

# High-purity gluon jet showers using secondary Lund jet planes

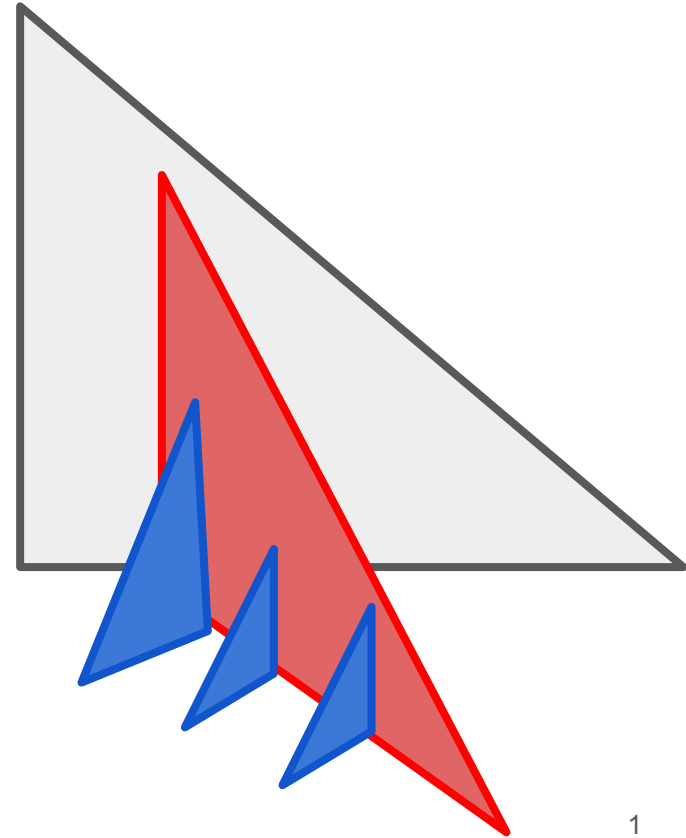
*[work in progress results]*

**Cristian Baldenegro,**  
with Alba Soto-Ontoso, Gregory Soyez

**BOOST 2024 @ Genoa, Italy**  
July 29th–August 2nd

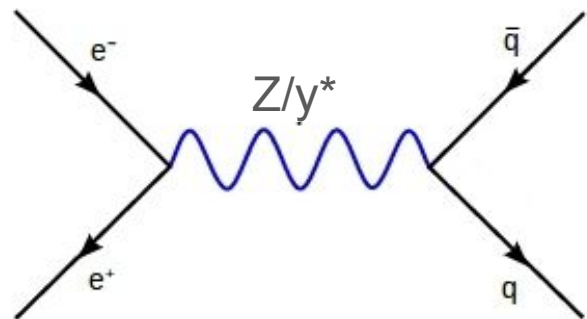


**SAPIENZA**  
UNIVERSITÀ DI ROMA

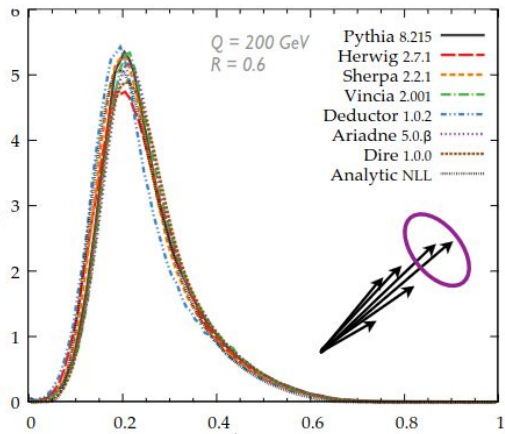


# Some context:

“Quark jet showers strongly constrained at LEP,  
gluon jet showers not as much”



$e^+e^- \rightarrow$  quarks ( $C_F = 4/3$ )

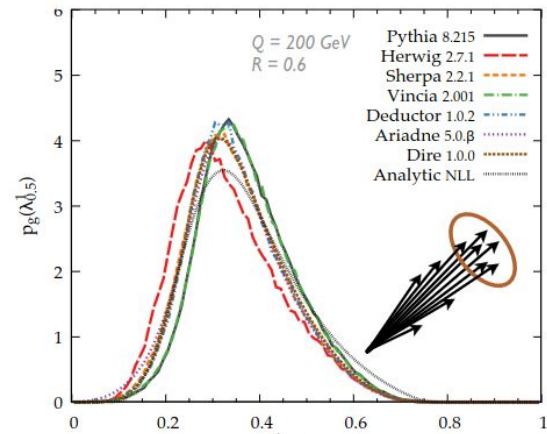


$$\text{LHA} = \sum_i z_i \sqrt{\theta_i}$$

**Smaller** spread among  
quark jet

**LEP constraints**

VS.  $e^+e^- \rightarrow$  gluons ( $C_A = 3$ )



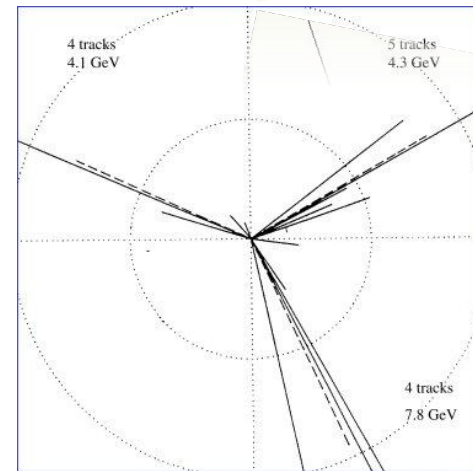
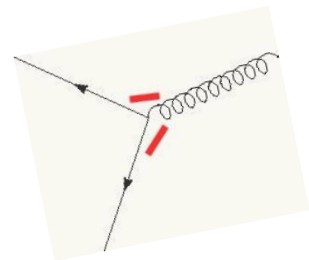
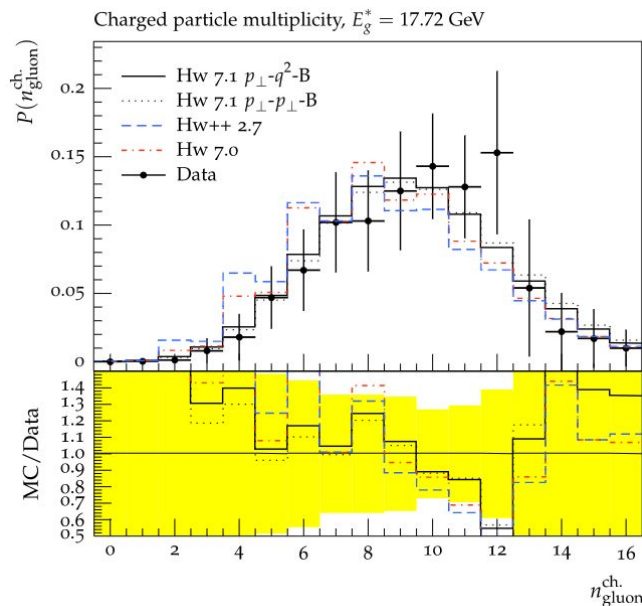
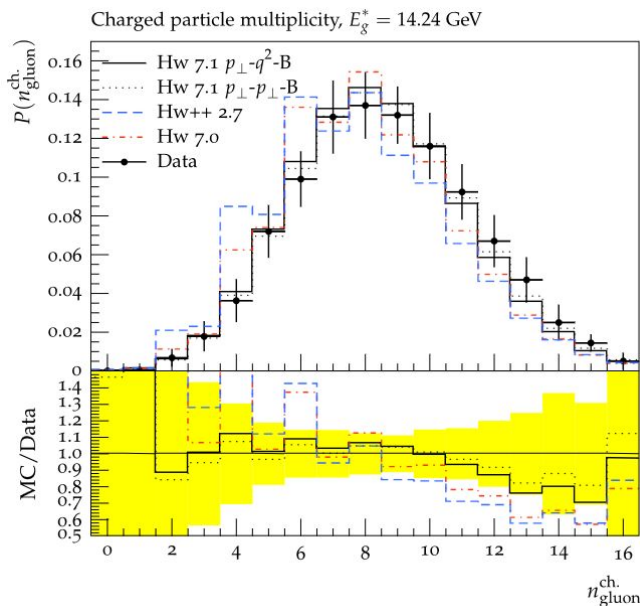
$$\text{LHA} = \sum_i z_i \sqrt{\theta_i}$$

**Larger** spread  
for gluon jets

**no LEP constraints!**

# Gluon-rich jet samples at LEP ( $e^+e^- \rightarrow bbg$ )

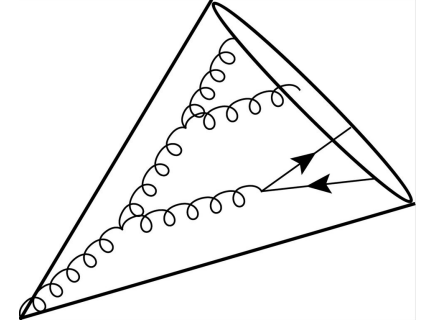
Data used in [Herwig7.2 tuning](#) (post Les Houches 2015)



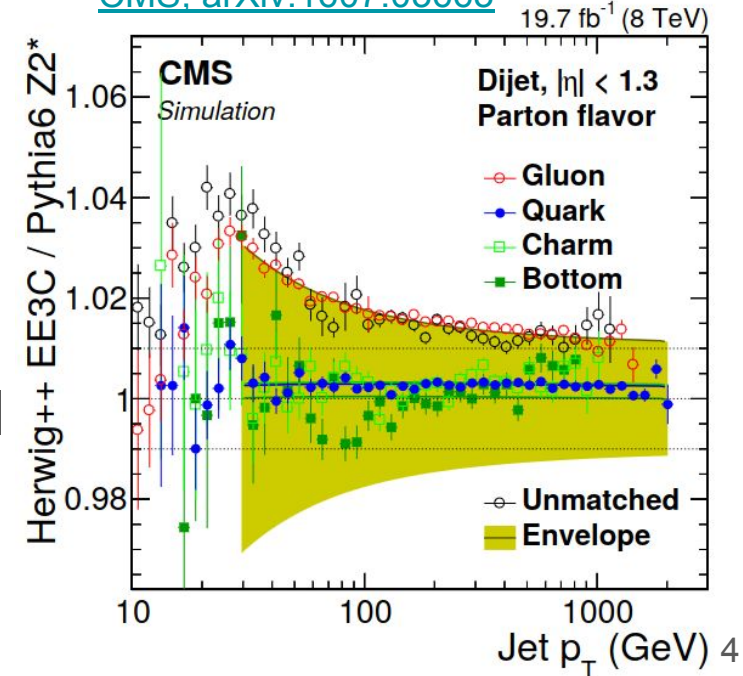
$n^{\text{ch}}$  of soft gluon jets ( $E_T \sim 14-18$  GeV), uncertainties of  $\sim 30-40\%$   
Otherwise, no other "pure" gluon jet samples available for MC tuning

# Why gluon jet radiation?

- Understand gluon radiation patterns
- Improve “vacuum” baseline for jet quenching MCs
- Reduce jet energy calibration uncertainties, affects all jet measurements at the LHC (e.g., **gluon jet response between Herwig7 vs Pythia8 in CMS\***)
- To reduce MC-biases in quark vs gluon discriminators



[CMS, arXiv:1607.03663](https://arxiv.org/abs/1607.03663)



**Challenging to isolate gluon jets at a hadron collider**

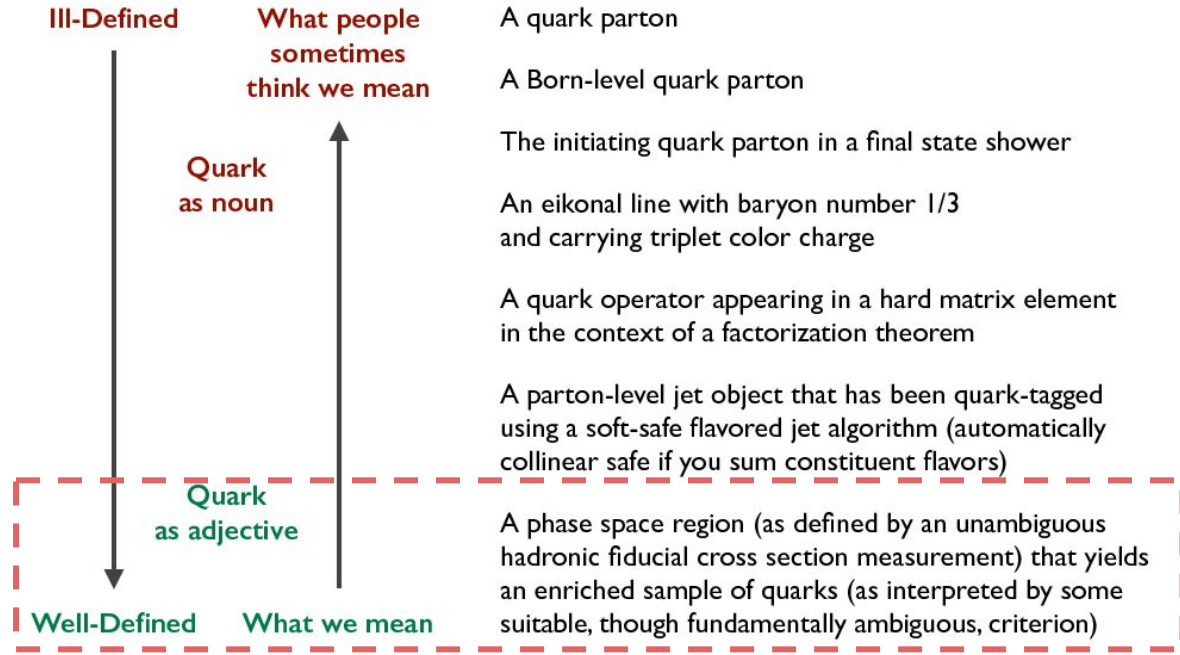
\* [ATLAS](#): baryon&kaon fractions play a big role too

# Intrinsic ambiguity of parton flavor

## What is a Quark Jet? (Or a gluon jet)

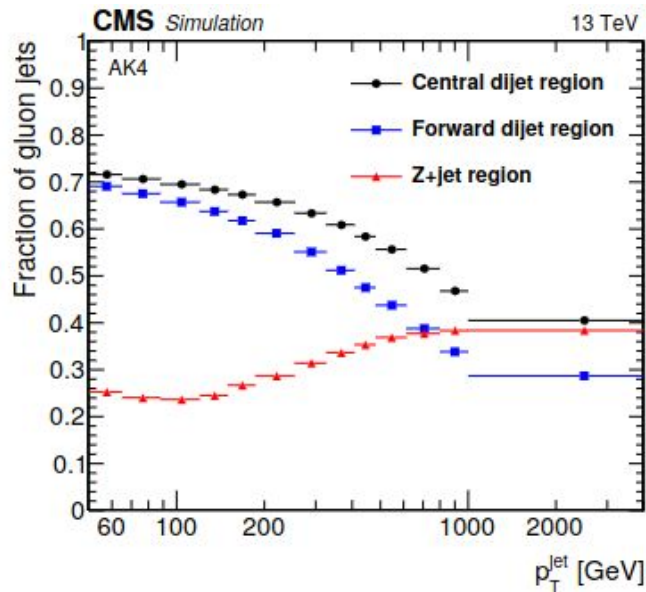
*From lunch/dinner discussions*

Les Houches 2015  
JHEP 1707 (2017) 091

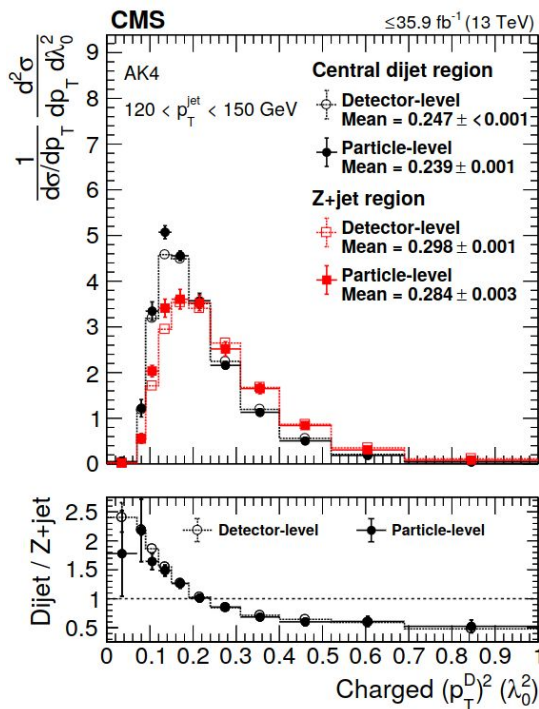


Hadron-level  
phase space regions

# Z+jet vs dijet

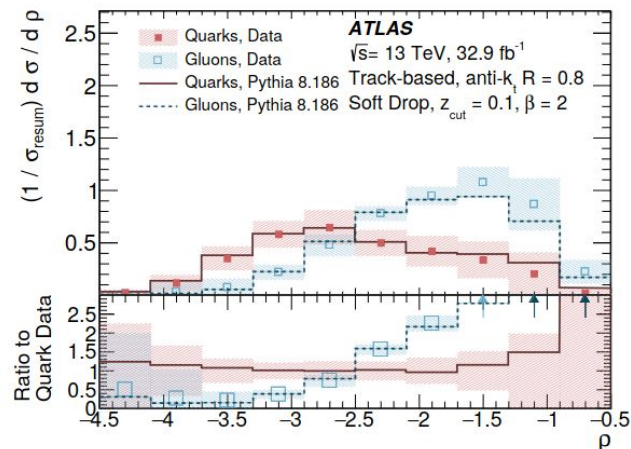


[CMS, JHEP 01 \(2022\) 188](#)



BOOST 2024

# Central vs forward jets → Quark-like & gluon-like topic models

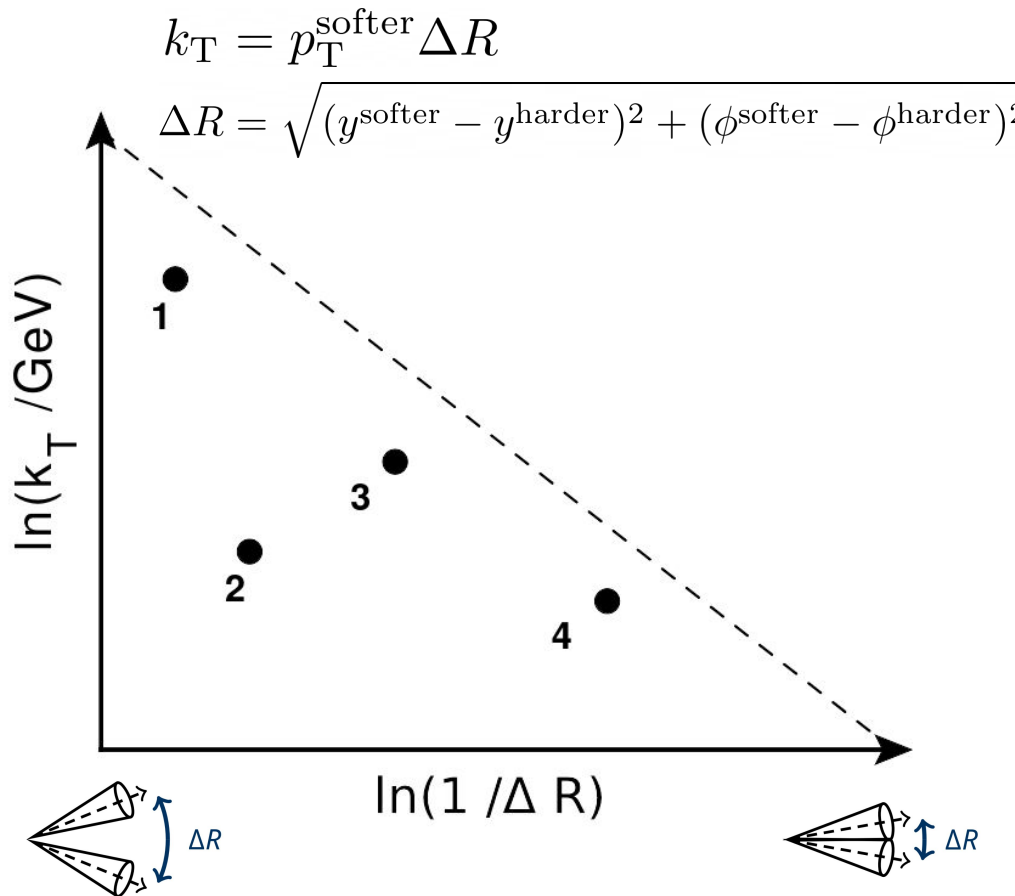
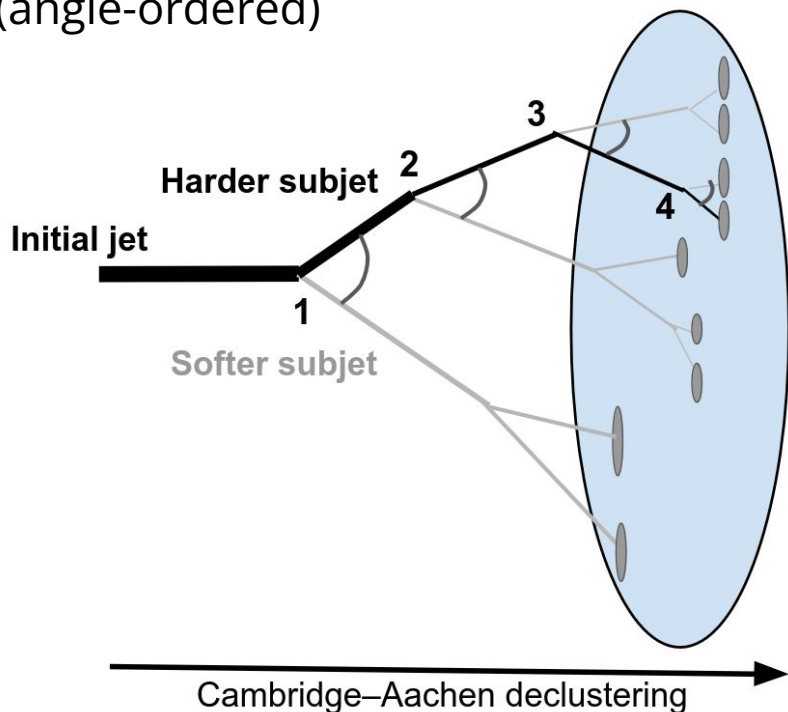


[ATLAS, PRD 101, 052007 \(2020\)](#)

# The primary Lund jet plane (quick recap)

*F. Dreyer, G. Salam, G. Soyez, JHEP12(2018)064*

Cambridge–Aachen reclustering to construct a tree of intrajet emissions (angle-ordered)



Define the *jet-averaged* number of emissions, (primary Lund jet plane density)

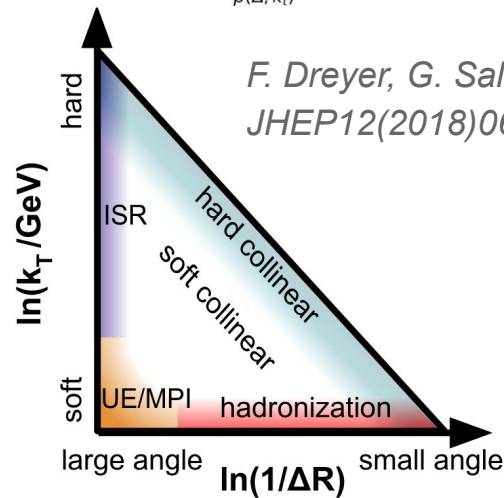
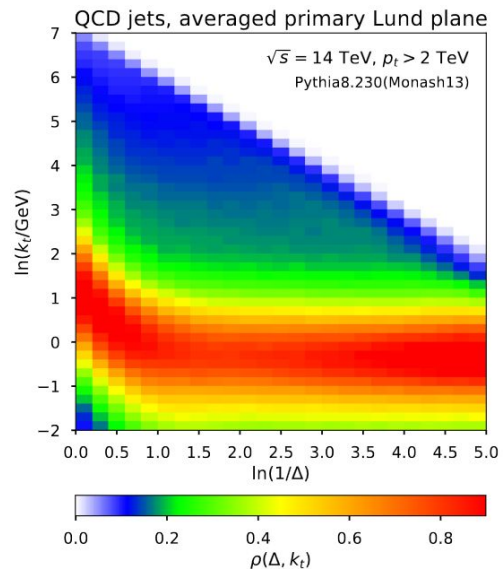
$$\rho(k_T, \Delta R) \equiv \frac{1}{N_{\text{jets}}} \frac{d^2 N_{\text{emissions}}}{d \ln(k_T/\text{GeV}) d \ln(R/\Delta R)}$$

“sculpted” by the running of  $\alpha_S(k_T)$  at LO

$$\rho(k_T, \Delta R)_{\text{LO}} \approx \frac{2}{\pi} C_R^{\text{eff}} \alpha_S(k_T)$$

With  $C_R = C_A = 3$  for  $g \rightarrow gg$  or  $C_F = 4/3$  for  $q \rightarrow qq$  splittings

Ability of “factorizing” effects



F. Dreyer, G. Salam, G. Soyez,  
JHEP12(2018)064



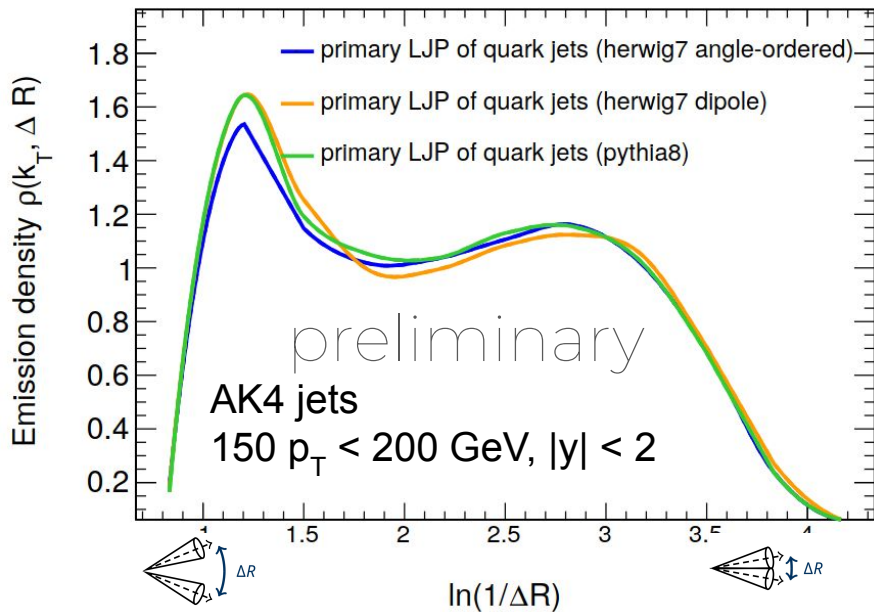
# Quarks vs gluon primary LJPs in pp collisions



Hadron-level sim.

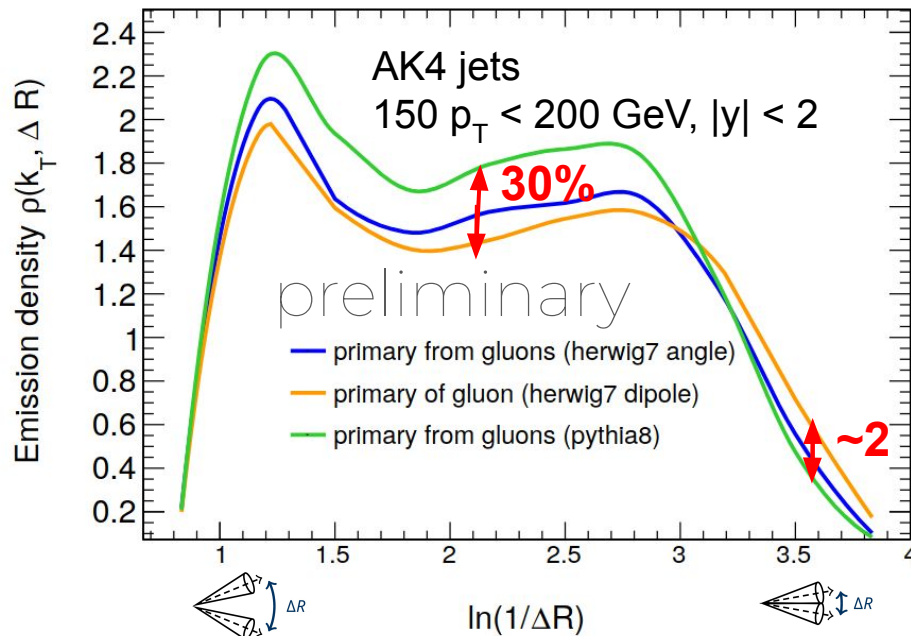
Same LJP slice at low  $k_T \sim 1$  GeV

## Quark jets ( $qq \rightarrow qq$ )



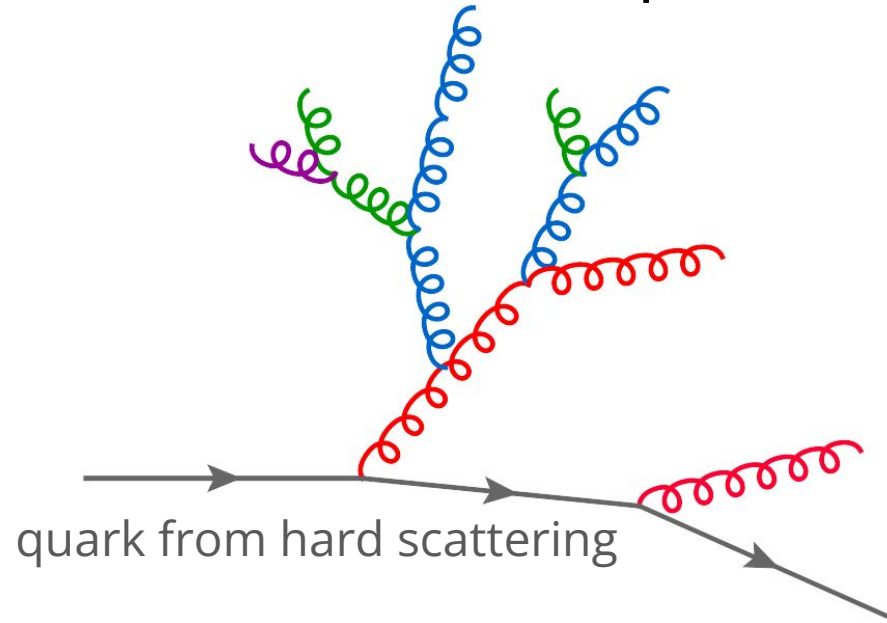
Spread of 1–5% (**LEP constraints**)

## Gluon jets ( $gg \rightarrow gg$ )



Much larger spread, up to 30% differences.  
Not as constrained by LEP!

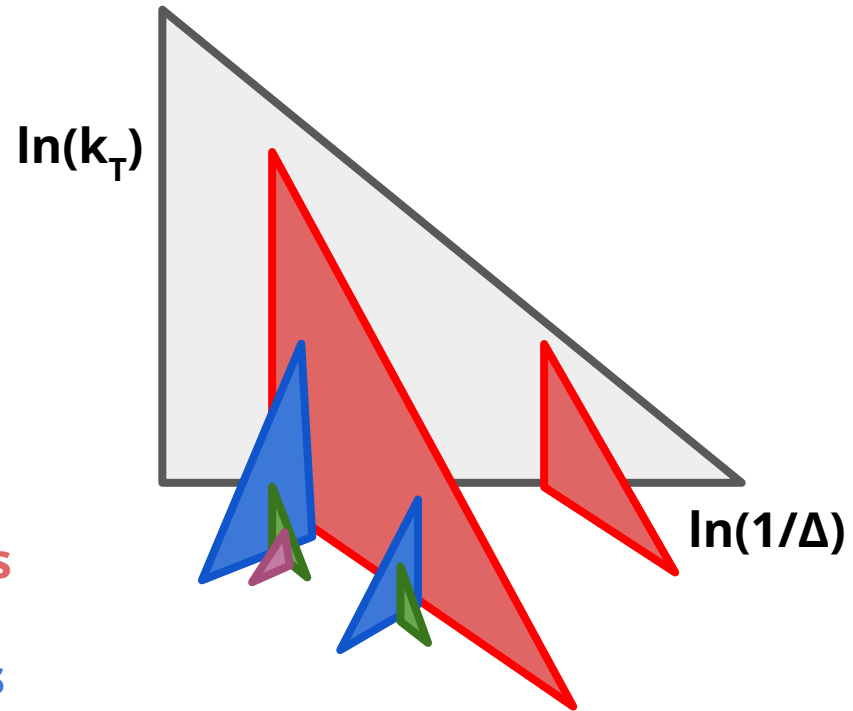
# Each QCD emission spawns its own Lund plane



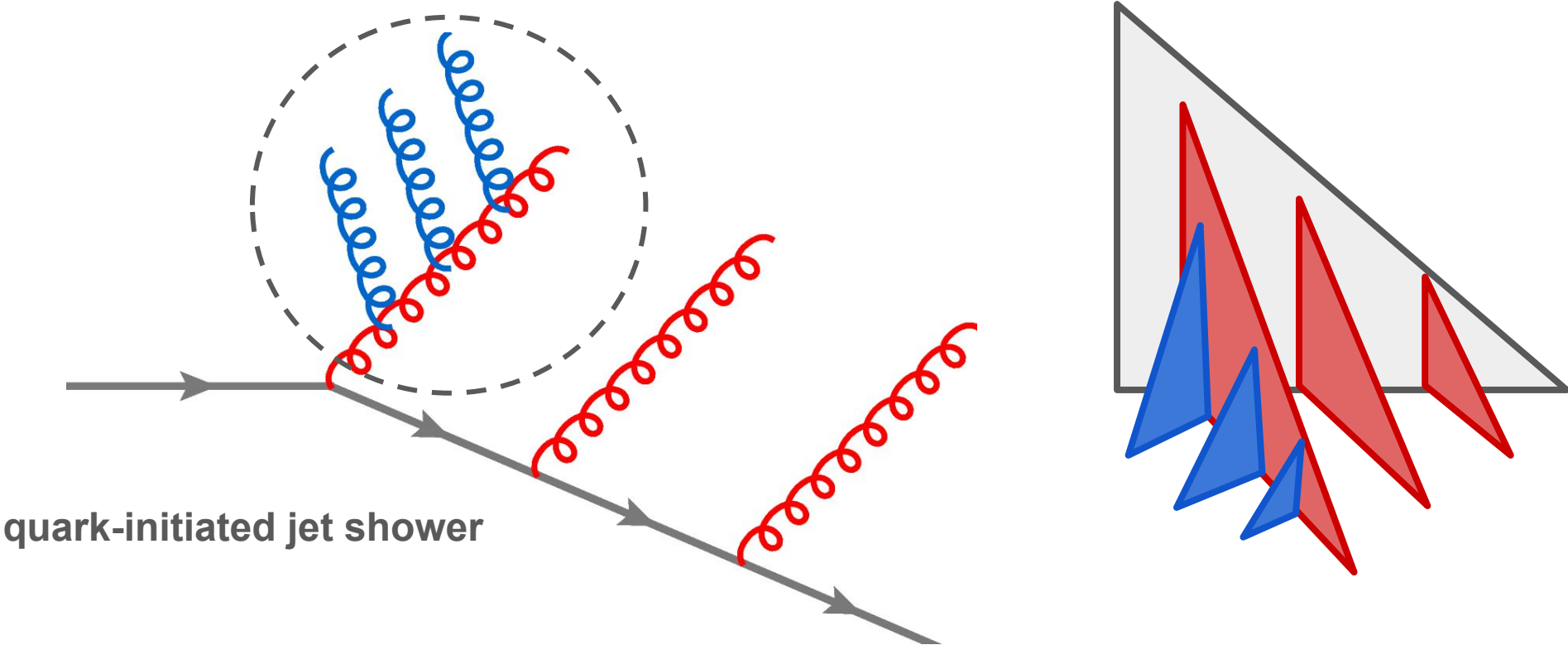
Emissions in **red** are the **"primary" emissions**

Emissions in **blue** are **"secondary" emissions**

Other colors represent "subsidiary" emissions



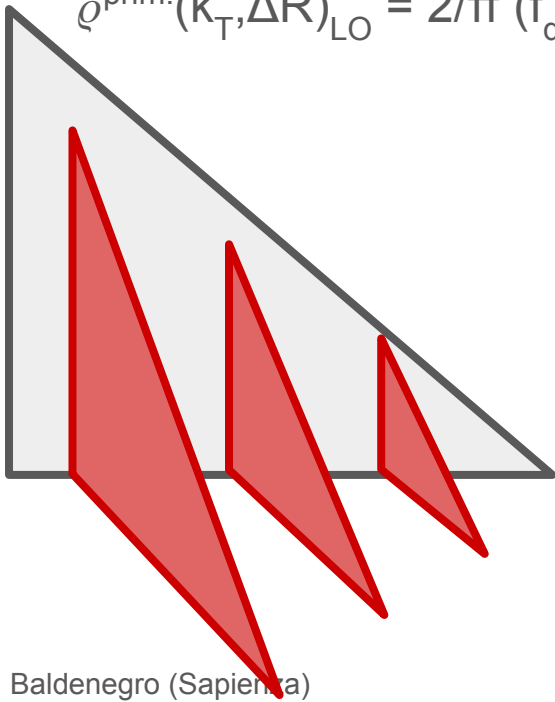
# Secondary Lund planes for gluon radiation



## Primary Lund plane

Average map for **mixture** of quark/gluon jets at high- $p_T$

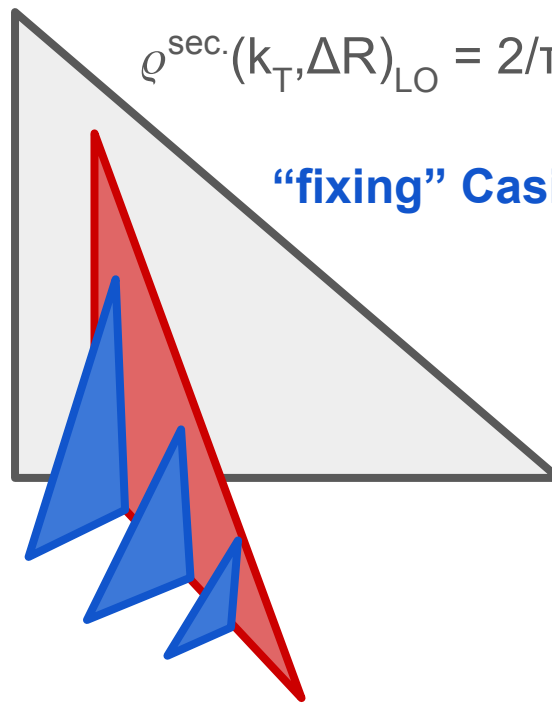
$$Q^{\text{prim.}}(k_T, \Delta R)_{\text{LO}} = 2/\pi (f_q C_F + f_g C_A) \alpha_S(k_T)$$



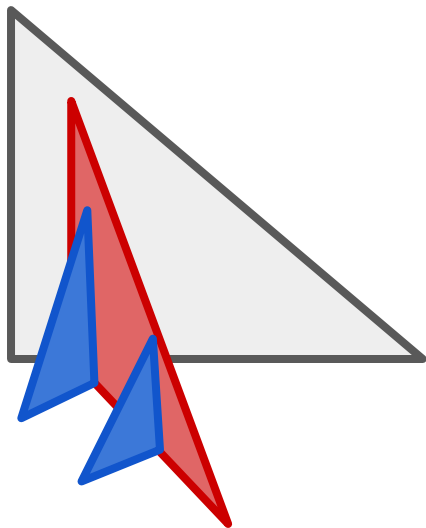
## Secondary Lund jet plane

If **primary emission** is chosen judiciously, can obtain gluon-rich jet sample at a lower  $p_T$

$$Q^{\text{sec.}}(k_T, \Delta R)_{\text{LO}} = 2/\pi \boxed{C_A \alpha_S(k_T)}$$

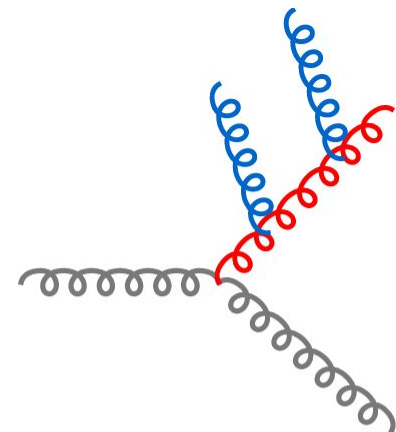
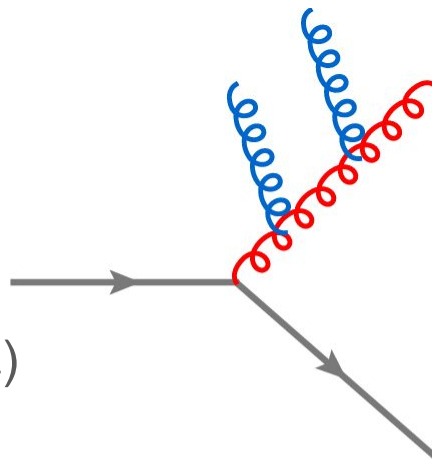


“fixing” Casimir factor



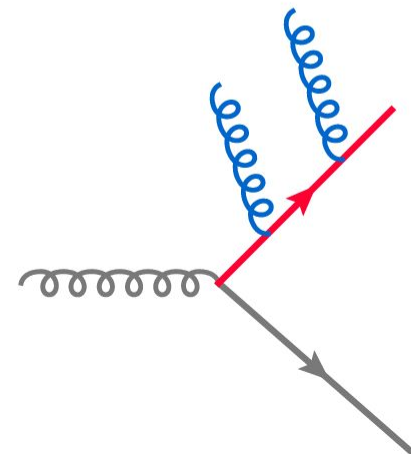
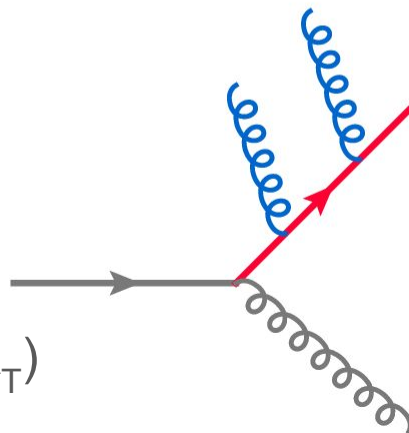
Gluon-dominated  
secondary Lund planes

$$Q^{\text{sec.}} \sim 2/\pi \boxed{C_A} \alpha_S(k_T)$$



Quark-dominated  
secondary Lund planes

$$Q^{\text{sec.}} \sim 2/\pi \boxed{C_F} \alpha_S(k_T)$$



# Which primary Lund emission?

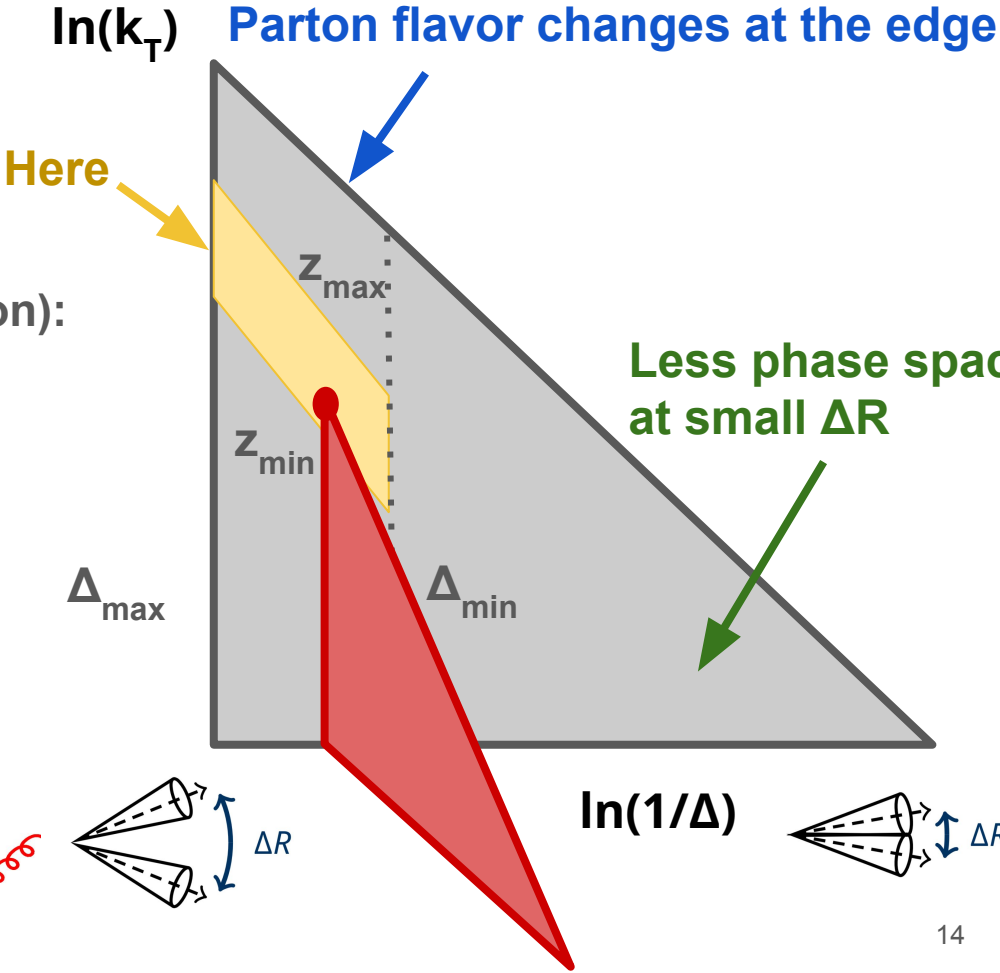
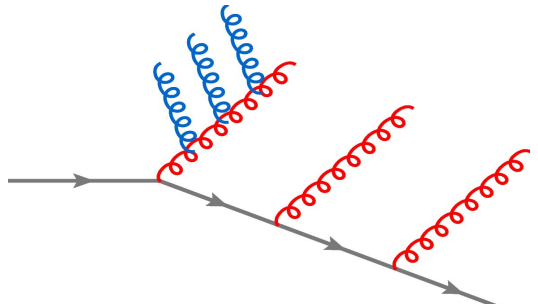
Collinear emission, but sufficiently large angles for phase space

(e.g.,  $\Delta R_{\min} \sim \frac{1}{2} R$ ,  $\Delta R_{\max} \sim R$ )

Soft emission (1/z pole of splitting function):

Asymmetric momentum balance,  
 $z = p_{T,\text{soft}} / (p_{T,\text{soft}} + p_{T,\text{hard}})$  (e.g.,  $0.2 < z < 0.25$ )

Phase-space region where parton flavor changes are negligible



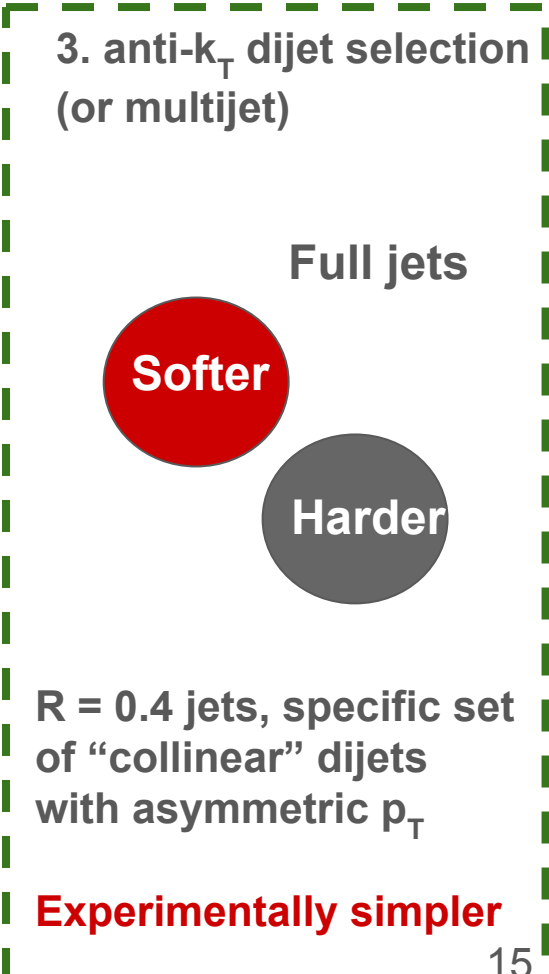
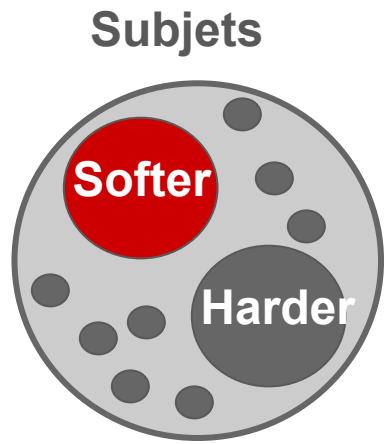
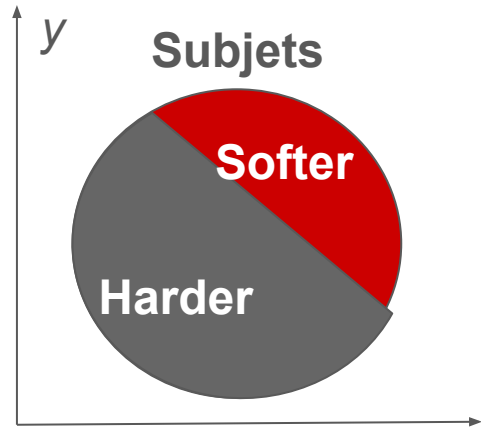
focus on this

# At least three setups (picking **leading (sub)jet** )

1. SoftDrop-like  
(Cambridge/Aachen tree)

2. Trimming  
( $R = 1.2 \rightarrow R = 0.4$ )

3. anti- $k_T$  dijet selection  
(or multijet)



Large  $R = 1.2$  jet with  $p_T^\varphi > 1$  TeV

Large  $R = 1.2$  jet with  $p_T > 1$  TeV  
 $\rightarrow$ recluster w/ small  $R = 0.4$

$R = 0.4$  jets, specific set  
of "collinear" dijets  
with asymmetric  $p_T$

SoftDrop emission with  $R_g > 0.6$   
&&  $0.1 < z_g < 0.3$

**Experimentally simpler**

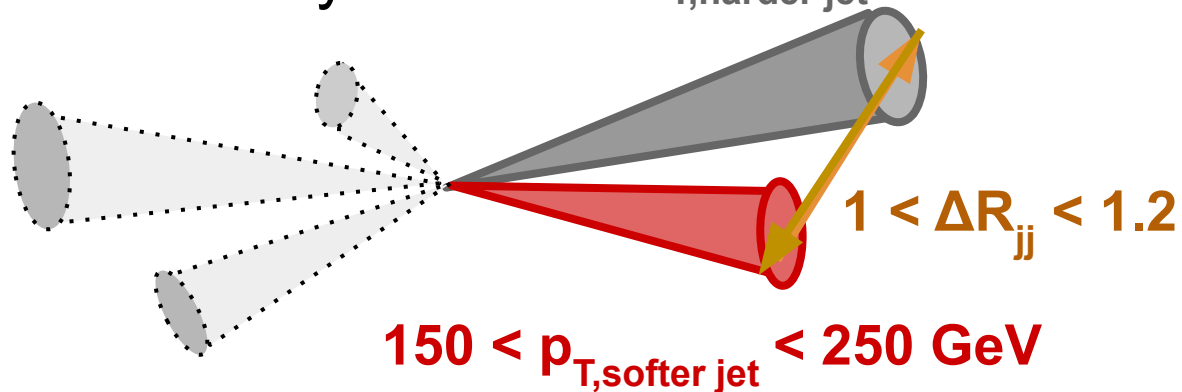
**Clustering distortions  
at large angles**

# Inclusive dijet selection

recoil jet radiation  
treated inclusively

Quark/gluon mixture

$p_{T,\text{harder jet}} > 700 \text{ GeV}$



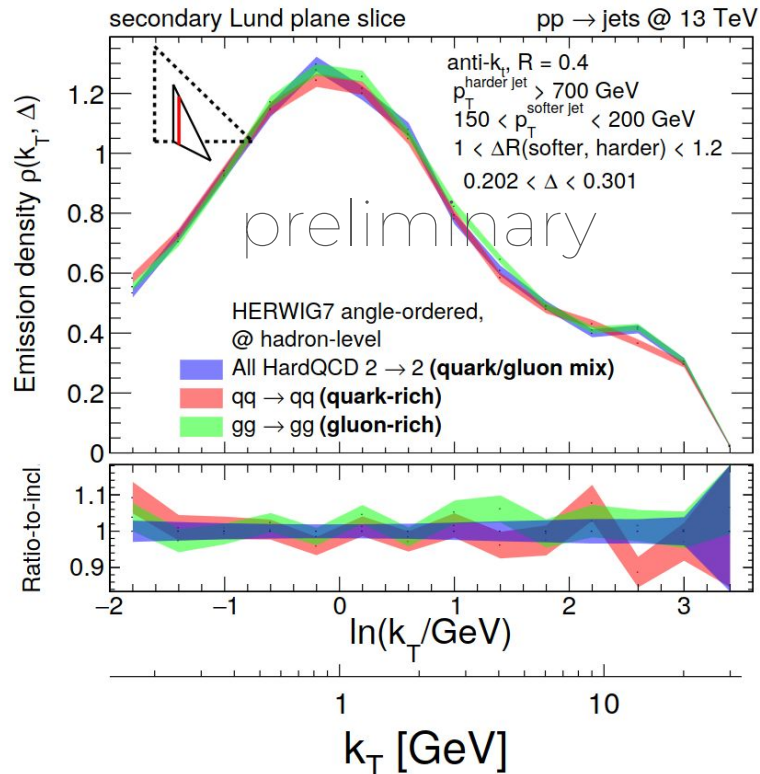
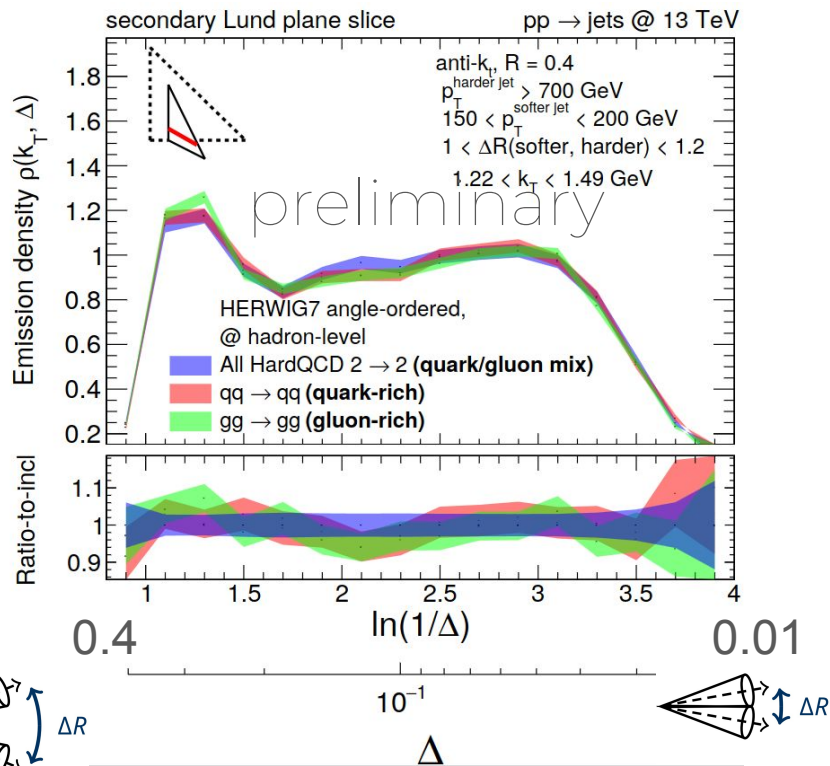
$\mathcal{O}(10^5 - 10^6)$  "high-purity"  
gluon-like jets w/ Run-2 stats

**gluon-enriched**

**NB:** baseline selection, can be fine-tuned



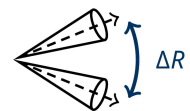
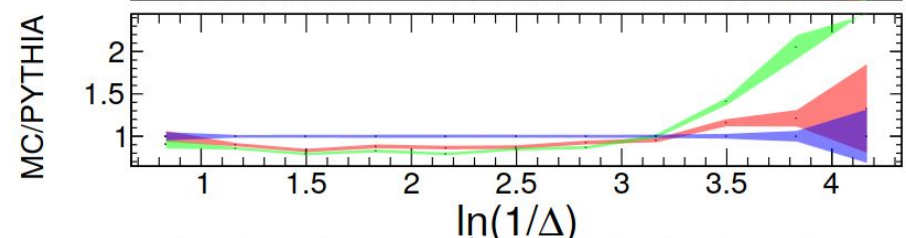
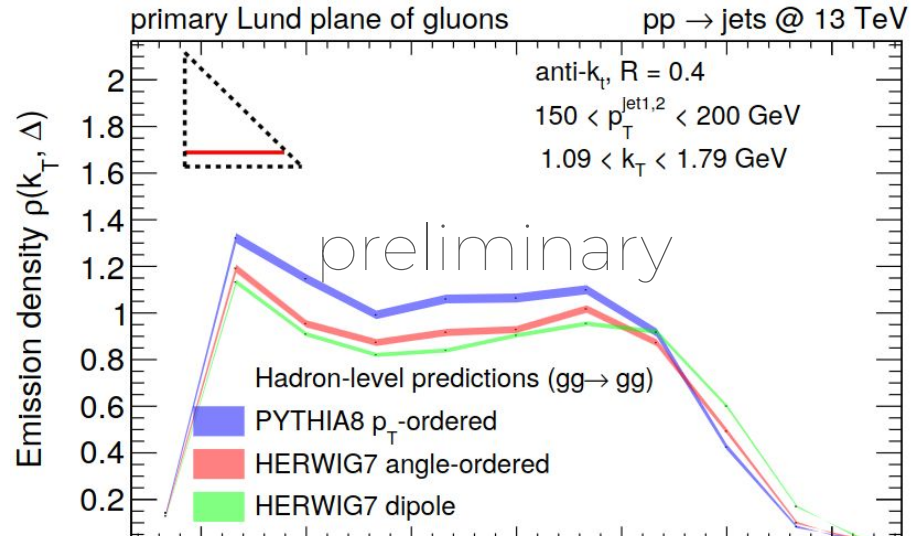
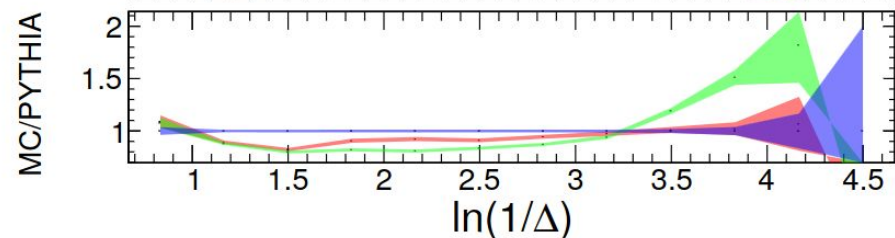
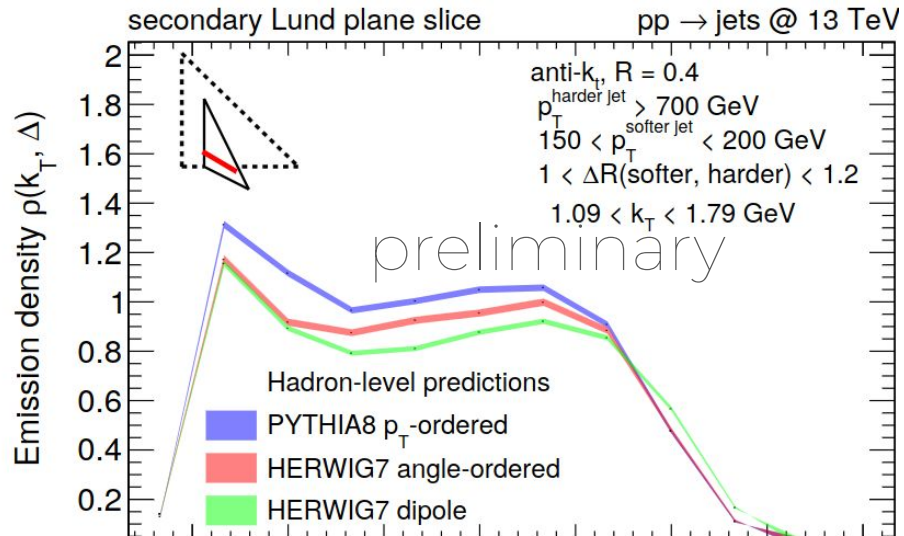
# Process-independence, PDF-independence



**Similar results** regardless of parton flavor of the hard scattering.  
 Can be checked in data w/ tight cuts on quark vs gluon taggers.

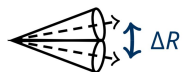
# Model discrimination power:

## secondary Lund plane vs primary Lund plane of gluons ( $gg \rightarrow gg$ )



$10^{-1}$

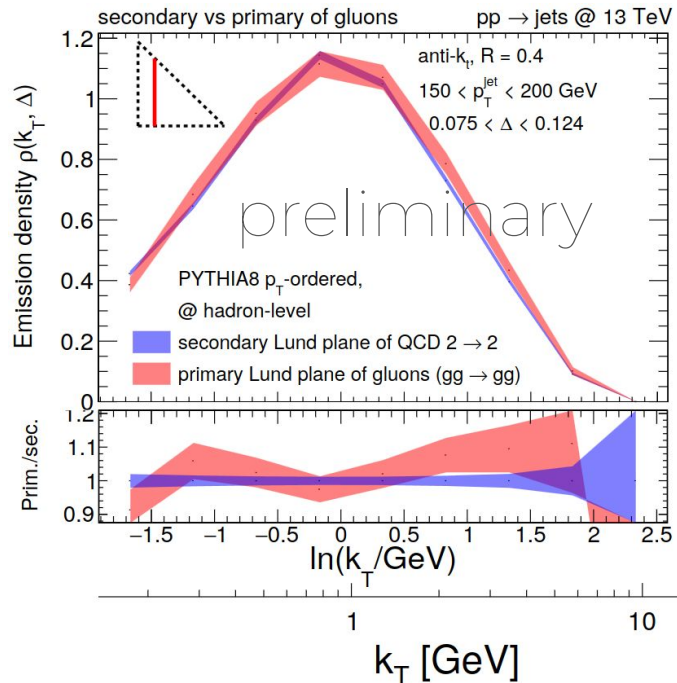
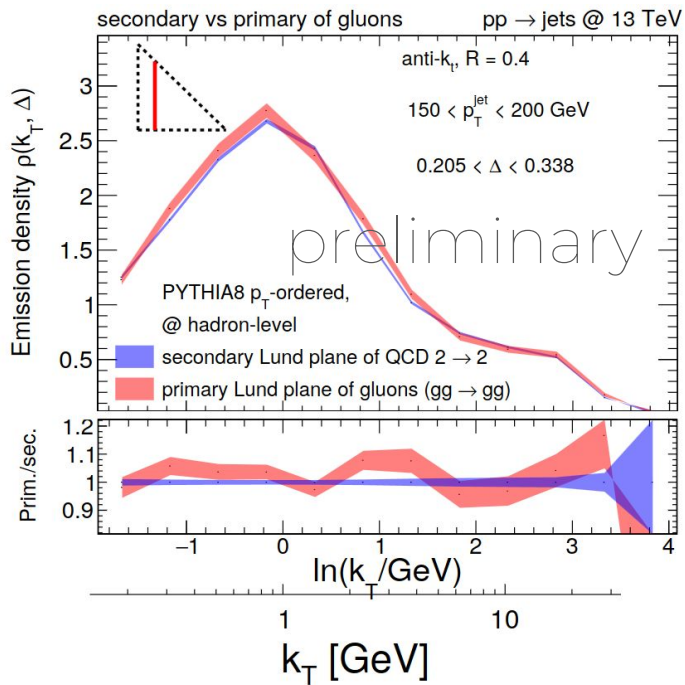
$\Delta$



$10^{-1}$

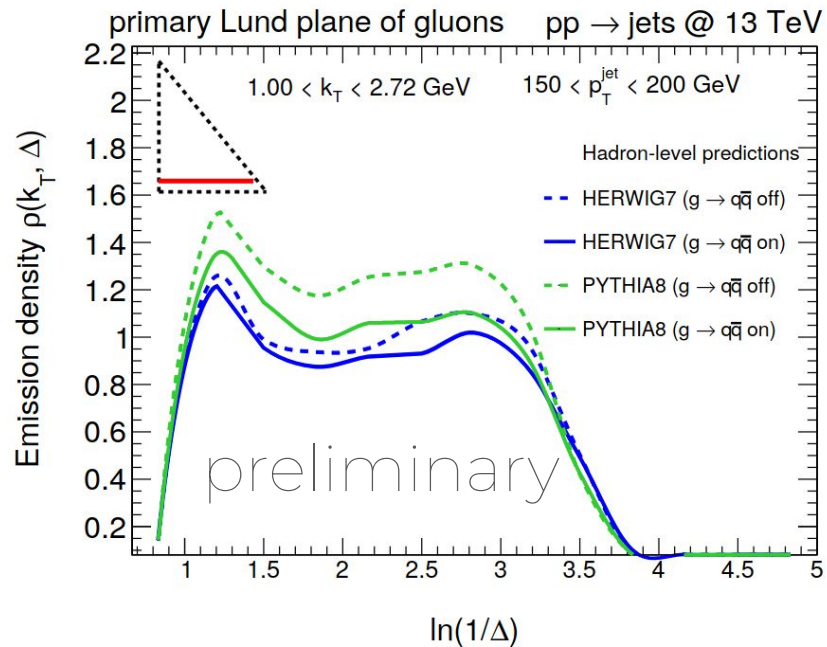
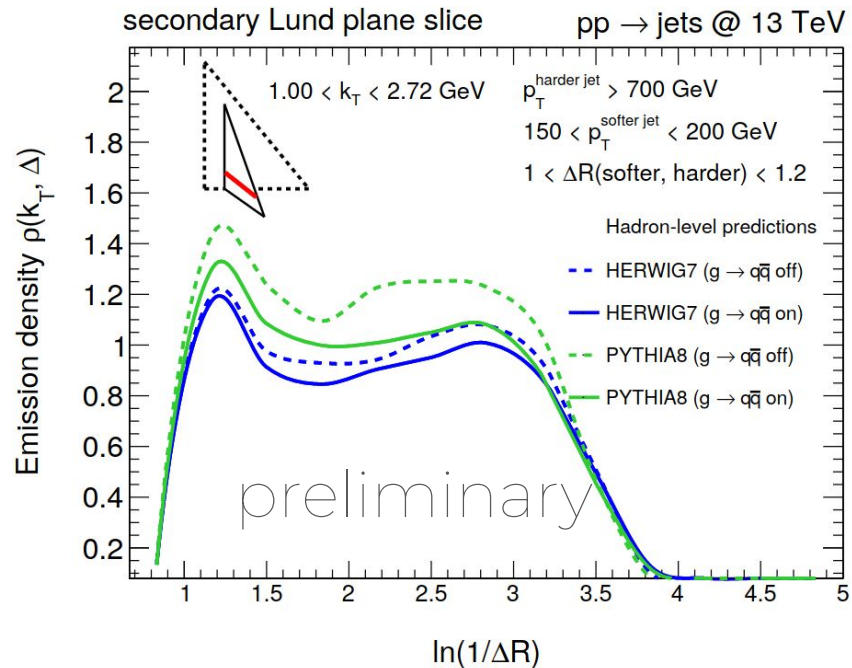
$\Delta$

# Secondary vs primary Lund jet plane of gluons ( $gg \rightarrow gg$ )



NB: reweighted  $p_T$  spectrum to remove jet  $p_T$  biases

# Gluon splitting ( $g \rightarrow qq$ on vs off)



Similar effects of  $g \rightarrow qq$  on vs off in both secondary vs primary Lund plane of gluons

# Summary

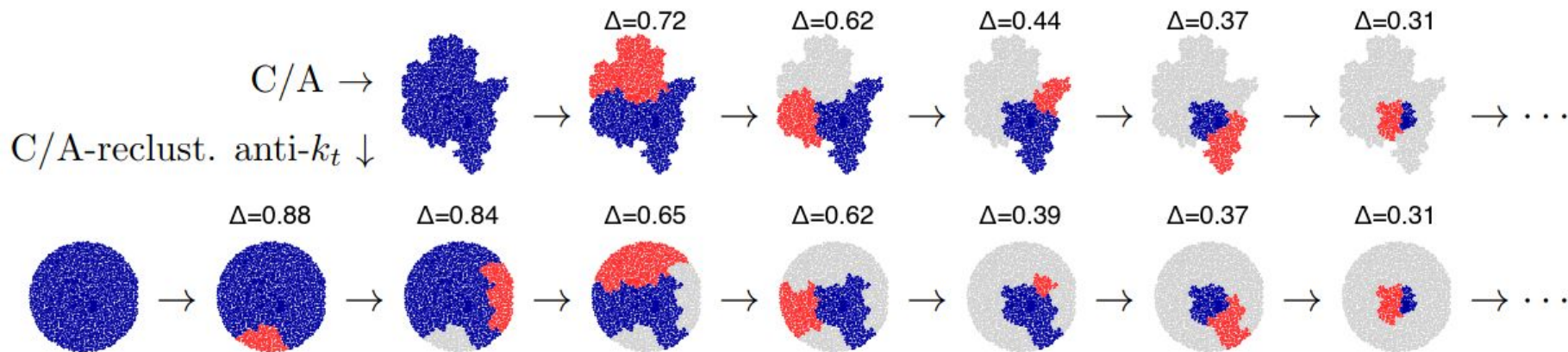
- Gluon-rich final state radiation using simple hadron-level cuts (“Rivet-friendly” for tuning)
- Resilient to flavor of partons in hard scattering (cf simulation studies using LO MC generators)
- Can be extended to other observables (dynamical  $k_T$ , groomed jet mass, angularities...)
- Potential applications for precision physics (e.g.,  $\alpha_s$  with resilience to quark/gluon fraction)

Would require a 2→3 fixed-order piece at lowest order  
(trade-off between q/g fraction vs order of pQCD)

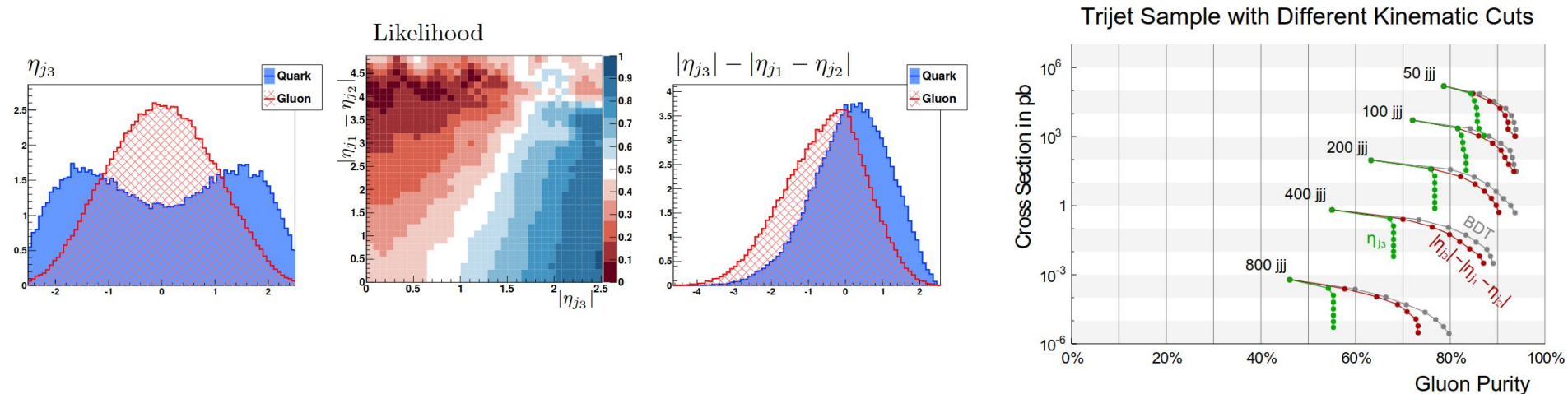
backup

# Distortions due to initial anti- $k_T$ clustering

[arXiv:1807.04758](https://arxiv.org/abs/1807.04758)



# Related proposal for gluon jet enrichment



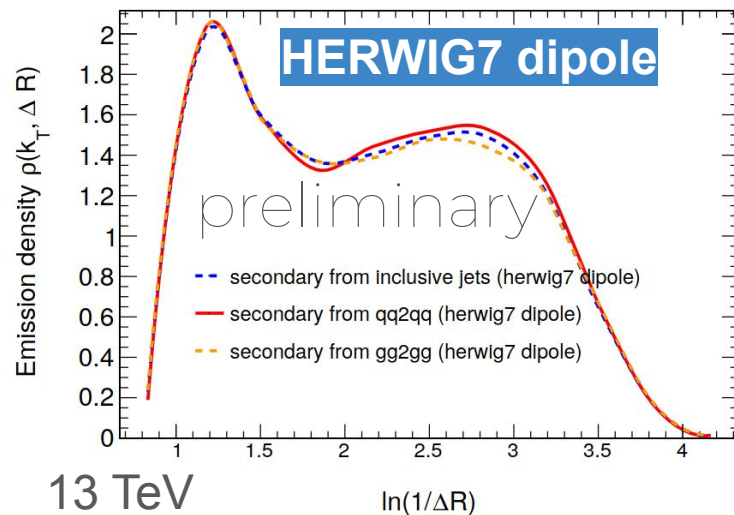
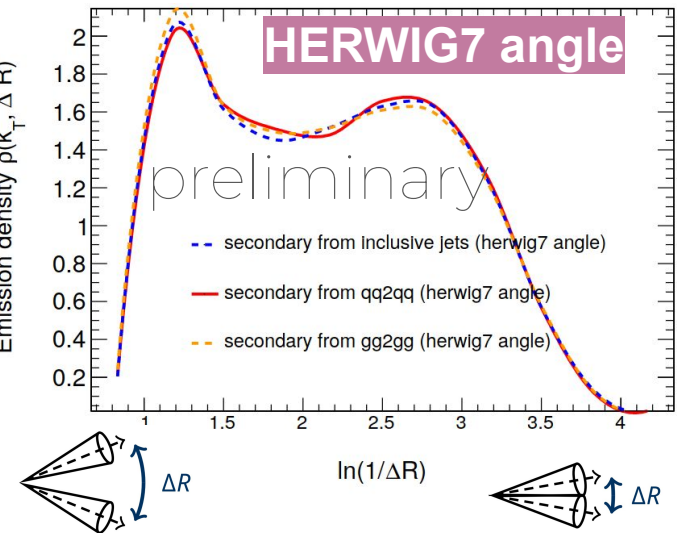
J. Gallicchio, M. D. Schwartz [arXiv.org/abs/1104.1175](https://arxiv.org/abs/1104.1175)

Rectangular cuts on based on BDT-training on trijet MC sample, using  $|\eta_3| - |\eta_1 - \eta_2|$  &  $\eta_3$  discriminant



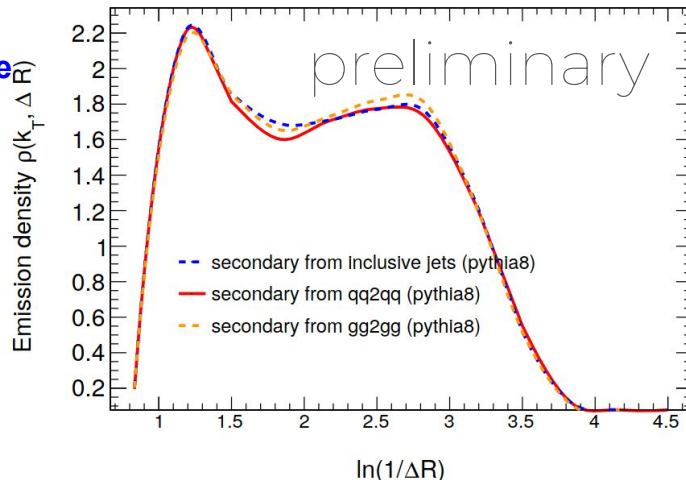
# Process- & PDF-independent observable

13 TeV



**PYTHIA8**

13 TeV



**Secondary LJP from quark-gluon mixture (inclusive jets)**

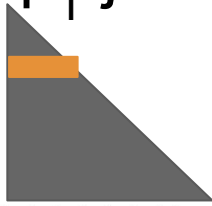
**Secondary LJP from quarks (qq→qq hard scattering)**

**Secondary LJP from gluons (gg→gg hard scattering)**

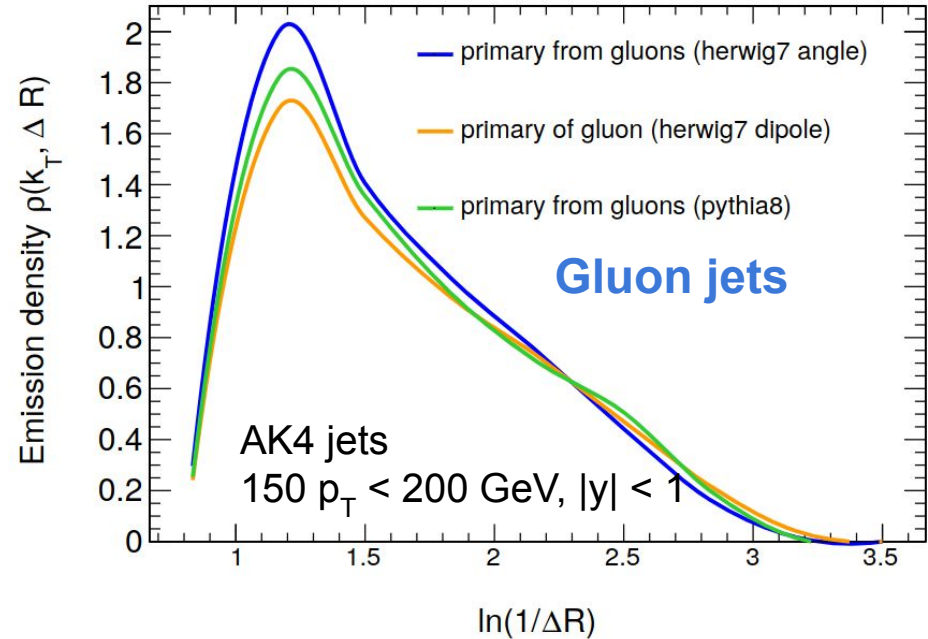
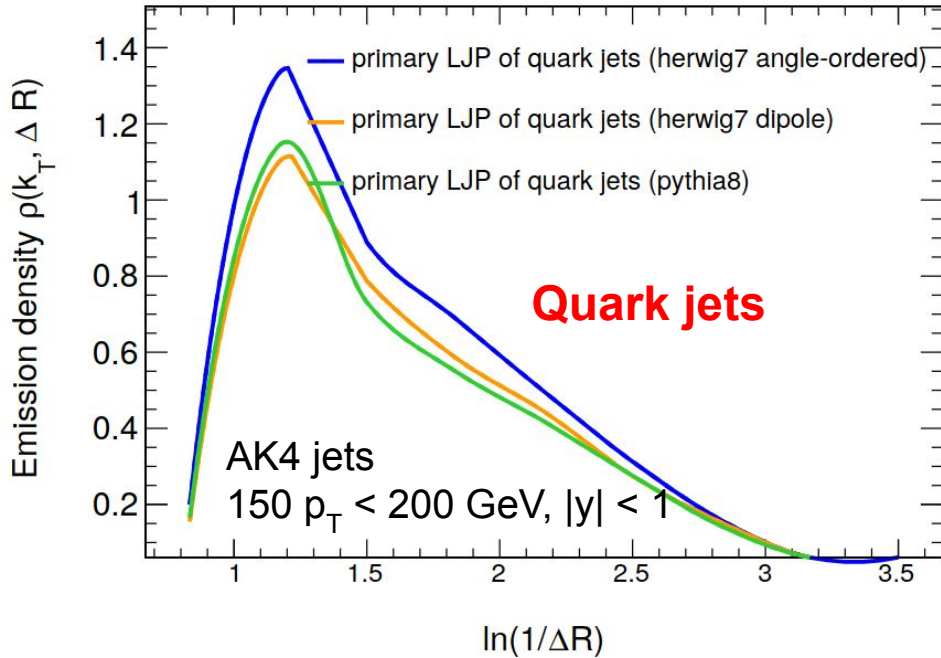
Differences negligible within expected sensitivity

Shape and normalization resilient to underlying q/g fraction

# “Quark jets constrained by LEP” mostly accurate for low $p_T$ jets cf reach of LEP



Differences in perturbative regime ( $k_T > \sim 5$  GeV) for quark and gluon jet showers



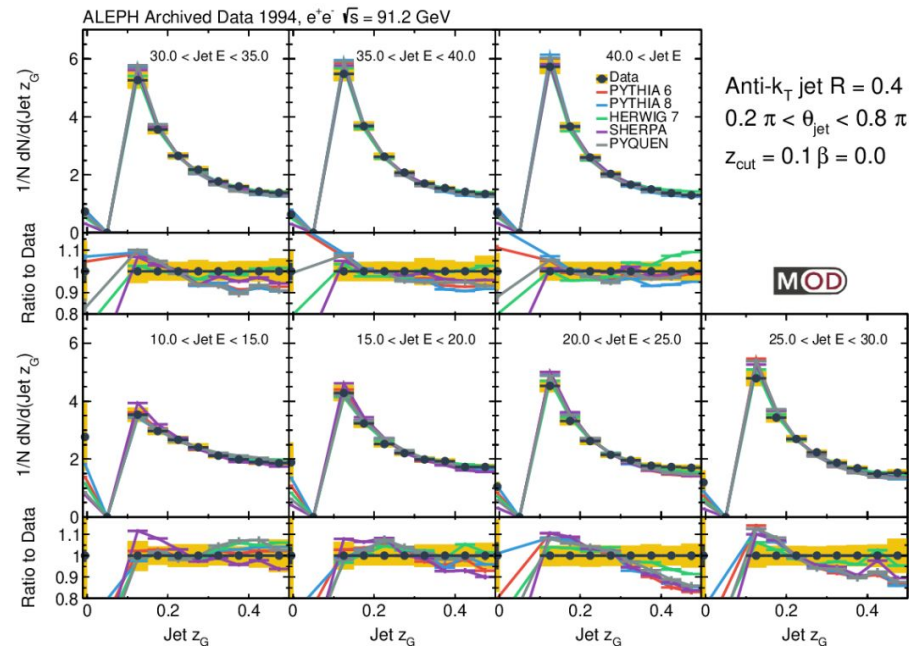
Herwig7 dipole usually closer to Pythia8 in the perturbative region

**Herwig7 angle-ordered usually higher in perturbative region**

# “Quark jets constrained by LEP”

Data/MC differences with Lund-based observables. For example, soft-drop  $z_G$  with archived ALEPH data shows mismodeling for  $z_G \sim 0.5$  (upper edge of Lund plane).

LHC data valuable to clarify mismodeling (dijet, Z+jet, UPC jets...) for high- $p_T$  quark jets



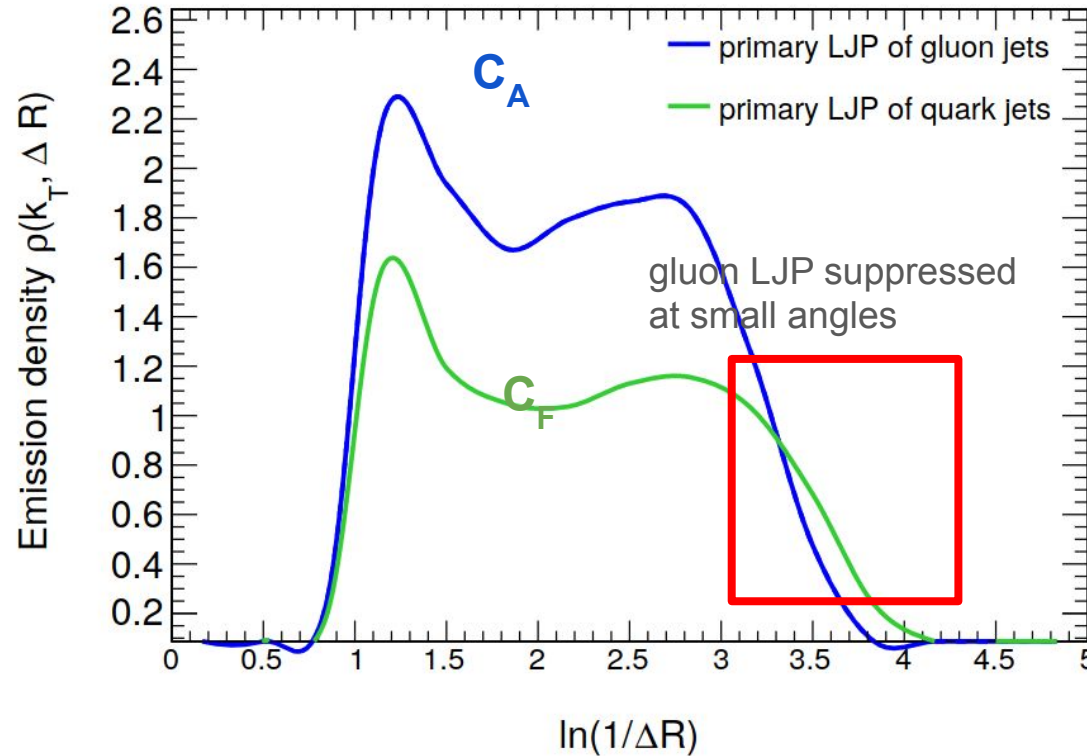
[Yi Chen et al  
arxiv.org/abs/2111.09914](https://arxiv.org/abs/2111.09914)

# Quarks vs gluon Lund planes



Not **just**  $C_A/C_F$  scaling! Leading parton momentum loss in the Lund tree histogram soft&collinear divergences, color reconnection effects, ...

**Gluon LJP is suppressed at small angles wrt quark LJP**



# Quark/gluon jet fraction issue

“ $\alpha_S$  always paired with a color factor,  $C_f \alpha_S$ ”

Different strategies have been adopted (w/ soft-drop mass).

- PDF uncertainties  
(H. S. Hannesdottir, A. Pathak, M. D. Schwartz, I. W. Stewart, [arXiv:2210.04901](https://arxiv.org/abs/2210.04901), [Les Houches 2017](#))
- Fit  $\alpha_S(m_Z)$  and quark/gluon fraction  
([Les Houches 2017](#))
- Statistically “demix” quark- and gluon-like samples  
([arXiv:2206.10642](https://arxiv.org/abs/2206.10642))
- Design observables with reduced q/g fraction sensitivity  
(cf [Meng Xiao](#)’s talk on energy correlators,  $\delta\alpha_S/\alpha_S \sim 4\%$ )

