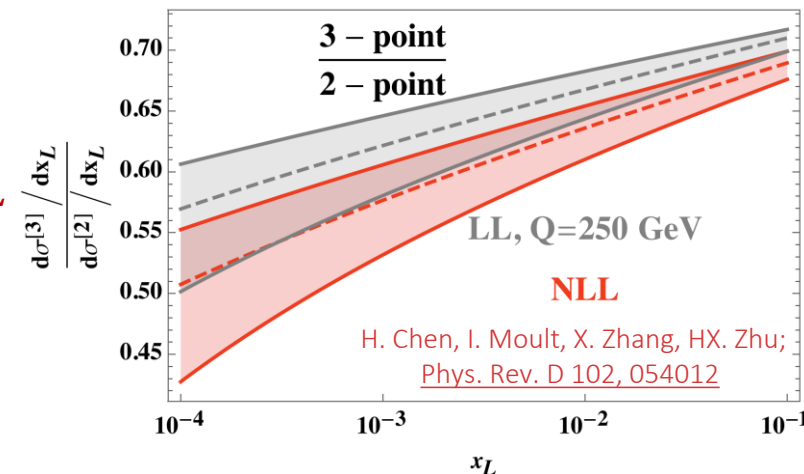
and q/g fractions

$$\frac{E3C}{E2C} = \frac{d\sigma^{[3,2]}}{dx_L} \propto \alpha_s(Q) \ln(x_L) + O(\alpha_s^2),$$

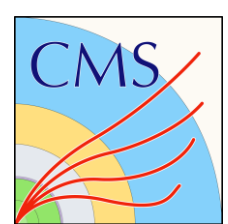
→ ratio mitigates dependence on q/g fraction, robust to detector effects, cancellation of PDF uncertainties, highlights dependence on $\alpha_s(Q)$

- Scale uncertainties still large at NLL due to perturbative corrections, with effect of corrections greatly reduced at NNLL accuracy

$$Q \sim p_{T,jet} \cdot x_L$$



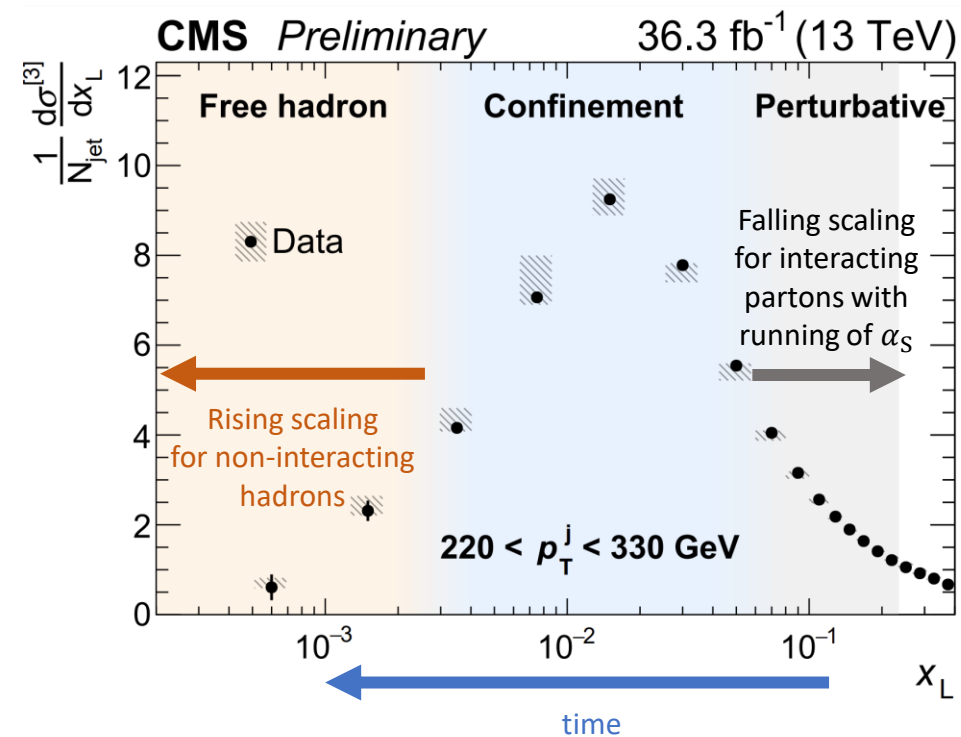
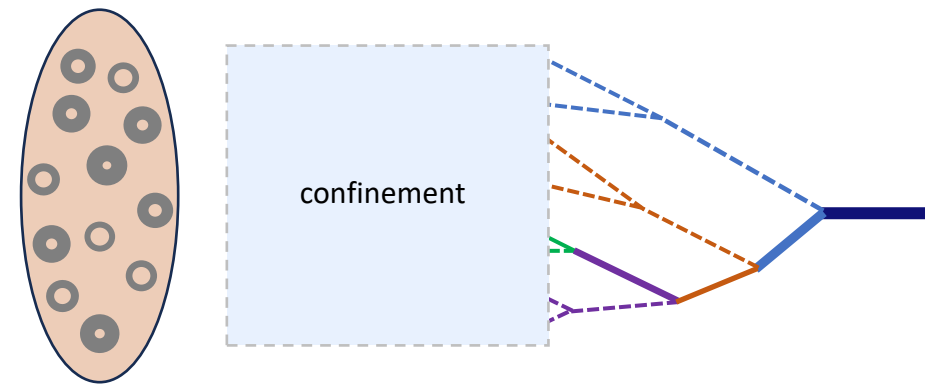
W. Chen, J. Gao, Y. Li, Z. Xu, X. Zhang, HX. Zhu;
[JHEP 05 \(2024\) 043](#)

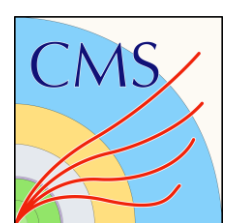


ENC: CMS measurement in Run 2

[arXiv:2402.13864](https://arxiv.org/abs/2402.13864)

- Inclusive jet selection requiring at least 2 jets:
 - $97 < p_T < 1784 \text{ GeV}$ (8 regions), $|\eta| < 2.1$, $|\Delta\phi(j_1, j_2)| > 2$,
 - anti- k_T jets with $R = 0.4$ ($Q \sim p_{T,\text{jet}} x_L: 5 - 80 \text{ GeV}$)
 - negligible background contributions from non-QCD physics processes
 - charged-hadron subtraction (CHS)
 - neutral and charged particles with $p_T > 1 \text{ GeV}$
 - measurement in 2016 data (36.3 fb^{-1}), enough events for precision, low PU
- First measurement of 3-point correlator, and extraction of strong coupling using E3C/E2C ratio
- Slope measurements of ratio vs. $\ln(x_L)$ sensitive to α_S
 - study in slices of p_T to probe running of the coupling with energy scale



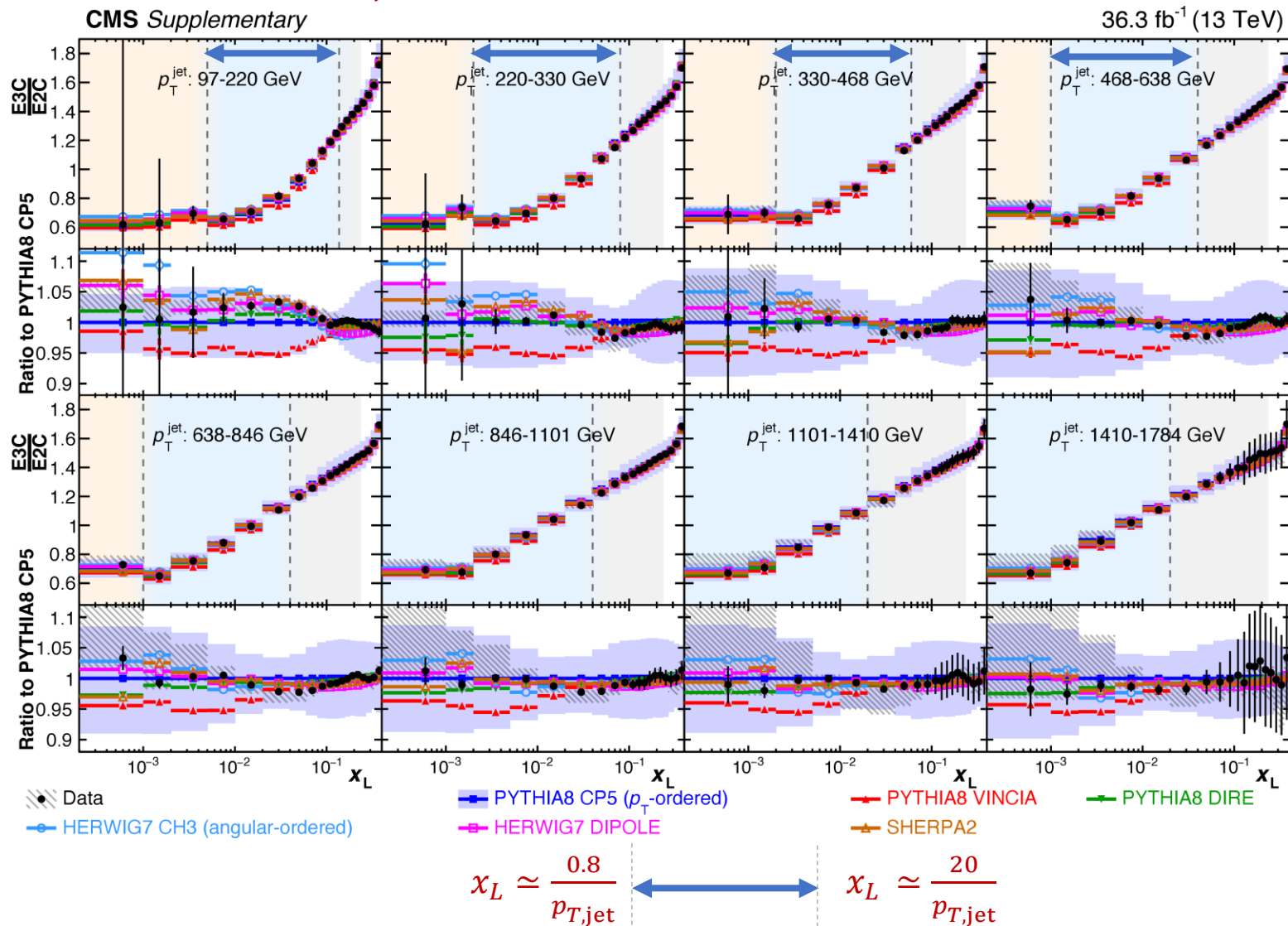


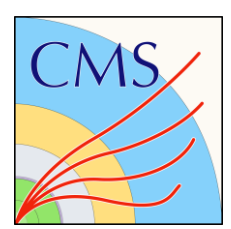
E3C/E2C: Unfolded measurements

arXiv:2402.13864

$Q \propto x_L \cdot p_{T,jet}$: Boundaries between regions shift to smaller x_L at high p_T

- Uncertainties and disagreements with data reduced in ratio E3C/E2C vs. x_L
 - ~10% data/MC disagreement reduced to ~3%
 - experimental systematics ~8% reduced to ~3%
- Leading contributions to uncertainties:
 - shower and model uncertainties
 - neutral hadron and photon energy scale
- Slope of distributions in perturbative region reduces at larger values of p_T

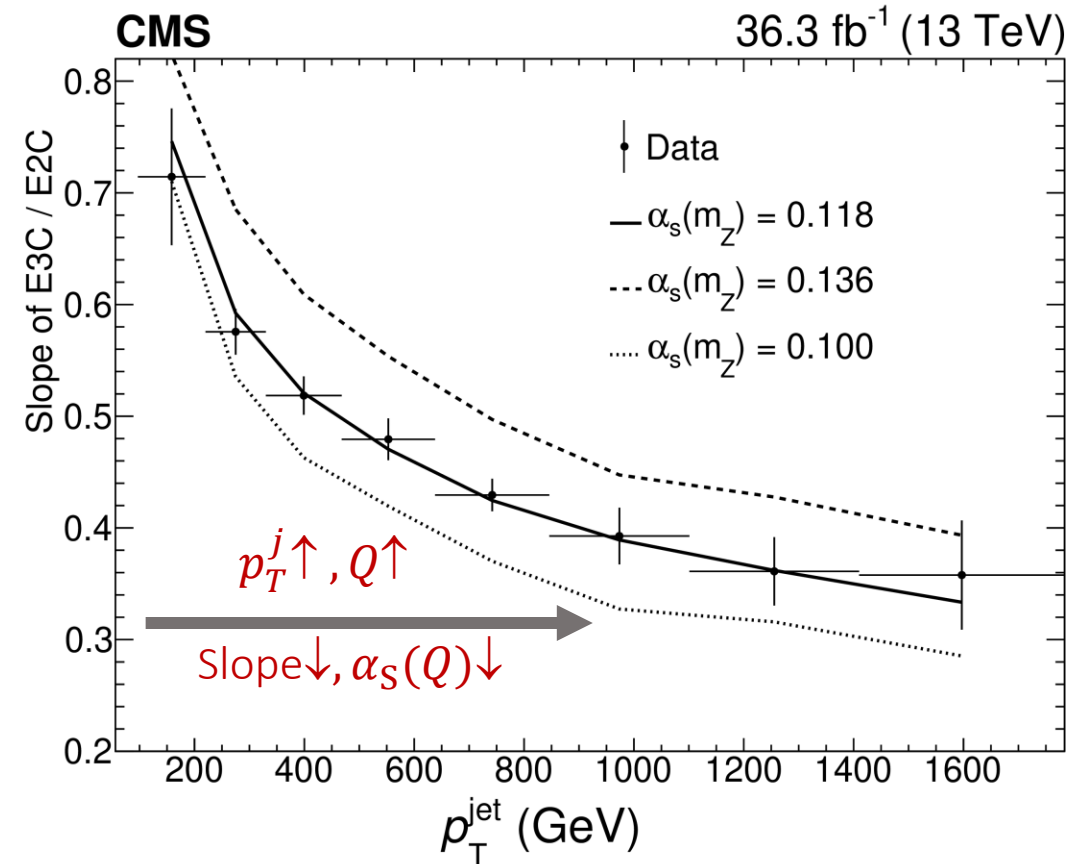


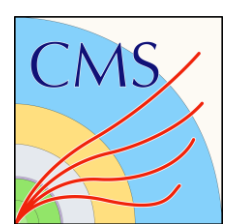


E3C/E2C: Observation of asymptotic freedom

[arXiv:2402.13864](https://arxiv.org/abs/2402.13864)

- Slopes of ratios in perturbative region reduces at higher p_T
- Fit $\Delta(E3C/E2C)/\Delta \ln x_L$ in a p_T region, and plot as a function of p_T (x-errors widths of p_T regions)
- **Direct observation of asymptotic freedom at large energy scales!**
- Comparisons to median values (in x_L) of three different theoretical predictions in perturbative region with variations of $\alpha_S(m_Z)$





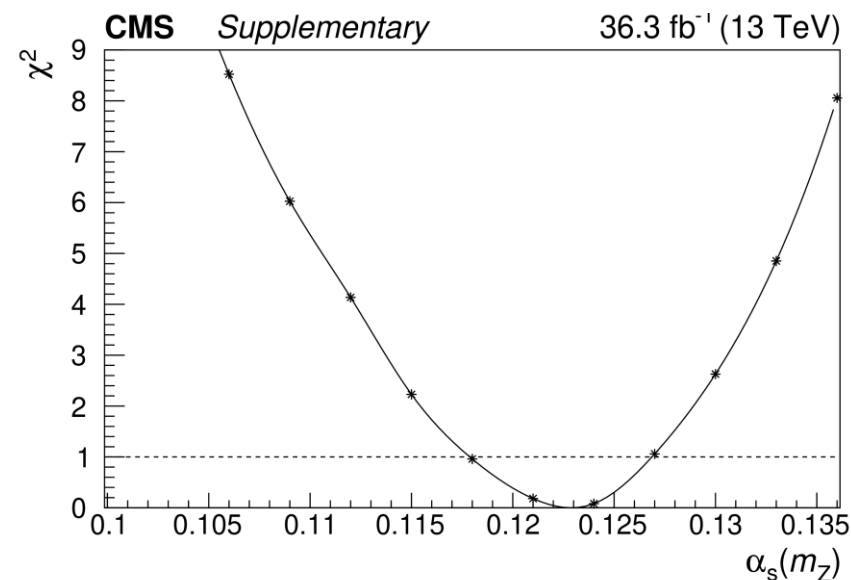
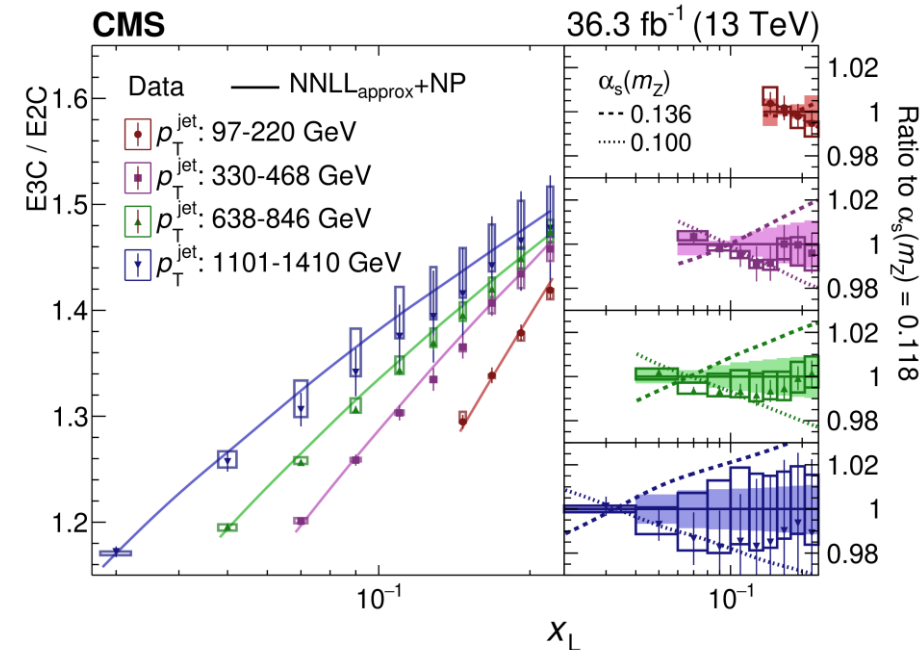
E3C/E2C: Precision extraction of α_s

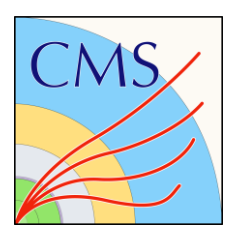
[arXiv:2402.13864](https://arxiv.org/abs/2402.13864)

- Direct extraction of coupling from E3C/E2C vs. x_L (pert. regime, $x_L < 0.234$)
- Extraction using comparisons with theoretical predictions at NLO+NNLL_{approx} for variations of $\alpha_s(m_Z)$
 - minimize χ^2 between measurement and prediction using total covariance
 - nuisance parameter for unknown per- p_T bin theory normalization in
 - nuisance parameters simultaneously varied, PS renormalization scale unc. replaced by those for NNLL_{approx} predictions

$$\alpha_s(m_Z) = 0.1229^{+0.0040(\text{stat.})+0.0030(\text{th.})+0.0023(\text{exp.})}_{-0.0012(\text{stat.})-0.0033(\text{th.})-0.0036(\text{exp.})}$$

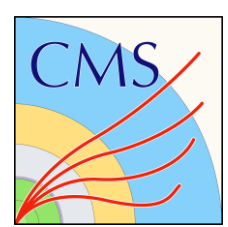
- Uncertainties $\sim 4\%$: most precise extraction of α_s leveraging jet substructure
- Leading systematics: QCD scale for NLO+NNLL_{approx} prediction, neutral hadron and photon energy scale
- ⇒ expect reduction of uncertainties when using charged particle only



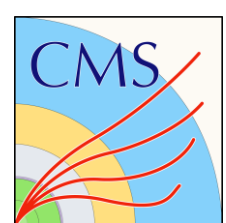


Summary

- Precision measurements of per-jet, multi-entry substructure observables:
 - sensitivity to fundamental QCD mechanisms over a large range of energy scales
 - comparisons to perturbative, higher-order QCD calculations for jet substructure
- Factorisation of effects of QCD phenomena for phase space of emissions in a jet with single observable:
using iterative declustering, extensive set of **handles to constrain parton showers and analytic predictions**
- Direct sensitivity to time evolution of shower, scaling behaviour of QCD, with objects grounded in field-theory:
observation of **confinement, asymptotic freedom** and **extraction of $\alpha_S(m_Z)$** from multi-particle correlations
- **MC model uncertainties dominant in jet substructure measurements:**
 - provide complementary handles for benchmarking and constraining event generators, parton shower and hadronization models in well factorized measurements



BACKUP SLIDES



Primary Lund jet plane density

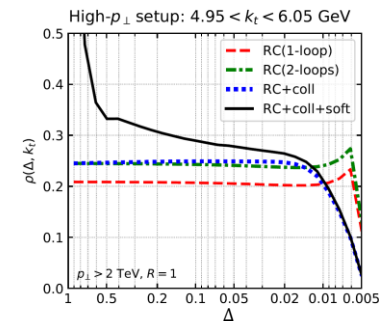
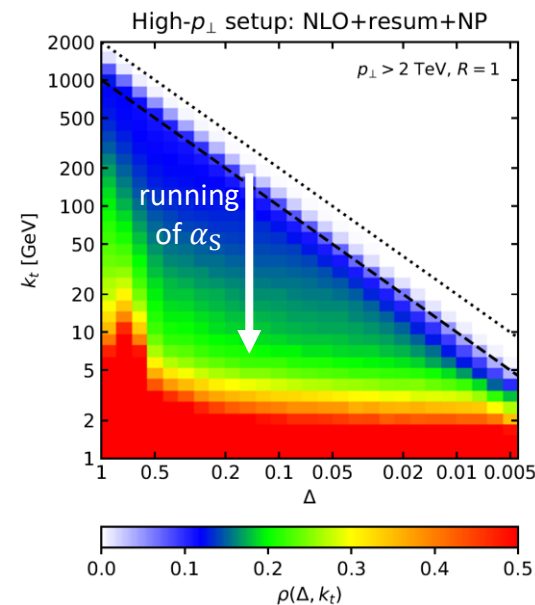
- Jet-averaged density (ρ) of 1 \rightarrow 2 splittings in the Lund plane
 - \rightarrow calculable in perturbative QCD, where at leading order, in soft and collinear limit, density scales with coupling,

$$\rho(\Delta R, k_T) = \frac{1}{N_{\text{jets}}} \frac{d^2 N_{\text{emissions}}}{d \ln(k_T / \text{GeV}) d \ln(R/\Delta R)} \approx \frac{2}{\pi} C_i \alpha_S(k_T),$$

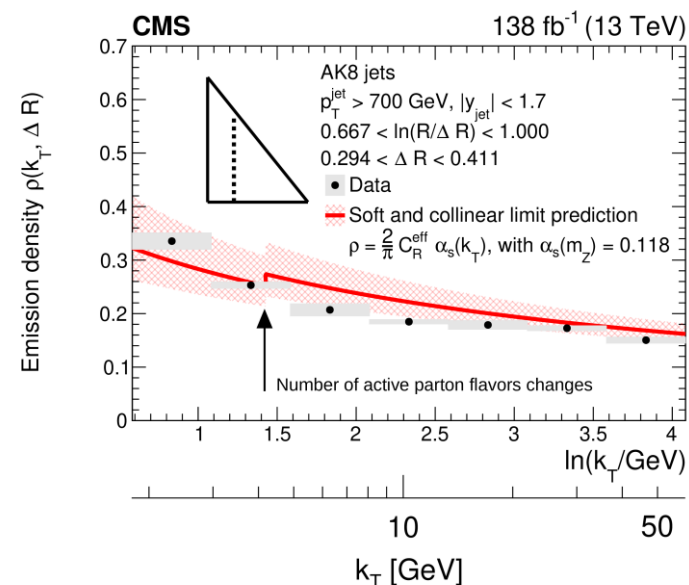
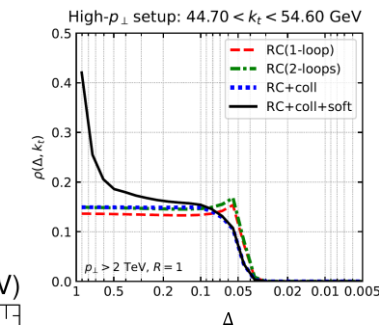
C_i : Casimir for quarks ($C_F = 4/3$) and gluons ($C_A = 3$)

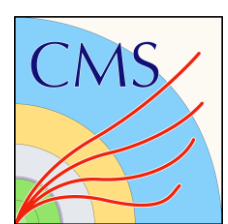
$$\alpha_S \propto \frac{1}{\ln\left(\frac{k_T}{\Lambda_{QCD}}\right)} \Rightarrow \sim \text{uniform } \rho \text{ at high } k_T, \rho \uparrow \text{ at low } k_T \text{ as } \alpha_S \gg 1$$

- Broad features of unfolded LJP density described well in soft and collinear limit,
 - \rightarrow simplified assumptions: 1-loop β function with $\alpha_S(m_Z) = 0.118$,
 - \rightarrow effective color factor $C_R = 0.59 C_F + 0.41 C_A \approx 2$ (from MC q/g fractions)



A. Lifson, G. Salam, G. Soyez, [JHEP 10 \(2020\) 170](#)

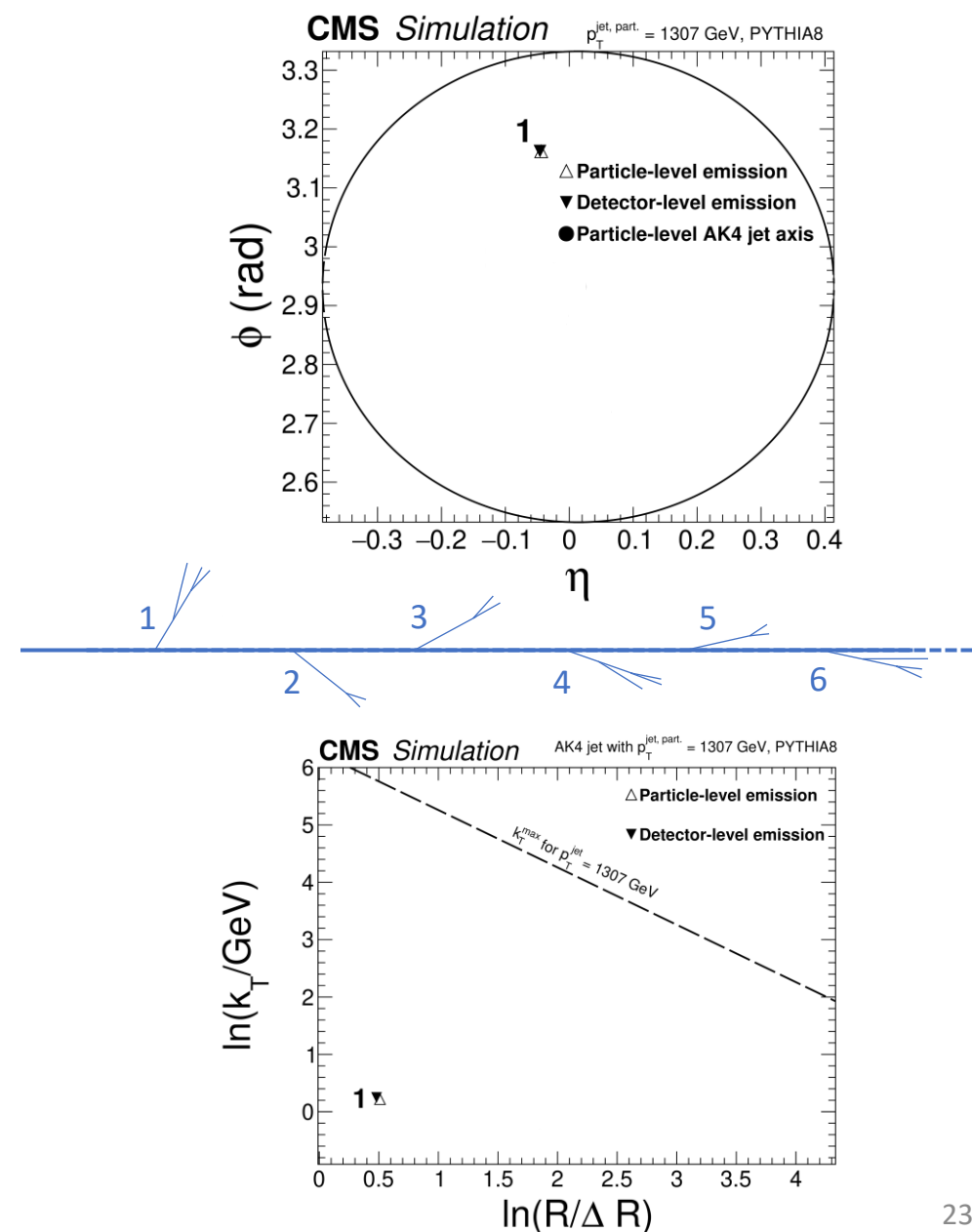


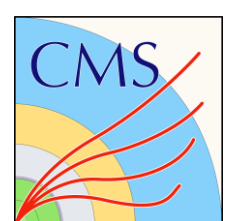


LJP: Unfolding and corrections

[JHEP 05 \(2024\) 116](#)

- Migration matrix for unfolding with geometric matching of detector- and truth-level jets and matching of emissions
 - match detector- and particle-level splittings in **PYTHIA8 CP5**;
choose closest in $\eta - \phi, \forall \Delta R(\Delta, \blacktriangledown) < 0.1$ for multiple matches
 - **background** (bin-by-bin) subtraction of unmatched detector-level emissions estimated in MC (**purity** corrections)

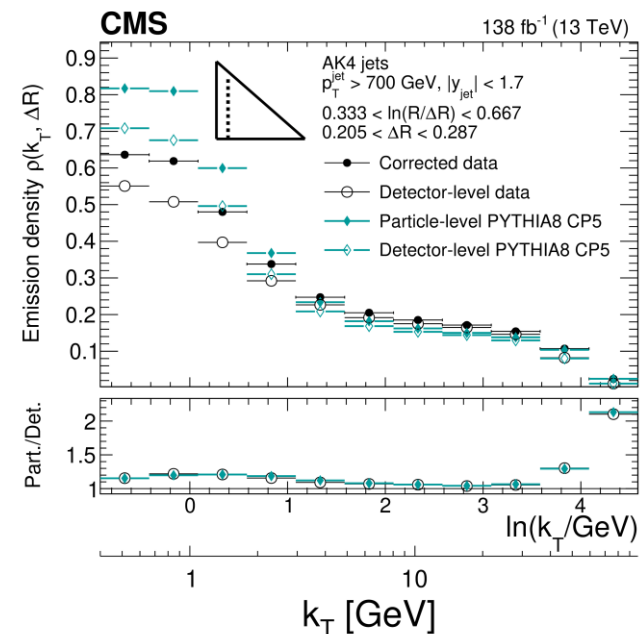
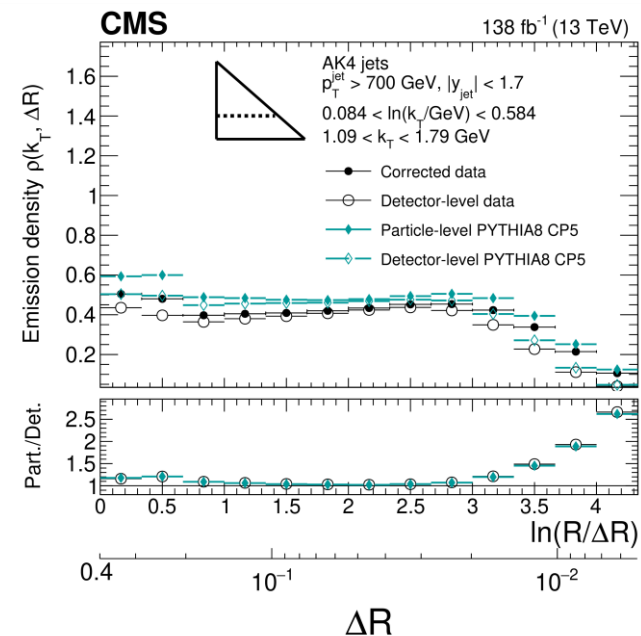


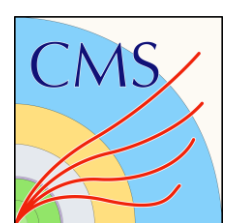


LJP: Unfolding and corrections

JHEP 05 (2024) 116

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 - **background** (bin-by-bin) subtraction of unmatched detector-level emissions estimated in MC (**purity** corrections)
- Primary LJP density **unfolded multidimensionally** ($p_{T,jet}, k_T, \Delta R$)
 - Multi-entry distribution, bin-to-bin statistical correlations: **5 – 10%**
 - **regularized D'Agostini unfolding**: minimise χ^2 between input and forward-folded unfolded distribution: 12(**8**) iterations for $R=0.4$ (**0.8**)
 - **correction** to N_{jets} for migrations between detector-/generator-level anti- k_T jet p_T ,
 - **efficiency** corrections (bin-by-bin) for unmatched hadron-level emissions in MC





LJP: Unfolding and corrections

JHEP 05 (2024) 116

- Migration matrix for unfolding geometric matching of detector- and truth-level jets, and the matching of emissions

→ match detector- and particle-level descriptions of splittings in nominal MC

(PYTHIA8 CP5): choose closest in $\eta - \phi, \forall \Delta R(\Delta, \nabla) < 0.1$

→ **background (bin-by-bin)** subtraction of unmatched detector-level emissions estimated in MC (**purity** corrections)

- Primary LJP measurements **unfolded multidimensionally** in $(p_{T,jet}, k_T, \Delta R)$

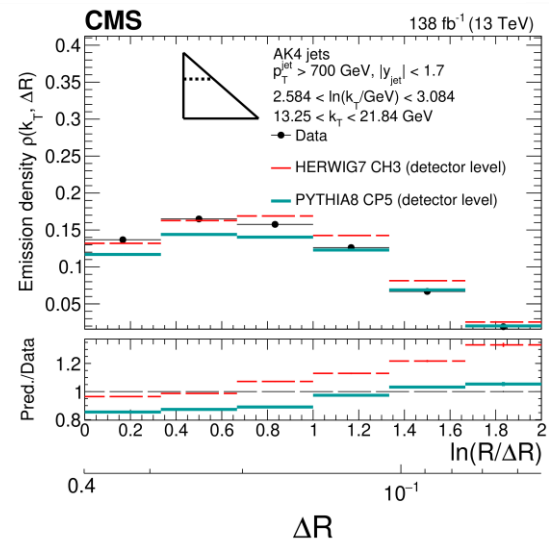
→ bin-to-bin stat. correlations: 5 – 10%

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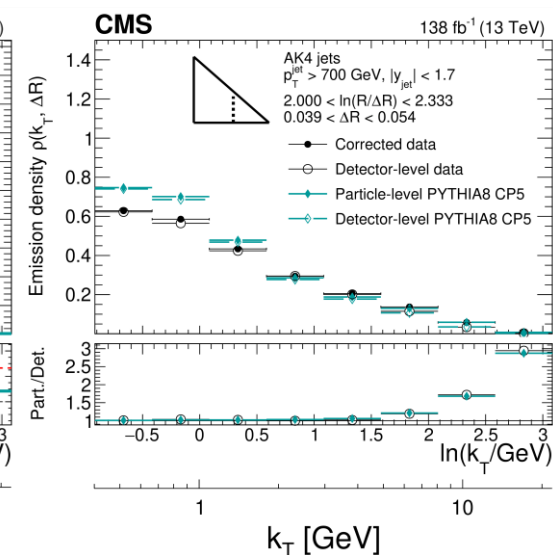
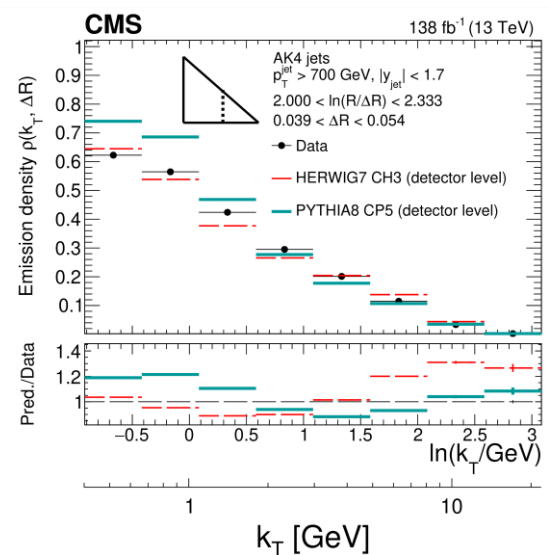
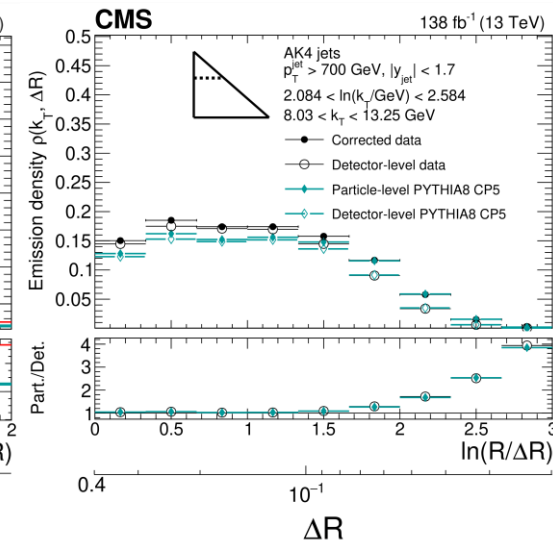
→ correction to N_{jets} for migrations between det./gen.-level anti- k_T jet p_T

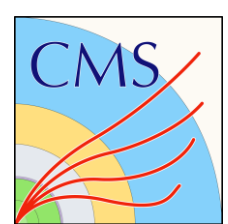
→ **efficiency** corrections (bin-by-bin) for unmatched hadron-level emissions in MC

Detector level



Particle level





LJP: Unfolding uncertainties

JHEP 05 (2024) 116

- Leading contributions

- parton shower + hadronization model uncertainty (dominant in bulk):

decorrelated MC prior and response matrix stat. contributions in regularized unf.

swap in HERWIG7 CH3 predictions for the prior/matrix from PYTHIA8 CP5;

2–7% contribution in bulk, ~20% at kinematic edge of LJP

- tracking efficiency uncertainty (dominant at high k_T):

1-2% contribution in bulk, 15–25% at kinematic edge of LJP/in pert. region;

includes contributions from losing subjets to cluster merging at $\Delta R \sim 0.05$

and (at low $k_T, \Delta R$) $p_T > 1$ GeV requirement for PF cand.

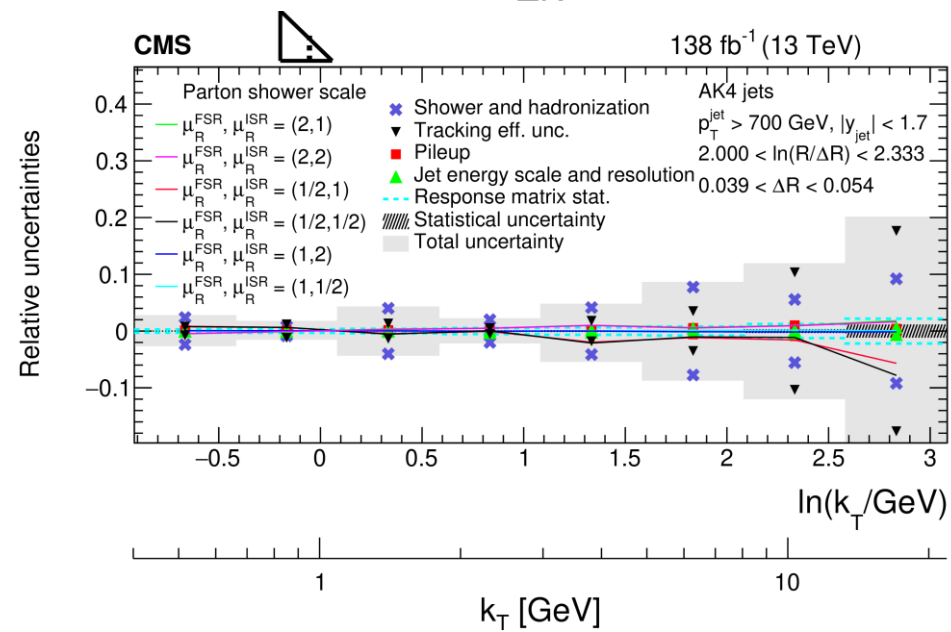
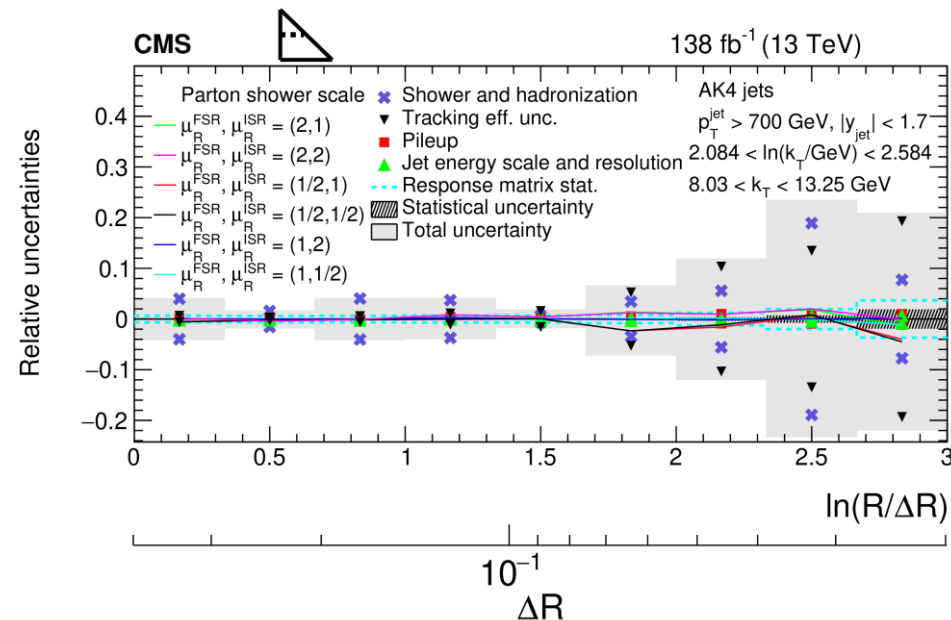
- Sub-percent contributions

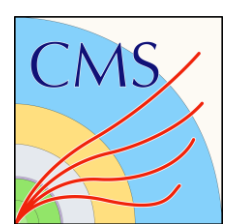
- parton shower scale

- finite statistics of the response matrix

- (global) jet energy scale and resolution

- pileup modeling





LJP: Unfolding uncertainties

JHEP 05 (2024) 116

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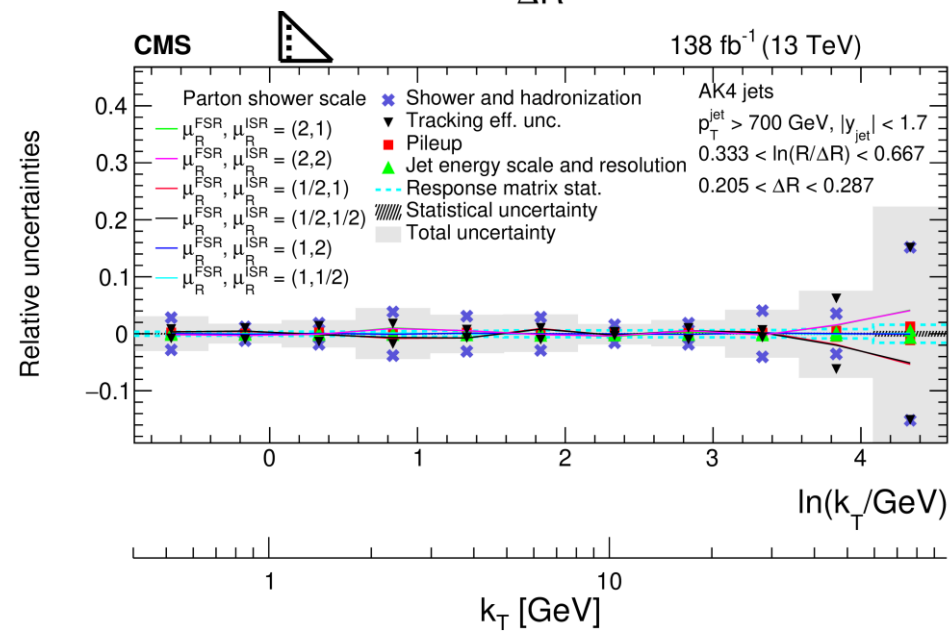
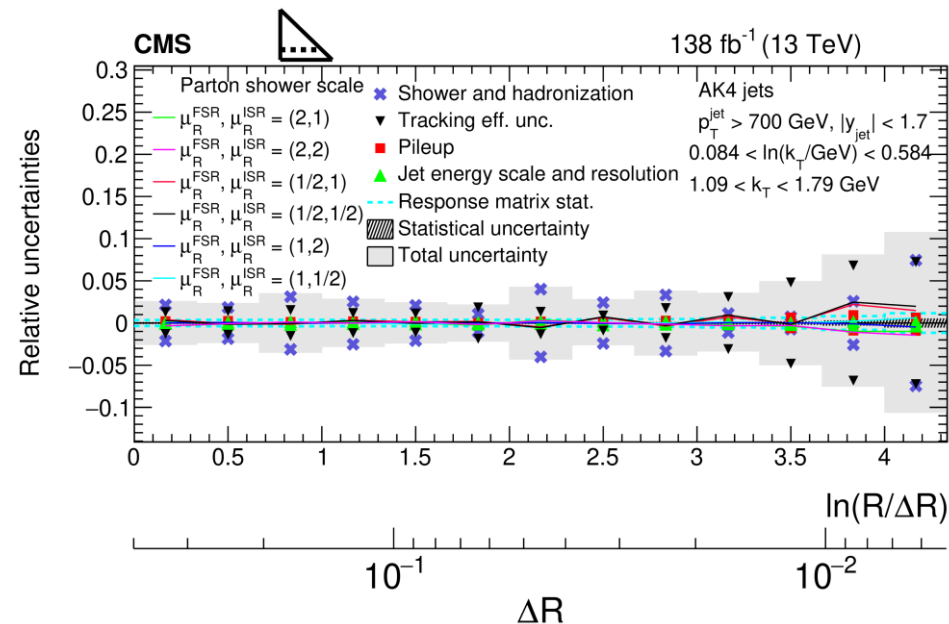
- **Sub-percent contributions**

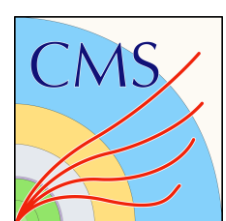
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- (global) **jet energy scale and resolution**

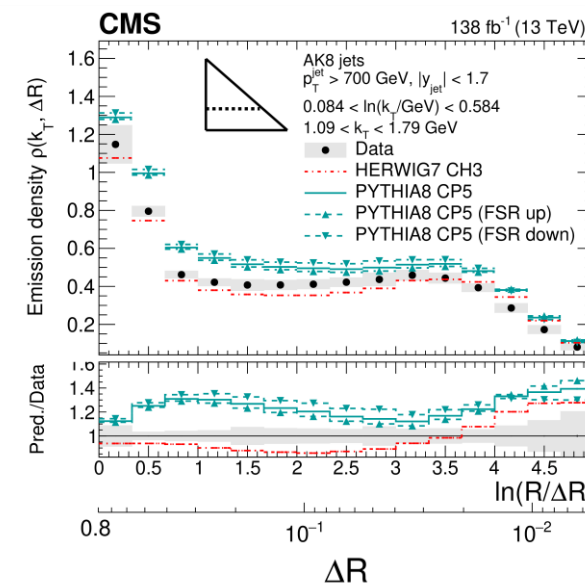
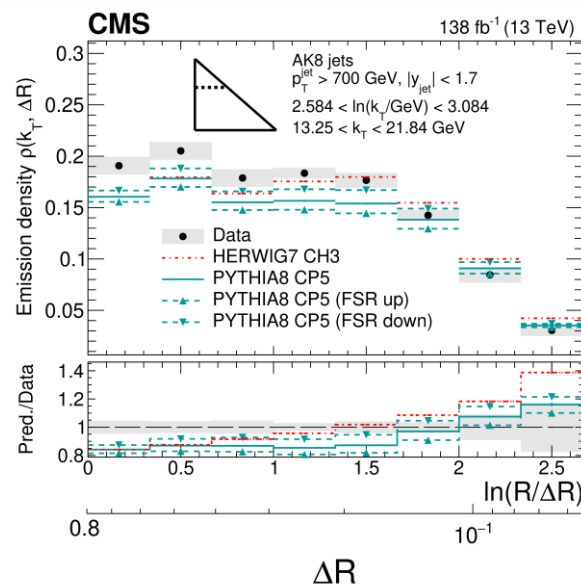
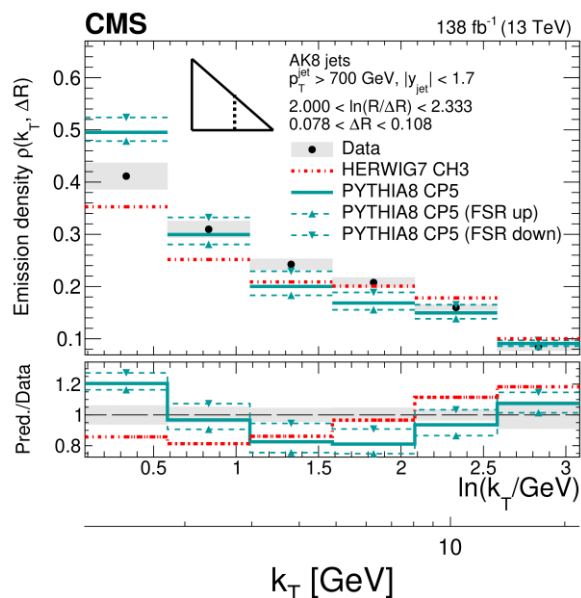
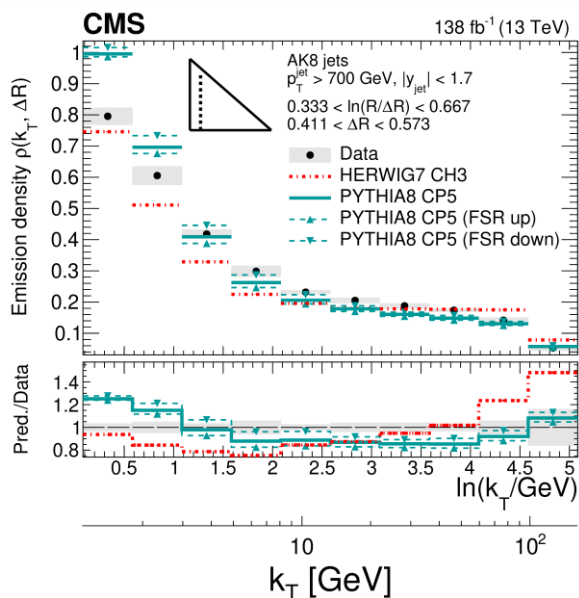
- **pileup modeling**





LJP: Constraining α_S^{FSR}

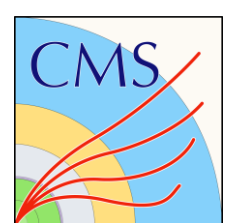
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- Comparison of **PYTHIA8 CP5** and **HERWIG7 CH3** to data:
 - differences: **PYTHIA8 CP5** 15–20%, **HERWIG7 CH3** 5–10%
 - neither describe data well in every region of the LJP
 - shapes of distributions similar for AK8 and AK4 jets

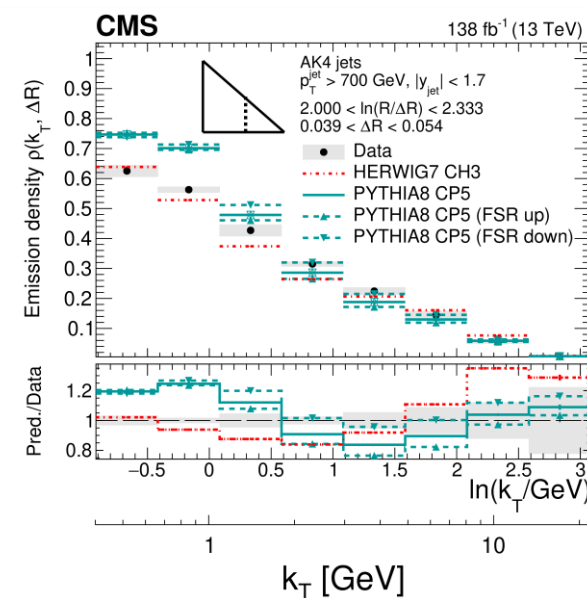
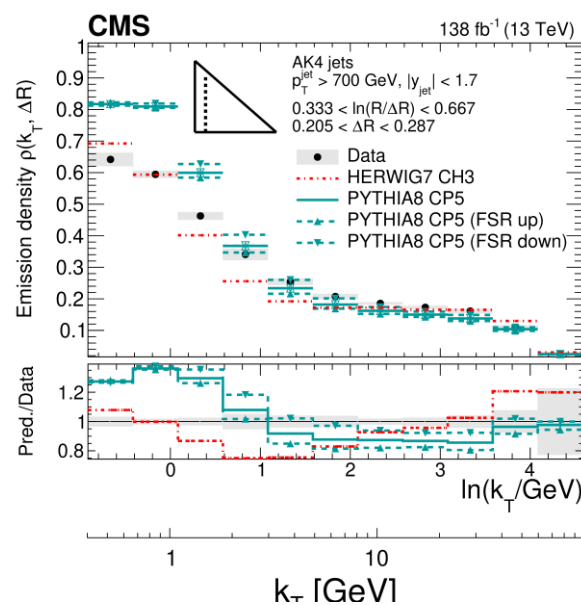
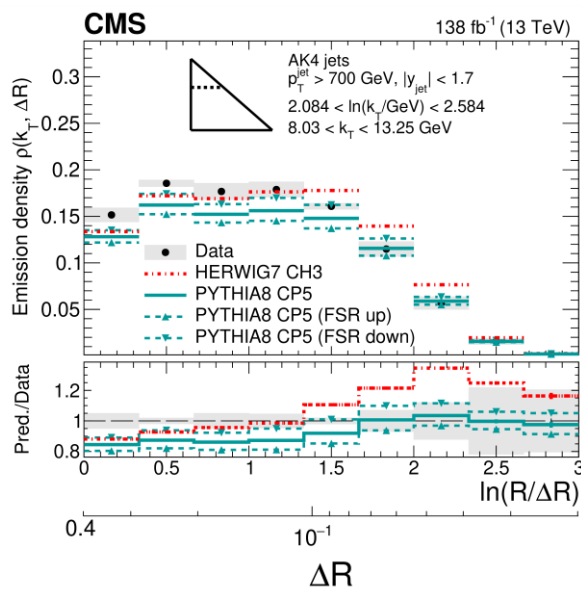
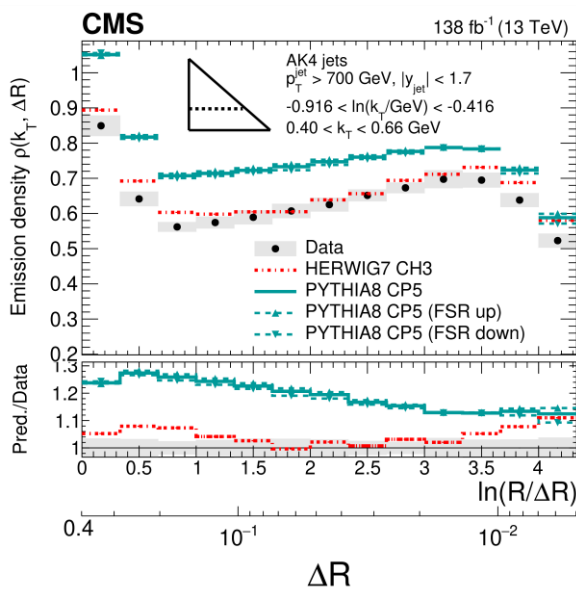
- LJP density linearly dependent on $\alpha_S^{\text{FSR}}(m_Z)$:
 - sensitive to choice of renormalization scale
 - ~10% band in perturbative region, shrinks at low k_T
 - higher $\alpha_S^{\text{FSR}}(m_Z)$ (FSR down) preferred at higher k_T

Missing NLO corrections in QCD branchings more relevant
 at high p_T where the shower evolves for longer



LJP: Constraining α_S^{FSR} (AK4)

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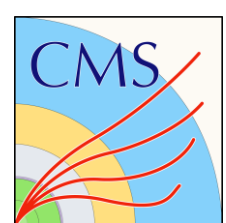


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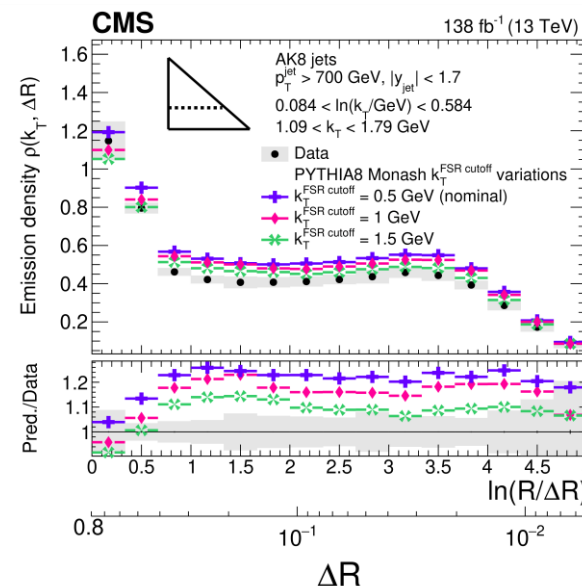
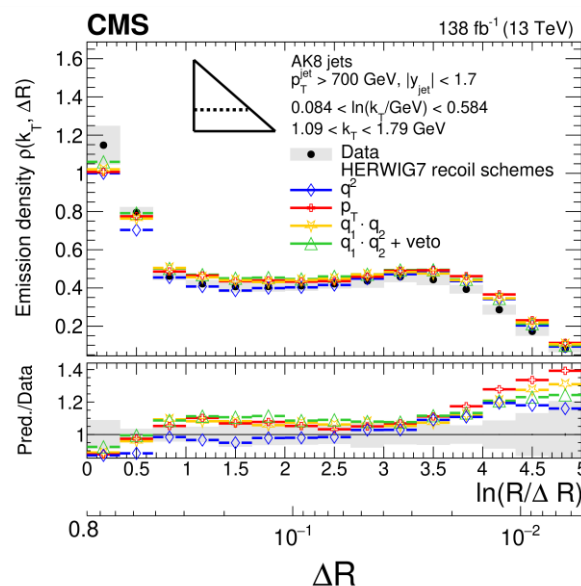
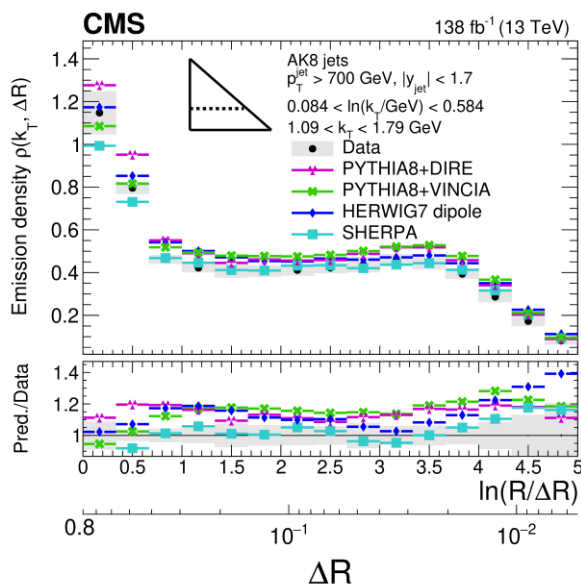
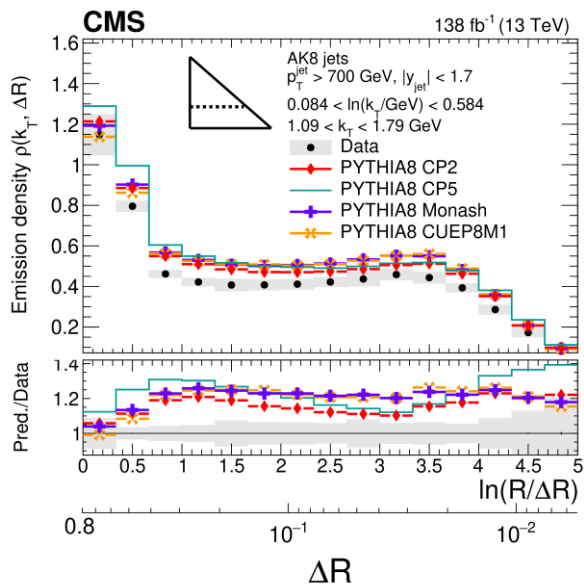
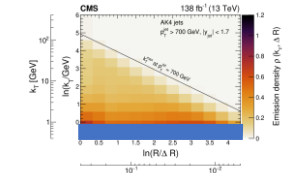
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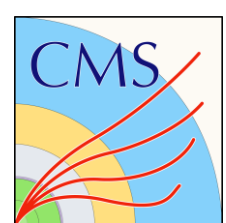
LJP: PS models and UE tunes at low k_T

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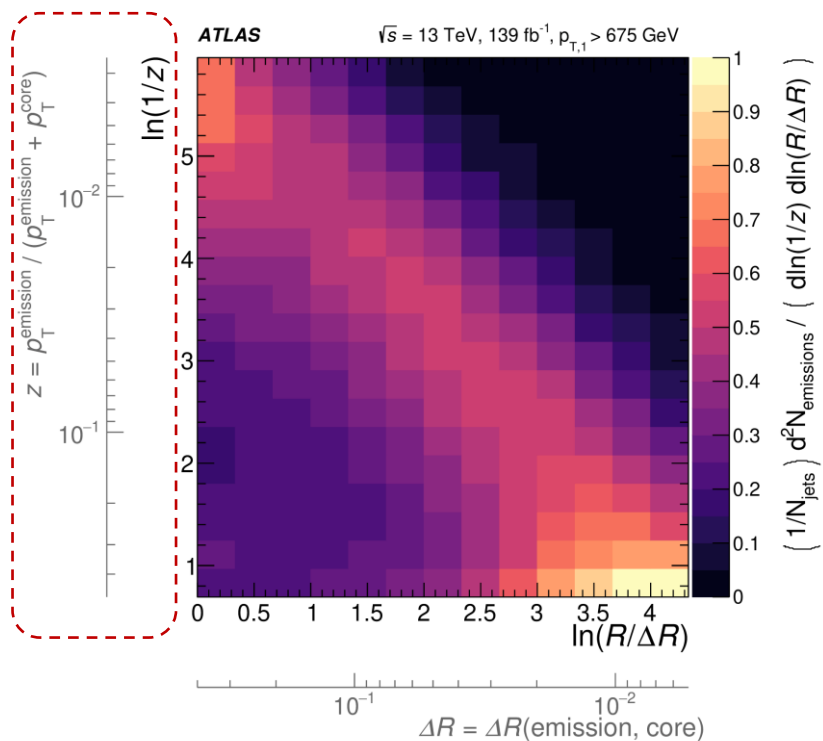


- At low k_T (dominated by hadronization and MPI contributions):
 - **PYTHIA8** tunes: higher values of $\alpha_S^{\text{FSR}}(m_Z)$ preferred, less so than in bulk
 - dipole shower models: **HERWIG7**, **SHERPA** (cluster fragmentation)
 - in better agreement than PYTHIA (Lund string fragmentation)
 - angle-ordered Herwig7.2 recoil schemes: q^2 best in non-pert. region
 - variations of k_T cutoff in **Monash** tune: larger k_T^{FSR} preferred

- **PYTHIA** consistently overshoots data at low k_T irrespective of showering variations, renormalization scale choices (see backups)
- Generally, larger k_T^{FSR} to terminate FSR evolution more compatible with data across MCs (e.g., **HERWIG7** and **SHERPA** $k_T^{\text{FSR}} = 1$ GeV)

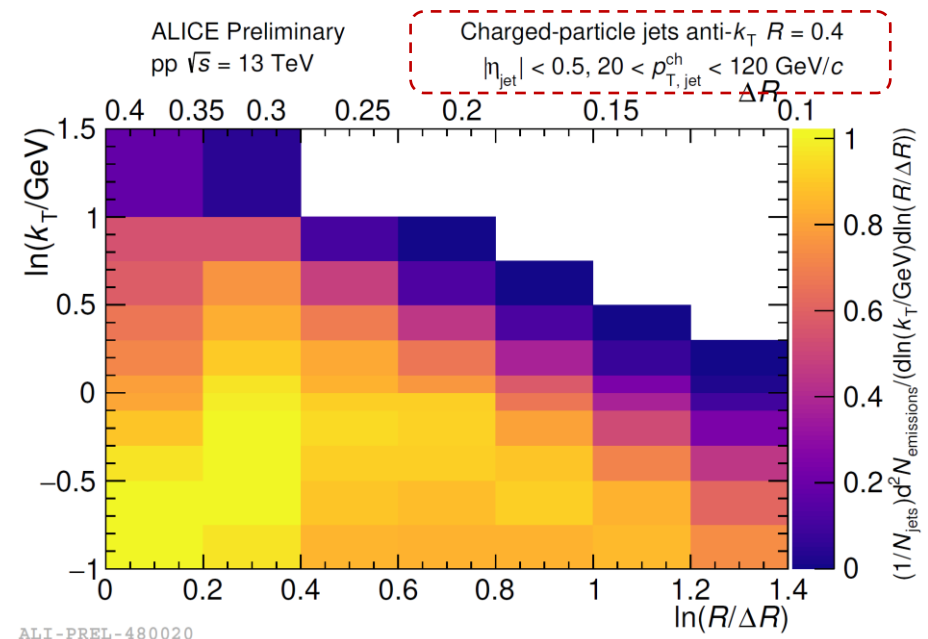
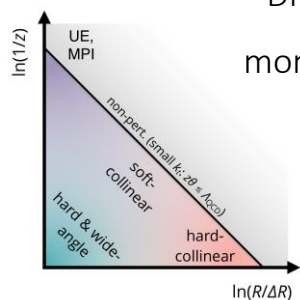


LJP: ATLAS & ALICE measurements

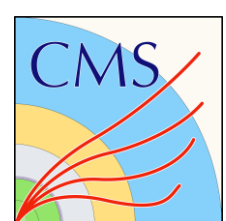


Different representation to CMS measurement, using momentum fraction $\ln(1/z)$ of emissions instead of k_T :

$$z = \frac{p_{T,\text{softer}}}{p_{T,\text{softer}} + p_{T,\text{harder}}}$$



Different range of measurement, $20 < p_{T,\text{jet}} < 120 \text{ GeV}$;
 probing mostly the wide-angle region, using low- k_T
 splittings in small radius ($R=0.4$) jets,

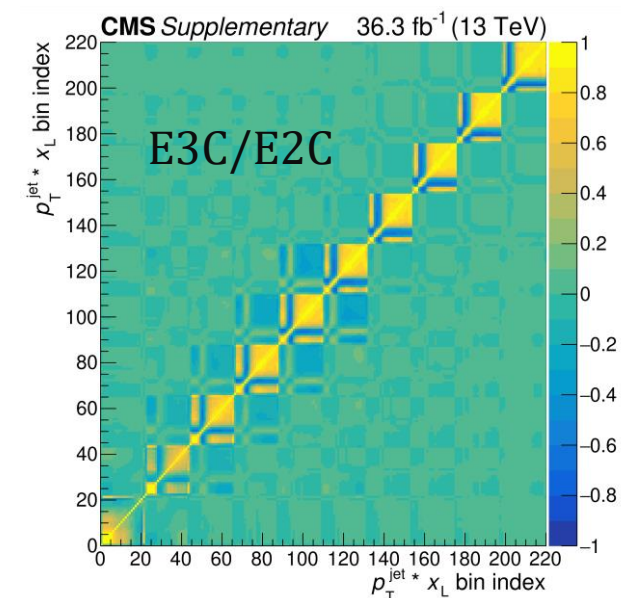
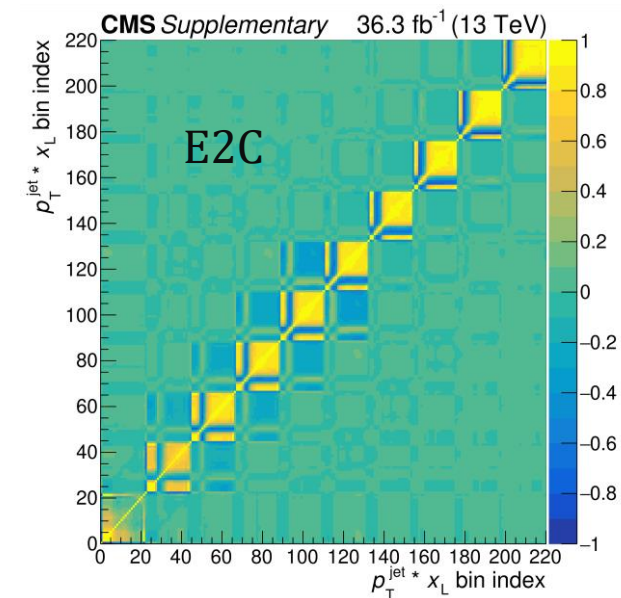


EnCs: Unfolding and corrections

[CERN-EP-2024-010](#)

- Migration matrix for unfolding requires geometric matching of detector- and generator-level jets ($\Delta R < 0.2$) and (PF) particles
 - uniquely matched at detector- and truth-level descriptions in nominal MC (PYTHIA8 CP5); mutually closest in plane of $\eta - \phi, \forall \Delta R(\Delta, \nabla) < 0.05$
 - jet matching efficiency: $> 99\%$
 - **purity correction (bin-by-bin fake subtraction)** for unmatched MC detector-level particles

- Measurements unfolded multidimensionally in $\left(p_{T,\text{jet}}, x_L, \overbrace{\frac{\prod_{a=1}^N E_{i_a}}{E^N}}^{\text{energy weight}} \right) [(8 + 2) \cdot (20 + 2) \cdot 20 \text{ bins}]$
 - multi-count observables, and two leading jets in event used \Rightarrow large (upto 40%) statistical correlations between x_L and p_T bins, track both in input covariance matrices
 - halve data being unfolded for EnC's, statistically decorrelated E2C and E3C unfolding
 - **iterative Bayesian unfolding (D'Agostini)**: 7 iterations until p-value > 0.05
 - **efficiency (bin-by-bin)** correction for counts of unmatched particle-level objects

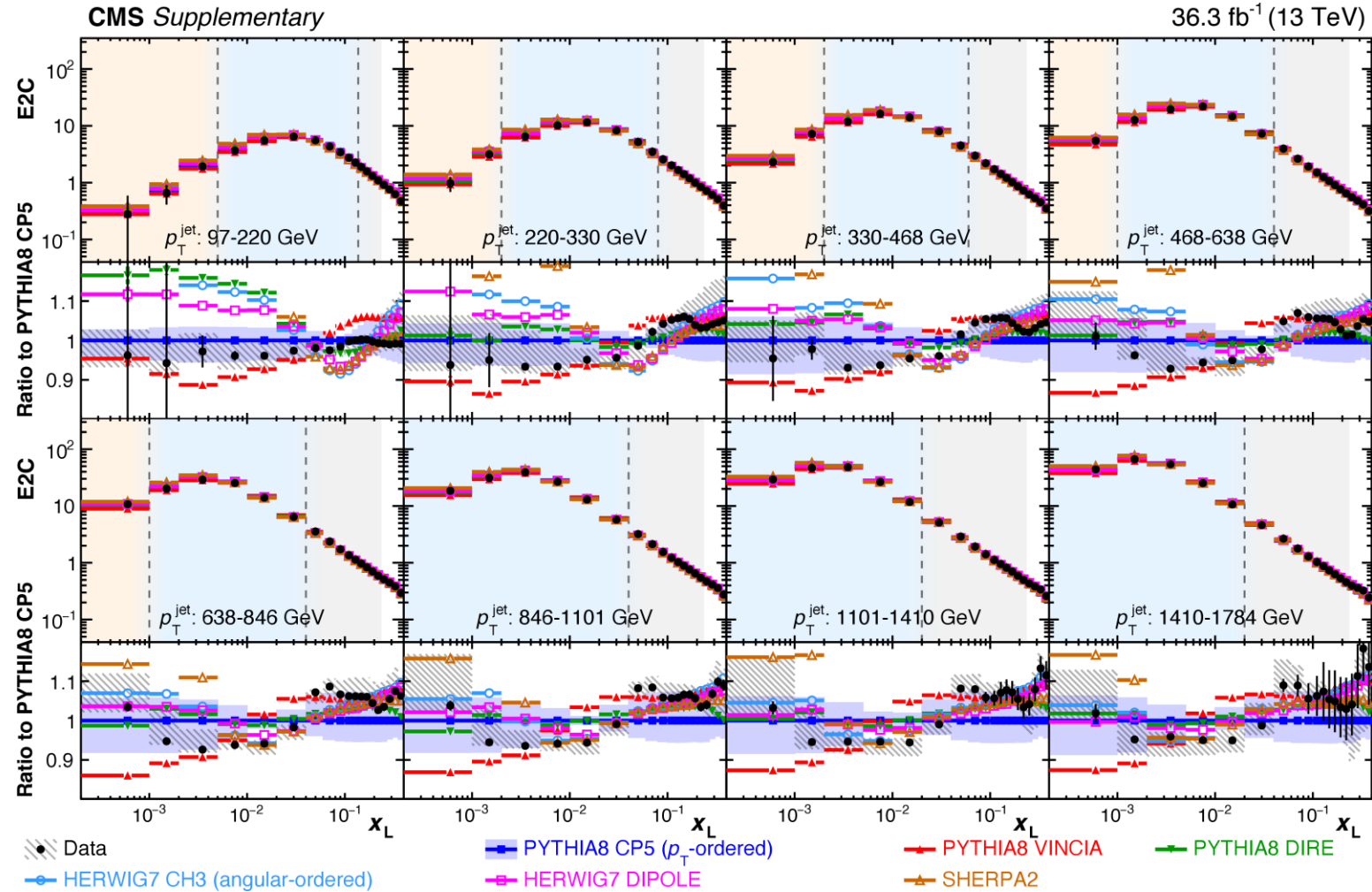


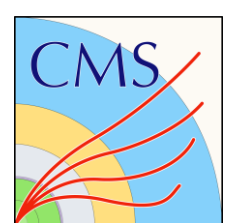


E2C: Unfolded measurements & uncertainties

CERN-EP-2024-010

- Data are compared to various parton shower models,
 - no one model to describe them all (across p_T bins)
 - $\sim 10 - 15\%$ disagreement generally, similar to the primary LJP density measurement
- Leading contributions to uncertainties:
 - shower and model uncertainties: $2 - 10\%$
 - neutral hadron energy scale: $1 - 2\%$
- Systematic contributions considered:
 - photon and charged/neutral hadron energy scale
 - (global) jet energy scale and resolution
 - PU, tracking efficiency, trigger preflring
 - QCD scale in parton shower and in hard scattering
 - Underlying event tune, parton shower tunes
 - PDF variations



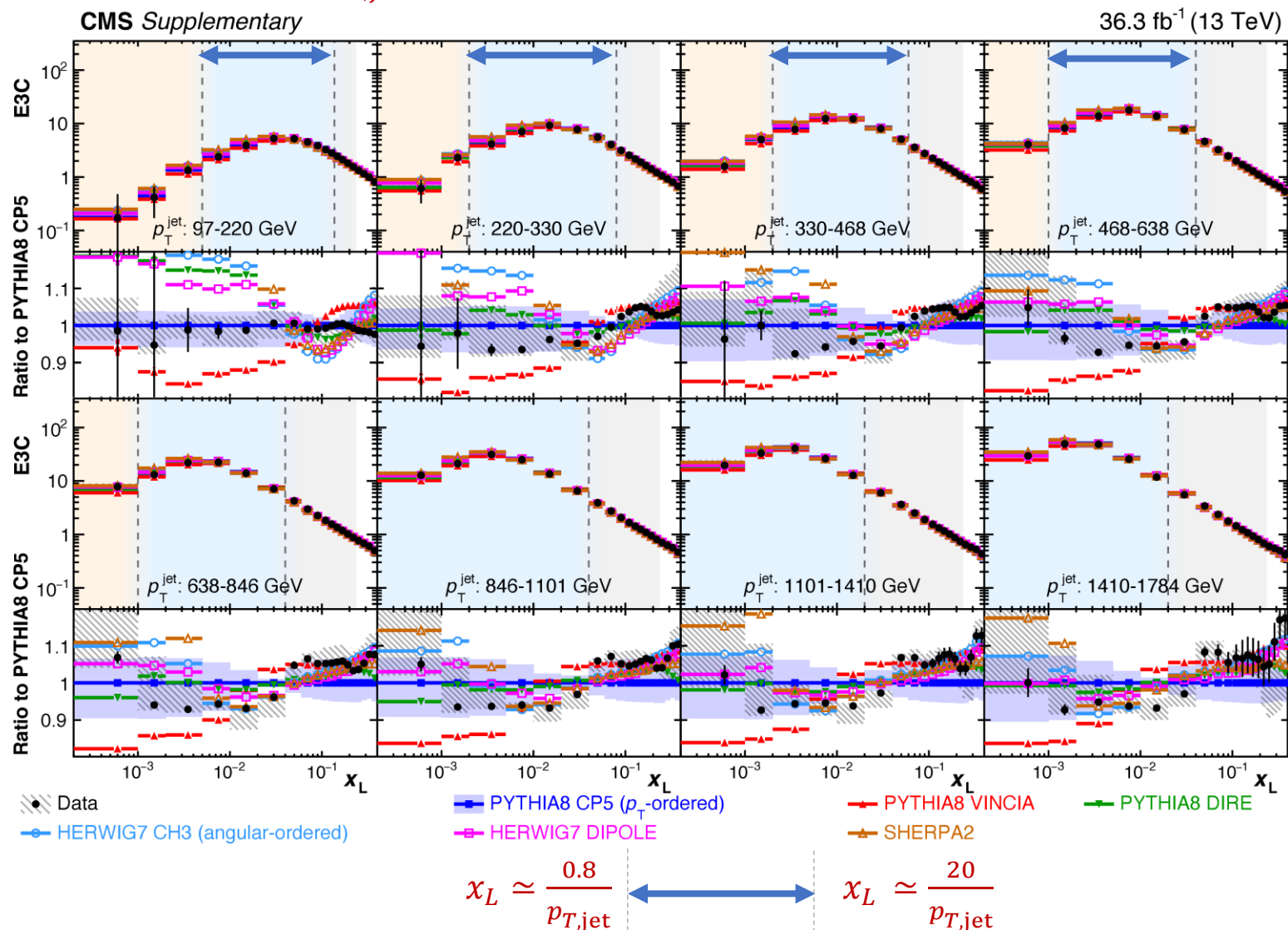


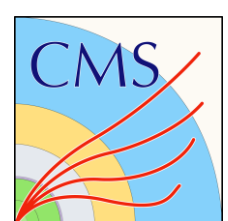
E3C: Unfolded measurements

CERN-EP-2024-010

$Q \propto x_L \cdot p_{T,jet}$: Boundaries between regions shift to smaller x_L at high p_T

- No one model to describe them all (across p_T bins)
 → ~ 10 – 20% disagreement generally, similar to the primary LJP measurement
- Leading contributions to uncertainties:
 → shower and model uncertainties: 2 – 10%
 → neutral particle energy scale: 1 – 2%



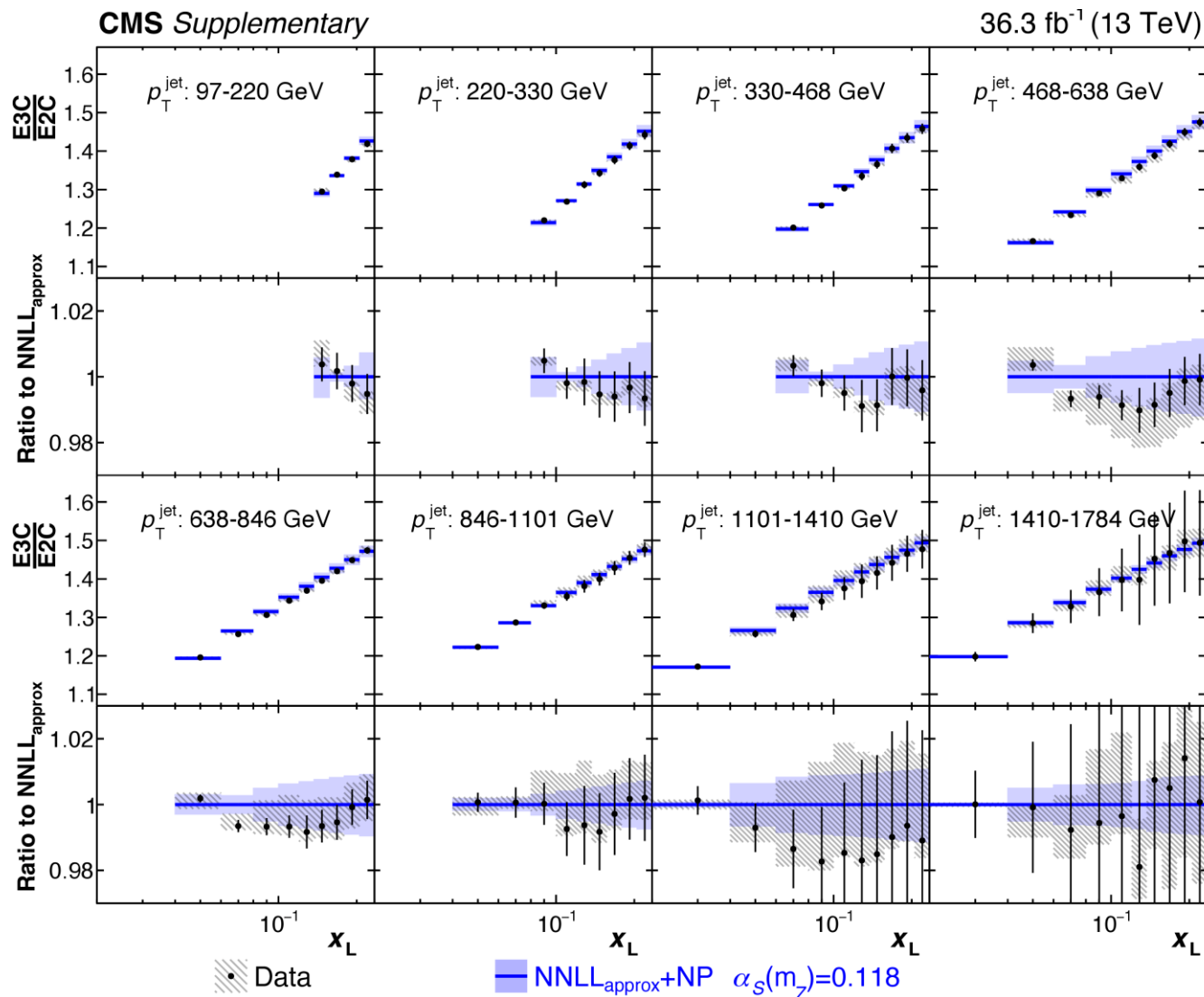


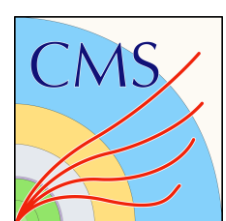
E3C/E2C: Comparisons to $\text{NLO}+\text{NNLL}_{\text{approx}}$

CERN-EP-2024-010

W. Chen, J. Gao, Y. Li, Z. Xu, X. Zhang,
HX. Zhu; [JHEP 05 \(2024\) 043](#)

- Bin-by-bin hadronization factor applied to $\text{NLO}+\text{NNLL}_{\text{approx}}$ calculations to match to unfolded hadron-level measurement
 - account for $p_T > 1$ GeV threshold for hadrons, averaged hadron/parton level distributions in PYTHIA and HERWIG
 - corrections 5-40% for E2C, E3C and 0-3% in ratio
- Data shapes agree well with calculations
- Theory systematics
 - QCD scale of $\text{NNLL}_{\text{approx}}$ predictions and of hard scattering
 - hadronisation factors, UE/PS modeling, PDF uncertainties





D'Agostini unfolding

- Iterative, unfolding with a stopping criterion over steps t , number of iterations \leftrightarrow level of regularisation

$$\lambda_j^{(t+1)} = \lambda_j^{(t)} \frac{\sum_{i=1}^n R_{i,j} v_{obs,i}}{\sum_{k=1}^n R_{i,k} \lambda_k^{(t)}} ; \text{ input prior (MC): } \lambda^{(0)} = \lambda^{MC} (v_{obs, MC})$$

- χ^2 -test in smeared space:

→ test compatibility of unfolded particle-level distribution, folded back to detector level

$$\text{minimize: } \chi^2 = (\vec{v}_{observed} - \vec{v}_{folded}) V_{(stat. \text{ only})}^{-1} (\vec{v}_{observed} - \vec{v}_{folded})$$

→ stop when folded and input (data-bkg.) distributions are statistically compatible ($p > 0.05$)

- **LJP measurement:** Decorrelating shower and hadronization uncertainties by uncorrelated variations of response matrix and input prior from nominal and alternate MCs: **PYTHIA8 CP5** and **HERWIG7 CH3**;
take the difference between unfoldings with nominal RM+MC prior (**PYTHIA8+PYTHIA8**) and alternates: (**PYTHIA8+ HERWIG7**), (**HERWIG7 +PYTHIA8**)
→ estimate **uncorrelated** systematic from symmetrized variations of shifts of alternate unfoldings