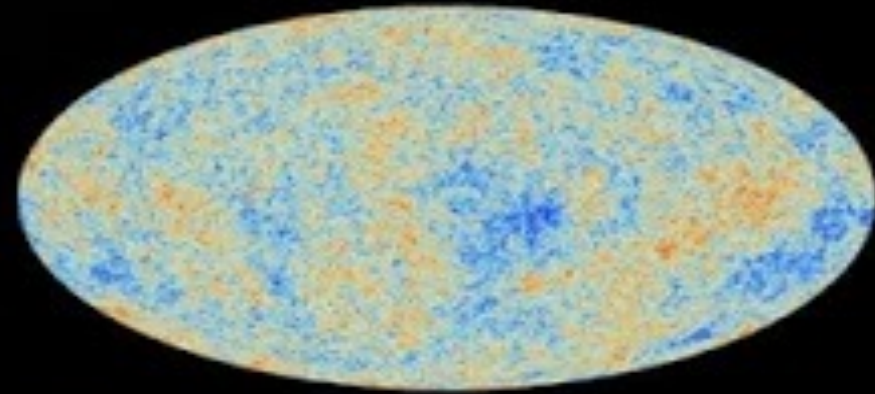


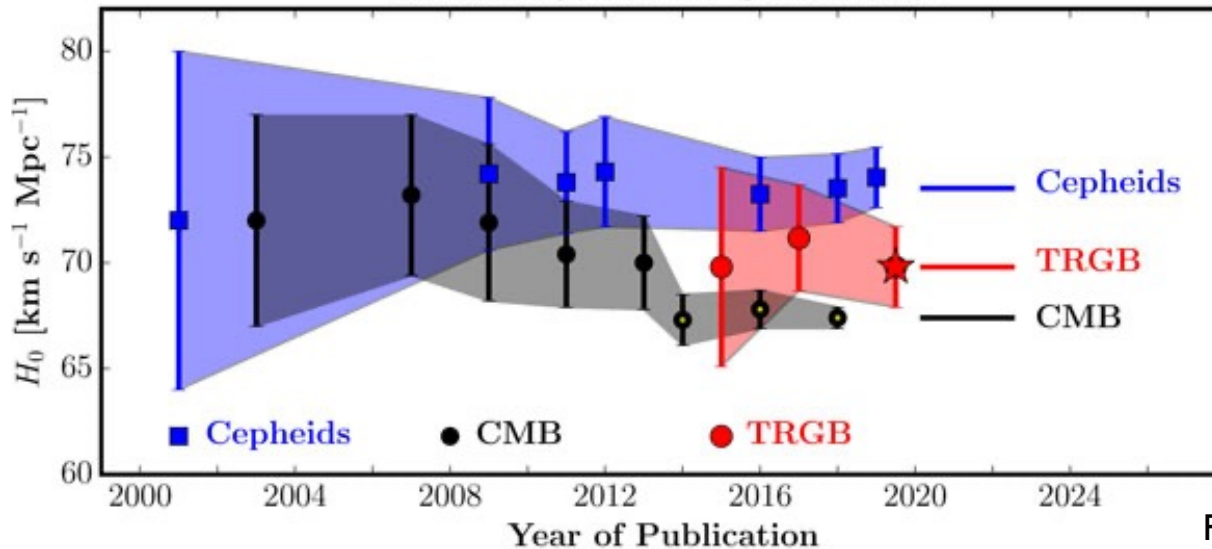
# The Hubble constant tension: The Cepheids' point of view

**Giulia De Somma**  
INAF-ASTROFIT fellow

In collaboration with Marcella Marconi



# The Hubble Constant Tension



$$H_0 = 73.04 \pm 1.4 \text{ km s}^{-1} \text{ Mpc}^{-1} \text{ (Riess et al. 2022)}$$

vs

$$H_0 = 67.7 \pm 0.4 \text{ km s}^{-1} \text{ Mpc}^{-1} \text{ (Planck collaboration, 2020)}$$

**5 $\sigma$  tension** between the early and late Universe  $H_0$  measurements

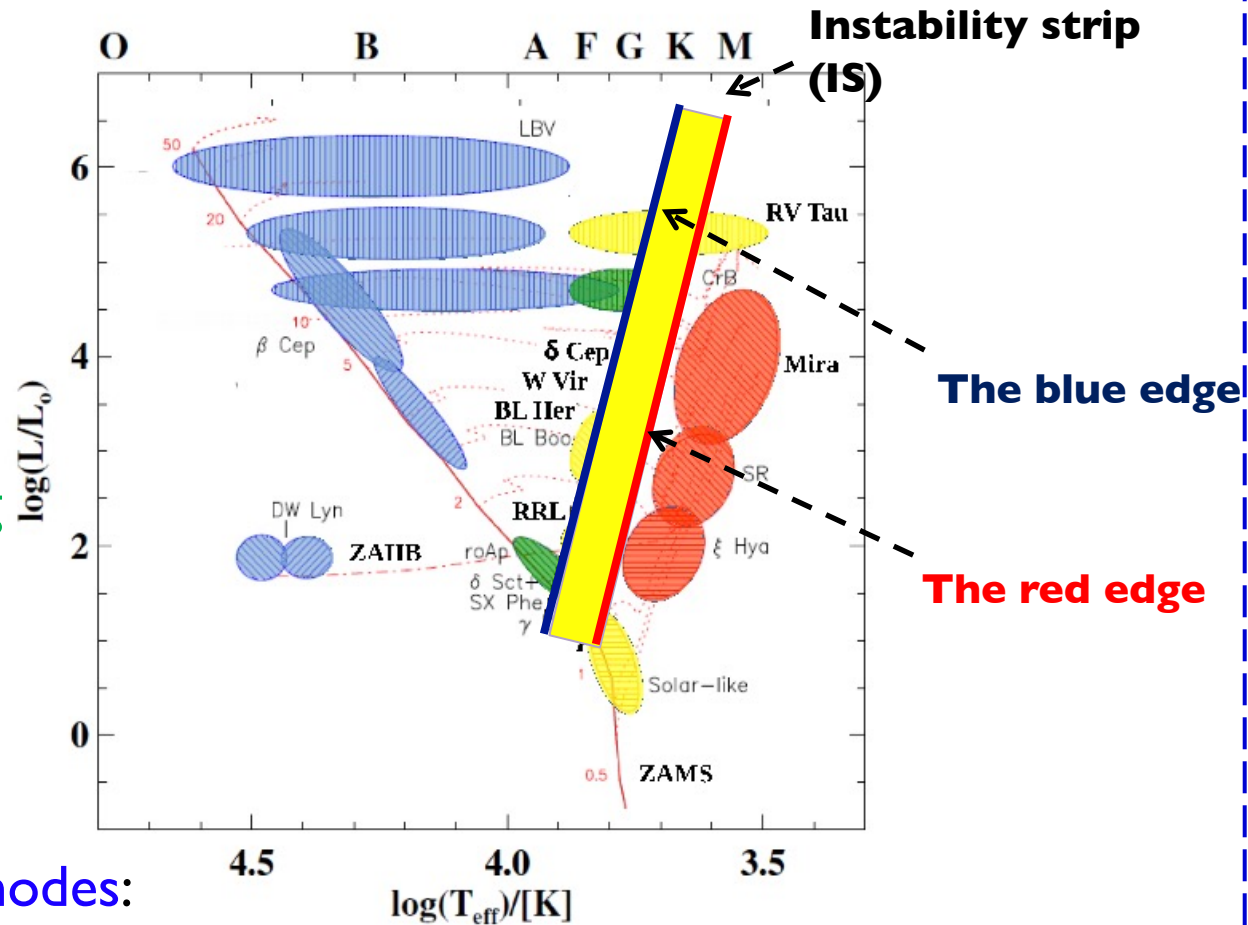
Systematic uncertainties  
in the calibration of the extragalactic distance scale based on CCs  
or  
new physics?

# Classical Cepheids (I)

Classical Cepheids (CCs) are young and intermediate-mass stars

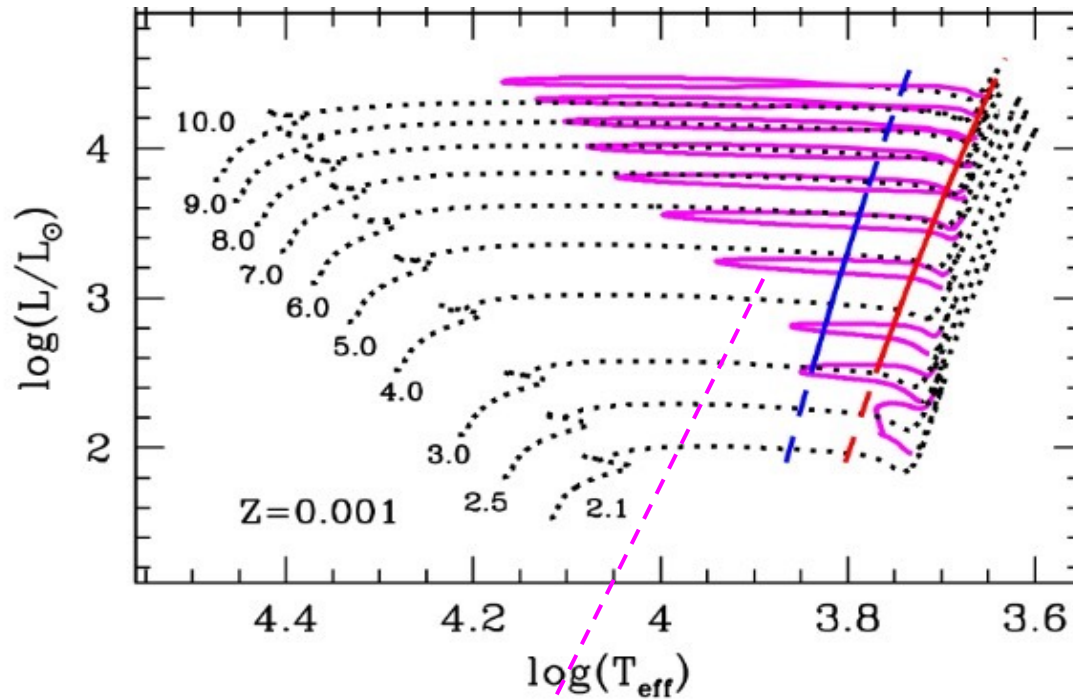
- $1d \leq P \leq 100d$
- $-2\text{mag} \leq M_V \leq -7\text{mag}$
- $3.0 \leq M/M_\odot \leq 13.0$
- $t < \text{hundreds of Myr}$

Pulsation in **three radial modes**:  
Fundamental (**F**),  
First Overtone (**FO**)  
and Second Overtone (**SO**)



# Classical Cepheids (II)

CCs cross the IS three times called FIRST, SECOND, and THIRD CROSSING



Associated with the so-called **'blue loop'** evolutionary phase of massive and intermediate-mass stars during the central Helium burning phase.

# The Pulsation Relations

Pulsating stars  $\rightarrow P\sqrt{\rho} = \text{constant}$  + Stefan-Boltzmann law  $\rightarrow$

$P$  is a function of  $M$ ,  $L$ , and  $T_{\text{eff}}$  (and chemical composition)

$$\log P = a + b \log T_{\text{eff}} + c \log(M/M_{\odot}) + d \log(L/L_{\odot})$$

## Classical Cepheid Relations

For the blue loop phase, a **Mass-Luminosity relation** is predicted by stellar evolution

$$\log L = a + b \log M + c \log Z + d \log Y$$

By inserting the ML relation in the previous  $PMLT_{\text{eff}} \rightarrow$  PLC relation

CCs obey a **Period-Luminosity-Color (PLC) relations**  $\rightarrow$  distances

By averaging over the color extension of the instability strip  $\rightarrow$  **PL relation**

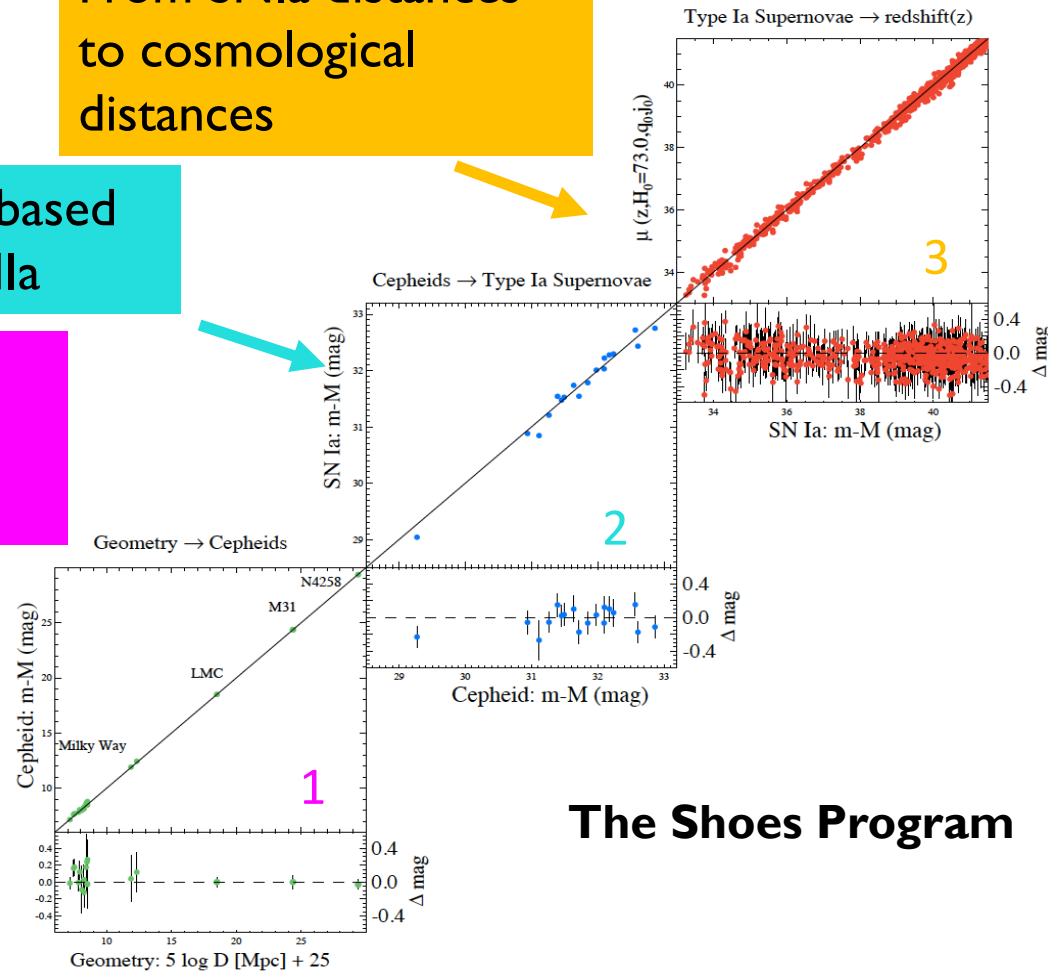
**PL and PLC relations make CCs the most used primary distance indicators in the extragalactic distance scale calibration**

# The Local Universe Measurement of $H_0$

From SNIa distances  
to cosmological  
distances

From Cepheid-based  
distances to SNIa

From geometric  
distance  
to Cepheids

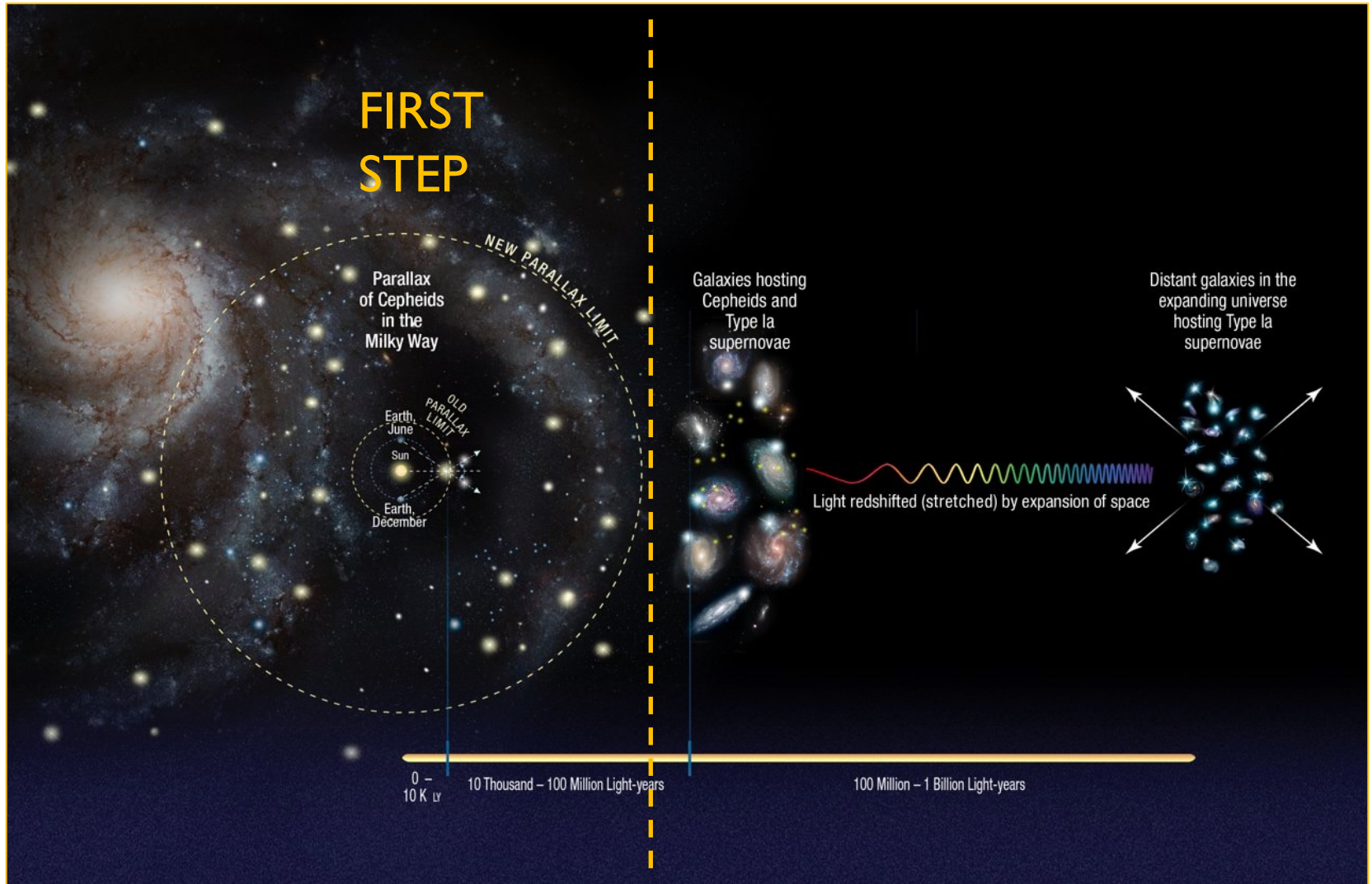


**The Shoes Program**

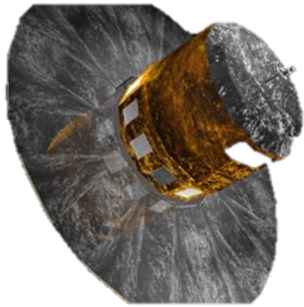
$$H_0 = 73.04 \pm 1.4 \text{ km s}^{-1} \text{ Mpc}^{-1} \text{ (Riess et al. 2022)}$$

To resolve the tension, **studying and removing the systematics** affecting each step is fundamental

# First Step: The Geometric Calibration of the Cepheid Distance Scale:



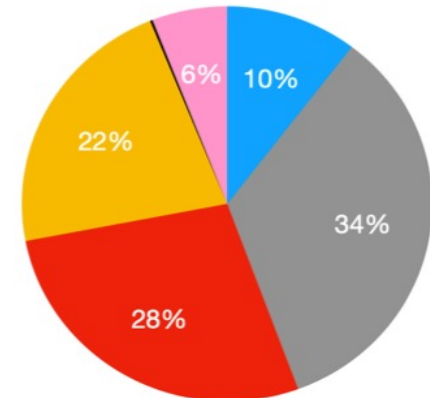
# The impact of the ESA Gaia Mission on the first step:



## Gaia summary

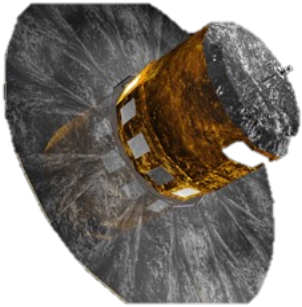
- Launch December 2013
- Operational at L2 since July 2014
- Astrometry and spectrophotometry ( $G$ ,  $G_{BP}$ ,  $G_{RP}$ ) for  $> 1$  billion objects
- Radial velocities (BP, RP, RVS) for  $> 100$  million objects
- Gaia's end-of-life is estimated at early 2025

**10.5 million variable sources with light curves**  
**24 variable types**

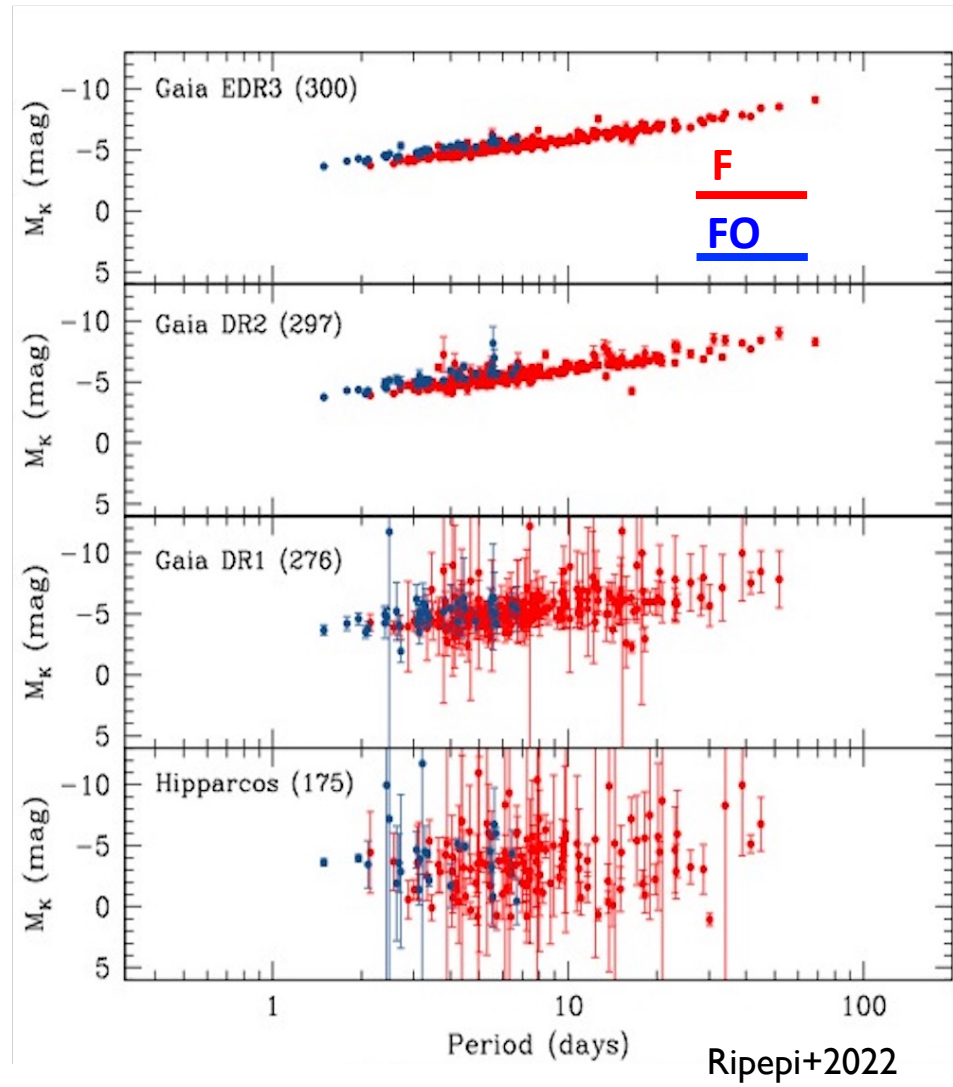
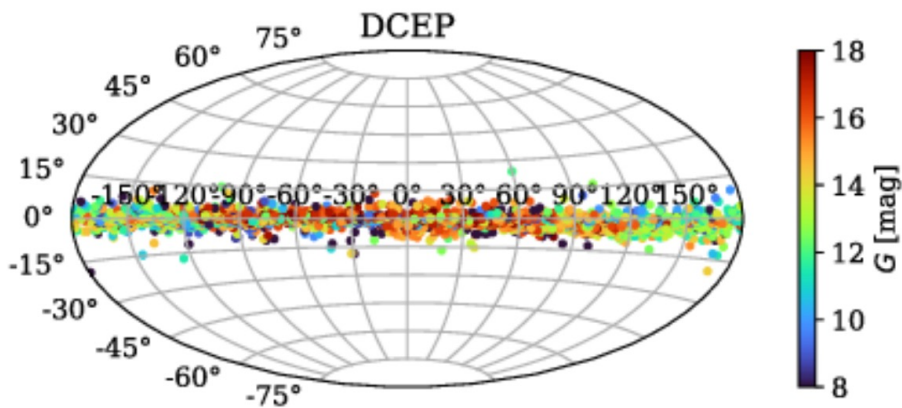




# The ESA Gaia Mission Contribution



3,434 MW CCs in Gaia DR3 → largest homogeneous dataset published so far.



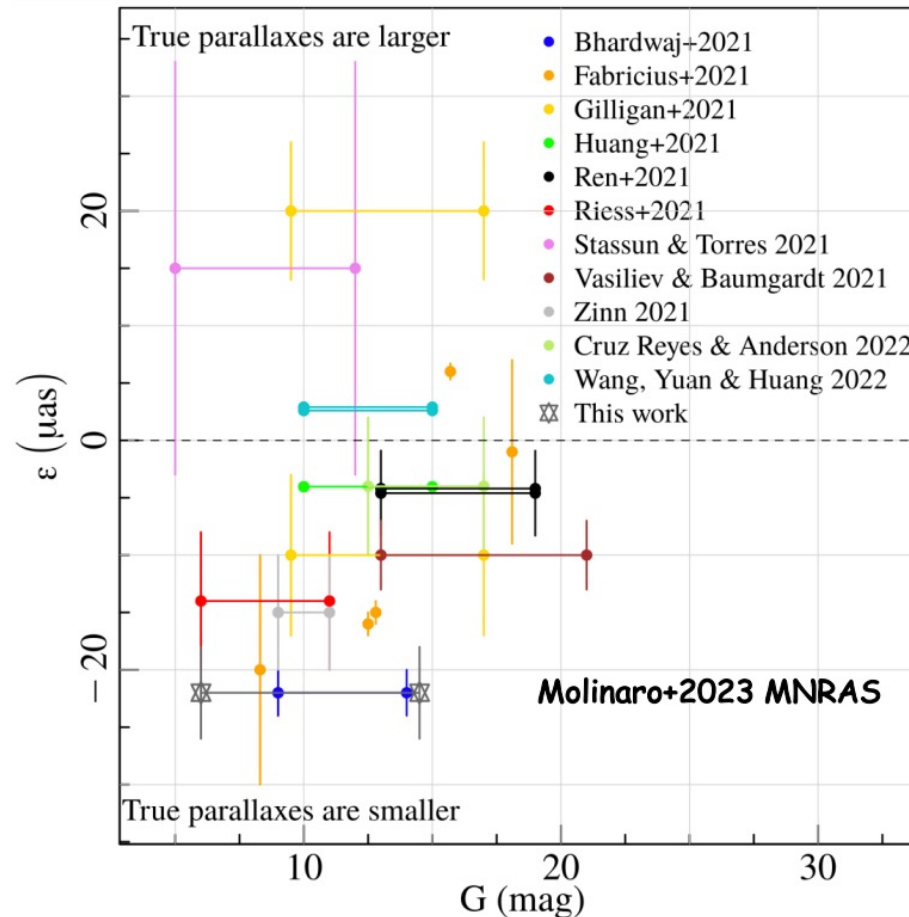
Ripepi+2022

The dispersion of the PL strongly reduces from Hipparcos to Gaia DR1 to Gaia EDR3

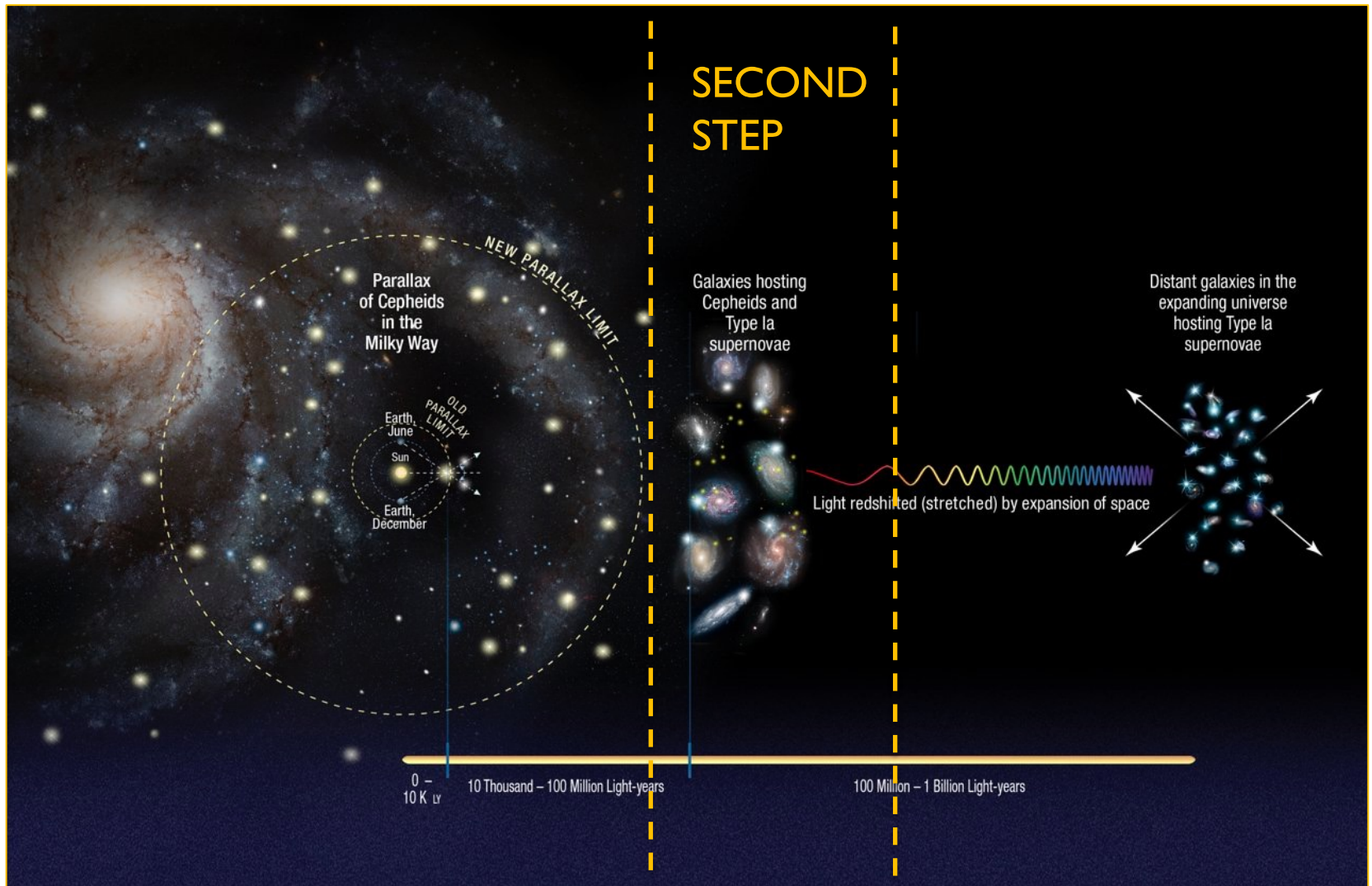
# The Gaia Parallax Zero Point Offset

The Gaia parallaxes show an offset of their zero point that depends on source color, magnitude, and position.

This effect will hopefully be reduced in future Gaia data releases.



# Second Step: The Calibration of SNIA in Galaxies Containing both CCs and SNIA



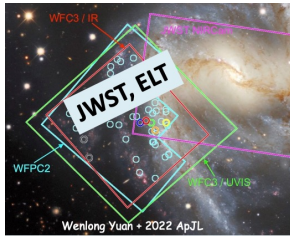
# The Systematic Uncertainties Affecting the PL, PLC and PW Relations

- PL intrinsic dispersion
- PL metallicity dependence
  - PL nonlinearity

To reduce



Work into near or mid-infrared filters



Use the PW relation

$$W(\lambda_2, \lambda_1) = m_{\lambda_1} - \left[ \frac{A(\lambda_1)}{E(m_{\lambda_2} - m_{\lambda_1})} \right] \times (m_{\lambda_2} - m_{\lambda_1})$$

In the B-V color  $\rightarrow W(B - V) = V - \gamma(B - V) \quad \gamma = \frac{A_V}{E(B - V)}$

- Dependence of PW on the assumed extinction law (e.g. in PW relations) on the environment

There are systematic uncertainties affecting the Cepheid distance scale related to the hydrodynamical modelling of pulsating stars

# Theoretical Approaches to Create a Pulsation Model

## □ 1D pulsation models

### ○ Linear:

- adiabatic → oscillation period
- nonadiabatic → oscillation period and the blue edge (Anderson et al. 2016, Kovacs&Karamiqucham 2021)

### ○ Nonlinear:

- radiative → oscillation period, amplitude, blue edge
- convective → period, amplitude, blue edge, red edge, light curves.  
radius curves, velocity curves  
(e.g. Gehmeyr et al.1990, Bono, Stellingwerf et al. 1994, Yeco 1998, Bono, Marconi, Stellingwerf 1999, Szabo et al. 2000, 2004)

## □ Multidimensional pulsation models

(e.g. *Mundprecht et al. 2013, 2015*)

# New Dataset of Nonlinear Convective Cepheid Pulsation Models

**By using a nonlinear and convective hydrodynamical code (Stellingwerf, 1994), I built the most detailed dataset of CC pulsation models**

- Wide range of masses and effective temperatures
- 4 chemical compositions
- 3 assumptions about the Mass-Luminosity relation
- 3 values for the efficiency of super adiabatic convection

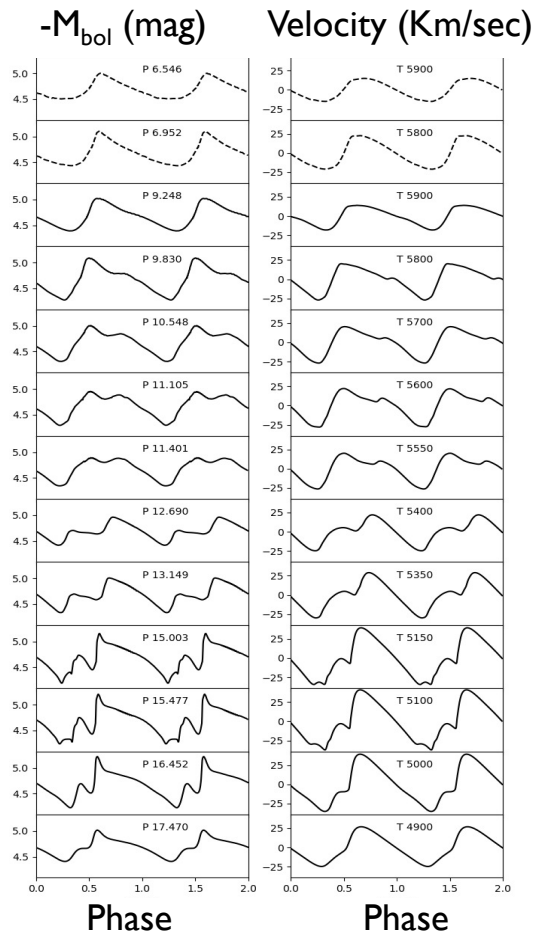
Low metallicity	{	<b>Z=0.004</b> <b>Y=0.25</b> → <b>696 stable F-mode</b> <b>110 stable FO-mode</b> <b>3 stable SO-mode</b>
		<b>Z=0.008</b> <b>Y=0.25</b> → <b>639 stable F-mode</b> <b>126 stable FO-mode</b> <b>3 stable SO-mode</b>
Solar metallicity	{	<b>Z=0.02</b> <b>Y=0.28</b> → <b>360 stable F-mode</b> <b>44 stable FO-mode</b>
Oversolar metallicity	{	<b>Z=0.03</b> <b>Y=0.28</b> → <b>127 stable F-mode</b> <b>4 stable FO-mode</b>

# The Atlas of Bolometric Light and Radial Velocity Curves

## Canonical ML $\alpha=1.5$

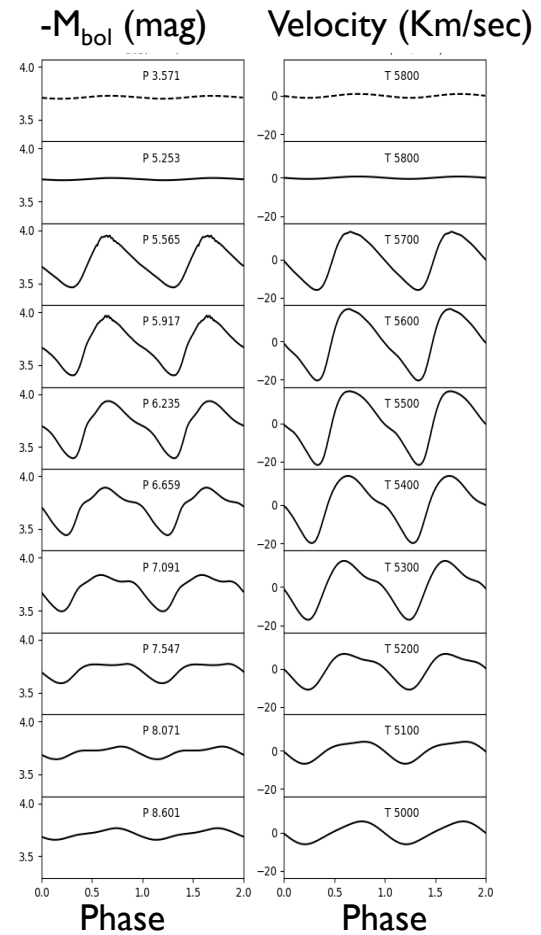
$Z=0.004$   $Y=0.25$

$7 M_{\odot}$



$Z=0.03$   $Y=0.28$

$6 M_{\odot}$





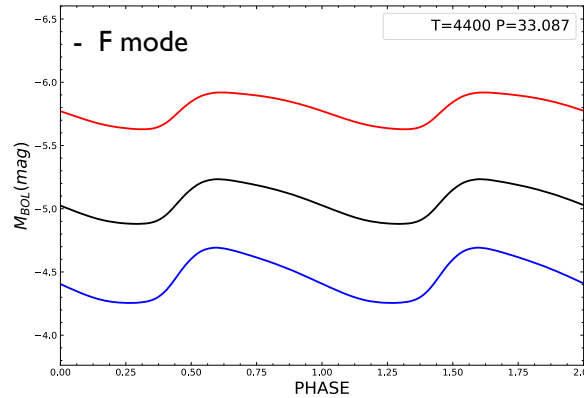
# From Bolometric to Gaia, HST-WFC3, Johnson and Rubin-LSST Filter Light Curves

By using bolometric corrections (Chen, Girardi et al. 2019 A&A), the bolometric light curves can be transferred into various photometric system passbands.

Filters:

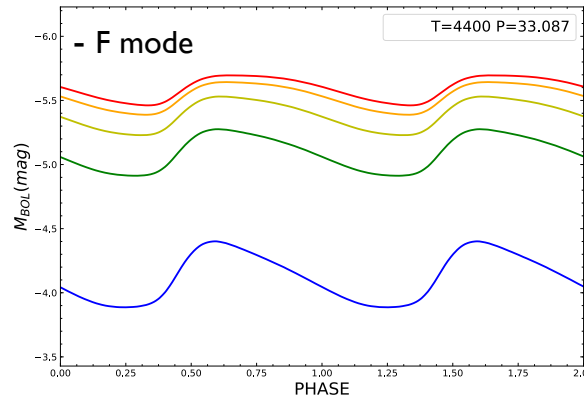
GAIA  $\rightarrow$   $G_{BP}$  (blue line),  $G$  (black line),  $G_{RP}$  (red line)  
RUBIN-LSST  $\rightarrow$   $g$  (blue line)  $r$  (green line)  $i$  (yellow line)  $z$  (orange line)  $Y$  (red line)

$M=3M_{\odot}$   $\log(L/L_{\odot})=2.32$   $\alpha=1.5$

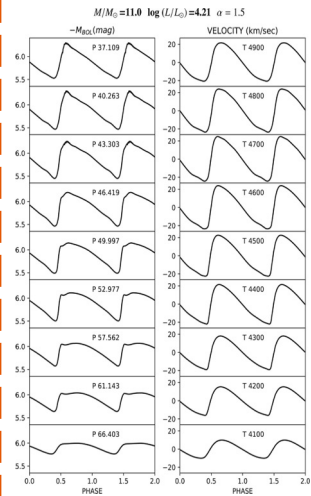


De Somma et al., 2020, ApJS

$M=9M_{\odot}$   $\log(L/L_{\odot})=3.92$   $\alpha=1.5$



De Somma et al. in preparation



The first theoretical atlas of Gaia and Rubin-LSST light curves

Nonlinear models



Converted light curves



The intensity weighted mean magnitudes, the pulsation amplitudes, and colors



The theoretical PLC, PW, and PWZ relations



Theoretical distances and parallaxes

The theoretical PLC and PW in the HST and Johnson filters, and  
**the first PLC and PW in Gaia**

$$\text{PLC} \rightarrow \langle G \rangle = a + b \log P + c (\langle G_{BP} \rangle - \langle G_{RP} \rangle)$$

For instance for  $Z=0.004$  ML can and  $\alpha = 1.5 \rightarrow \langle G \rangle = -3.143 - 3.741 + 3.107 (\langle G_{BP} \rangle - \langle G_{RP} \rangle)$

For instance for  $Z=0.02$  ML can and  $\alpha = 1.5 \rightarrow \langle G \rangle = -3.451 - 3.854 + 3.223 (\langle G_{BP} \rangle - \langle G_{RP} \rangle)$

$$\text{PW} \rightarrow \langle W \rangle = \langle G \rangle - 1.9 \langle G_{BP} - G_{RP} \rangle = a + b \log P$$

For instance for  $Z=0.008$  ML can and  $\alpha = 1.5 \rightarrow \langle W \rangle = -2.670 - 3.341 \log P$

For instance for  $Z=0.03$  ML can and  $\alpha = 1.5 \rightarrow \langle W \rangle = -2.779 - 3.264 \log P$

# The metal-Dependent Period-Wasenhheit relations

$$W = a + b \log P + c [\text{Fe}/\text{H}]$$

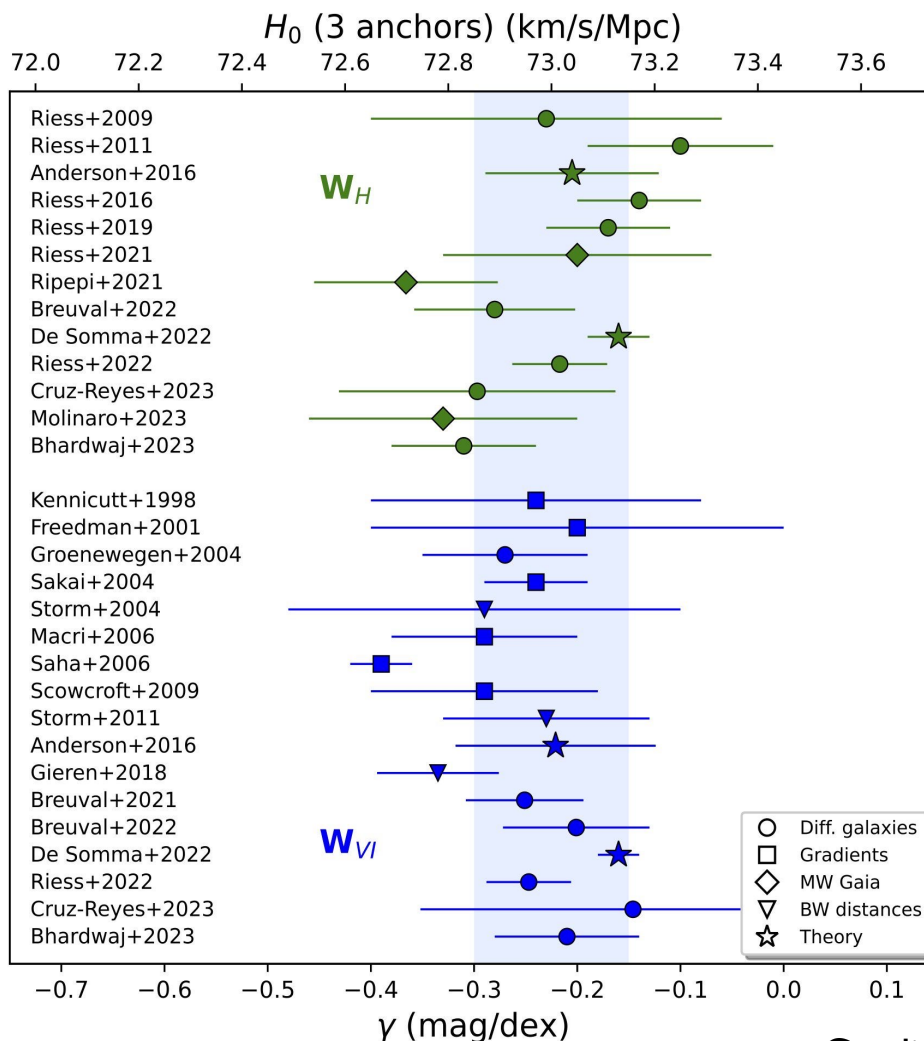
$\alpha_{\text{ml}}$	ML	$a$	$b$	$c$	$\sigma_a$	$\sigma_b$	$\sigma_c$	$\sigma$	$R^2$
<b>F</b>									
1.5	A	-6.018	-3.314	-0.189	0.009	0.016	0.021	0.118	0.993
1.7	A	-6.072	-3.379	-0.129	0.010	0.016	0.021	0.090	0.996
1.9	A	-6.170	-3.472	-0.245	0.023	0.018	0.040	0.072	0.998
1.5	B	-5.853	-3.234	-0.190	0.011	0.016	0.022	0.139	0.991
1.7	B	-5.871	-3.262	-0.260					
1.9	B	-5.968	-3.370	-0.189					
1.5	C	-5.694	-3.270	-0.105					
1.7	C	-5.722	-3.274	-0.140					
1.9	C	-5.800	-3.327	-0.167					
<b>FO</b>									
1.5	A	-6.676	-3.450	-0.221					
1.7	A	-6.818	-3.627	-0.243					
1.9	A	-6.933	-3.688	-0.349					
1.5	B	-6.634	-3.566	-0.304					
1.7	B	-6.616	-3.533	-0.303					
1.9	B	-6.719	-3.627	-0.304	0.066	0.050	0.068	0.030	0.998
1.5	C	-6.473	-3.510	-0.235	0.043	0.051	0.038	0.038	0.996
1.7	C	-6.486	-3.506	-0.261	0.049	0.056	0.051	0.030	0.998

Metal-dependent PW relations point towards a metallicity effect on the zero point varying from  $\sim -0.1$  dex to  $\sim -0.2$  dex for the F-mode relations and from  $\sim -0.1$  dex to  $\sim -0.3$  dex for the FO-mode relations.

De Somma et al. 2022 ApJS

At fixed period and color, models predict that more metallic Cepheids are brighter  
 → effect on the distance scale!

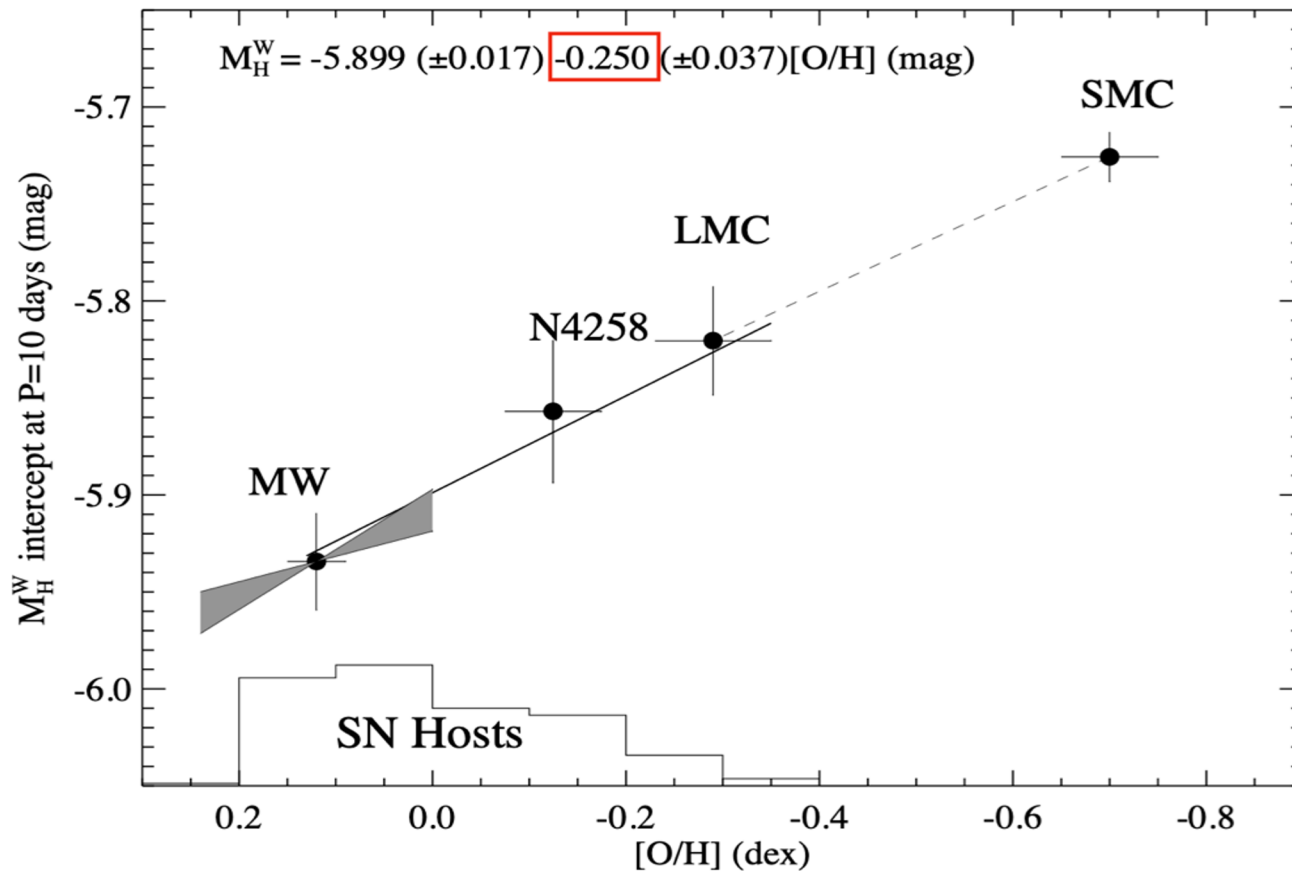
## Theoretical vs Empirical metallicity corrections



Credit: L.Breuval

Theoretical and empirical results are in good agreement!!

# Metallicity Correction: Small Effect on $H_0$



Overall, Cepheids in anchor galaxies (MW, LMC, NGC 4258) and in SNIa host galaxies have approximately the same metallicity → according to Riess et al. → no impact on  $H_0$

# The Role of the Mass Luminosity Relation

**The ML relation theoretically determines the coefficients of the PLC and in turn, PL and PW relations → impact on CC distance determinations → impact on  $H_0$  estimation**

# Predicted Distance to the Large Magellanic Cloud



**Standard ML**

$$\mu_{\text{LMC}} = 18.67 (0.05) \text{ mag}$$

**SML +  $\Delta\text{LogL}=0.2$  dex**

$$\mu_{\text{LMC}} = 18.56 (0.05) \text{ mag}$$

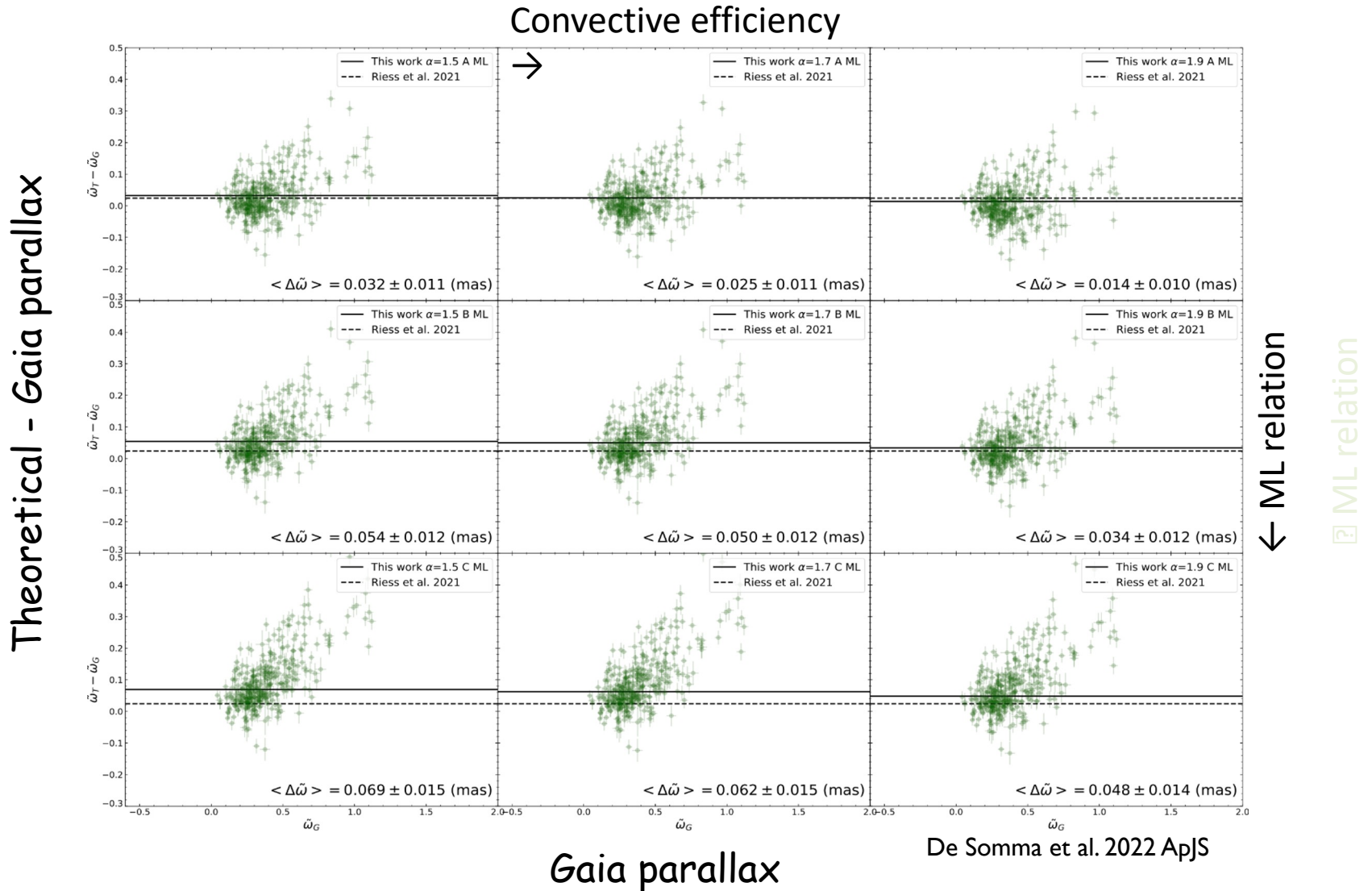
**SML +  $\Delta\text{LogL}=0.4$  dex**

$$\mu_{\text{LMC}} = 18.40 (0.05) \text{ mag}$$



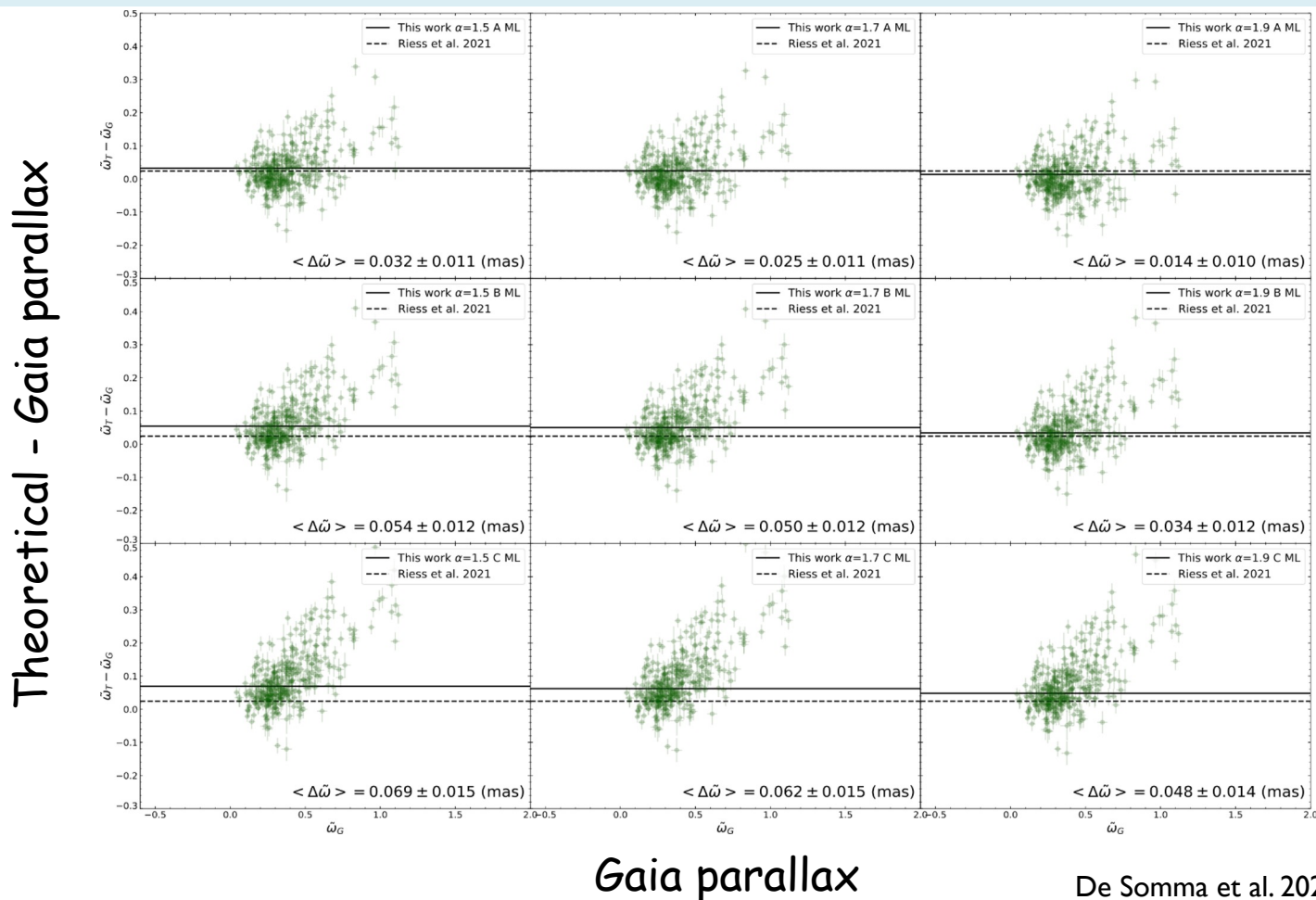
# Theoretical versus Gaia parallaxes for Galactic Cepheids (I)

Theoretical parallaxes were obtained by applying the PWZ:  $W = a + b \log P + c [\text{Fe}/\text{H}]$



# Theoretical versus Gaia parallaxes for Galactic Cepheids (II)

## The effect of the ML relation



$$\frac{\Delta \mathcal{B}}{\mathcal{B}} \sim \frac{\Delta H_0}{H_0}$$

← ML relation

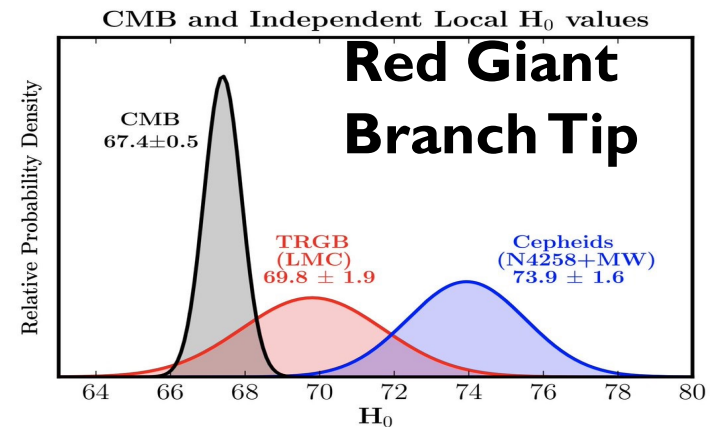
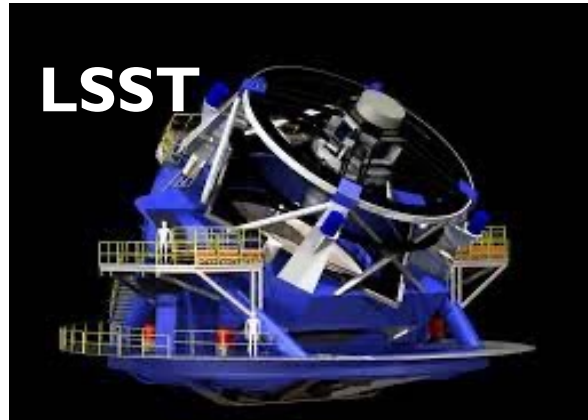
De Somma et al. 2022 ApJS

**Brighter/fainter ML relation implies a shorter/longer distance scale  
→ increase/decrease of  $H_0$**

## Conclusion

- The Hubble constant tension is one of the most debated topics in both cosmology and astrophysics
- The stellar route is largely based on Classical Cepheids
- Modeling these pulsating stars through nonlinear convective hydrodynamical computations is useful for constraining the residual systematics
- Models predict a dependence of the Cepheid distance scale on metallicity that is consistent with empirical evaluations
- Models suggest that a non-universal ML relationship can have a significant role

# Future Perspectives



Any questions, comments, and requests to collaborate are welcome!!!!

Thank you

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INAF-astronomical Observatory of Capodimonte