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# Online Track Reconstruction and Calibration for the Mu3e Experiment

Haris Murugan

Supervisor: Prof. Dr. Niklaus Berger

“Monthly Review Meeting of Intense”

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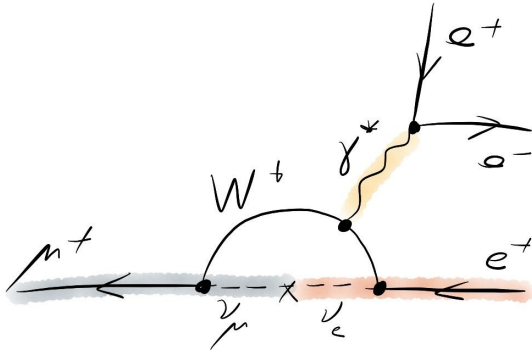
Institute of Nuclear Physics,  
**Johannes Gutenberg-Universität Mainz**



H2020 MSCA ITN  
G.A. 858199

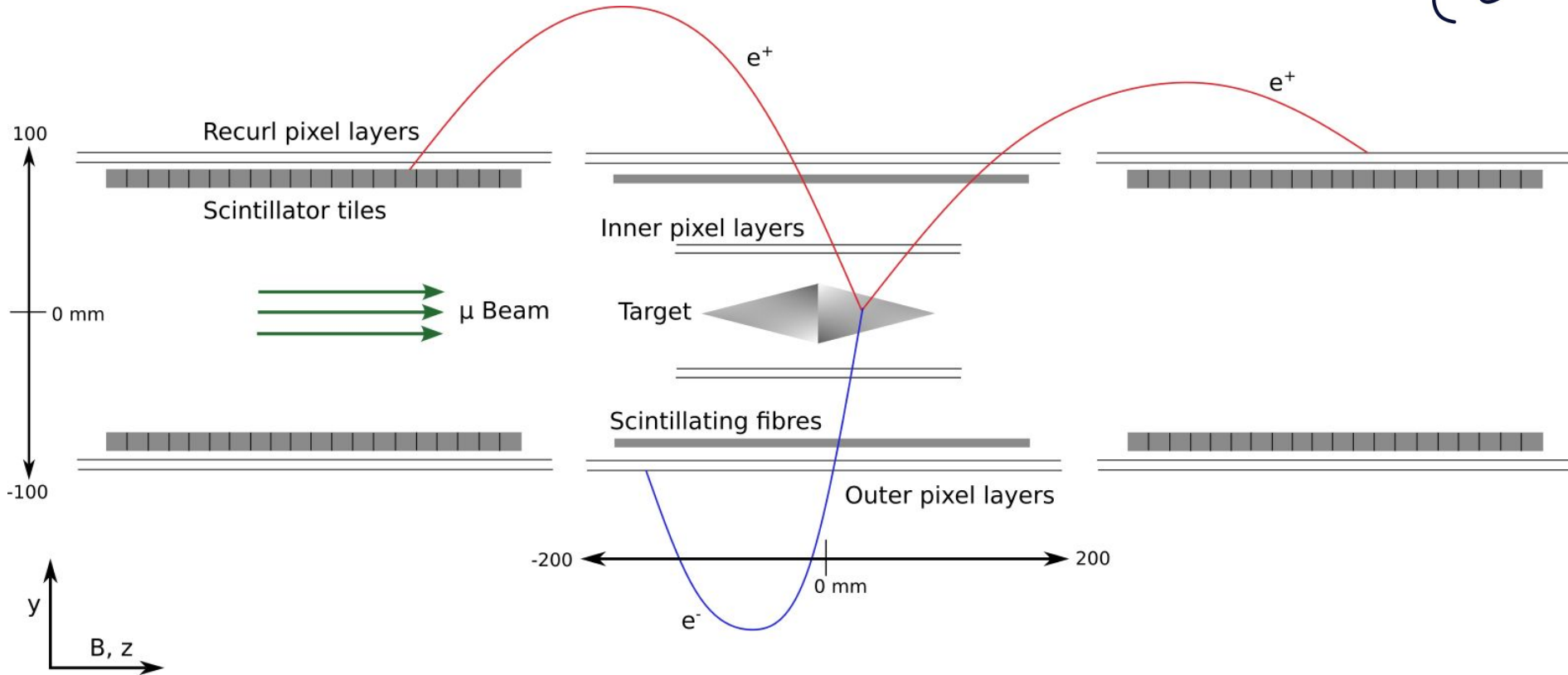
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# Mu3e Experiment



- We aim to observe or exclude the decay of a positive muon to two positrons and an electron.
- In standard model, possible via neutrino mixing but suppressed to unobservable level ( $\text{Br} < 10^{-54}$ ).
- Observation would be a violation of the lepton flavour conservation.
- SINDRUM limit the sensitivity to  $\text{Br} < 10^{-12}$  (1988) PSI.
- Phase I - muon rate of  $1 \times 10^8 \text{ s}^{-1}$  and  $\text{Br} < 2 \times 10^{-15}$ .

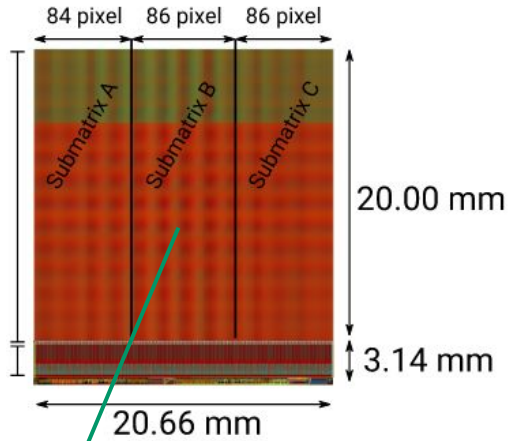
# Mu3e Detector



# Detector Subsystems



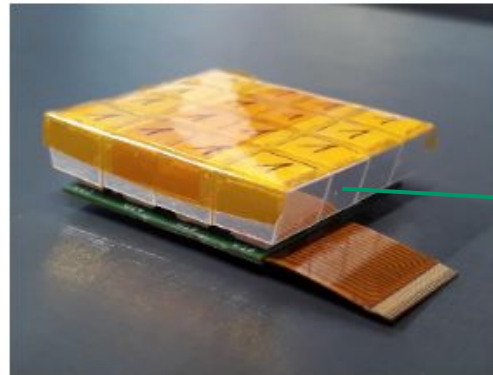
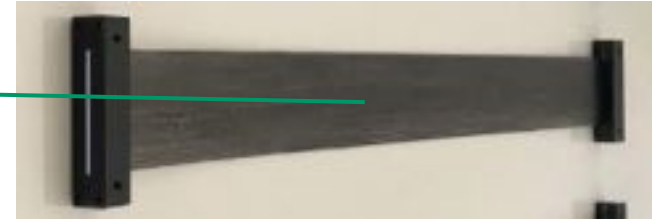
## Tracking detector



MUPIX: High Voltage Active Pixel Sensors, pixels and the detector electronics are integrated into the same chip

## Timing detector

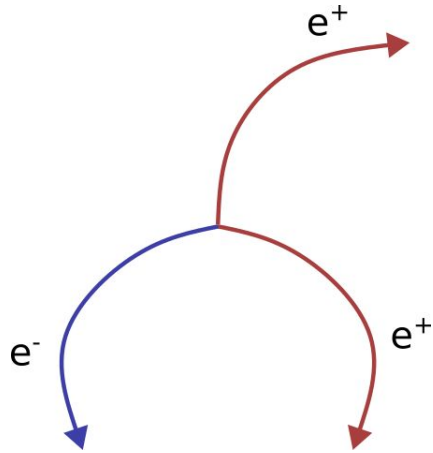
Scintillation fiber:  
timing resolution is  $\sim 1$  ns



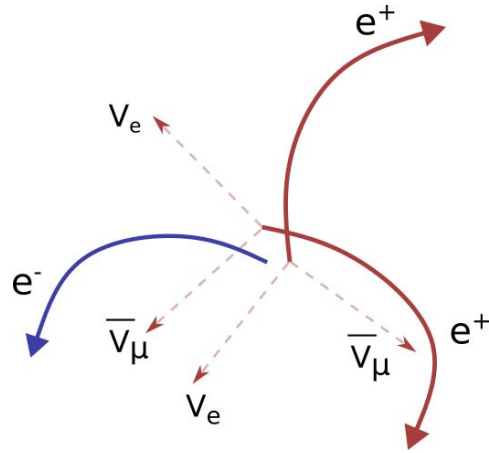
Scintillation Tiles: timing resolution about 70 ps



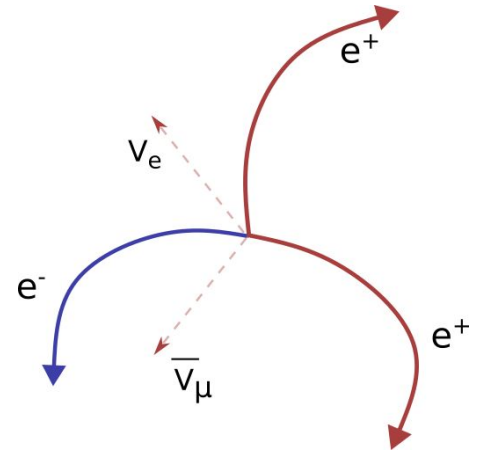
# Signal and Background processes



Signal

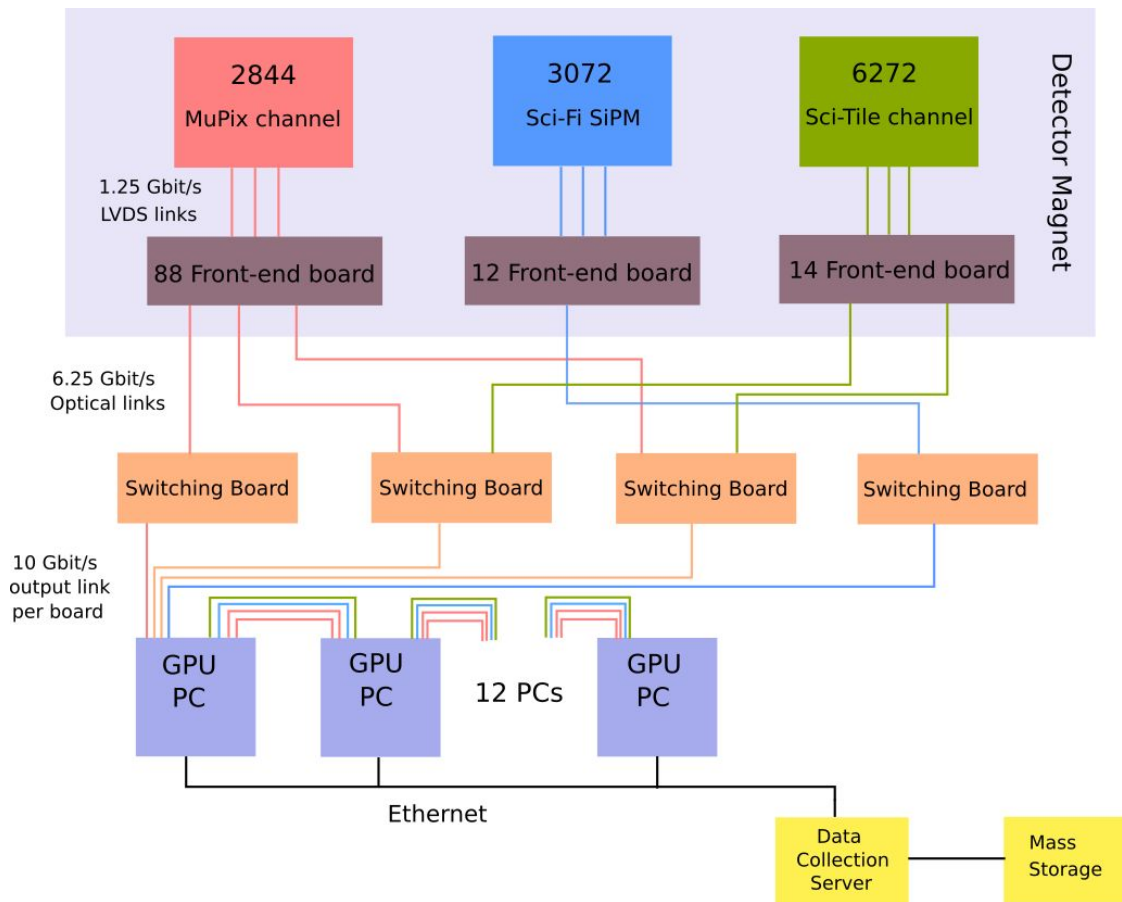


Combinatorial Background



Internal photon conversion  
(Br =  $3.4 \times 10^{-5}$ )

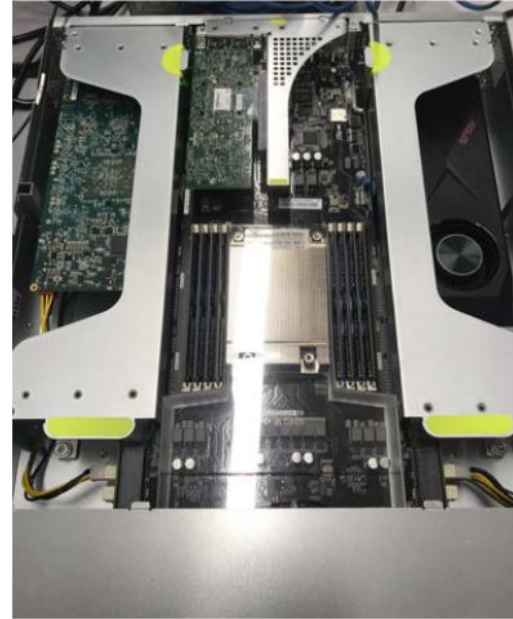
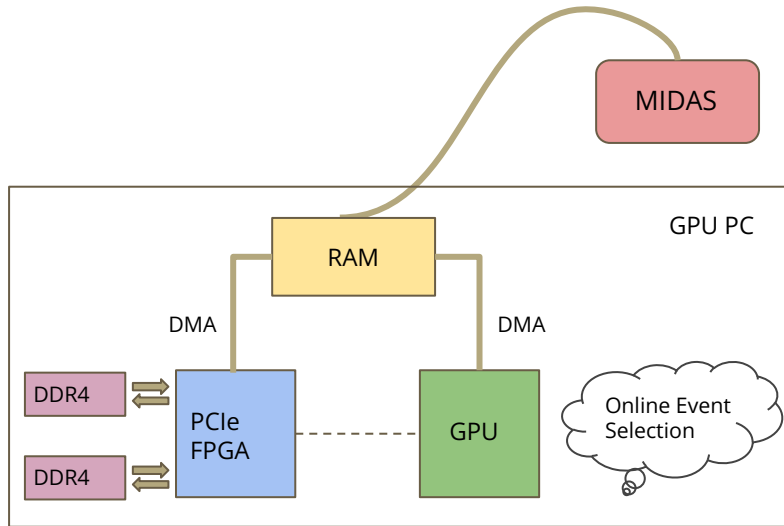
# Readout System



| Detector      | Rate (Gbit/s) |
|---------------|---------------|
| Pixel sensors | 56            |
| Fibers        | 28            |
| Tiles         | 17            |
| <b>Total</b>  | <b>101</b>    |

# Filter Farm

- Objective - select signal candidate events by reconstruction of tracks and vertices. To reduce data rate by a factor of 100.

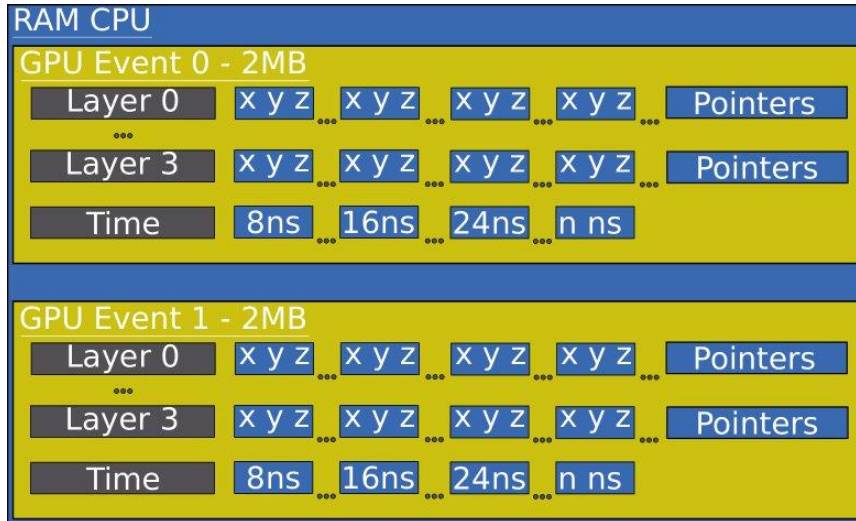


- NVIDIA GeForce RTX 3080 Ti.
- DE5a-NET FPGA card by Terasic.





# Memory Data Layout

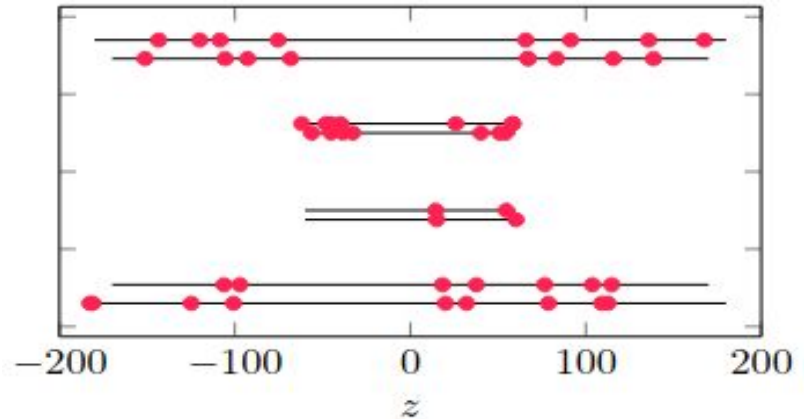
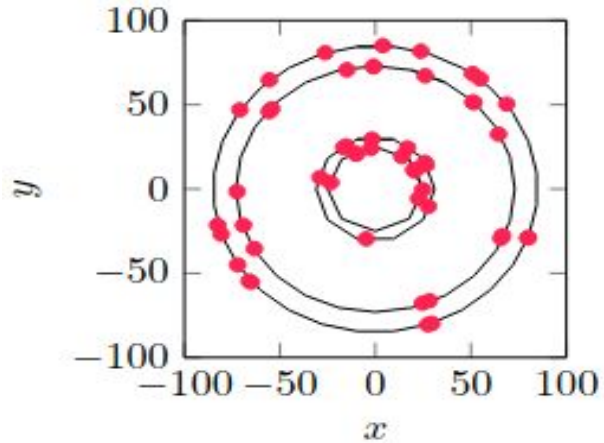






# Frames - Time Slices

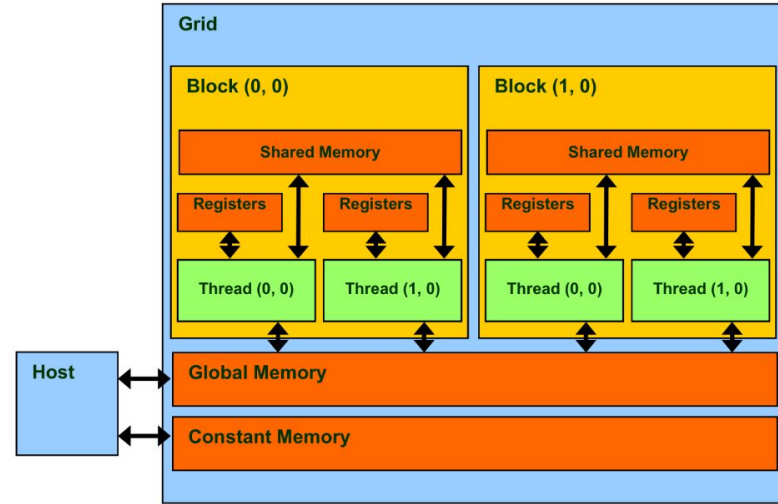
- Each frame is a snapshot of 64ns. Needs to be discussed and finalized.
- Threshold performance -  $1.5625 \times 10^7$  frames per second.



# Online Event Selection

- Selection Cuts: Geometric cuts.
- Track Reconstruction: Hit triplet-based reconstruction.
- Vertex Selection: Reconstruction of possible event vertices.

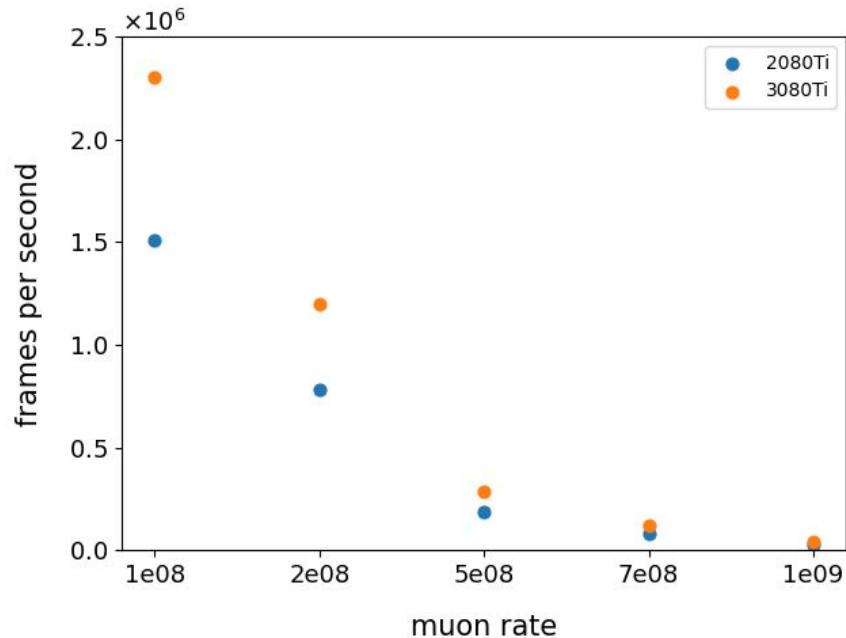
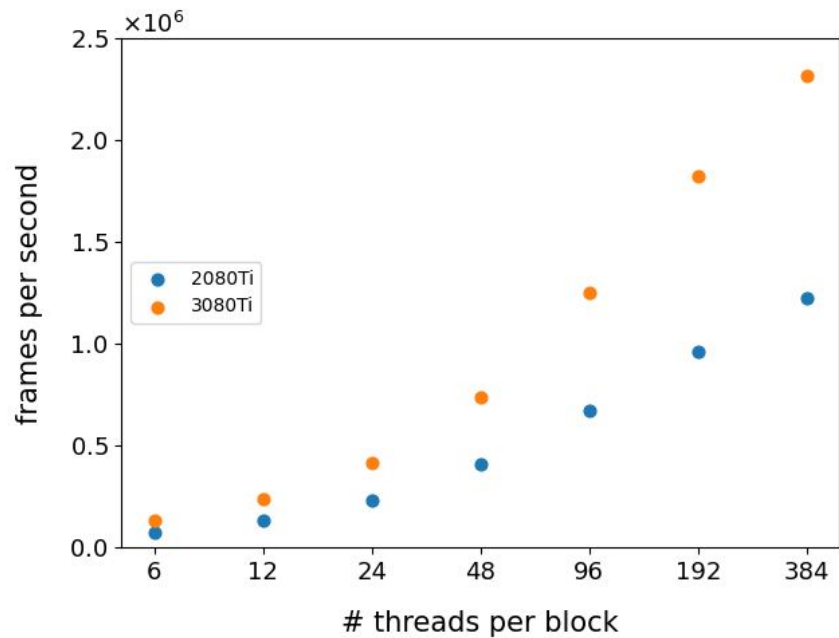
# Parallel computing on GPU



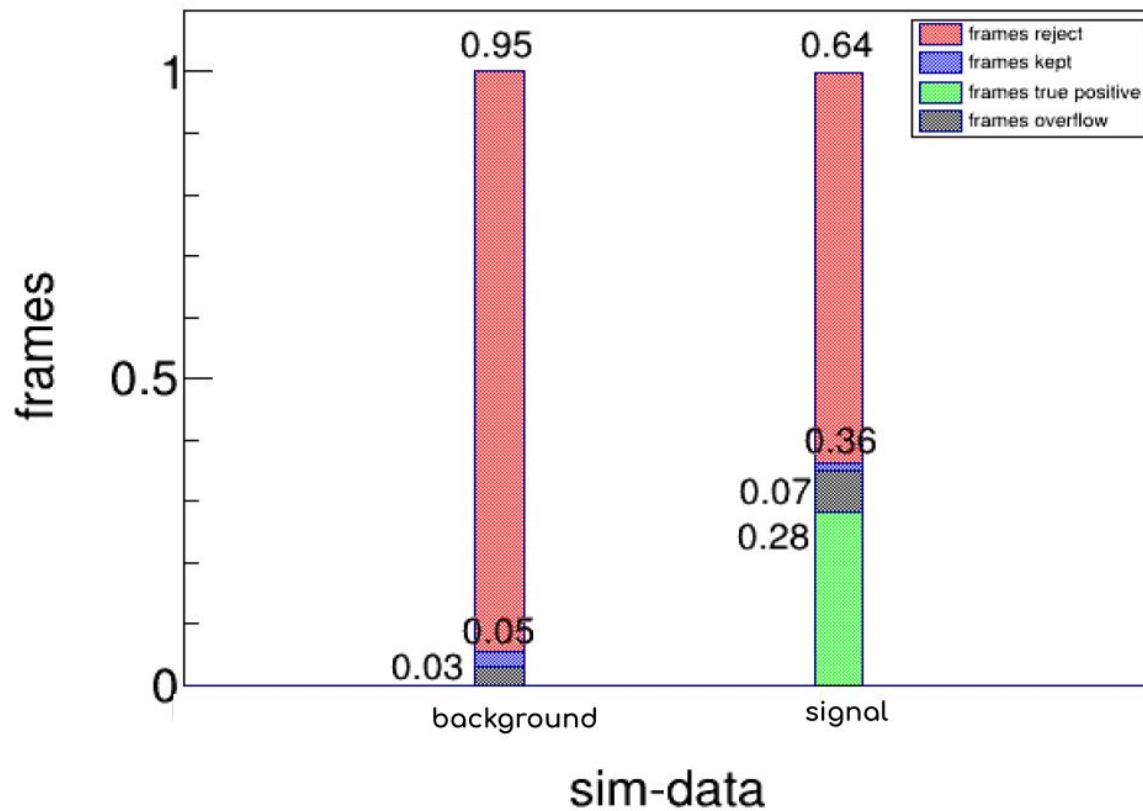
- Each SM consists of 64 CUDA cores in 2080Ti and 128 CUDA cores in 3080Ti.

- Warps of 32 threads execute at once in streaming multiprocessors (SM)

# Performance

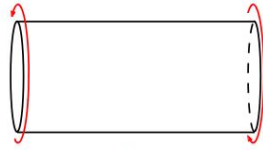


# Efficiency

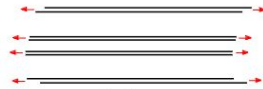


# Camera System for Calibration

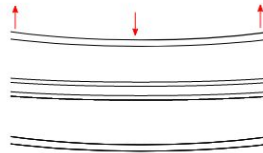
# Weak Modes



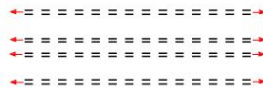
(A) Torsion



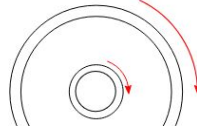
(C) Shearing



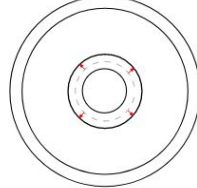
(E) Bowing



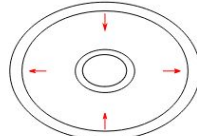
(G) Stretching



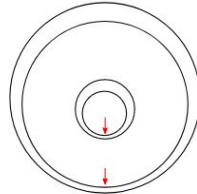
(B) Curling



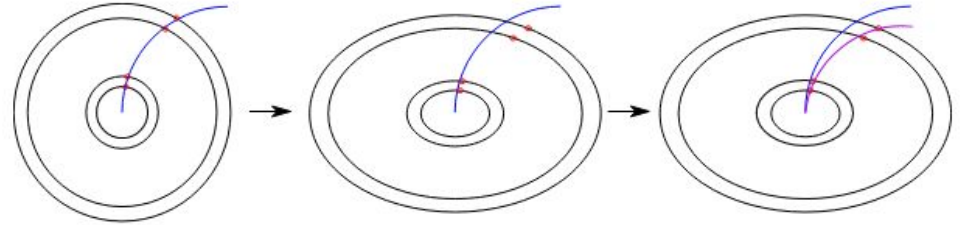
(D) Radial



(F) Elliptical

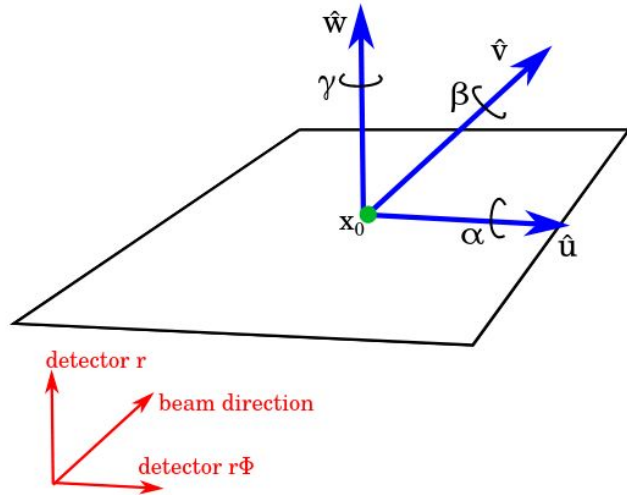


(H) Sagitta



- In blue, the true track is depicted.
- If the barrel is deformed elliptically, the blue track will have a worse  $\chi^2$  than without the deformation.
- Purple track can be reconstructed with the same  $\chi^2$  as the original blue one.

# Misalignment

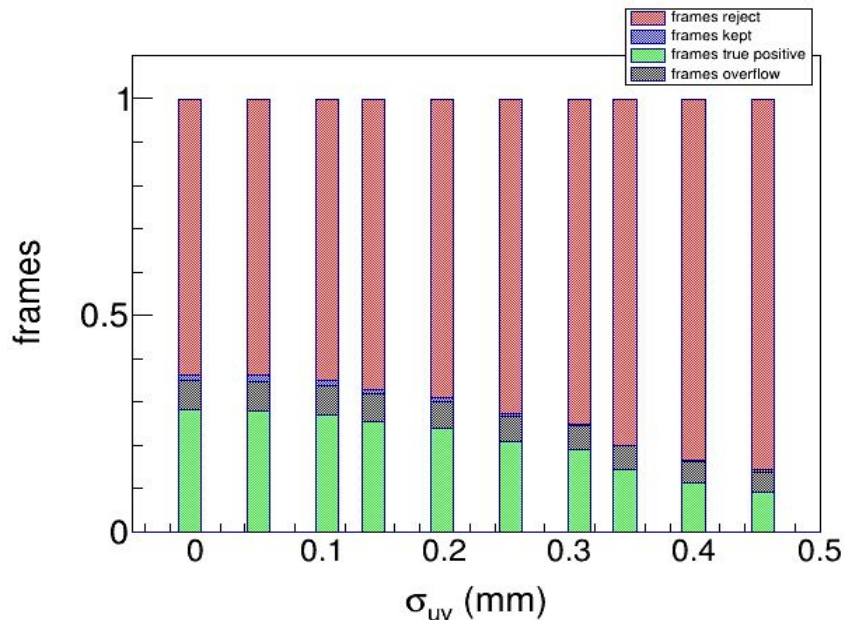
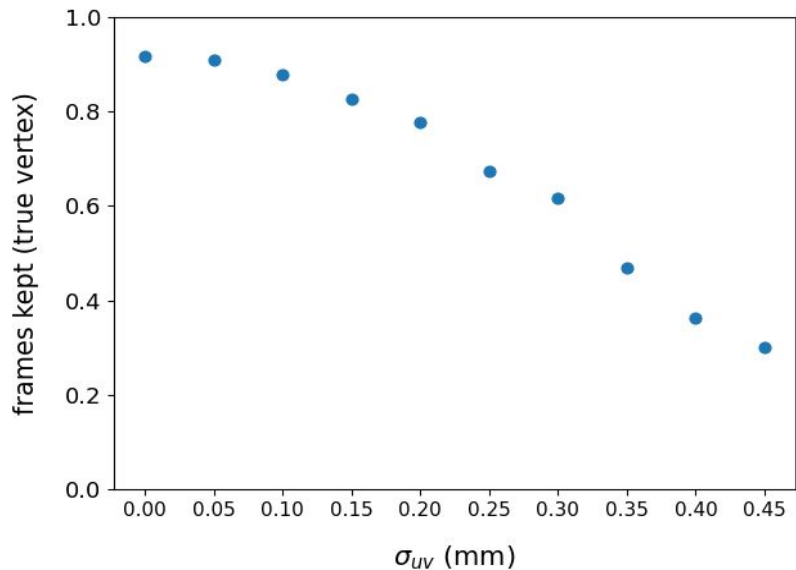


| $\sigma_{\text{off, u,v}}$ (mm) | $\sigma_{\text{rot, } \alpha, \beta}$ (mm) | $\sigma_{\text{off, w}}$ (mm) | $\sigma_{\text{rot, } \gamma}$ (mm) |
|---------------------------------|--|-------------------------------|-------------------------------------|
| 0.05 (0.45)                     | 5 (10)                                     | 0.005 (0.1)                   | 5 (10)                              |

- Deviations of more than 400  $\mu\text{m}$  corresponding to 5 times the pixel pitch (pixel-size) are expected.

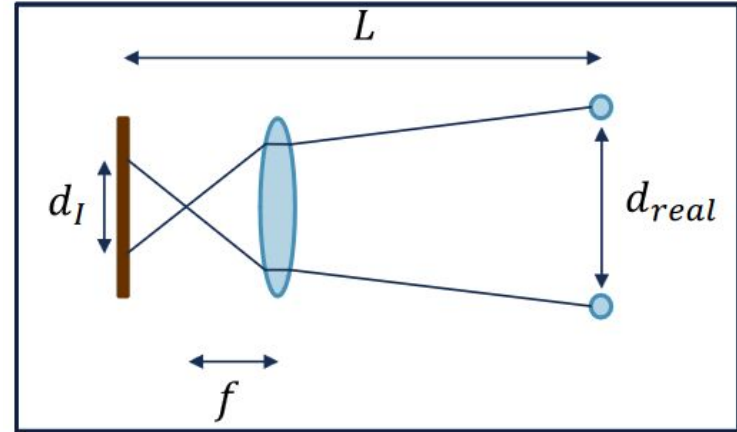
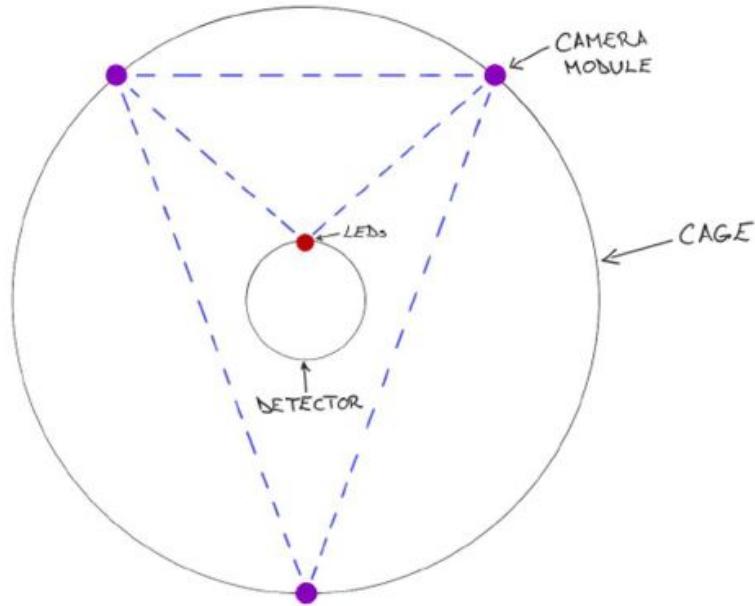


# Online Efficiency



- $\sigma_{\text{off,w}} = 0.1$  mm and  $\sigma_{\text{rot},\alpha,\beta,\gamma} = 10$  mRad were applied in all steps.
- Efficiency of Online Event Selection is compared with Monte Carlo truths.

# Camera System

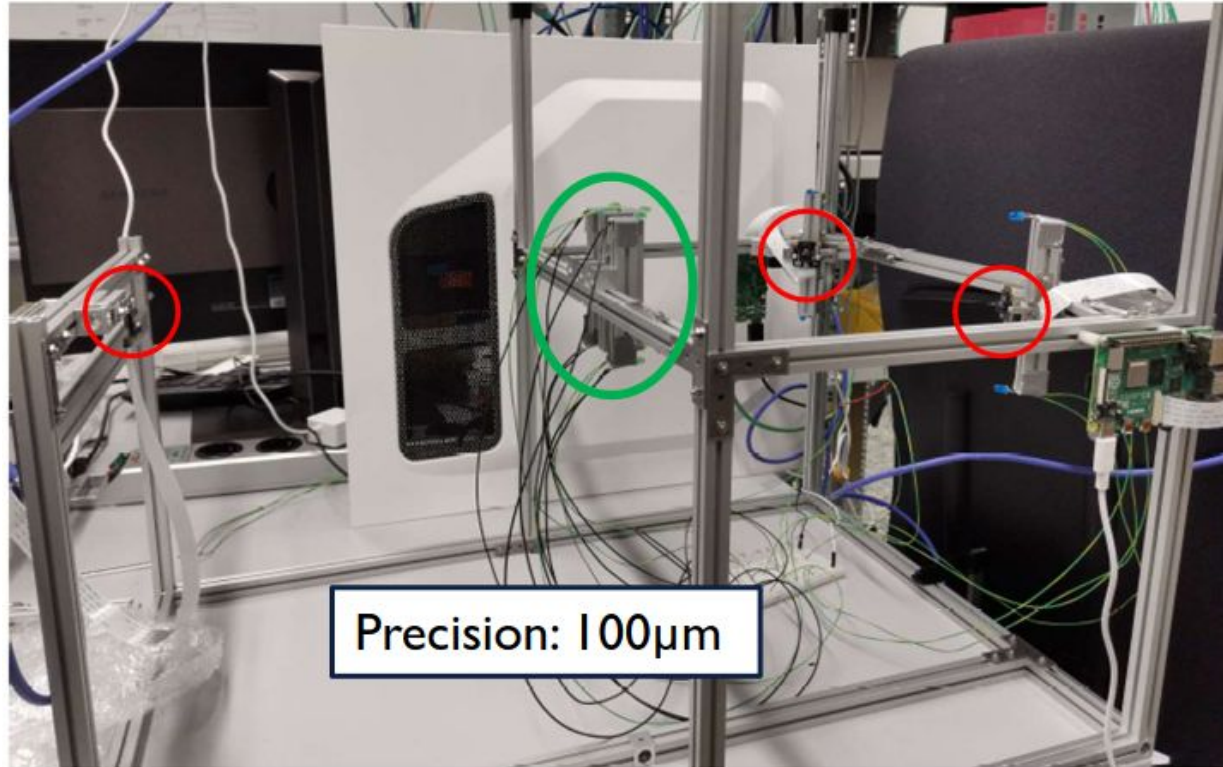


$$\frac{d_I}{d_{real}} = M = \frac{f}{f - L}$$

# Lab setup



Main Camera

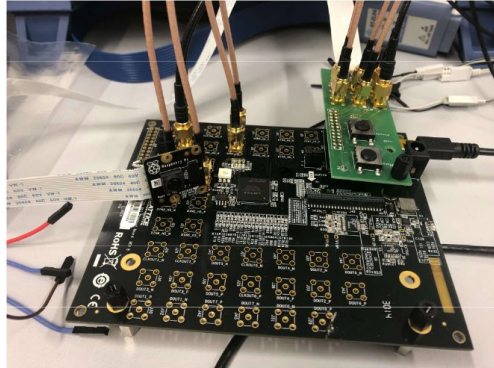
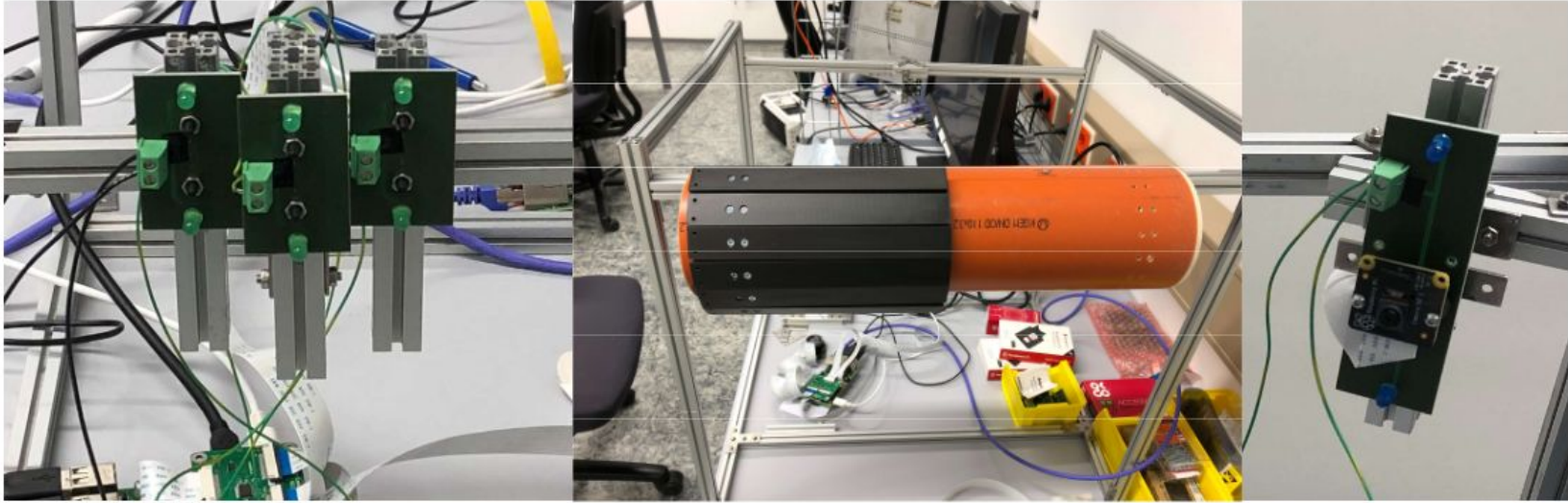


2 cameras with  
LED's

LED's on the  
detector

Precision: 100 $\mu$ m

# Updation

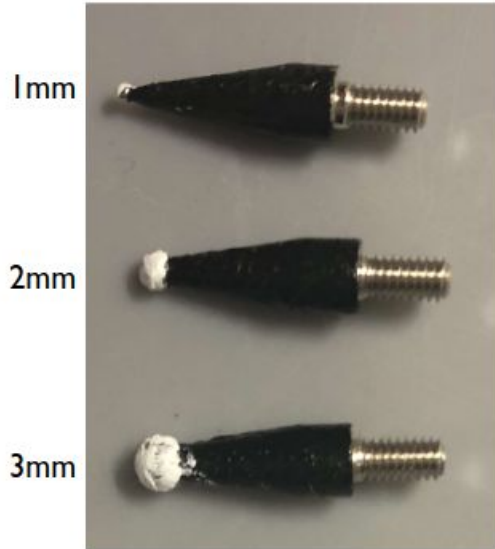


- MachXO3L DSI breakout board.
- Adapter card.

# Tooling balls



3 sizes tested



Double reflections due to 2 light sources

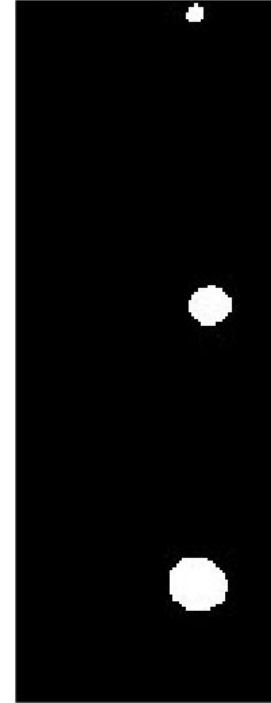
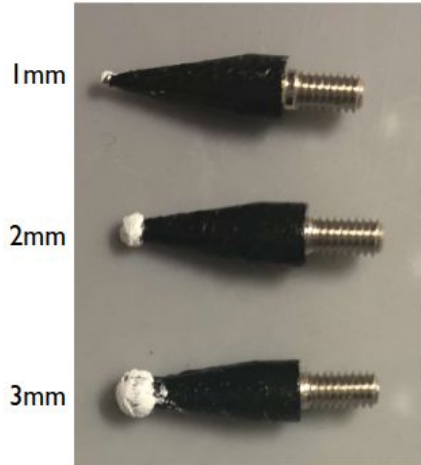


Diffuse reflection

# Tooling balls



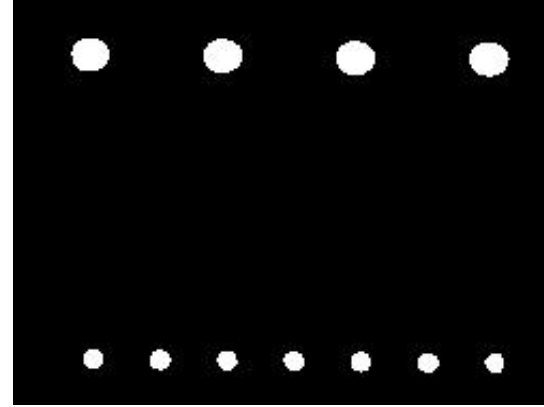
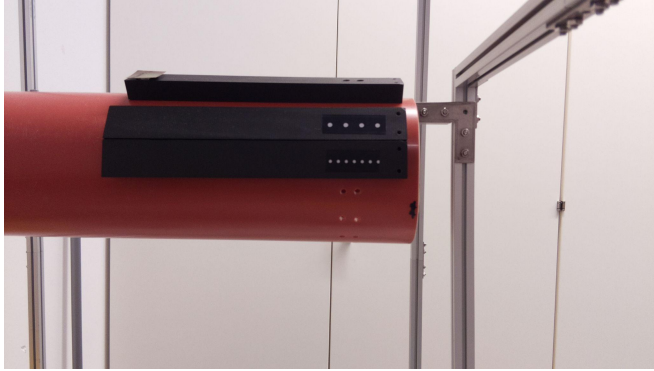
3 sizes tested



Estimated  
distance from  
camera:

**410.483 mm**

# Reflective Strips

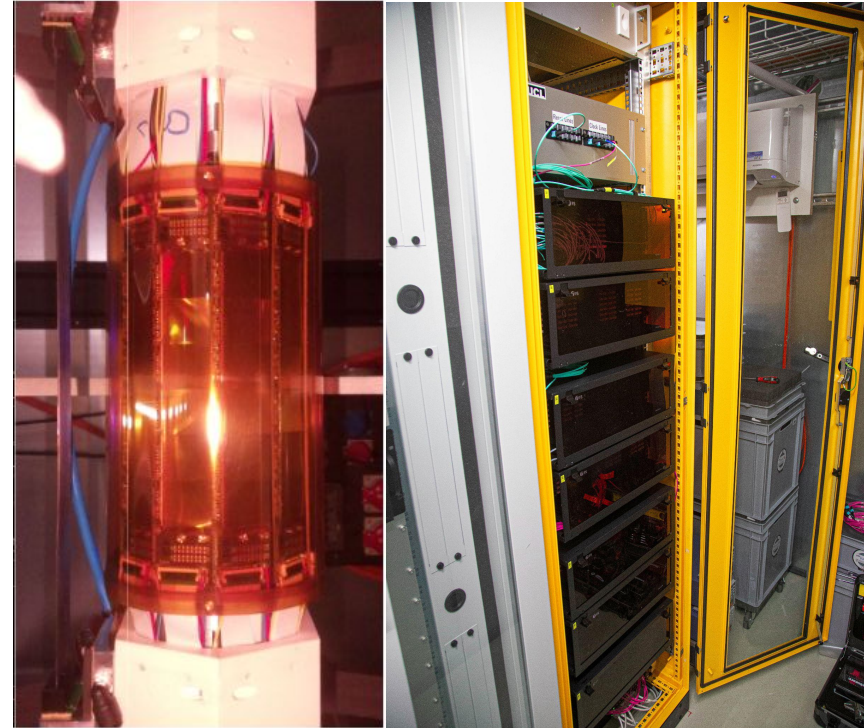


- Reflective tapes are visible and is a better option over tooling balls since they lay flat on the surface of the detector.
- Can see the contrast difference between tapes and tooling balls.

# Conclusion



- Implement new data memory layout for to load frames for the online reconstruction.
- Merge the online software to the MIDAS frontend.
- Use MIDAS frontend to view online histograms for QA.
- Develop Online Track Alignment for GPU selection.
- Use Camera Calibration inputs for the Online Track Alignment.
- Need to finalize the decision on reflective tapes.





# PhD Requirements:

- Completed the teaching assistantship of Advanced Practical course on Balmer series for the mandatory three semesters.

# Workshops and Conferences

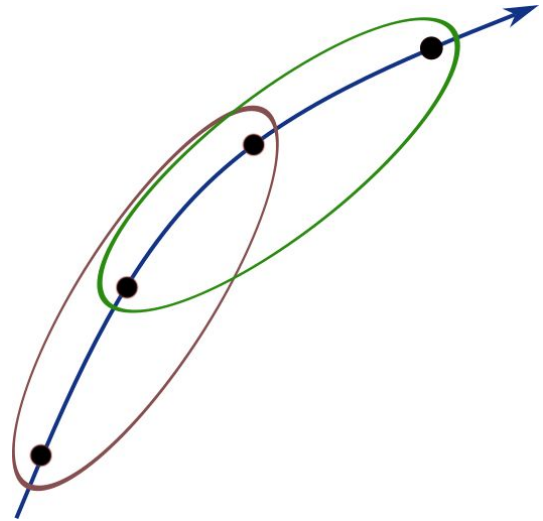
- “Mu3e Collaboration Meeting”, (Villigen, April 28-29, 2022) workshop held at Paul Scherrer Institute;
- “EPT Summer Camp for Physics TAs”, (Zuoz, August 12-14, 2022) engaging physics tutoring summer camp organised by ETH Zürich;
- “Paul Scherrer Institute Particle Physics Summer School – Vision and Precision”, (Zuoz, August 14-20, 2022) lectures and talks organised by Paul Scherrer Institute.
- “PRISMA+ Cluster of Excellence” (Geisenheim, September 19-21, 2022) gave a talk about my dissertation.
- “DPG Conference”, (Dresden, March 20-24, 2023) held and organized by Deutsche Physikalische Gesellschaft e.V.; gave a talk.
- “Mu3e Collaboration Meeting”, (Wengen, March 28-31, 2023) presented works.

# Backup

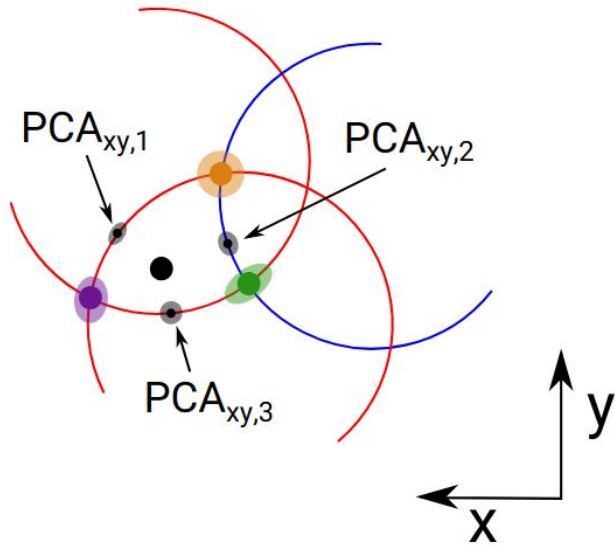
# Track Reconstruction



- 3D Multiple Scattering (MS) fit.
- Finds the curvature, minimising the MS angles for each triplet.
- Fits the triplets from first 3 layers after preselection.
- Helix trajectory is propagated to the 4th layer and the closest hit is found.
- The global curvature from both helix is used find the track parameters.

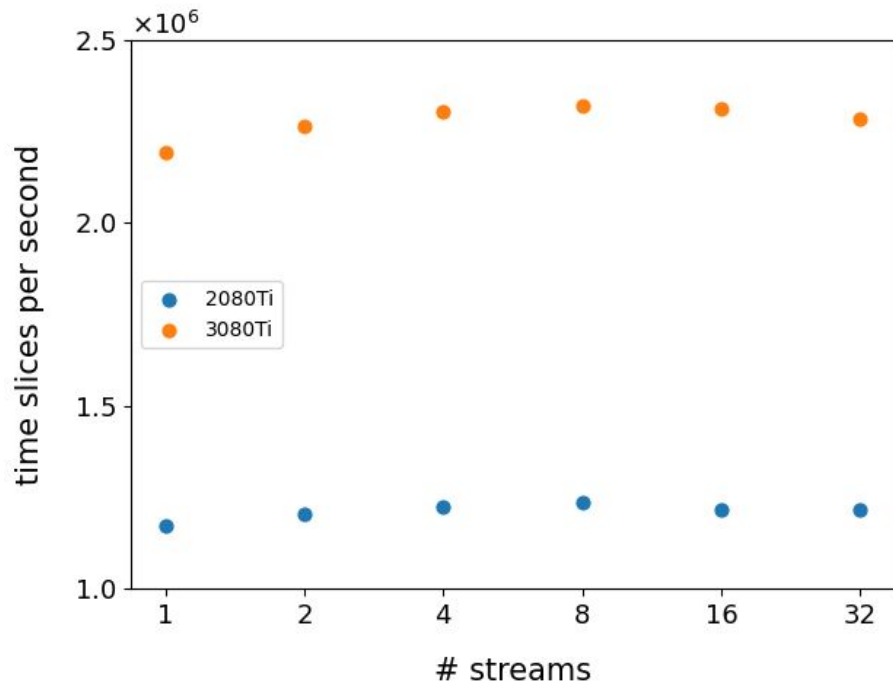
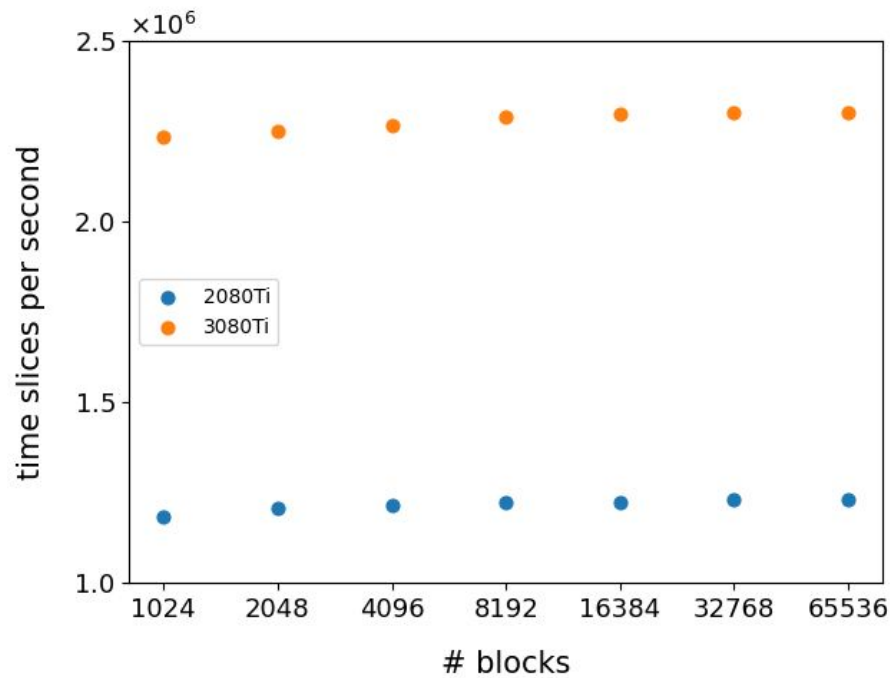


# Vertex Selection



- With curvature the  $e^-$  and  $e^+$  can be identified.
- Only when all three tracks intersect in the transverse plane then the weights are calculated.
- The weights are from the MS in the first detector plane and due to the pixel size.
- The total energy of all particles, must match the muons rest mass and total momentum is zero.
- Time slices with signal vertices are kept.

# Performance



# Selection Cuts



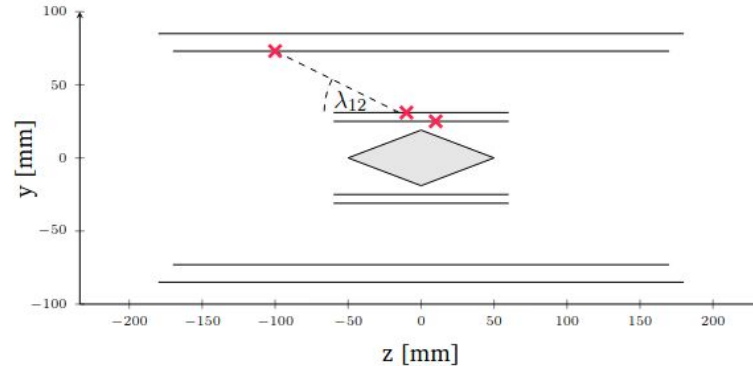
- Slope difference  $\Delta\lambda$  between the slopes of consecutive layer hits in the longitudinal plane.

$$\tan \lambda_{ij} = \frac{z_j - z_i}{h_{t,j} - h_{t,i}}$$

$$\Delta\lambda = \tan \lambda_{12} - \tan \lambda_{01}$$

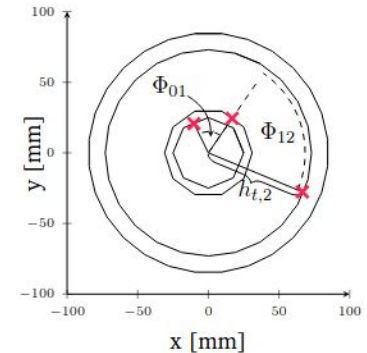
- In transverse plane we observe the angle  $\Phi_{ij}$  between hits of two consecutive layers in relation to the origin:

$$\cos \Phi_{ij} = \frac{\mathbf{h}_{t,i} \cdot \mathbf{h}_{t,j}}{h_{t,i} h_{t,j}}$$



- $z_0 - z_1 < 30$  mm
- The transverse radius of the circle going through all three hits

$$r_{t,c} = \frac{d_{01} d_{12} d_{20}}{2[(\mathbf{h}_0 - \mathbf{h}_1) \times (\mathbf{h}_2 - \mathbf{h}_1)]_z}$$

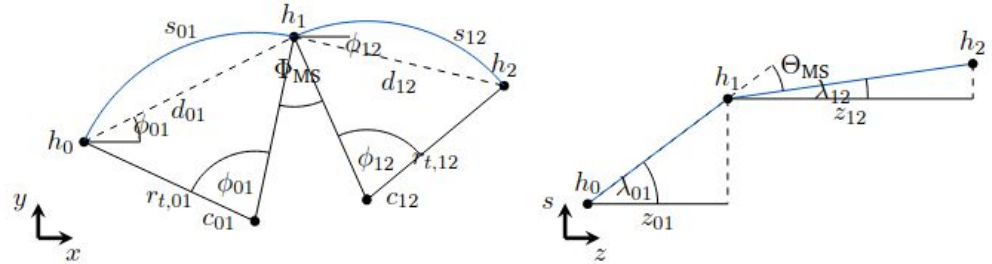


# Track Reconstruction



- For reconstruction Triplet fit is used.
- We search for the track minimizing the objective function. Assuming no momentum loss and thus a constant curvature  $k$ .

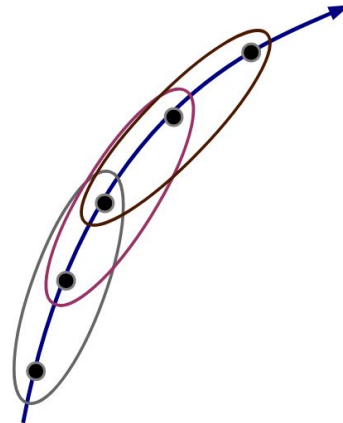
$$\chi^2(\kappa) = \frac{\Phi_{MS}(\kappa)^2}{\sigma_{\Phi}^2} + \frac{\Theta_{MS}(\kappa)^2}{\sigma_{\Theta}^2}.$$



- More than three hits for a full track fit requires to accommodate for multiple triplets.

$$\chi_{\text{global}}^2(\kappa) = \sum_t^{n_{\text{triplets}}} \chi_t^2(\kappa).$$

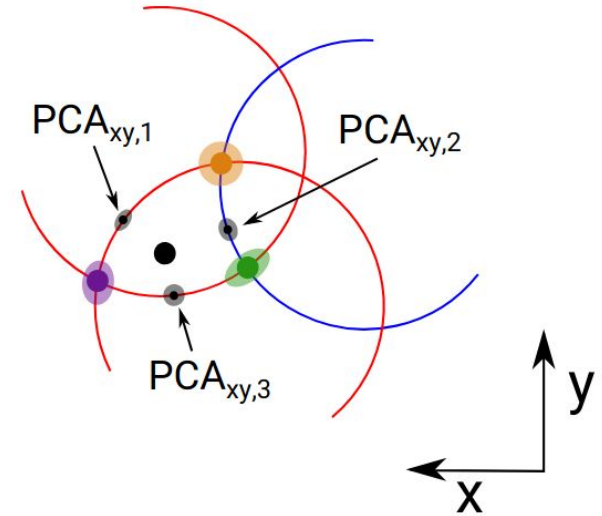
- A global curvature is found for all triplet combinations minimising the MS angles for each triplet.



# Vertex Fit



- All combinations of two positrons and one electron are considered within each time slice. We calculate the total energy of all particles in the triplet using their curvature  $\kappa$ .
- The total energy of all particles, must match the muons rest energy.
- The weighted mean is calculated only if all three reconstructed tracks intersect and it is calculated for all combinations of three intersections from three tracks.
- The  $\chi^2$  for a vertex estimate is computed from the differences between the point of closest approach and the weighted mean both in the transverse plane and in the z-coordinate.



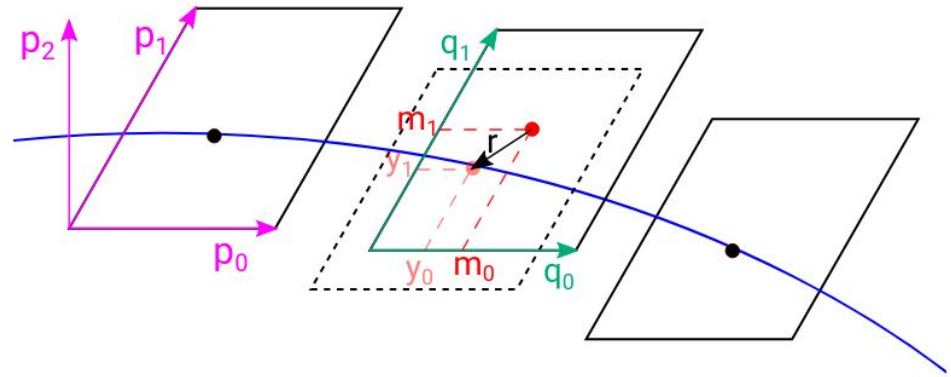


# Track-based Alignment



$$r_{ij} = m_{ij} - f(\mathbf{q}_j, \mathbf{p})$$

$$\chi^2(\mathbf{q}_j, \mathbf{p}) = \sum_j^{\text{tracks}} \sum_i^{\text{hits}} \left( \frac{r_{ij}}{\sigma_{ij}} \right)^2$$



- We get residuals after fitting individual particle tracks with an adequate track model.
- From these residuals, one can derive geometry corrections.
- These track fits however assume a fixed set of global parameters. As a result, the obtained residuals will be biased in case of shifts in global parameters.