An Approach to Pin Down the Top Mass Parameter in MC Generators

This talk reports on new work Oliver Jin,
Simon Plätzer and Daniel Samitz

arXiv:1807.06617 arXiv:2404.09856 arXiv:2408.xxxxx

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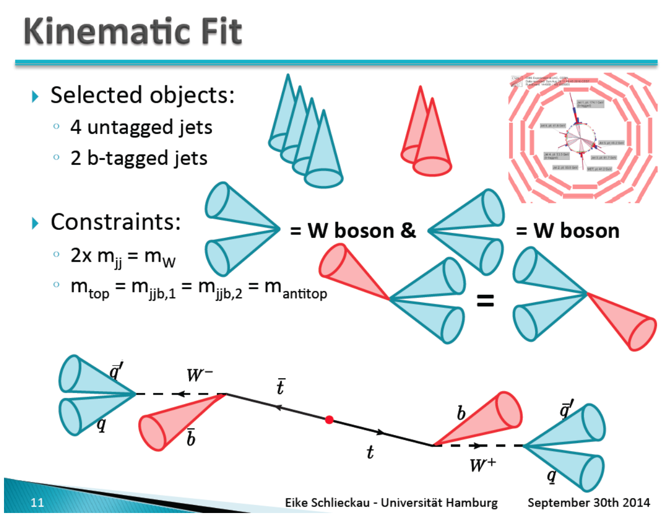
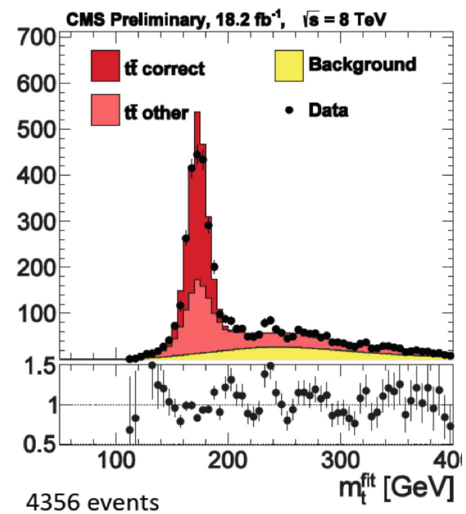
Most Precise Top Mass Measurements Method

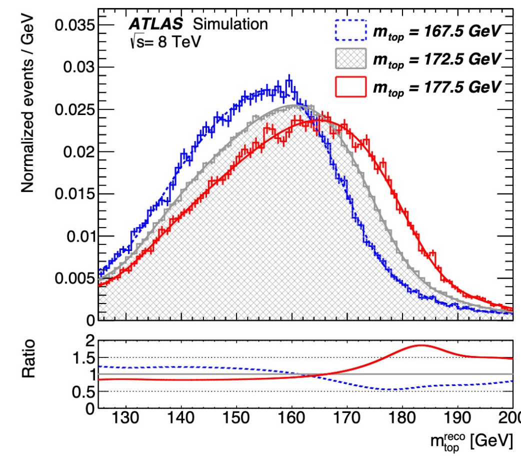
LHC+Tevatron: Direct top mass measurements



CMS-PAS-TOP-14-002



4356 events



$$m_t^{\mathrm{MC}} = 171.77 \pm 0.37 \text{ GeV}$$

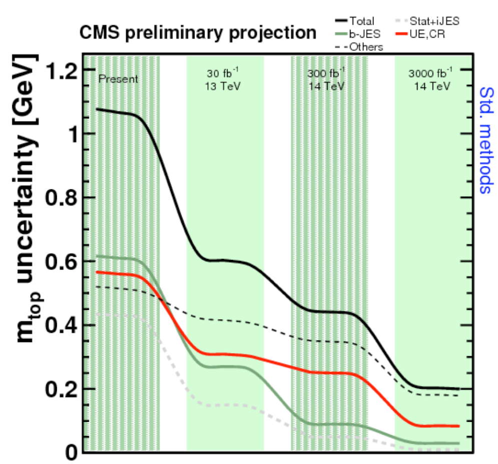
CMS collaboration. arXiv: 2302.01967

→ talk by Mark Owen

kinematic mass determination

based on the picture of a top quark particle

Determination of the best-fit value of the Monte-Carlo top quark mass parameter



⊕ High top mass sensitivity

⊖ Precision of MC ?

⊖ Meaning of m_t^{MC} ?

← Δm_t ~ 200 MeV (projection)

What is m_t^{MC} ?

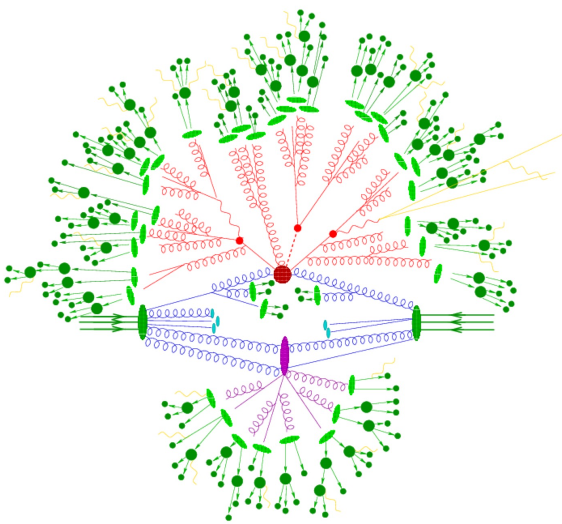
What does the question mean in the first place?

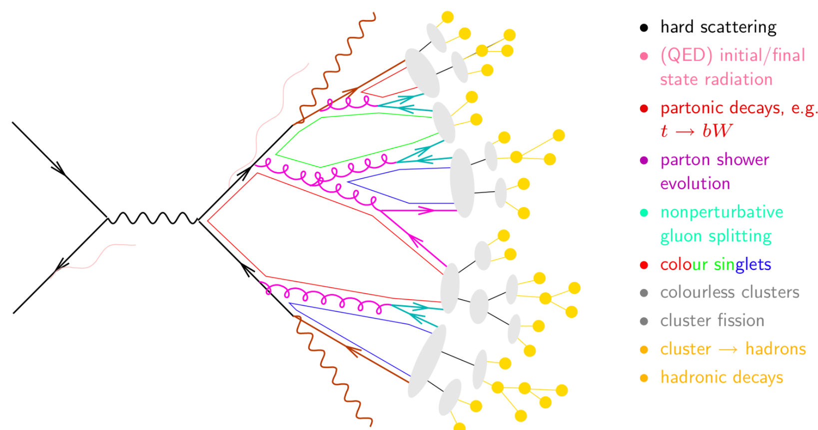
→ It means that we can provide the relation

$$m_t^{\rm MC} = m_t^{\rm scheme}(\mu) + \frac{\alpha_s(\mu)}{\pi}\delta m^{\rm scheme} + \ldots$$

where $\delta m^{\rm scheme}$ can be **computed in pQCD**

The issue is complicated as we must understand and control the interplay of the different components of MC event generators.





→ Aim: Define and quantify a "**MC top mass scheme**"

- Defined in pQCD (→ parton shower)
- Controlled at the observable hadron level. (→ hadron level)

Approaches to remedy the m_t^{MC} problem

- Indirect top quark mass measurements → ATLAS/CMS e.g. arXiv:2403.01313
  - Unfold data to parton level top-anti top on-shell particle distributions (e.g. m_{tt}) to be compared to N(N)LO fixed order calculations for on-shell top quarks
  - MC modelling aspects now contained in the hadron-to-parton unfolding carried out with the MC generator (no "theory of unfolding", but different systematics)
  - Uncertainties not yet as small as for direct determinations as observables are of more inclusive character
- 'Hadron' level analytic QCD predictions for top mass determinations
  - Fat top jets with soft drop grooming
    → MPI currently provides a practical limitation for LHC

    Mantry, Pathak, Stewart, AHH (2017)
    Mantry, Pathak, Stewart, AHH (2019)
    ATL-PHYS-PUB-2021-034
    → Naseem's talk
  - Energy correlators
    → new type of top mass sensitivity related to decay opening angle

    Holguin, Moult, Pathak, Procura (2022)
    Holguin, Moult, Pathak, Procura, Schöfbeck (2023)
    → Aditya's talk

  → Comparison with data or hadron level MC simulations
- This talk is about work to truly understand and control the MC top quark mass parameter m_t^{MC} → Improve/understand MCs so that direct measurements can be interpreted reliably.

What is m_t^{MC} ?

There are 4 essential ingredients to resolve the problem from first principles:

(B) Hadron level analytic QCD predictions

(A) Understanding of top as a quantum state

→ beyond the picture of a top particle

Parton Shower Cutoff

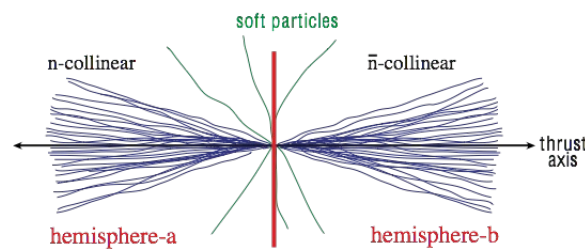
(C) N(N)LL precise MC parton shower

(D) Factorization compatible MC hadronization model

Currently there is only 1 observable class where all 4 ingredients are available and controlled.

Jet mass based event-shape observables in e^+e^- collisions for boosted top pair production in dijet region:

→ 2-jettiness, thrust, … (decay insensitive, NNLL)



Aim of this talk:

- Discuss interplay of (A) – (D) provide conceptual and practical basis to determine and control m_t^{MC} for MC event generators
- Review (A) – (C) from previous work. New development for (D)
- Explicit realization for e^+e^- event-shape top resonance distribution (e.g. 2-jettiness) for Herwig 7.2 as a proof of principle

(A) Beyond the picture of a top particle

The top quark does not hadronize due to its large width $\Gamma_t \gg \Lambda_{QCD}$. It therefore has some characteristics of a physical particle (hadron).

BUT: If we stick to the picture of a physical top particle the only mass that is ever relevant is the pole mass = pole of the top propagator.

Due to the top quarks color charge, however, this picture is too restricted when we want to understand the MC top quark mass.

What we mean by a top quark is however related to

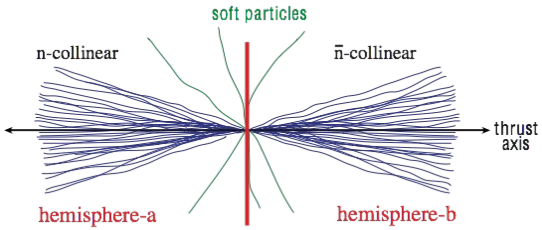
well known aspect

- a particular experimental measurement prescription (of a color singlet state)
  → calculations/simulations must properly account color neutralization effects
  → implies that we need accurate hadron level QCD predictions/simulations

novel aspect

- the way how we treat soft gluons in the top rest frame
  → MC simulations impose an IR cut Q_0 of the parton shower gluon evolution
  → the shower cutoff Q_0 acts as a resolution scale
  → changes the physical meaning of the top quark mass in the simulation, but also the scheme of hadronization corrections for the entire process
  → impact of the shower cutoff needs to be quantified and controlled accurately

(B) Boosted top eventshapes



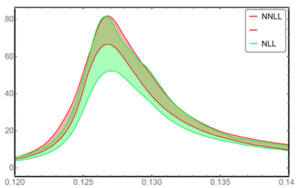
$$\tau \;=\; 1 - \max_{\vec{n}} \frac{\sum_i |\vec{n}\cdot\vec{p}_i|}{Q} \;\overset{\tau\to 0}{\approx}\; \frac{M_1^2 + M_2^2}{Q^2} \qquad Q = E_{\rm c.m.}$$

2-jettiness: insensitive to details of top decay

Hadron level SCET:

$$\frac{\mathrm{d}\sigma}{\mathrm{d}\tau}(\tau, Q, m, \delta m) = \int_0^{Q\tau} \mathrm{d}\ell\, \underbrace{\frac{\mathrm{d}\hat{\sigma}_s}{\mathrm{d}\tau}\Big(\tau - \frac{\ell}{Q}, Q, m, \delta m\Big)}_{\text{parton cross section}}\; S_{\rm mod}(\ell)$$

Non-perturbative shape function (universal for massive and massless quarks)



Fleming, Mantry, Stewart, AHH (2007)

Bachu, Mateu, Pathak, Stewart, AHH (2022)

- $S_{\rm mod}$ leading nonperturbative corrections only from large-angle soft radiation: linear sensitive to $\Lambda_{\rm QCD}$
- Any top mass renormalization scheme can be implemented $\quad m_t^{\rm pole} = m + \delta m$

- Can be calculated with a finite IR cutoff Q_0 for the parton cross section
- IR cutoff Q_0 = factorization scale for parton-level vs. hadronization corrections
  - Defines scheme for $S_{\rm mod}$ (large-angle soft radiation): $S_{\rm mod}(l) \to S_{\rm mod}(l, Q_0)$
  - Defines scheme for parton distribution: $\dfrac{d\hat{\sigma}}{d\tau}(\tau, Q, m) \to \dfrac{d\hat{\sigma}}{d\tau}(\tau, Q, m, Q_0)$

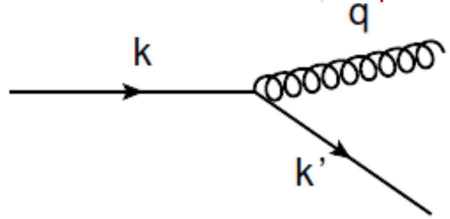
(C) Angular ordered parton shower (Herwig)

→ Coherent Branching algorithm (default Herwig shower):

Dokshitzer, Fadin, Khoze (1982)
Bassetto, Ciafaloni, Marchesini (1983)
Catani, Marchesini, Webber (1991)
Gieseke, Stephens, Webber (2003)

$$k'^{\mu} = z k^{-} \frac{n^{\mu}}{2} + \frac{k'^2 - q_{\perp}^2}{z k^{-}} \frac{\overline{n}^{\mu}}{2} - q_{\perp}^{\mu}$$

$$q^{\mu} = (1-z) k^{-} \frac{n^{\mu}}{2} + \frac{q^2 - q_{\perp}^2}{(1-z) k^{-}} \frac{\overline{n}^{\mu}}{2} + q_{\perp}^{\mu}$$



momentum conservation:

$$k^2 = \frac{k'^2}{z} + \frac{q^2}{1-z} + \frac{q_{\perp}^2}{z(1-z)}$$

evolution variables: $z\,,\ \tilde{q} = \dfrac{q_{\perp}^2}{z^2(1-z)^2}$

probabilities from splitting functions and Sudakov form factors

color coherence of soft gluon emissions → angular ordering: $z_i^2 \tilde{q}_i^2 > \tilde{q}_{i+1}^2$

→ NLL precise analytic jet mass distribution (mass generated from one boosted quark)

$k^2 \approx$ hemisphere mass (does not account for out of cone radiation)

$$\begin{aligned} J(Q^2, k^2 - m^2, m^2) &= \delta(k^2 - m^2) \\ &+ \int_0^{Q^2} \frac{d\tilde{q}^2}{\tilde{q}^2} \int_0^1 dz\, P_{QQ}\big[\alpha_s(z(1-z)\tilde{q}), z, m\big]\,\theta\Big(\tilde{q}^2 - \frac{Q_0^2 + m^2(1-z)^2}{z^2(1-z)^2}\Big) \\ &\times \Big[z J\big(z^2\tilde{q}^2, z(k^2 - m^2) - z^2(1-z)\tilde{q}^2\big) - J\big(\tilde{q}^2, k^2 - m^2\big)\Big] \end{aligned}$$

(C) Angular ordered parton shower (Herwig)

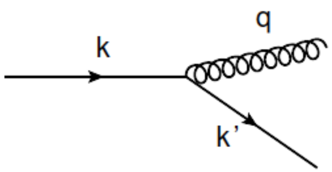
Parton level cross section

Catani, Trentadue, Turnock Webber (1993)

$$\frac{d\hat{\sigma}}{d\tau} = \int dk^2\, dk'^2\, \delta(\tau - \frac{k^2 + k'^2}{Q^2})\, J(Q^2, k^2) J(Q^2, k'^2)$$

AHH, Plätzer, Samitz (2018)

- Agrees exactly with partonic cross section obtained from analytic factorized SCET calculations at NLL!
- CB is NLL precise for inclusive event shapes.
- For massless quarks <u>and</u> massive quarks



- <u>Analytic calculation:</u> for vanishing shower cutoff Q_0=0: $m_t^{MC} = m_t^{pole}$ (one-shell self energy contribution does not arise in CB!)

BUT: Parton showers in MC generators have an finite shower cutoff Q_0 to prevent infinite multiplicities $\rightarrow$ <u>acts as finite resolution scale that is physical for the MC</u>

- We track the dominant <u>linear dependence on Q_0</u> from large-angle soft and ultra-collinear (=soft in top rest frame) radiation
- <u>Matches analogous results from analytic factorization theorem</u>
- Realized accurately by Herwig's shower

$$q_\perp > Q_0$$

Linear Shower Cutoff Dependence

Massless quarks: (effects on large-angle soft radiation)

AHH, Plätzer, Samitz (2018)

$$\frac{d\hat{\sigma}}{d\hat{\tau}}(\hat{\tau}, Q, Q_0) = \frac{d\hat{\sigma}}{d\hat{\tau}}(\hat{\tau}, Q) + \frac{1}{Q}\Delta_{\rm soft}(Q_0)\,\frac{d^2\hat{\sigma}}{d\hat{\tau}^2}(\hat{\tau}, Q)$$

$$= \frac{d\hat{\sigma}}{d\hat{\tau}}\left(\hat{\tau} + \frac{1}{Q}\Delta_{\rm soft}(Q_0), Q\right)$$

$$\Delta_{\rm soft}(Q_0) = 16\,Q_0\,\frac{\alpha_s(Q_0)C_F}{4\pi} + \mathcal{O}(\alpha_s^2(Q_0))$$

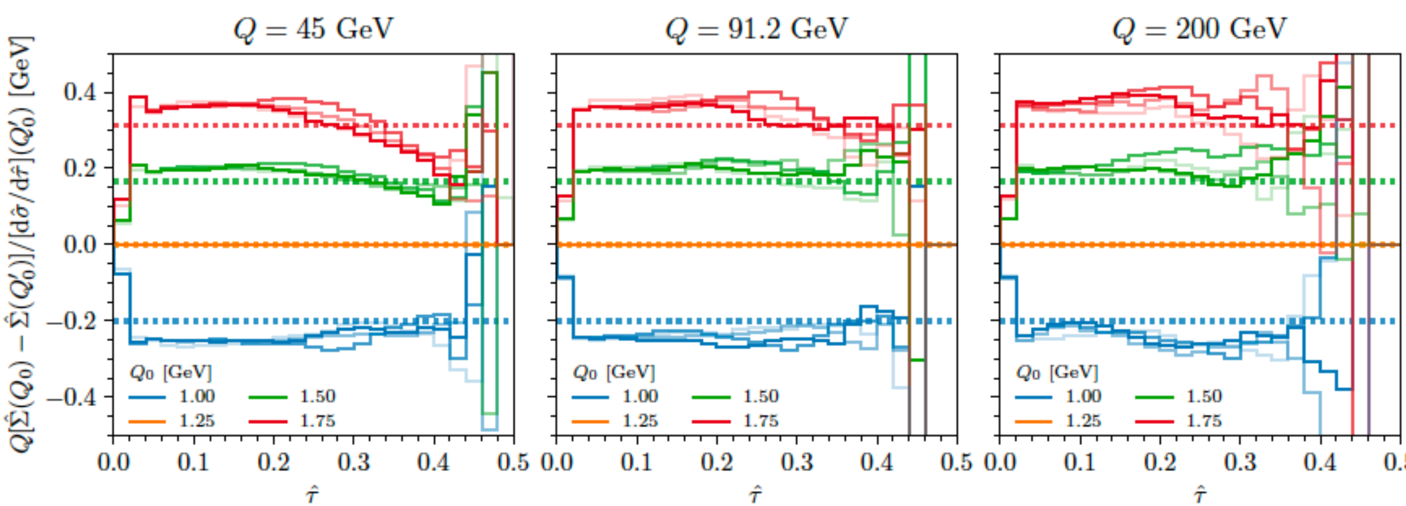
$$Q\,\frac{\hat{\Sigma}(\hat{\tau}, Q, Q_0) - \hat{\Sigma}(\hat{\tau}, Q, Q_0')}{\frac{d\hat{\sigma}}{d\hat{\tau}}(\hat{\tau}, Q, Q_0')} = \Delta_{\rm soft}(Q_0, Q_0')$$

→ 2-jettiness cumulant distribution:

$$\Delta_{\rm soft}(Q_0, Q_0') = 16\int_{Q_0'}^{Q_0} dR\,\left[\frac{\alpha_s(R)C_F}{4\pi}\right]$$

Herwig CB shower versus pQCD:

(Herwig 'true' parton level had to be added)



Different lines: different matrix element and matching schemes

Linear Shower Cutoff Dependence

AHH, Plätzer, Samitz (2018)

Massive quarks: (effects on large-angle-soft + ultra-collinear radiation)

Modifies pole of top propagator away from m_t^{pole} :

$m_t^{pole} \rightarrow m_t(Q_0) = m_t^{pole} - \delta m(Q_0)$, $\delta m(Q_0) = 2/3\ \alpha_s(Q_0)\ Q_0 + \ldots$

→ 2-jettiness resonance position:

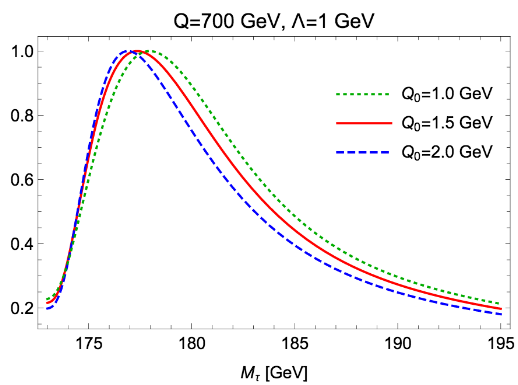
$$\frac{d}{d\ln Q_0}\tau_{\rm peak}^{\rm parton}(Q_0) = \frac{C_F\alpha_s(Q_0)}{4\pi}\frac{Q_0}{Q}\left[16 - 8\pi\frac{m_t}{Q}\right]$$

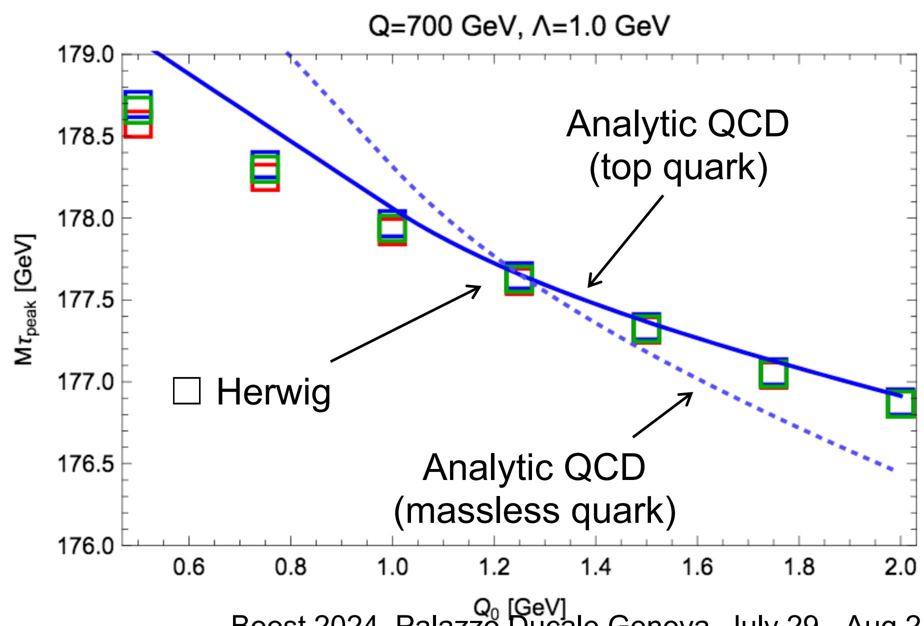
both linear Q_0-contributions cancel

large-angle soft

Must be compensated by hadronization corrections in S_{mod}

ultra-collinear (from all radiation except self-energy)

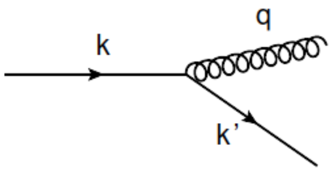




(C) Angular ordered parton shower (Herwig)

AHH, Plätzer, Samitz (2018)

For inclusive jet-mass-related event shapes the Herwig top mass parameter represents a Q_0-dependent mass scheme that can be related to other mass schemes at NLO:



$$q_\perp > Q_0$$

$$m_t^{\text{CB}}(Q_0) = m_t^{\text{pole}} - \frac{2}{3} Q_0 \alpha_s(Q_0) + \mathcal{O}(\alpha_s(Q_0)^2)$$

$$m_t^{\text{CB}}(Q_0) = m_t^{\text{MSR}}(Q_0) - \frac{2}{3}\left(1 - \frac{2}{\pi}\right) Q_0 \alpha_s(Q_0) + \mathcal{O}(\alpha_s^2(Q_0))$$

(1) Does this survive the hadronization model?

→ Hadron level simulations should be Q_0-independent

→ Shower cut has to be considered as a factorization scale and its proper control in QCD is essential to control parton level and hadronization separately.

(2) How universal is the result? → Needs careful additional work and similar analyses for other types of observables.

(D) Factorization compatible hadronization model

AHH, Jin, Plätzer, Samitz arXiv:2404.09856

Standard shower cut treatment for all MC generators:

- Shower-cutoff scale Q_0 = one of many hadronization model parameters

BUT: To gain control over the shower's top mass parameter:

Plätzer arXiv:2204.06956

- The shower-cutoff scale Q_0 must be promoted to a factorization scale,
  → hadron level descriptions are shower-cut independent.
- We must scrutinize the hadronization model to satisfy the constraints from pQCD concerning its behavior and shower-cut dependence
- For 2-jettiness: tuning for different Q_0 values (including top mass sensitive data) must yield a Q_0-dependent MC top mass parameter consistent with $m_t^{CB}(Q_0)$

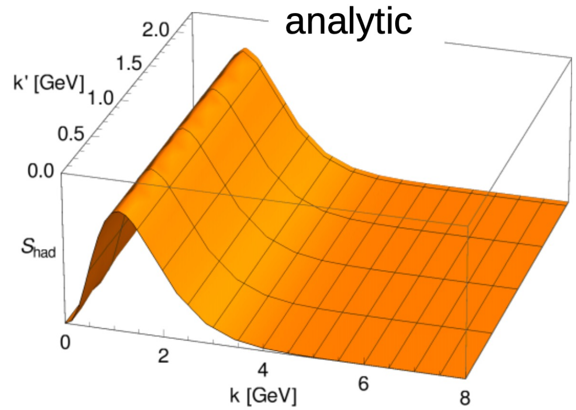
(D) Factorization compatible hadronization model

AHH, Jin, Plätzer, Samitz arXiv:2404.09856

This implies non-trivial QCD constraints on the properties of the migration matrix:

$$\frac{\mathrm{d}\sigma}{\mathrm{d}\tau}(\tau, Q) = \int \mathrm{d}\hat{\tau}\, \frac{\mathrm{d}\hat{\sigma}}{\mathrm{d}\hat{\tau}}(\hat{\tau}, Q)\; T(\tau, \hat{\tau}, \{Q, Q_0\}))$$

$$T\left(\frac{k}{Q} = \tau - \hat{\tau}, \frac{k'}{Q} = \hat{\tau}, \{Q, Q_0\}\right)$$



(1) Transfer matrix should have this form:

$$T(\tau, \hat{\tau}, Q, Q_0) = T(\tau - \hat{\tau}, Q_0) = Q S_{\mathrm{mod}}\left(\frac{\tau - \hat{\tau}}{Q}\right)$$

(2) Q_0-dependence of the first moment constrained at NLO QCD:

$$\Omega_1(Q_0) \equiv \frac{1}{2}\int \mathrm{d}\ell\, \ell\, S_{\mathrm{had}}(\ell, Q_0)$$

$$\Omega_1(Q_0{\prime}) = \frac{1}{2}\Delta_{\mathrm{soft}}(Q_0', Q_0) + \Omega_1(Q_0)$$

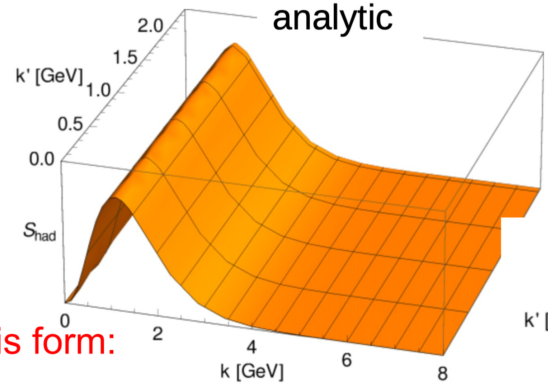
(D) Factorization compatible hadronization model

Results from Q_0-tuned MC simulations: default model

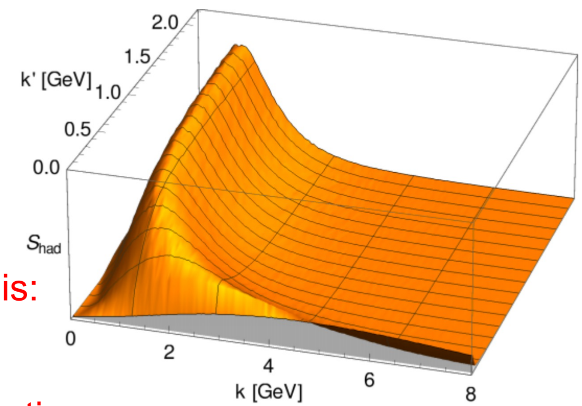
AHH, Jin, Plätzer, Samitz
arXiv:2404.09856

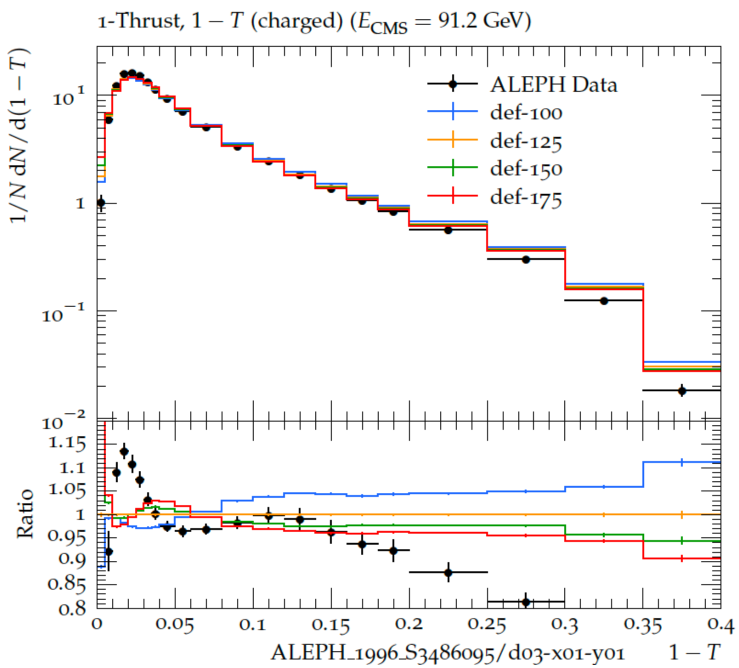
$$T\left(\frac{k}{Q} = \tau - \hat{\tau}, \frac{k'}{Q} = \hat{\tau}, \{Q, Q_0\}\right)$$

migration matrix should have this form:



But it actually looks like this:





Peak region hadronization inconsistent with QCD factorization!

Description of observables at hadron level not quite shower-cutoff independent (Thrust at $Q=M_z$)

Q_0 = (1.00, 1.25, 1.50, 1.75) GeV

(Reference data for tune: Simulation for Q_0=1.25 GeV)

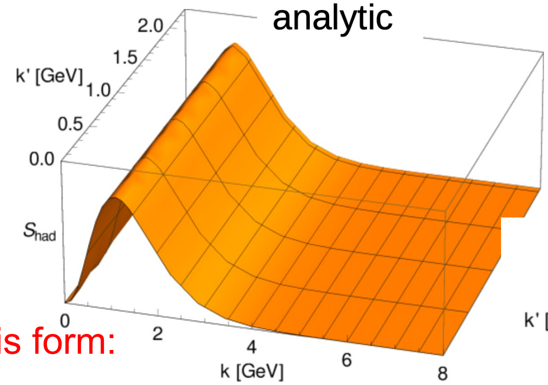
(D) Factorization compatible hadronization model

Results from Q_0-tuned MC simulations: Default model

AHH, Jin, Plätzer, Samitz
arXiv:2404.09856

$$T\left(\frac{k}{Q}=\tau-\hat{\tau},\frac{k'}{Q}=\hat{\tau},\{Q,Q_0\}\right)$$

migration matrix should have this form:



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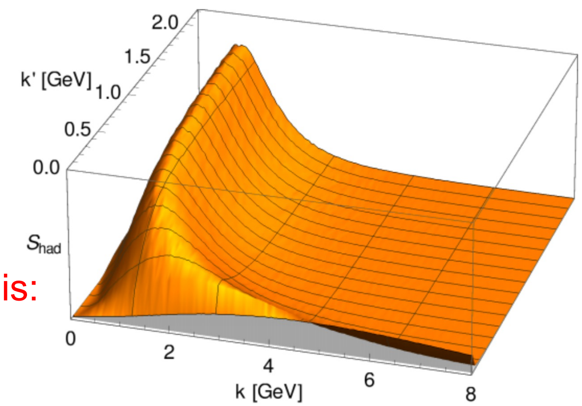
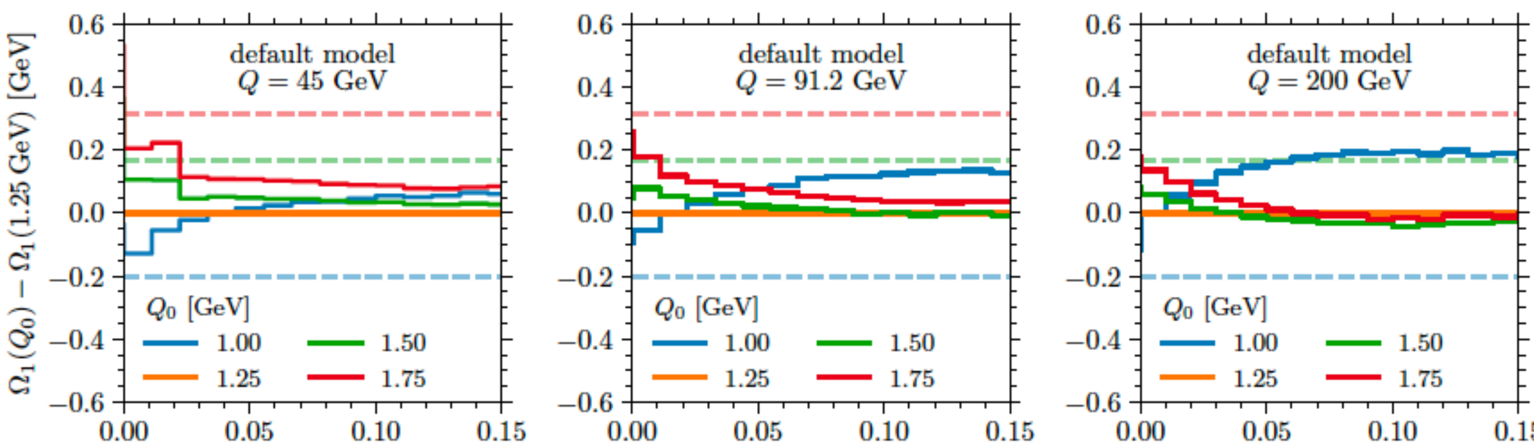


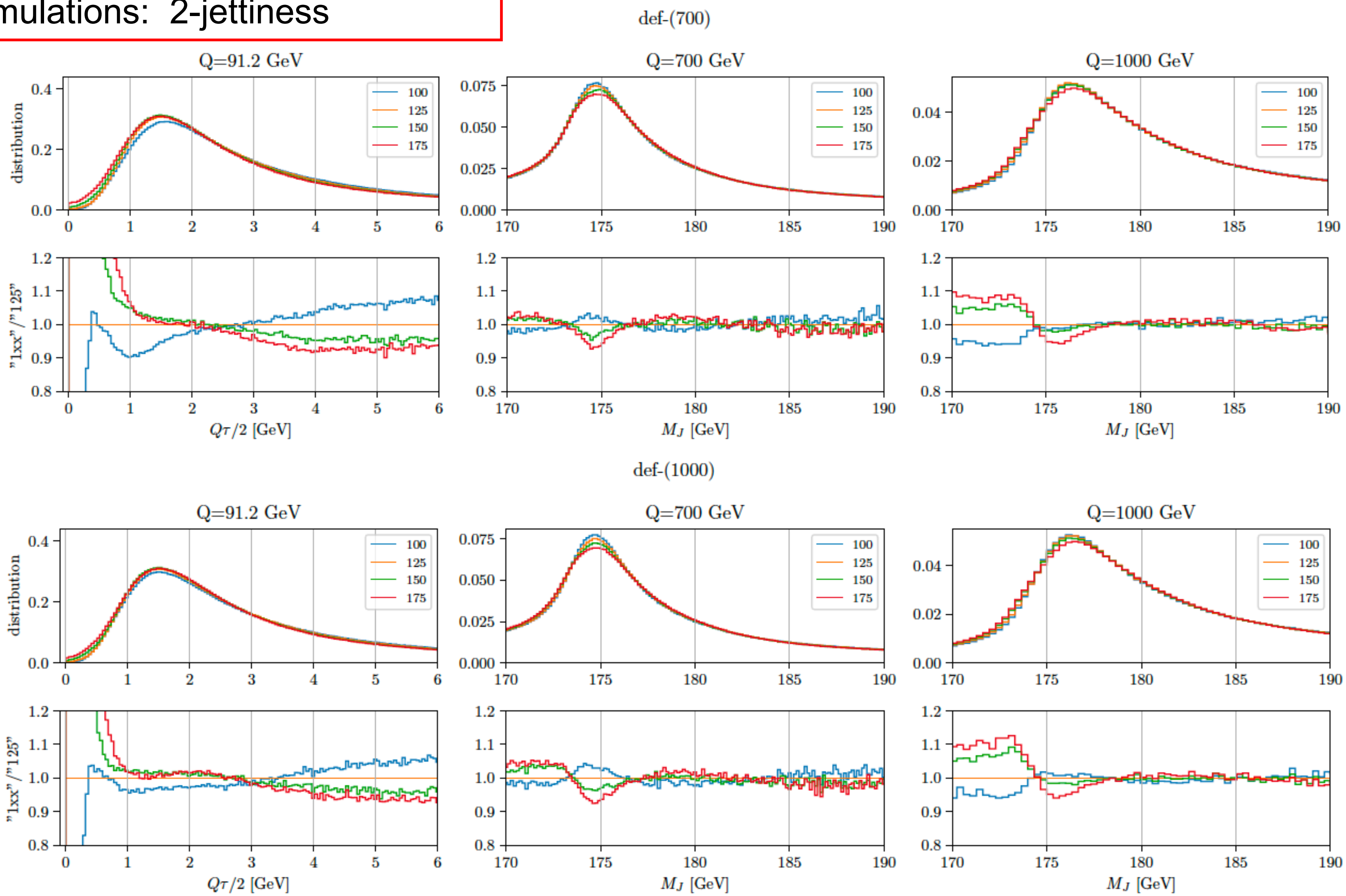
First moment does not satisfy the NLO QCD Q_0- evolution well



(D) Factorization compatible hadronization model

Predictions from Q_0-tuned MC simulations: 2-jettiness

AHH, Jin, Plätzer, Samitz
to appear

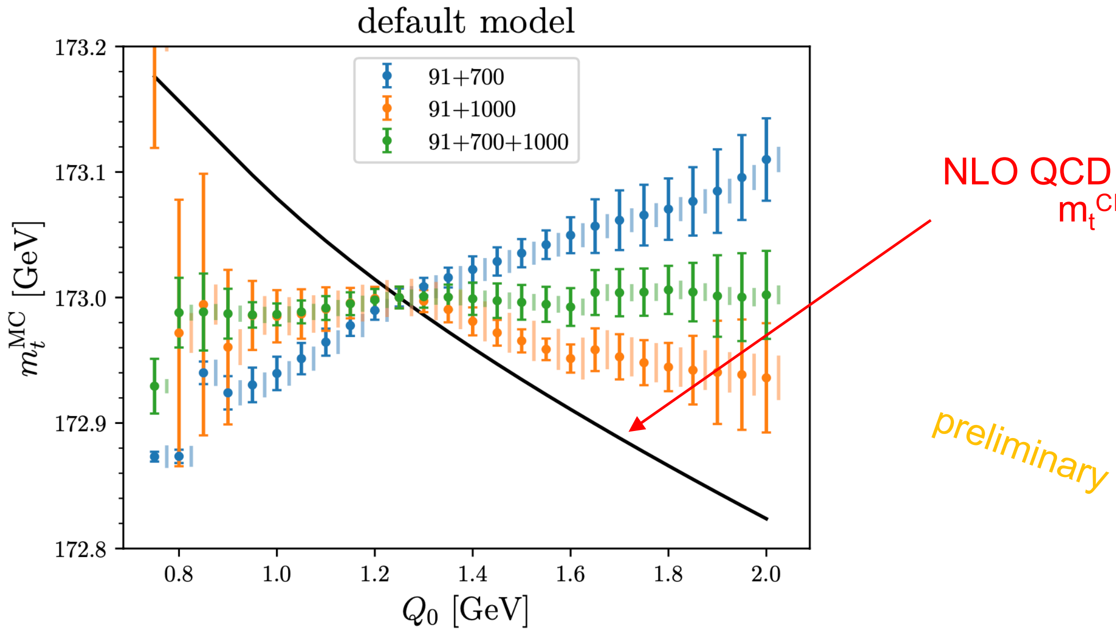


(D) Factorization compatible hadronization model

AHH, Jin. Plätzer, Samitz to appear

Q$_0$-dependent tunes m_t^{MC} :

- Also tune the top mass parameter m_t^{MC} for different Q_0 values (to reference data generated for Q_0=1.25 GeV



Default Herwig hadronization model modifies m_t^{MC} in an unphysical way incompatible with QCD factorization: uncertainty ~ 0.5 GeV

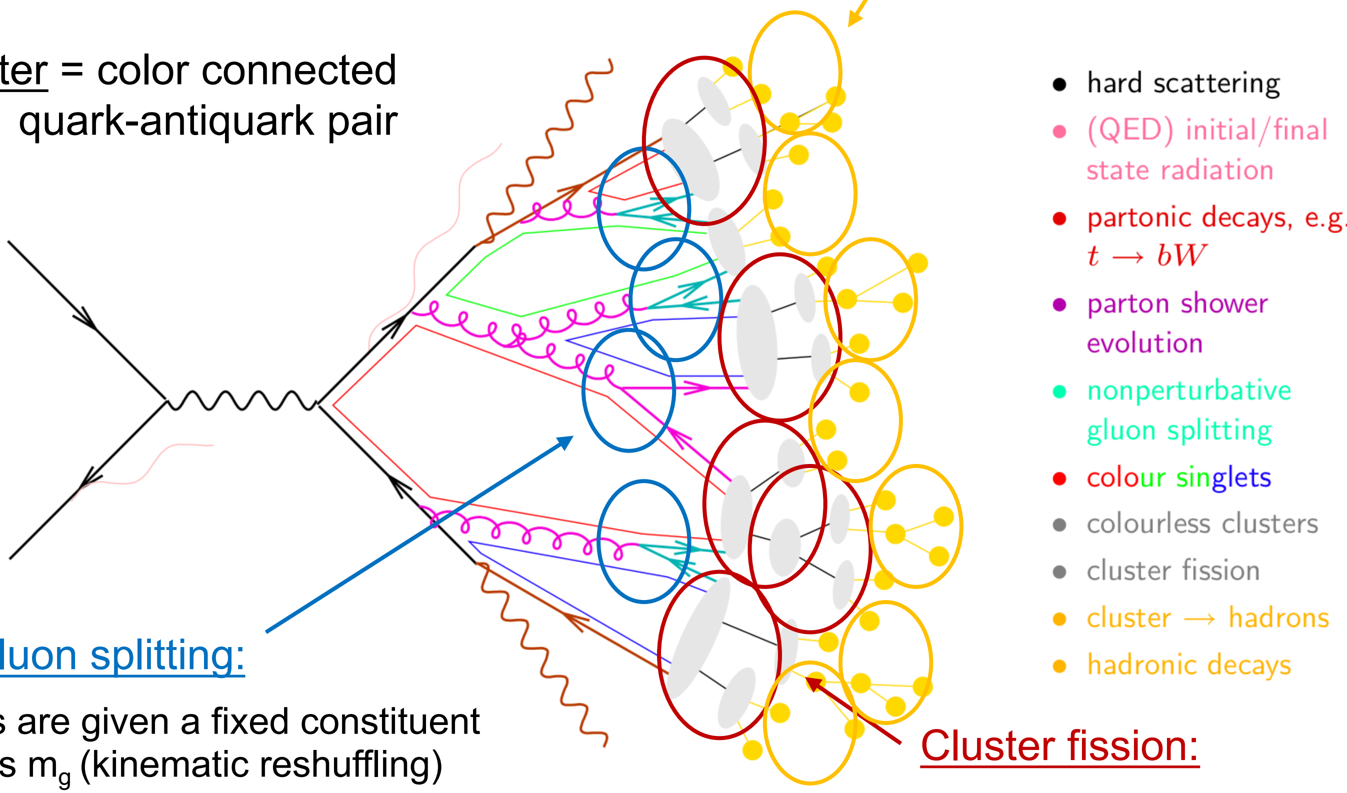
→ $m_t^{Herwig}(Q_0) \neq m_t^{CB}(Q_0)$ for the default hadronization model

(D) Factorization compatible hadronization model

Cluster hadronization model (basics, no details):

Cluster = color connected quark-antiquark pair

Hadron formation and decays



Forced gluon splitting:

- Gluons are given a fixed constituent masses m_g (kinematic reshuffling)
- Isotropic decay into light qqbar pair in gluon rest frame

Cluster fission:

- Cluster fission as a 1-dim process along the qqbar axis
- Adhoc functional ansatz for cluster mass distribution

➡ Ad hoc modelling: not designed to adapt Q_0

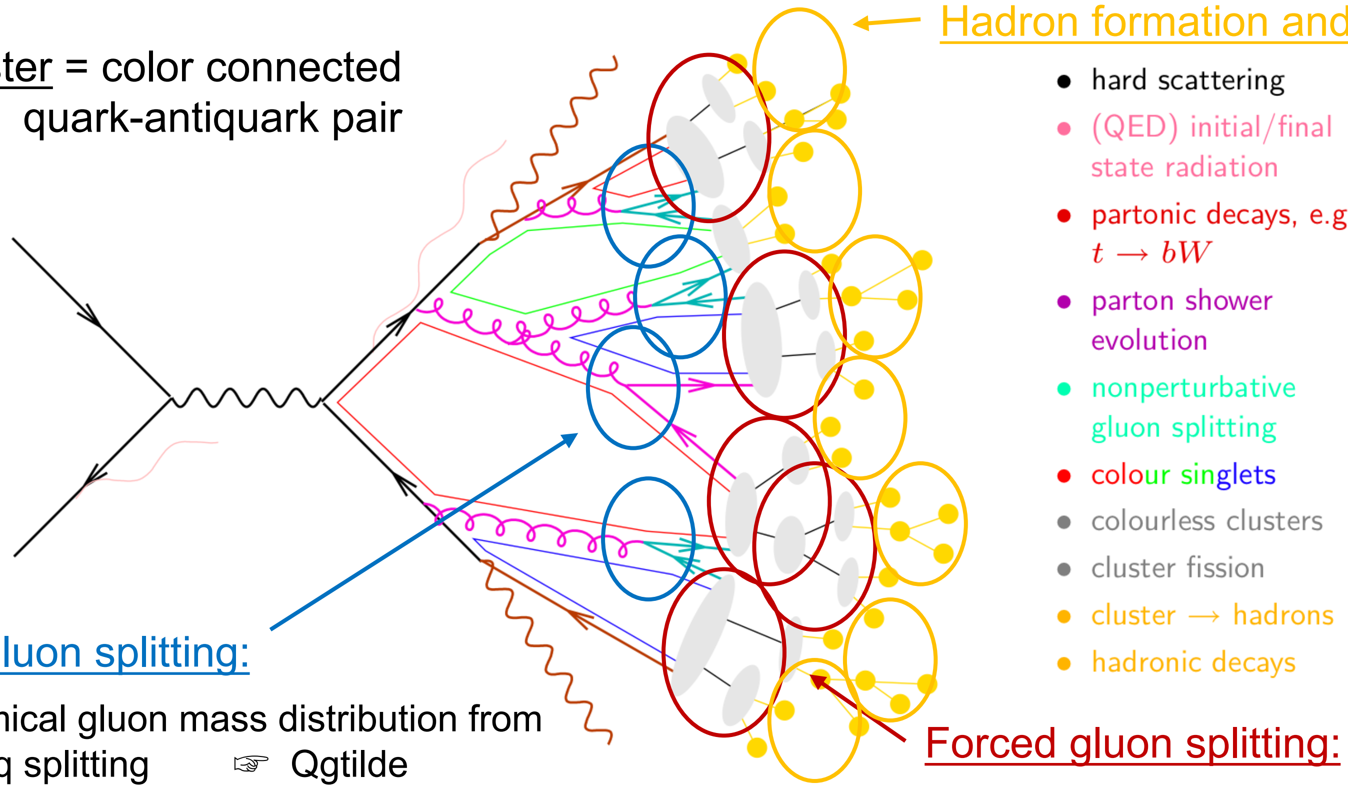
(D) Factorization compatible hadronization model

AHH, Jin. Plätzer, Samitz 2024.09856

Modified cluster hadronization that mimics aspects of parton shower dynamics:

Cluster = color connected quark-antiquark pair

Hadron formation and decays



Forced gluon splitting:

- Dynamical gluon mass distribution from g → qq splitting ☞ Qgtilde
- Kinematics in analogy to parton shower

Forced gluon splitting:

- Cluster splitting from branching q → q g and splitting g → qq ☞ Qqtilde
- Kinematics in analogy to the parton shower

➡ Model parameters can consistently adapt to changes of Q_0

Q_0-dependent tuning analyses

AHH, Jin, Plätzer, Samitz
arXiv:2404.09856

Tuning software: APPRENTICE

Reference tune = standard e^+e^- tune (Z-pole LEP data [3180 observable bins]

Reference data = simulated data for Q_0= 1.25 GeV for

- Z-pole LEP data [3180]
- Z-pole 2-jettiness [peak region]
- ttbar 2-jettiness at E_{cm} = 700 and 1000 GeV [peak region]

Q_0-dependent tunes: tunes to reference data for different shower cut Q_0 values

Tuned parameters: 6 tuning parameters + m_t^{MC}

Default model

- m_g (force gluon splitting)
- PSplit (cluster fission, mass distr.)
- Cl_{max} (cluster fission, condition)
- Cl_{pow} (cluster fission, condition)
- PwtSquark (cluster hadronization)
- PwtDIquark (cluster hadronization)

Dynamic model

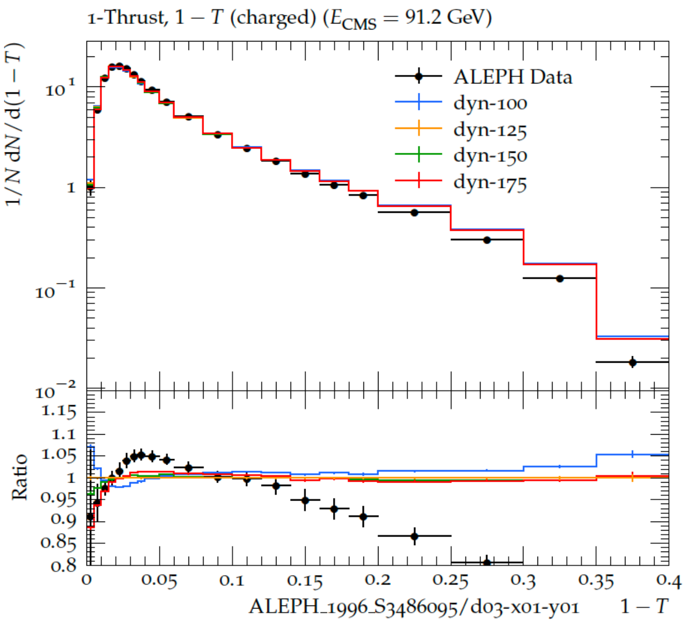
- Qgtilde (forced gluon splitting)
- Qqtilde (cluster fission splitting)
- Cl_{max} (cluster fission, condition)
- Cl_{pow} (cluster fission, condition)
- PwtSquark (cluster hadronization)
- PwtDIquark (cluster hadronization)

Interpolation grids: cubic and quartic polynomials

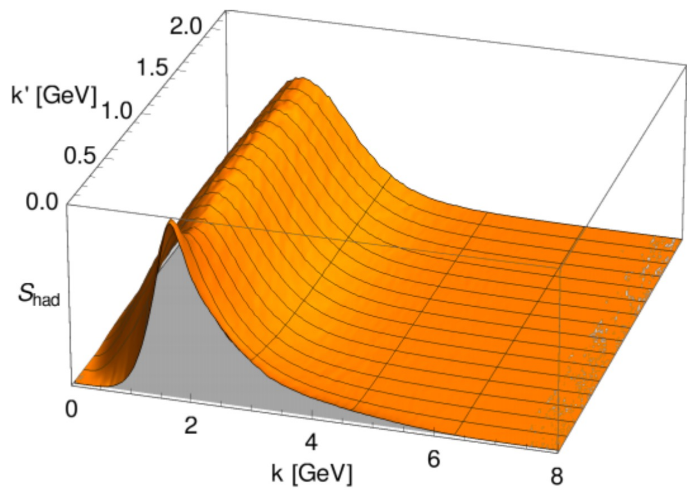
(D) Factorization compatible hadronization model

AHH, Jin. Plätzer, Samitz to appear

Migration function much better consistent with QCD factorization



Observables much less dependent on Q_o



Tunes m_t^{MC} fully consistent with expectations from analytic QCD calculation

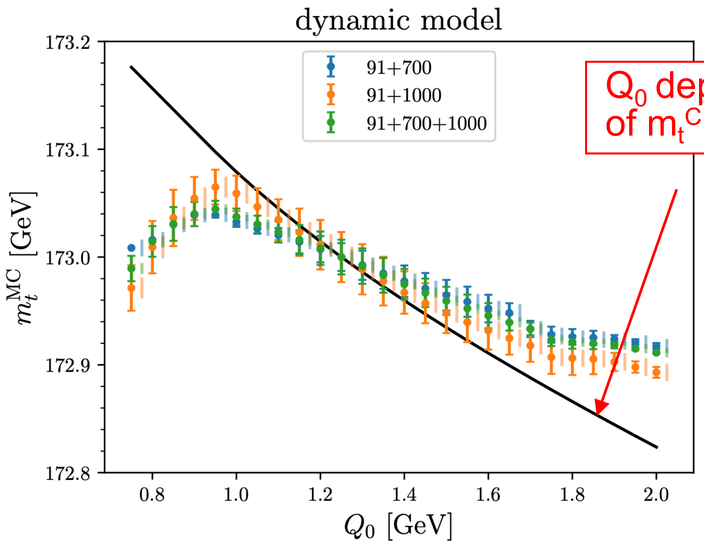
(“pseudo data” generated for Q_0=1.25 GeV)

$\Rightarrow$ $m_t^{Herwig}(Q_0) = m_t^{CB}(Q_0)$

within a precision of better than 50 MeV

Thrust

preliminary

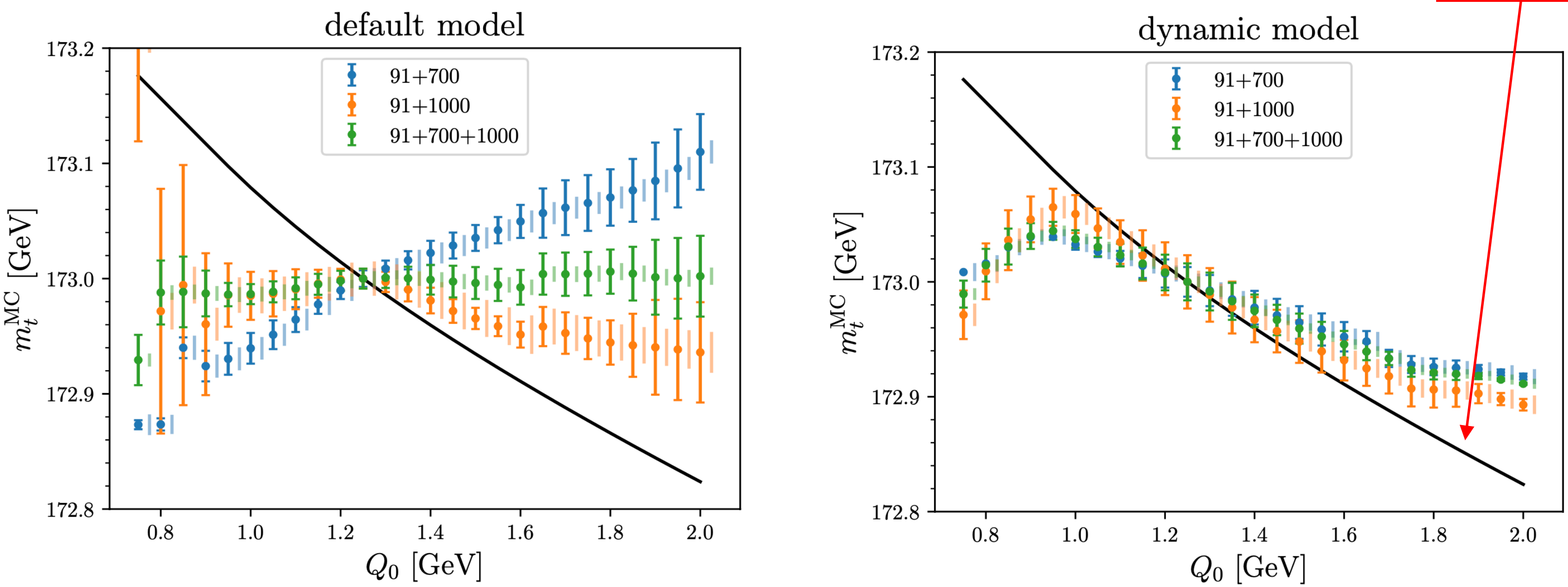


Q_0 dependence of $m_t^{CB}(Q_0)$

Old Default Model vs. New Dynamical Model

AHH, Jin. Plätzer, Samitz to appear

Shower cutoff dependence of tuned MC top quark mass to reference data including top quark 2-jettiness distributions at 700 and/or 1000 GeV



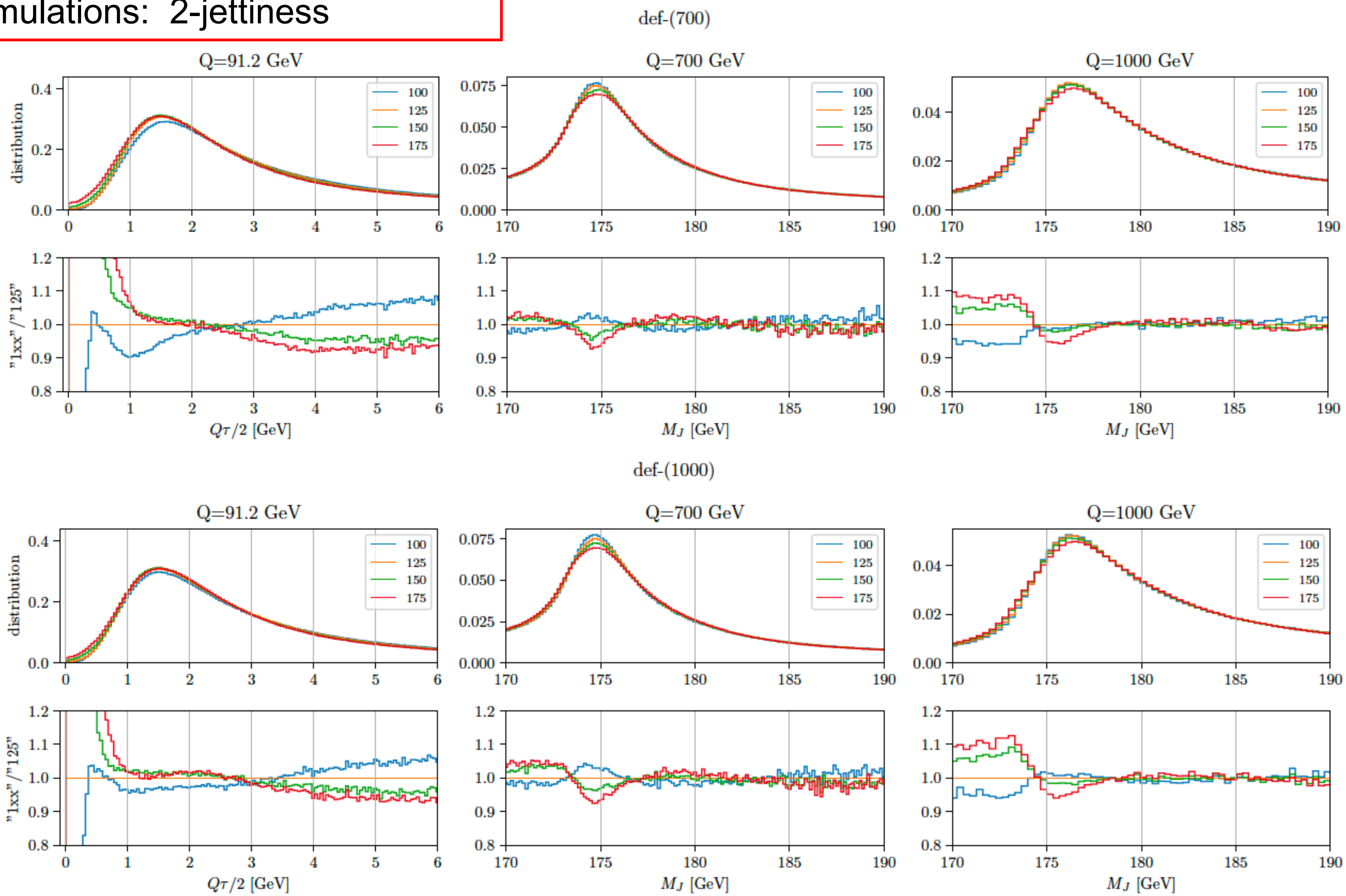
Q_0 dependence expected from $m_t^{CB}(Q_0)$

Agreement of m_t^{MC} with $m_t^{CB}(Q_0)$ within 50 MeV !

Old Default Model vs. New Dynamical Model

AHH, Jin, Plätzer, Samitz
to appear

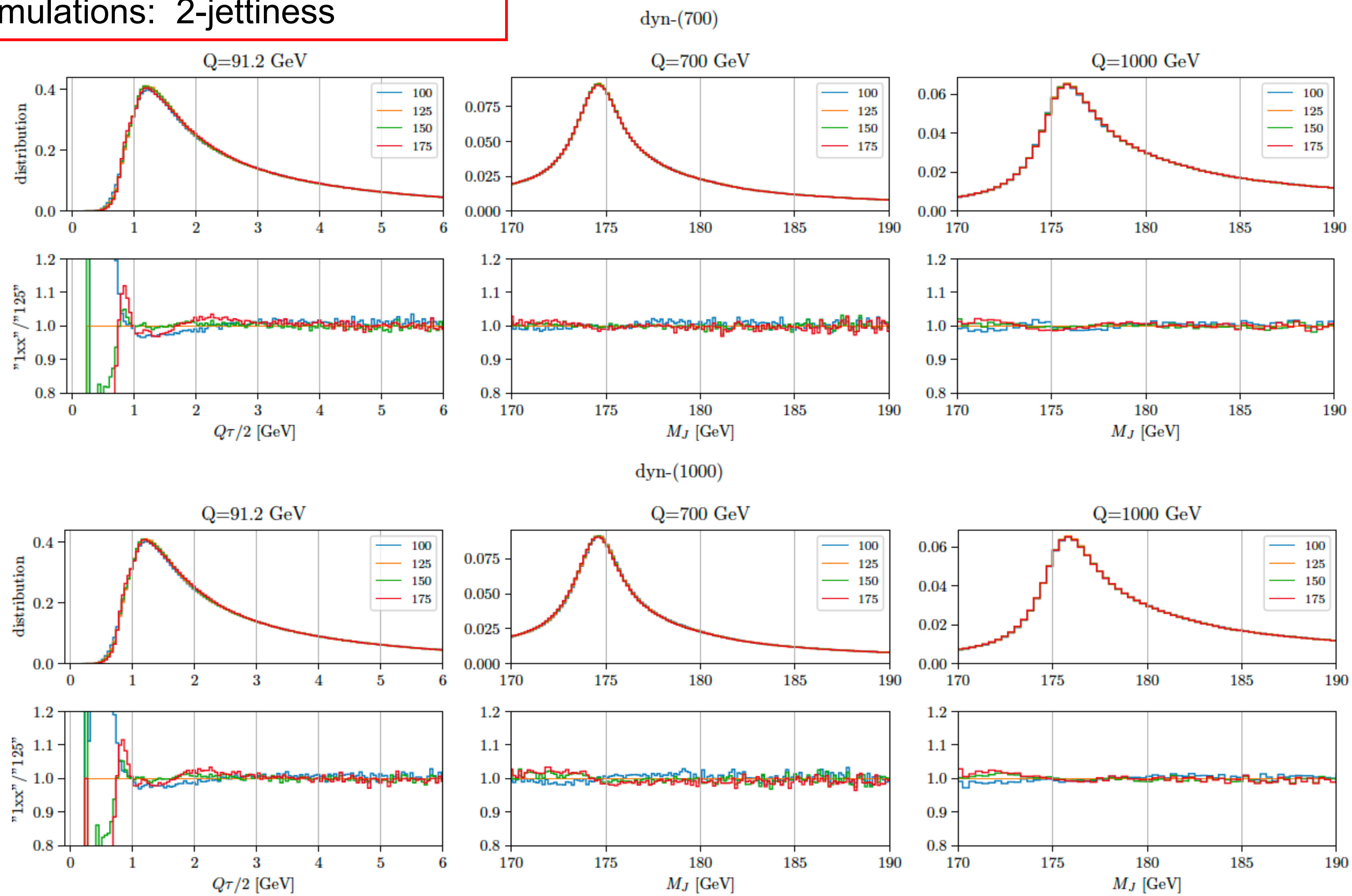
Predictions from Q_0-tuned MC simulations: 2-jettiness



Old Default Model vs. New Dynamical Model

AHH, Jin, Plätzer, Samitz
to appear

Predictions from Q_0-tuned MC simulations: 2-jettiness

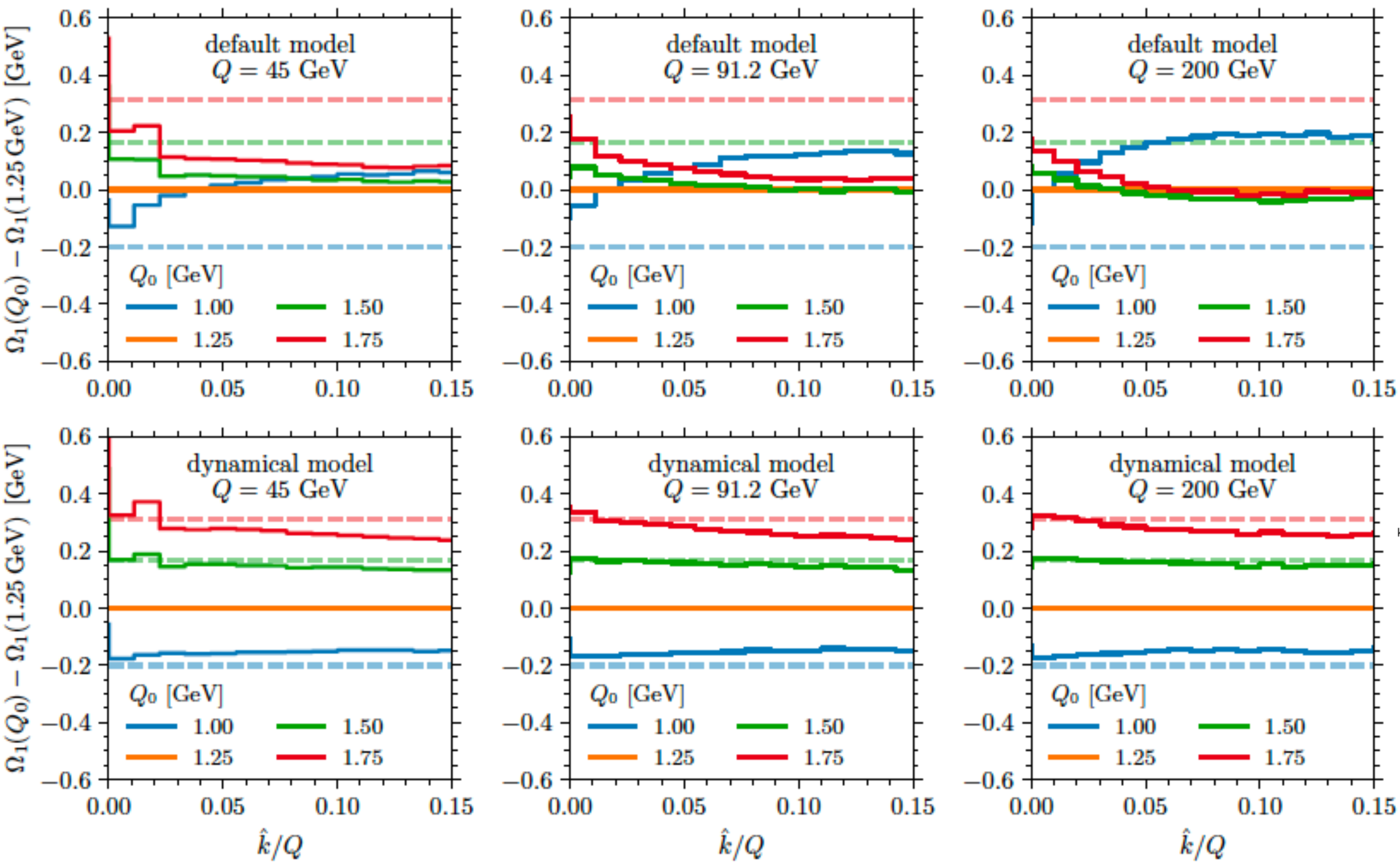


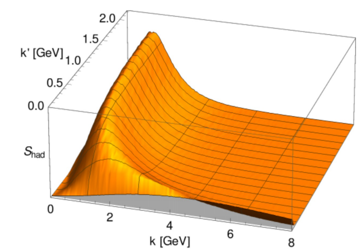
Old Default Model vs. New Dynamical Model

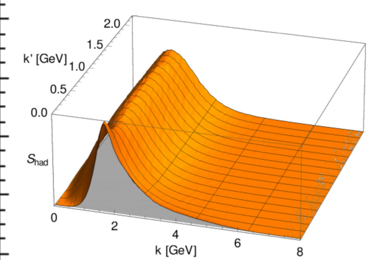
AHH, Jin. Plätzer, Samitz 2404.09856

Shower cutoff dependence of <u>first moment Ω_1 of migration matrix</u> from simulations for 2-jettiness → "MC scheme for hadronization correction"

$$\Omega_1^{\rm MC}(\hat{k}, Q, Q_0) - \Omega_1^{\rm MC}(\hat{k}, Q, Q_{0,\rm ref} = 1.25\,\mathrm{GeV})$$







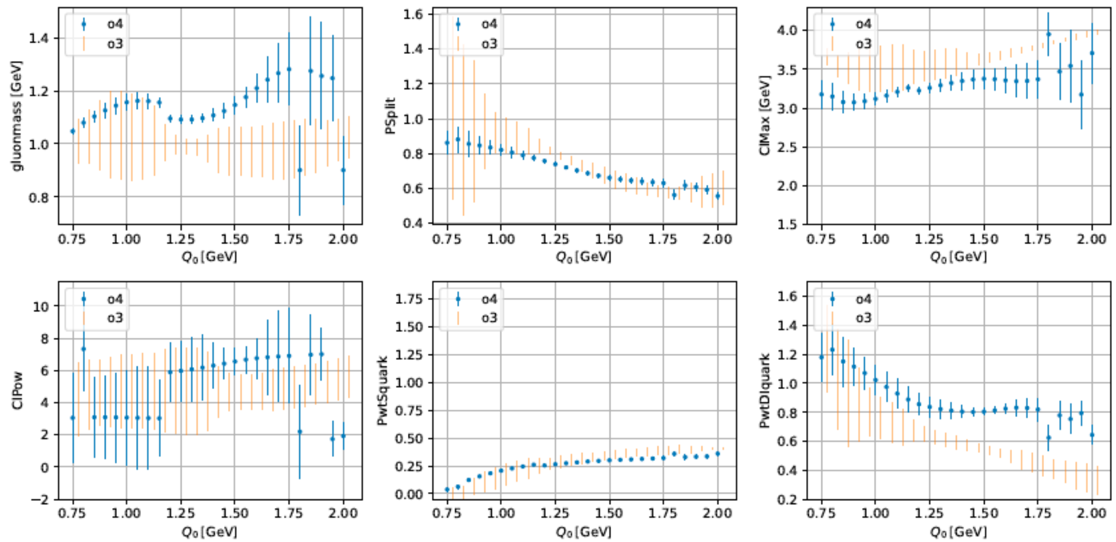
Thrust

Old Default Model vs. New Dynamical Model

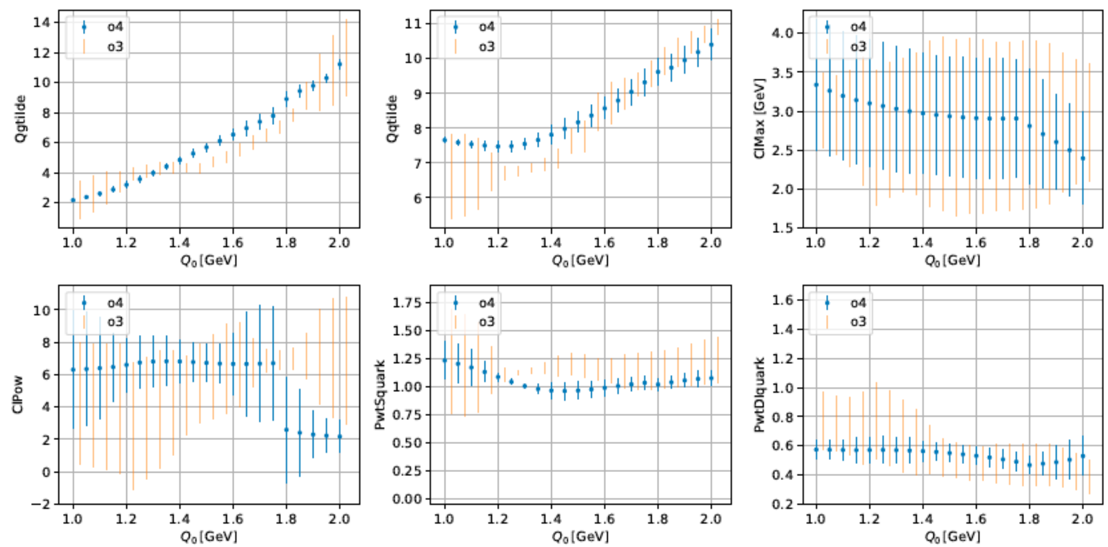
Tuned parameters for Q_0-dependent tuning analyses (apart from m_t^{MC})

AHH, Jin, Plätzer, Samitz
arXiv:2404.09856

Default model



Dynamical model



Final remarks and Outlook

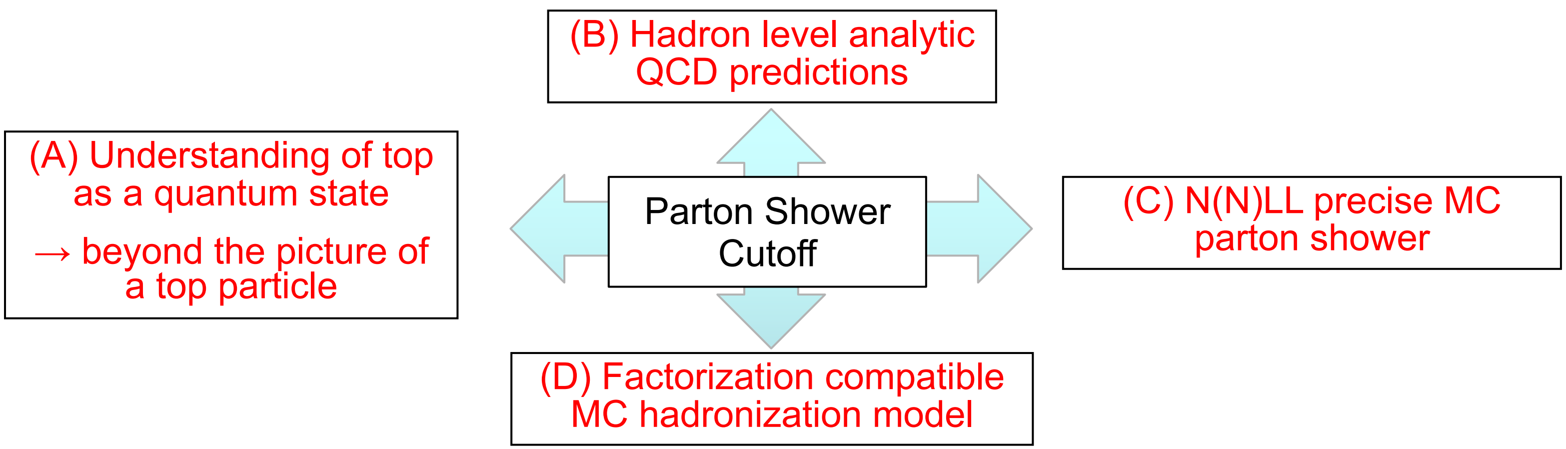
→ **Proof-of-principle:** It is possible to promote the MC top mass parameter m_t^{MC} to a renormalization scheme so that its NLO relation to any other top mass renormalization scheme can be calculated.

→ $m_t^{MC} = m_t^{CB}(Q_0)$

→ Key aspect: Parton shower cutoff Q_0 = Factorization scale separating pQCD and npQCD

→ Currently: Concretely working machinery available only for e^+e^- event-shapes via tuning analyses for different Q_0 values

→ The realization of (A)-(D) in this work provides a concrete blueprint that can now be applied to other classes of observables more closely related to direct measurements.



Final remarks and Outlook

- Main aim of future work: Generalization and study of universality
  → conceptual insights and applications for top mass and beyond
    e.g. MC Hadronization corrections with controlled scheme dependence
  → complements general developments of MCs towards becoming QCD tools

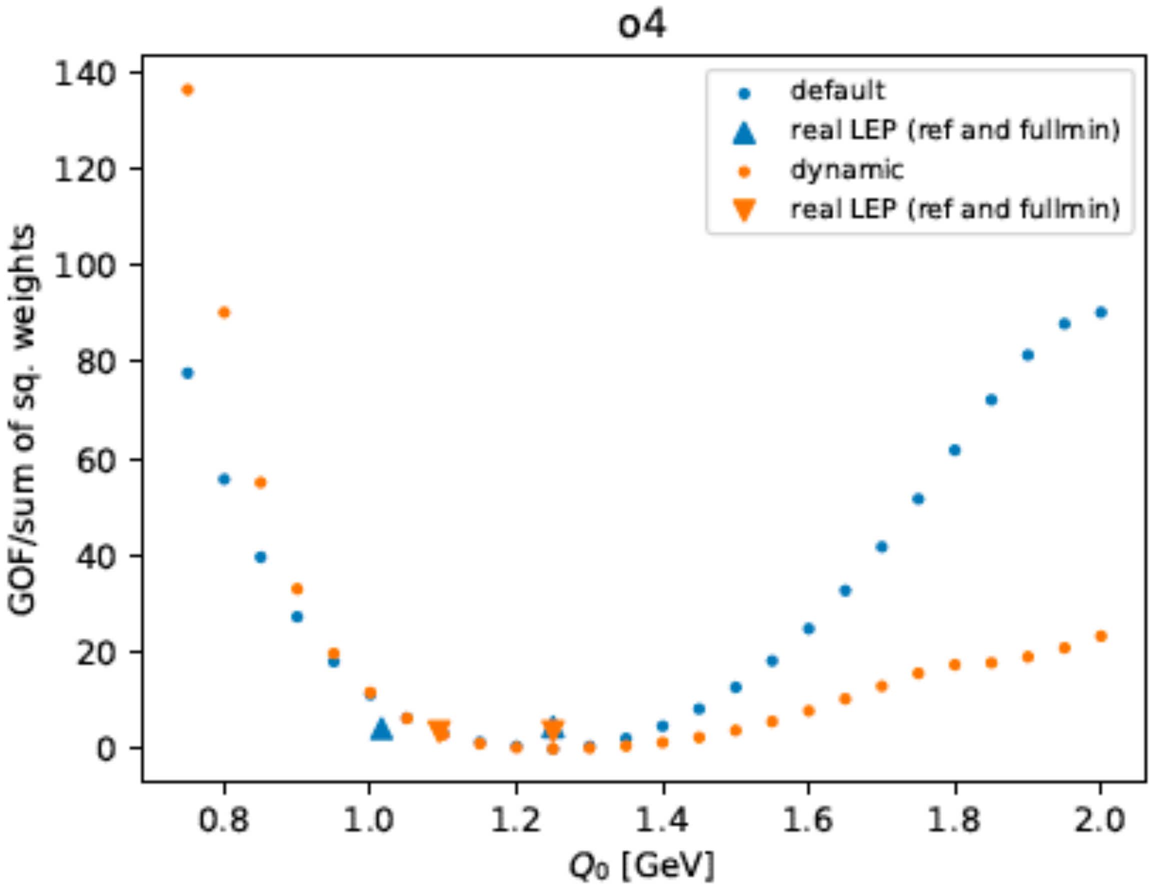
- Future plans:
  - investigate dipole showers (N(N)LL), string hadronization (Pythia)
  - investigate other shower cutoff prescriptions
  - other observables, e.g. differential in top decay (→ e.g. $M_{\text{b-jet lepton}}$)
    energy correlators
    → IR sensitivity & non-perturbative corrections
  - long-term aim: b-jets with small jet radius (non-global)
  - establish a m_t^{MC} verification tool box
    → final approach may be not as elaborate as shown in this talk

- Cetero censeo: MPI and UE hadronization models still needs to be better understood from the QCD perspective

Old Default Model vs. New Dynamical Model

AHH, Jin, Plätzer, Samitz arXiv:2404.09856

Shower cutoff Q_0 minimal χ^2-values obtained in the tuning fits



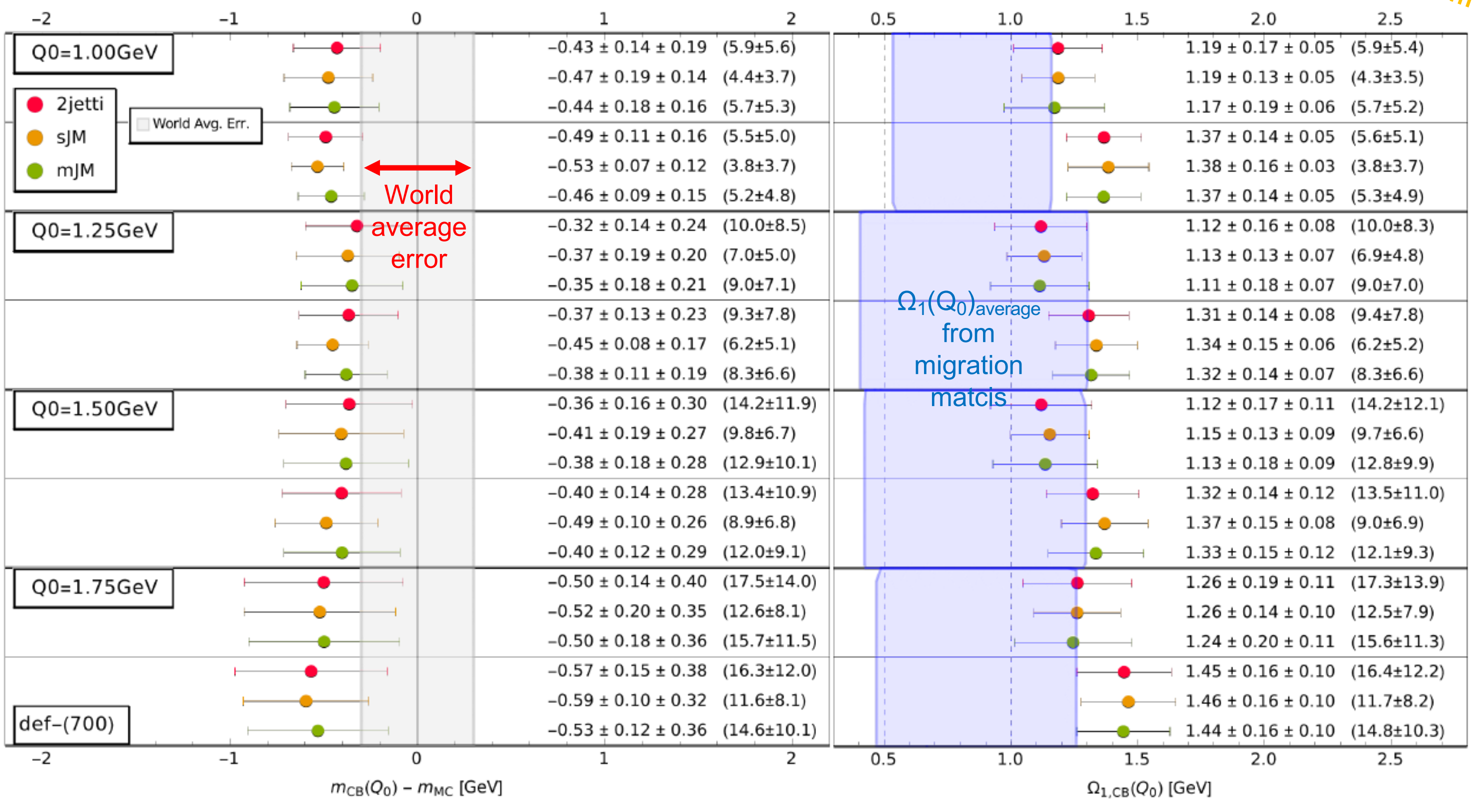
Old Default Model vs. New Dynamical Model

AHH, Jin. Plätzer, Samitz to appear

Cross check: apply top mass calibration to determine $m_t^{CB}(Q_0)$

preliminary

default model



Default: m_t^{MC} incompatible with $m_t^{CB}(Q_0)$

First moment of migration matrix with large variations, Q_0-evolution not visible

Dynamical: m_t^{MC} compatible with $m_t^{CB}(Q_0)$

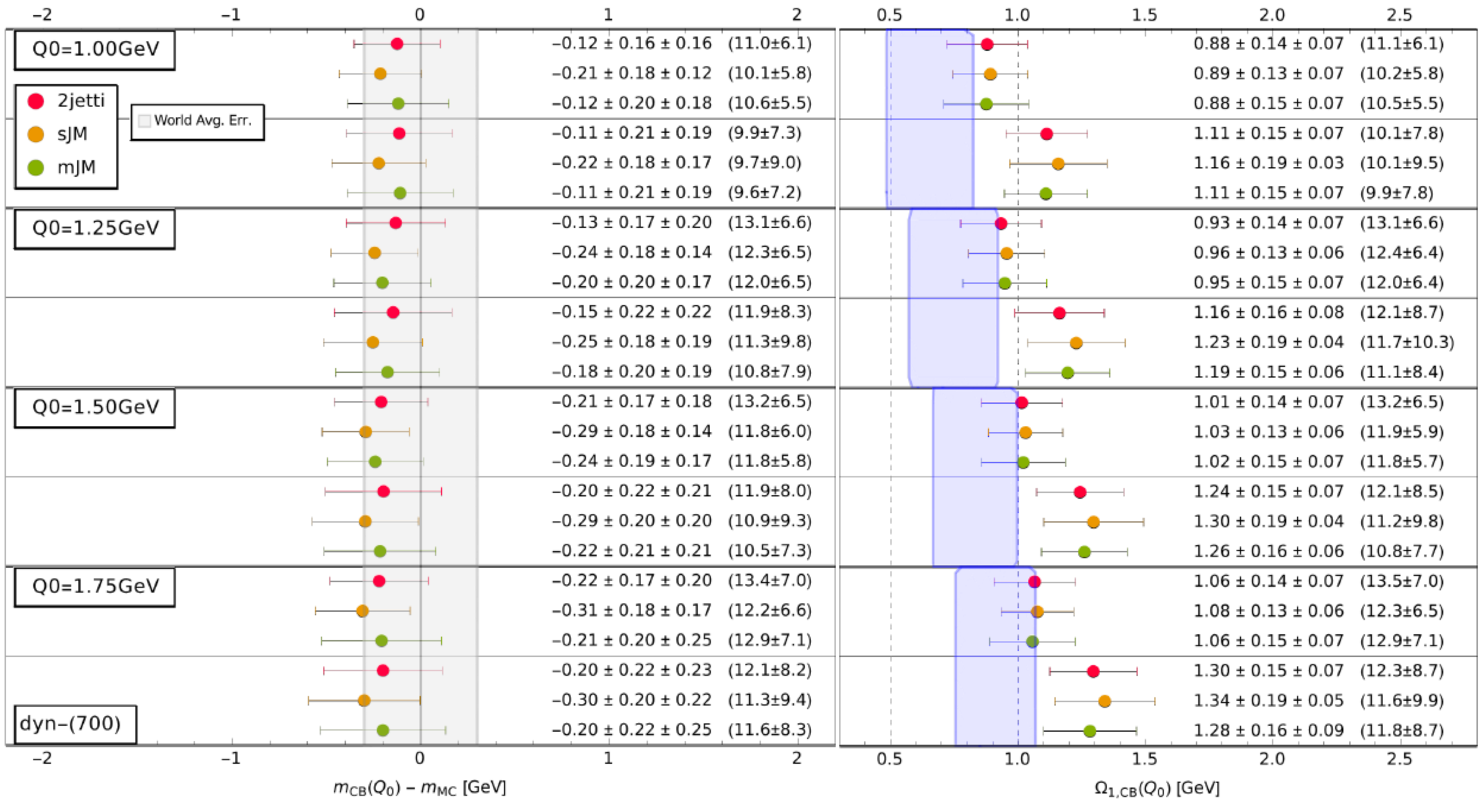
First moment of migration matrix with smaller variations, Q_0-evolution clearly visible

Old Default Model vs. New Dynamical Model

AHH, Jin. Plätzer, Samitz to appear

Cross check: apply top mass calibration to determine $m_t^{CB}(Q_0)$

dynamical model



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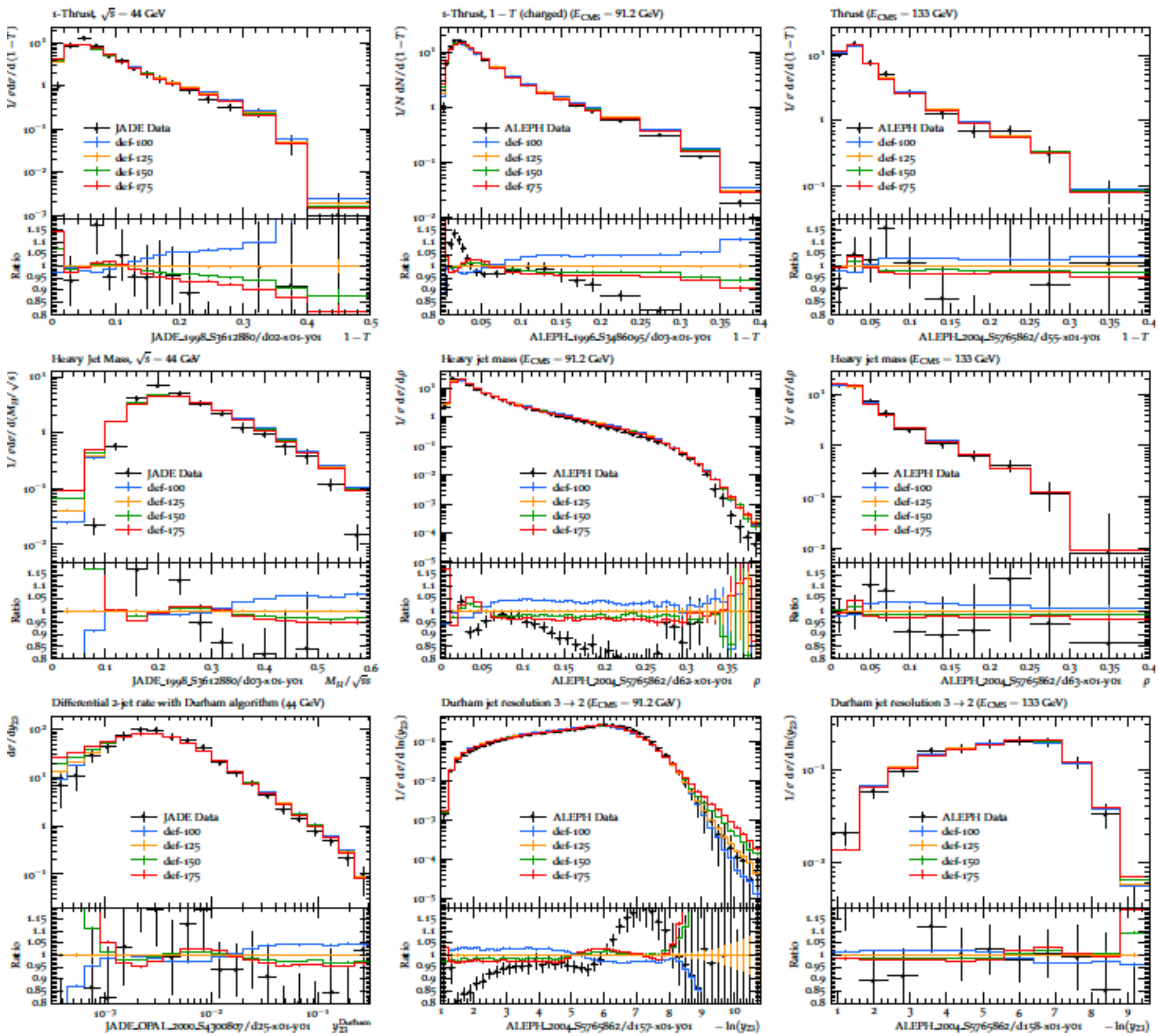
Old Default Model vs. New Dynamical Model

AHH, Jin, Plätzer, Samitz arXiv:2404.09856

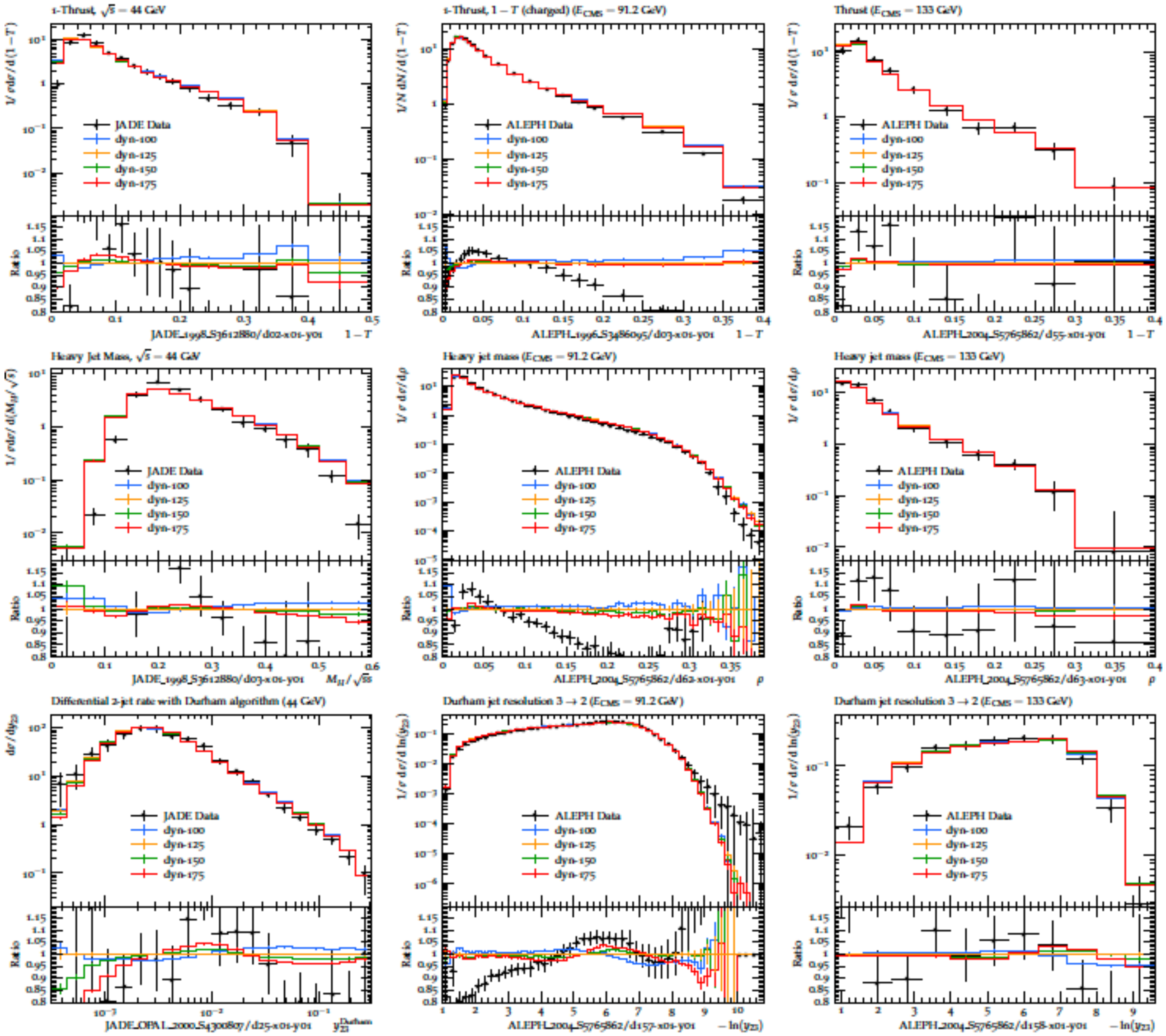
Default



Old Default Model vs. New Dynamical Model

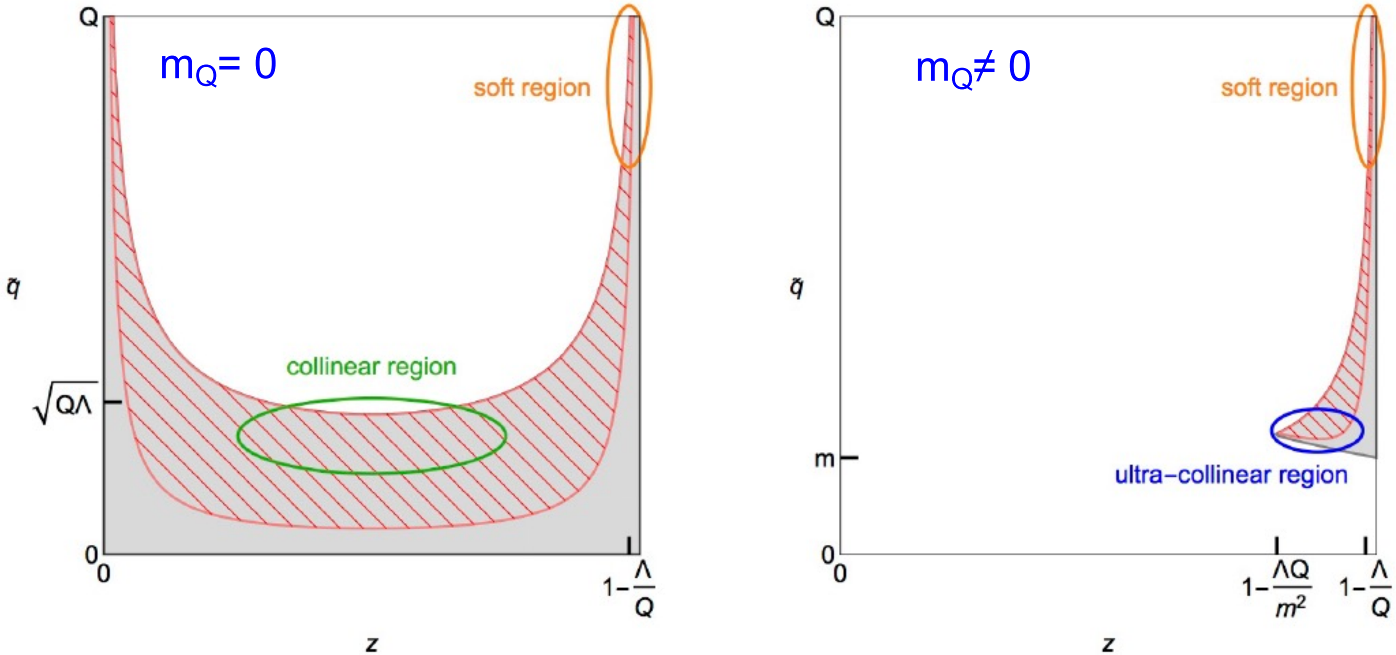
AHH, Jin, Plätzer, Samitz arXiv:2404.09856

Dynamical



Phase Space and Power Counting (Q_0=0)

AHH, Plätzer, Samitz arXiv:1807.06617



phase space regions for $\tau_{\rm peak} \sim \frac{\Lambda}{Q} \ll 1,\, m=0$		
	coherent branching	QCD factorization
n-coll.	$z \sim (1-z) \sim 1$ $\tilde{q} \sim (Q\Lambda)^{\frac{1}{2}}$ $q_\perp \sim (Q\Lambda)^{\frac{1}{2}}$	$q^\mu \sim (\Lambda, Q, (Q\Lambda)^{\frac{1}{2}})$
soft	$1-z \sim \frac{\Lambda}{Q},\; z \sim 1$ $\tilde{q} \sim Q$ $q_\perp \sim \Lambda$	$q^\mu \sim (\Lambda, \Lambda, \Lambda)$

phase space regions for $\tau_{\rm peak} - \tau_{\rm min} \sim \frac{\Lambda}{Q} \ll 1,\, m \neq 0$		
	coherent branching	QCD factorization
u. coll.	$1-z \sim \frac{Q\Lambda}{m^2},\; z \sim 1$ $\tilde{q} \sim m$ $q_\perp \sim \frac{Q}{m}\Lambda$	$q^\mu \sim (\Lambda, \frac{Q^2}{m^2}\Lambda, \frac{Q}{m}\Lambda)$
soft	$1-z \sim \frac{\Lambda}{Q},\; z \sim 1$ $\tilde{q} \sim Q$ $q_\perp \sim \Lambda$	$q^\mu \sim (\Lambda, \Lambda, \Lambda)$