# Time-of-Flight Requirements to Mitigate Blurring Induced by Annihilation Photon Acollinearity

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# *Theoretical* spatial resolution limit at the center of a PET camera [Moses, 2011]

$${\it R_{\sf spatial}} \geq lpha \sqrt{{\it R_p^2 + R_a^2 + R_l^2 + R_{\sf Det}^2}$$

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- R<sub>a</sub>: Annihilation photons acollinearity (APA)



Inspired from www.depts.washington.edu/imreslab

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- *R<sub>a</sub>*: Annihilation photons acollinearity (APA)
- *R*<sub>l</sub>: Detectors coupling
- *R*<sub>Det</sub>: Detectors width (FWHM: *d*/2)



Detection module schematic

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Ultimate "realistic" spatial resolution for a whole-body scanner: 2.49 mm FWHM

- $d = 3.0 \rightarrow 1.5 \text{ mm FWHM}$
- APA of 0.55° FWHM and an 80 cm diameter scanner  $\rightarrow$  1.9 mm FWHM

# Mitigating the effect of detector size using ultrafast TOF



Spatial blur > TOF blur

Hot Spots simulated with 13 ps FWHM TOF [Toussaint et al., 2020b]

#### Results

# Mitigating the effect of detector size using ultrafast TOF



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### **Requirements**:

 $\bullet\,$  TOF FWHM  $\approx\,$  detector size

### Results

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Hot Spots simulated with 13 ps FWHM TOF [Toussaint et al., 2020b]

### **Requirements**:

- TOF FWHM  $\approx$  detector size
- Coincidence event statistics (Inverse problem)

# Ultrafast TOF on APA changes the shape of its blur

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Direct image formation with perfect TOF resolution [Toussaint et al., 2020a]

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#### **Requirements**:

- Only with  $\leq$ 13 ps?
- Achievable with realistic detector size?

### Ultrahigh TOF resolution: are we there yet?



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• 2033: 10 ps

# Ultrahigh TOF resolution: are we there yet?

### Examples of progress in coincidence time resolution:

- 30 ps FWHM (3.2 mm deep; lead glass; MCP-PMT [Ota et al., 2019])
- 123 ps FWHM (2x2x3 mm<sup>3</sup>; BGO; FBK SiPM [Gundacker et al., 2023])
- 95 ps FWHM (3×3×19 mm<sup>3</sup>; LYSO Ce,Ca; HF readout [Nadig et al., 2023])

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- Lower bound of the requirements to **mitigate** the blur induced by **APA** for whole-/total-body PET scanners
  - TOF resolution
  - Coincidence event statistics
- Estimate the potential gain in spatial resolution
  - Is it worth it? [Schaart et al., 2020]

#### GATE 9.2 simulations [Sarrut et al., 2022]

- Scanner diameter: 81 cm (Whole-body PET scanner)
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- Scanner diameter: 81 cm (Whole-body PET scanner)
- Detectors size: 2 mm wide
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- Detectors depth: 0.1 mm (Reduce DOI-induced timing bias)
- No decoding error

#### **TOF resolutions:**

 $\approx$ 13, 26, 65 and 130 ps FWHM (i.e., 2, 4, 5, 20 mm FWHM)

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### **Coincidence event statistics**

- "Typical" acquisition (*FullStat*)
  - Based on the sensitivity of the UHR scanner [Doyon et al., 2023] and converted to the simulated phantom volume

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### **Coincidence event statistics**

- "Typical" acquisition (*FullStat*)
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- Half of the "typical" acquisition (*HalfStat*)
- A tenth of the "typical" acquisition (1/10thStat)

basicTOR:

Back-to-back source with 0.55° FWHM APA [Shibuya et al., 2007]

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Idea:

• "Median" 3D TOR of the EXPLORER: 102 cm long [Badawi et al., 2019]

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- $\bullet\,$  Equivalent to  $0.55^\circ$  FWHM APA for a 102 cm long TOR
- Expected APA blurring: 2.4 mm FWHM
- Theoretical spatial resolution limit: 2.6 mm FWHM

# Quantify spatial resolution gain



A Hot Spots phantom



Another Hot Spots phantom

### Hot Spots phantoms parameter:

- Spots size: 1.0 mm to 3.0 mm with steps of 0.2 mm
- Number of coincidences for *FullStat*:  $\approx$  7 M
- Activity distribution: spot-to-background ratio of 4:1

# Quantify spatial resolution gain



A Hot Spots phantom

### Reconstruction:

- Algorithm: TOF MLEM
- TOF discretization: uniform TOF bins and adapted to TOF resolution
- $\bullet$  System matrix: highly accurate representation with 0.31  $\times$  0.31  $mm^2$  voxels
- Stopping criteria: minimize mean squared error with ground truth



Another Hot Spots phantom

# Quantify spatial resolution gain



A Hot Spots phantom



Another Hot Spots phantom



Position of the line profiles

### Spots resolvability:

- $\bullet\,$  Peak and valley estimation: Mean of a ROI 30% of the spot size
- Background mean was estimated and corrected prior to ratio evaluation
- Decision criterion: ≥90% valley-to-peaks ratio that satisfies the Rayleigh resolution criterion [Hallen et al., 2020]

### In pratice? BigBrain with FDG-like distribution



BigBrain [Amunts et al., 2013]

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BigBrain with FDG-like distribution

Acquisition:

- 128 replications of the 2D scanner axialy (256 mm axial FOV)
- $\approx\!\!13$ , 26, 65 and 130 ps FWHM
- basicTOR vs obliqueTOR
- $\approx 100$  M coincidences



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### Reconstruction:

- MLEM TOF using CASToR with continuous TOF [Merlin et al., 2018]
- Projector: 25 rays multi-Siddon
- $0.4 \times 0.4 \times 0.4 \text{ mm}^3$  voxels



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### Gains (all values are in FWHM):

- 13 ps TOF: 0.8-1.0 mm
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# BigBrain, *basicTOR*



Tranverse view. Same color-scale. Similar noise in the grey matter. *Theoretical* spatial resolution: 2.2 mm FWHM. APA: **1.9 mm FWHM**.

# BigBrain, *basicTOR*







TOF: 65 ps, 12 it.



TOF: 26 ps, 10 it.







TOF: 13 ps, 6 it. Groundtruth ROI position Theoretical spatial resolution: 2.2 mm FWHM

# BigBrain, obliqueTOR



TOF: 65 ps, 12 it.



TOF: 13 ps, 6 it.

Groundtruth

Tranverse view. Same color-scale. Similar noise in the grey matter. *Theoretical* spatial resolution: 2.6 mm FWHM. APA: **2.4 mm FWHM**.

#### Results

# BigBrain, obliqueTOR







TOF: 65 ps, 12 it.



TOF: 26 ps, 8 it.

Carles Sta





TOF: 13 ps, 6 it. Groundtruth ROI position Theoretical spatial resolution: 2.6 mm FWHM

### Main goal:

Investigate the **requirements** on TOF resolution and event statistics to **mitigate the APA**-induced blurring in the context of **whole-body and total-body PET** cameras

### Highlights:

- Hot Spots phantom: gain achieved in all cases (0.4 to 1.0 mm FWHM)
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#### Future works:

• Larger detectors

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### Future works:

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- Better 3D reconstructions (more iterations, better system matrix?)



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# Ultrafast TOF on APA changes the shape of its blur - details

mm, 5k iter

mm 20k iter

mm, 5k iter

15 mm. 20k iter

14 16

8 10

Line profile of two point sources

with 13 ps FWHM TOF

Distance from center, mm



Direct image formation with perfect TOF resolution [Toussaint et al., 2020a]

### **Requirements:**

- Only with <13 ps?
- Achievable with realistic detector size?

2.03

2.02 ntensity, a.u.

2.01

2.00

(106)



Spatial FWHM of point sources with 13 ps FWHM TOF



Theoretical spatial resolution: 2.6 mm FWHM. APA: 2.4 mm FWHM.

TOF: 26 ps, 14 it.

TOF: 130 ps, 28 it.

TOF: 13 ps, 8 it.



Theoretical spatial resolution: 2.2 mm FWHM. APA: 1.9 mm FWHM.



### Gains (all values are in FWHM):

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