

Overview of time-dependent CP violation in B meson decays

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on behalf of Belle II collaboration

Time-dependent CP violation in B mesons

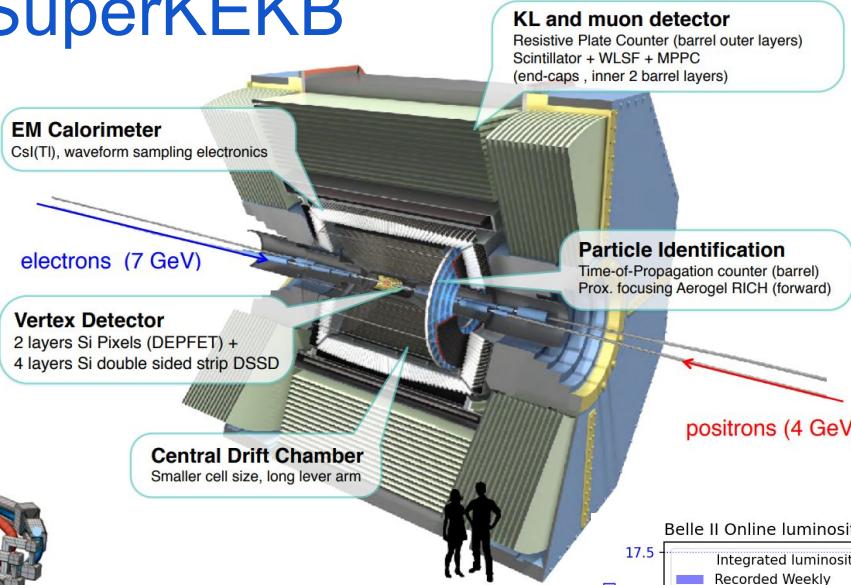
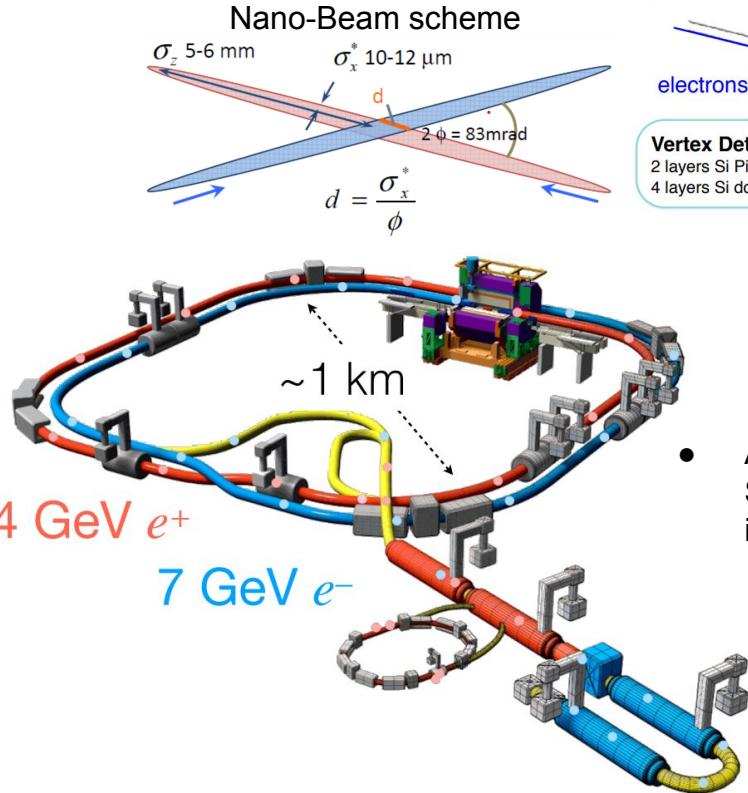


- Belle II detector at SuperKEKB and LHCb detector at LHC
- Experimental methods
- Time-dependent CP violation
- Flavor taggers in experiments
- Time-dependent CP violation results
 - $\sin 2\phi_1$ and $\sin 2\phi_1^{\text{eff}}$ measurements
 - $J/\psi K_S^0$, $\eta' K_S^0$, ϕK_S^0 , $\pi^0 K_S^0$ and $K_S^0 K_S^0 K_S^0$ analyses
 - ϕ_s , ϕ_s^{sss} , Γ_s and ϕ_3 analyses
- Systematic uncertainties limitations
- Perspective for future measurements
- Conclusion

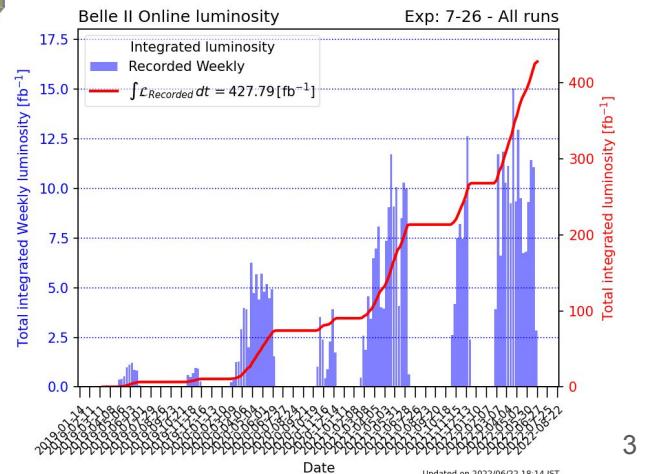
Belle II detector at SuperKEKB



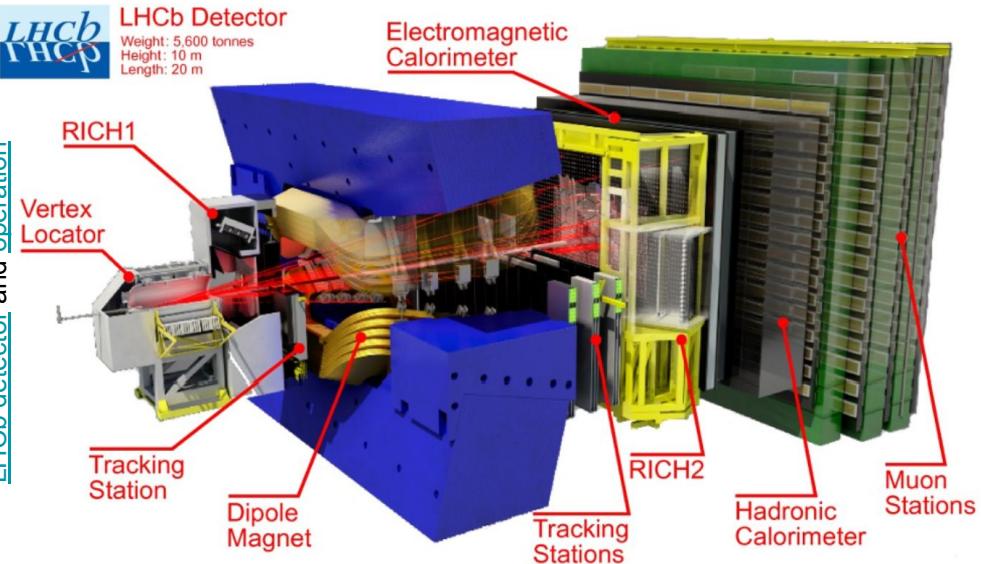
Belle II detector and its luminosity



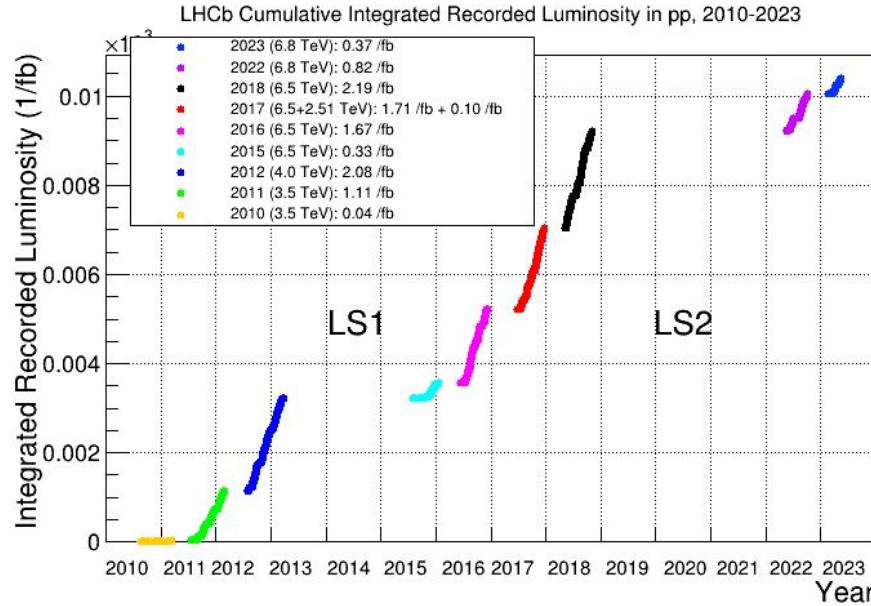
- Asymmetric e^+e^- collisions at the SuperKEKB accelerator complex in Japan
 - Recorded world's highest instantaneous luminosity ($4.7 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$)
 - Collected 362 fb^{-1} dataset at the $Y(4S)$ in 2019-22, corresponding to $387 \text{ M } B\bar{B}$ pairs



LHCb detector at LHC



- Single armed forward spectrometer
- Large sample of semileptonic decays
- All b-hadron species accessible
- Decay time resolution ~ 45 ps
- $\Delta p/p = 0.5 - 1.0 \%$
- eff(kaonID) $\sim 95 \%$
- eff(muonID) $\sim 97 \%$
- Pion mis-ID fraction $\sim 10 \%$

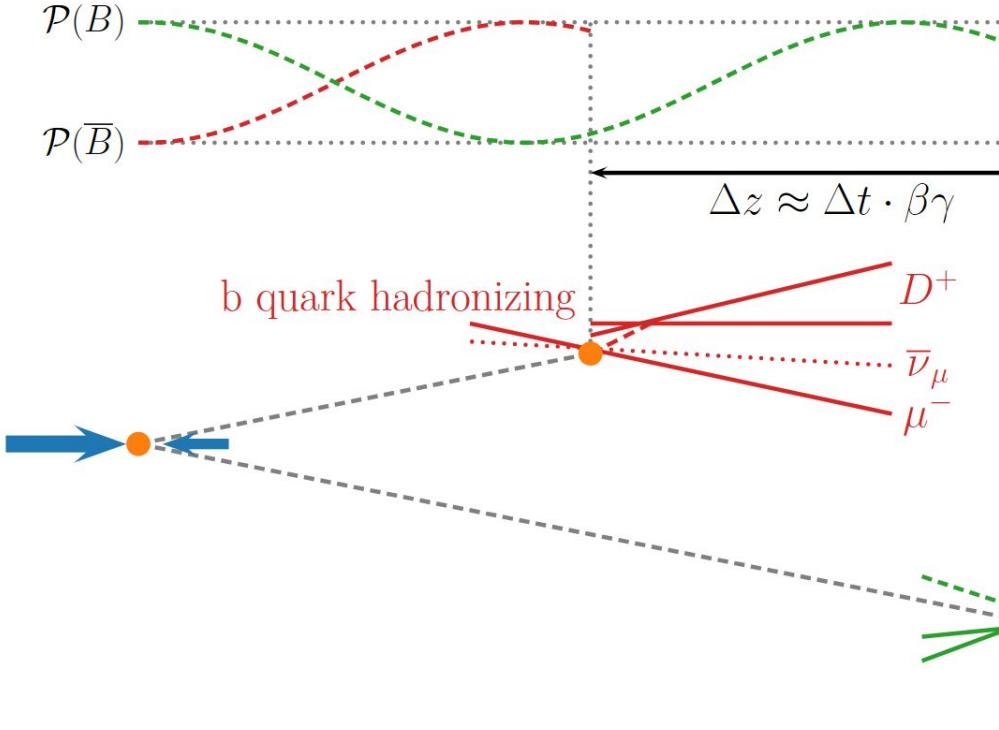


Time-dependent CP violation in B mesons



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Experimental methods

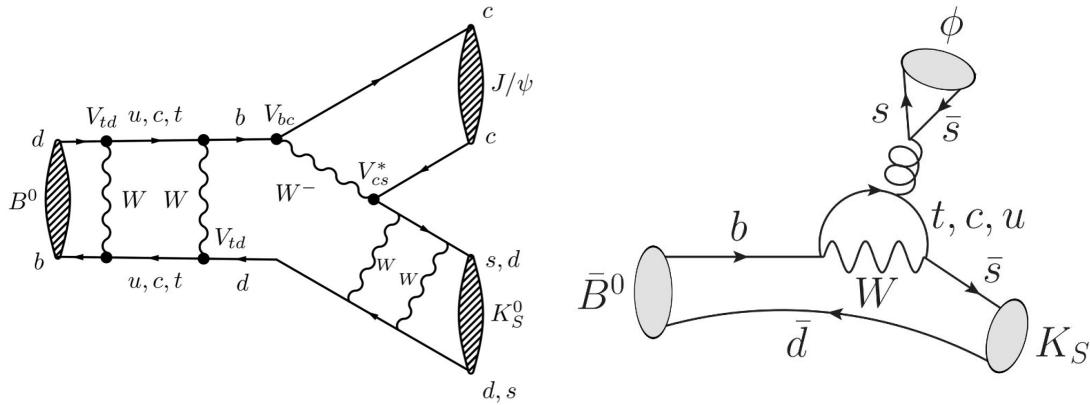


- To measure time-dependent asymmetry in B mesons we need to know:
 - Flavor of the other b quark
 - Proper decay time (difference)

- In Belle II, produced quantum entangled states allows measurement time difference between states
- In LHCb, oscillation in signal side and opposite oscillation is not guaranteed, time is measured in relation to production of B̄B pairs

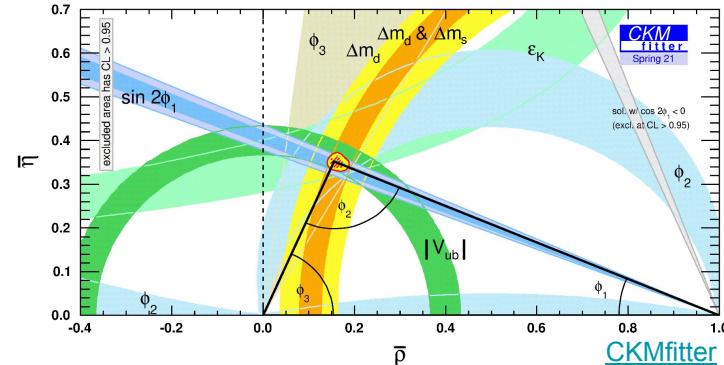
Time-dependent CP violation

- The measurements of $\phi_1 = \beta$ can be performed either at:
 - Tree dominated in $c\bar{c}s$ transition using $J/\psi K^0$ channel
 - Loop dominated in $q\bar{q}s$ transition using e.g. ϕK^0 channel



$$\begin{aligned}\mathcal{A}_{\text{CP}}(\Delta t) &= \frac{\Gamma(\bar{B}^0 \rightarrow f) - \Gamma(B^0 \rightarrow f)}{\Gamma(\bar{B}^0 \rightarrow f) + \Gamma(B^0 \rightarrow f)} \\ &= S_f \sin(\Delta m_d \Delta t) - C_f \cos(\Delta m_d \Delta t)\end{aligned}$$

- Six measurements done by Belle II
- One measurement done by LHCb



Mixing-induced CP asymmetry: $S_f \sim \sin(2\phi_1) = \sin(2\beta)$
 Direct CP asymmetry: C_f

Time-dependent CP violation

- Another measurements in B_s^0 meson sector (LHCb only):

- For $B_s^0 \rightarrow VV$ (vectors), angular analysis of ϕ_s , ϕ_s^{sss} :

$$\begin{aligned} \mathcal{A}_{\text{CP}}(t) &= \frac{\Gamma(\bar{B}_s^0 \rightarrow f) - \Gamma(B_s^0 \rightarrow f)}{\Gamma(\bar{B}_s^0 \rightarrow f) + \Gamma(B_s^0 \rightarrow f)} \\ &= \eta_f \cdot \sin \phi_s \cdot \sin \Delta m_s t \end{aligned}$$

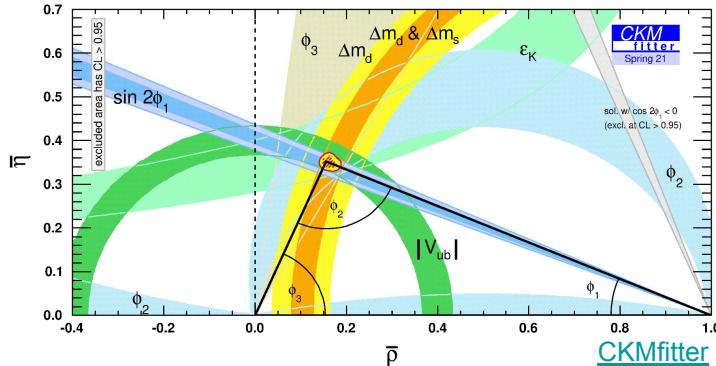
- Difference between decay widths of heavy and light mass eigenstates $\Delta\Gamma_s$
- Asymmetry measurement of $\phi_3 = \gamma$ angle

$$\begin{aligned} \Gamma(B_s^0(t) \rightarrow f/\bar{f}) &\sim e^{-\Gamma_s t} (\cosh(\frac{\Delta\Gamma_s}{2}t) + C_{f/\bar{f}} \cos(\Delta m_s t) + \\ &A_{f/\bar{f}}^{\Delta t} \sinh(\frac{\Delta\Gamma_s}{2}t) - S_{f/\bar{f}} \sin(\Delta m_s t)) \end{aligned}$$

$$C_f = C_{\bar{f}} = \frac{1 - r_{D_s K}^2}{1 + r_{D_s K}^2}$$

$$A_f^{\Delta\Gamma} = \frac{-2r_{D_s K}^2 \cos(\delta - (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$

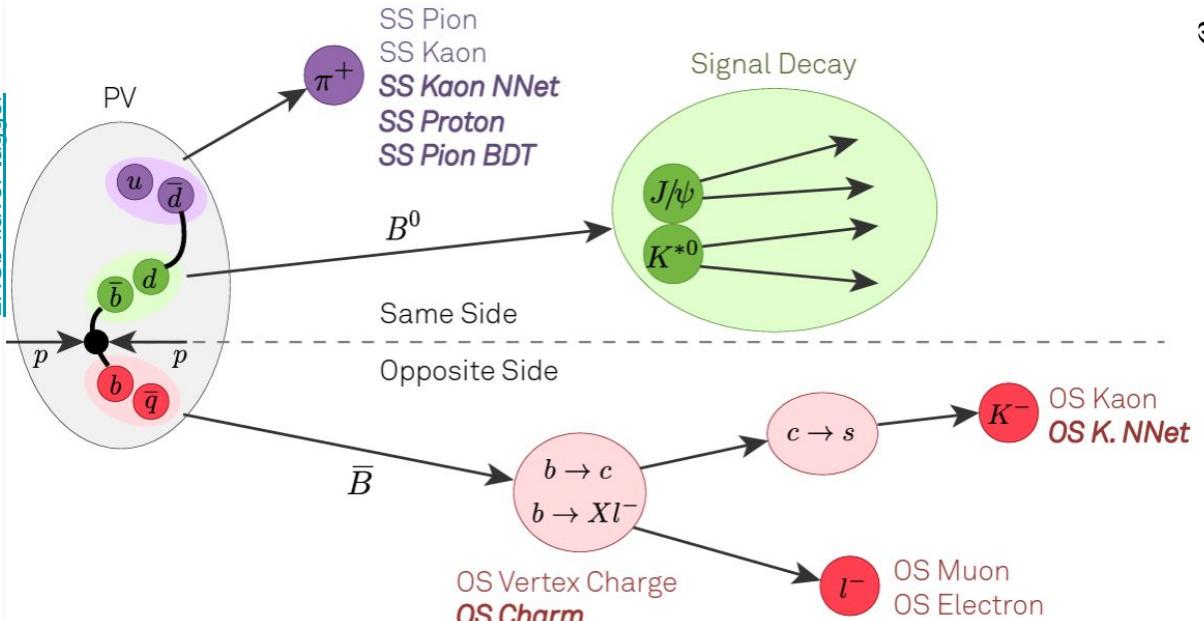
$$A_{\bar{f}}^{\Delta\Gamma} = \frac{-2r_{D_s K}^2 \cos(\delta + (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$



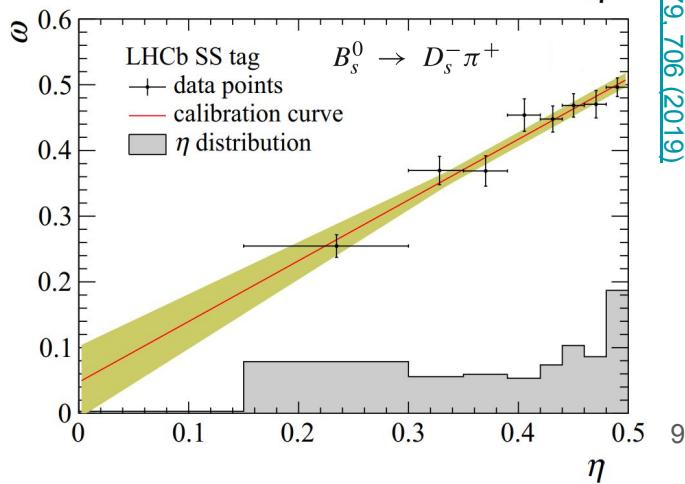
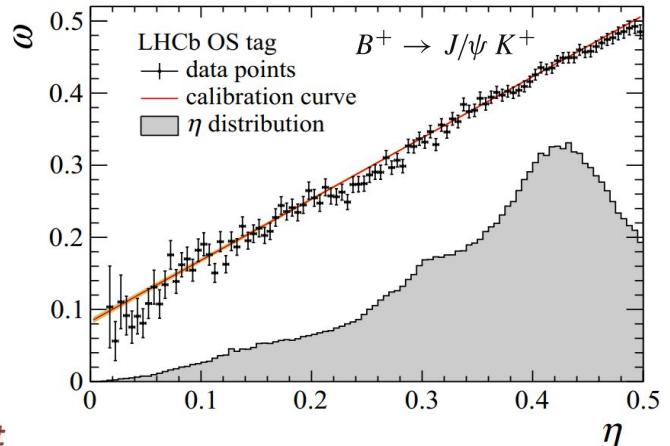
$$S_f^{\Delta\Gamma} = \frac{2r_{D_s K}^2 \sin(\delta - (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$

$$S_{\bar{f}}^{\Delta\Gamma} = \frac{2r_{D_s K}^2 \sin(\delta + (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$

Flavor taggers at LHCb

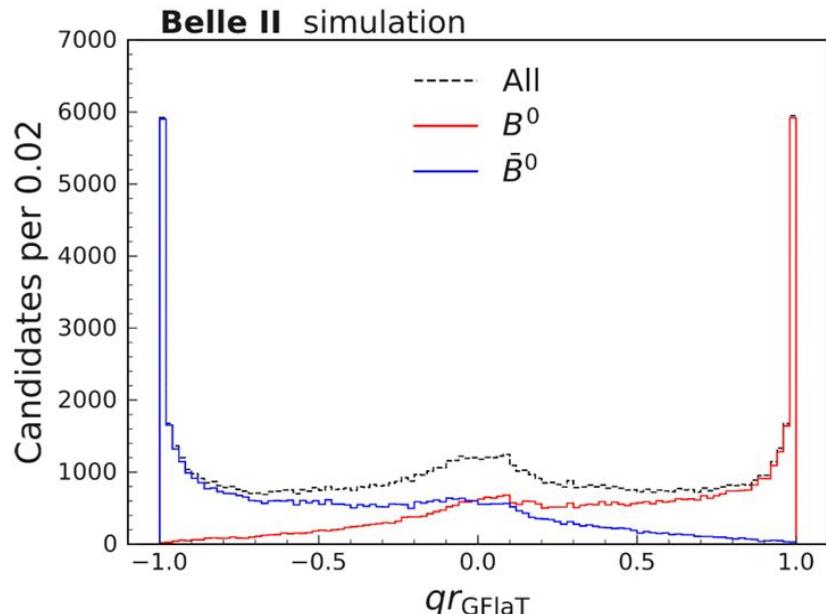


- Inputs of taggers are charge of daughter and granddaughters and they are output to $q\eta$
- Tagging power of combined OS and SS taggers:
 - 2015+2016: $\epsilon_{\text{eff}} = 4.18 \pm 0.15 \%$
 - 2017: $\epsilon_{\text{eff}} = 4.22 \pm 0.16 \%$
 - 2018: $\epsilon_{\text{eff}} = 4.36 \pm 0.16 \%$



Flavor taggers at Belle II

- Traditional algorithm (Category based Flavor Tagger):
exploit single particle's property (using e.g. charge of
daughters, ...) outputted into qr
 - Typical flavor-specific decay modes are called categories
and they are combined for output
 - Interrelations of particles are not fully exploited
- Graph-Neutral-Network based Flavor Tagger (GFlaT)
 - Pairs of particles are used as input information for the
GFlaT
 - Single particle's information is used as well.
- Performance using Data:
 - $\epsilon_{\text{eff}} \text{ (Graph)} = 37.39 \pm 0.39 \%$
 - $\epsilon_{\text{eff}} \text{ (Category)} = 31.68 \pm 0.38 \%$
- GFlaT increase tagging efficiency about **18%**
compared to category based flavor tagger
- Using GFlaT we are able reduce statistical uncertainty
in TDCPV analysis about **8%**

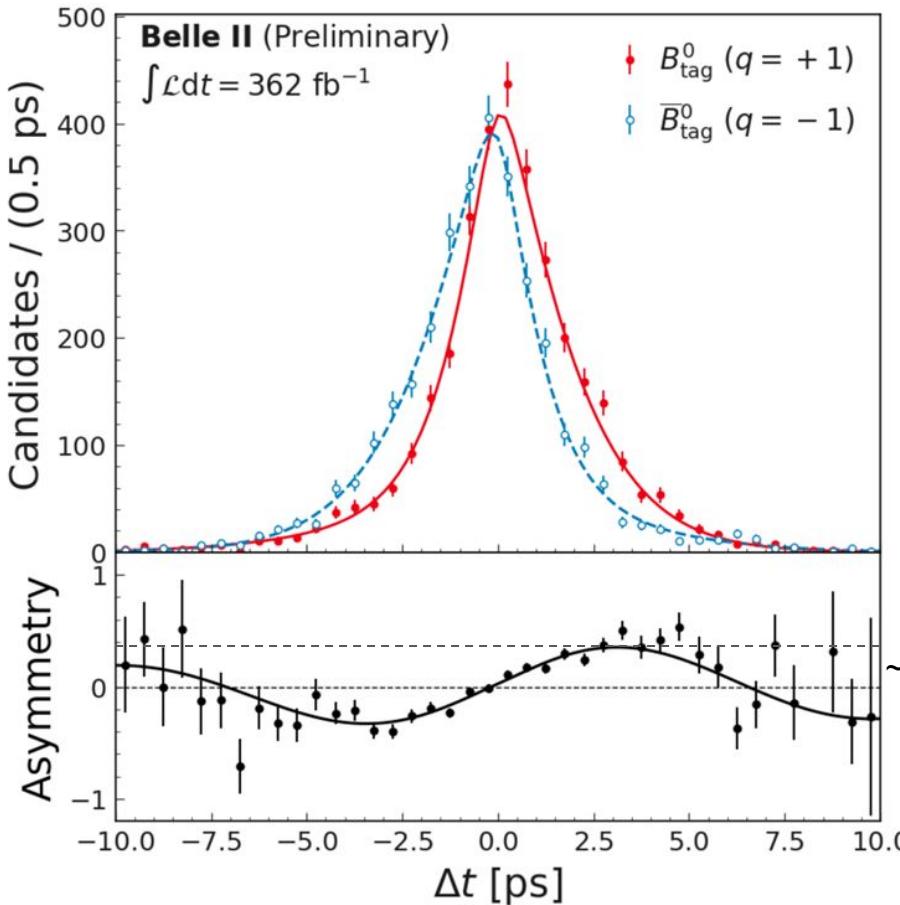


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Results of $\sin(2\phi_1)$ at Belle II



$B^0 \rightarrow J/\psi (\rightarrow \ell\ell) K_S^0 (\rightarrow \pi^+ \pi^-) :$

$$S_{J/\psi K_S^0} = 0.724 \pm 0.035 \text{ (stat)} \pm 0.014 \text{ (syst)}$$

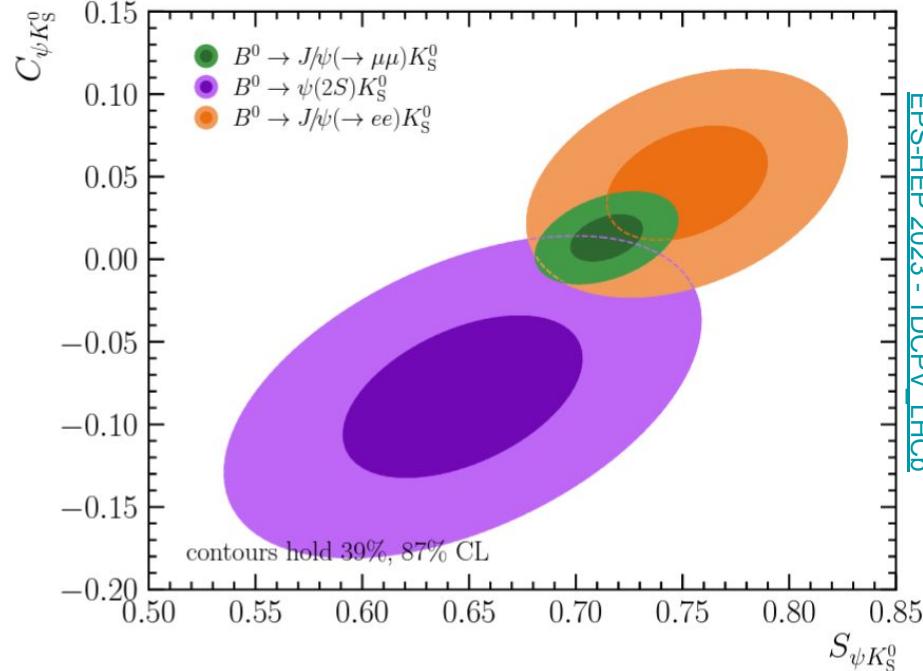
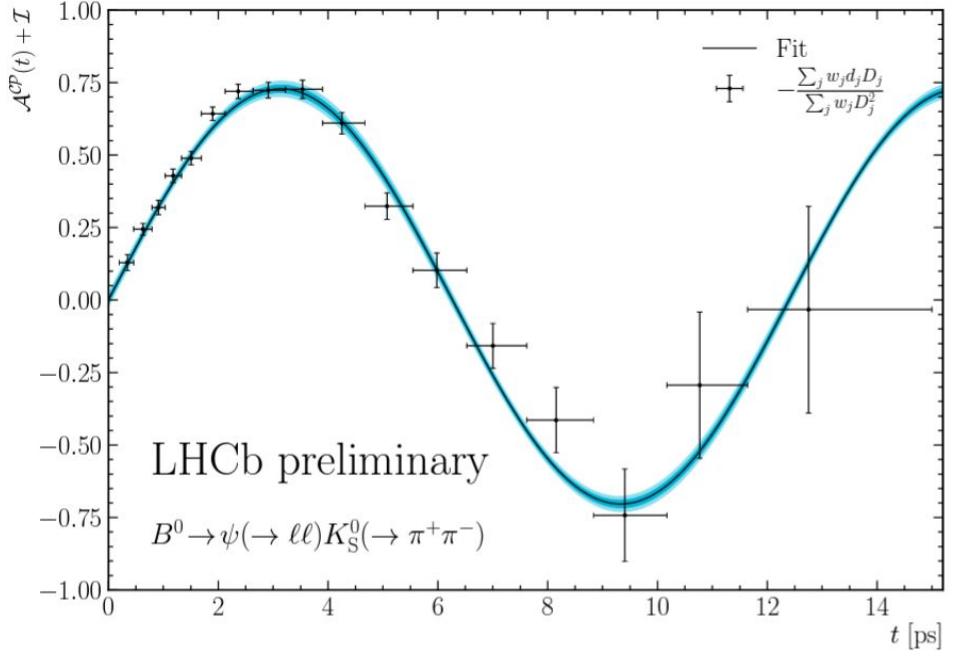
$$C_{J/\psi K_S^0} = -0.035 \pm 0.026 \text{ (stat)} \pm 0.012 \text{ (syst)}$$

HFLAV :

$$S_{J/\psi K_S^0} = 0.669 \pm 0.017$$

$$C_{J/\psi K_S^0} = 0.005 \pm 0.015$$

Result of $\sin(2\phi_1)$ at LHCb



$B^0 \rightarrow \{J/\psi(\rightarrow \ell\ell) \& \psi(2S)(\rightarrow \mu^+\mu^-)\} K_S^0 (\rightarrow \pi^+\pi^-)$: HFLAV :

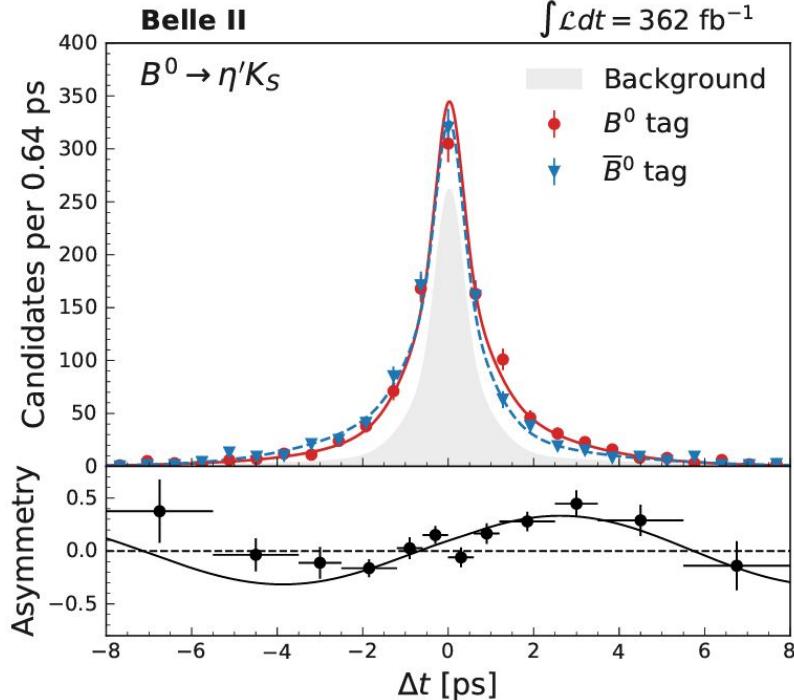
$$S_{\psi K_S^0}^{\text{Run 1+2}} = 0.716 \pm 0.013 \text{ (stat)} \pm 0.008 \text{ (syst)}$$

$$C_{\psi K_S^0}^{\text{Run 1+2}} = 0.012 \pm 0.012 \text{ (stat)} \pm 0.003 \text{ (syst)}$$

$$S_{\psi K_S^0} = 0.669 \pm 0.017$$

$$C_{\psi K_S^0} = 0.005 \pm 0.015$$

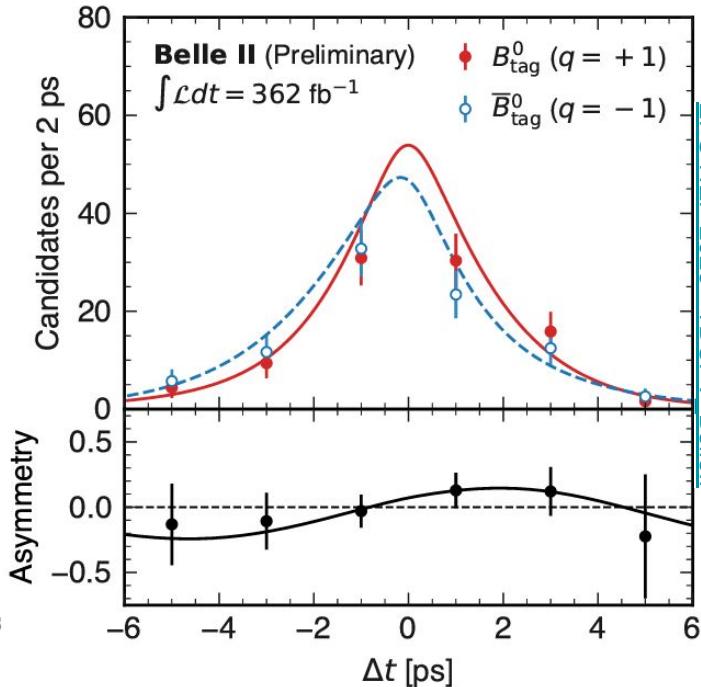
Results of $\sin(2\phi_1)^{\text{eff}}$ at Belle II



$$B^0 \rightarrow \eta' (\rightarrow \{\rho\gamma \& \eta [\rightarrow \gamma\gamma]\pi^+\pi^-}) K_S^0 (\rightarrow \pi^+\pi^-) :$$

$$S_{\eta' K_S^0} = 0.67 \pm 0.10 \text{ (stat)} \pm 0.04 \text{ (syst)}$$

$$C_{\eta' K_S^0} = -0.19 \pm 0.08 \text{ (stat)} \pm 0.03 \text{ (syst)}$$



HFLAV :

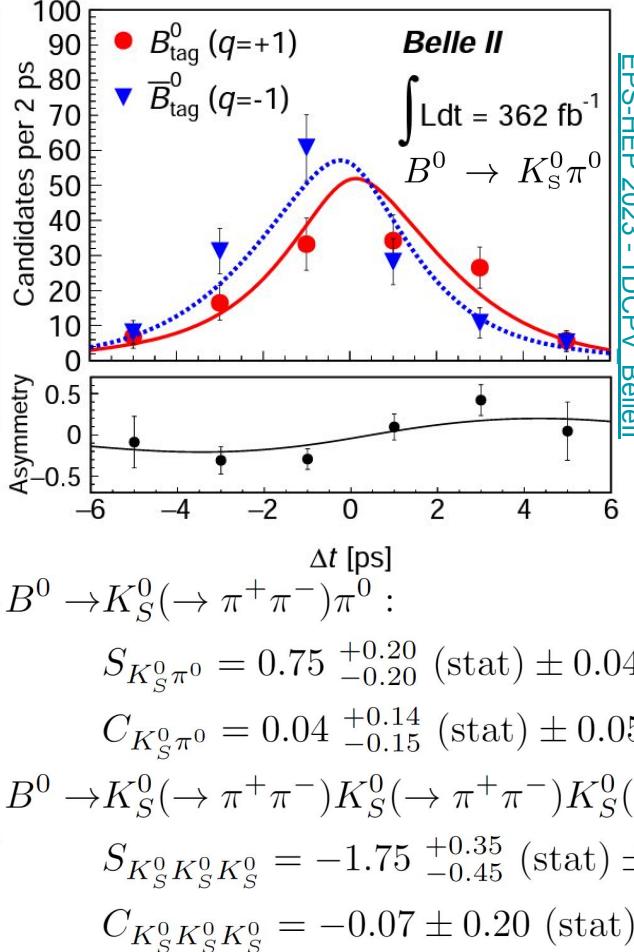
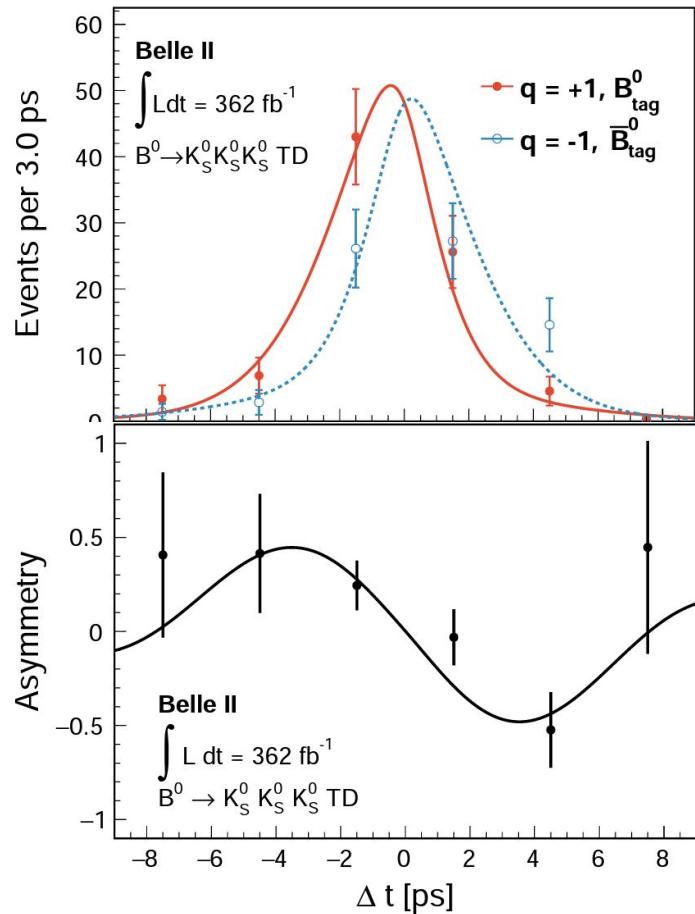
$$S_{\eta' K_S^0} = 0.63 \pm 0.06$$

$$C_{\eta' K_S^0} = -0.05 \pm 0.04$$

$$S_{\phi K_S^0} = 0.74^{+0.11}_{-0.13}$$

$$C_{\phi K_S^0} = 0.01 \pm 0.14$$

Results of $\sin(2\phi_1)^{\text{eff}}$ at Belle II



HFLAV :

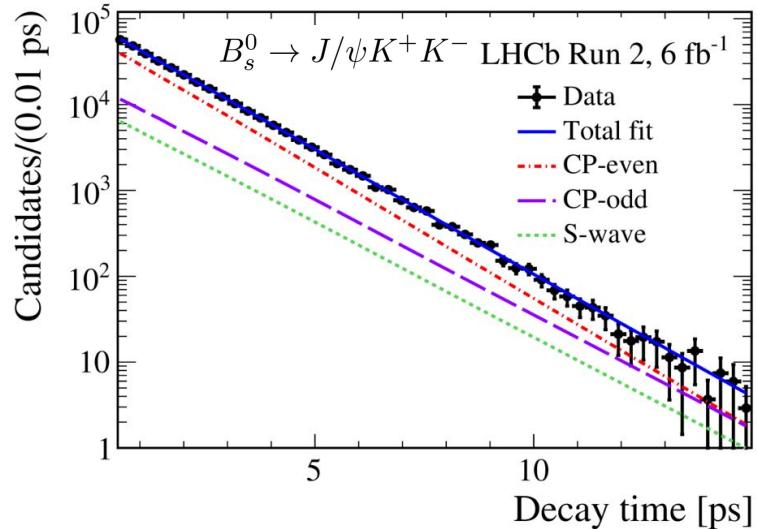
$$S_{K_S^0 \pi^0} = 0.57 \pm 0.17$$

$$C_{K_S^0 \pi^0} = 0.01 \pm 0.10$$

$$S_{K_S^0 K_S^0 K_S^0} = -0.83 \pm 0.17$$

$$C_{K_S^0 K_S^0 K_S^0} = -0.15 \pm 0.12$$

Results of ϕ_s , ϕ_s^{sss} by LHCb

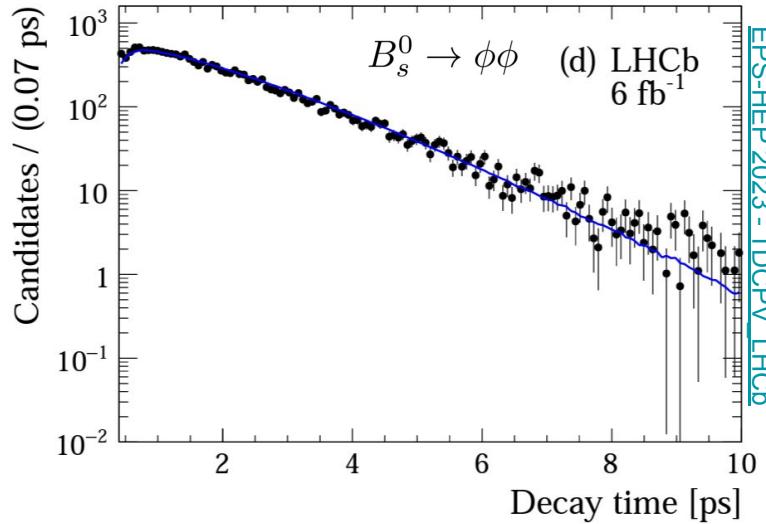


parameter	value	\pm	stat	\pm	syst
ϕ_s [rad]	-0.039	\pm	0.022	\pm	0.006

$$\text{Run 1 + 2 : } \phi_s = -0.044 \pm 0.020 \text{ rad}$$

HFLAV :

$$\phi_s = -0.039 \pm 0.016 \text{ rad}$$



parameter	value	\pm	stat	\pm	syst
ϕ_s^{sss} [rad]	-0.042	\pm	0.075	\pm	0.009

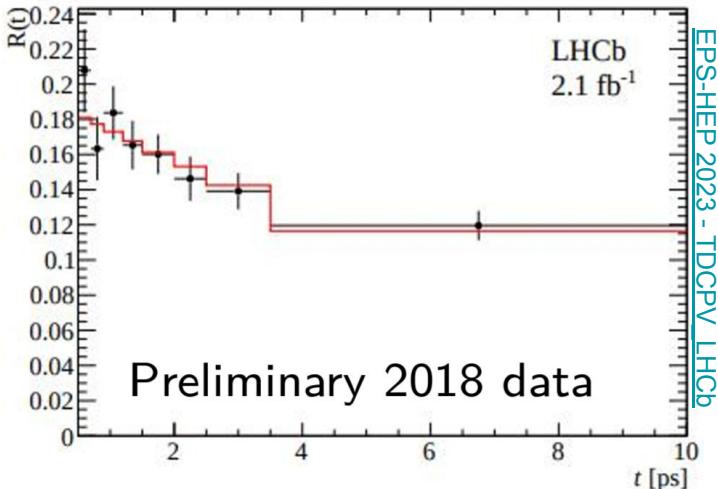
$$\text{Run 1 + 2 : } \phi_s^{sss} = -0.074 \pm 0.069 \text{ rad}$$

As expected CP violation is very small in these channels

Results of $\Delta\Gamma_s$, γ by LHCb



$$\mathcal{R}(t) = \frac{N_L}{N_H} \propto \frac{[e^{-\Gamma_s t(1+y)}]_{t_1}^{t_2}}{[e^{-\Gamma_s t(1+y)}]_{t_1}^{t_2}} \cdot \frac{1-y}{1+y}$$



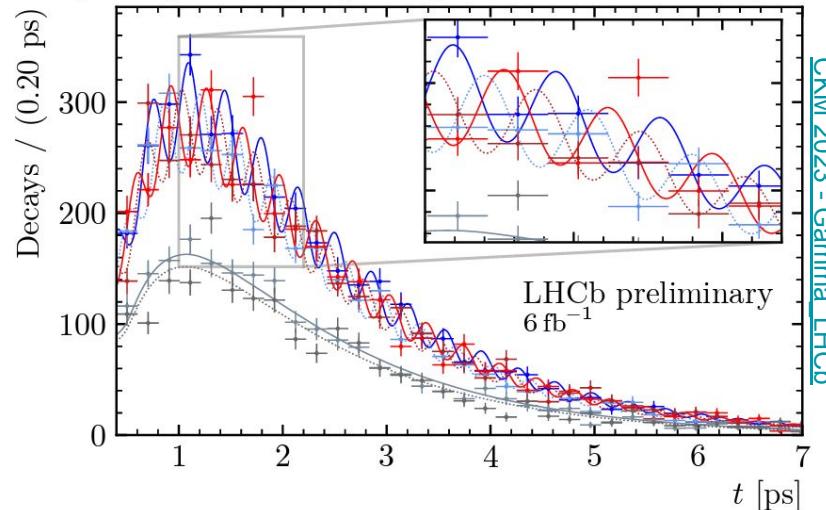
From $B_s^0 \rightarrow J/\psi\eta'$ and $B_s^0 \rightarrow J/\psi\pi^+\pi^-$:

$$\Delta\Gamma_s = 0.087 \pm 0.012 \text{ (stat)} \pm 0.009 \text{ (syst)} \text{ ps}^{-1}$$

HFLAV :

$$\Delta\Gamma_s = 0.074 \pm 0.006 \text{ ps}^{-1}$$

$\dagger\dagger B_s^0 \rightarrow D_s^- K^+$ $\dagger\dagger \bar{B}_s^0 \rightarrow D_s^- K^+$ $\dagger\dagger$ Untagged $D_s^- K^+$
 $\dagger\dagger B_s^0 \rightarrow D_s^+ K^-$ $\dagger\dagger \bar{B}_s^0 \rightarrow D_s^+ K^-$ $\dagger\dagger$ Untagged $D_s^+ K^-$



$$\gamma = 74 \pm 11^\circ$$

HFLAV :

$$\gamma = 65.9 {}^{+3.3} {}^{-3.5} {}^\circ$$

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Uncertainties and limitations for $B^0 \rightarrow J/\psi K_S^0$



LHCb

$$S_{\psi K_S^0}^{\text{Run 1+2}} = 0.716 \pm 0.013 \text{ (stat)} \pm 0.008 \text{ (syst)}$$

$$C_{\psi K_S^0}^{\text{Run 1+2}} = 0.012 \pm 0.012 \text{ (stat)} \pm 0.003 \text{ (syst)}$$

Source	$\sigma(S)$	$\sigma(C)$
Fitter validation	0.0004	0.0006
$\Delta\Gamma_d$ uncertainty	0.0055	0.0017
FT calibration portability	0.0053	0.0001
FT $\Delta\epsilon_{\text{tag}}$ portability	0.0014	0.0017
Decay-time bias model	0.0007	0.0013

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Dominant

Scaled to statistics

Belle II

$$S_{J/\psi K_S^0} = 0.724 \pm 0.035 \text{ (stat)} \pm 0.014 \text{ (syst)}$$

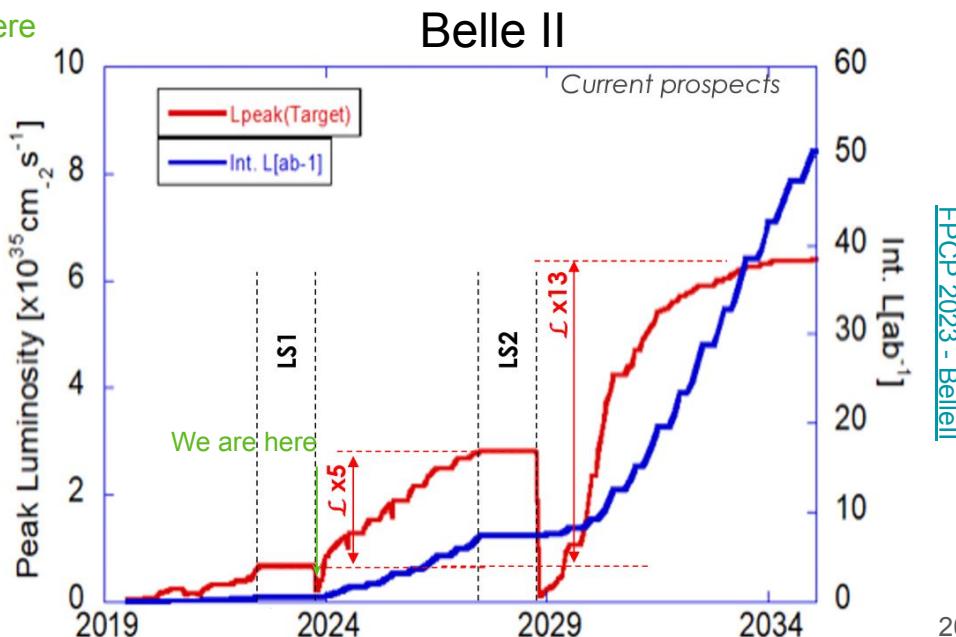
$$C_{J/\psi K_S^0} = -0.035 \pm 0.026 \text{ (stat)} \pm 0.012 \text{ (syst)}$$

Source	$\sigma(\epsilon_{\text{tag}})$ [%]	$\sigma(S_{CP})$	$\sigma(C_{CP})$
$B^0 \rightarrow D^{(*)-}\pi^+$ sample size	0.43	0.004	0.007
$B^0 \rightarrow J/\psi K_S^0$ sample size		0.035	0.026
Fit model			
Analysis bias	0.02	0.002	0.005
Fixed resolution parameters	0.07	0.004	0.004
τ & Δm_d	0.06	0.001	0.000
$\sigma_{\Delta t}$ binning	0.04	0.000	0.000
Δt measurement			
Alignment	0.06	0.005	0.003
Beam spot	0.16	0.002	0.002
CMS Energy	0.03	0.000	0.001
Backgrounds			
$B^0 \rightarrow D^{(*)-}\pi^+$ sWeight bias	0.24	0.001	0.001
$B^0 \rightarrow D^{(*)-}\pi^+\Delta E$ background	0.11	0.001	0.001
Signal ΔE shape	0.08	0.002	0.000
Tag-side interference	—	0.010	0.007
Total systematic	0.34	0.014	0.012

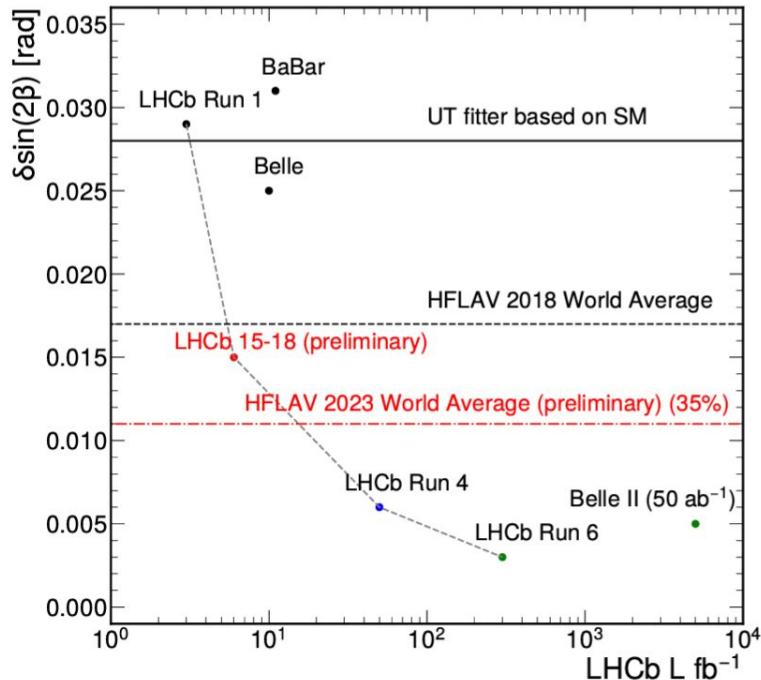
Future prospects



- Current status:
 - Belle II: $\sim 428 \text{ fb}^{-1}$ ($\sim 1\% \int L_{\text{total}}$)
 - LHCb: $\sim 9 \text{ fb}^{-1}$ ($\sim 3\% \int L_{\text{total}}$)
- Next runs:
 - Belle II: $\sim 5 \text{ ab}^{-1}$ ($\sim 10\% \int L_{\text{total}}$)
 - LHCb: $\sim 50 \text{ fb}^{-1}$ ($\sim 16\% \int L_{\text{total}}$)



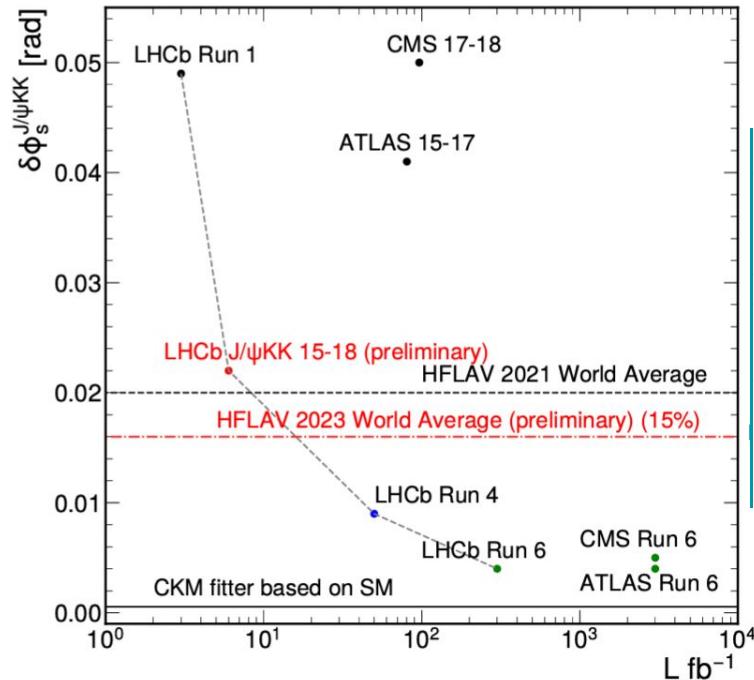
Future prospects - statistical uncertainty



$\delta \sin(2\phi_1)$ using $B^0 \rightarrow \eta' K^0$

L (ab^{-1})	stat. (10^{-2})	syst. (10^{-2})	total (10^{-2})
5	2.7	2.1 (1.7)	3.4 (3.2)
50	0.85	1.8 (1.3)	2.0 (1.5)

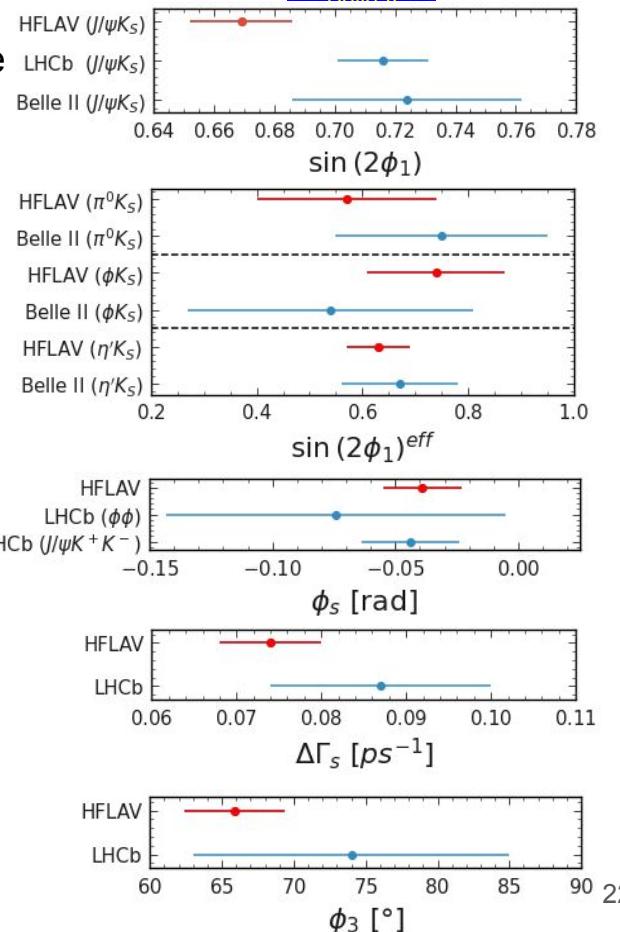
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Conclusions and outlook

- Time-dependent CP violation measurements in B meson decays were introduced
- Flavor taggers used in Belle II and LHCb experiments were explained
- Results for several time-dependent CP violation analyses have been shown:
 - $\sin(2\phi_1)$ measurements using $J/\psi K_S^0$
 - $\sin(2\phi_1)^{eff}$ measurements using $\eta' K_S^0$, $\pi^0 K_S^0$, ϕK_S^0 and $K_S^0 K_S^0 K_S^0$
 - Φ_s , Φ_s^{sss} , Γ_s and γ analyses
- Uncertainties of measurements with dominated factors were discussed
- In future, LHCb and Belle II will deliver more precise measurements

Year	Luminosity [fb^{-1}]		$\delta(\sin(2\phi_1)/2\beta)$
	LHCb	Belle II	
2018	3	0	0.017
2023	9	362	0.011
2032	50	5 000	0.006
2041	300	50 000	0.004



Backup

Time-dependent CP violation

- Another measurements in B_s^0 meson sector (LHCb only):

- Angular analysis of ϕ_s , ϕ_{sss} ,

$$\begin{aligned} \mathcal{A}_{\text{CP}}(\Delta t) &= \frac{\Gamma(\bar{B}_s^0 \rightarrow f) - \Gamma(B_s^0 \rightarrow f)}{\Gamma(\bar{B}_s^0 \rightarrow f) + \Gamma(B_s^0 \rightarrow f)} \\ &= \eta_f \cdot \sin \phi_s \cdot \sin \Delta m_s t \end{aligned}$$

- Yield ratio $\Delta \Gamma_s$

$$\mathcal{R}(t) = \frac{N_L}{N_H} \propto \frac{[e^{-\Gamma_s t(1+y)}]_{t_1}^{t_2}}{[e^{-\Gamma_s t(1+y)}]_{t_1}^{t_2}} \cdot \frac{1-y}{1+y}$$

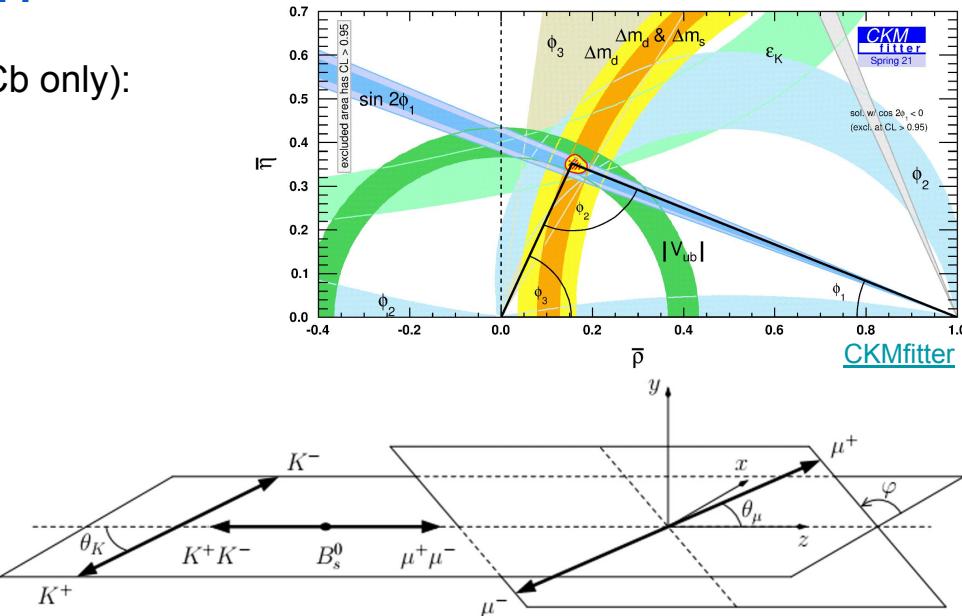
- Asymmetry measurement of $\phi_3 = \gamma$ angle

$$\begin{aligned} \Gamma(B_s^0(t) \rightarrow f/\bar{f}) &\sim e^{-\Gamma_s t} (\cosh(\frac{\Delta \Gamma_s}{2} t) + C_{f/\bar{f}} \cos(\Delta m_s t) + \\ &A_{f/\bar{f}}^{\Delta t} \sinh(\frac{\Delta \Gamma_s}{2} t) - S_{f/\bar{f}} \sin(\Delta m_s t)) \end{aligned}$$

$$C_f = C_{\bar{f}} = \frac{1 - r_{D_s K}^2}{1 + r_{D_s K}^2}$$

$$A_f^{\Delta \Gamma} = \frac{-2r_{D_s K}^2 \cos(\delta - (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$

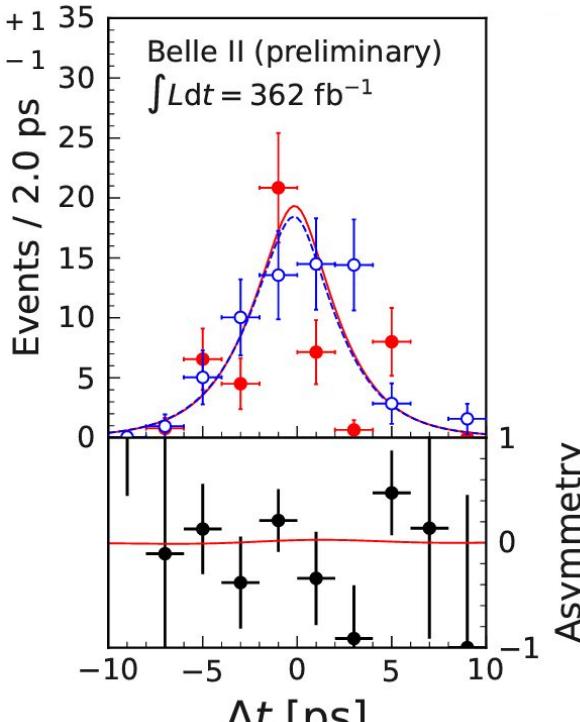
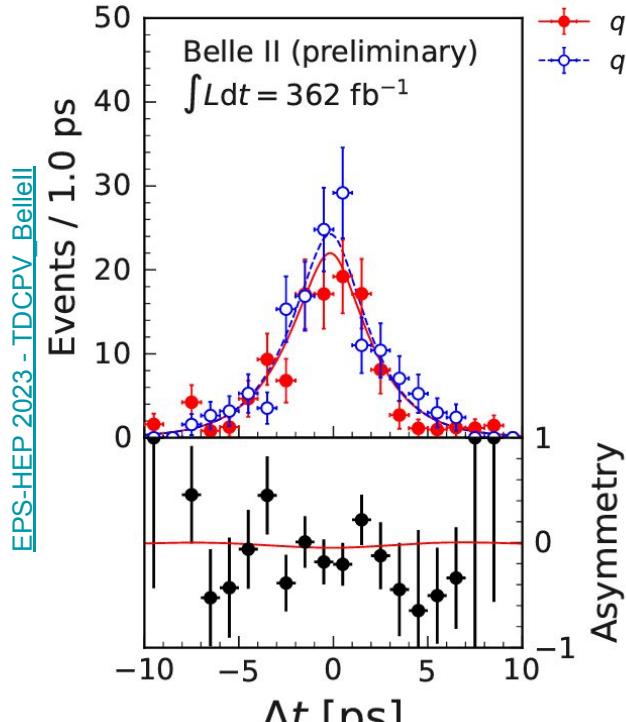
$$A_{\bar{f}}^{\Delta \Gamma} = \frac{-2r_{D_s K}^2 \cos(\delta + (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$



$$S_f^{\Delta \Gamma} = \frac{2r_{D_s K}^2 \sin(\delta - (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$

$$S_{\bar{f}}^{\Delta \Gamma} = \frac{2r_{D_s K}^2 \sin(\delta + (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$

Results of $\sin(2\phi_1/2\beta)^{\text{eff}}$ at Belle II



Due to polarization of photon $\sin(2\phi_1/2\beta)^{\text{eff}} \sim 0$.

HFLAV :

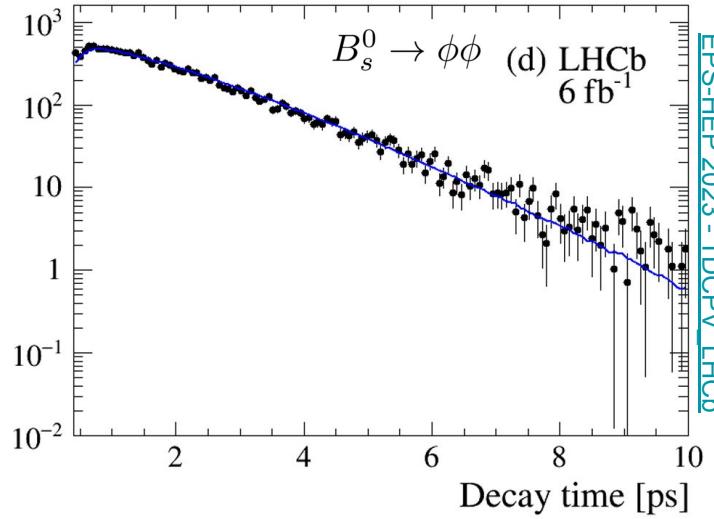
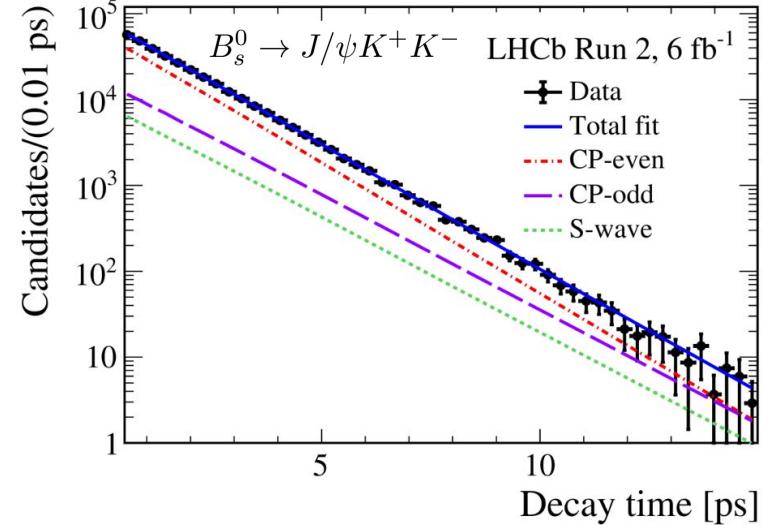
$$S_{K^{*0}\gamma} = -0.16 \pm 0.22$$

$$C_{K^{*0}\gamma} = -0.04 \pm 0.14$$

$$S_{K_S^0\pi^0\gamma} = 0.50 \pm 0.68$$

$$C_{K_S^0\pi^0\gamma} = 0.20 \pm 0.39$$

Results of ϕ_s , ϕ_s^{sss} by LHCb



parameter	value	± stat	± syst
ϕ_s [rad]	-0.039	± 0.022	± 0.006
$ \lambda $	1.001	± 0.011	± 0.005
$ A_\perp ^2$	0.2463	± 0.0023	± 0.0024
$ A_0 ^2$	0.5179	± 0.0017	± 0.0032
$\delta_\perp - \delta_0$ [rad]	2.903	± 0.0075	± 0.048
$\delta_\parallel - \delta_0$ [rad]	3.146	± 0.061	± 0.052

Run 1 + 2 : $\phi_s = -0.044 \pm 0.020$ rad

Run 1 + 2 : $|\lambda| = 0.990 \pm 0.010$

parameter	value	± stat	± syst
ϕ_s^{sss} [rad]	-0.042	± 0.075	± 0.009
$ \lambda $	1.004	± 0.030	± 0.009
$ A_\perp ^2$	0.384	± 0.007	± 0.003
$ A_0 ^2$	0.310	± 0.006	± 0.003
$\delta_\perp - \delta_0$ [rad]	2.463	± 0.029	± 0.009
$\delta_\parallel - \delta_0$ [rad]	2.769	± 0.105	± 0.011

Run 1 + 2 : $\phi_s^{sss} = -0.074 \pm 0.069$ rad

Run 1 + 2 : $|\lambda| = 1.009 \pm 0.07 \pm 0.030$

$$\phi_{s,0} = -0.18 \pm 0.09 \text{ rad}$$

$$\phi_\parallel - \phi_{s,0} = 0.12 \pm 0.09 \text{ rad}$$

$$\phi_\perp - \phi_{s,0} = 0.17 \pm 0.09 \text{ rad}$$

$$|\lambda_0| = 1.02 \pm 0.17$$

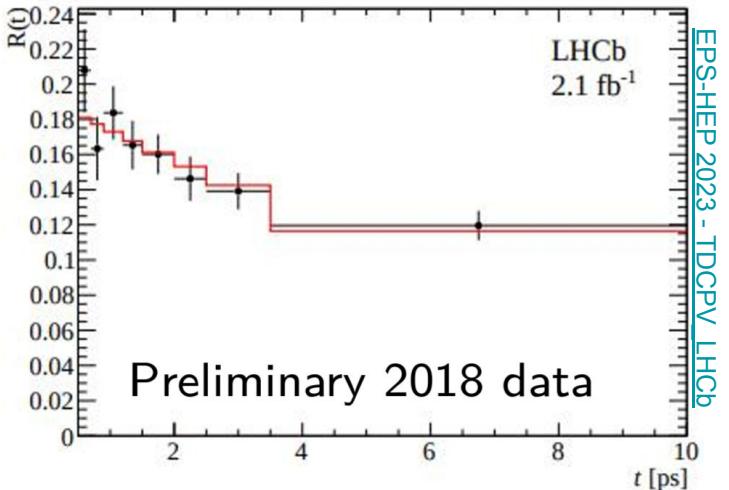
$$|\lambda_\perp/\lambda_0| = 0.97 \pm 0.22$$

$$|\lambda_\parallel/\lambda_0| = 0.78 \pm 0.21$$

Results of $\Delta\Gamma_s$, γ by LHCb

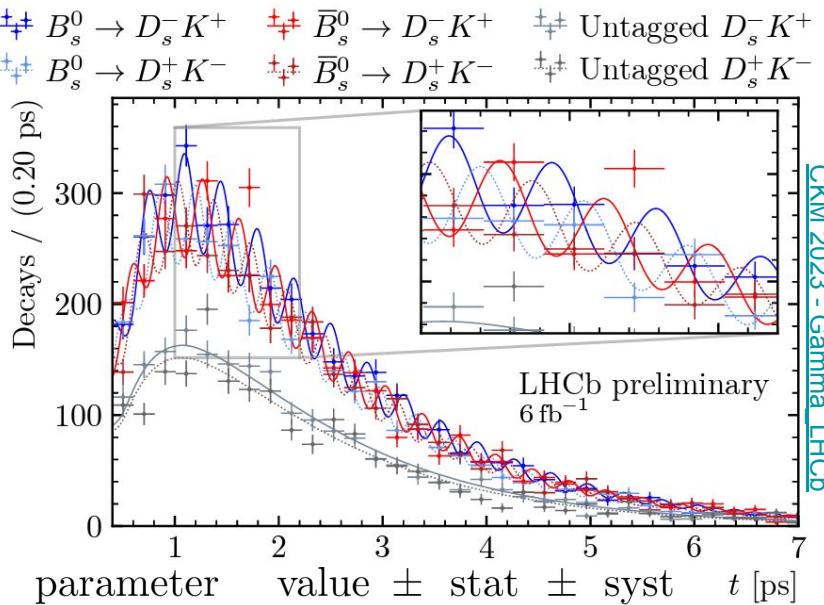


$$\mathcal{R}(t) = \frac{N_L}{N_H} \propto \frac{[e^{-\Gamma_s t(1+y)}]_{t_1}^{t_2}}{[e^{-\Gamma_s t(1+y)}]_{t_1}^{t_2}} \cdot \frac{1-y}{1+y}$$



From $B_s^0 \rightarrow J/\psi\eta'$ and $B_s^0 \rightarrow J/\psi\pi^+\pi^-$:

$$\Delta\Gamma_s = 0.0087 \pm 0.0012 \text{ (stat)} \pm 0.0009 \text{ (syst)} \text{ ps}^{-1}$$



C_f	$0.791 \pm 0.061 \pm 0.022$
$A_f^{\Delta\Gamma}$	$0.051 \pm 0.134 \pm 0.037$
S_f	$-0.071 \pm 0.084 \pm 0.023$
$A_{\bar{f}}^{\Delta\Gamma}$	$0.303 \pm 0.125 \pm 0.036$
$S_{\bar{f}}$	$-0.503 \pm 0.084 \pm 0.025$
$\gamma [^\circ]$	74 \pm 11

Systematic uncertainties $B^0 \rightarrow \eta' K_S^0$, $B^0 \rightarrow \phi K_S^0$



Source	$C_{\eta' K_S^0}$	$S_{\eta' K_S^0}$
Signal and continuum yields	< 0.001	0.002
SxF and $B\bar{B}$ yields	< 0.001	0.006
C_{BDT} mismodeling	0.004	0.010
Signal and background modelling	0.020	0.014
Observable correlation	0.008	0.001
Δt resolution fixed parameters	0.005	0.009
Δt resolution model	0.004	0.019
Flavor tagging	0.007	0.004
τ_{B^0} and Δm_d	< 0.001	0.002
Fit bias	0.003	0.002
Tracker misalignment	0.004	0.006
Momentum scale	0.001	0.001
Beam spot	0.002	0.002
B -meson motion in $\Upsilon(4S)$ frame	< 0.001	0.017
Tag-side interference	0.005	0.011
$B\bar{B}$ background asymmetry	0.008	0.006
Candidate selection	0.007	0.009
Total	0.027	0.037

Source	$\sigma(A)$	$\sigma(S)$
Calibration with $B^0 \rightarrow D^{(*)-} \pi^+$ decays		
Calibration sample size	± 0.010	± 0.009
Calibration sample systematic	± 0.010	± 0.012
Sample dependence	-0.005	+0.021
Fit model		
Fit bias	+0.017 -0.028	+0.033 -0.062
$B^0 \rightarrow K^+ K^- K_S^0$ backgrounds	-0.020	-0.011
Fixed fit shapes	± 0.009	± 0.022
τ_{B^0} and Δm_d uncertainties	± 0.006	± 0.022
$A_{K^+ K^- K_S^0}$ and $S_{K^+ K^- K_S^0}$	± 0.014	± 0.013
$B\bar{B}$ backgrounds	+0.030 -0.019	+0.017 -0.031
Tag-side interference	< 0.001	+0.012
Multiple candidates	+0.032	-0.002
Δt measurement		
Detector misalignment	+0.002	-0.002
Momentum scale	± 0.001	± 0.001
Beam spot	± 0.002	± 0.002
Δt approximation	< 0.001	-0.018
Total systematic	+0.052 -0.046	+0.058 -0.082
Statistical	± 0.201	± 0.256

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Systematic uncertainties $B^0 \rightarrow K_s^0 \pi^0 \gamma$



Source	$K^{*0} \gamma$		$K_s^0 \pi^0 \gamma$	
	S	C	S	C
E and p scales	± 0.017	± 0.015	± 0.083	± 0.047
Vertex measurement	± 0.021	± 0.009	± 0.023	± 0.036
Flavor tagging	± 0.005	$^{+0.012}_{-0.009}$	± 0.008	$^{+0.013}_{-0.009}$
Event-by-event fractions	± 0.003	$^{+0.004}_{-0.003}$	± 0.032	± 0.013
Resolution functions	± 0.014	± 0.009	± 0.032	± 0.013
Physics parameters	< 0.001	< 0.001	± 0.003	< 0.001
$B\bar{B}$ asymmetries	$^{+0.010}_{-0.021}$	± 0.022	$^{+0.023}_{-0.015}$	$^{+0.032}_{-0.033}$
Tag-side interference	< 0.001	-0.002	$+0.001$	$+0.001$
Total	$+0.033$ -0.037	$+0.032$ -0.031	$+0.100$ -0.098	$+0.071$ -0.070

Systematic uncertainties $B^0 \rightarrow K_s^0 \pi^0$, $B^0 \rightarrow K_s^0 K_s^0 K_s^0$



$B^0 \rightarrow K_s^0 \pi^0$

Source	δC	δS
Flavor tagging	0.013	0.011
Resolution function	0.014	0.022
$B\bar{B}$ background asymmetry	0.030	0.018
$q\bar{q}$ background asymmetry	0.028	< 0.001
Signal modeling	0.004	0.003
Background modeling	0.006	0.018
Fit bias	0.005	0.011
Best candidate selection	0.005	0.010
τ_{B^0} and Δm_d	< 0.001	< 0.001
Tag-side interference	0.006	0.011
VXD misalignment	0.004	0.005
Total	0.047	0.040

$B^0 \rightarrow K_s^0 K_s^0 K_s^0$

Source	S	C
τ_{B^0} , τ_{B^+} , and Δm_d	0.009	0.000
Signal modeling	0.014	0.008
Δt resolution function	0.013	0.008
Background Δt modeling	0.004	0.002
Flavor tagging	0.013	0.012
Fit bias	0.014	0.004
Tag-side interference	0.011	0.006
Vertex reconstruction	0.011	0.004
Tracker misalignment	0.008	0.007
Total	0.032	0.020

Systematic uncertainties $B_s^0 \rightarrow J/\psi K^+ K^-$



* Uncertainties ($\times 0.01$) Dominant sys. Sub-dominant sys. Stat. limited

Source	$ A_0 ^2$	$ A_\perp ^2$	ϕ_s [rad]	$ \lambda $	$\delta_\perp - \delta_0$ [rad]	$\delta_{ } - \delta_0$ [rad]	$\Gamma_s - \Gamma_d$ [ps $^{-1}$]	$\Delta\Gamma_s$ [ps $^{-1}$]	Δm_s [ps $^{-1}$]
Mass parametrization	0.04	0.03	0.03	0.02	0.15	0.12	0.02	0.04	0.03
Mass: shape statistical	0.04	0.04	0.05	0.09	0.62	0.33	0.02	0.01	0.11
Mass factorization	0.11	0.10	0.42	0.19	0.54	0.60	0.12	0.16	0.18
B_c^+ contamination *	0.04	0.05	—	0.02	—	0.17	(0.07)	(0.03)	—
D-wave component	0.04	0.04	0.02	—	0.07	0.13	0.01	0.03	0.02
Ghost tracks	0.07	0.04	0.02	0.10	0.18	0.18	0.02	—	0.01
Multiple candidates	0.01	—	0.27	0.22	0.90	0.41	0.01	0.01	0.24
Particle identification	0.06	0.09	0.27	0.27	1.31	0.51	0.05	0.15	0.46
C_{SP} factors	—	0.01	0.01	0.03	0.73	0.41	—	0.01	0.04
DTR model portability	—	—	0.08	0.03	0.26	0.09	—	—	0.09
DTR calibration	—	—	0.03	0.02	0.11	0.07	—	—	0.05
Time bias correction	0.04	0.05	0.06	0.05	0.77	0.11	0.03	0.05	0.44
Angular efficiency	0.05	0.14	0.25	0.32	0.42	0.44	0.01	0.02	0.13
Angular resolution	0.01	0.01	0.02	0.01	0.02	0.08	—	0.01	0.02
Kinematic weighting	0.24	0.09	0.01	0.01	0.98	0.86	0.02	0.03	0.31
Momentum uncertainty	0.08	0.04	0.04	—	0.07	0.11	0.01	—	0.13
Longitudinal scale	0.07	0.04	0.04	—	0.10	0.09	0.02	—	0.31
Neglected correlations	—	—	—	—	4.20	4.96	—	—	—
Total sys. unc.	0.32	0.24	0.6	0.5	4.8	5.2	0.14	0.24	0.9
Stat. unc.	0.17	0.23	2.2	1.1	7.5	6.0	0.14	0.44	3.3

*The uncertainty of the B_c^+ contamination for $\Delta\Gamma_d^s$ and $\Delta\Gamma_s$ is included in the fit to data and does not contribute to the quoted total systematic uncertainty.

Systematic uncertainties $B_s^0 \rightarrow \phi\phi$



Source	$\phi_s^{s\bar{s}s}$	$ \lambda $	$ A_0 ^2$	$ A_\perp ^2$	$\delta_{ } - \delta_0$	$\delta_\perp - \delta_0$
Time resolution	4.9	2.6	0.8	0.8	0.1	3.4
Flavor tagging	4.8	4.7	0.9	1.3	1.2	9.7
Angular acceptance	3.9	4.9	1.4	1.7	4.7	1.2
Time acceptance	2.3	1.7	0.1	0.1	5.6	0.7
Mass fit & factorization	2.2	4.4	1.9	2.3	2.3	2.5
MC truth match	1.1	0.2	0.1	0.1	0.2	0.3
Fit bias	0.8	0.7	0.9	0.3	3.6	0.7
Candidate multiplicity	0.3	0.2	0.1	0.8	0.2	0.1
Total	8.8	8.6	2.7	3.3	8.5	10.7

Systematic uncertainties $B_s^0 \rightarrow J/\psi \eta' / \pi\pi, \gamma$



$B_s^0 \rightarrow J/\psi \eta' / B_s^0 \rightarrow J/\psi \pi\pi$

$B_s^0 \rightarrow D_s^+ K^-$

Source	Value [ns ⁻¹]
Simulation sample size	4.6
Acceptance Model	3.0
Bin centre method	0.3
<i>CP</i> violation	0.1
Γ_s	0.1
$J/\psi \eta'$ background model	6.9
$J/\psi \pi^+ \pi^-$ background model	0.8
Total	9.0

Source	C_f	$A_f^{\Delta\Gamma}$	$A_{\bar{f}}^{\Delta\Gamma}$	S_f	$S_{\bar{f}}$
Δm_s	0.007	0.004	0.004	0.108	0.103
Detection asymmetry	—	0.079	0.083	0.006	0.007
Multivariate fit	0.045	0.095	0.121	0.088	0.112
Flavour tagging	0.256	0.026	0.028	0.012	0.070
Decay-time resolution model	0.195	0.002	0.003	0.058	0.167
Decay-time bias	0.062	0.027	0.046	0.188	0.167
Decay-time acceptance, Γ_s , $\Delta\Gamma_s$	0.006	0.225	0.231	0.003	0.003
Decay-time acceptance ratios	0.001	0.018	0.018	—	—
Neglecting correlations	0.137	0.081	0.054	0.135	0.043
Total	0.358	0.273	0.285	0.278	0.294