



Future Perspectives on Primordial Black Holes

Rome — 12 December 2023

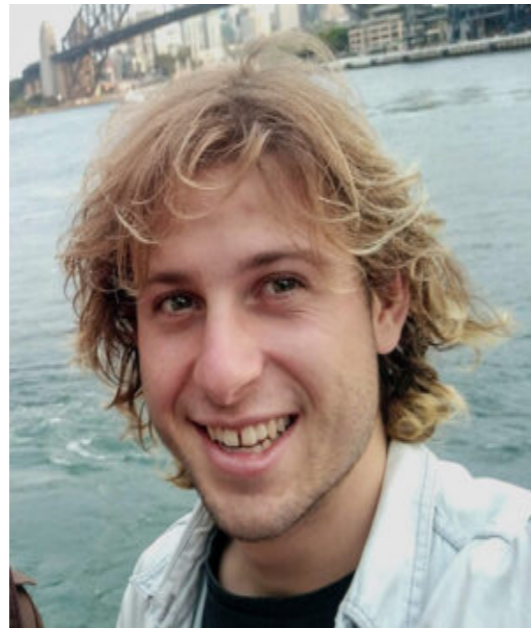
On the Cosmological Bound on Primordial Black Holes

MAURO VALLI

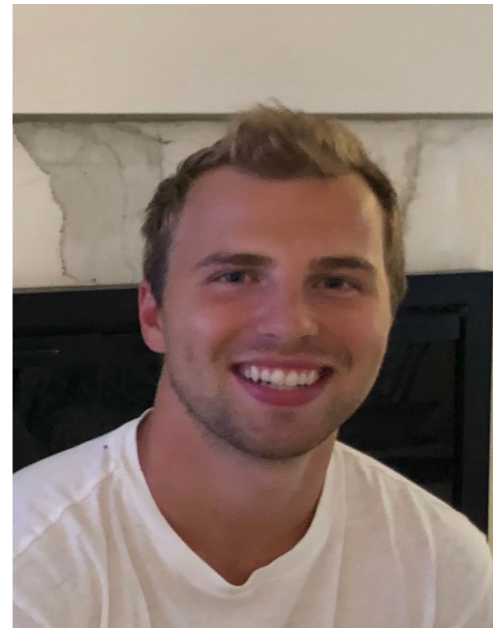
INFN Rome



*Réddite quae sunt
Caésaris Caésari*



Dominic Agius
IFIC / U. Valencia



Gregory Suczewski
YITP / Stony Brook U.

- + **Francesca Scarcella** (U. Montpellier, **NEXT SPEAKER**)
- + **Daniele Gaggero** (INFN Pisa) & **Rouven Essig** (YITP)

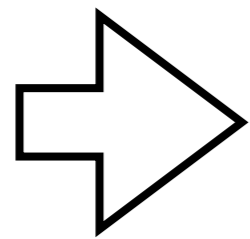
PBHs & Cosmo



Model of Inflation / Phase Transition such that:

$$\tau_{\text{fall}} \sim 1/\sqrt{4\pi G_N \delta\rho} < \tau_{\text{press}} \sim 1/(c_s H)$$

i.e., **overdense** region locally **revert expansion & collapse**



Non-standard power spectrum @ small scales!

— *Ann. Rev. Nucl. Part. Sci.* 70 (2020) 355-394 —

- COBE/FIRAS bound on CMB distortions $\rightarrow M_{\text{PBH}}/M_{\odot} \lesssim 10^5$
— *APJ* 758 (2012) 76 / *PRD* 90 (2014) 083514 —
- $P(\zeta)$ non-gaussian, PBHs induce DM isocurvature $\rightarrow |f_{\text{NL}}| \lesssim 10^{-3}$
— *PRD* 91 123534 (2015) / *JCAP* 1504 (2015) 034 —

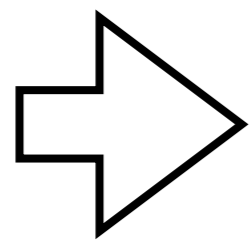
PBHs & Cosmo



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PBHs expected to evaporate due to Hawking radiation

$$T_{\text{BH}} = (8\pi G_N M_{\text{BH}})^{-1} \sim \left(\frac{10^{-10} M_{\odot}}{M_{\text{BH}}} \right) T_{\text{rec}}$$

- BBN & CMB constrain injection of high-energy particles in the plasma

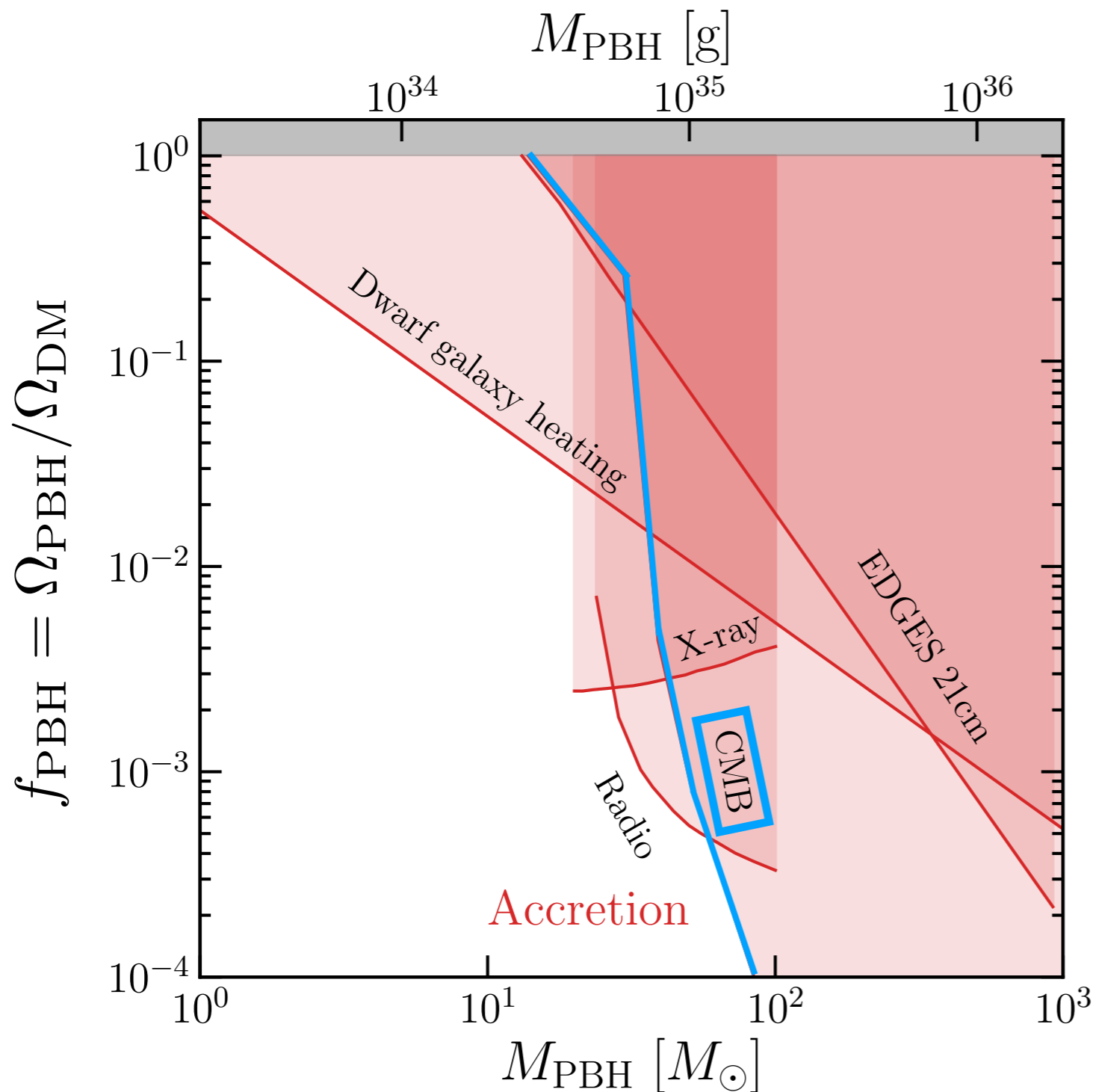
— *PRD 81 (2010) 104019 / PRD 102 (2020) 103512* —

- If $M_{\text{PBH}} \gtrsim 10^{-18} M_{\odot}$, $\tau_{\text{PBH}} \gtrsim 13.8$ billion yrs $\rightarrow f_{\text{PBH}} \equiv \frac{\Omega_{\text{PBH}}}{\Omega_{\text{DM}}} > 0$

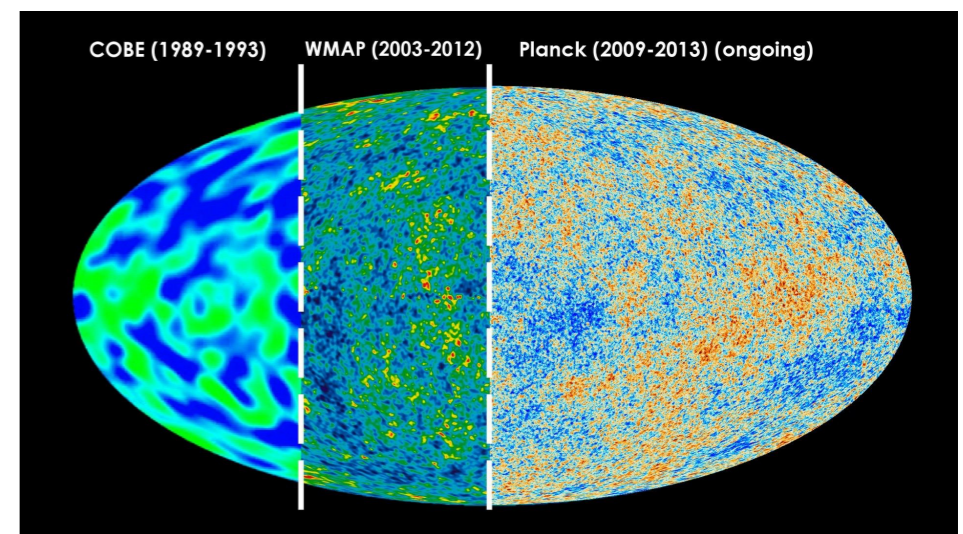
Focus of this Talk

PBHs of stellar masses can accrete matter \rightarrow energetic photon emission!

— *ApJ*. 680 (2008) 829 —



Cosmological bound
on *heavy* PBHs
largely dominated by

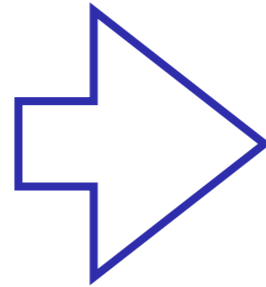


Q: CARVED IN STONE?

Physics of the Bound

Energy injection from exotica (PBHs)

$$\left. \frac{dE}{dV dt} \right|_{\text{inj.}}(z) \neq 0$$



Effective 3-level atom model

$$\begin{cases} \frac{dx_e}{dz} = \mathcal{C}_e[x_e, T_M] \\ \frac{dT_M}{dz} = \mathcal{C}_M[x_e, T_M] \end{cases}$$

Line-of-sight sol. of Boltzmann hierarchy affected mainly via alteration of:

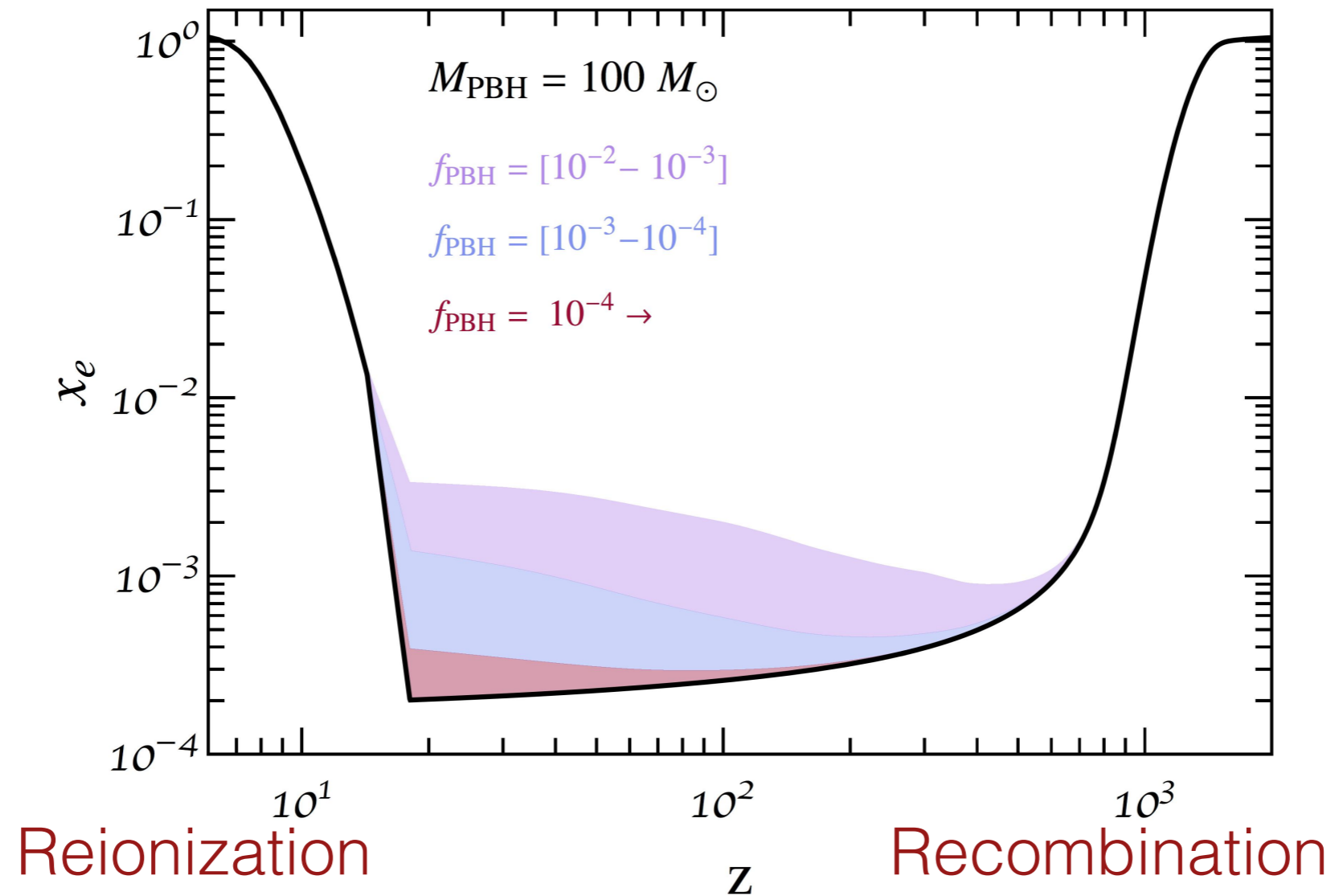
$$\tau(z) = \int_0^z n_H(z') x_e(z') \sigma_T \frac{dt}{dz'} dz' \quad \text{Thompson Optical Depth}$$

$$v(z) = \left| \frac{d\tau}{dz} \right| \exp(-\tau) \quad \text{Visibility Function}$$

CMB vs PBHs

PBHs messing up $X_e = n_e/n_H$ from “rec” to “rein” (effects also on T_M)

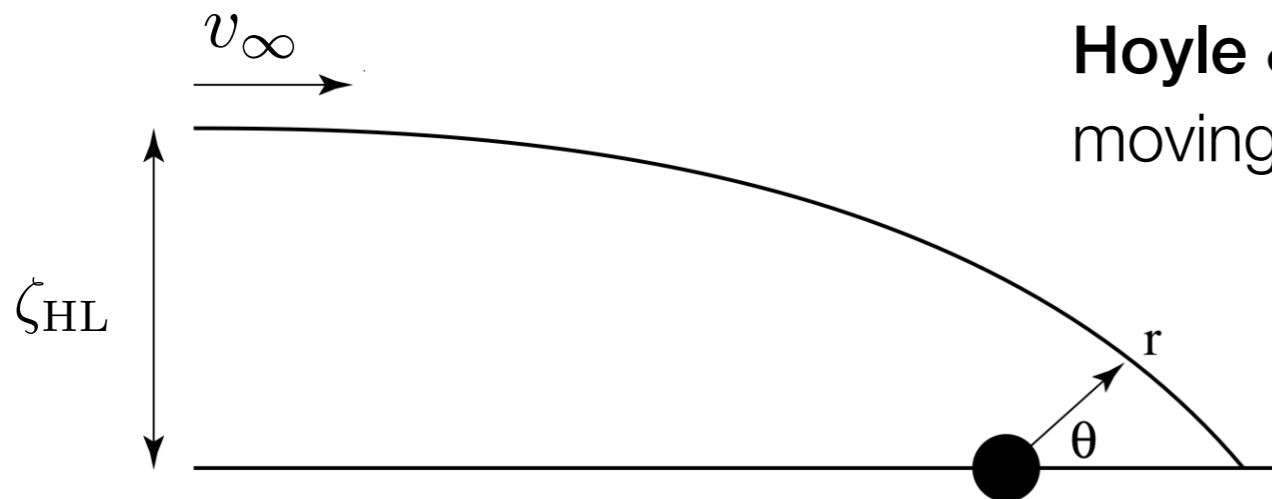
— *Phys.Rev.D 100 (2019) 043540* —



ON CMB: late “rec” (peaks shift in C_{ℓ}^{TT}) + early “rein” (extra bump in C_{ℓ}^{EE})

— *JCAP 1703 (2017) 043* —

Accretion I01

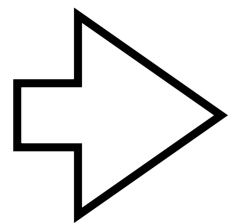


Hoyle & Lyttleton: accretion by a point-like mass M moving at a steady speed through infinite gas cloud.

Material will be accreted if following satisfied:

$$\frac{1}{2}v_{\infty}^2 < \frac{G_N M}{r} \Leftrightarrow \zeta < \zeta_{\text{HL}} \equiv \frac{2G_N M}{v_{\infty}^2}$$

— JCAP 1703 (2017) 043 —



ACCRETION RATE: $\dot{M}_{\text{HL}} = \pi \zeta_{\text{HL}}^2 v_{\infty} \rho_{\infty} = \frac{4\pi G_N^2 M^2 \rho_{\infty}}{v_{\infty}^3}$

Bondi generalization of **HL** result (**BHL**):

which matches up to a fudge factor λ the original HL rate as sound speed c_s of medium becomes negligible.

$$\dot{M}_{\text{BHL}} = \lambda \frac{4\pi G_N^2 M^2 \rho}{v_{\text{eff}}^3}$$

OBS.

λ tuned to observations (neutron stars, SMBH, AGNs)

— ρ = density of the medium

— $v_{\text{eff}} = \sqrt{v_{\text{rel}}^2 + c_s^2}$

Disc or Not Disc



$$L \lesssim \dot{M}$$

NOT ALL POTENTIAL ENERGY
GOES INTO RADIATION!

IN 4π APPROX., SOME ANALYTIC RESULTS:

$$10^{-5} L_{\text{Edd}}/\dot{M} \lesssim \epsilon \equiv L/\dot{M} \lesssim 10^{-3} L_{\text{Edd}}/\dot{M}$$

— PRD 95 (2017) 043534 —

VS



MORE REALISTICAL CASE, DISC ACCRETION ...

— PRD 96 (2017) 8 083524 —

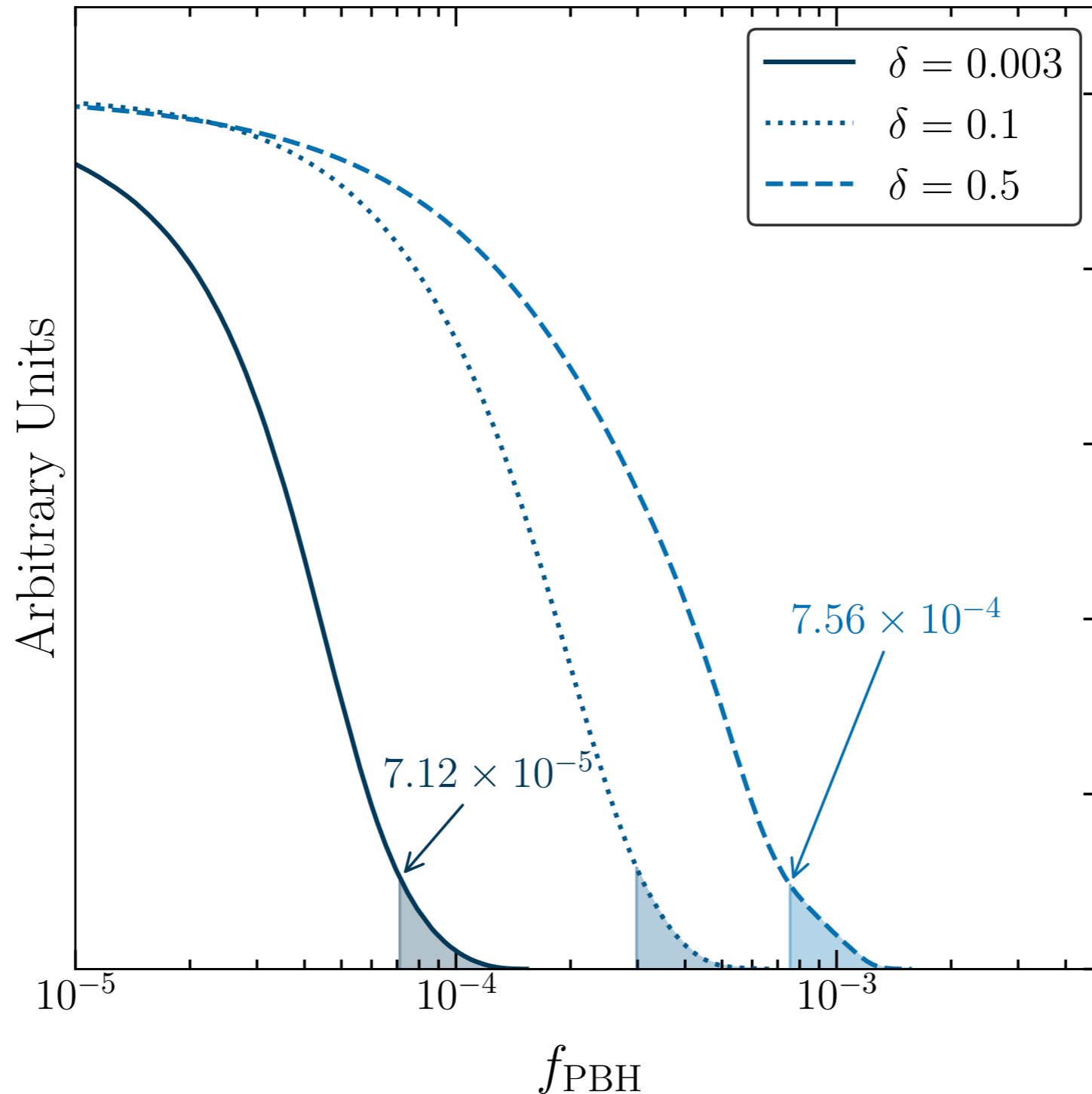
ADVECTION DOMINATED ACCRETION FLOW (ADAF)

BOLOMETRIC EFFICIENCY MAINLY SET BY

$\delta = \% \text{ OF IONS INTERACTING W/ LEPTONS}$

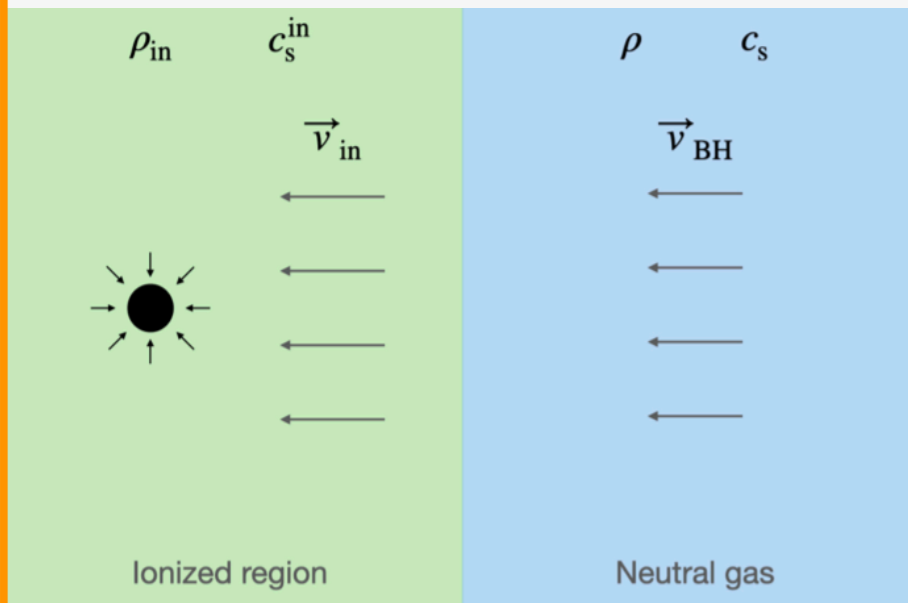
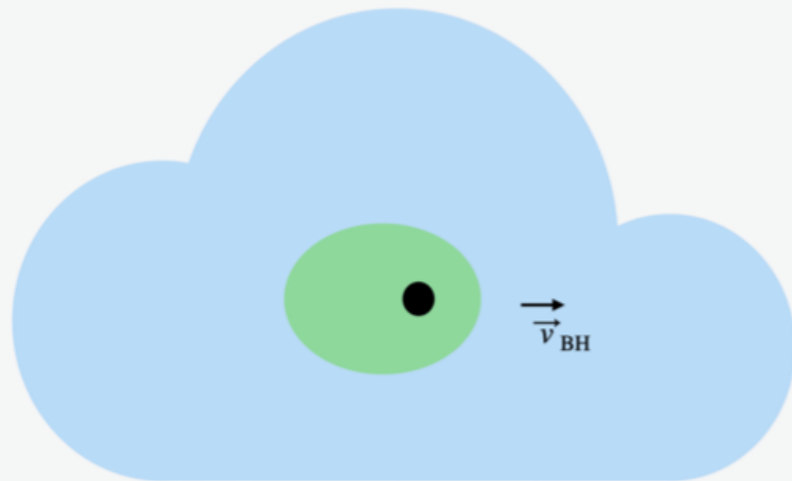
Focus #1

Role of the disc impacts accretion \rightarrow one order of magnitude on f_{PBH} !



Beyond BHL

F. Scarcella — *Ph.D. thesis*



- BHL holds within ionized bubble
- Euler's eq.s link the two regions

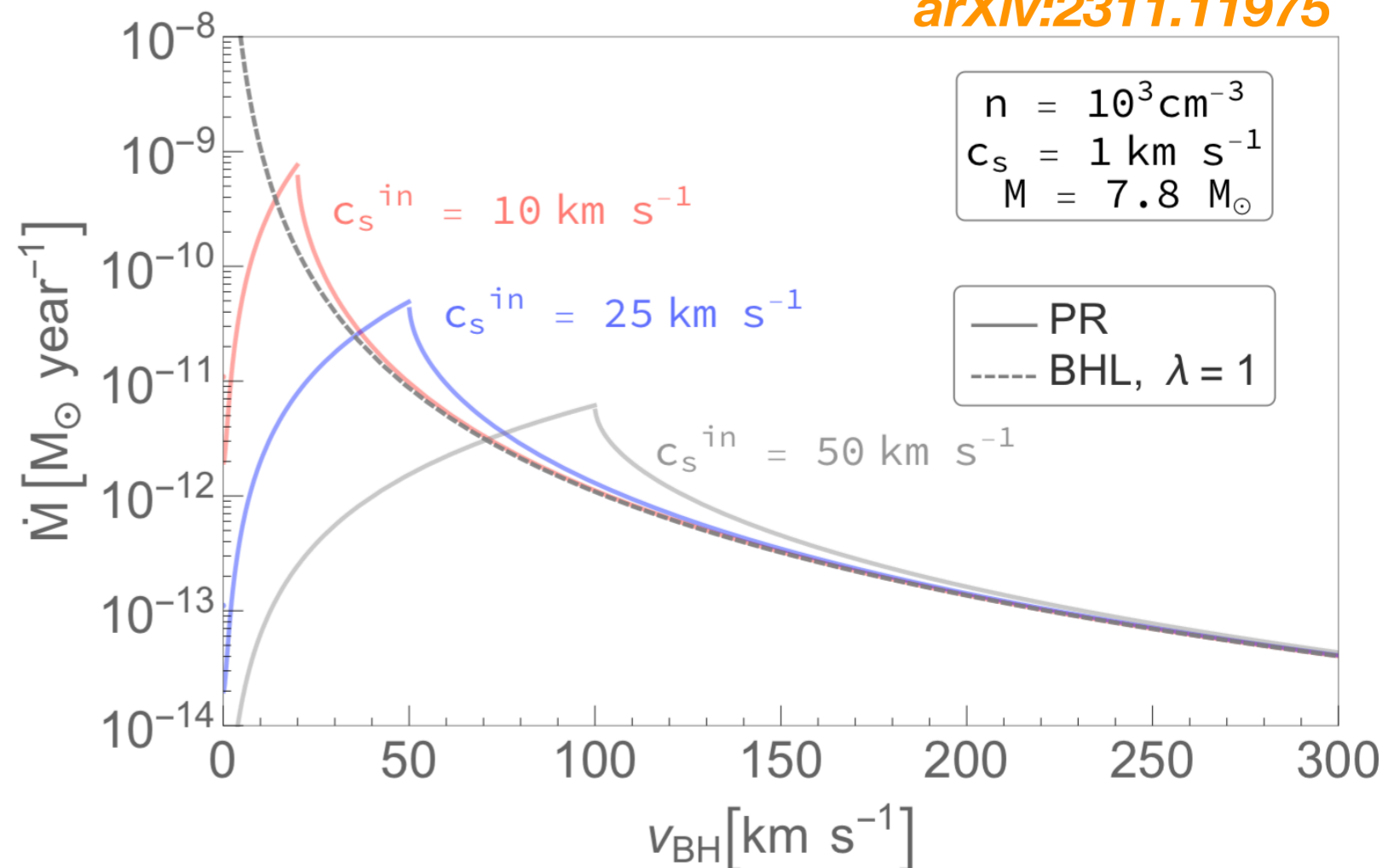
Park & Ricotti (PR13): hydro sim.s show ionizing effect of radiation emitted during accretion process.

— **APJ 767 163 (2013)** —



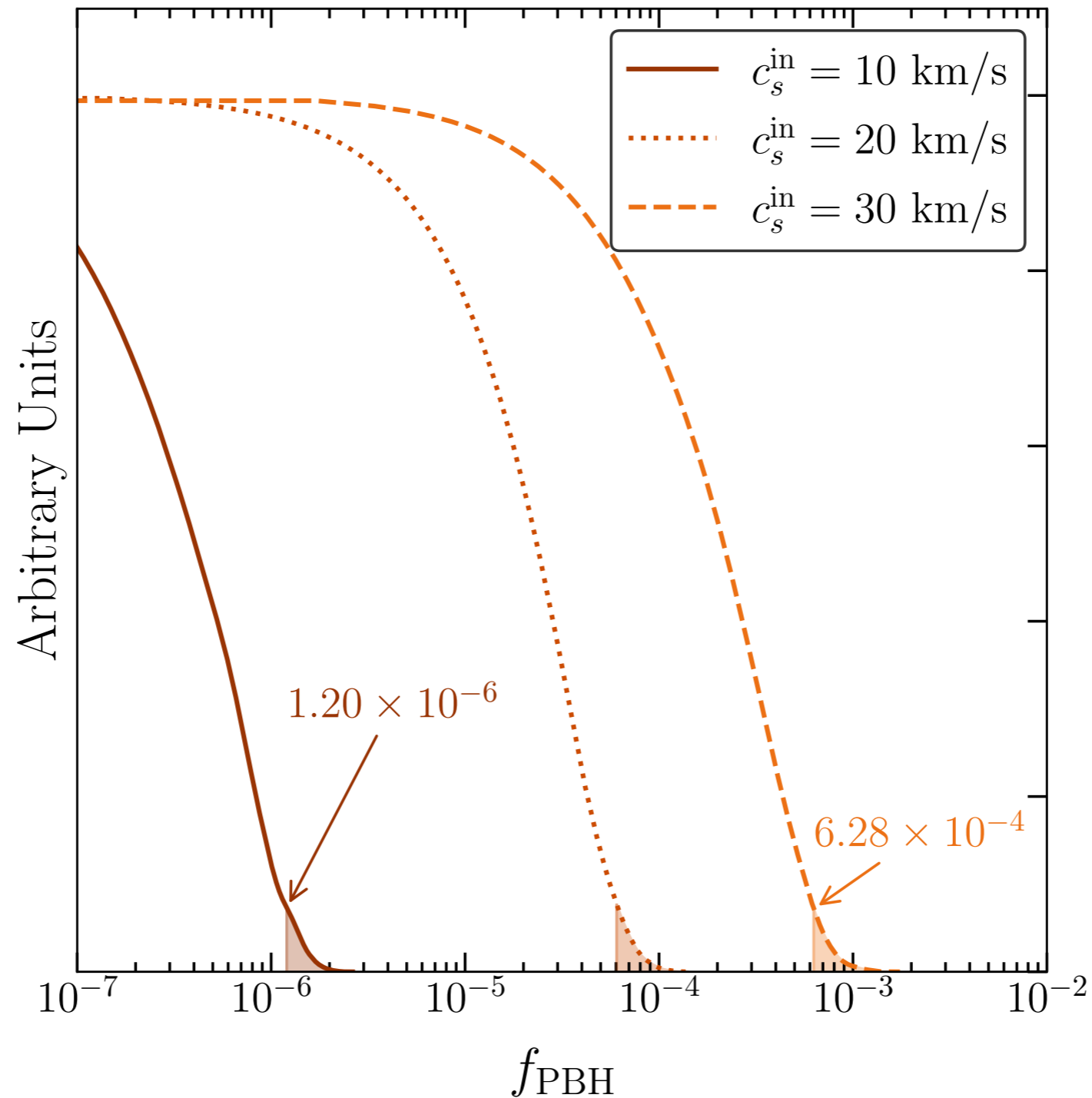
Non-negligible radiative feedback makes accretion rate less efficient at low v_{rel}

arXiv:2311.11975



Focus #2

The inner speed of sound in PR13 accretion model is a key parameter!

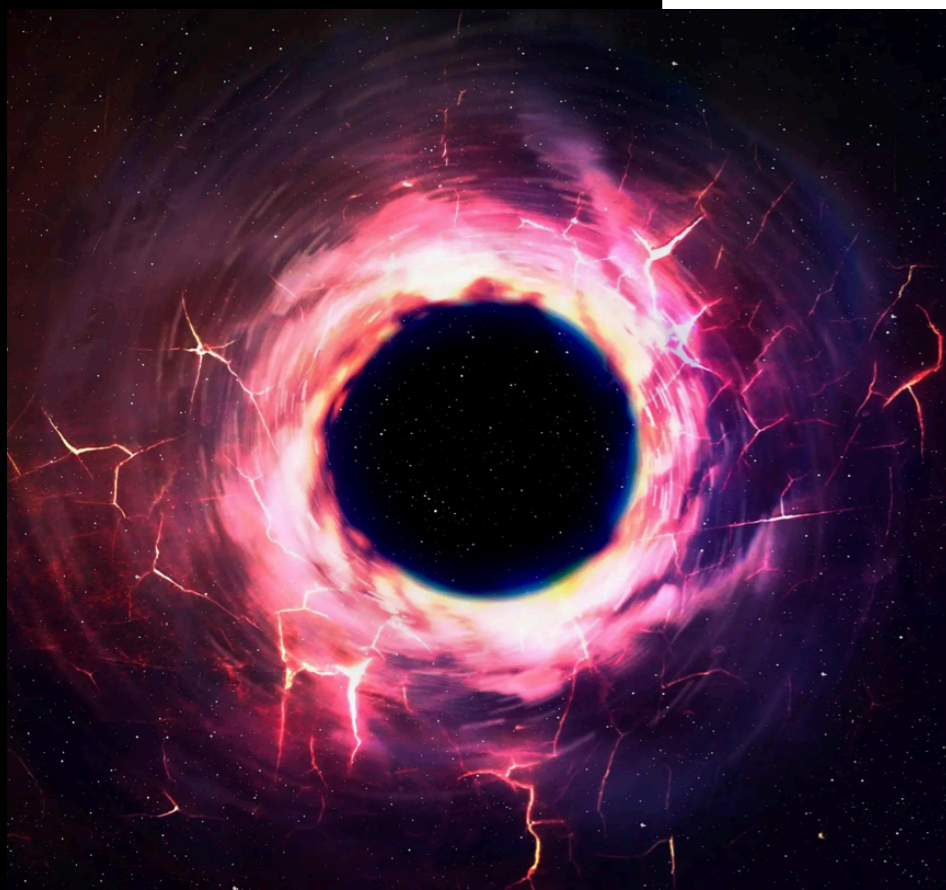


Do not forget about DM

Breakthrough Study Confirms Hypothesis of Density Spike of Dark Matter Near Black Holes

Guardian mag © June 09, 2023

Guardian Mag



— APJL 943 (2023) L11 —

$$f_{\text{PBH}} \ll 1 \Rightarrow \text{DM} \neq \text{PBH around!}$$

A GRAVITATIONALLY BOUND DM HALO IS EXPECTED TO FORM AROUND PBHS

EDUCATED GUESS

FREE-FALLING BARYONIC MATTER INTO PBH FEELS A DEEPER POTENTIAL WELL

$$\dot{M} \sim \zeta_{\text{eff}}^2 v_{\text{eff}} \rho$$

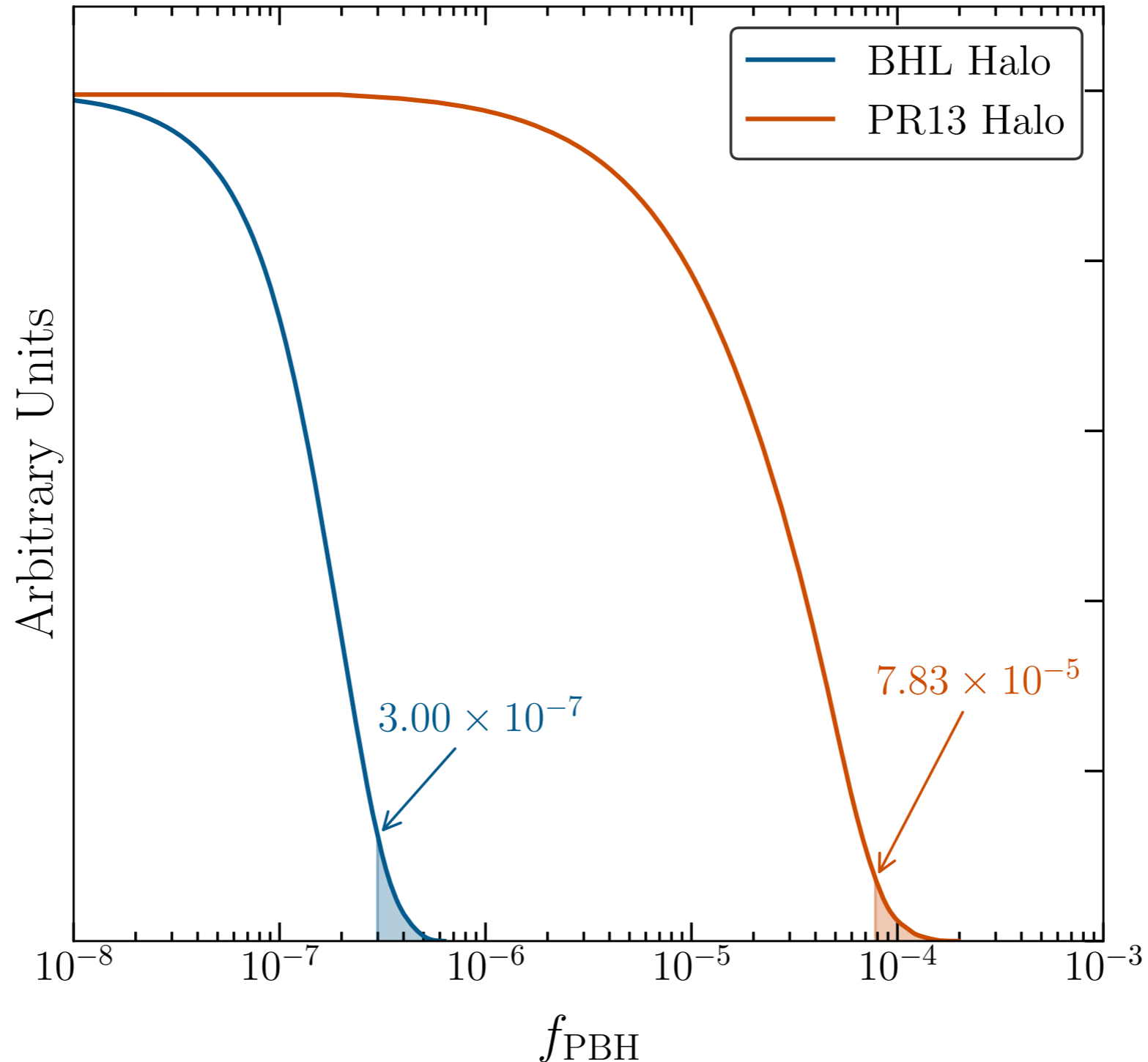
$$\frac{G_{\text{N}} M_{\text{PBH}}}{\zeta_{\text{eff}}} - \Phi_{\text{DM}} = v_{\text{eff}}^2$$

EFFECT APPRECIABLE PHENOMENOLOGICALLY FOR BHL MODEL, NOT FOR PR13 ACCRETION

D.Agius, G.Suczewski, et al. — TO APPEAR SOON

Focus #3

The impact of DM halo is intimately related to the underlying accretion model !



A “standardized” recipe

- Modify your **favorite Boltzmann solver** to include extra energy injection

CAMB / **CLASS** https://github.com/lesgourg/class_public

- 1 — Implement a “realistic” accretion model for PBHs (i.e., also **emitted spectrum**)

Ann.Rev.Astron.Astrophys. 52 (2014) 529

- 2 — Model **baryon - PBH relative vel.** from “rec” to “rein” & average over it

Linear theory usually assumed: $\langle v_{rel} \rangle = \min[1, (1+z)/10^3] \times 30 \text{ km/s}$

- 3 — Translate energy injection rate into energy deposition rate via:

* Semi-analytic approach

PRD 95 (2017) 043534

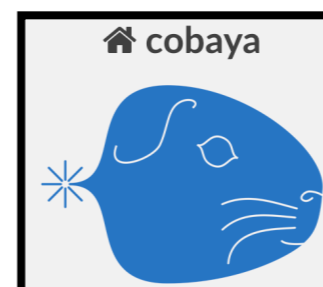
* Tabulated transfer functions

PRD 87 (2013) 123513

- Adopt << **best dataset** >> & your **favorite sampler** for Bayesian inference

ACT + SPT latest release
BAO consensus likelihood
Planck ‘18 TTTEEE + lens

Cobaya / Monte Python

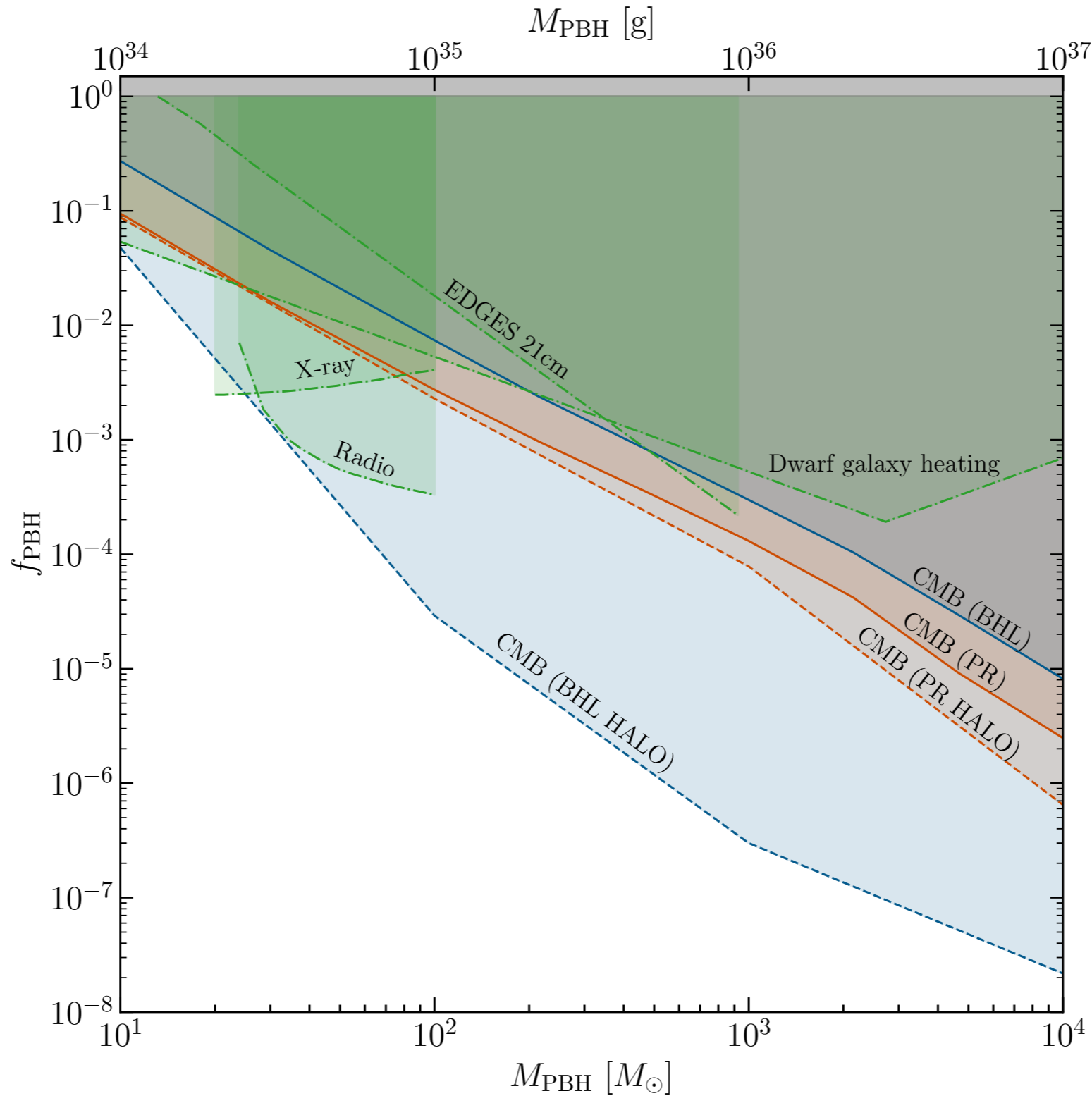


<https://github.com/CobayaSampler/cobaya>



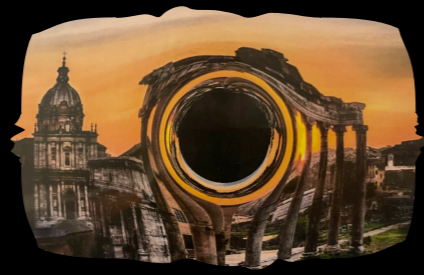
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*D. Agius,
G. Suczewski,
D. Gaggero,
F. Scarcella,
R. Essig & MV*

CMB (PR13) IN AGREEMENT WITH WHAT RECENTLY DERIVED IN **PRD 107 (2023) 043537**



Take Home

- CMB \longleftrightarrow sensitive probe of PBHs as (a fraction of) DM, f_{PBH}

— ACCRETION OF MATTER DOES MATTER —
ESPECIALLY W/ DARK MATTER

$$f_{\text{PBH}} \lesssim 10^{-7} \text{ @ } 95\% \text{ (BHL+DM halo)}$$

$$f_{\text{PBH}} \lesssim 10^{-4} \text{ @ } 95\% \text{ (PR13+DM halo)}$$

— from CMB + BAO for $M_{\text{PBH}}/M_{\odot} = 10^3$ —

- CMB ruling out $f_{\text{PBH}} > 1\%$ for $M_{\text{PBH}}/M_{\odot} > 10^2$ still very true

WHAT'S NEXT

- * Baryon - PBH velocity beyond linear theory
- * Role of PBH mass function & merger history