#### **GRAPH NEURAL NETWORK PER** L'IDENTIFICAZIONE DI LEPTONI TAU IN ESPERIMENTI AI FUTURI COLLIDER e<sup>+</sup>e<sup>-</sup>

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## INTRODUCTION

- ongoing work aiming at studying and optimising the physics potential of future collider experiments (principally FCCee and CepC)
  - case study: τ-identification with the IDEA dual-readout calorimeter (DRC) concept
    - leverage modern machine learning methods based on differentiable deep neural networks
    - study performance using only standalone DRC information
    - helps also in optimising the detector and design of the readout electronics

#### • tasks studied:

- classification of τ-decays and separation from QCD jets based on Dynamic Graph Neural Networks (DGCNN)
- development of a novel Bayesian-DGCNN for robust estimation of NN predictions
- DGCNN-based object detection (identification of tau/jet constituents) for proto particle-flow algorithms
- evolutions & ononging work:
  - improve object detection capabilities with hybrid architectures: GNN + encoder/decoder Transformer
  - model acceleration on FPGAs for real-time use (triggers/monitor of physics streams/...)
- ML\_INFN/AI\_INFN

• plan to use the results of these studies to prepare one or more tutorials on advanced topics (Bayesian-NN, Hybrid architectures, Model Compression, ...) for



#### FCC-ee & -hh

original study requested by ESPP in 2013, started in 2014 as main way to guarantee research continuity in HEP at CERN in the post HL-LHC era

integrated project in two consecutive phases:

- -stage 2: FCC-hh ~100 TeV hadron collider at the energy frontier + optional ions/eh machines

complementary physics goals & common infrastructures and civil engineering



https://link.springer.com/article/10.1140/epjst/e2019-900045-4 FCC CDRs: https://link.springer.com/article/10.1140/epjst/e2019-900087-0

-stage 1: FCC-ee - ~90-400 GeV e+e- collider as Higgs, EW and top factory at the maximal achievable luminosity









### FCC-ee LUMINOSITY



luminosity x10<sup>3÷5</sup> LEP thanks to the use of techniques developed for B-factories - independent rings for e<sup>+</sup> and e<sup>-</sup>: more bunches, higher currents w/o parasitic collisions - crab waist and asymmetric IP, and continuous injection - parameters optimised to keep same totale power for synchrotron radiation at all CM energies (100 MW) - total consumption with 50% of the klystrons active is 200 MW (compare with LHC: 210 MW and HL-LHC: 260 MW)



100 000 Z / second

- 1Z/second at LEP
- 10 000 W / hour
  - 20 000 W in 5 years at LEP
- 1 500 Higgs bosons / day
  - 10-20 times more than ILC
- 1 500 top quarks / day

 $Ldt \sim 1 - 40 \, \mathrm{ab^{-1}/year}$ HZ Z

√s [GeV]



#### FCC-ee CM ENERGY

15 years physics: 4(Z) + 2(WW) + 3(H) + 1LS + 5(tt) not necessarily in this order ...



-physics at the Z pole allows study of light fermions (τ and b - factory)

the properties of gluons in higgs decays:



- -clean environment and substantial yields open the possibility to study  $e^+e^- \rightarrow HZ \rightarrow gg\mu^+\mu^-$







#### Clic-Like Detector: adapted from CLIC design



- 2T B-field (CMS-style)
- Silicon ID (pixel + tracker)
- 3D imaging Silicon-tungsten ECAL
- Scintillator + FE HCAL
- MS: steel yoke instrumented with RPCs

### **FCC-ee CONCEPTUAL REFERENCE DETECTORS**

International Detector for Electron-positron Accelerators: specific design for FCC-ee / CepC



- 2T SC solenoid 2T ultra-thin and transparent before calorimeters
- Silicon vertex detector + short-drift, ultra-light wire chamber
- Silicon wrapper pre-shower/timing counter
- Single **Dual-readout calorimeter for EM&HAD calorimetry** + optional crystal DR EM
- MS: thin iron yoke equipped with RPCs





### **DRC PRINCIPLE**

correct shower energy event by event for non-compensation by measuring the EM fraction in hadronic shower by sampling with two readouts of different e/h response: Cherenkov (C) mostly sensitive to the em shower component, Scintillation (S) sensitive to all



different patterns of S vs C light from different particles, combined with the fine segmentation provided by the fibres can be leveraged also for powerful particle identification ...









## **IDEA DRC FULL SIMULATION**



#### 



• full G4 simulation of the calorimeter geometry:



- includes B field and solenoid material in front of the calorimeter
- fiber-sampling calorimeter: Cu absorber, 1mm fibres, 1.5mm pitch
- read out of each single fibre via SiPM
- 130 M channels, excellent granularity and lateral shape  $\bullet$ sensitivity:

$$\Delta \theta$$
,  $\Delta \varphi = \sim 0.035^{\circ}$ 

- parametrised simulation of SiPM readout and signal processing
  - dark counts, crosstalk, afterpulses, saturation, noise, ...





### DATASETS



- Pythia8  $e^+e^- \rightarrow Z \rightarrow \tau\tau$  and qq at Z pole
- 5000 events for each decay mode

- Information available for each fibre:
  - geometrical quantities:  $\Delta \theta$ ,  $\Delta \phi$  wrt the tau/jet cluster center  $\bullet$
  - energetic quantities: # of photo-electrons in fibres and energy (scintillation and Cherenkov)  $\bullet$
  - $\bullet$ Threshold, Time of Peak
- Ground truth labels:
  - fiber type (scintillating or cherenkov)  $\bullet$
  - decay type label



SiPM information (1 SiPM per fibre): Integral and Peak of the SiPM output, Time of Arrival, Time over



0

1

 $\mathbf{2}$ 

3

4

 $\mathbf{5}$ 

6



#### **EXAMPLES OF EVENTS WITH FULL GRANULARITY**





#### **EXAMPLES OF EVENTS WITH FULL GRANULARITY**





#### MAIN ISSUES IN TRAINING A DL MODEL TO IDENTIFY **TAUS IN DRC**

- sparsity of data representation: fired fibres are 5-10% of the total  $\leftarrow$  makes use of CNN architectures inefficient and hard to train
  - **solution:** use point-cloud/graph representations

- ability to extract confidence measures on the prediction of the ANN models modern modern ANNs are known to be not well calibrated (e.g. softmax outputs vs true class probabilities)
  - solution: calibrate the ANN output, for example by using dropout to adjust the output, or by using conformal predictions or bayesian weights to directly quantify the model uncertainty



### DATA REPRESENTATION

- Image-based: treating the energy deposition on each fiber as the pixel intensity creates an image of the event in fixed-shape mesh
  Point cloud-based: unordered sets of entities distributed irregularly in space, analogous to the point cloud representation of 3D shapes
  - natural representation for Convolutional Neural Networks
  - unclear how to incorporate additional information from the fibers
  - very sparse and inefficient representation: jets/tau decays have O(10) to O(100) particles → more than 90% of the pixels are blank



- clouds allow rich internal structures
- straightforward to incorporate additional information of the fibers (fibre type, energy, time information, ...)
- the architecture of the neural network has to be carefully designed to fully exploit the potential of this representation → Graph Neural Networks (also RNN, Transformers, ...)

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## **DGCNN ARCHITECTURE**



#### local feature extractor $x = \{\theta, \phi, geometrical features, \}$ SiPM features, ...}

- simplify inclusion of additional features and SiPM information
- zero valued vectors and masking in case of events with lower active fibres
- hyper-parameters chosen using a validation set

Y. Wang et al., arXiv:1801.07829 [cs.CV]





- simple and flexible architecture optimised for point cloud inputs able to learn both local (trough the edge convolution) and global (through skip connections & feature aggregator) structures on the input data

- # of input fibres fixed and treated as model hyper parameter, discarding those with lowest signals or adding







## EDGE CONVOLUTION

Regular convolution operators cannot be applied on point clouds:

- points distribution is usually irregular (unlike uniform grids of the pixels in an image) - they're not invariant under permutation of the points

which is possible to define convolution operations







Viable solution: EDGE convolution: point cloud represented as a graph with Vertices (the points themselves) and Edges (connections between each point to its k nearest neighbouring points): results in a regular distribution for each point, for





## **τ DECAY IDENTIFICATION WITH DGCNN**

- Classification task:
  - 8-classes: 7 tau decays + QCD jets
  - training/validation/test sets: 22k/6k/7k events (balanced among classes)  $\bullet$
- Data-preprocessing:
  - simple geometrical clustering, no specific selection or fiducial volume applied • saved fibres signal around each cluster  $(\sqrt{\Delta\theta^2 + \Delta\phi^2}) < 1)$
- DGCNN inputs:
  - jet/tau representation: 2D point-cloud of fibres coordinates
  - fiber type (S, C), #photo-electrons, SiPM's: Integral and Peak of the SiPM output, ToT, ToA, ToP (in different combinations)

S.Giagu, M. di Filippo, L.Torresi, Tau leptons identification with Graph Neural Networks at future electron-positron colliders, Front. Phys., Volume 10 - 2022 16





## DATA AUGMENTATION VIA DROPOUT

- - exposed to the network
- much better generalisation obtained leveraging both methods
- dropout levels optimised on validation set



overfitting and memorisation for the DGNN model controlled using two different implementations of the dropout regularisation: • (traditional) in the network: some of the parameters of the last MLP block are randomly zeroed during the training phase • (as data augmentation/perturbation regularisation) at input level: some of the fired fibers are switched off before to be



S.Giagu, M. di Filippo, L.Torresi, Front. Phys., Volume 10 - 2022 17







## **IDEAL PERFORMANCE ON TEST SET**

8-class classification task w/ DGCNN

small confusion only within topologically similar decays

	τ→evv	98.53	0.45	0.65	
	τ →πν	3.20	91.35	2.21	
	τ →ππ <sup>0</sup> ν	1.34	3.49	86.87	
BB	τ →ππ <sup>0</sup> π <sup>0</sup> ν	0.46	0.25	12.09	Ş
Truth	τ →πππν	0.11	3.14	1.24	
•	τ →ππππ <sup>0</sup> ν	0.16	0.30	1.82	
	$\tau \rightarrow \mu \nu \nu$	1.24	0.25	0.06	
	Z →qq jets	0.13	0.21	0.21	
		r ou	× 12		

stat. uncertainty on accuracies ~3÷5%

#### input features: coordinates, type of fibre (S/C), and #of photo-electrons in each fibre





small confusion only within topologically similar decays

Predicted BR

S.Giagu, M. di Filippo, L.Torresi, <u>Front. Phys., Volume 10 - 2022</u> 18





#### PERFORMANCE ONLY USING GEOMETRICAL OR GEOM. + FIBER TYPE INFORMATION

#### input features: coordinates only

	T→evv	90.36	4.07	2.21	0.03	0.00	0.00	3.34	0.00
Truth BR	$T \rightarrow TTV$	2.57	86.24	5.39	0.25	3.59	0.17	1.57	0.22
	$T \rightarrow \Pi \Pi^0 V$	2.10	18.92	72.67	2.76	1.97	1.01	0.27	0.30
	$T \rightarrow \pi \pi^0 \pi^0 V$	0.74	3.54	58.43	33.04	0.84	2.81	0.05	0.54
	τ →πππν	0.11	9.88	6.22	0.46	75.32	6.49	0.00	1.52
	$T \rightarrow \Pi \Pi \Pi \Pi \Pi^0 V$	0.11	1.49	9.30	2.90	38.28	43.75	0.05	4.12
	$\tau \to \mu \nu \nu$	2.50	0.70	0.17	0.00	0.03	0.00	96.60	0.00
	Z →qq jets	0.08	0.33	0.63	0.94	2.92	3.09	0.08	91.92
		~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	× \					× ×	~ ~ ~
		-2	2	2	'ho2	ToToL	TT	ITTTO	×42 S

#### **coordinates + type** of fibre (S/C)

→evv	90.36	4.07	2.21	0.03	0.00	0.00	3.34	0.00		T →evv	96.95	0.79	0.62	0.03	0.00	0.00	1.58	0.03	
→πv	2.57	86.24	5.39	0.25	3.59	0.17	1.57	0.22		$T \rightarrow TTV$	3.09	89.03	3.48	0.41	2.02	0.39	1.44	0.14	
→ππ <sup>0</sup> ∨	2.10	18.92	72.67	2.76	1.97	1.01	0.27	0.30	Ř	$T \rightarrow \pi \pi^0 V$	1.77	4.83	80.45	9.25	1.61	1.67	0.16	0.25	
τπ <sup>0</sup> π <sup>0</sup> ν	0.74	3.54	58.43	33.04	0.84	2.81	0.05	0.54	lth B	τ →ππ <sup>0</sup> π <sup>0</sup> ν	0.30	0.38	10.43	84.55	0.16	3.87	0.05	0.25	
πππν	0.11	9.88	6.22	0.46	75.32	6.49	0.00	1.52	Tru	Τ →ΠΠΠΛ	0.16	3.52	1.38	0.35	84.82	8.79	0.03	0.95	
ппп <sup>0</sup> v	0.11	1.49	9.30	2.90	38.28	43.75	0.05	4.12	-	τ →ππππ <sup>0</sup> ν	0.11	0.24	1.98	2.60	10.19	82.60	0.08	2.20	
μνν	2.50	0.70	0.17	0.00	0.03	0.00	96.60	0.00		$\tau \to \mu \nu \nu$	2.53	0.48	0.11	0.00	0.03	0.00	96.82	0.03	
q jets	0.08	0.33	0.63	0.94	2.92	3.09	0.08	91.92		Z →qq jets	0.08	0.25	0.19	1.05	2.54	4.08	0.06	91.75	
Predicted BR Predicted BR										in jers									
average accuracy: 73.7%						average accuracy: 88.3%						)							
double-readout geometry alone allows excellent tau identification																			



#### PERFORMANCE USING REALISTIC SIPM READOUT INFORMATION

#### using only geometry and Integral/Peak of the signal

average accuracy: 88.8%



comparable identification performance w/r the ideal case

adding also SiPM timing information average accuracy: **91.4%** 

![](_page_19_Figure_7.jpeg)

**Truth BR** 

![](_page_19_Figure_10.jpeg)

### CHECK OF POSSIBLE BIAS ON ENERGY

![](_page_20_Figure_1.jpeg)

no bias observed over distribution of total energy per event

#### **UNCERTAINTY IN THE CLASSIFICATION: BAYESIAN-DGCNN**

- Neural networks based on point values for weights may suffer of overconfidence when analysing new data especially for predictions in regions with few or w/o examples in the training set
- Bayesian neural networks mitigate the problem by introducing probability distributions over the weights and predicting distributions instead of point values
  - a Bayesian-NN learns a variational approximation of the true posterior distribution P(w|D), and predict an estimate of the expected value E<sub>P(w|D)</sub>[P(y|x,w)] → since the weights are random variables, each predictions is a random variable too
  - allows to measure uncertainty, identify outliers in the input, regularise the whole model
- Designed and implemented in pytorch a full Bayesian version of a DGCNN (leveraging the Bayes by Backprop algorithm (<u>https://arxiv.org/abs/1505.05424</u>):

$$p(y \mid x, D) = \int p(x \mid y, w) p(w \mid D) dw$$

bayesian inference

generally intractable via MC integration

replace it with a variational (eg optimisation) problem

![](_page_21_Figure_10.jpeg)

![](_page_21_Picture_11.jpeg)

#### $p(w \mid D) \approx q_{\theta}(w \mid D)$

approximate p with a more tractable parametric distribution q (eg. gaussian) w/ learnable parameters (eg a NN)

![](_page_21_Picture_14.jpeg)

### **BAYES BY BACKPROP**

find optimal  $\theta^*$  by minimising the Kullback-Leibler divergence between p and q

θ

$$\mathsf{KL}[q_{\theta}(w \mid D) \parallel p(w \mid D)] = \int q_{\theta}(w \mid D) \log \frac{q_{\theta}(w \mid D)}{p(w \mid D)} dw$$

![](_page_22_Figure_4.jpeg)

in practice as  $q_{\theta}$  is an ANN, the Kingma local reparameterization trick is used to make the whole expression differentiable

![](_page_22_Picture_6.jpeg)

#### $\theta^* = \arg\min \mathsf{KL}[q_{\theta}(w \mid D) \parallel p(w \mid D)]$

we have another integral here, but now q is more tractable and we can approximated it via MC sampling

with  $w^{(i)}$  samples sampled from  $q_{\theta}(w \mid D)$ 

<u>Blundell et al., arXiv:1505.05424</u>

![](_page_22_Picture_11.jpeg)

### **BAYESIAN-DGCNN**

![](_page_23_Figure_1.jpeg)

- better classification performance wrt the point DGCNN
- class probabilities better aligned with physics expectations

![](_page_23_Figure_5.jpeg)

all bayesian layers (EdgeConv, MLP, etc.), w/ gaussian priors (uncorrelated between layers and neurons)

![](_page_23_Figure_8.jpeg)

![](_page_23_Picture_9.jpeg)

### **BAYESIAN-DGCNN**

ROC for  $\tau \rightarrow \pi \pi^0 v$  vs all other channels

![](_page_24_Figure_2.jpeg)

ROC for  $\tau \rightarrow \pi \pi \pi \nu$  vs all other channels

![](_page_24_Figure_4.jpeg)

![](_page_24_Figure_5.jpeg)

![](_page_24_Picture_6.jpeg)

![](_page_24_Picture_7.jpeg)

### **BAYESIAN-DGCNN**

![](_page_25_Figure_1.jpeg)

B-DGCNN:10 samples per prediction no threshold on minimum confidence

B-DGCNN:10 samples per prediction minimum threshold on confidence 0.7

Number of	Minimum	Events	Test A
Samples	Confidence	Considered	
1 3 10	0.0	100 %	0. 0. 0.
3	0.5	94.83 %	0.
	0.7	80.33 %	0.
	0.9	62.27 %	0.
10	0.5	94.72 %	0.9
	0.7	79.82 %	0.9
	0.9	60.52 %	0.9

![](_page_25_Picture_5.jpeg)

![](_page_25_Picture_6.jpeg)

### JET CONSTITUENTS ID

- DGCNN and dual-readout calorimeter high granularity can be exploited for object (particle) detection inside taus and jets
  - a proto-step for a particle flow algorithms
  - can be implemented with a similar approach as in segmentation tasks (eg pixel/node/fiber-level classification)
- DenseNet like modification of the DGCNN architecture for a segmentation task:

![](_page_26_Figure_5.jpeg)

- identify the particle associated to the larger energy deposit in each fibre
- label each fibre by extrapolating Monte Carlo truth particles from production to the DRC into the IDEA magnetic
- redict the label associated to each fibre train the DGCN
- Initial study: ເພາະອີບວint DGCNN only

![](_page_26_Figure_10.jpeg)

![](_page_26_Figure_15.jpeg)

![](_page_26_Figure_16.jpeg)

![](_page_26_Picture_17.jpeg)

### **RESULTS SEGMENTATION**

Two nice examples:  $\tau^{\pm} \rightarrow \pi^{\pm} \pi^{0} \nu_{\tau} \rightarrow \pi^{\pm} \gamma \gamma \nu_{\tau}$ 

![](_page_27_Figure_2.jpeg)

![](_page_27_Picture_3.jpeg)

#### tau visibile energy reconstructed using:

- DRC for photons

ruth for other particles

![](_page_27_Picture_7.jpeg)

![](_page_27_Picture_8.jpeg)

## **RESULTS SEGMENTATION**

#### Two "less nice" results:

ex 1  $\tau \rightarrow e \nu_e \nu_\tau$ 

![](_page_28_Figure_3.jpeg)

#### **Ground Truth**

![](_page_28_Figure_5.jpeg)

ex 2

 $\tau \to \pi \pi^0 \nu_\tau \to \pi \gamma \gamma \nu_\tau$ 

w/ overlapping photons

![](_page_28_Figure_9.jpeg)

![](_page_28_Figure_10.jpeg)

#### Reconstructed

![](_page_28_Figure_12.jpeg)

![](_page_28_Picture_13.jpeg)

### **ONGOING DEVELOPMENTS**

- improve jet constituents ID by moving from DGCNN segmentation to Graph-Transformer object detection
- hybrid architecture: GNN → high-level representation → Transformed encoder/decoder → bounding box predictions
  - GNN encode the graph for the transformed architecture and extracts compact representation of the global graph structure
  - the transformer encoder process this data to produce an embedding context representing the whole graph
  - this embedding is passed to a transformer decoder that takes as input a small fixed of learned positional embeddings (object queries) and attends to the encoder output
  - the self-attention and the encoder-decoder attention over the embedding and the object queries allows the model to analyse all objects together using pair-wise relations between them, and to independently decode it into box coordinates and class labels by a FFN head
  - the FFN head is a shared MLP that predict class and bounding box for each object
- results will be ready in time for the fall meetings/conferences ...

![](_page_29_Figure_10.jpeg)

![](_page_29_Figure_11.jpeg)

![](_page_29_Picture_12.jpeg)