

Search for a muon EDM with  
the frozen-spin technique



Francesco Renga  
INFN Roma

# Disclaimer

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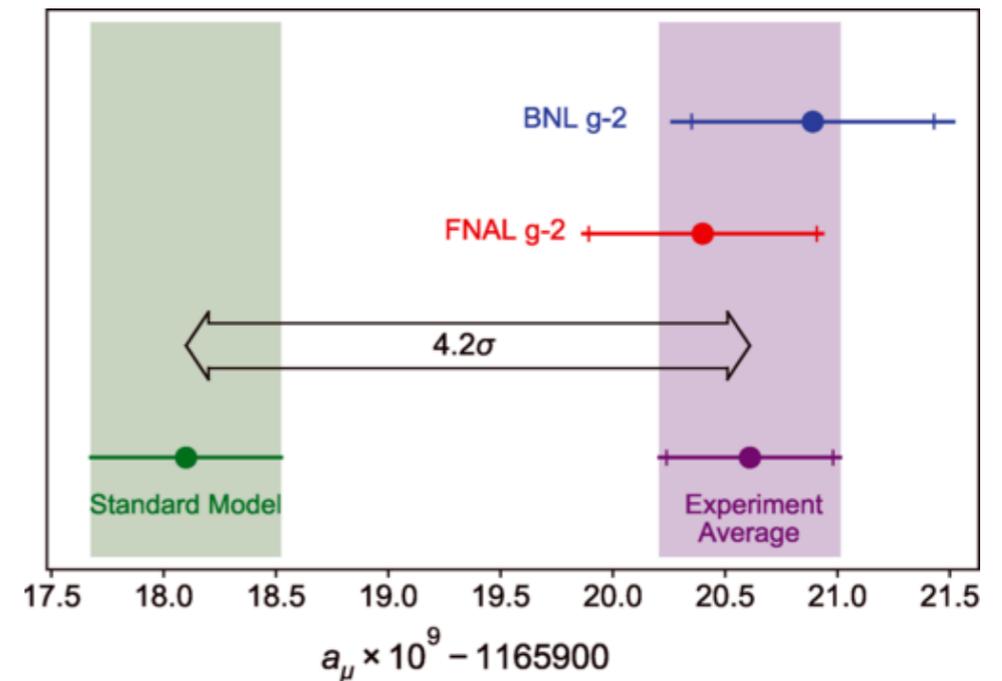
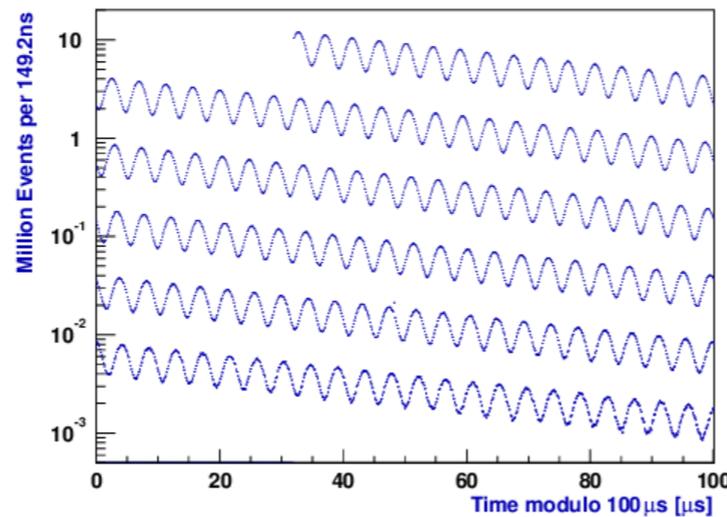
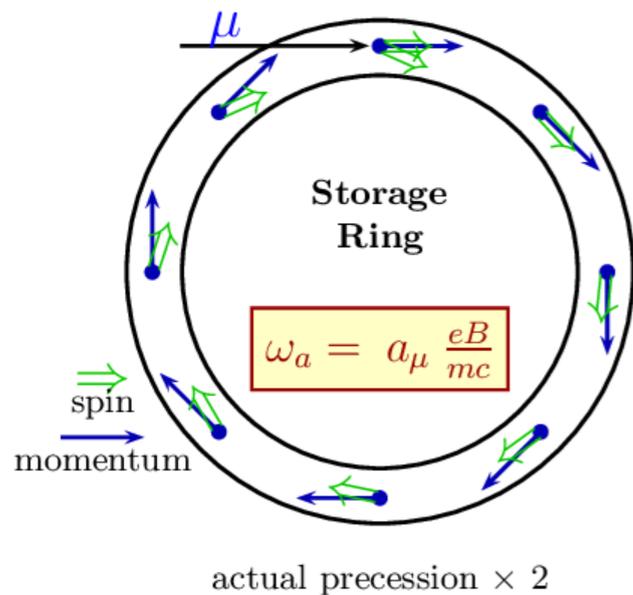
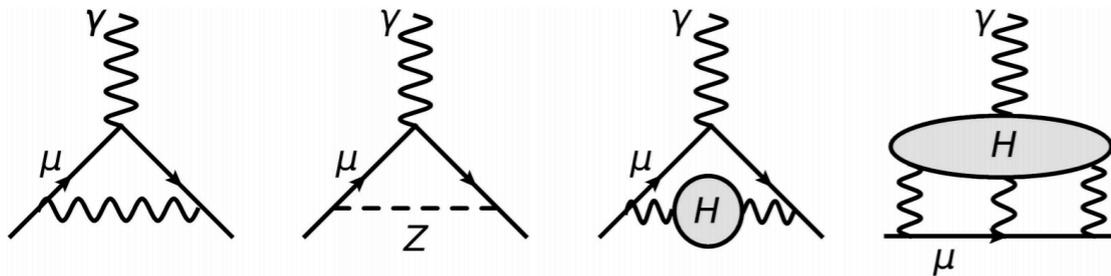
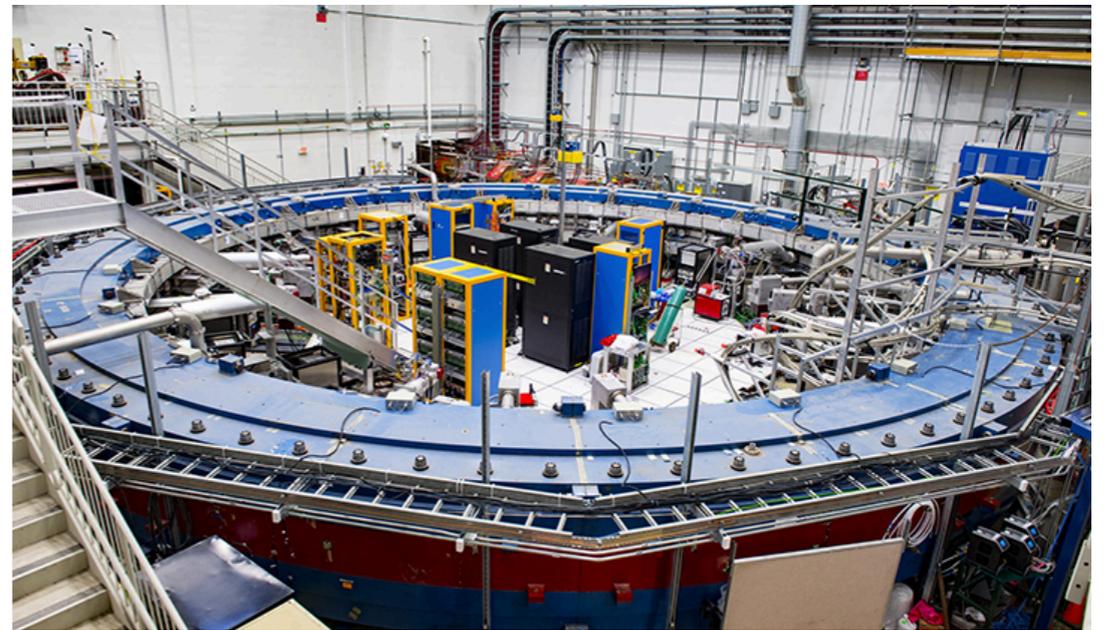
- Progetto non ancora presentato ufficialmente in CSN1:
  - non chiediamo l'apertura di una sigla per il 2023
  - presentazione introduttiva alla riunione di luglio, richiesta fondi per R&D e beam test per il prossimo anno
  - Sezioni attive: Roma, Pisa (+ manifestazione di interesse da Genova, Lecce, Pavia, Bologna e Padova)
- Progetto presentato al comitato scientifico del laboratorio di particelle del Paul Scherrer Institut (PSI), sotto forma di Lol, nel gennaio 2021:
  - feedback positivo dal comitato
  - si prevede di sottoporre un proposal formale alla prossima riunione nel gennaio 2023

# Physics Motivation

# The g-2

- The long-standing deviation of the anomalous magnetic moment of the muon ( $a_\mu = g_\mu - 2$ ) from SM predictions have been confirmed by the new FNAL experiment

**Phys. Rev. Lett. 126 (2021) 14, 141801**



# Dipole interactions in effective field theories

## ANOMALOUS MAGNETIC MOMENT

$$a_{l_i} = -\frac{4m_{l_i}}{e} \text{Re} c_R^{l_i l_i}$$

Processes intrinsically connected

NP explanation for g-2 is likely to imply large LFV and muon EDM

A. Crivellin and M. Hoferichter, arXiv:1905.03789  
 K. S. Babu, B. Dutta and R. N. Mohapatra, Phys. Rev. Lett. 85 (2000) 5064  
 E. O. Iltan, Eur. Phys. J. C 54 (2008) 583



**g-2 @ FNAL**

$$\mathcal{H}_{\text{eff}} = c_R^{l_f l_i} \bar{l}_f \sigma_{\mu\nu} P_R l_i F^{\mu\nu}$$

**This talk**

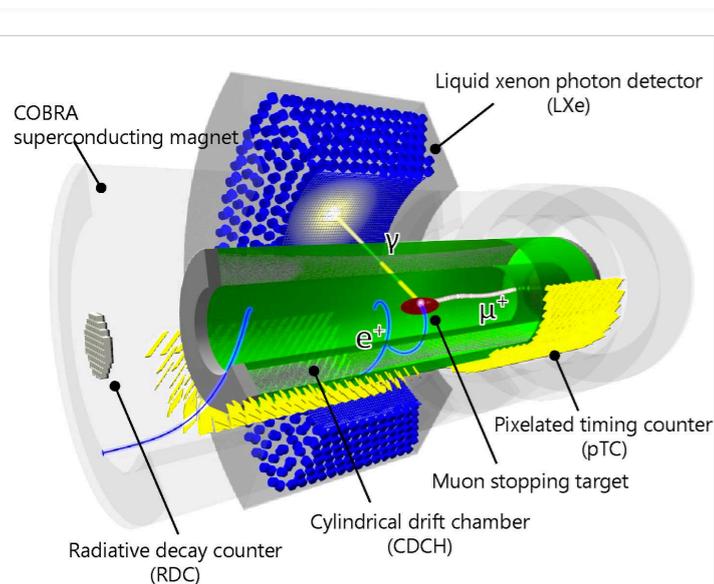
$$d_{l_i} = -2 \text{Im} c_R^{l_i l_i}$$

**ELECTRIC DIPOLE MOMENT (EDM)**

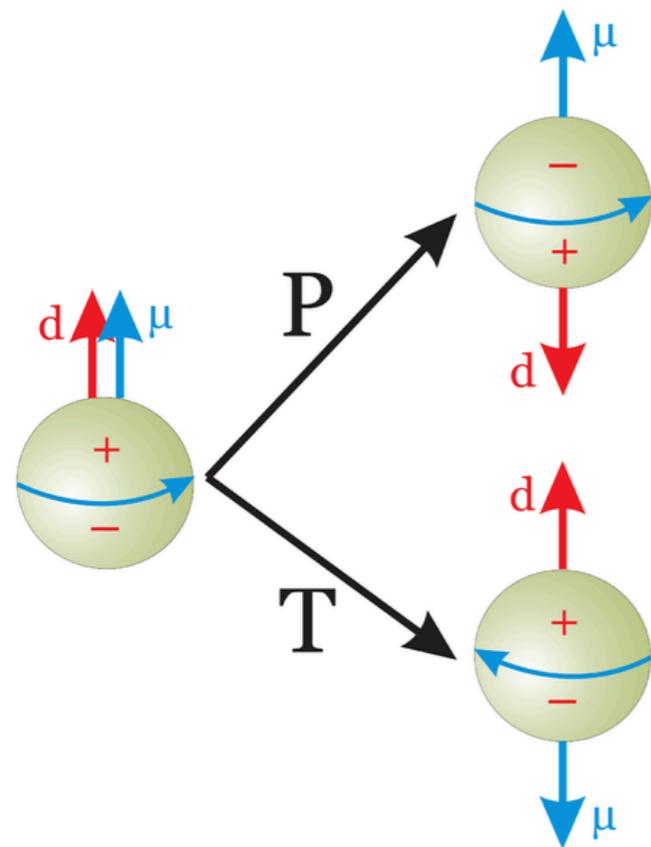
$$\text{Br}[\mu \rightarrow e\gamma] = \frac{m_\mu^3}{4\pi \Gamma_\mu} (|c_R^{e\mu}|^2 + |c_R^{\mu e}|^2)$$

**LEPTON FLAVOUR VIOLATION (LFV)**

**MEG II @ PSI**



# Electric dipole moments



Magnetic dipole moment

$$U = - \vec{\mu} \cdot \vec{B}$$

**P- and T-even**

Electric dipole moment

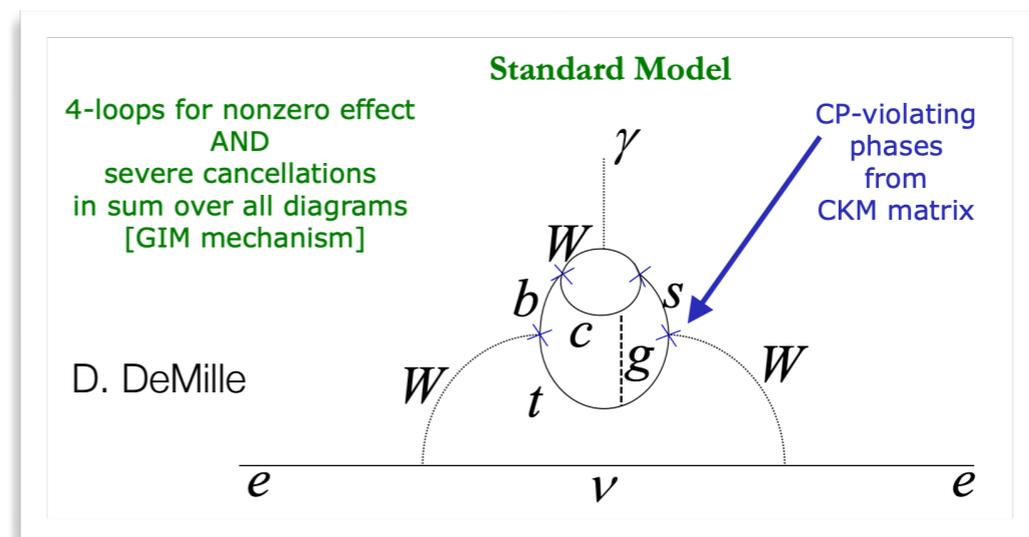
$$U = - \vec{d} \cdot \vec{E}$$

**P- and T-odd CPV!!!**

- EDMs of fundamental particles imply CP violation (CPV)
- leptons EDM in the SM from CKM phases in loops involving quarks  $\rightarrow$  very small, not accessible

$$\vec{\mu} = \frac{ge}{2mc} \vec{s}$$

$$\vec{d} = \frac{\eta e}{2mc} \vec{s}$$



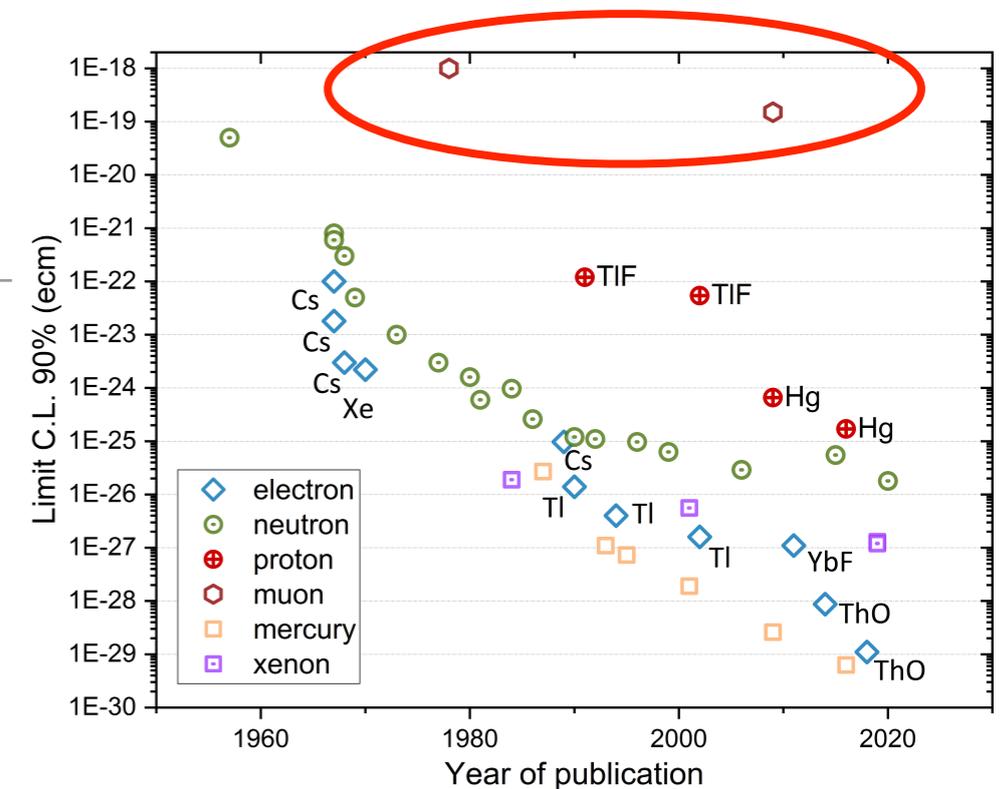
# Electron and muon EDM

- Muon EDM: strong link with  $g-2$ , would imply new sources of CPV (**matter-antimatter asymmetry of the universe**) and is negligible in the SM
- Strong constraints exist on the electron EDM (spin precession in molecular systems excited by lasers):
  - the muon EDM was somehow experimentally overlooked, due to the indirect constraint coming from the electron EDM under minimal flavour violation (MFV) assumptions

$$|d_e|_{\text{exp}} \leq 8 \times 10^{-30} e \text{ cm} \quad \xrightarrow{\text{MFV}} \quad |d_\mu|_{\text{ind}} \leq 1.6 \times 10^{-27} e \text{ cm}$$

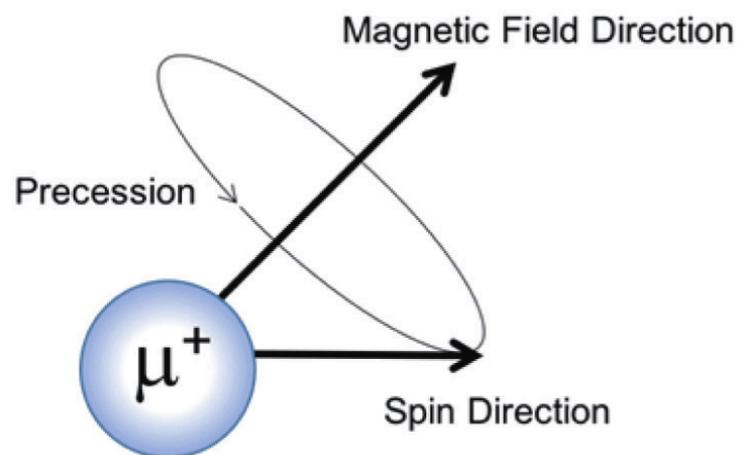
$$|d_\mu|_{\text{exp}} \leq 1.5 \times 10^{-19} e \text{ cm}$$

- Current muon EDM limits produced as by-product of  $g-2$  experiments
- **Indeed the new tensions in flavour physics, pointing toward Lepton Flavour Universality Violation (LUFV), challenge the MFV scenario and make a dedicated experiment to search for a muon EDM of great interest**



# Experimental techniques for muon EDM searches

# Dipole moments in electromagnetic fields



Magnetic spin precession  
in the particle rest frame

$$\vec{\omega}_L = 2 \vec{\mu} \cdot \vec{B}^* / \hbar$$

$$\vec{\mu} = \frac{ge}{2mc} \vec{s}$$

Electric spin precession  
in the particle rest frame

$$\vec{\omega}_d = 2 \vec{d} \cdot \vec{E}^* / \hbar$$

$$\vec{d} = \frac{\eta e}{2mc} \vec{s}$$

Electromagnetic spin precession  
in the laboratory rest frame

Cyclotron  
frequency

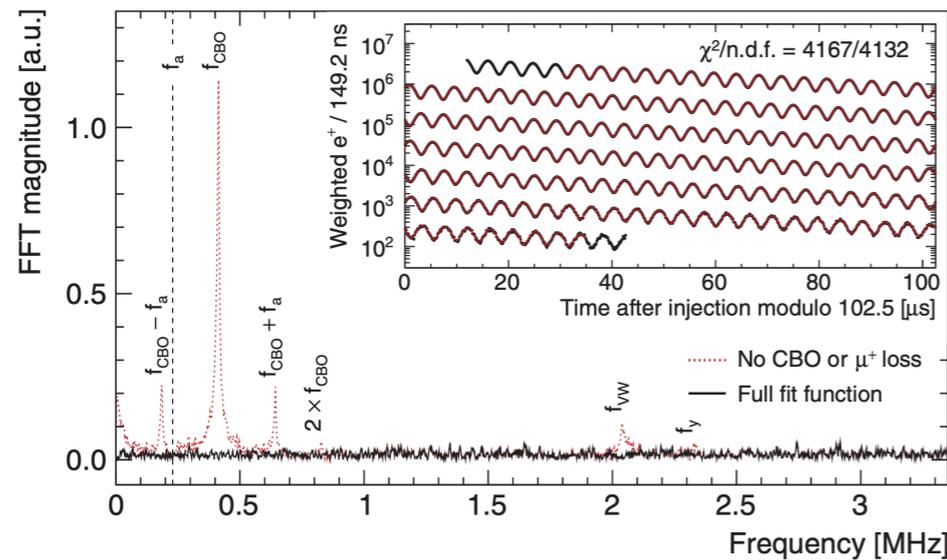
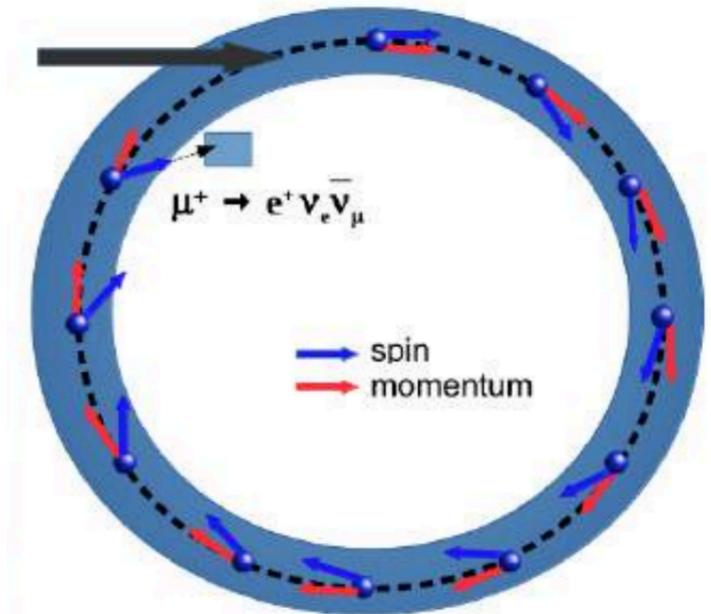
Thomas-Bargmann-Michel-Telegdi Equation (T-BMT)

$$\vec{\Omega} = \vec{\Omega}_0 - \vec{\Omega}_c = \frac{q}{m} \left[ a \vec{B} - \frac{a\gamma}{(\gamma+1)} (\vec{\beta} \cdot \vec{B}) \vec{\beta} - \left( a + \frac{1}{1-\gamma^2} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

$$+ \frac{\eta q}{2m} \left[ \vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} - \frac{\gamma}{(\gamma+1)c} (\vec{\beta} \cdot \vec{E}) \vec{\beta} \right] \quad \text{EDM contribution}$$

# Muon g-2 measurements in storage rings

- Thanks to parity violation, the **horizontally precessing** spin is reflected into the angular distribution of electrons produced in muon decays
- Counts on detectors at a given angle oscillate with frequency  $\Omega$



$$\vec{\beta} \perp \vec{B}$$

$$\gamma \simeq 1/\sqrt{a}$$

$$p \simeq 3.09 \text{ GeV}/c$$

("magic" momentum)

$$\vec{\Omega} = \vec{\Omega}_0 - \vec{\Omega}_c = \frac{q}{m} \left[ a\vec{B} - \frac{\omega\gamma}{(\gamma+1)} (\vec{\beta} \cdot \vec{B}) \vec{\beta} - \left( a + \frac{1}{1-\gamma^2} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

$$+ \frac{\eta q}{2m} \left[ \vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} - \frac{\gamma}{(\gamma+1)c} (\vec{\beta} \cdot \vec{E}) \vec{\beta} \right].$$

**Neglected**

# Muon EDM from g-2 experiments

- Search for **vertical precession** due to the **“relativistic” electric field observed by the muon in its rest frame**,  $\vec{E}^* = \gamma c \vec{\beta} \times \vec{B} \sim 13.5 \text{ GV/m}$
- Although the experiments are not optimised for this measurement, the vertical granularity of the detectors combined with such a huge field still allows a precise measurement of the muon EDM

$$|d_\mu|_{\text{exp}} \leq 1.5 \times 10^{-19} e \text{ cm}$$

*Phys.Rev.D* 80 (2009) 052008 [BNL Muon g-2]

$$\gamma \simeq 1/\sqrt{a}$$

$$p \simeq 3.09 \text{ GeV}/c$$

(“magic” momentum)

$$\vec{\beta} \perp \vec{B}$$

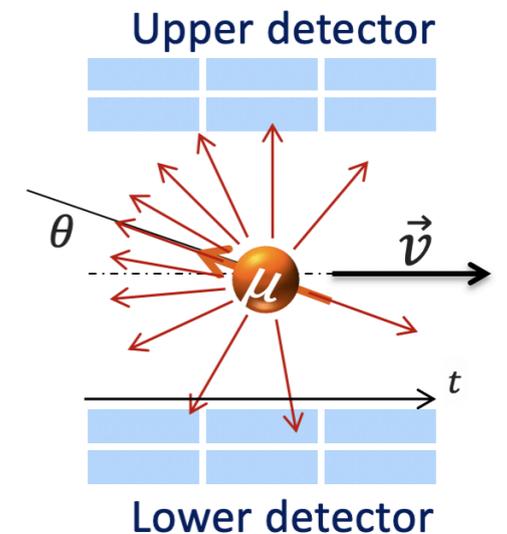
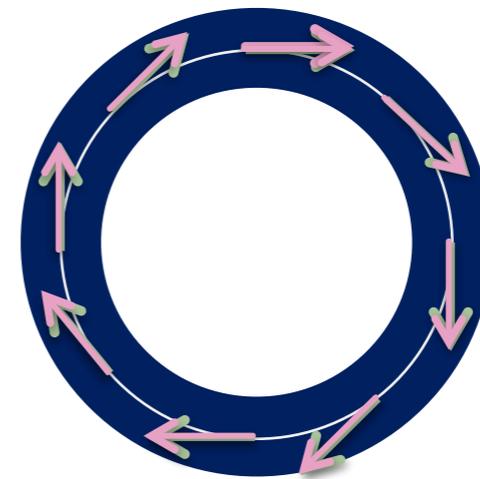
$$\vec{\Omega} = \vec{\Omega}_0 - \vec{\Omega}_c = \frac{q}{m} \left[ a\vec{B} - \frac{\omega\gamma}{(\gamma+1)} (\vec{\beta} \cdot \vec{B}) \vec{\beta} - \left( a + \frac{1}{1-\gamma^2} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

“Relativistic”  
electric field

$$+ \frac{\eta q}{2m} \left[ \vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} - \frac{\gamma}{(\gamma+1)c} (\vec{\beta} \cdot \vec{E}) \vec{\beta} \right] \cdot \text{Small}$$

# The frozen spin technique

- An electric field is applied to cancel the horizontal precession
- For  $\eta = 0$ , the spin is locked parallel to the momentum (as it has been produced in  $\pi$  decays)
- Search for a **vertical precession** due to a non-null EDM in the relativistic electric field



$\vec{\beta} \perp \vec{B}$  + apply an electric field  $E_f \simeq aBc\beta\gamma^2$  so that

$$a\vec{B} = \left( a - \frac{1}{\gamma^2 - 1} \frac{\vec{\beta} \times \vec{E}}{c} \right)$$

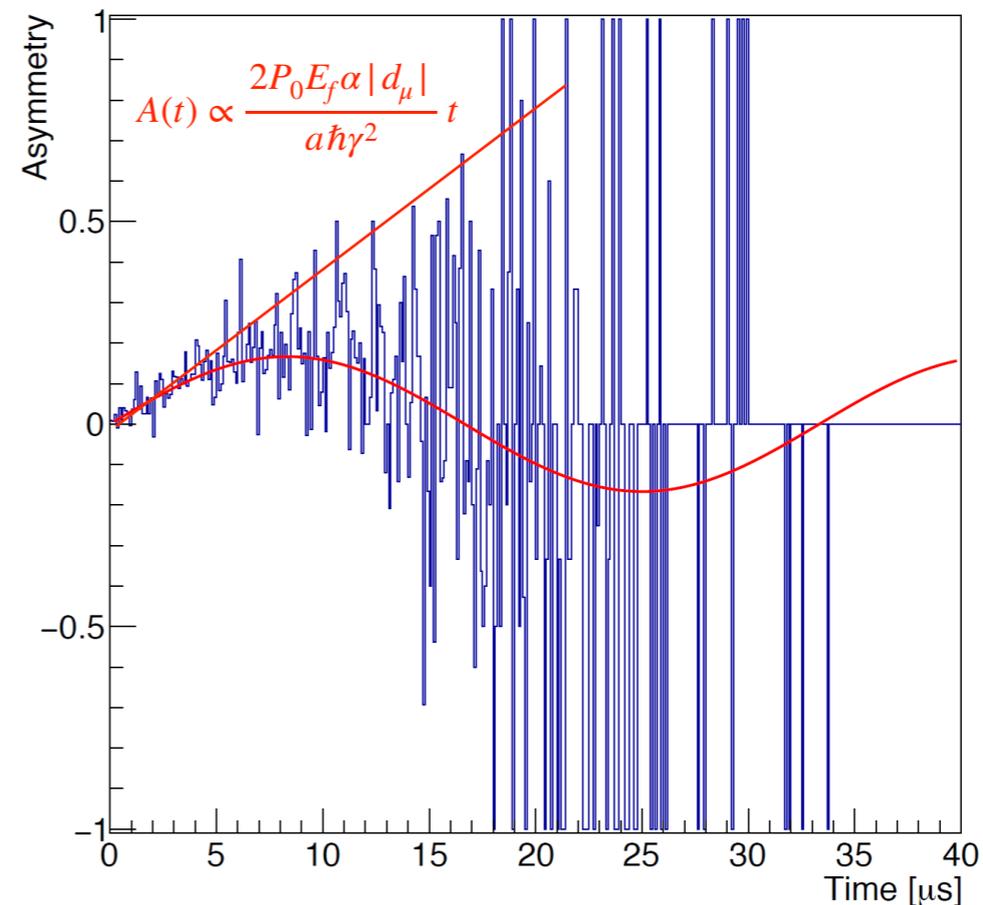
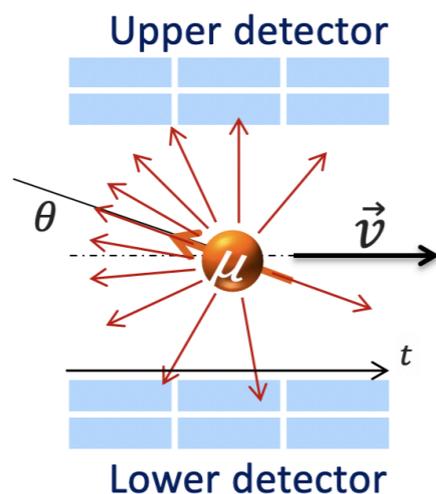
$$\vec{\Omega} = \vec{\Omega}_0 - \vec{\Omega}_c = \frac{q}{m} \left[ a\vec{B} - \frac{a\gamma}{(\gamma + 1)} (\vec{\beta} \cdot \vec{B}) \vec{\beta} - \left( a + \frac{1}{1 - \gamma^2} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

“Relativistic”  
electric field

$$+ \frac{\eta q}{2m} \left[ \vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} - \frac{\gamma}{(\gamma + 1)c} (\vec{\beta} \cdot \vec{E}) \vec{\beta} \right] \cdot \text{Small}$$

# Experimental signal: up/down asymmetry

$$A(t) = \frac{N_{\uparrow}(t) - N_{\downarrow}(t)}{N_{\uparrow}(t) + N_{\downarrow}(t)}$$



**Sensitivity from the asymmetry averaged over the muon decay time distribution (lifetime =  $\gamma\tau_{\mu}$ )**

$$\sigma(|d_{\mu}|) = \frac{d|d_{\mu}|}{d\bar{A}} \sigma(\bar{A}) \sim \frac{a\hbar\gamma}{2P_0E_f\sqrt{N}\tau_{\mu}\alpha}$$

$P_0$  = initial polarisation degree  
 $E$  = electric field in the lab frame  
 $N$  = number of observed decays  
 $\tau_{\mu}$  = muon lifetime  
 $\alpha$  = mean decay asymmetry ( $\sim 0.3$ )

**The “PENTA” formula**

# A muon EDM search at PSI

# The muonEDM Proposal

- A formal proposal for a Muon EDM experiment was presented in January 2023 to the PSI Research Committee for Particle Physics

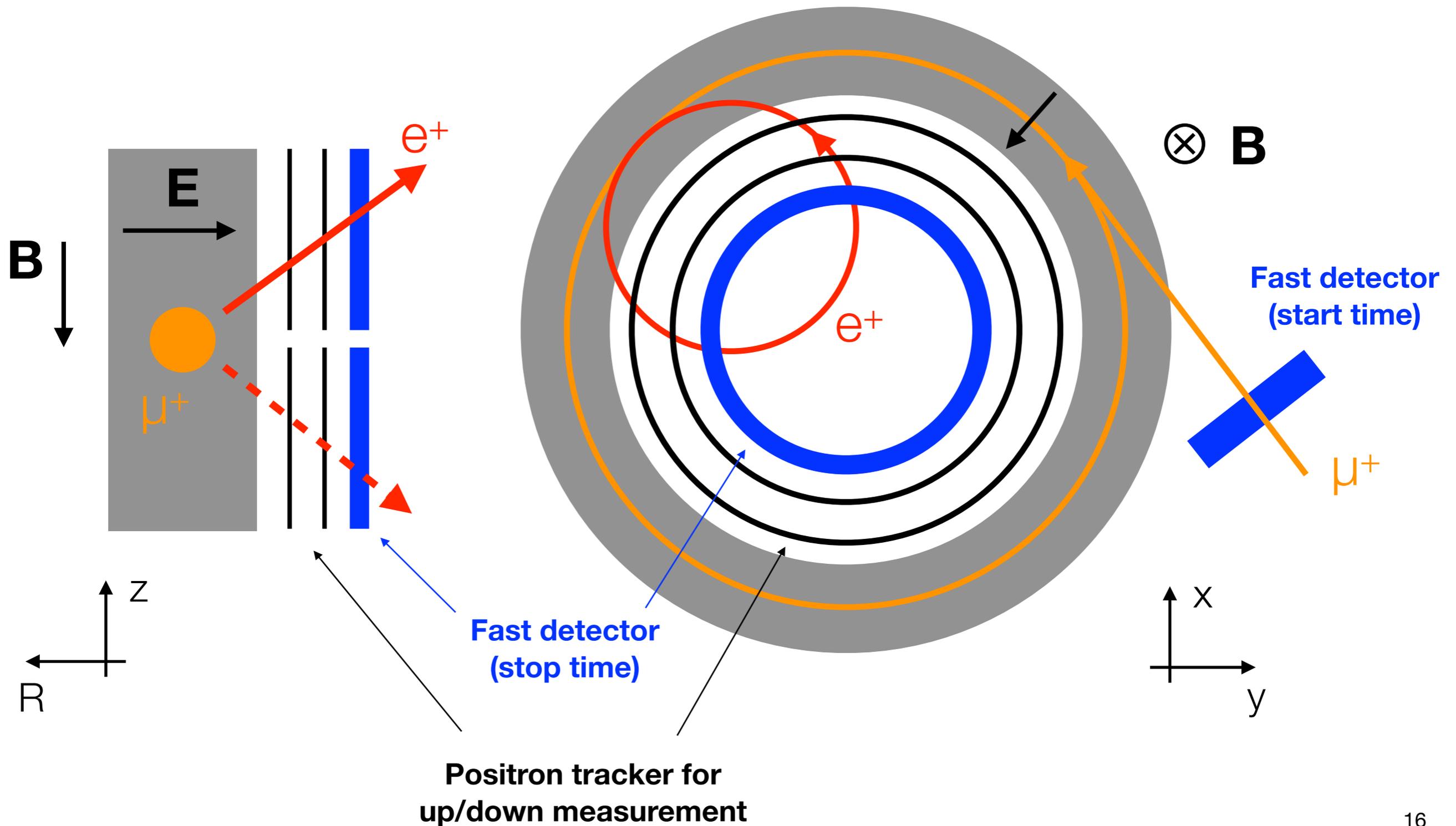


A. Adelman<sup>1,2</sup> M. Backhaus<sup>1</sup> C. Chavez Barajas<sup>3</sup> N. Berger<sup>4</sup> T. Bowcock<sup>3</sup> C. Calzolaio<sup>2</sup> G. Cavoto<sup>5,6</sup>  
 R. Chislett<sup>7</sup> A. Crivellin<sup>2,8,9</sup> M. Daum<sup>2</sup> M. Fertl<sup>10</sup> M. Giovannozzi<sup>8</sup> G. Hesketh<sup>7</sup> M. Hildebrandt<sup>2</sup>  
 I. Keshelashvili<sup>11</sup> A. Keshavarzi<sup>12</sup> K.S. Khaw<sup>13,14</sup> K. Kirch<sup>1,2</sup> A. Kozlinsky<sup>4</sup> A. Knecht<sup>2</sup> M. Lancaster<sup>12</sup>  
 B. Märkisch<sup>15</sup> F. Meier Aeschbacher<sup>2</sup> F. Méot<sup>16</sup> A. Nass<sup>11</sup> A. Papa<sup>2,17</sup> J. Pretz<sup>11,18</sup> J. Price<sup>3</sup> F. Rathmann<sup>11</sup>  
 F. Renga<sup>6</sup> M. Sakurai<sup>1</sup> P. Schmidt-Wellenburg<sup>2</sup> A. Schöning<sup>19</sup> C. Voena<sup>6</sup> J. Vossebeld<sup>3</sup> F. Wauters<sup>4</sup> and P. Winter<sup>20</sup>



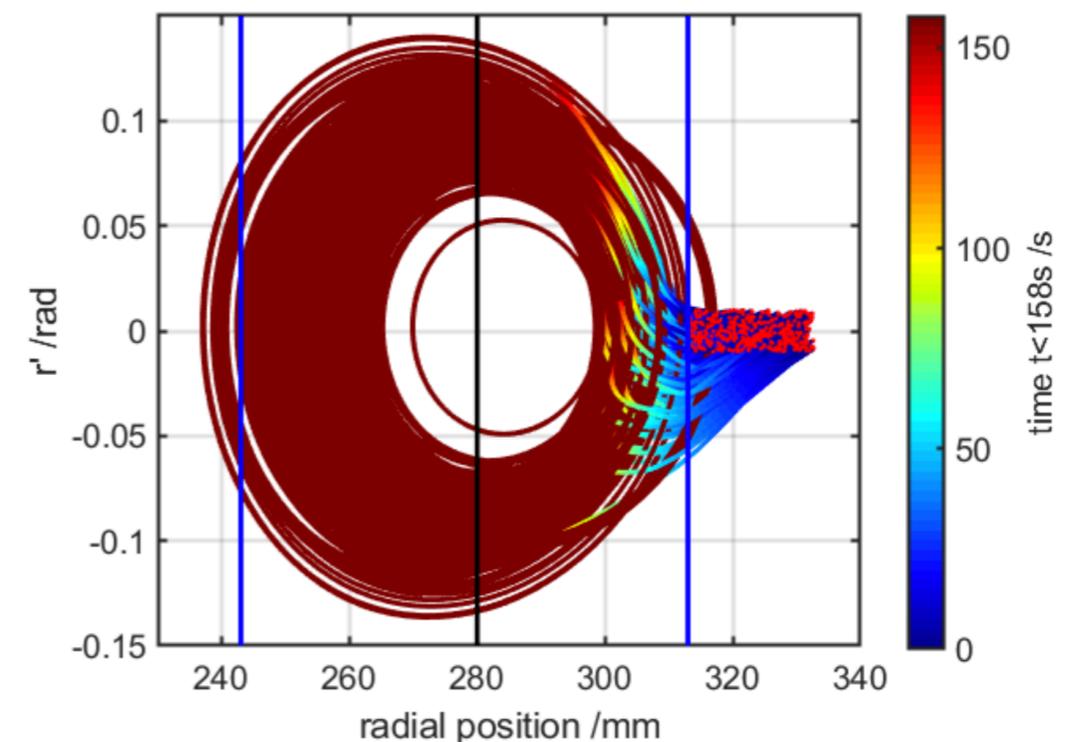
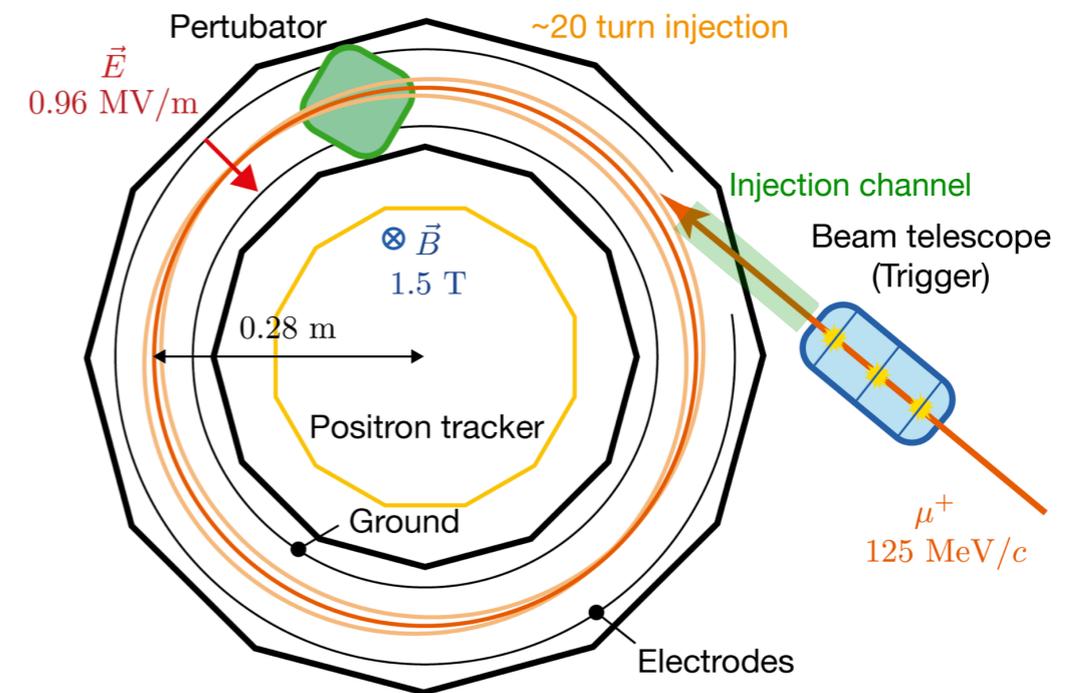
# Experimental approach

$$A(t) = \frac{N_{\uparrow}(t) - N_{\downarrow}(t)}{N_{\uparrow}(t) + N_{\downarrow}(t)}$$



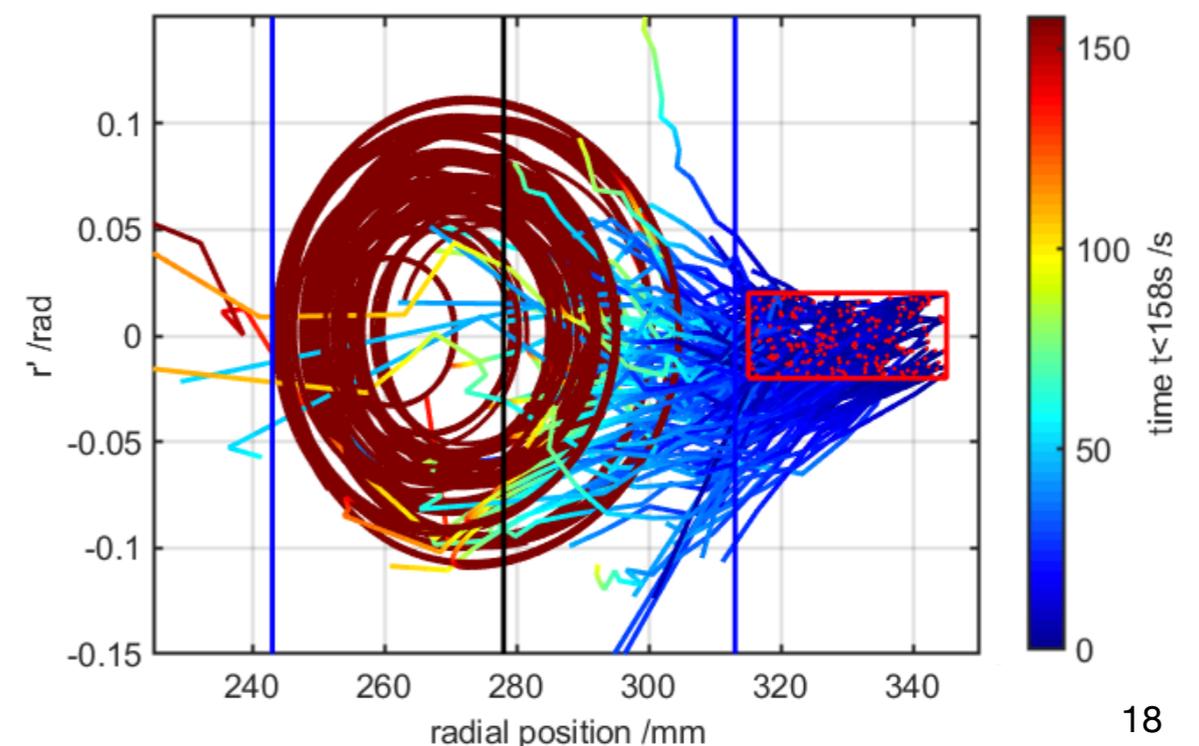
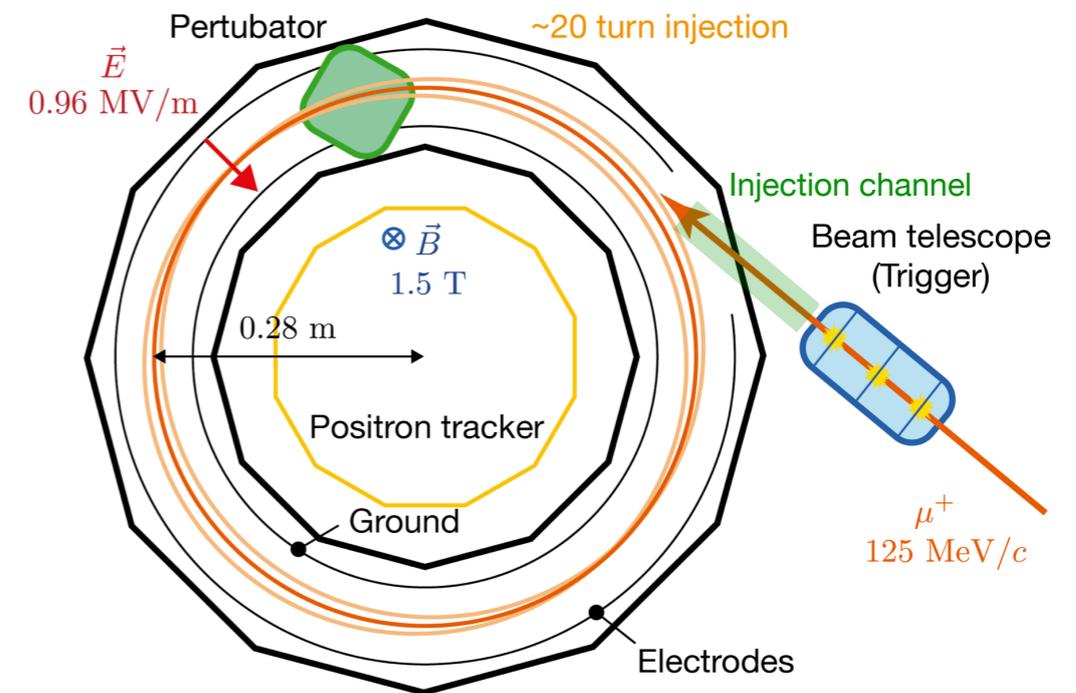
# Experimental concepts — Storage ring

- Compact storage ring with lateral injection through a magnetic channel
- Need a **magnetic kick within 1 revolution (< 10 ns)** to avoid hitting the injection channel after 1 turn
- In principle, 0.14% injection efficiency is possible considering the emittance of the PSI beam lines



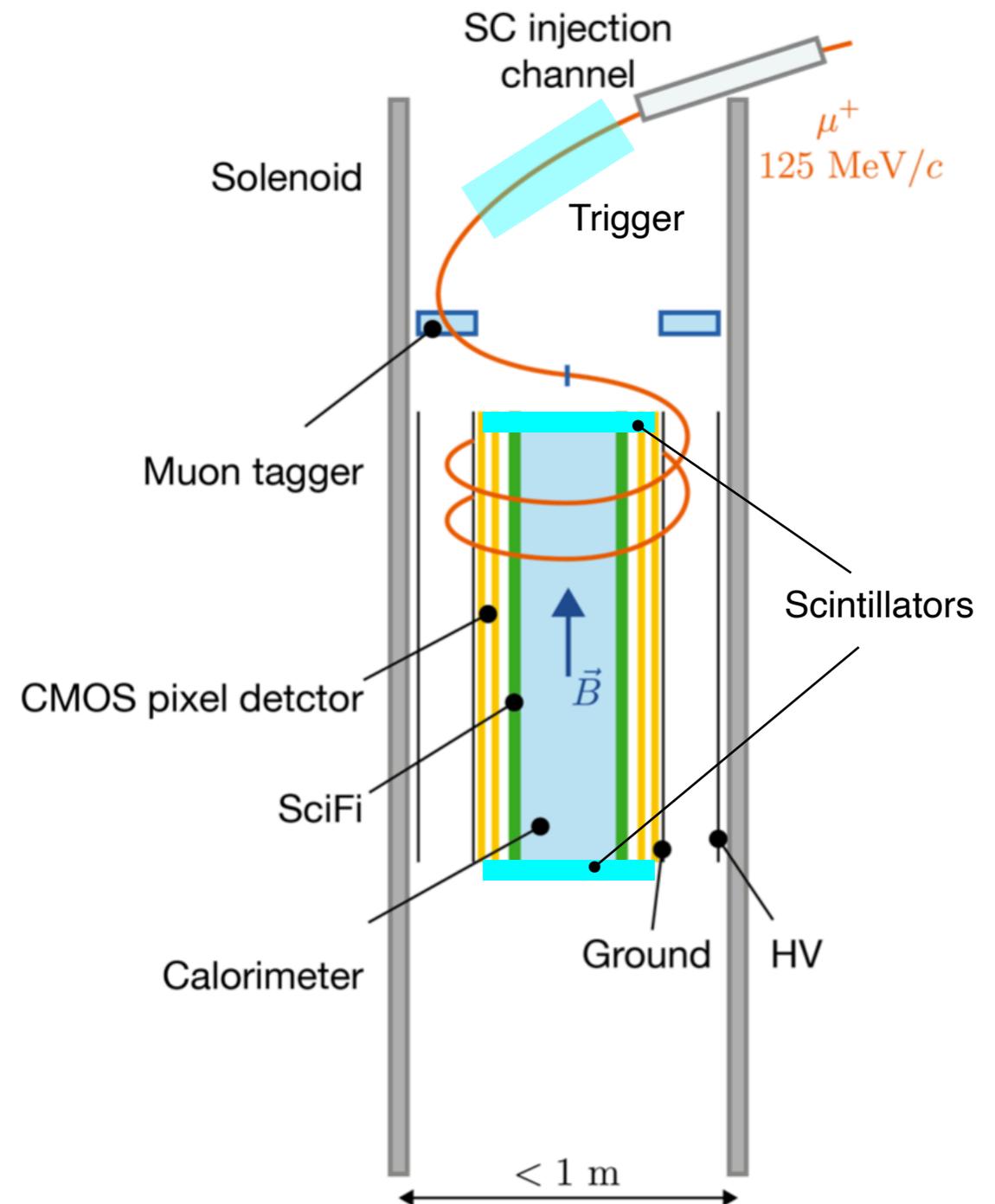
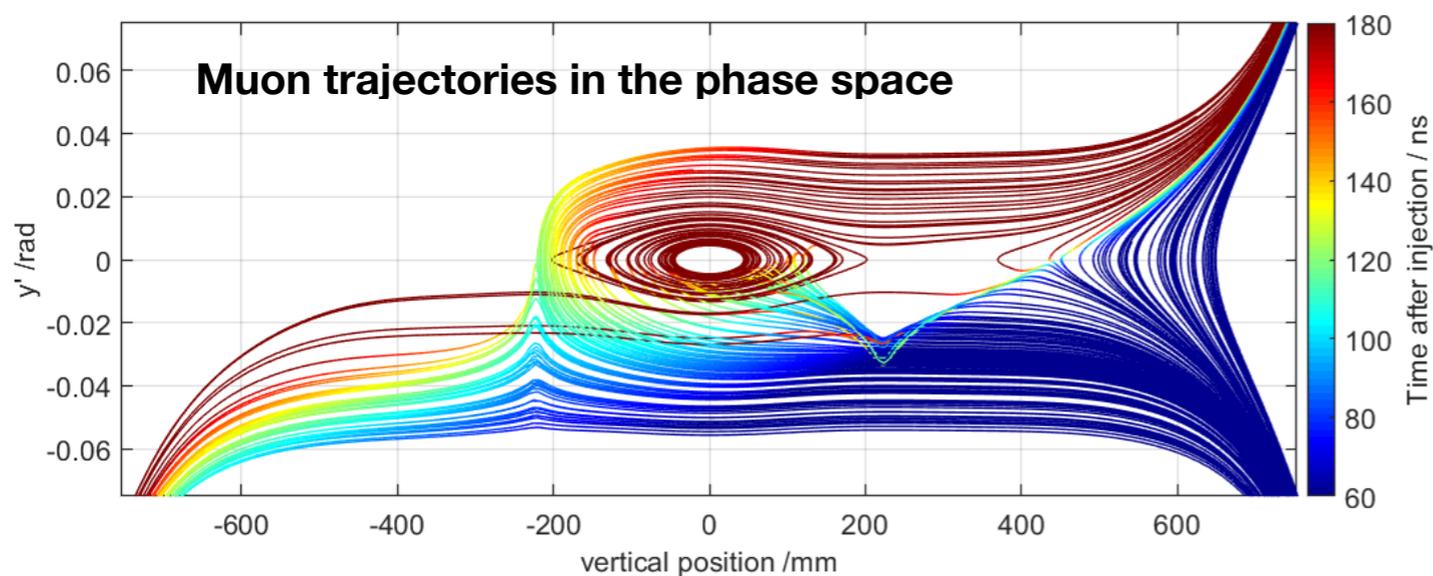
# Experimental concepts — Storage ring

- Compact storage ring with lateral injection through a magnetic channel
- Need a **magnetic kick within 1 revolution (< 10 ns)** to avoid hitting the injection channel after 1 turn
- In principle, 0.14% injection efficiency is possible considering the emittance of the PSI beam lines
- In practice, before the orbit stabilises, muons are lost due to **MS through the E-field electrodes**
  - **efficiency**  $\sim 10^{-4}$
  - positron detection rate  $\sim 10$  kHz



# Experimental concepts — Helix muonEDM

- Vertical injection into a 3T solenoid
- Also need a **kick** to stabilise the orbit in the central region, but **within > 50 ns**
- **Minimal material budget** along the muon trajectories
- **$5 \times 10^{-4}$  capture efficiency**
  - 50 kHz detection rate

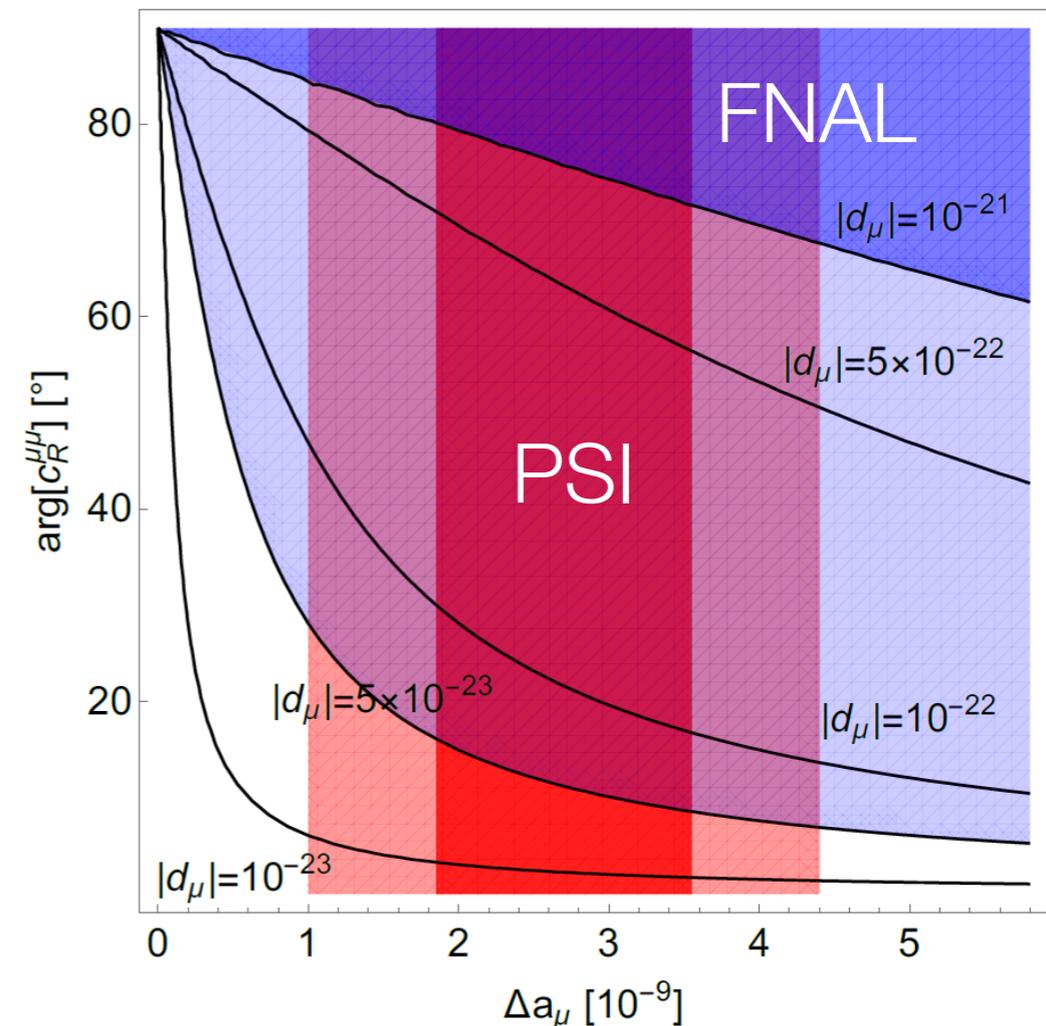


# Sensitivity and Physics reach (1 year run)

- $a = 1.12 \times 10^{-3}$
- $\gamma = 1.55$
- $P_0 = 0.93$
- $E = 20 \text{ kV/cm}$
- $N = 50 \text{ MHz} \times 200 \text{ days} = 7 \times 10^{11}$
- $\tau = 2.2 \times 10^{-6} \text{ s}$
- $\alpha = 0.3$

$$\sigma(|d_\mu|) \approx \frac{a\hbar\gamma}{2P_0E_f\sqrt{N}\tau_\mu\alpha}$$

$$\sigma(|d_\mu|) \leq 6 \times 10^{-23} e \cdot \text{cm}$$



# A staged approach

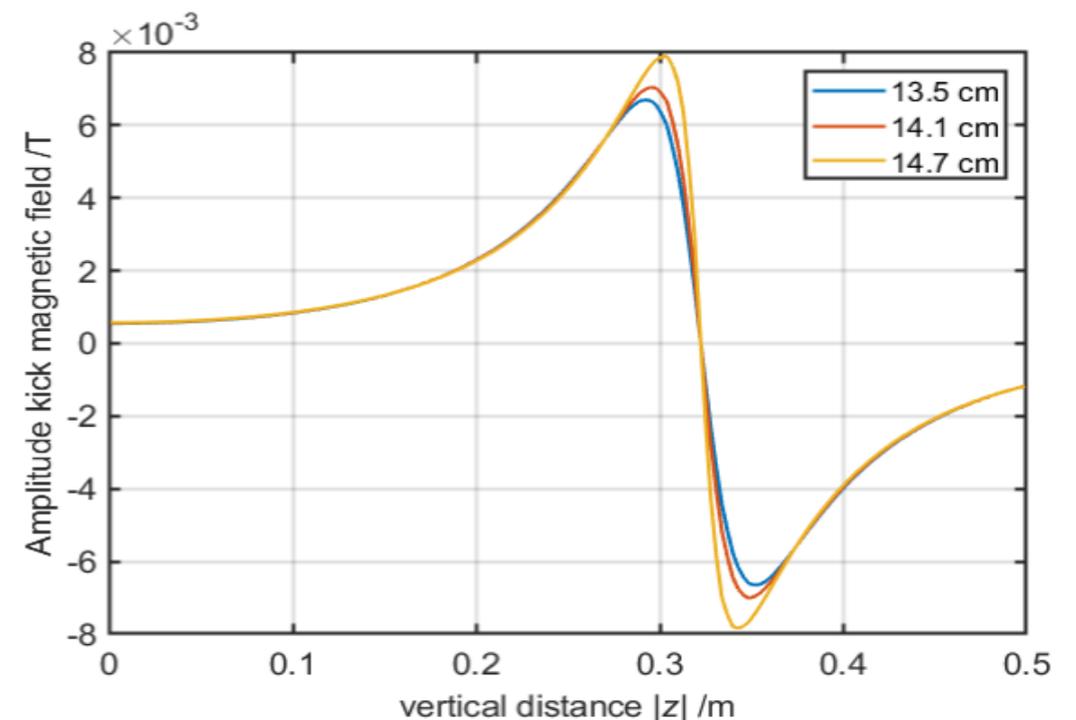
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- Phase-1 (precursor experiment):
  - **goals: demonstrate the feasibility of injection principle and frozen spin technique + improve the current limit by x50** (competitive with final results from ongoing g-2 experiments)
  - existing magnet (3 T, 10 cm bore)
  - non-optimal beam line (28 MeV/c) to match the magnet strength and size and to avoid conflicts with other activities
  - $E \sim 3$  kV/cm
  - simplest detector solutions
  - partially covered by an ERC CoG at PSI
- Phase-2
  - **goal: improve the current limit by x2000**
  - dedicated magnet (3T)
  - best suited beam line (125 MeV/c)
  - $E \sim 20$  kV/cm
  - optimal detector solutions

# Challenges

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- Fast and very thin detectors in the injection channel to trigger the magnetic kick
- Fast ramping of kick magnets
- Detectors with minimal material budget, operating in vacuum
- Accurate rotation of the full apparatus to invert the injection direction and suppress systematics from disuniformities of the fields
- Large eddy currents from the magnetic kick



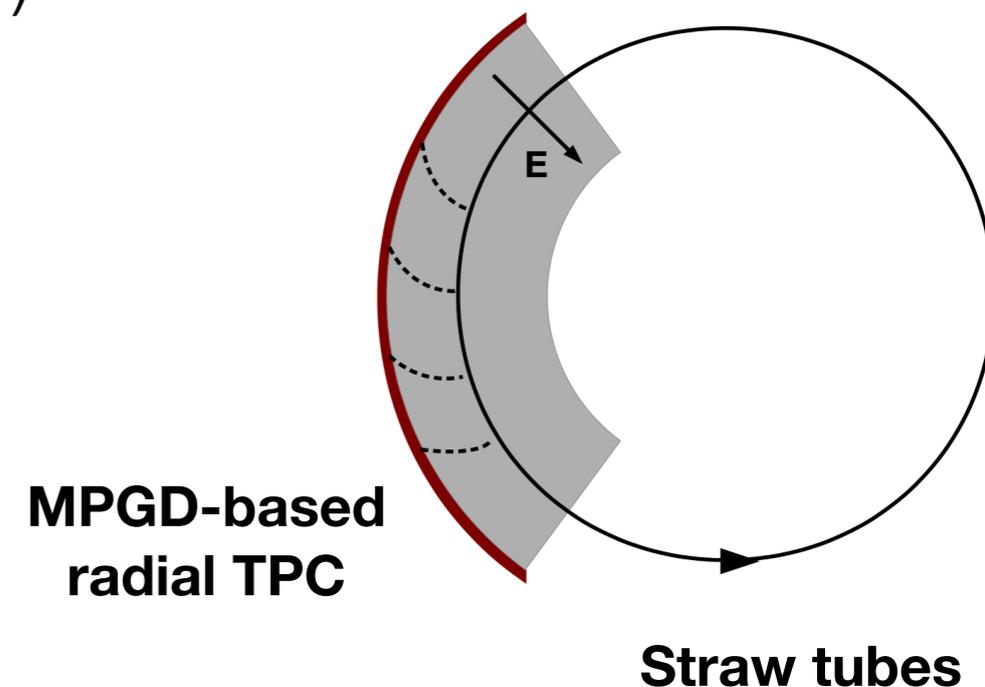
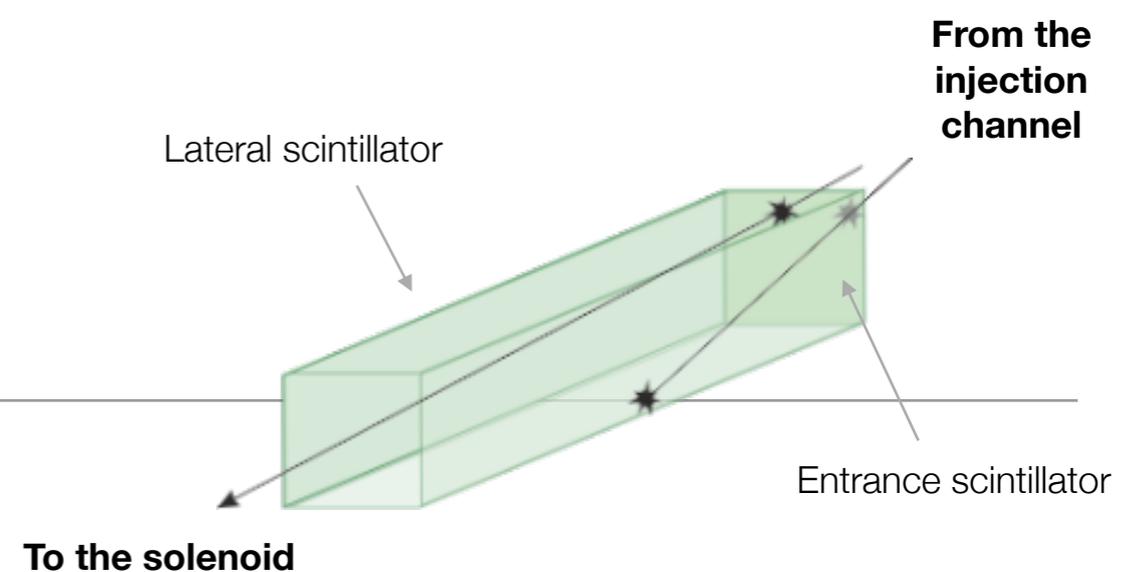
# Detector developments

- Fast kick trigger from muons:

- extremely thin scintillator to preserve the muon emittance (critical to keep a high capture efficiency)

- Very light muon tracker to characterise the beam and the trigger before the EDM measurement — **high granularity TPC**

- Positron tracking and timing in a harsh environment (vacuum, limited space, eddy currents...) — **scintillating fibers/ silicon detectors**



# INFN Roma: interests and opportunities

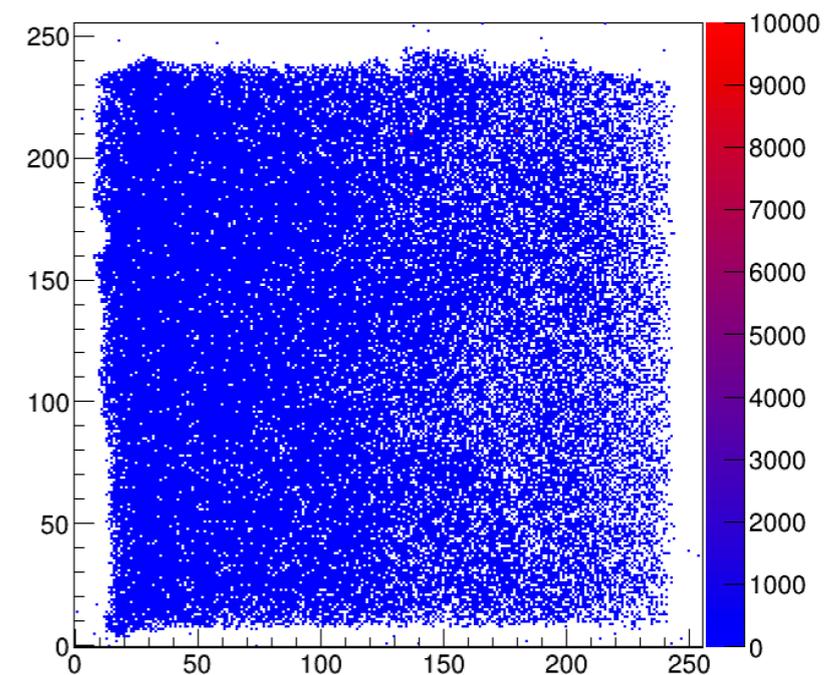
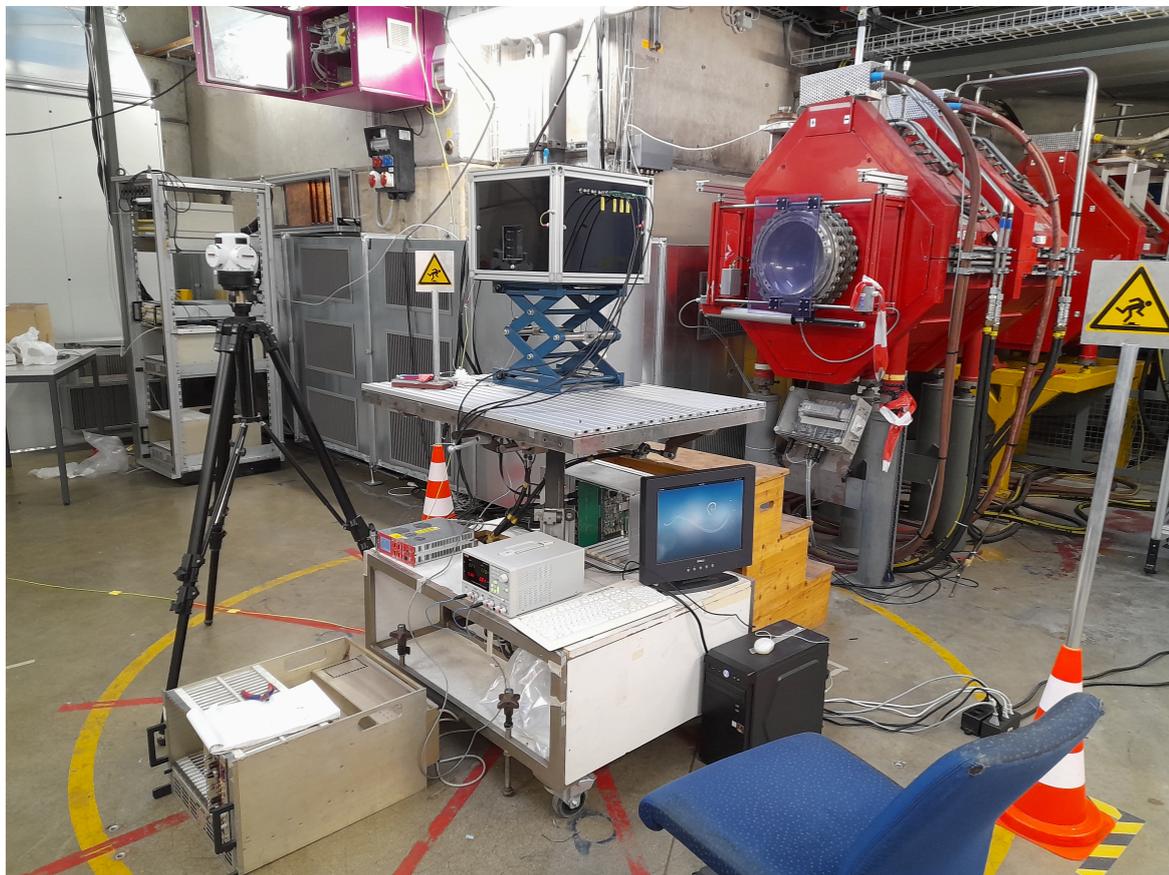
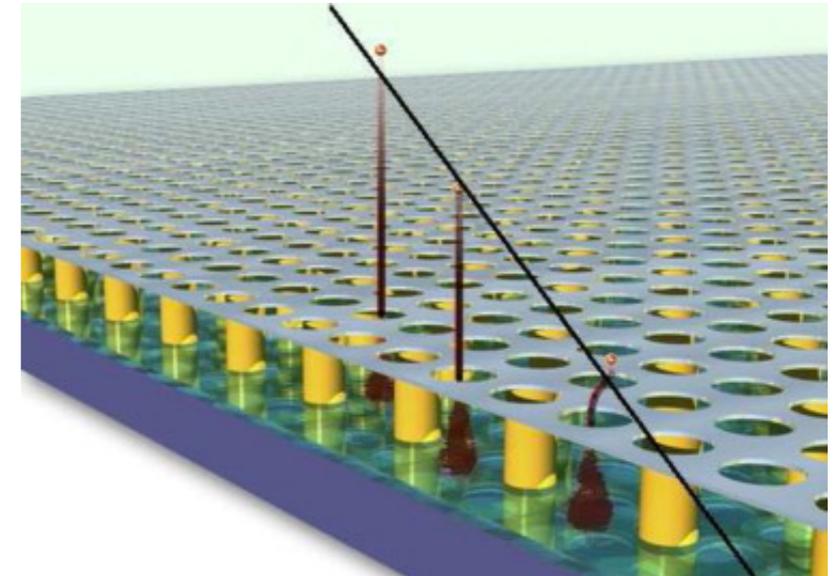
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- Muon tracker:
  - R&D for a TPC with high granularity readout
- Mechanical integration
  - Criticalities in engineering manpower availability at PSI
  - Concrete possibility of taking a leading role
- Many other opportunities if there are people interested to join:
  - beam injection
  - fast trigger electronics
  - analysis and simulation
  - ...

# Muon tracker R&D (INFN Roma & Sapienza)

- TPC with high granularity readout (GridPix)
  - two test beams in 2022 @ PSI
  - one paper submitted to JINST, second paper in preparation

**50  $\mu\text{m}$  pixel readout**



# Tentative Schedule

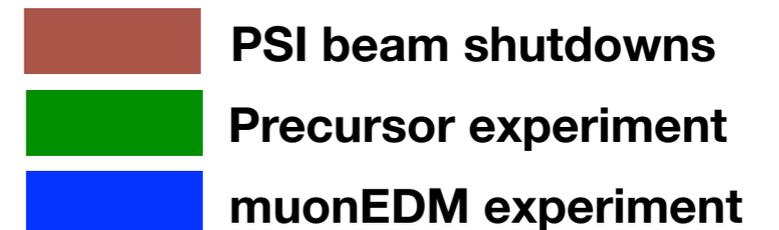


- First tests with the precursor setup: **2026**
  - demonstration of injection and frozen spin

- PSI long shutdown: **2027**
  - upgrade of the muon beam lines

- Precursor experiment: **2028**

- Final experiment: **2030 - 2031**
  - in combination with innovative beam-cooling approaches (muCool) could yield a much higher injection probability



# Conclusions

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- A dedicated experiment to search for a muon EDM is highly desirable to complete the experimental coverage on dipole interactions and new sources of CP violation
- Excellent prospects for a ground-breaking muon EDM experiment at PSI within this decade
  - improving the limit by 3 orders of magnitudes, down to  $6 \times 10^{-23} \text{ e} \cdot \text{cm}$  per year
  - improving the expected limit from FNAL g-2/EDM by a factor 20
- Still in a conceptual design phase, many challenges to face, a lot of room for new ideas and new contributions
- Close synergies with other activities at INFN Roma: MEG (physics, logistic), RD51-DRD1 (detectors, electronics), aMUSE (physics, beam studies)

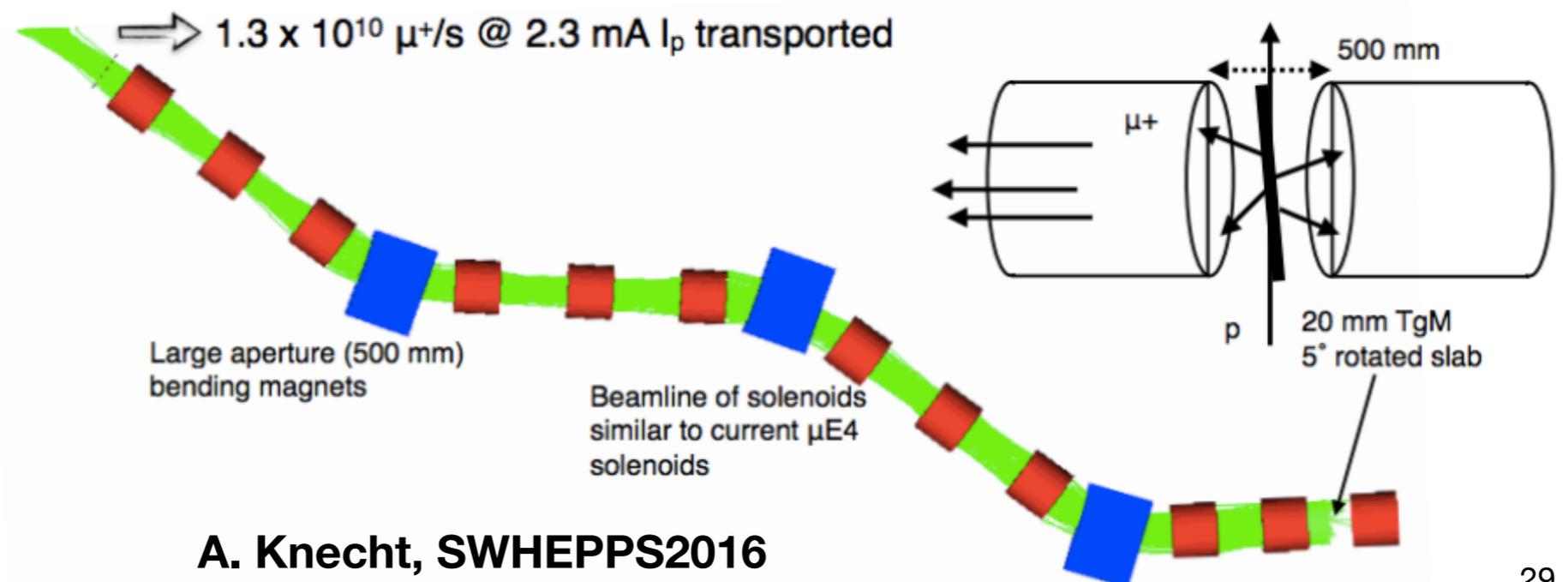
Backup

# The HiMB Project @ PSI

- PSI is designing a high intensity muon beam line (HiMB) with a goal of  $\sim 10^{10}$   $\mu$ /sec (x100 the MEG-II beam)
- Optimization of the beam optics:
  - improved muon capture efficiency at the production target
  - improved transport efficiency to the experimental area

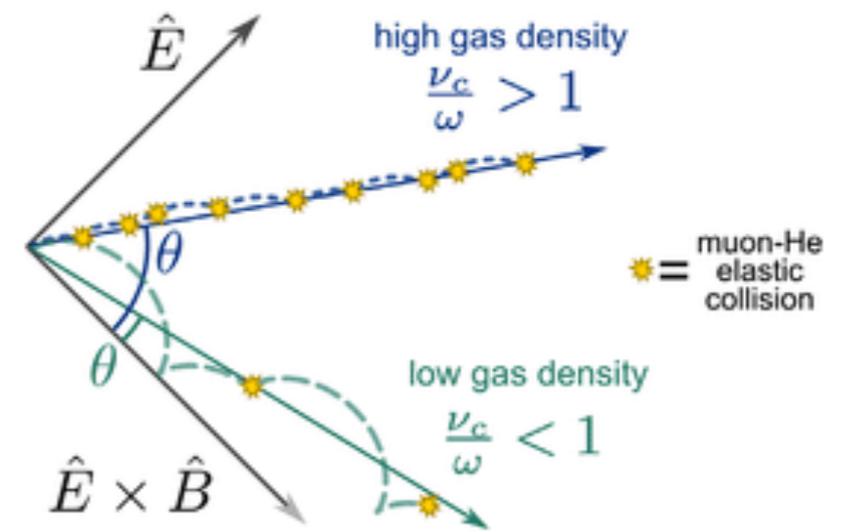
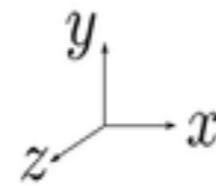
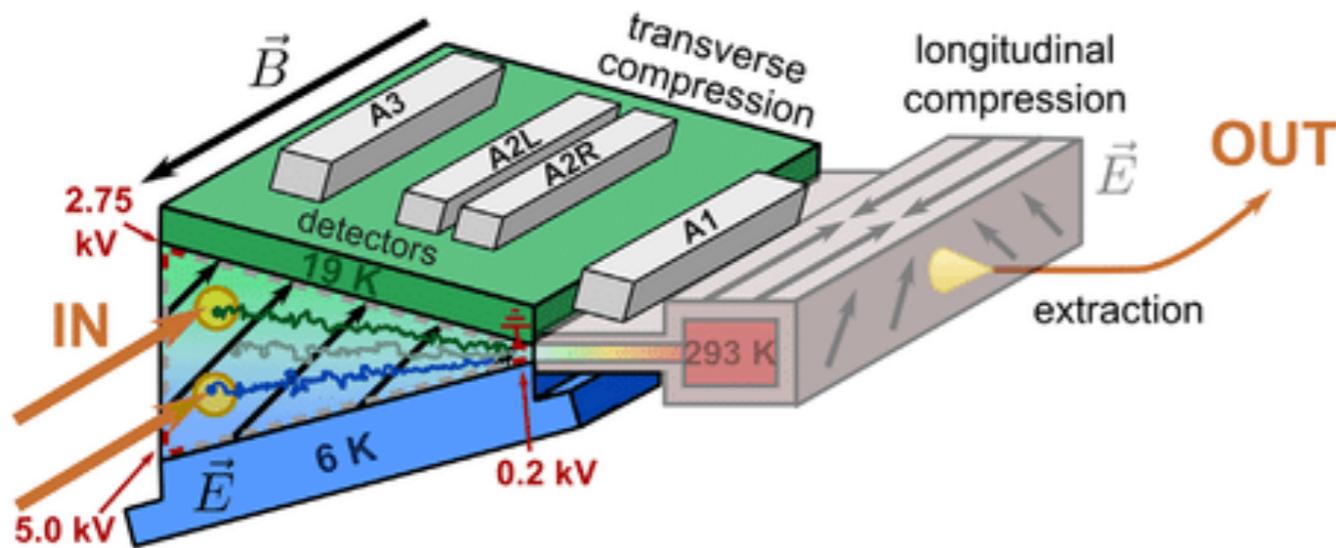
x4  $\mu$  capture eff.  
x6  $\mu$  transport eff.

**$1.3 \times 10^{10}$   $\mu$ /s**  
in the experimental area  
with 1400 kW beam power



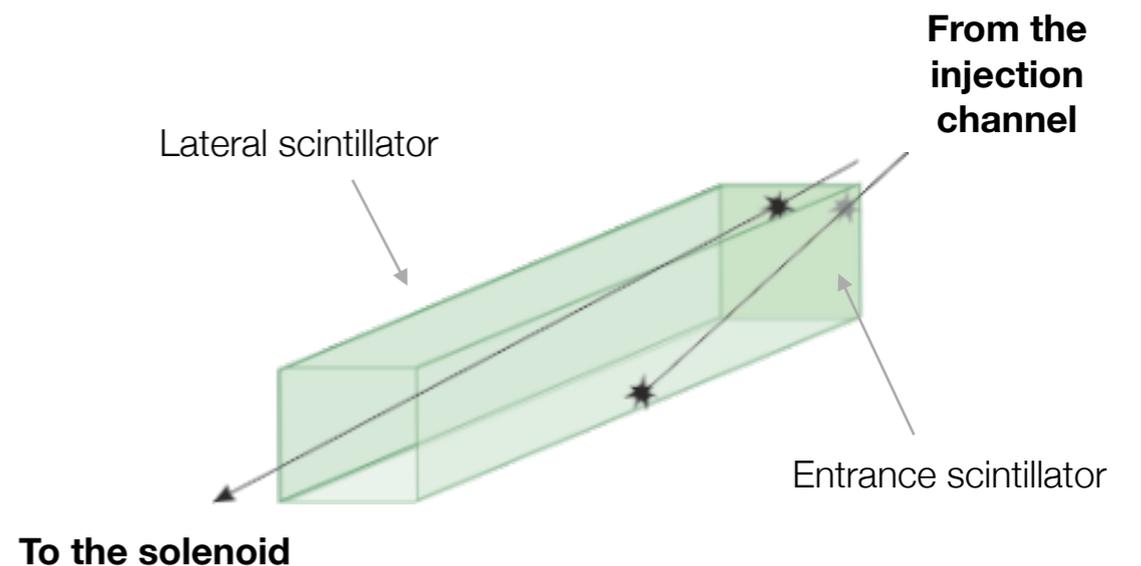
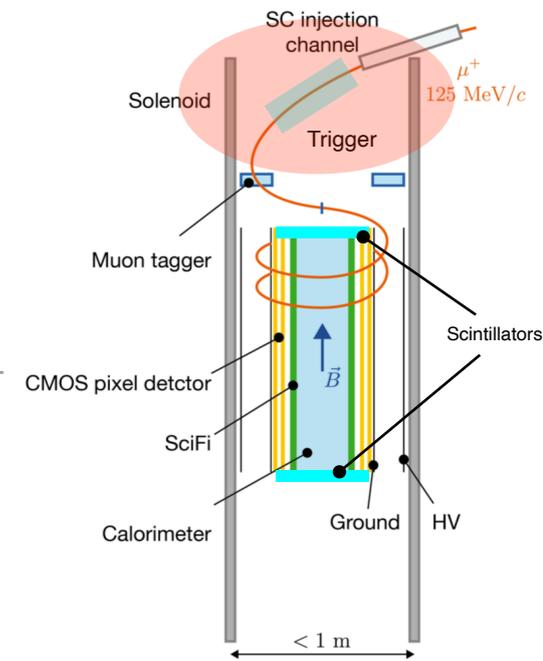
A. Knecht, SWHEPPS2016

# muCool



# The Detector — Entrance trigger

- A muon detector with reasonable timing performances ( $\sim$  ns) is needed at the entrance to:
  - set the  $T_0$  for the precession measurement
  - trigger the magnetic kick
  - start the measurement cycle
- $O(10$  MHz) muons pass the injection channel, only  $O(60$  kHz) are in a phase space region that allows the capture:
  - to avoid a large dead time, need to trigger only muons that can be captured

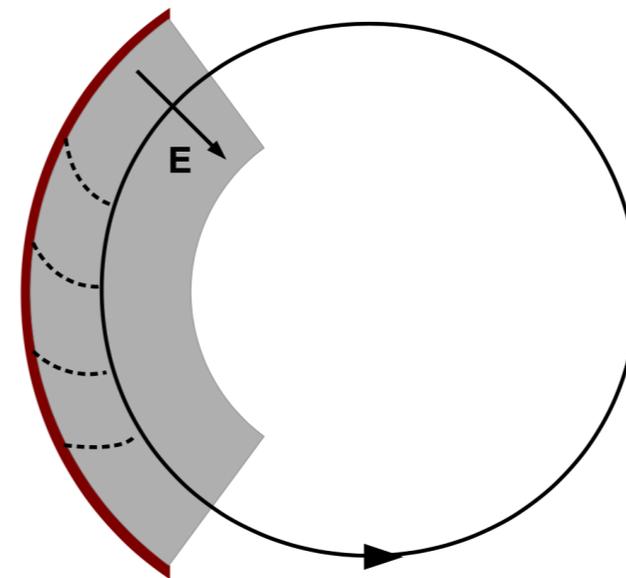
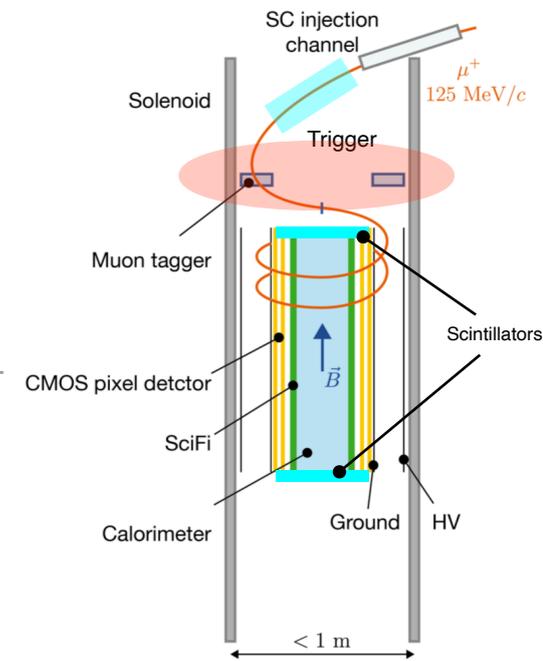


## Anti-coincidence between entrance and lateral scintillators

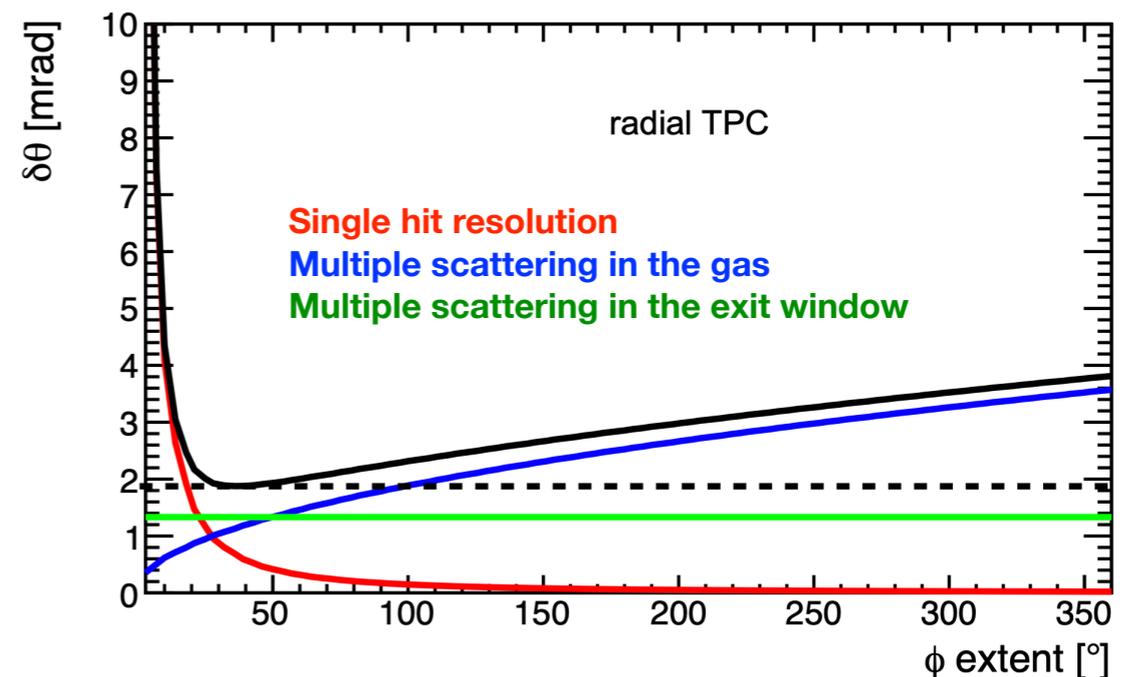
*Only muons on a trajectory close to the nominal one will be triggered*

# The Detector — Muon tagger

- Among triggered muons, there will be still some with a relatively large vertical angle in the measurement region
  - the measurement of the decay angle can be biased
- A muon tracker/tagger can identify such events for a proper treatment
  - needs  $\sigma(\theta) \sim 1$  mrad  $\rightarrow$  very precise and very light

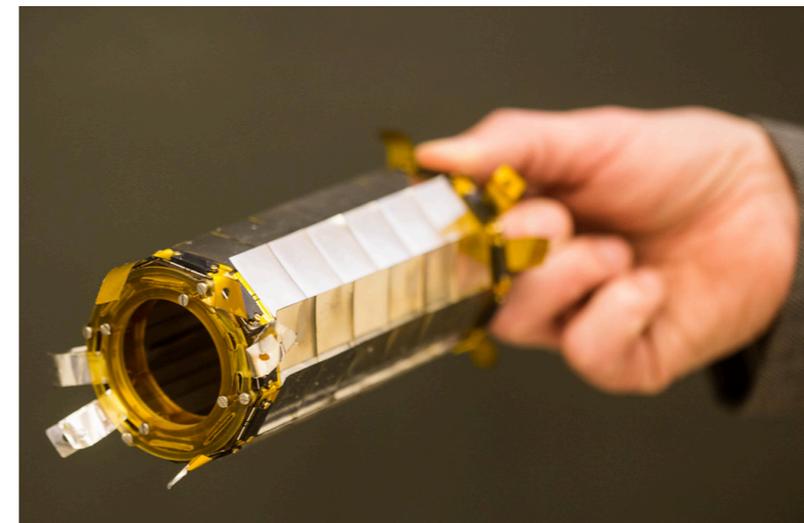
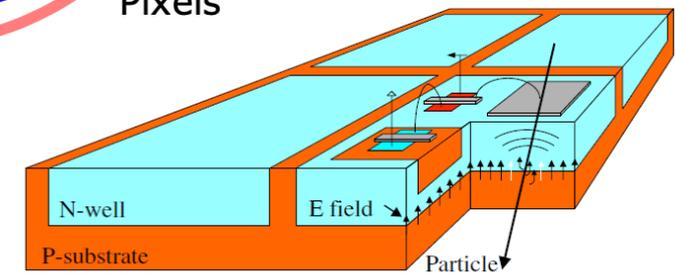
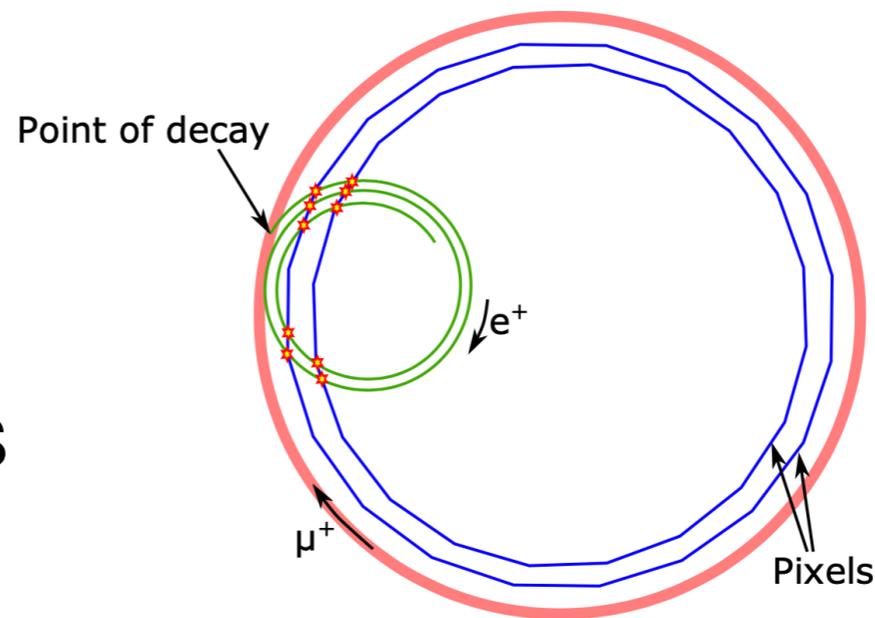
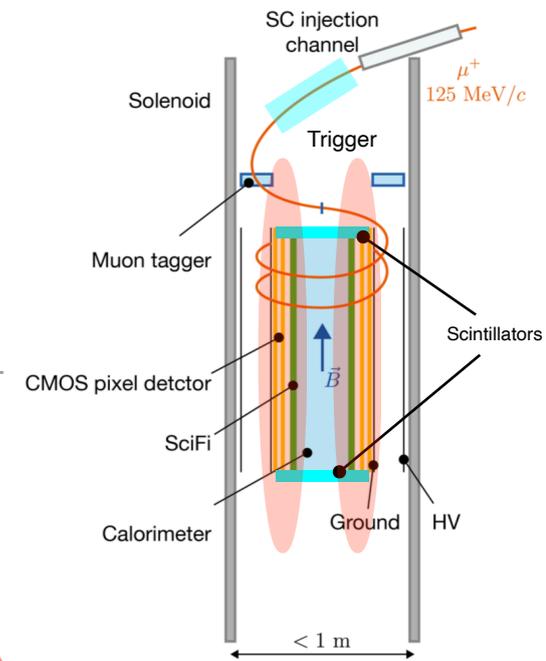


**MPGD-based radial TPC**



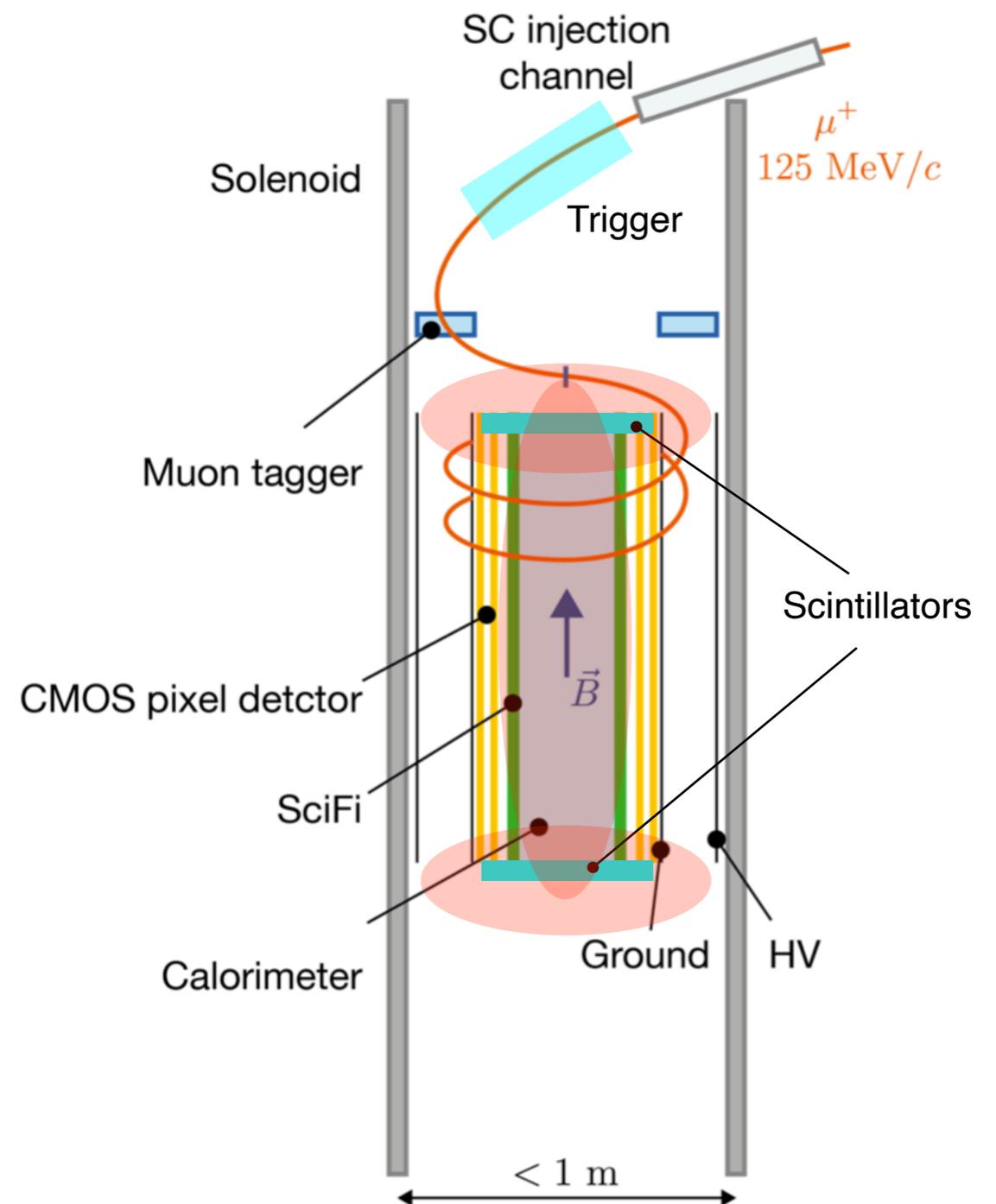
# The Detector — Positron tracker

- Silicon pixels (50  $\mu\text{m}$  DMAPS)
  - very good solution for low-momentum positrons
  - precise determination of the trajectory to determine the up/down asymmetry
  - Design derived from Mu3e ( $\mu^+ \rightarrow e^+e^+e^-$  @ PSI)



# The Detector — End signals

- The measurement has to be stopped as early as possible to allow a new entrance trigger and avoid dead time
- Stop signal should arrive when:
  - a positron from the muon decay is detected
  - the muon exits the measurement region
- Fast scintillators to:
  - measure the decay time
  - lift the veto for a subsequent entrance trigger
  - identify muons exiting the measurement region before decaying



# Systematic uncertainties

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- The main sources of systematic uncertainties were discussed in the paper by Farley *et al.*

1.  $B_r \neq 0$
2. Misalignment of B and E planes
3. Electric field not on a plane  $\rightarrow$  magnetic precession in the rest frame  $\rightarrow$  vertical precession in the lab frame
4. Residual (g-2) precession + locally non-horizontal orbit = vertical precession
5.  $B_\theta \neq 0$
6. Early-to-late detector effects

*Vertical orbit oscillations!  
Average to 0, but can deteriorate the  
quality of the asymmetry fit*

*Can be canceled by comparing  
**clockwise (CW)** and  
**counter-clockwise (CCW)**  
injection*

**CW vs. CCW**

+

*Single muon storage avoids high  
detector rates changing with time*

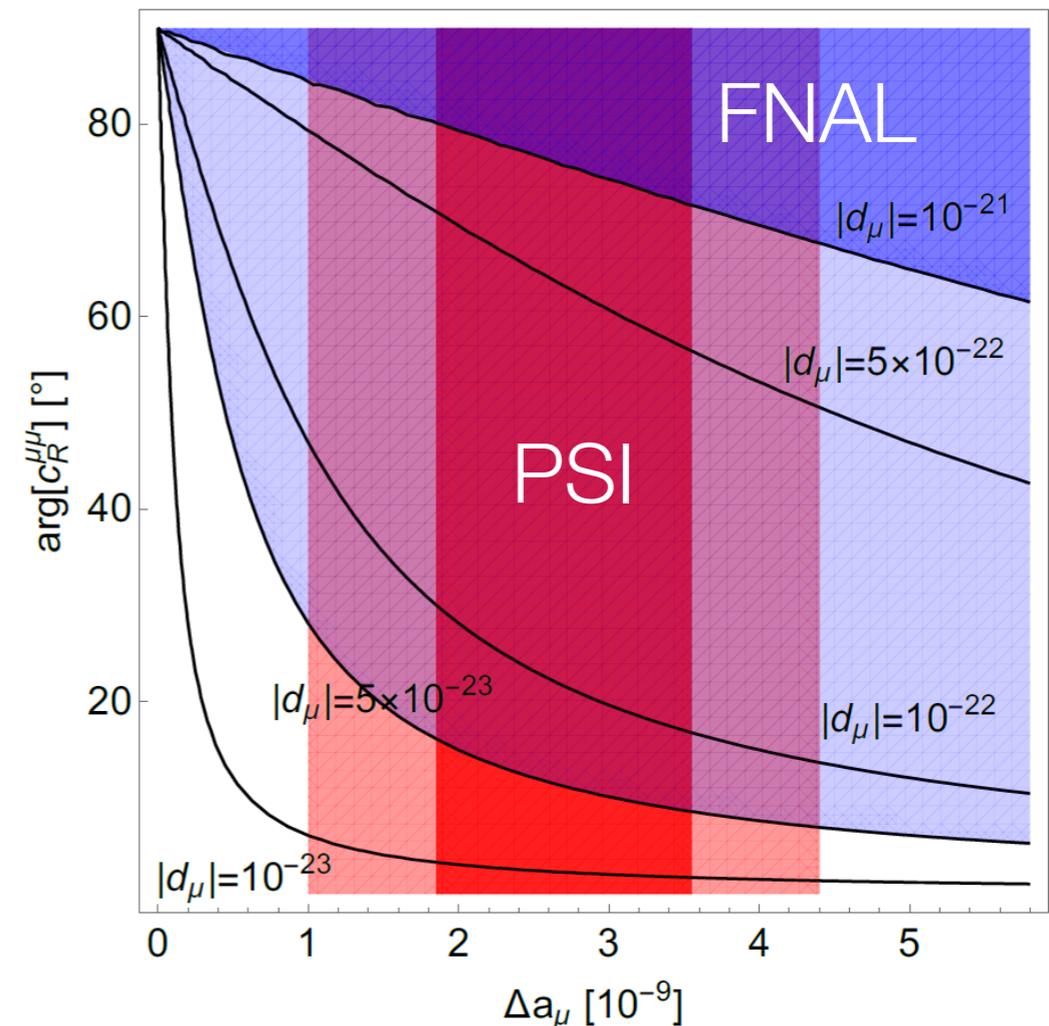
+

*injection effects measured without  
muons*

# Sensitivity and Physics reach (1 year run)

- $a = 1.12 \times 10^{-3}$
- $\gamma = 1.55$
- $P_0 = 0.93$
- $E = 2 \text{ MV/m}$
- $N = 50 \text{ MHz} \times 200 \text{ days} = 7 \times 10^{11}$
- $\tau = 2.2 \times 10^{-6} \text{ s}$
- $\alpha = 0.3$

$$\sigma(|d_\mu|) \approx \frac{a\hbar\gamma}{2P_0E_f\sqrt{N}\tau_\mu\alpha}$$



$$\sigma(|d_\mu|) \leq 6 \times 10^{-23} e \cdot \text{cm}$$