GRAPH NEURAL NETWORK PER L'IDENTIFICAZIONE DI LEPTONI TAU IN ESPERIMENTI AI FUTURI COLLIDER e⁺e⁻

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INTRODUCTION

- ongoing work aiming at studying and optimising the physics potential of future collider experiments (principally FCCee and CepC)
 - case study: τ-identification with the IDEA dual-readout calorimeter (DRC) concept
 - leverage modern machine learning methods based on differentiable deep neural networks
 - study performance using only standalone DRC information
 - helps also in optimising the detector and design of the readout electronics

• tasks studied:

- classification of τ-decays and separation from QCD jets based on Dynamic Graph Neural Networks (DGCNN)
- development of a novel Bayesian-DGCNN for robust estimation of NN predictions
- DGCNN-based object detection (identification of tau/jet constituents) for proto particle-flow algorithms
- evolutions & ononging work:
 - improve object detection capabilities with hybrid architectures: GNN + encoder/decoder Transformer
 - model acceleration on FPGAs for real-time use (triggers/monitor of physics streams/...)
- ML_INFN/AI_INFN

• plan to use the results of these studies to prepare one or more tutorials on advanced topics (Bayesian-NN, Hybrid architectures, Model Compression, ...) for



FCC-ee & -hh

original study requested by ESPP in 2013, started in 2014 as main way to guarantee research continuity in HEP at CERN in the post HL-LHC era

integrated project in two consecutive phases:

- -stage 2: FCC-hh ~100 TeV hadron collider at the energy frontier + optional ions/eh machines

complementary physics goals & common infrastructures and civil engineering



https://link.springer.com/article/10.1140/epjst/e2019-900045-4 FCC CDRs: https://link.springer.com/article/10.1140/epjst/e2019-900087-0

-stage 1: FCC-ee - ~90-400 GeV e+e- collider as Higgs, EW and top factory at the maximal achievable luminosity









FCC-ee LUMINOSITY



luminosity x10^{3÷5} LEP thanks to the use of techniques developed for B-factories - independent rings for e⁺ and e⁻: more bunches, higher currents w/o parasitic collisions - crab waist and asymmetric IP, and continuous injection - parameters optimised to keep same totale power for synchrotron radiation at all CM energies (100 MW) - total consumption with 50% of the klystrons active is 200 MW (compare with LHC: 210 MW and HL-LHC: 260 MW)



100 000 Z / second

- 1Z/second at LEP
- 10 000 W / hour
 - 20 000 W in 5 years at LEP
- 1 500 Higgs bosons / day
 - 10-20 times more than ILC
- 1 500 top quarks / day

 $Ldt \sim 1 - 40 \, \mathrm{ab^{-1}/year}$ HZ Z

√s [GeV]



FCC-ee CM ENERGY

15 years physics: 4(Z) + 2(WW) + 3(H) + 1LS + 5(tt) not necessarily in this order ...



-physics at the Z pole allows study of light fermions (τ and b - factory)

the properties of gluons in higgs decays:



- -clean environment and substantial yields open the possibility to study $e^+e^- \rightarrow HZ \rightarrow gg\mu^+\mu^-$







Clic-Like Detector: adapted from CLIC design



- 2T B-field (CMS-style)
- Silicon ID (pixel + tracker)
- 3D imaging Silicon-tungsten ECAL
- Scintillator + FE HCAL
- MS: steel yoke instrumented with RPCs

FCC-ee CONCEPTUAL REFERENCE DETECTORS

International Detector for Electron-positron Accelerators: specific design for FCC-ee / CepC



- 2T SC solenoid 2T ultra-thin and transparent before calorimeters
- Silicon vertex detector + short-drift, ultra-light wire chamber
- Silicon wrapper pre-shower/timing counter
- Single **Dual-readout calorimeter for EM&HAD calorimetry** + optional crystal DR EM
- MS: thin iron yoke equipped with RPCs





DRC PRINCIPLE

correct shower energy event by event for non-compensation by measuring the EM fraction in hadronic shower by sampling with two readouts of different e/h response: Cherenkov (C) mostly sensitive to the em shower component, Scintillation (S) sensitive to all



different patterns of S vs C light from different particles, combined with the fine segmentation provided by the fibres can be leveraged also for powerful particle identification ...









IDEA DRC FULL SIMULATION





• full G4 simulation of the calorimeter geometry:



- includes B field and solenoid material in front of the calorimeter
- fiber-sampling calorimeter: Cu absorber, 1mm fibres, 1.5mm pitch
- read out of each single fibre via SiPM
- 130 M channels, excellent granularity and lateral shape \bullet sensitivity:

$$\Delta \theta$$
, $\Delta \varphi = \sim 0.035^{\circ}$

- parametrised simulation of SiPM readout and signal processing
 - dark counts, crosstalk, afterpulses, saturation, noise, ...





DATASETS



- Pythia8 $e^+e^- \rightarrow Z \rightarrow \tau\tau$ and qq at Z pole
- 5000 events for each decay mode

- Information available for each fibre:
 - geometrical quantities: $\Delta \theta$, $\Delta \phi$ wrt the tau/jet cluster center \bullet
 - energetic quantities: # of photo-electrons in fibres and energy (scintillation and Cherenkov) \bullet
 - \bullet Threshold, Time of Peak
- Ground truth labels:
 - fiber type (scintillating or cherenkov) \bullet
 - decay type label



SiPM information (1 SiPM per fibre): Integral and Peak of the SiPM output, Time of Arrival, Time over



0

1

 $\mathbf{2}$

3

4

 $\mathbf{5}$

6



EXAMPLES OF EVENTS WITH FULL GRANULARITY





EXAMPLES OF EVENTS WITH FULL GRANULARITY





MAIN ISSUES IN TRAINING A DL MODEL TO IDENTIFY **TAUS IN DRC**

- sparsity of data representation: fired fibres are 5-10% of the total \leftarrow makes use of CNN architectures inefficient and hard to train
 - **solution:** use point-cloud/graph representations

- ability to extract confidence measures on the prediction of the ANN models modern modern ANNs are known to be not well calibrated (e.g. softmax outputs vs true class probabilities)
 - solution: calibrate the ANN output, for example by using dropout to adjust the output, or by using conformal predictions or bayesian weights to directly quantify the model uncertainty



DATA REPRESENTATION

- Image-based: treating the energy deposition on each fiber as the pixel intensity creates an image of the event in fixed-shape mesh
 Point cloud-based: unordered sets of entities distributed irregularly in space, analogous to the point cloud representation of 3D shapes
 - natural representation for Convolutional Neural Networks
 - unclear how to incorporate additional information from the fibers
 - very sparse and inefficient representation: jets/tau decays have O(10) to O(100) particles → more than 90% of the pixels are blank



- clouds allow rich internal structures
- straightforward to incorporate additional information of the fibers (fibre type, energy, time information, ...)
- the architecture of the neural network has to be carefully designed to fully exploit the potential of this representation → Graph Neural Networks (also RNN, Transformers, ...)

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DGCNN ARCHITECTURE



local feature extractor $x = \{\theta, \phi, geometrical features, \}$ SiPM features, ...}

- simplify inclusion of additional features and SiPM information
- zero valued vectors and masking in case of events with lower active fibres
- hyper-parameters chosen using a validation set

Y. Wang et al., arXiv:1801.07829 [cs.CV]





- simple and flexible architecture optimised for point cloud inputs able to learn both local (trough the edge convolution) and global (through skip connections & feature aggregator) structures on the input data

- # of input fibres fixed and treated as model hyper parameter, discarding those with lowest signals or adding







EDGE CONVOLUTION

Regular convolution operators cannot be applied on point clouds:

- points distribution is usually irregular (unlike uniform grids of the pixels in an image) - they're not invariant under permutation of the points

which is possible to define convolution operations







Viable solution: EDGE convolution: point cloud represented as a graph with Vertices (the points themselves) and Edges (connections between each point to its k nearest neighbouring points): results in a regular distribution for each point, for





τ DECAY IDENTIFICATION WITH DGCNN

- Classification task:
 - 8-classes: 7 tau decays + QCD jets
 - training/validation/test sets: 22k/6k/7k events (balanced among classes) \bullet
- Data-preprocessing:
 - simple geometrical clustering, no specific selection or fiducial volume applied • saved fibres signal around each cluster $(\sqrt{\Delta\theta^2 + \Delta\phi^2}) < 1)$
- DGCNN inputs:
 - jet/tau representation: 2D point-cloud of fibres coordinates
 - fiber type (S, C), #photo-electrons, SiPM's: Integral and Peak of the SiPM output, ToT, ToA, ToP (in different combinations)

S.Giagu, M. di Filippo, L.Torresi, Tau leptons identification with Graph Neural Networks at future electron-positron colliders, Front. Phys., Volume 10 - 2022 16





DATA AUGMENTATION VIA DROPOUT

- - exposed to the network
- much better generalisation obtained leveraging both methods
- dropout levels optimised on validation set



overfitting and memorisation for the DGNN model controlled using two different implementations of the dropout regularisation: • (traditional) in the network: some of the parameters of the last MLP block are randomly zeroed during the training phase • (as data augmentation/perturbation regularisation) at input level: some of the fired fibers are switched off before to be



S.Giagu, M. di Filippo, L.Torresi, Front. Phys., Volume 10 - 2022 17







IDEAL PERFORMANCE ON TEST SET

8-class classification task w/ DGCNN

small confusion only within topologically similar decays

| | τ→evv | 98.53 | 0.45 | 0.65 | |
|-------|-------------------------------------|-------|-------|-------|---|
| | τ →πν | 3.20 | 91.35 | 2.21 | |
| | τ →ππ ⁰ ν | 1.34 | 3.49 | 86.87 | |
| BB | τ →ππ ⁰ π ⁰ ν | 0.46 | 0.25 | 12.09 | Ş |
| Truth | τ →πππν | 0.11 | 3.14 | 1.24 | |
| • | τ →ππππ ⁰ ν | 0.16 | 0.30 | 1.82 | |
| | $\tau \rightarrow \mu \nu \nu$ | 1.24 | 0.25 | 0.06 | |
| | Z →qq jets | 0.13 | 0.21 | 0.21 | |
| | | r ou | × 12 | | |

stat. uncertainty on accuracies ~3÷5%

input features: coordinates, type of fibre (S/C), and #of photo-electrons in each fibre





small confusion only within topologically similar decays

Predicted BR

S.Giagu, M. di Filippo, L.Torresi, <u>Front. Phys., Volume 10 - 2022</u> 18





PERFORMANCE ONLY USING GEOMETRICAL OR GEOM. + FIBER TYPE INFORMATION

input features: coordinates only

| | T→evv | 90.36 | 4.07 | 2.21 | 0.03 | 0.00 | 0.00 | 3.34 | 0.00 |
|----------|---|---|--------|-------|-------|-------|-------|-------|----------|
| Truth BR | $T \rightarrow TTV$ | 2.57 | 86.24 | 5.39 | 0.25 | 3.59 | 0.17 | 1.57 | 0.22 |
| | $T \rightarrow \Pi \Pi^0 V$ | 2.10 | 18.92 | 72.67 | 2.76 | 1.97 | 1.01 | 0.27 | 0.30 |
| | $T \rightarrow \pi \pi^0 \pi^0 V$ | 0.74 | 3.54 | 58.43 | 33.04 | 0.84 | 2.81 | 0.05 | 0.54 |
| | τ →πππν | 0.11 | 9.88 | 6.22 | 0.46 | 75.32 | 6.49 | 0.00 | 1.52 |
| | $T \rightarrow \Pi \Pi \Pi \Pi \Pi^0 V$ | 0.11 | 1.49 | 9.30 | 2.90 | 38.28 | 43.75 | 0.05 | 4.12 |
| | $\tau \to \mu \nu \nu$ | 2.50 | 0.70 | 0.17 | 0.00 | 0.03 | 0.00 | 96.60 | 0.00 |
| | Z →qq jets | 0.08 | 0.33 | 0.63 | 0.94 | 2.92 | 3.09 | 0.08 | 91.92 |
| | | ~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~ | × \ | | | | | × × | ~ ~ ~ |
| | | -2 | 2 | 2 | 'ho2 | ToToL | TT | ITTTO | ×42 S |

coordinates + type of fibre (S/C)

| →evv | 90.36 | 4.07 | 2.21 | 0.03 | 0.00 | 0.00 | 3.34 | 0.00 | | T →evv | 96.95 | 0.79 | 0.62 | 0.03 | 0.00 | 0.00 | 1.58 | 0.03 | |
|---|-------|-------|-------|-------|-------|-------------------------|-------|-------|-------|-------------------------------------|-------|-------|-------|-------|-------|-------|-------|-------|--|
| →πv | 2.57 | 86.24 | 5.39 | 0.25 | 3.59 | 0.17 | 1.57 | 0.22 | | $T \rightarrow TTV$ | 3.09 | 89.03 | 3.48 | 0.41 | 2.02 | 0.39 | 1.44 | 0.14 | |
| →ππ ⁰ ∨ | 2.10 | 18.92 | 72.67 | 2.76 | 1.97 | 1.01 | 0.27 | 0.30 | Ř | $T \rightarrow \pi \pi^0 V$ | 1.77 | 4.83 | 80.45 | 9.25 | 1.61 | 1.67 | 0.16 | 0.25 | |
| τπ ⁰ π ⁰ ν | 0.74 | 3.54 | 58.43 | 33.04 | 0.84 | 2.81 | 0.05 | 0.54 | lth B | τ →ππ ⁰ π ⁰ ν | 0.30 | 0.38 | 10.43 | 84.55 | 0.16 | 3.87 | 0.05 | 0.25 | |
| πππν | 0.11 | 9.88 | 6.22 | 0.46 | 75.32 | 6.49 | 0.00 | 1.52 | Tru | Τ →ΠΠΠΛ | 0.16 | 3.52 | 1.38 | 0.35 | 84.82 | 8.79 | 0.03 | 0.95 | |
| ппп ⁰ v | 0.11 | 1.49 | 9.30 | 2.90 | 38.28 | 43.75 | 0.05 | 4.12 | - | τ →ππππ ⁰ ν | 0.11 | 0.24 | 1.98 | 2.60 | 10.19 | 82.60 | 0.08 | 2.20 | |
| μνν | 2.50 | 0.70 | 0.17 | 0.00 | 0.03 | 0.00 | 96.60 | 0.00 | | $\tau \to \mu \nu \nu$ | 2.53 | 0.48 | 0.11 | 0.00 | 0.03 | 0.00 | 96.82 | 0.03 | |
| q jets | 0.08 | 0.33 | 0.63 | 0.94 | 2.92 | 3.09 | 0.08 | 91.92 | | Z →qq jets | 0.08 | 0.25 | 0.19 | 1.05 | 2.54 | 4.08 | 0.06 | 91.75 | |
| Predicted BR Predicted BR | | | | | | | | | | in jers | | | | | | | | | |
| average accuracy: 73.7% | | | | | | average accuracy: 88.3% | | | | | |) | | | | | | | |
| double-readout geometry alone allows excellent tau identification | | | | | | | | | | | | | | | | | | | |



PERFORMANCE USING REALISTIC SIPM READOUT INFORMATION

using only geometry and Integral/Peak of the signal

average accuracy: 88.8%



comparable identification performance w/r the ideal case

adding also SiPM timing information average accuracy: **91.4%**



Truth BR



CHECK OF POSSIBLE BIAS ON ENERGY



no bias observed over distribution of total energy per event

UNCERTAINTY IN THE CLASSIFICATION: BAYESIAN-DGCNN

- Neural networks based on point values for weights may suffer of overconfidence when analysing new data especially for predictions in regions with few or w/o examples in the training set
- Bayesian neural networks mitigate the problem by introducing probability distributions over the weights and predicting distributions instead of point values
 - a Bayesian-NN learns a variational approximation of the true posterior distribution P(w|D), and predict an estimate of the expected value E_{P(w|D)}[P(y|x,w)] → since the weights are random variables, each predictions is a random variable too
 - allows to measure uncertainty, identify outliers in the input, regularise the whole model
- Designed and implemented in pytorch a full Bayesian version of a DGCNN (leveraging the Bayes by Backprop algorithm (<u>https://arxiv.org/abs/1505.05424</u>):

$$p(y \mid x, D) = \int p(x \mid y, w) p(w \mid D) dw$$

bayesian inference

generally intractable via MC integration

replace it with a variational (eg optimisation) problem

$p(w \mid D) \approx q_{\theta}(w \mid D)$

approximate p with a more tractable parametric distribution q (eg. gaussian) w/ learnable parameters (eg a NN)

BAYES BY BACKPROP

find optimal θ^* by minimising the Kullback-Leibler divergence between p and q

θ

$$\mathsf{KL}[q_{\theta}(w \mid D) \parallel p(w \mid D)] = \int q_{\theta}(w \mid D) \log \frac{q_{\theta}(w \mid D)}{p(w \mid D)} dw$$

in practice as q_{θ} is an ANN, the Kingma local reparameterization trick is used to make the whole expression differentiable

$\theta^* = \arg\min \mathsf{KL}[q_{\theta}(w \mid D) \parallel p(w \mid D)]$

we have another integral here, but now q is more tractable and we can approximated it via MC sampling

with $w^{(i)}$ samples sampled from $q_{\theta}(w \mid D)$

<u>Blundell et al., arXiv:1505.05424</u>

BAYESIAN-DGCNN

- better classification performance wrt the point DGCNN
- class probabilities better aligned with physics expectations

all bayesian layers (EdgeConv, MLP, etc.), w/ gaussian priors (uncorrelated between layers and neurons)

BAYESIAN-DGCNN

ROC for $\tau \rightarrow \pi \pi^0 v$ vs all other channels

ROC for $\tau \rightarrow \pi \pi \pi \nu$ vs all other channels

BAYESIAN-DGCNN

B-DGCNN:10 samples per prediction no threshold on minimum confidence

B-DGCNN:10 samples per prediction minimum threshold on confidence 0.7

| Number of | Minimum | Events | Test A |
|--------------|------------|------------|----------------|
| Samples | Confidence | Considered | |
| 1 3 10 | 0.0 | 100 % | 0. 0. 0. |
| 3 | 0.5 | 94.83 % | 0. |
| | 0.7 | 80.33 % | 0. |
| | 0.9 | 62.27 % | 0. |
| 10 | 0.5 | 94.72 % | 0.9 |
| | 0.7 | 79.82 % | 0.9 |
| | 0.9 | 60.52 % | 0.9 |

JET CONSTITUENTS ID

- DGCNN and dual-readout calorimeter high granularity can be exploited for object (particle) detection inside taus and jets
 - a proto-step for a particle flow algorithms
 - can be implemented with a similar approach as in segmentation tasks (eg pixel/node/fiber-level classification)
- DenseNet like modification of the DGCNN architecture for a segmentation task:

- identify the particle associated to the larger energy deposit in each fibre
- label each fibre by extrapolating Monte Carlo truth particles from production to the DRC into the IDEA magnetic
- redict the label associated to each fibre train the DGCN
- Initial study: ເພາະອີບວint DGCNN only

RESULTS SEGMENTATION

Two nice examples: $\tau^{\pm} \rightarrow \pi^{\pm} \pi^{0} \nu_{\tau} \rightarrow \pi^{\pm} \gamma \gamma \nu_{\tau}$

tau visibile energy reconstructed using:

- DRC for photons

ruth for other particles

RESULTS SEGMENTATION

Two "less nice" results:

ex 1 $\tau \rightarrow e \nu_e \nu_\tau$

Ground Truth

ex 2

 $\tau \to \pi \pi^0 \nu_\tau \to \pi \gamma \gamma \nu_\tau$

w/ overlapping photons

Reconstructed

ONGOING DEVELOPMENTS

- improve jet constituents ID by moving from DGCNN segmentation to Graph-Transformer object detection
- hybrid architecture: GNN → high-level representation → Transformed encoder/decoder → bounding box predictions
 - GNN encode the graph for the transformed architecture and extracts compact representation of the global graph structure
 - the transformer encoder process this data to produce an embedding context representing the whole graph
 - this embedding is passed to a transformer decoder that takes as input a small fixed of learned positional embeddings (object queries) and attends to the encoder output
 - the self-attention and the encoder-decoder attention over the embedding and the object queries allows the model to analyse all objects together using pair-wise relations between them, and to independently decode it into box coordinates and class labels by a FFN head
 - the FFN head is a shared MLP that predict class and bounding box for each object
- results will be ready in time for the fall meetings/conferences ...

