

HIGH-QUALITY POLARISED ELECTRON BUNCHES FROM COLLIDING PULSE INJECTION

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Spin-polarised electron beams find widespread use

Compact source of polarised electrons could spark innovation and progress in many fields

- > Polarised electron beams extensively used for
 - > Material science
 - > Atomic, molecular physics
 - > Nuclear physics
 - > Particle physics
- > Polarised electron beams can generate polarised photon and positron beams
- > Longitudinal spin of main interest in high energy physics
- > Also: polarisation important for fusion!

$$P = \frac{N_{\uparrow} - N_{\downarrow}}{N_{\uparrow} + N_{\downarrow}}$$

$$P_{\kappa} = \frac{1}{N} \sum_i^N \vec{S}_{\kappa,i}$$

Conventional spin polarised electron sources

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Electrons align spin opposite to B-field

$$U_{mag} = -\vec{\mu} \cdot \vec{B}$$

Used at storage rings

Relaxation time ~hours

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Polarised atoms of the photocathode material

Guns used at many facilities

Limited peak current

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Spin rotators (3)

Rotate spin from longitudinal to transverse

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(2) Pierce et al, *APL* **26** 670 (1975)

(3) Moffeit et al, SLAC-TN-05-045

Advanced sources of spin polarised electron beams

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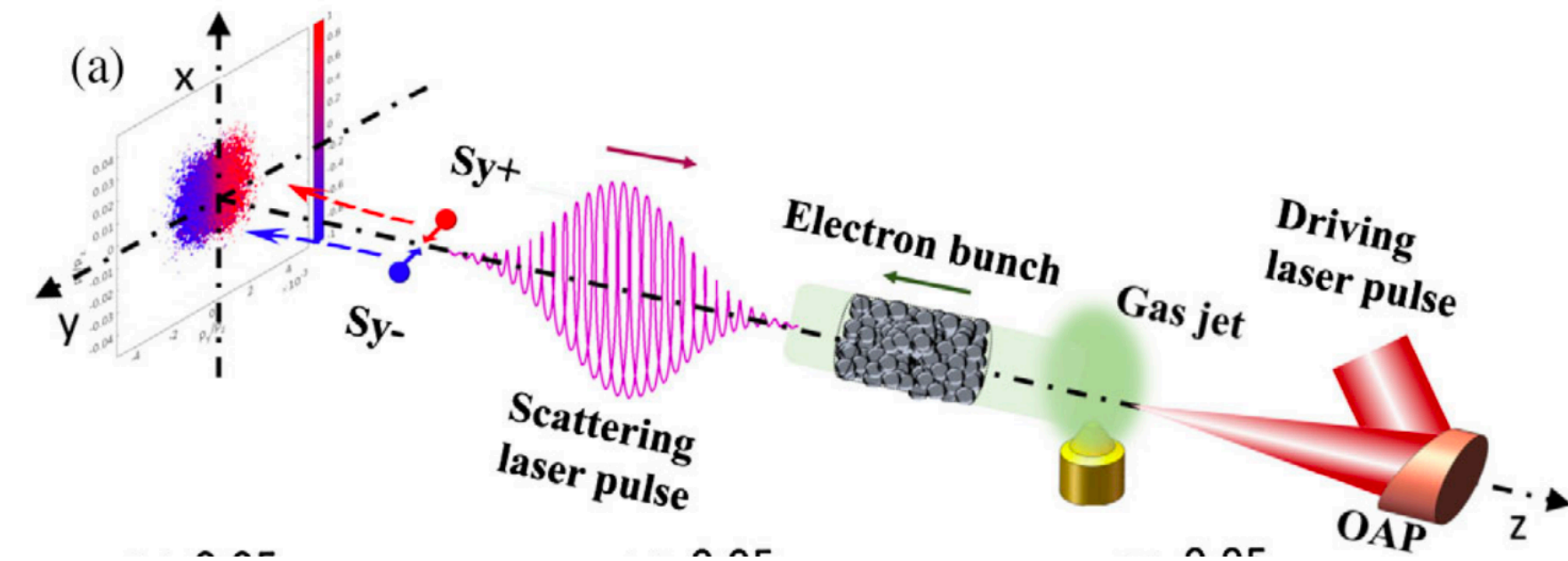
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 - > Sokolov-Ternov in colliding laser fields (4)



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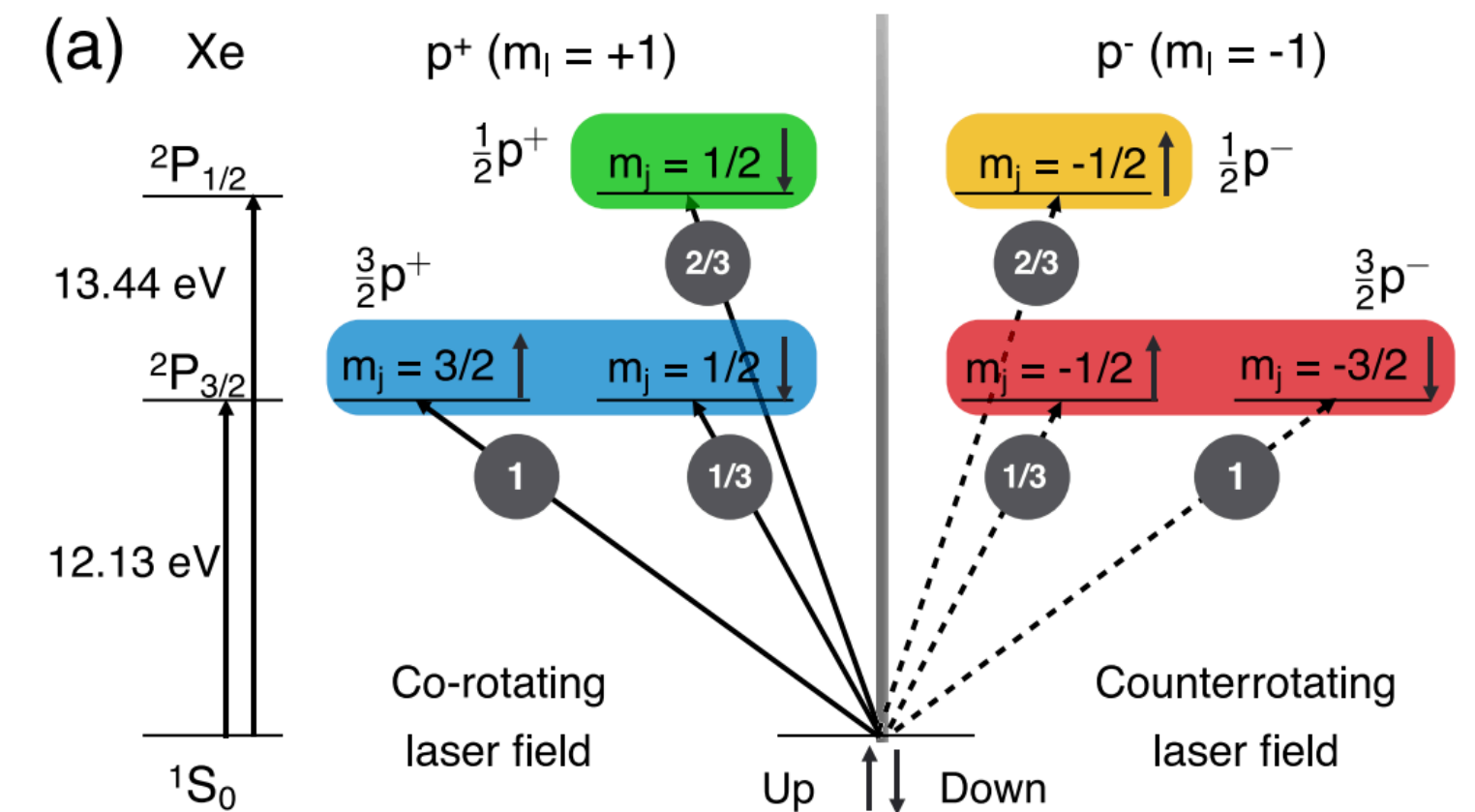
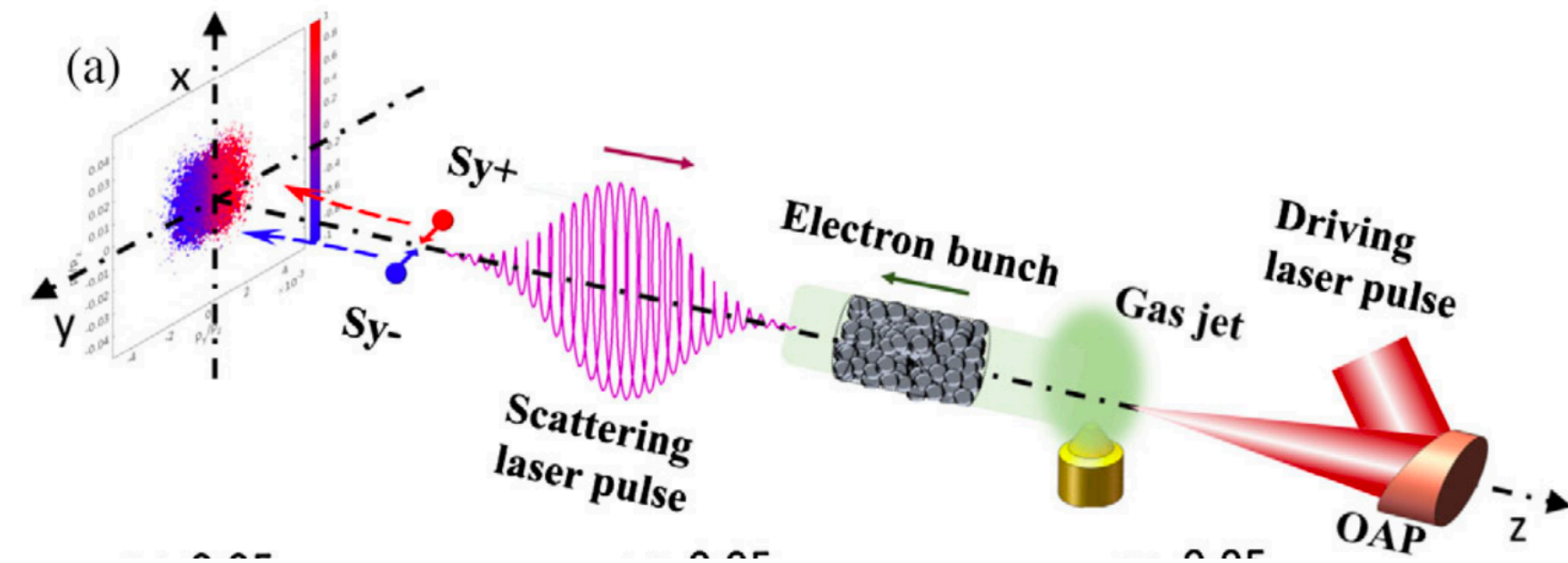
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- > **Plasma-based methods**
 - > Selective multi-photon ionisation (5)
 - > Pre-polarised plasma sources (6-9)



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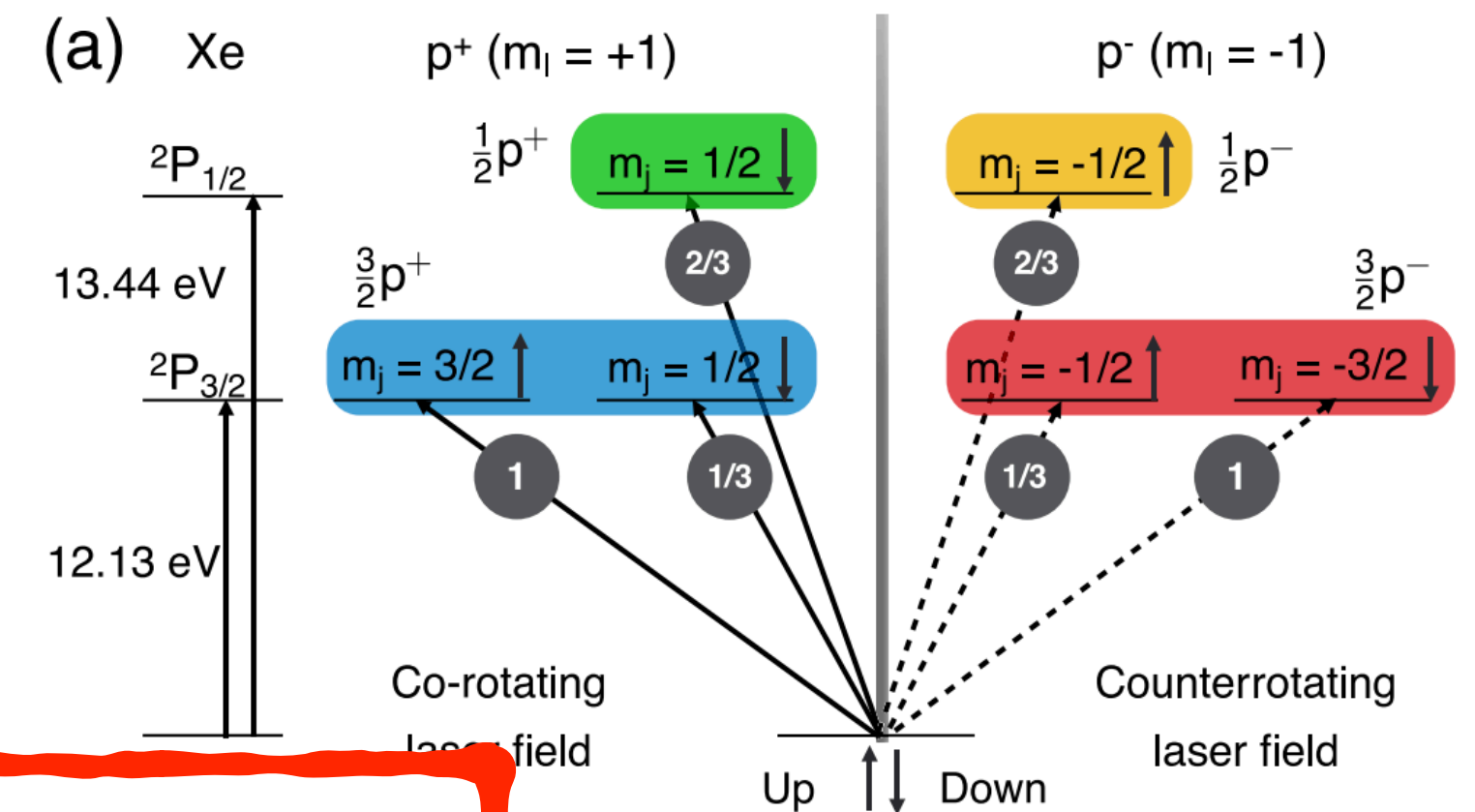
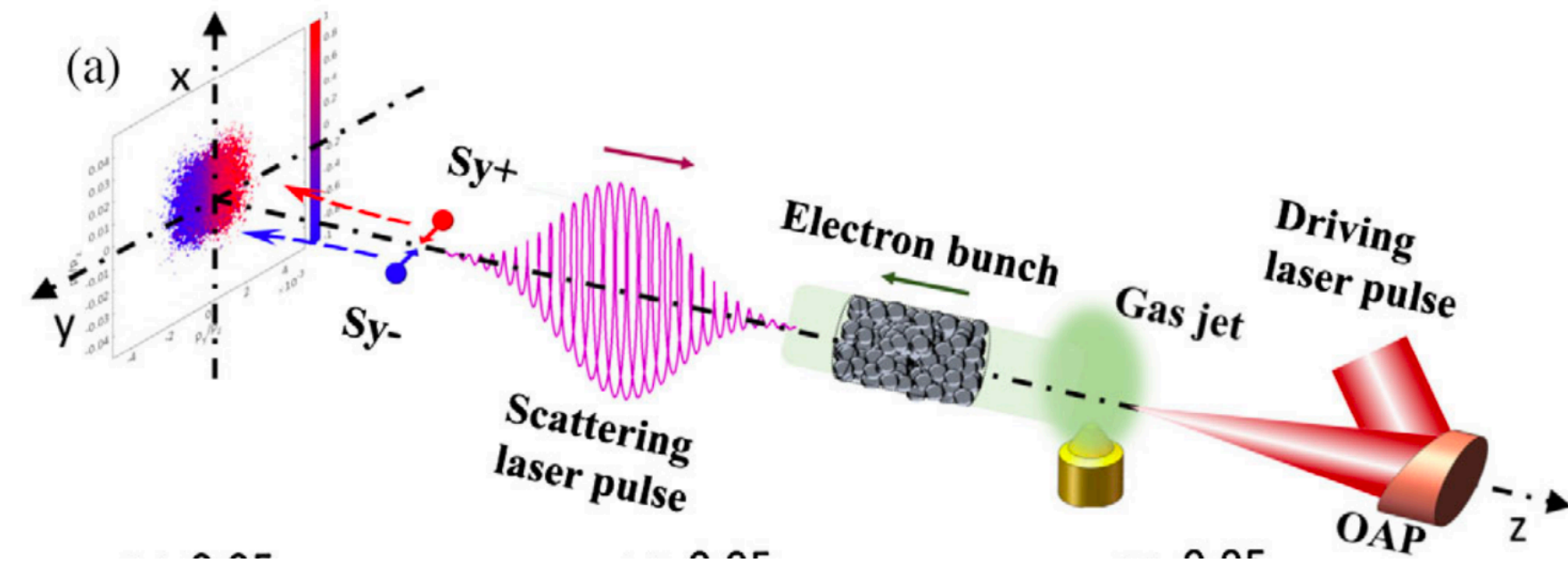
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No experimental demonstrations yet!

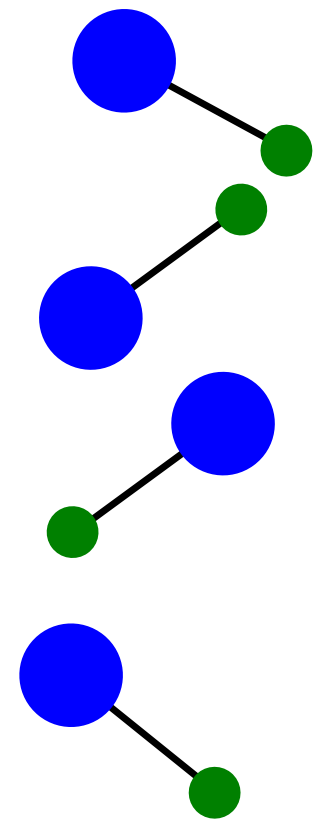
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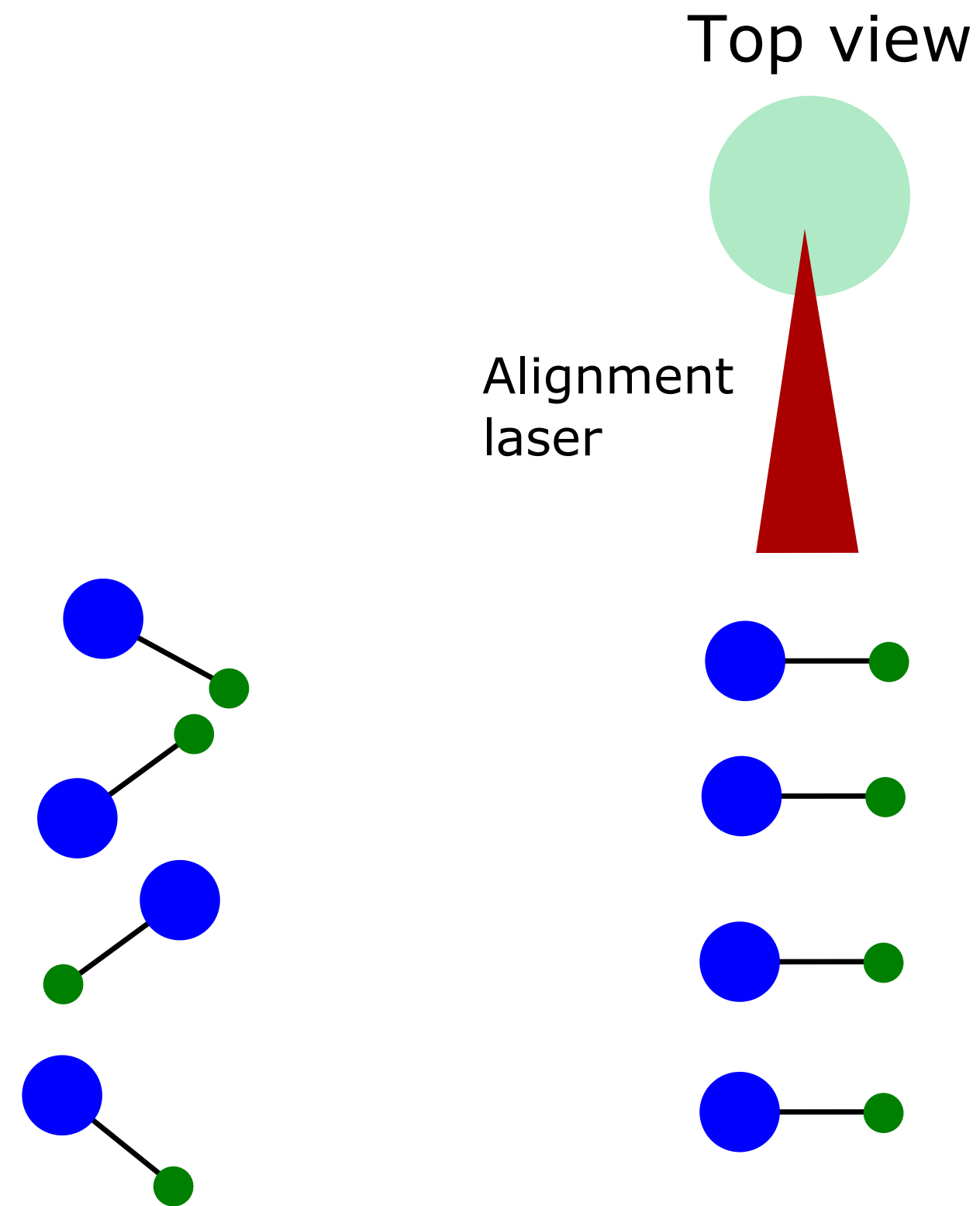
Concepts for pre-polarised plasma sources are available

Laser-based generation of spin-aligned atoms through dissociation of halide molecules



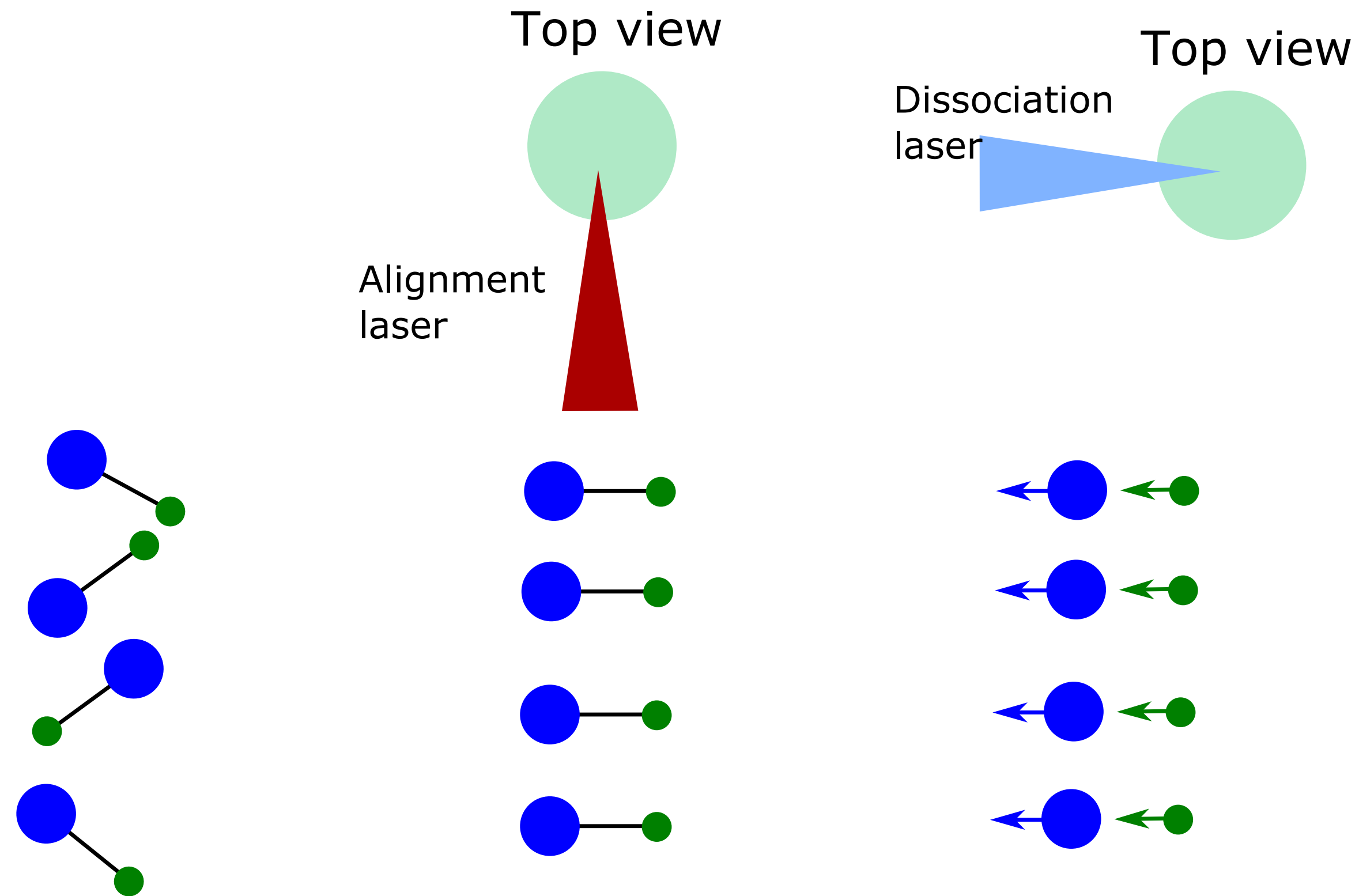
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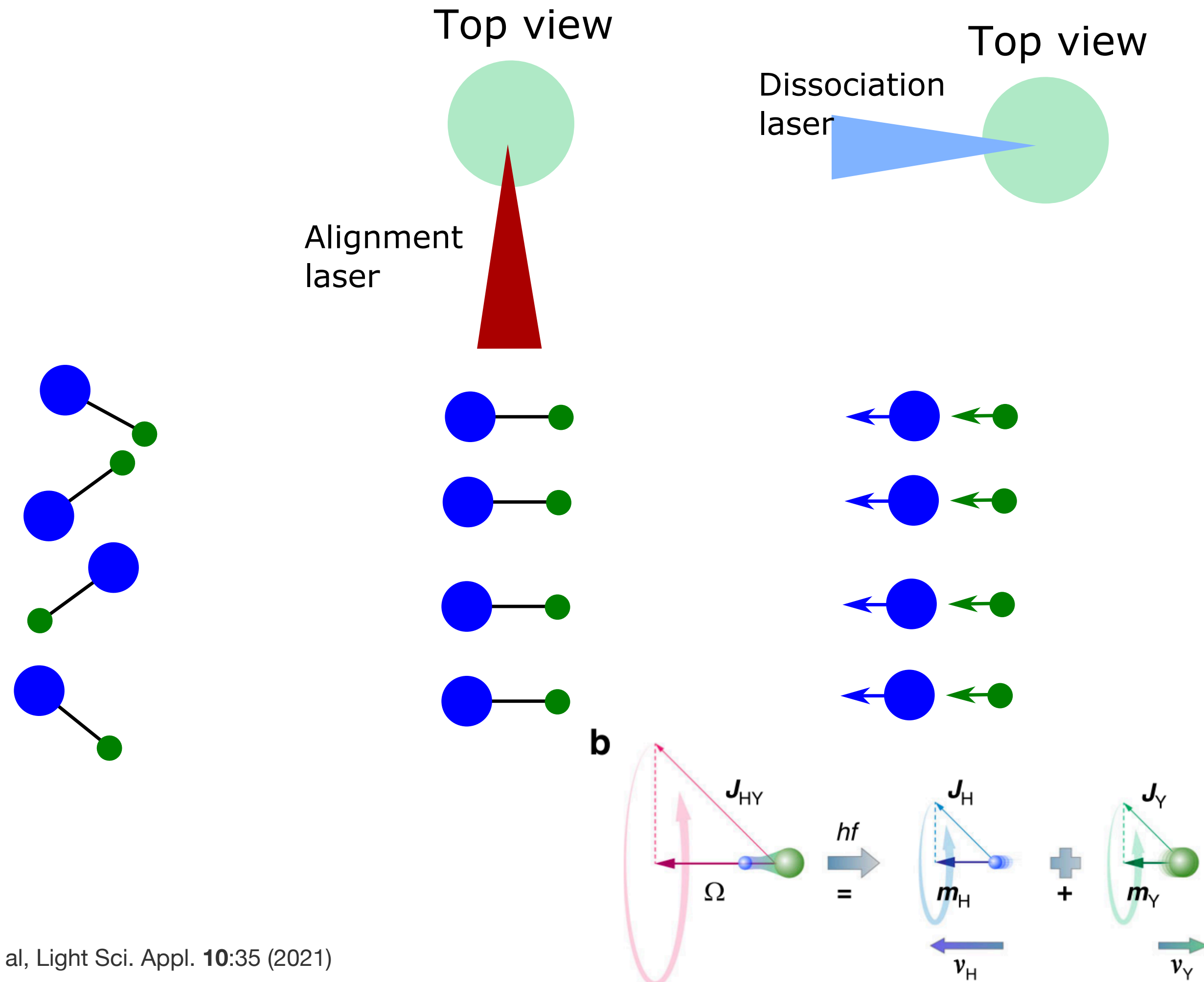
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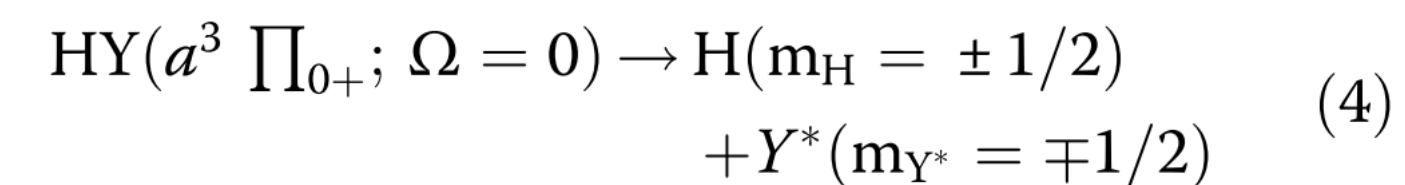
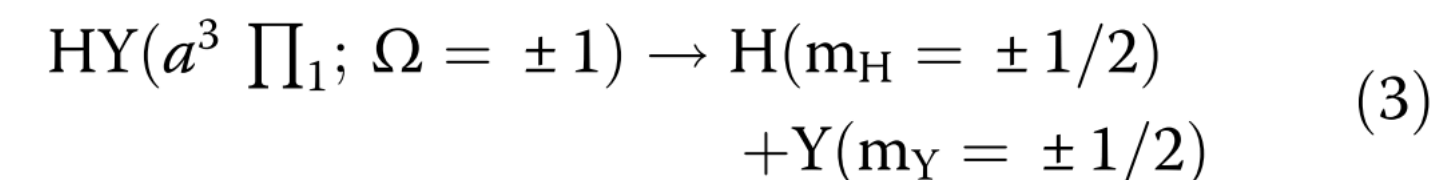
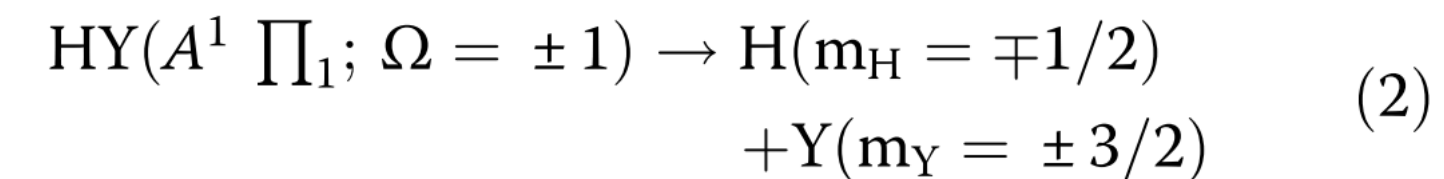
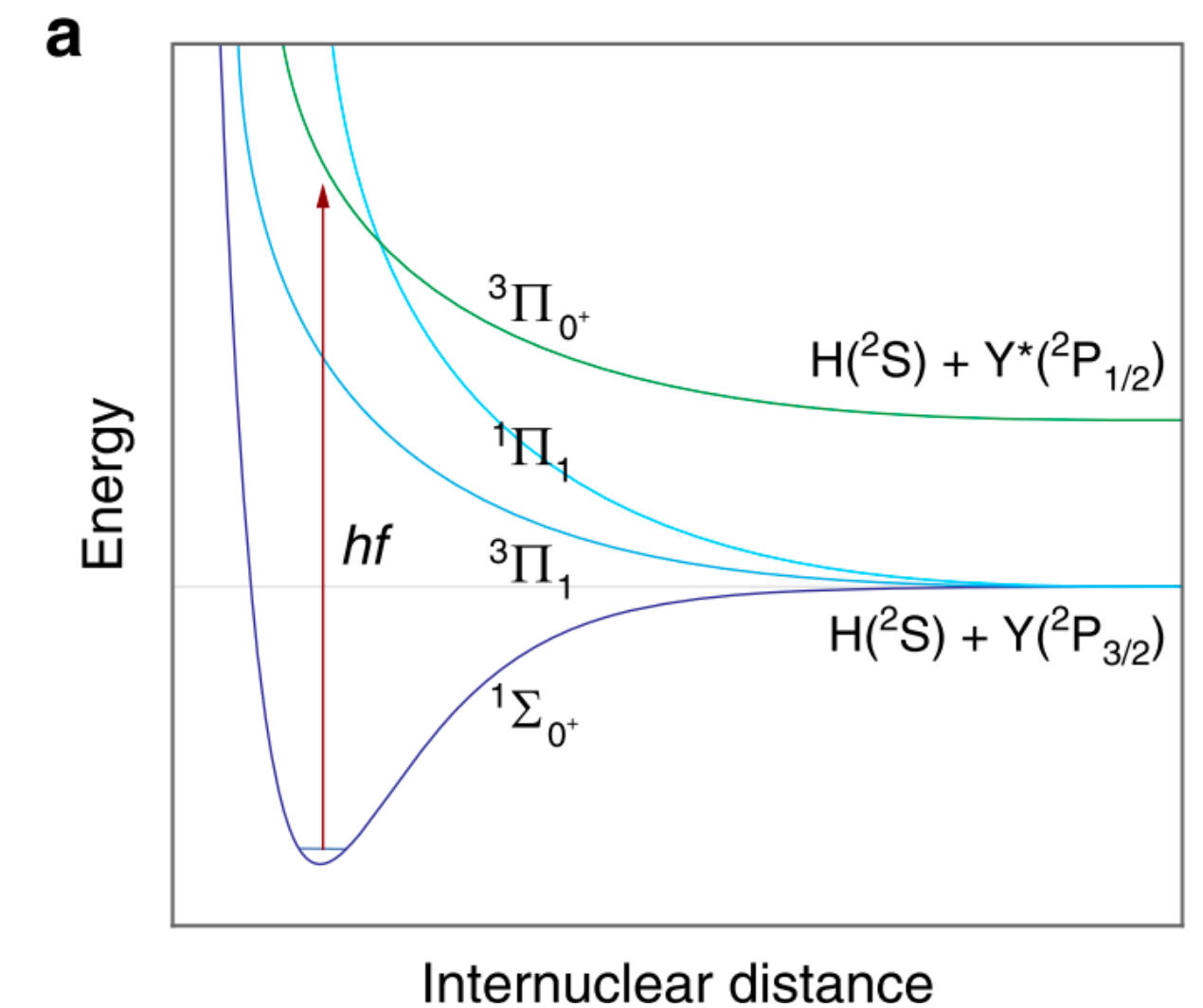
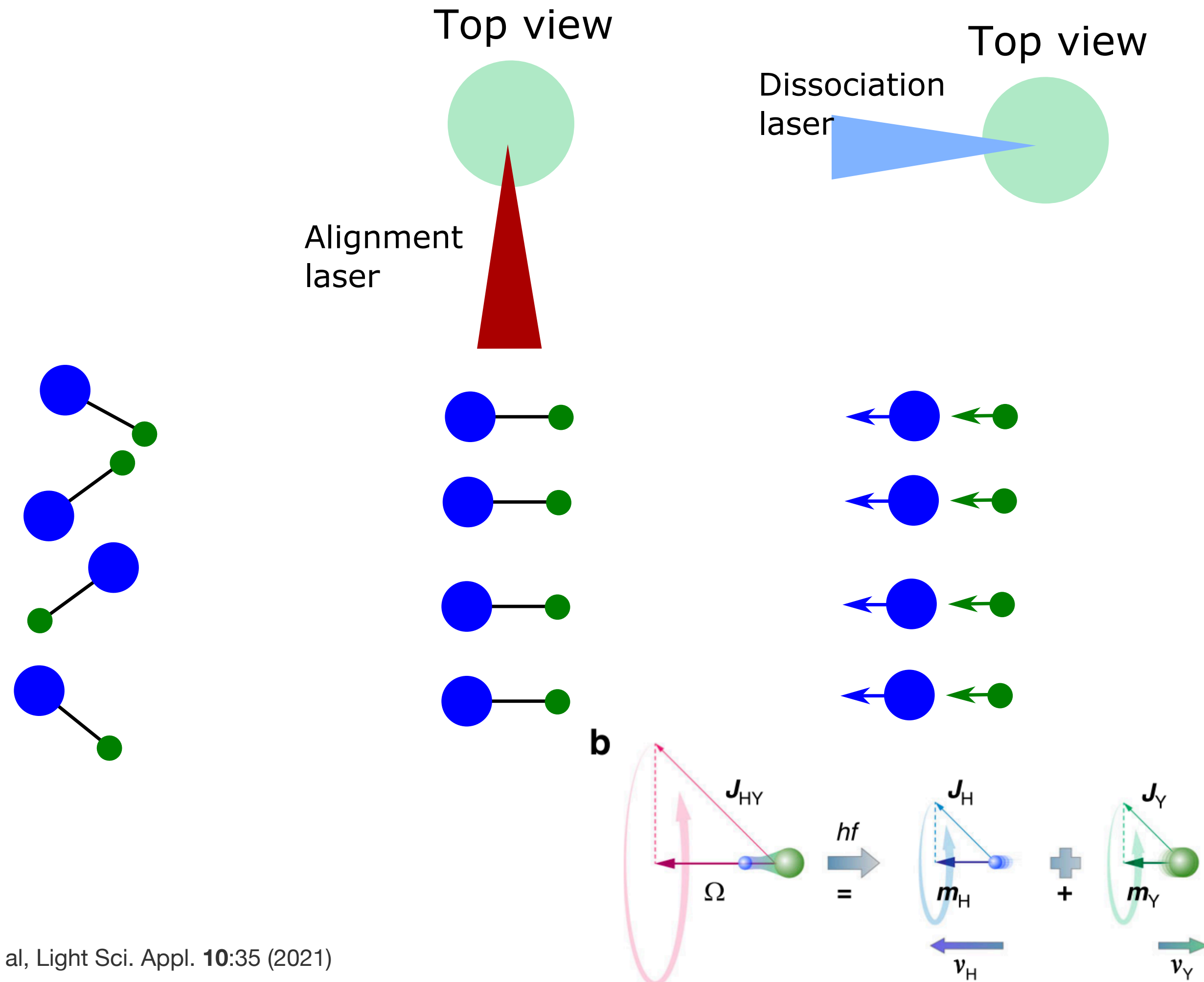
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Spin dynamics in (L)PAs

Very strong fields in laser-drivers and inside the bubble can lead to depolarisation

Spin
precession

Sokolov-Ternov
Effect

Stern-Gerlach
force

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Thomas-Bargmann-Michel-Telegdi
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Sokolov-Ternov: timescale ~us
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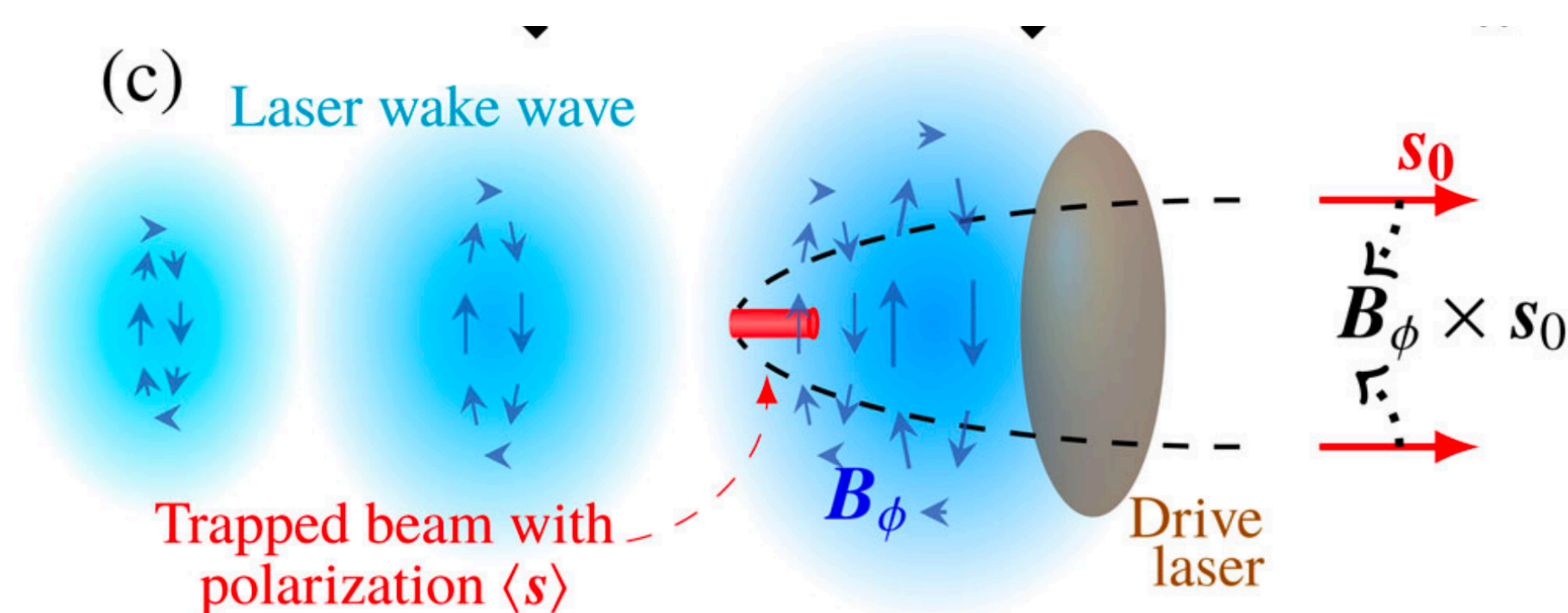
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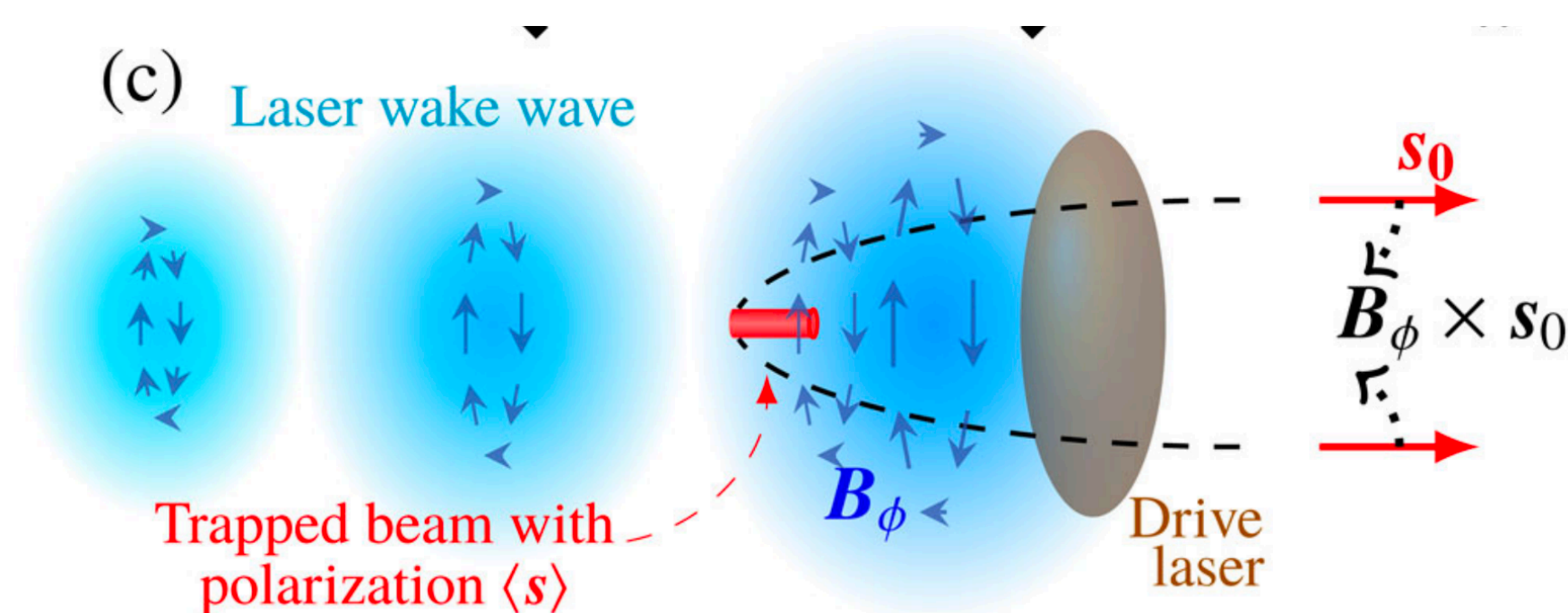
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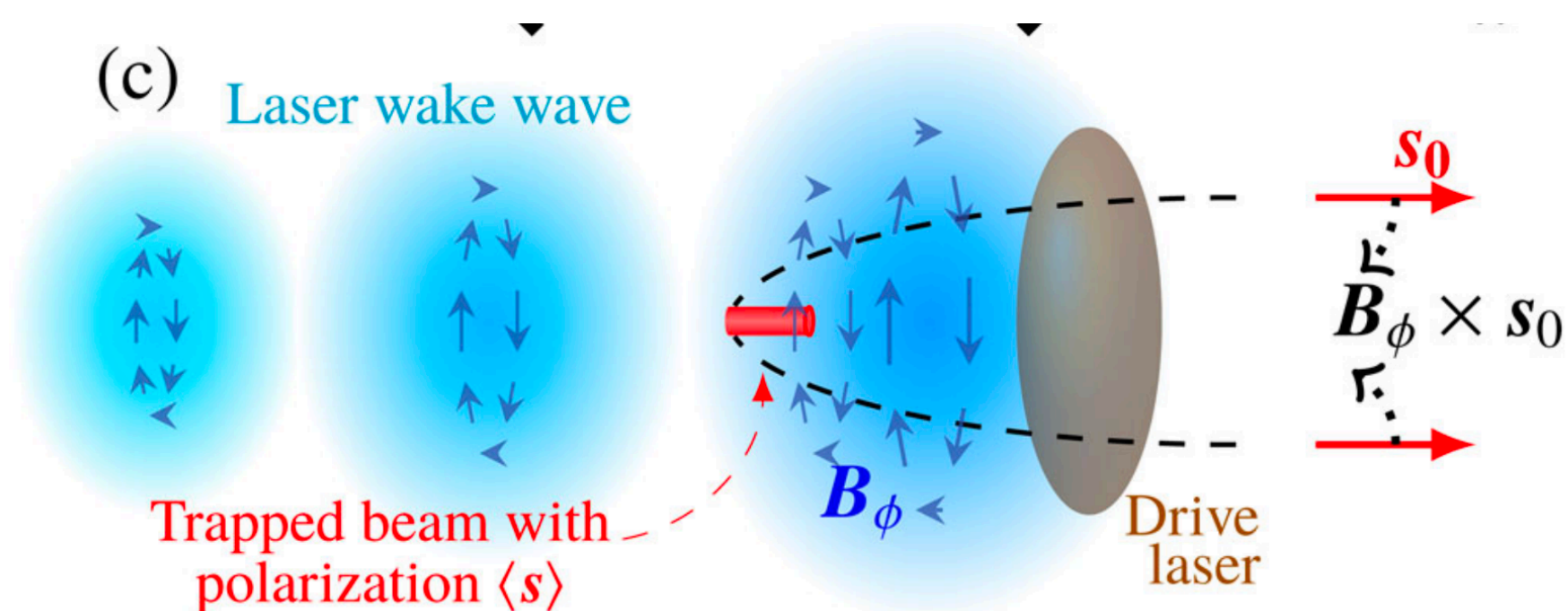
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 - > Stay close to axis
- > Strong \mathbf{E} fields lead to precession
 - > But all electrons together, so P stays high



Thomas-Bargmann-Michel-Telegdi equation

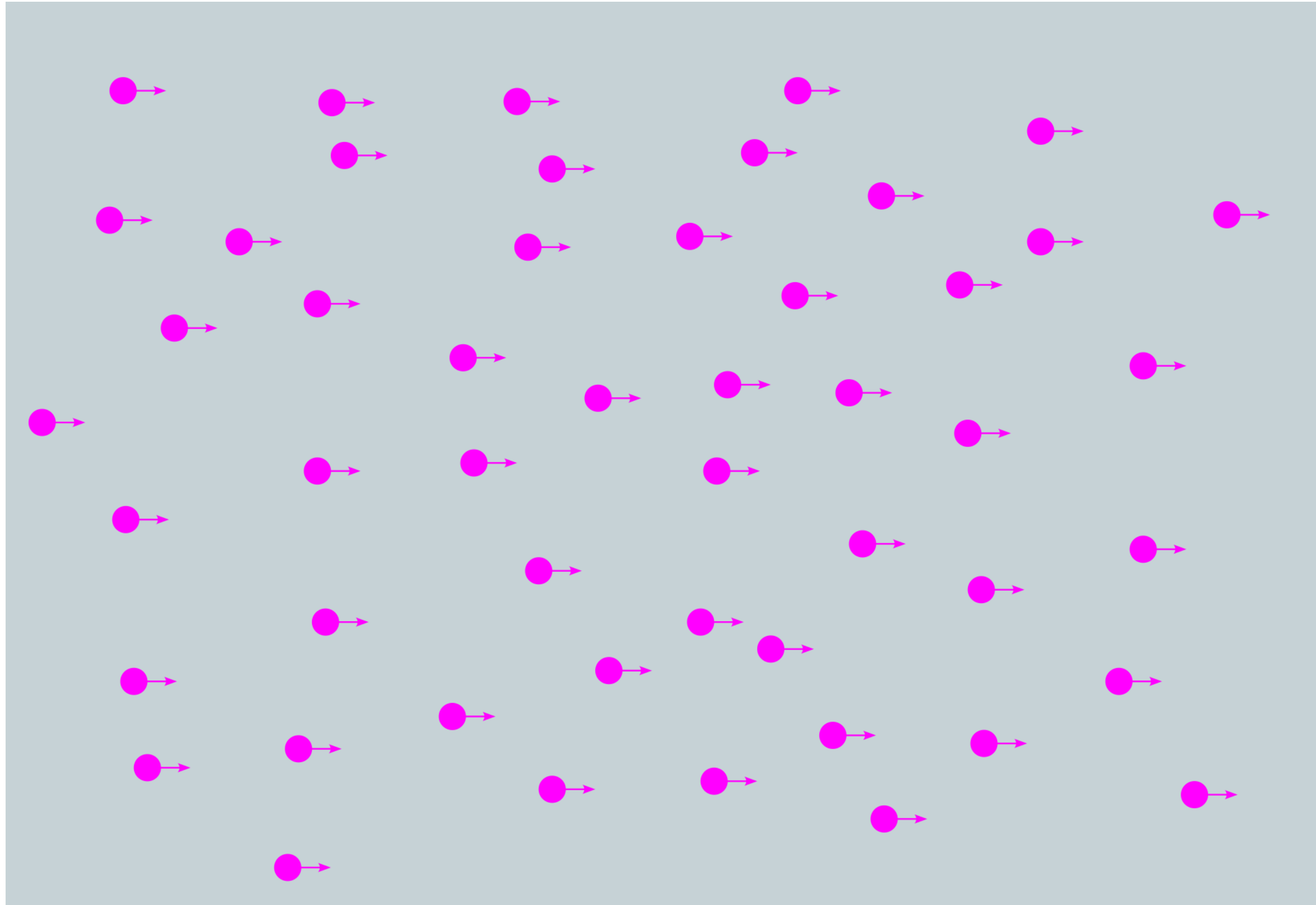
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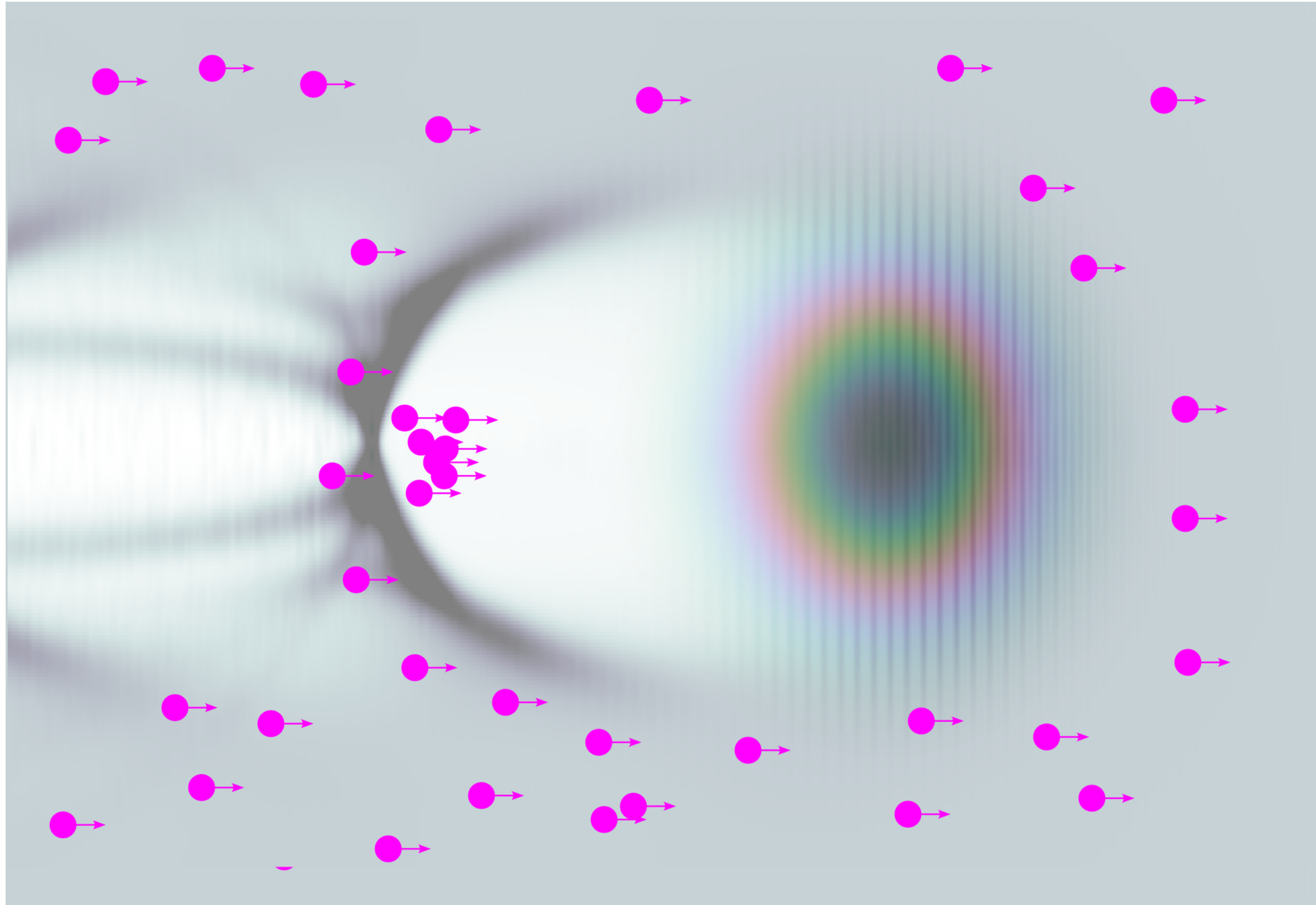
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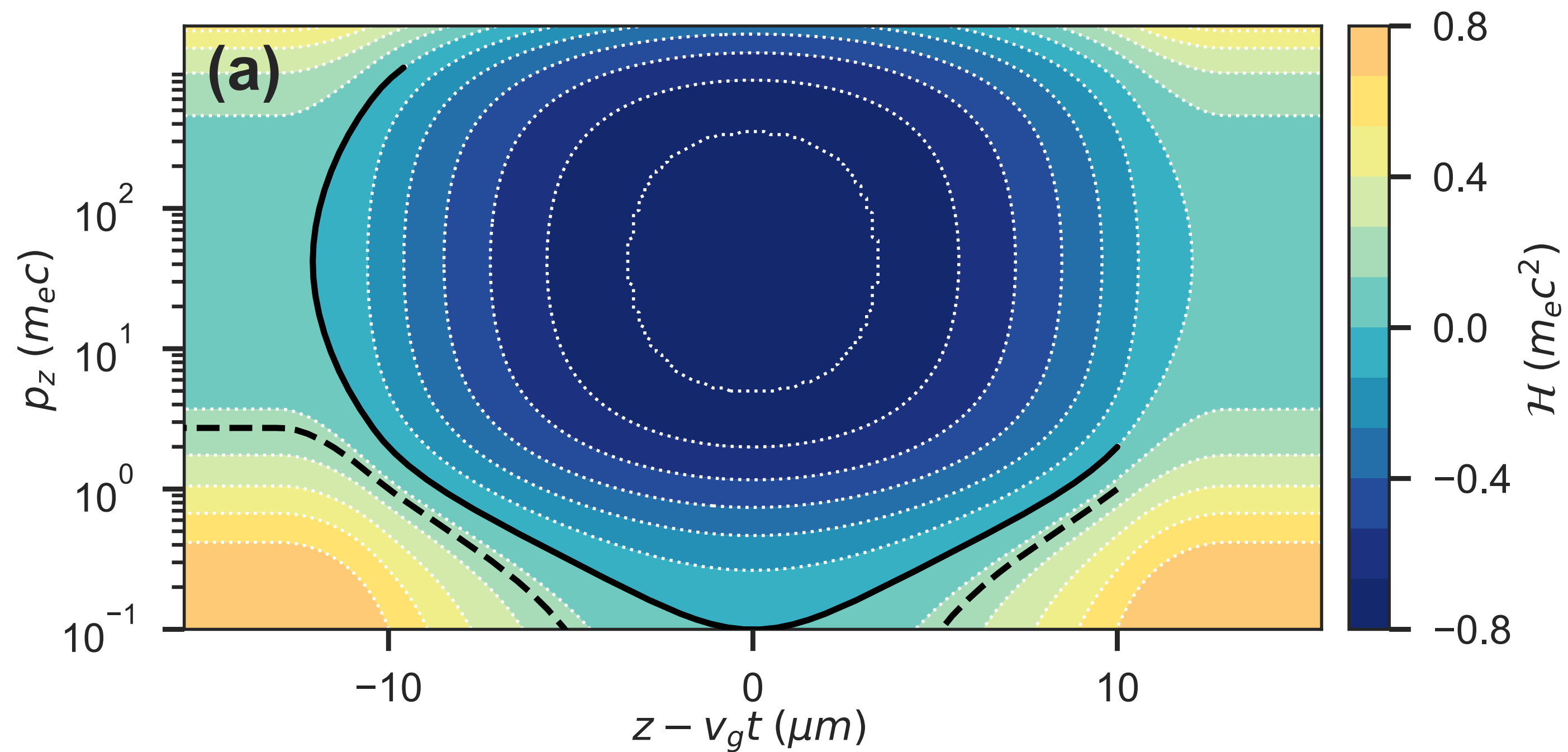


Injection requires sufficient longitudinal momentum

$$\mathcal{H}(\xi, p_z) = -|e|\varphi(\xi) + c\sqrt{m_e^2 c^2 + p_z^2} - v_d p_z$$

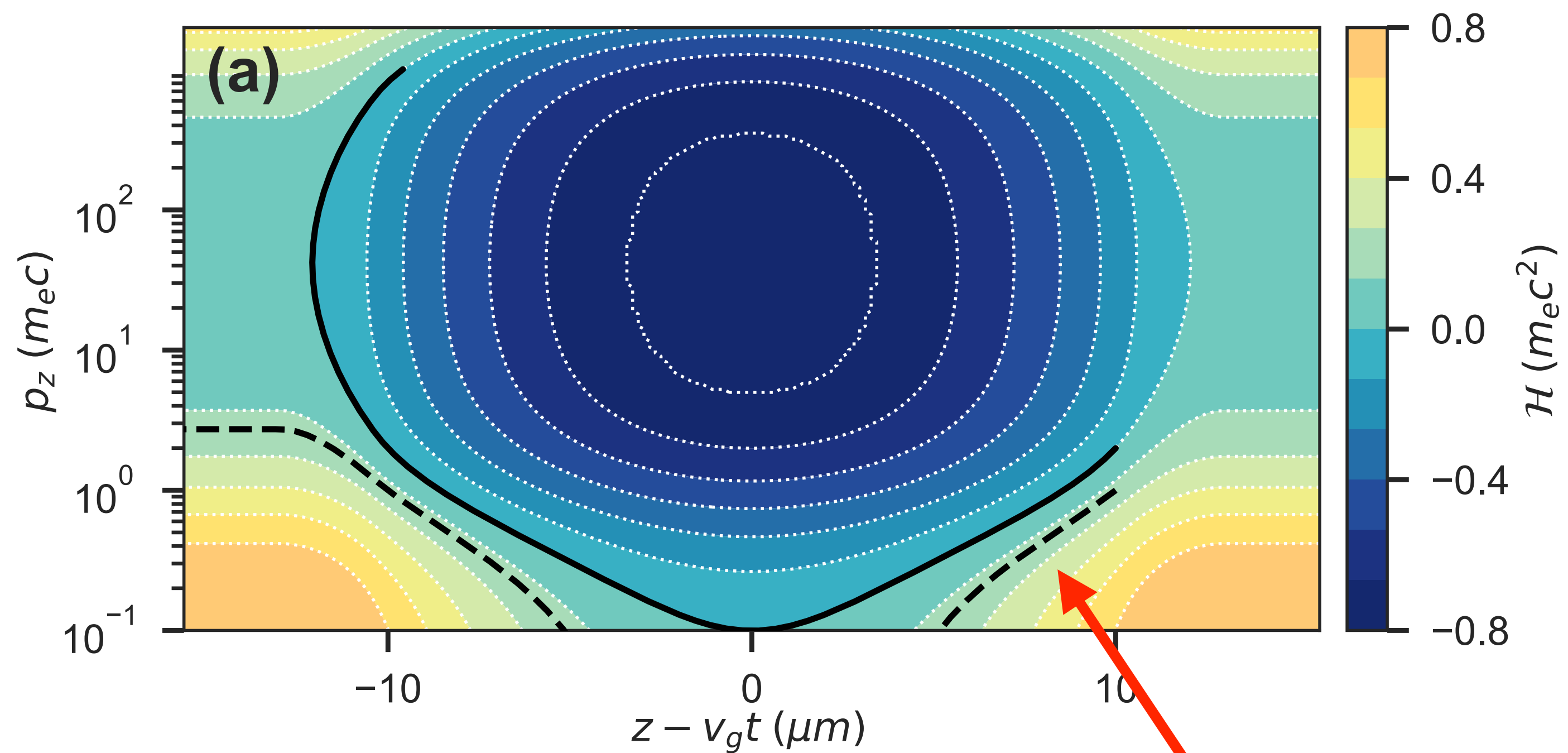
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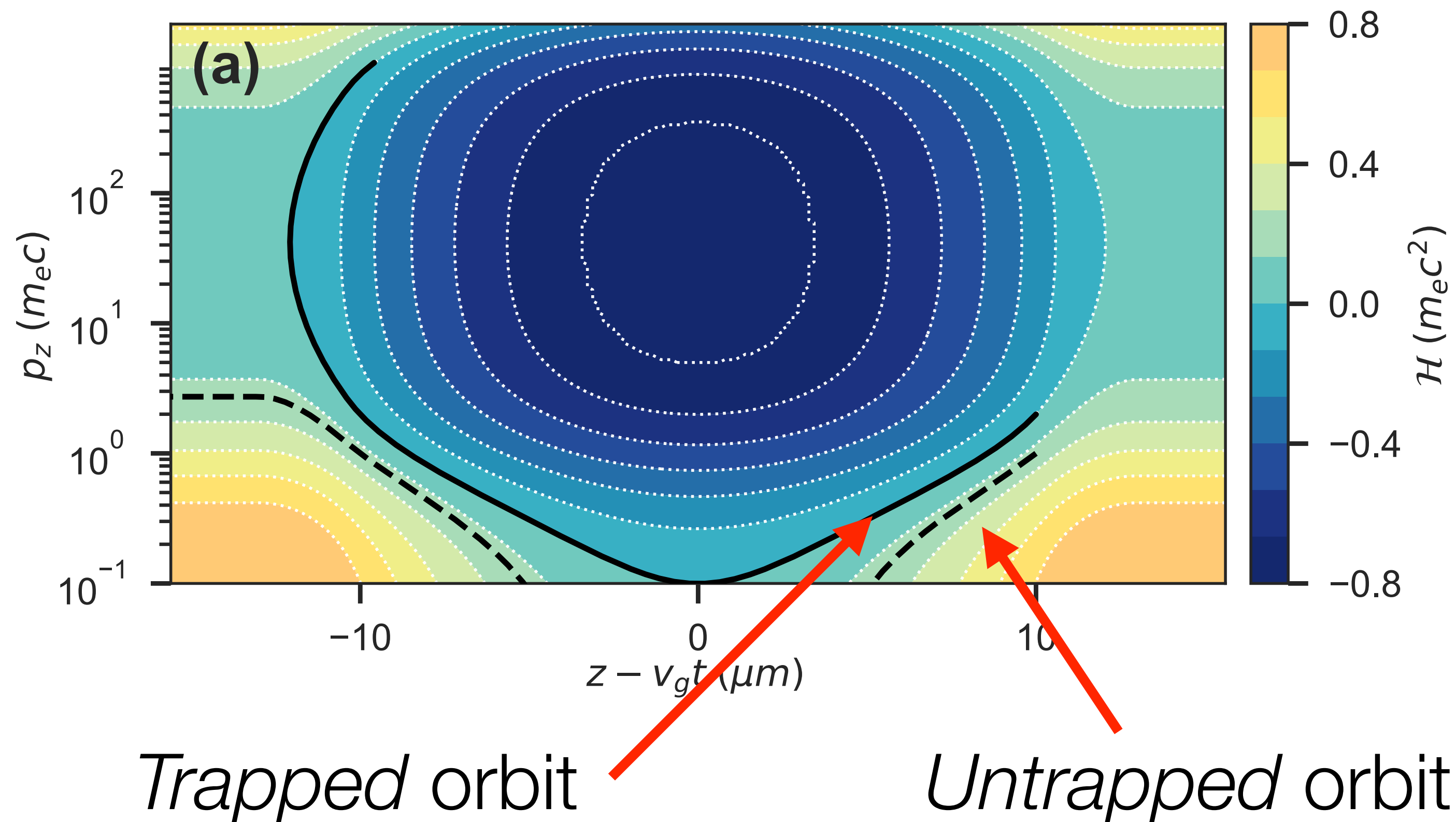
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Untrapped orbit

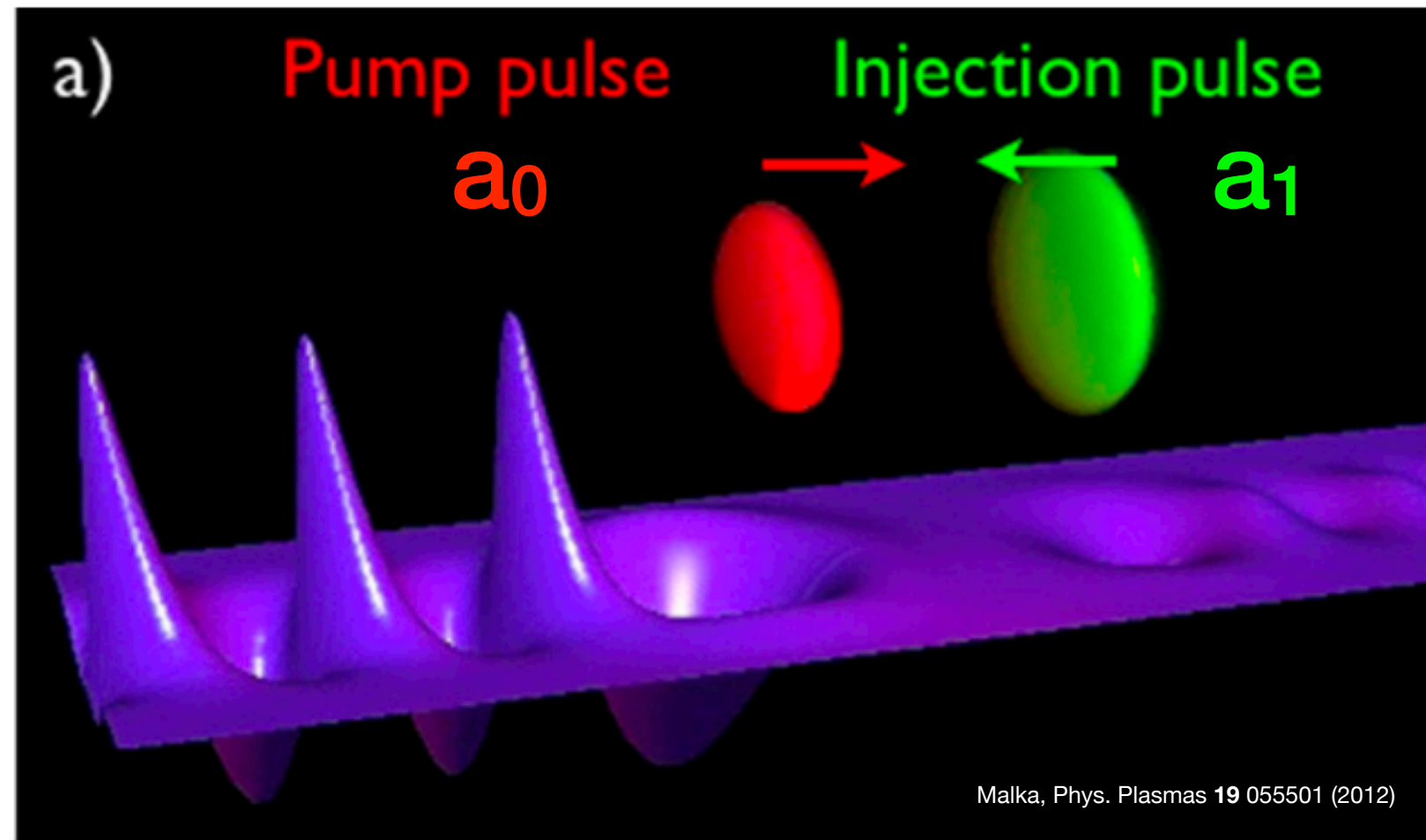
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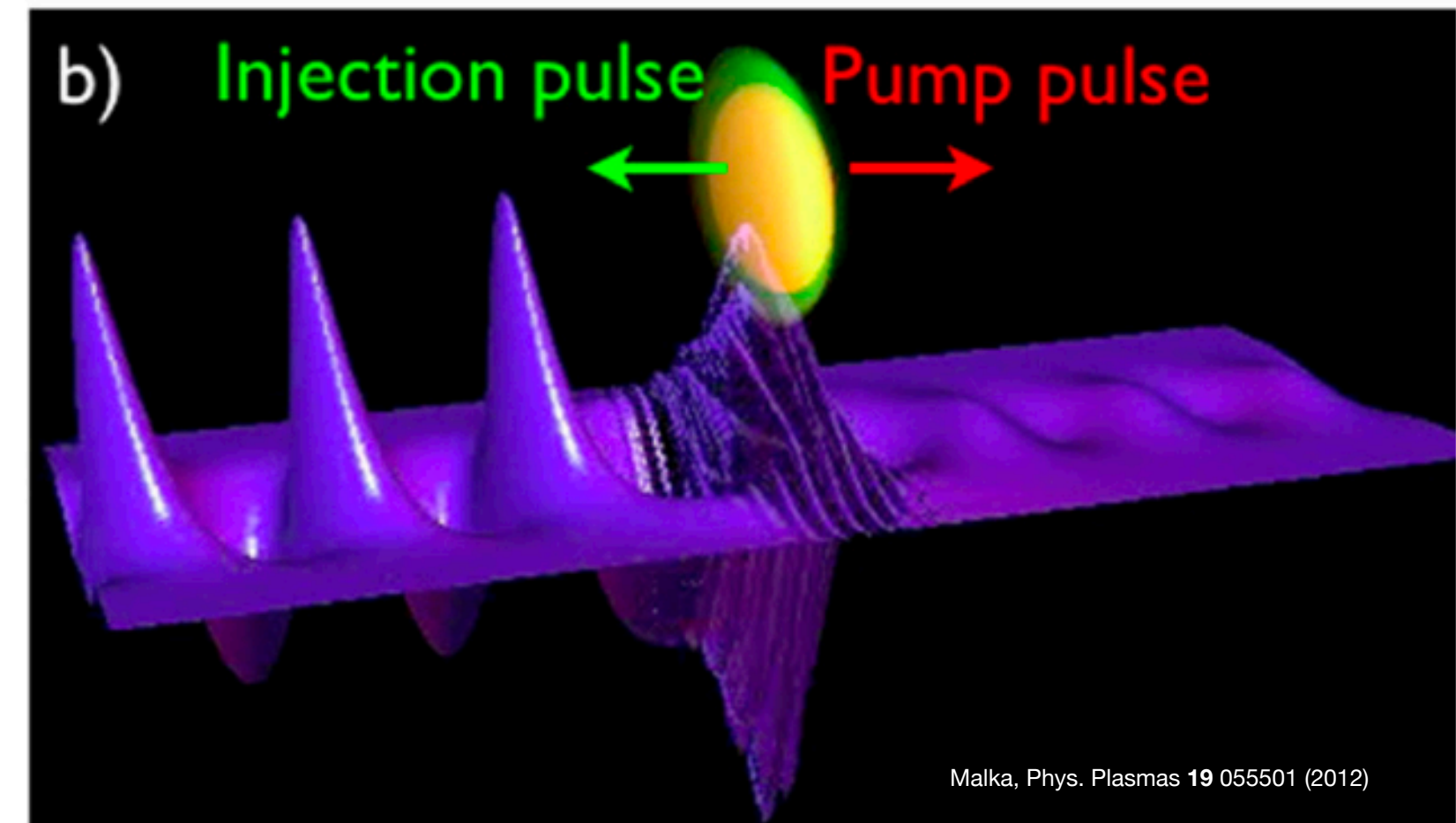
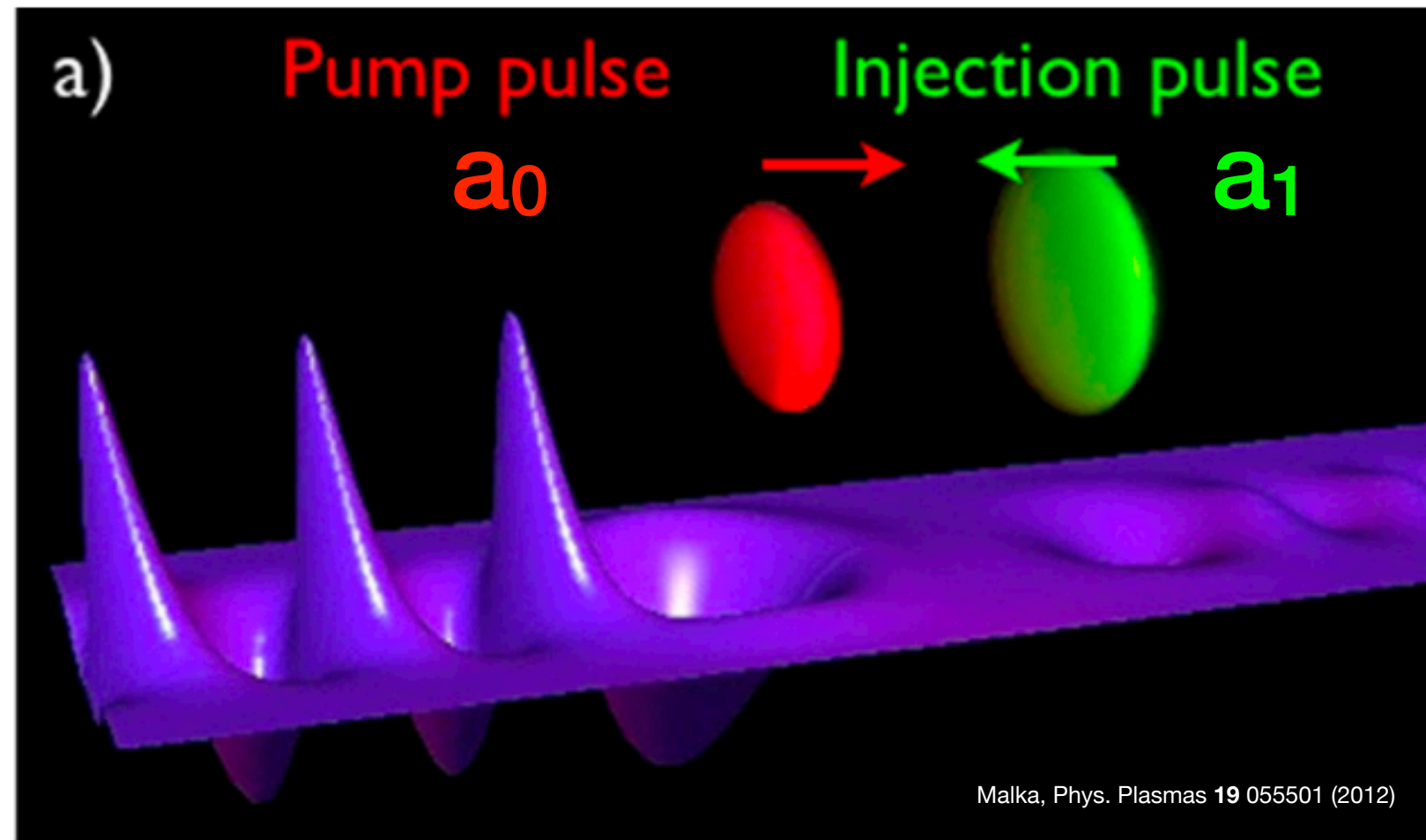
Colliding two laser pulses can lead to trapping

Stochastic heating in the lasers' interaction region gives electrons residual longitudinal momentum



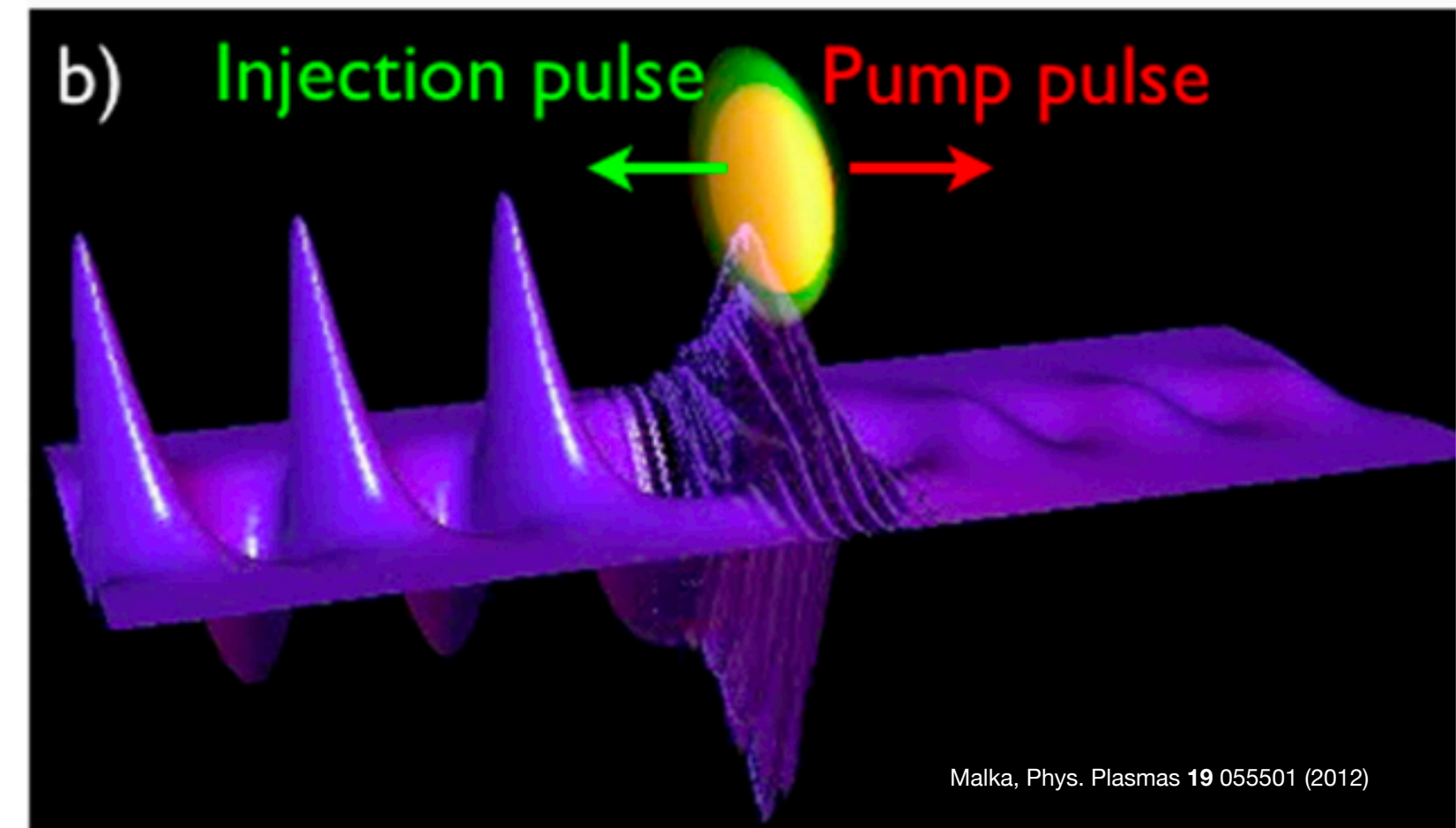
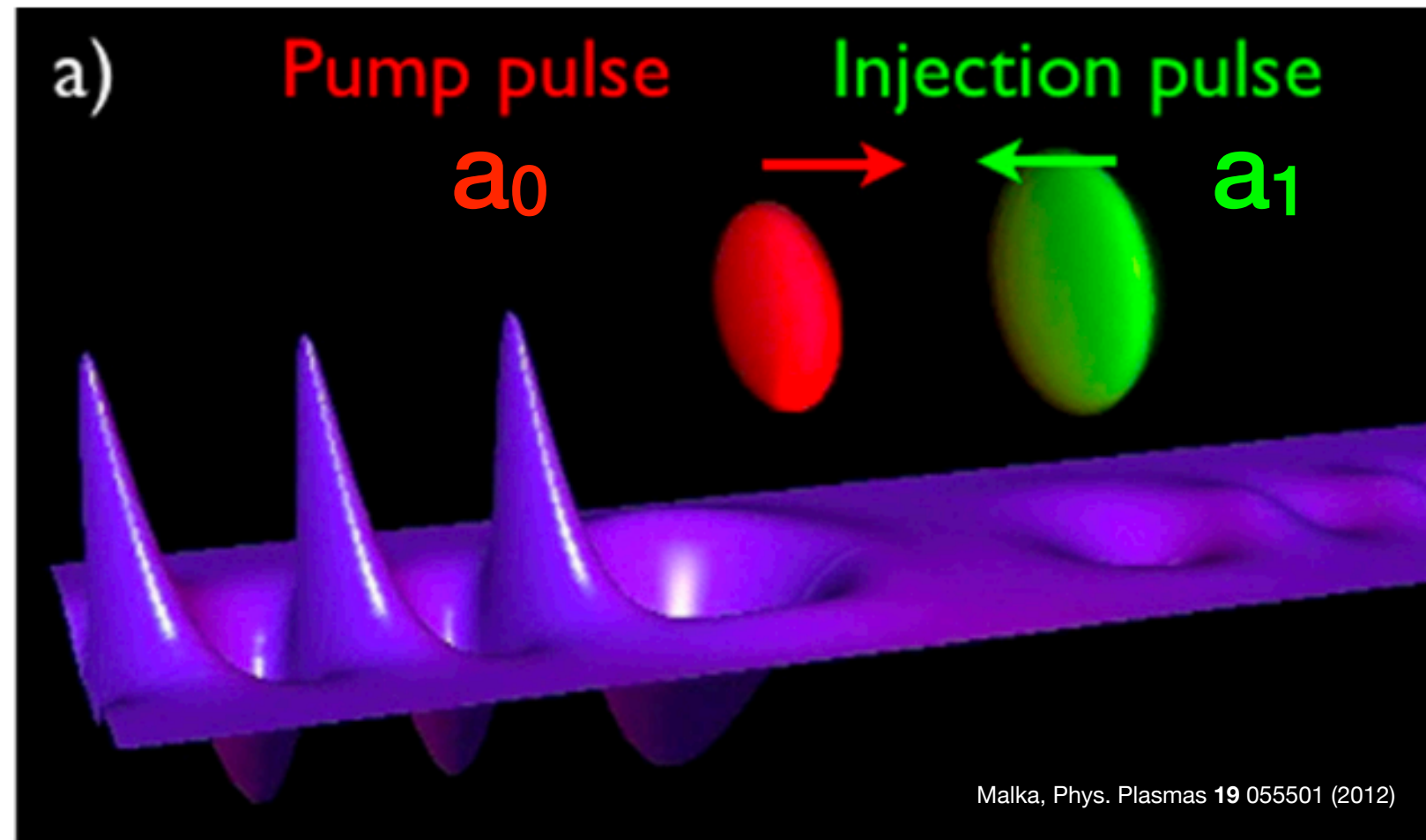
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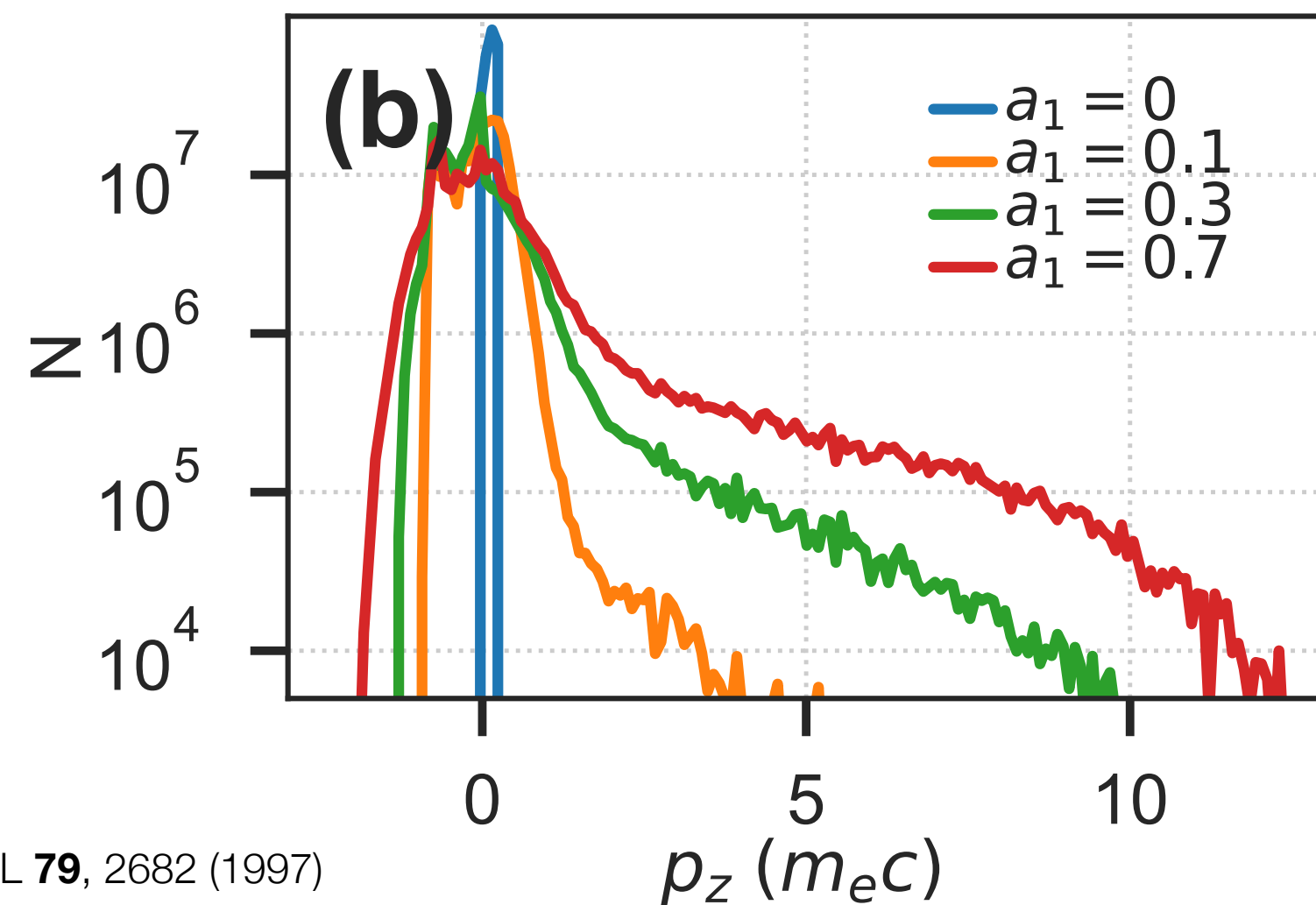
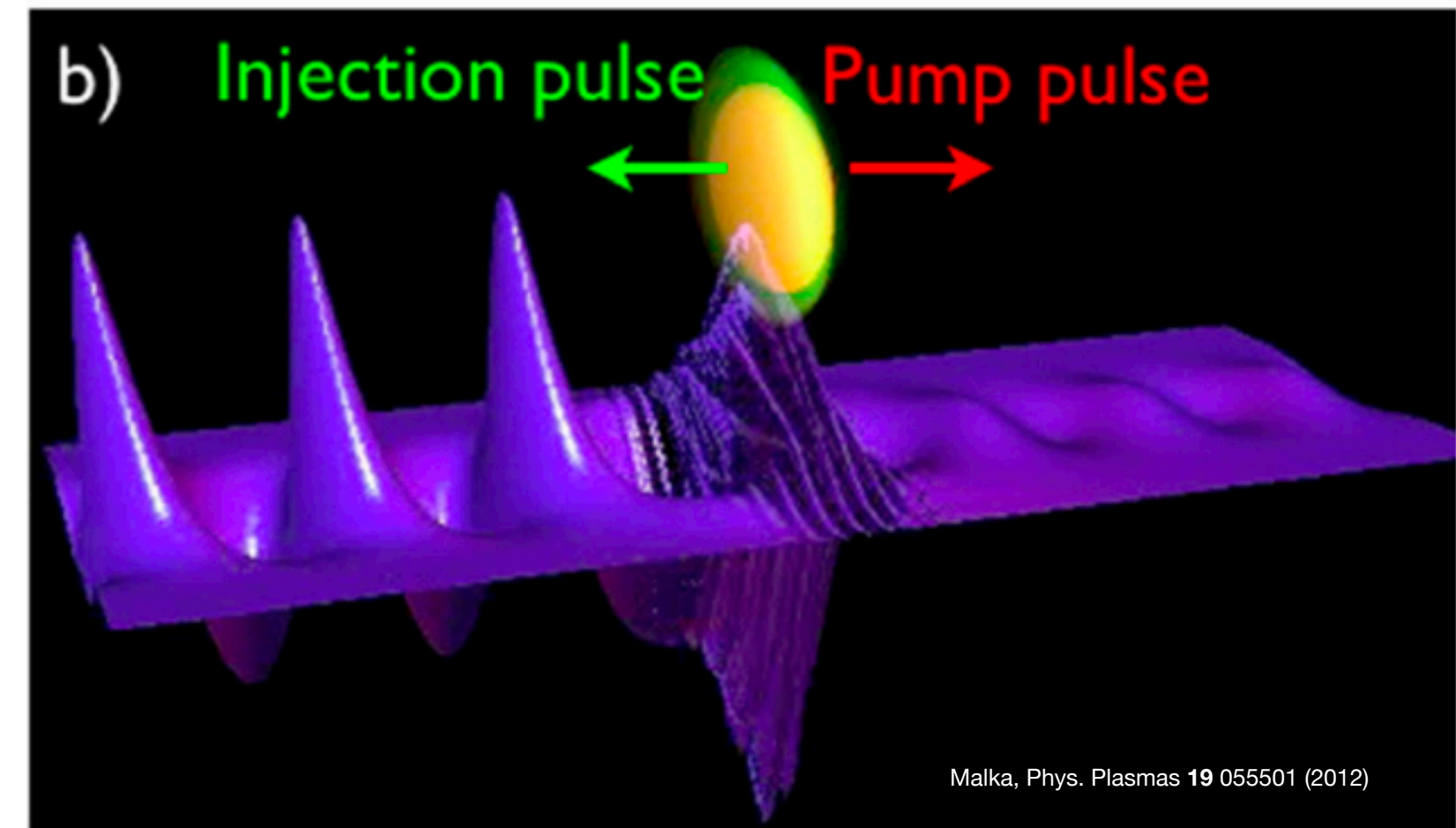
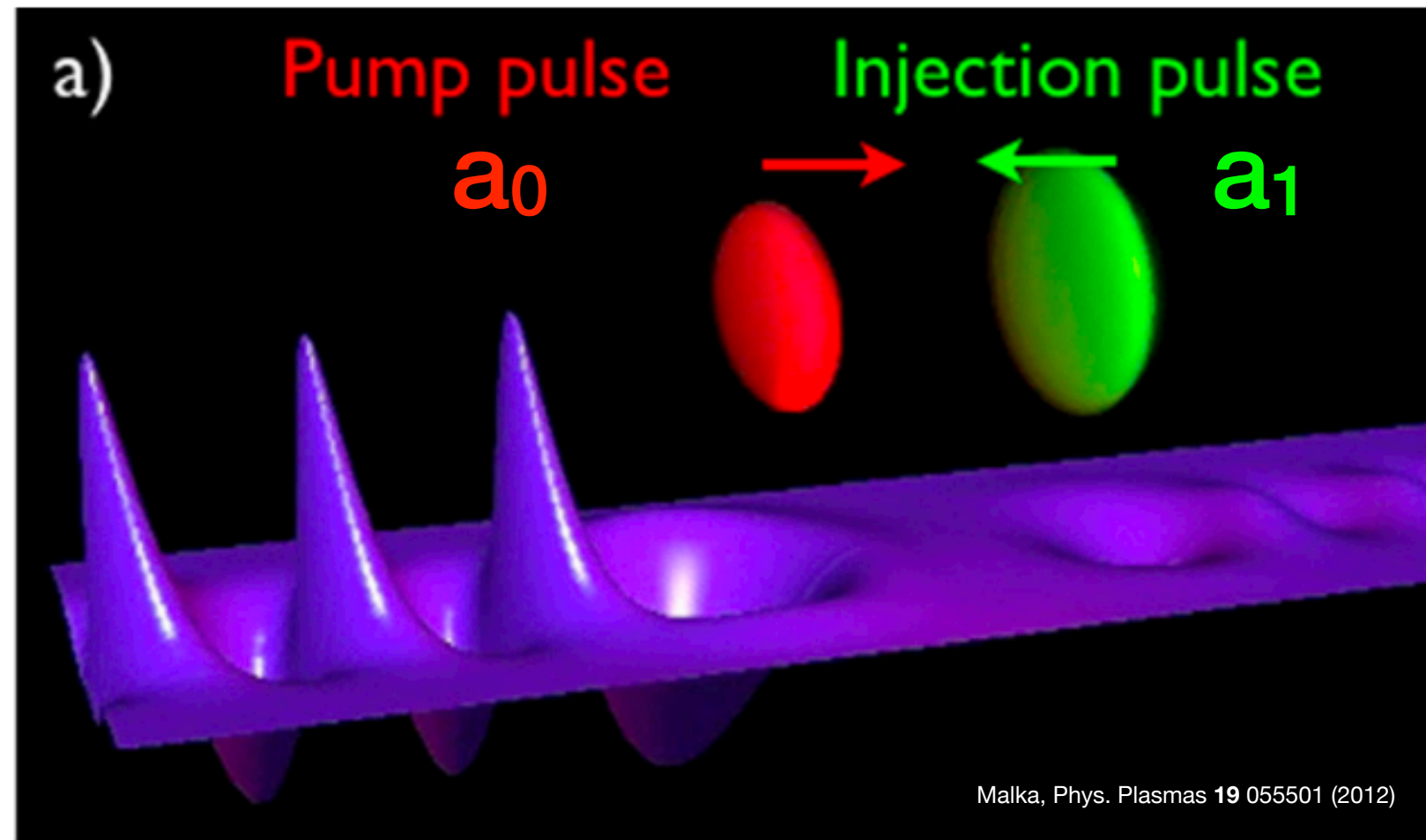
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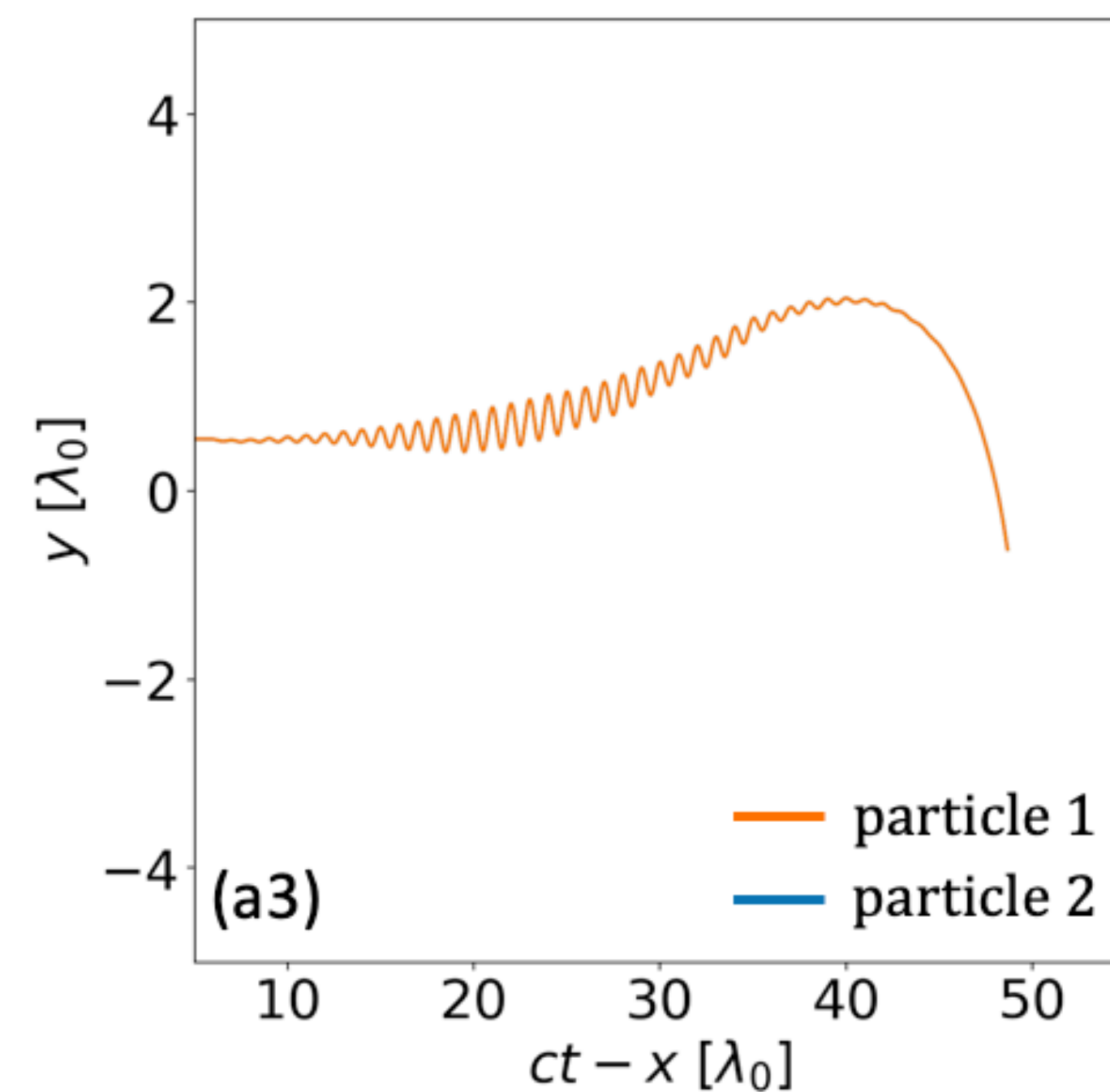
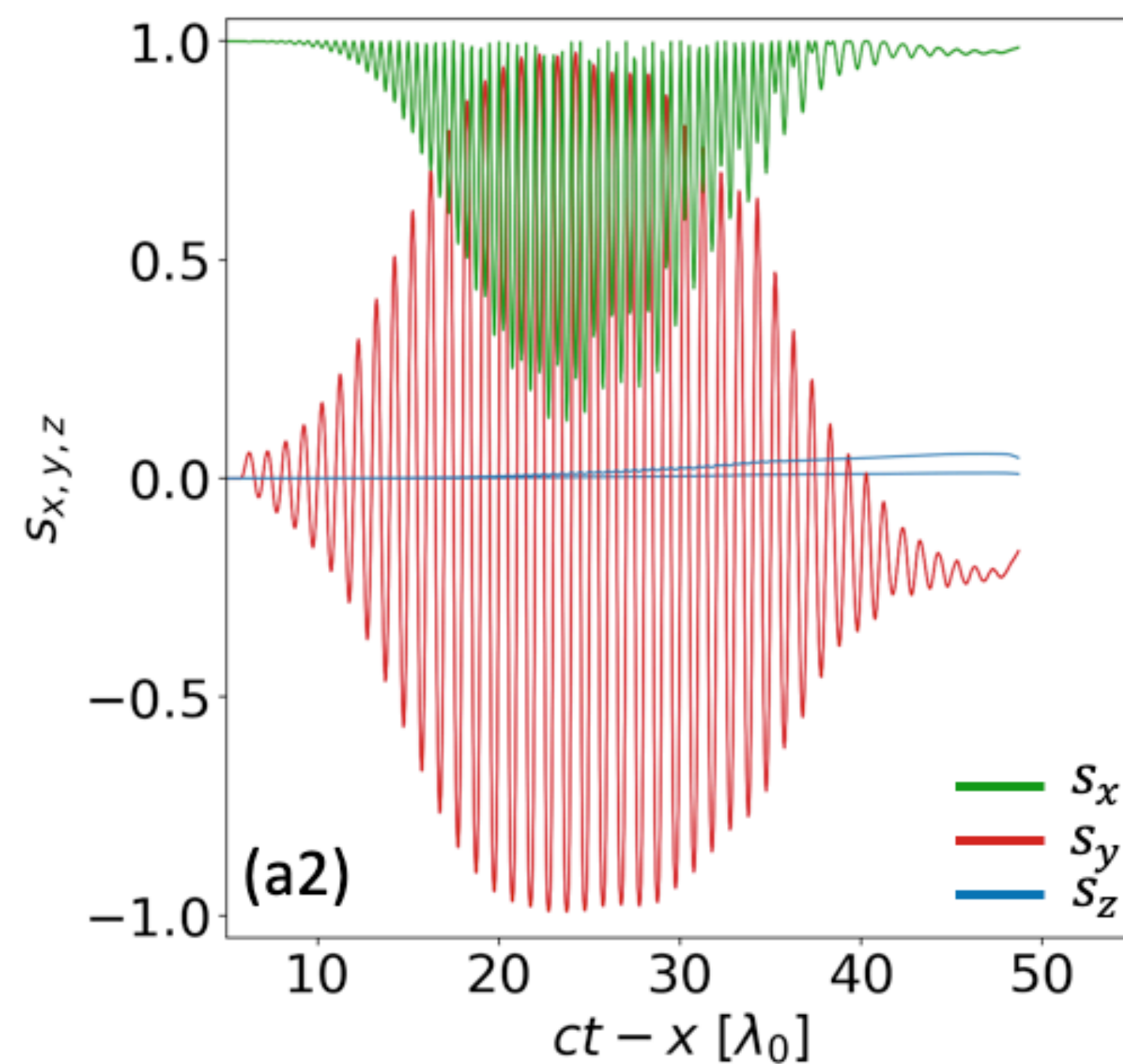
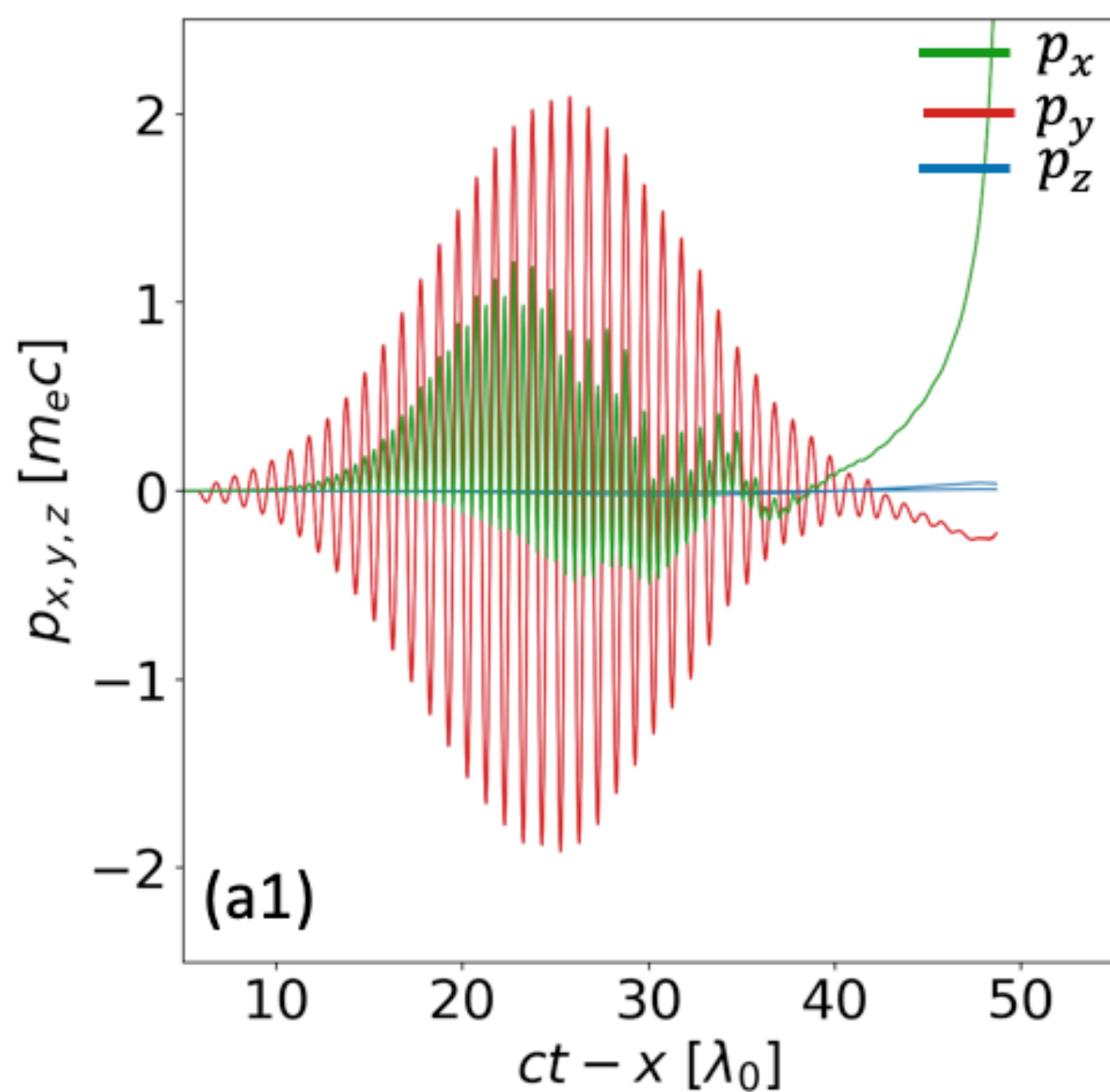
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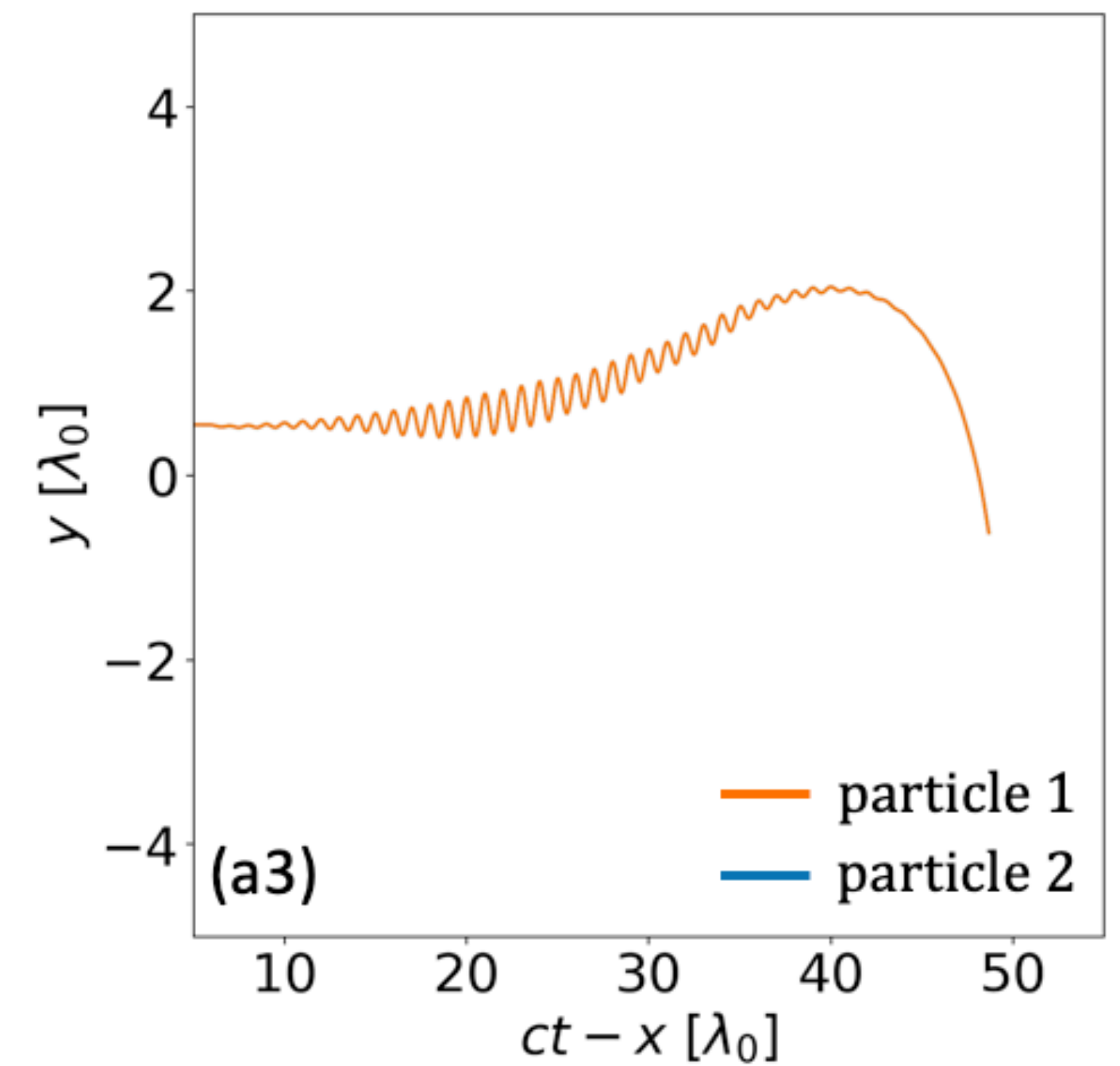
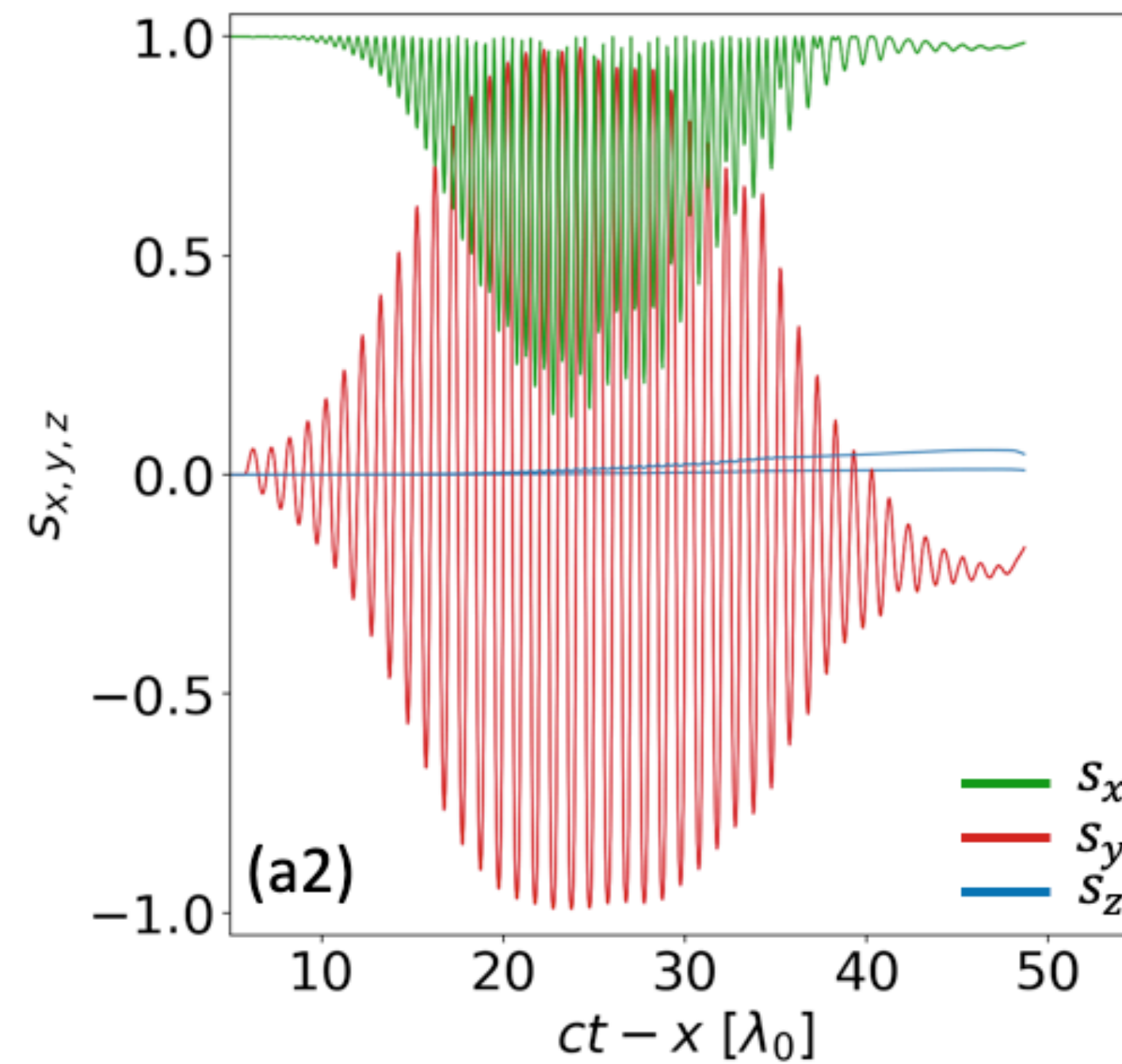
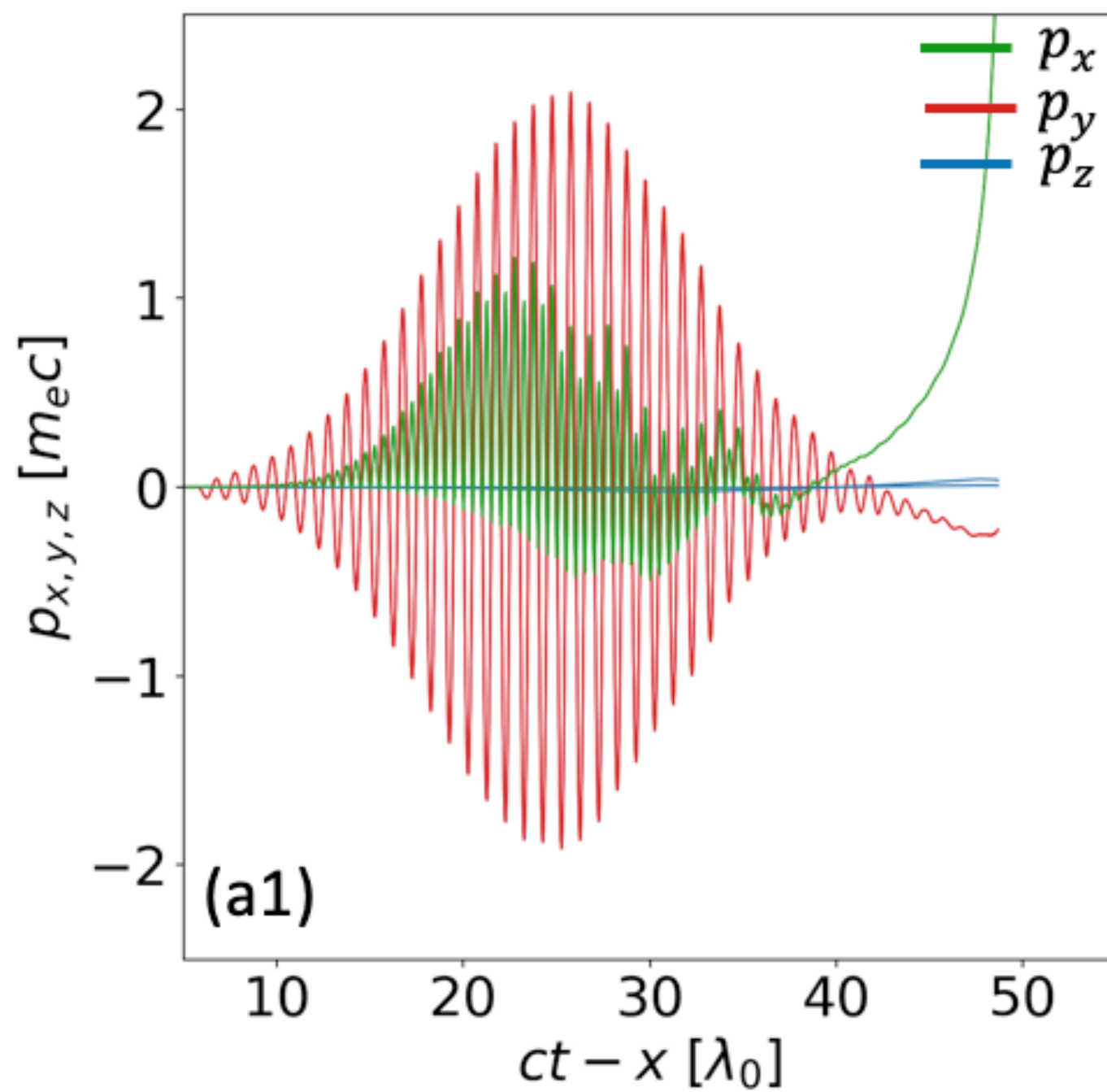
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Spin evolution in colliding pulse injection

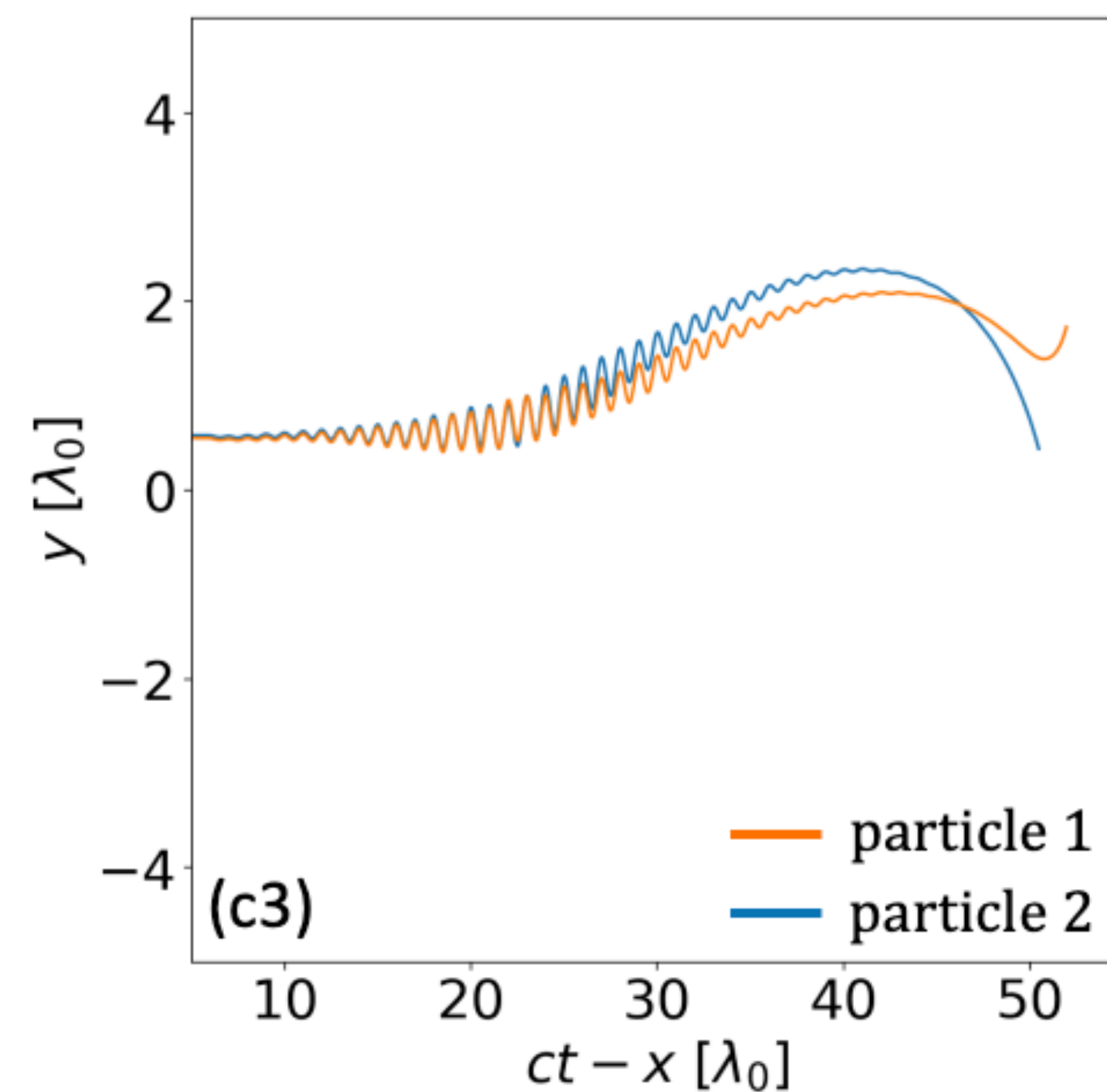
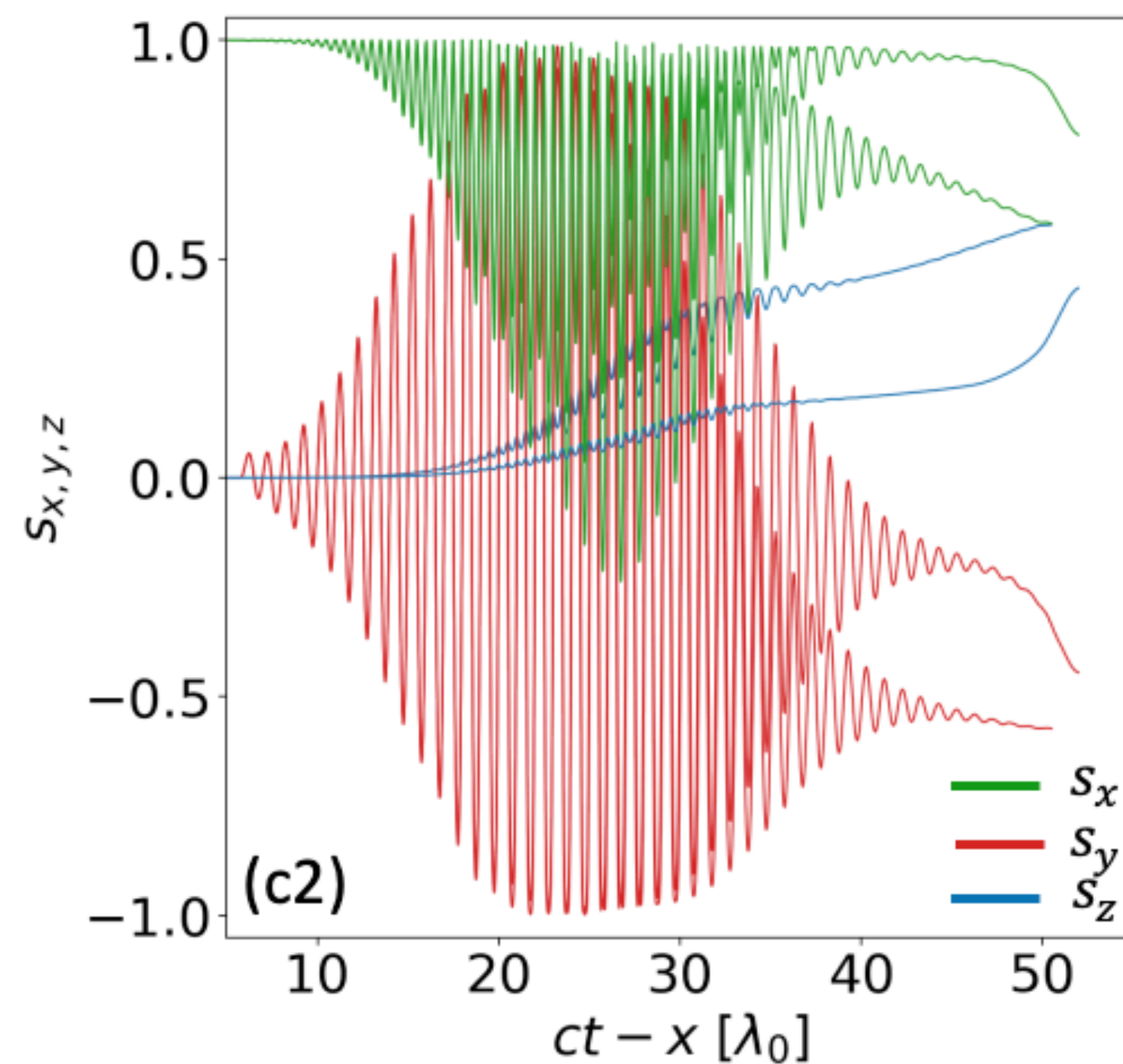
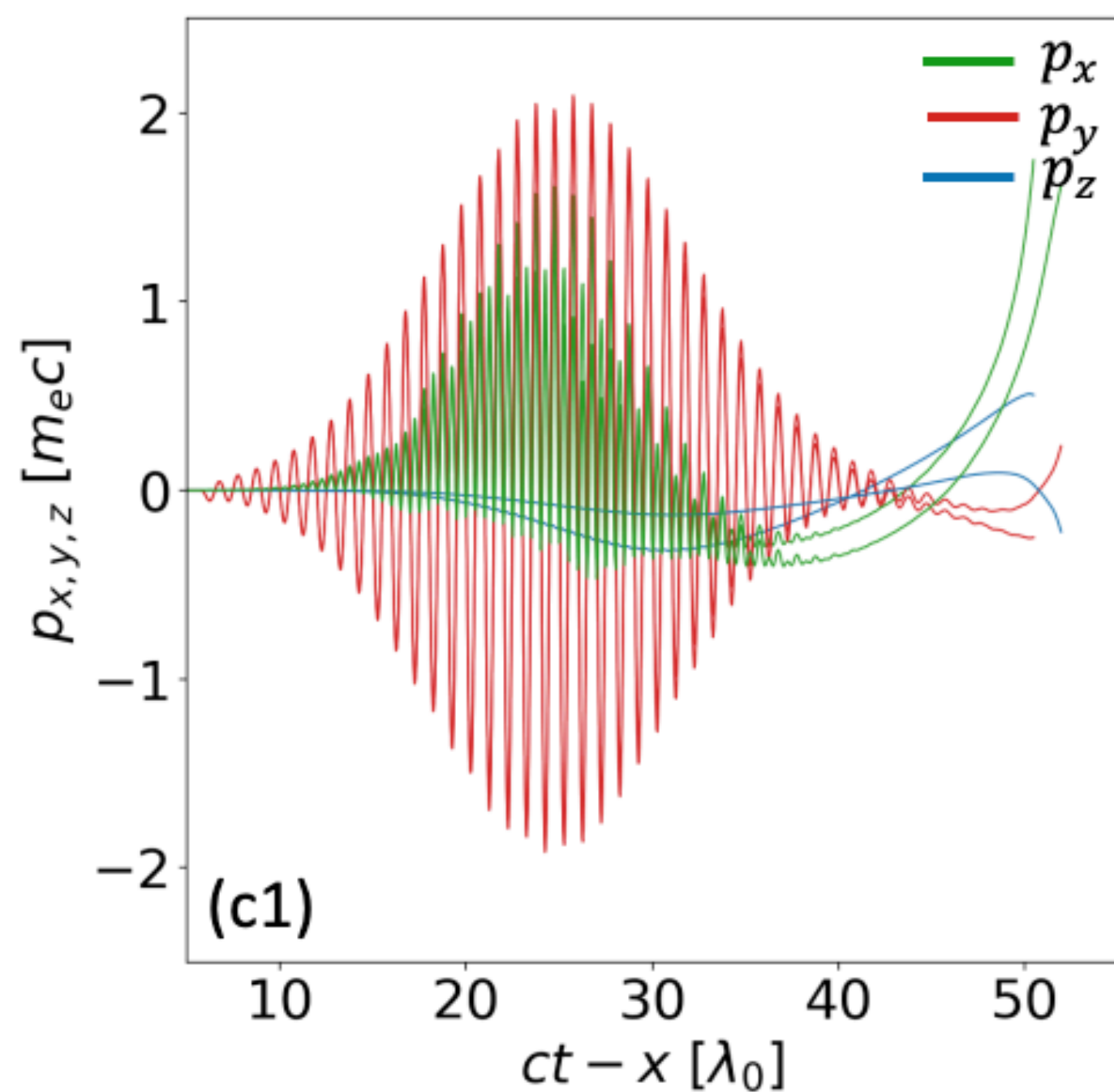


Spin evolution in colliding pulse injection

Precession 😊

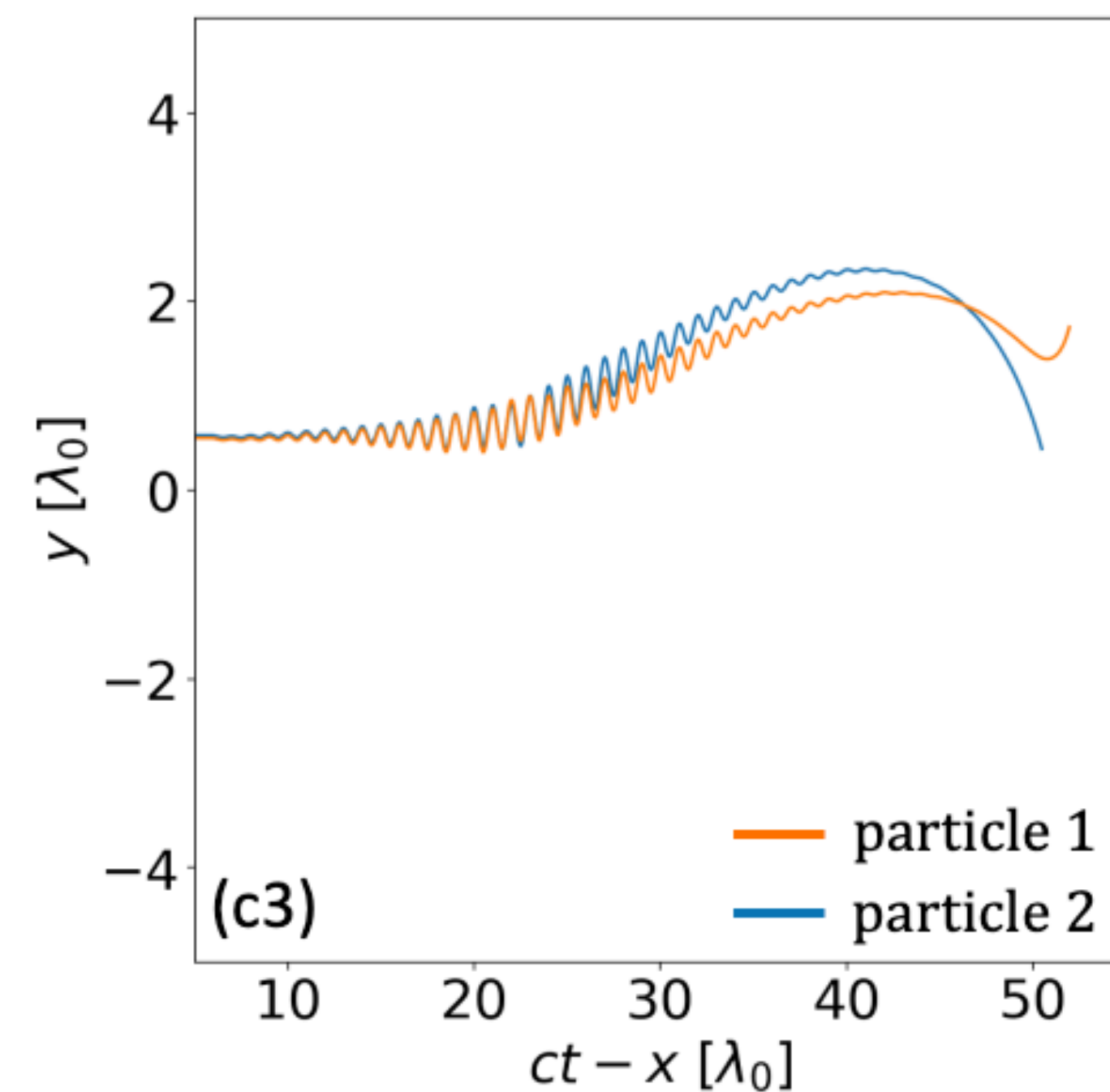
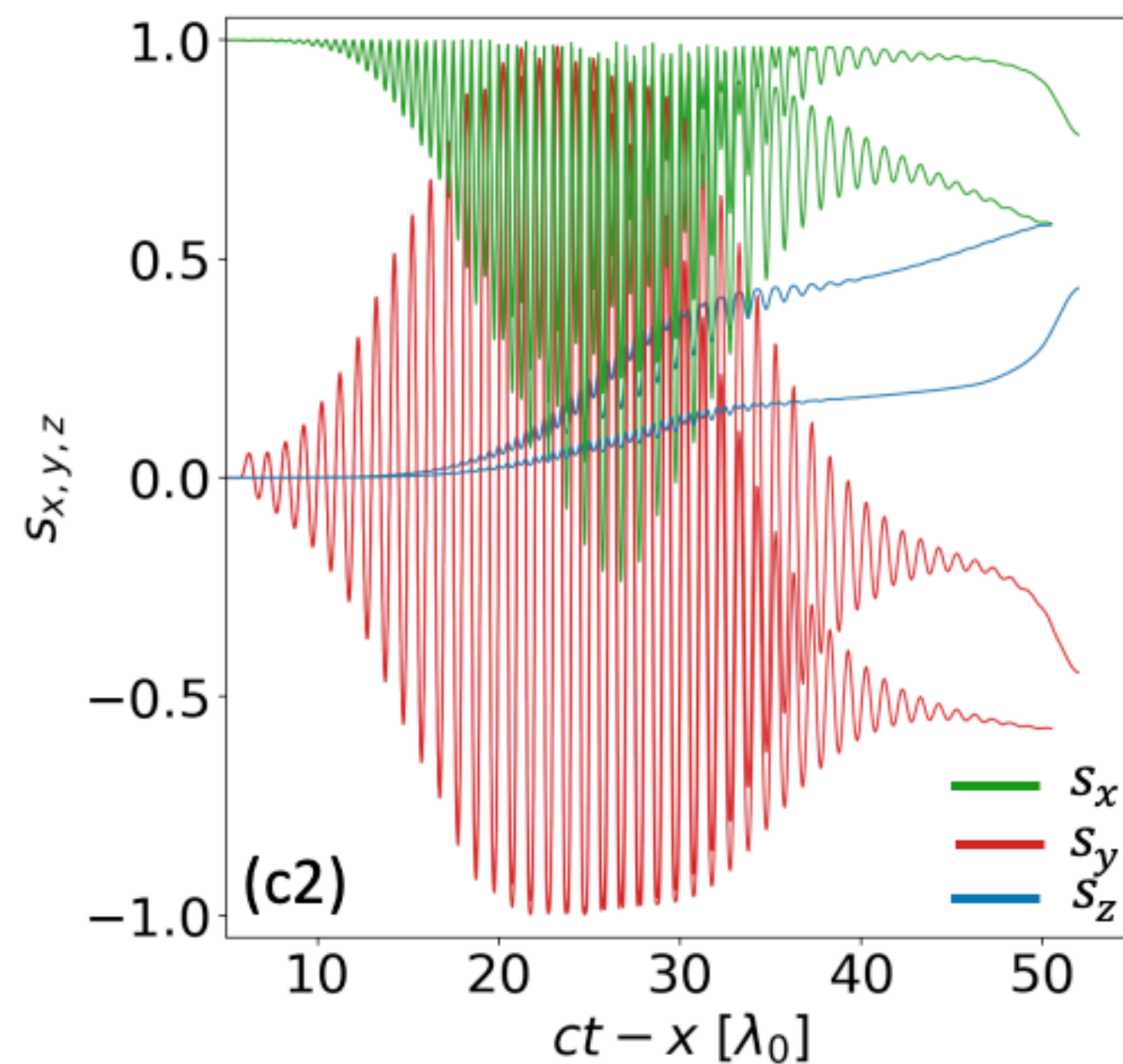
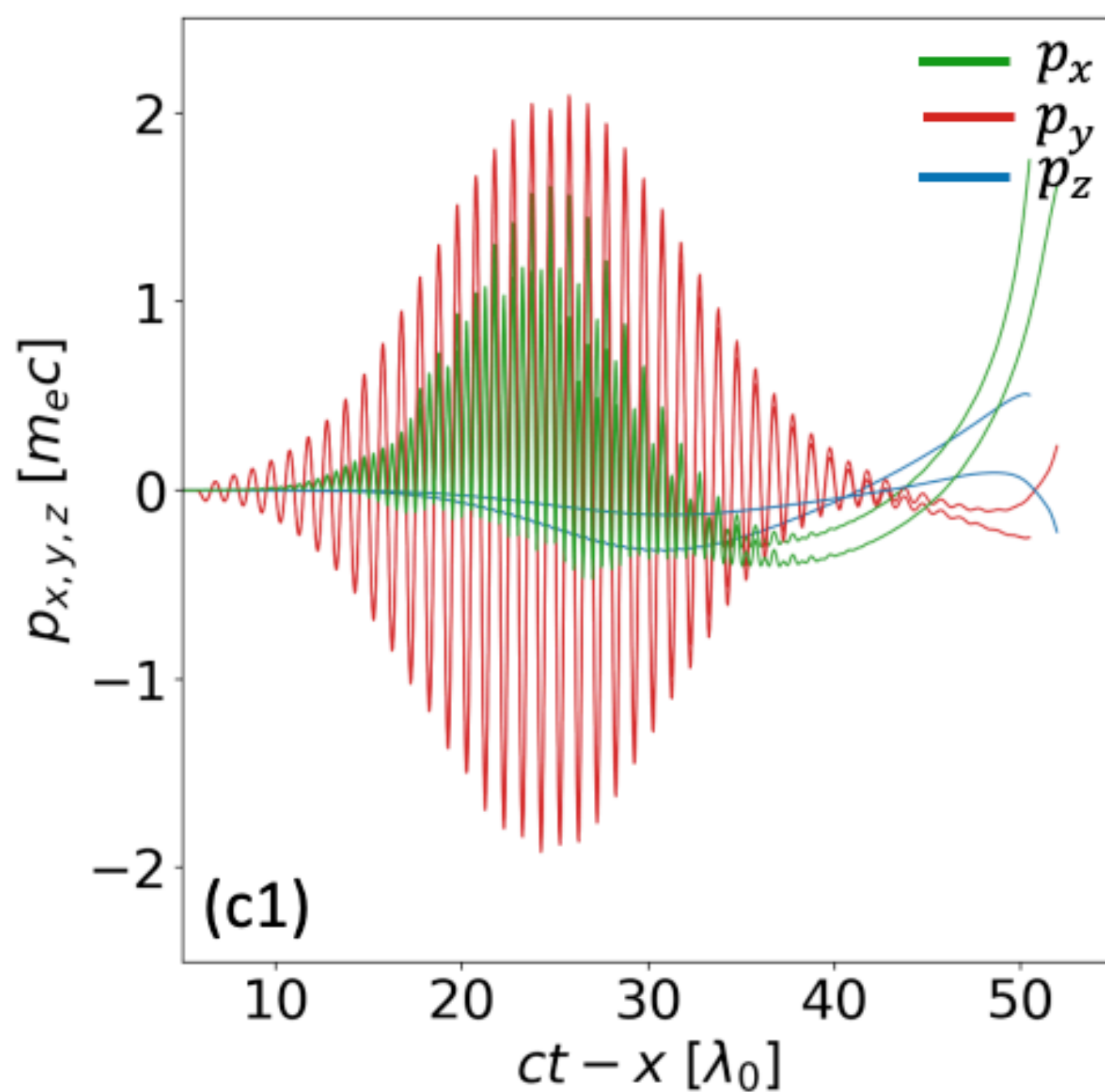


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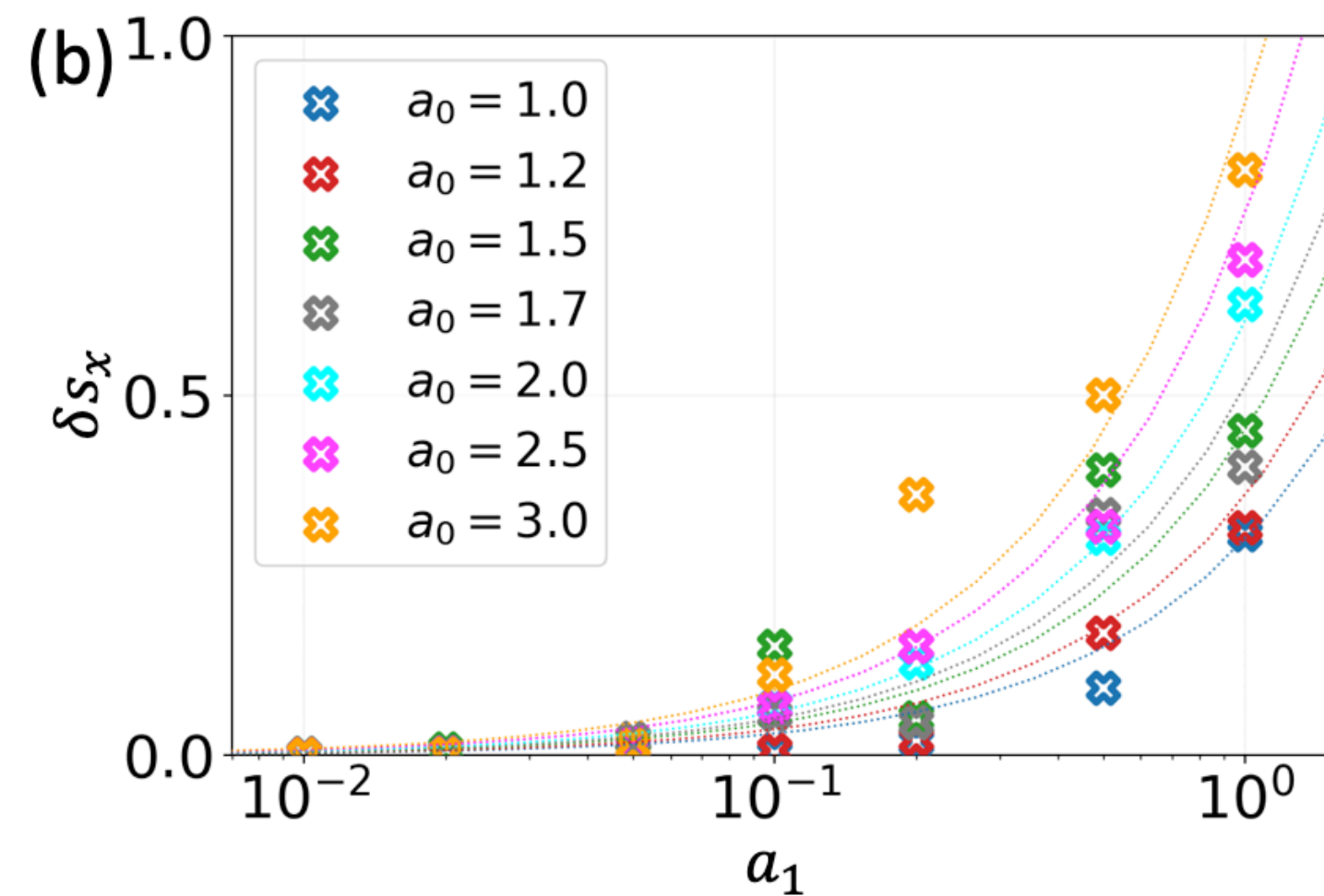
Stochastic motion 😞



Spin evolution in colliding pulse injection

Stochastic motion in beatwave leads to stochastic spin evolution for some electrons

Test particles in 25 fs plane waves

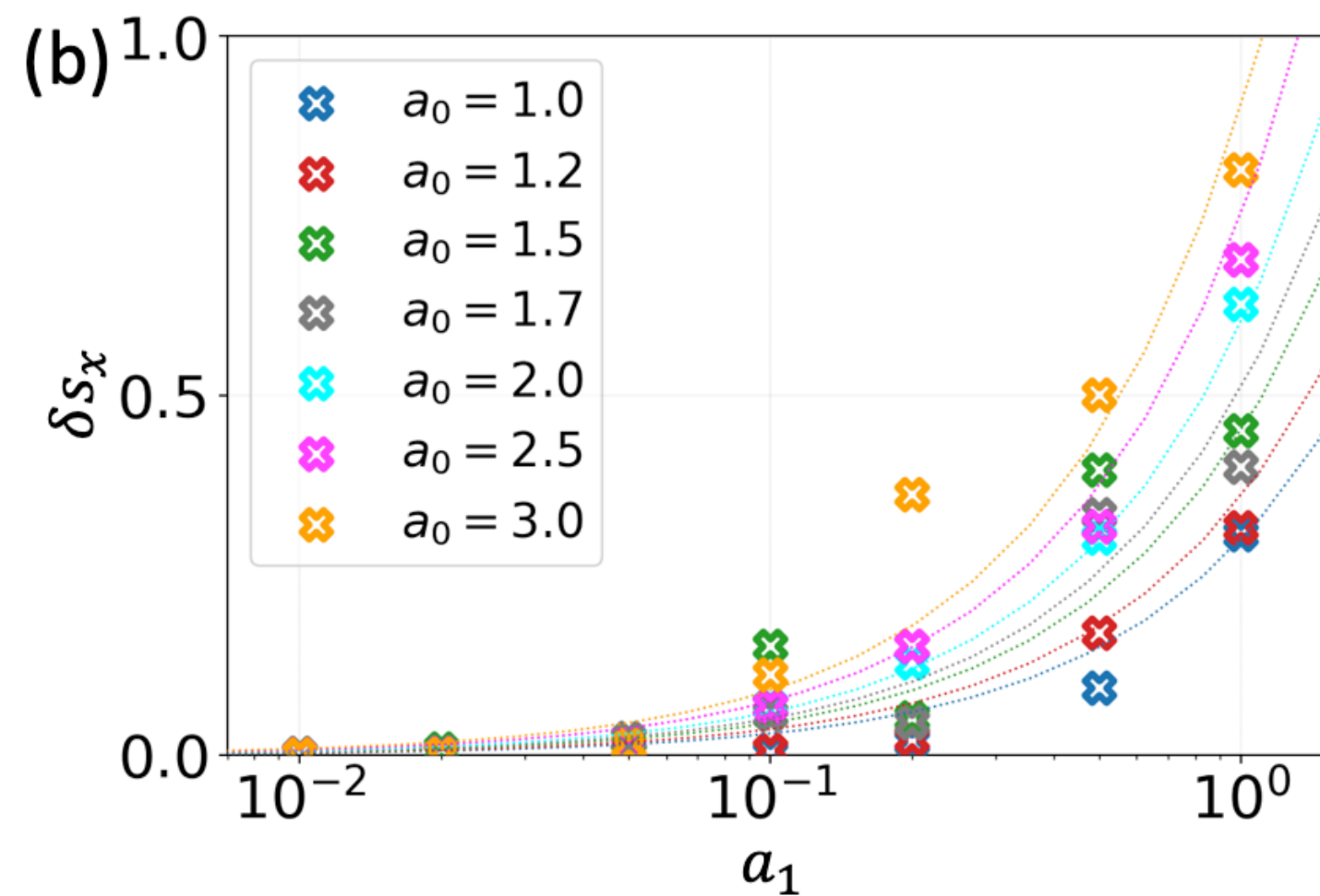


$$\delta s_z \equiv 1 - s_z = 0.25a_0a_1$$

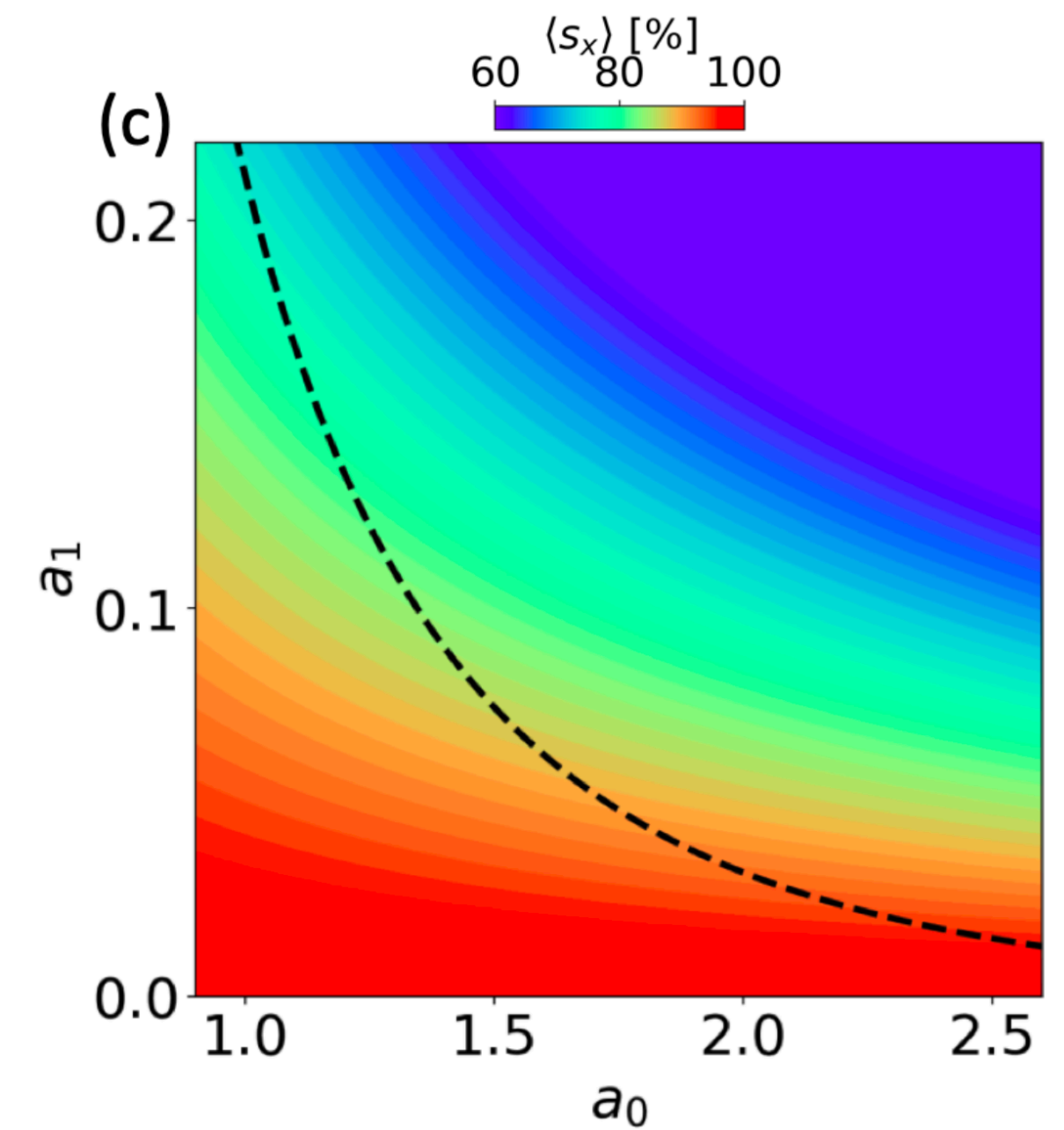
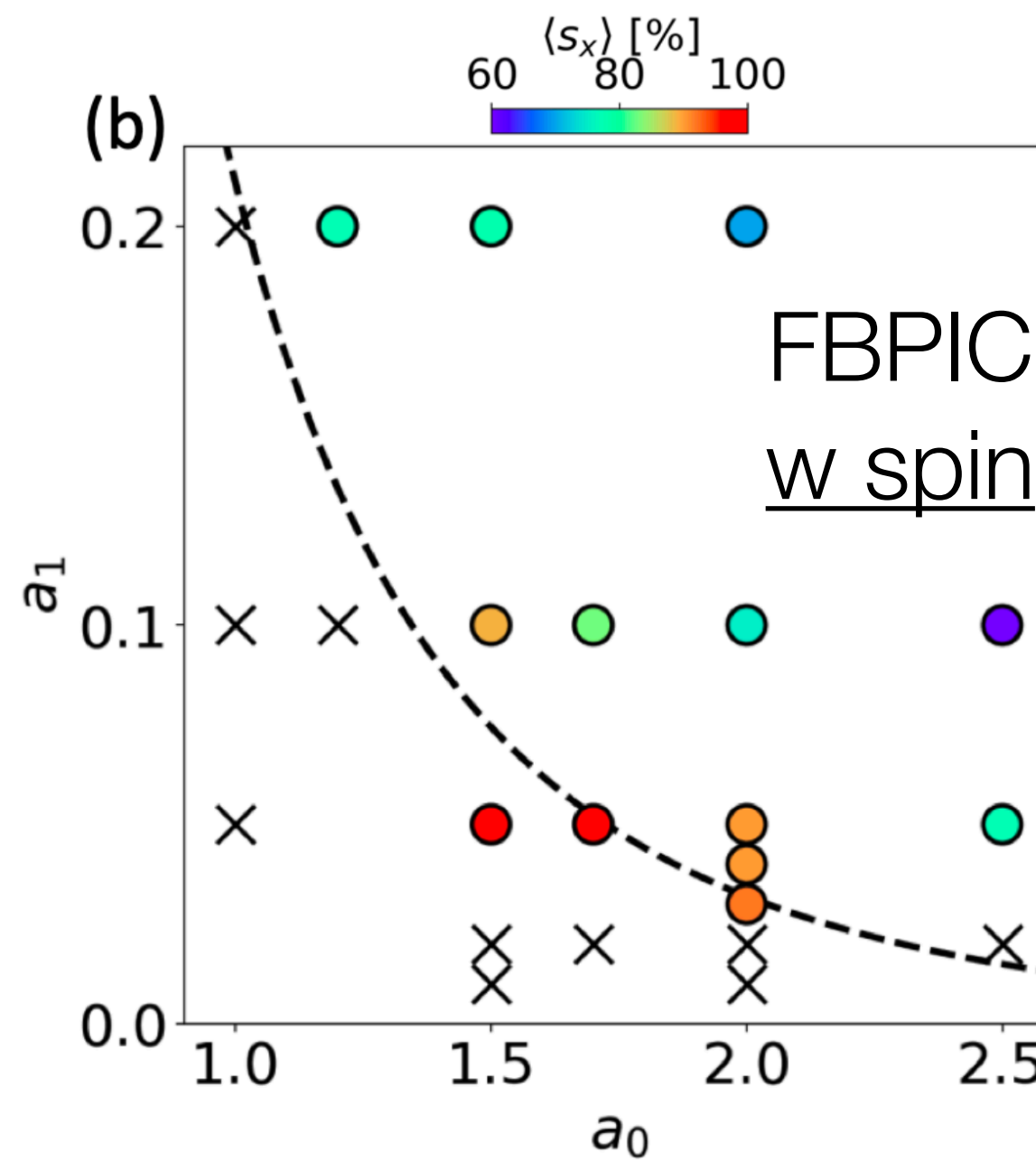
Spin evolution in colliding pulse injection

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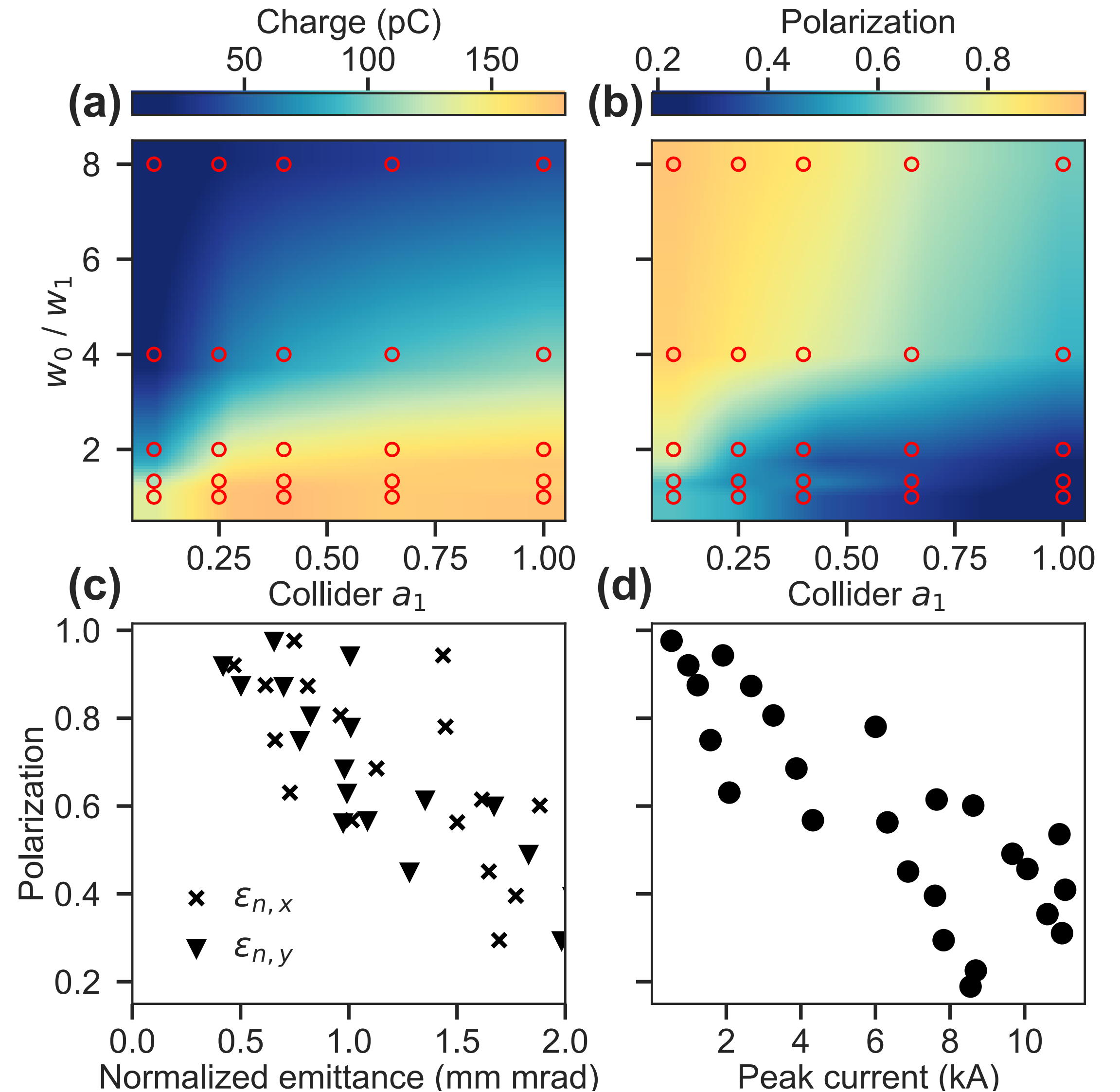


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Colliding pulse injection creates high-current polarised beams

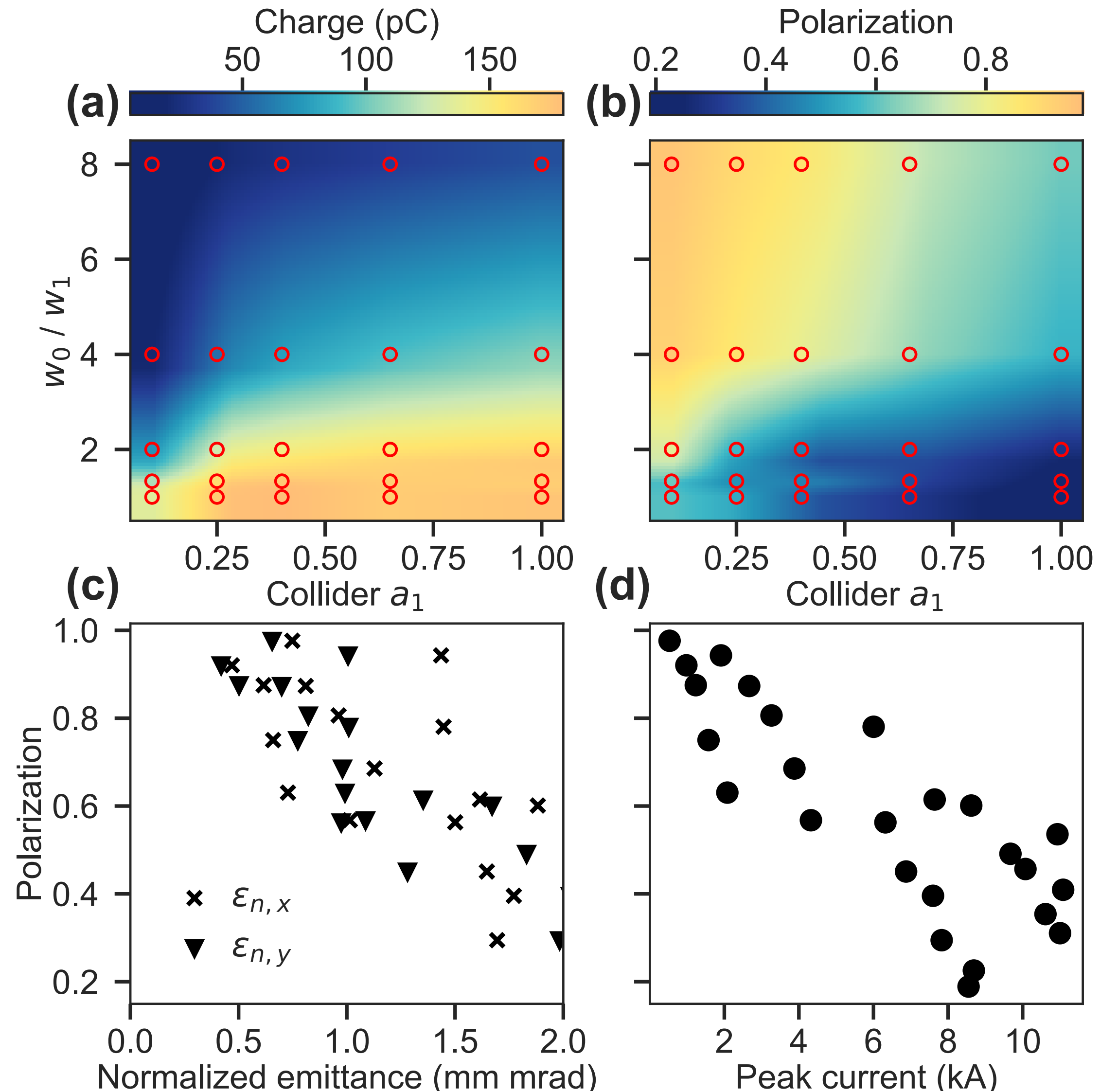
Control over the driver and collider laser enables balancing charge and polarisation degree



Colliding pulse injection creates high-current polarised beams

Control over the driver and collider laser enables balancing charge and polarisation degree

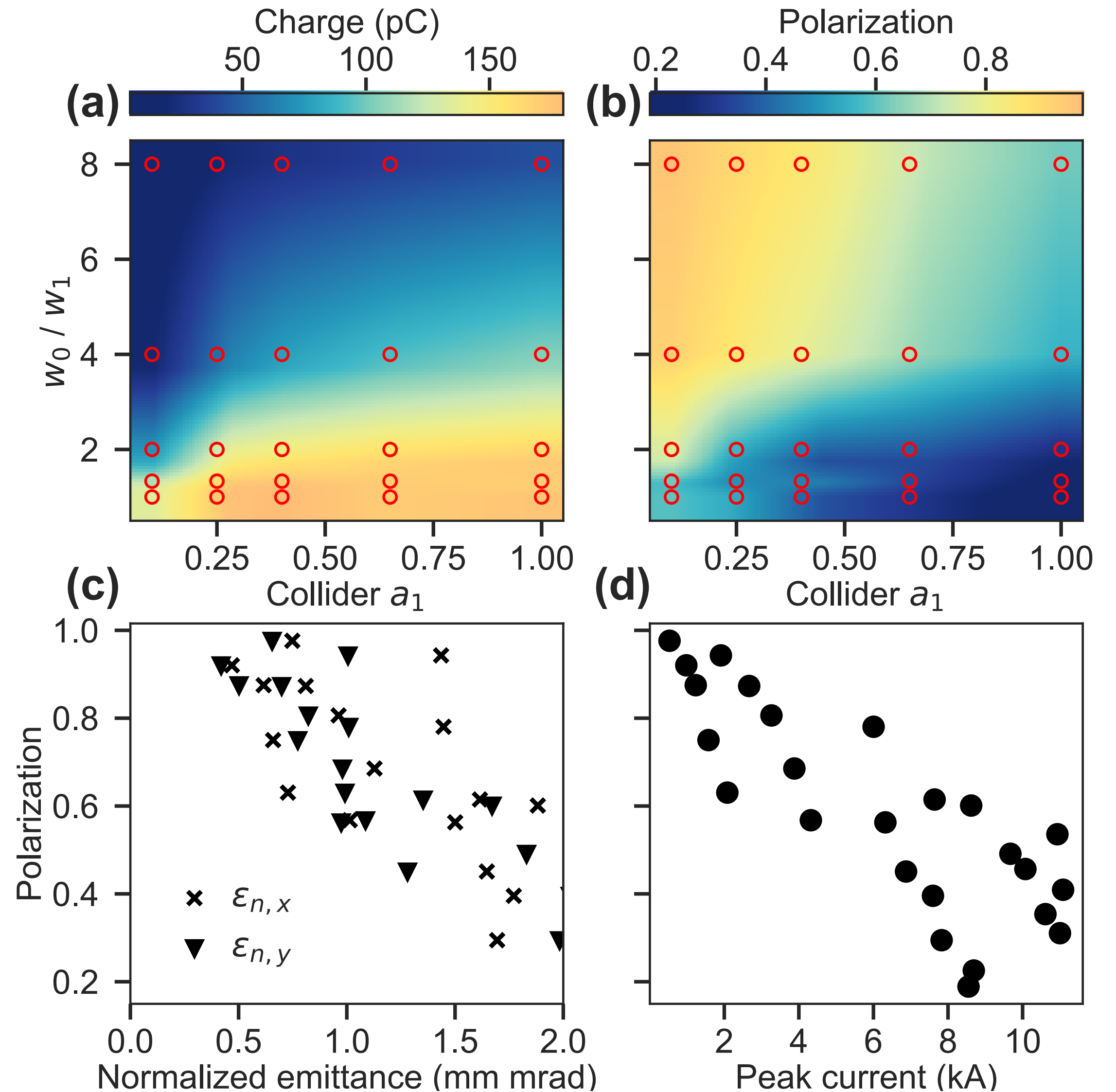
> Without any optimisation, can get



Colliding pulse injection creates high-current polarised beams

Control over the driver and collider laser enables balancing charge and polarisation degree

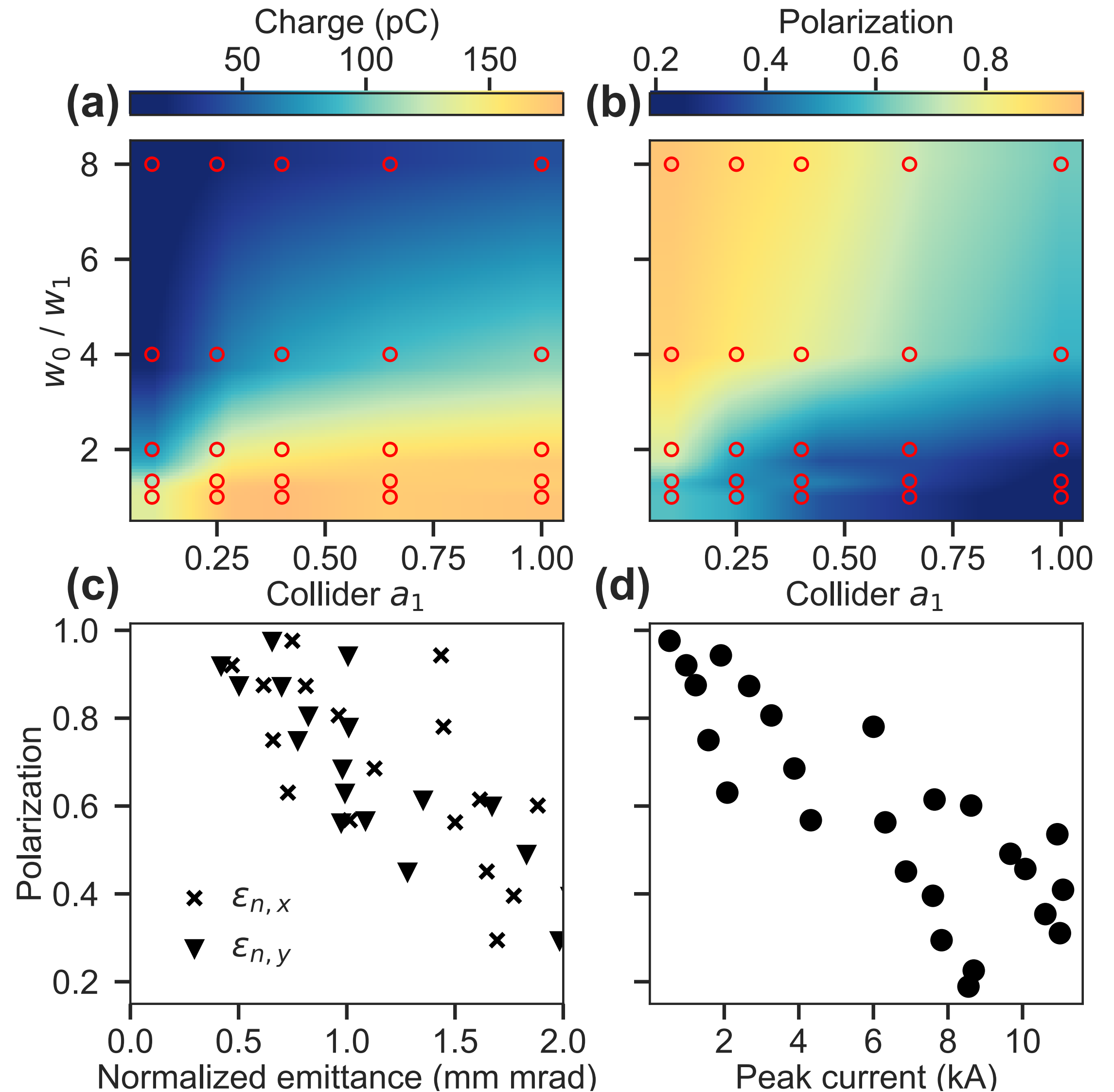
- > Without any optimisation, can get
- > Highly polarised (>90%) beams



Colliding pulse injection creates high-current polarised beams

Control over the driver and collider laser enables balancing charge and polarisation degree

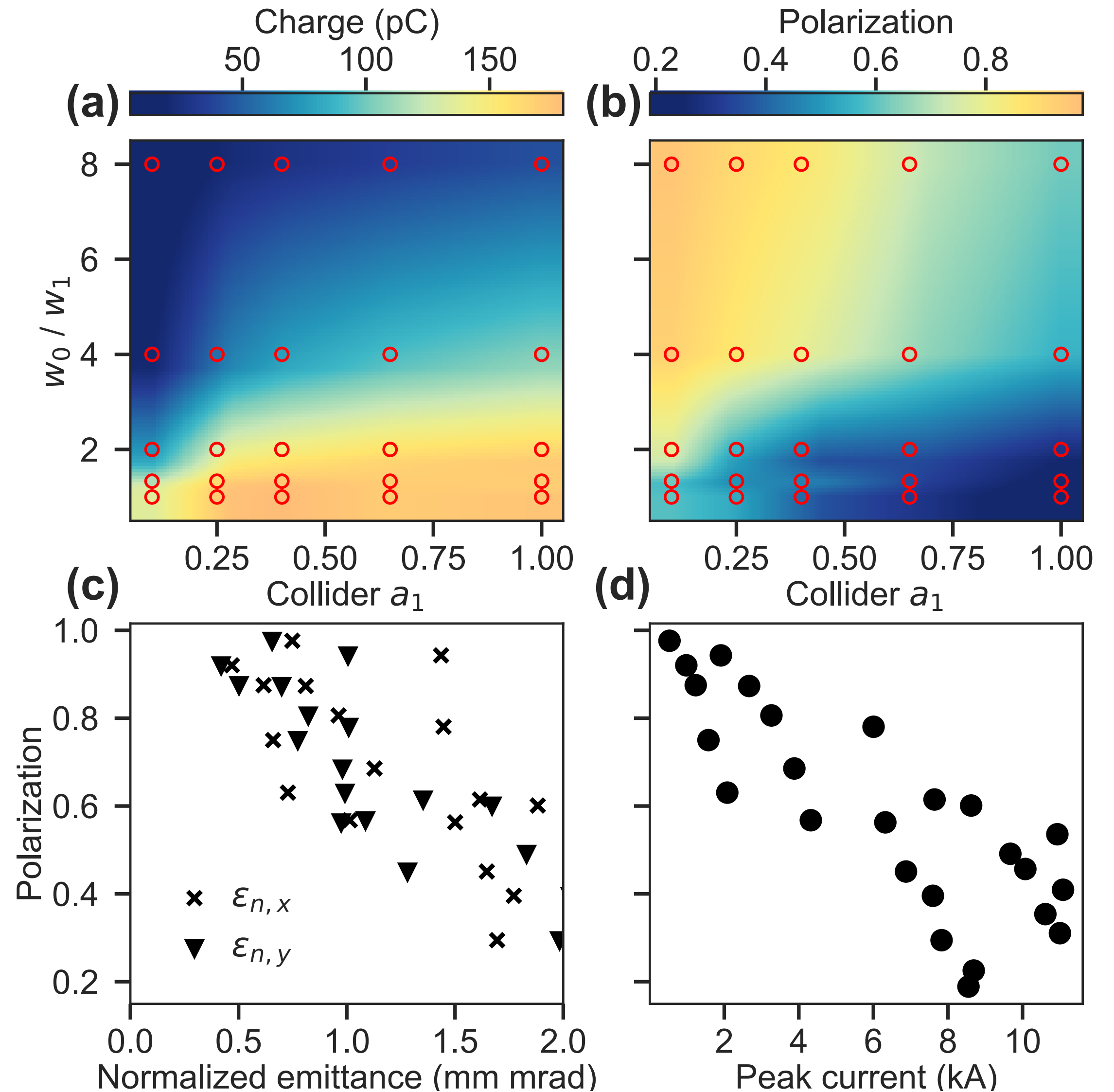
- > Without any optimisation, can get
- > Highly polarised (>90%) beams
- > Sub-micron emittance



Colliding pulse injection creates high-current polarised beams

Control over the driver and collider laser enables balancing charge and polarisation degree

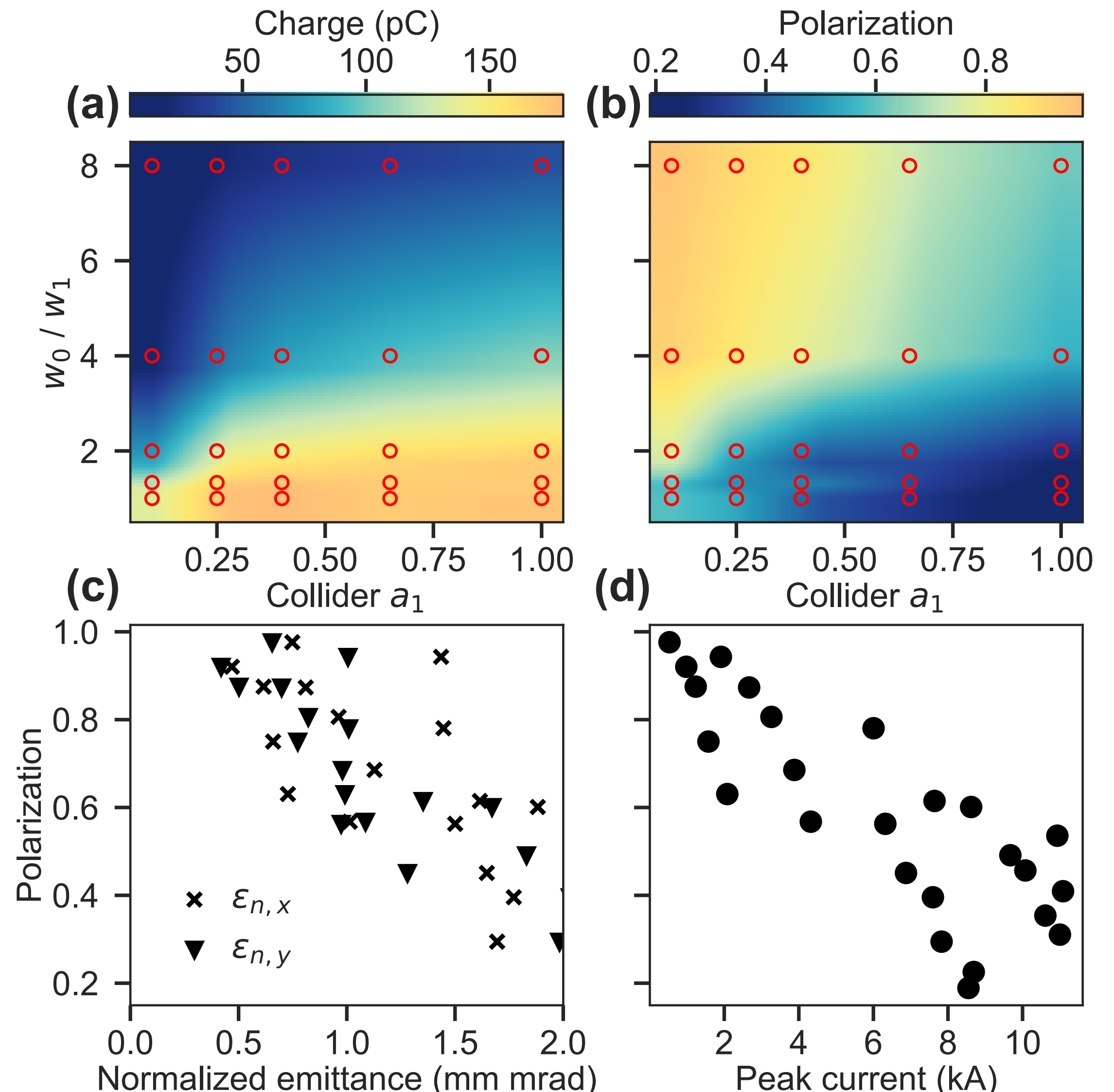
- > Without any optimisation, can get
- > Highly polarised (>90%) beams
- > Sub-micron emittance
- > 6kA with 80% polarisation



Colliding pulse injection creates high-current polarised beams

Control over the driver and collider laser enables balancing charge and polarisation degree

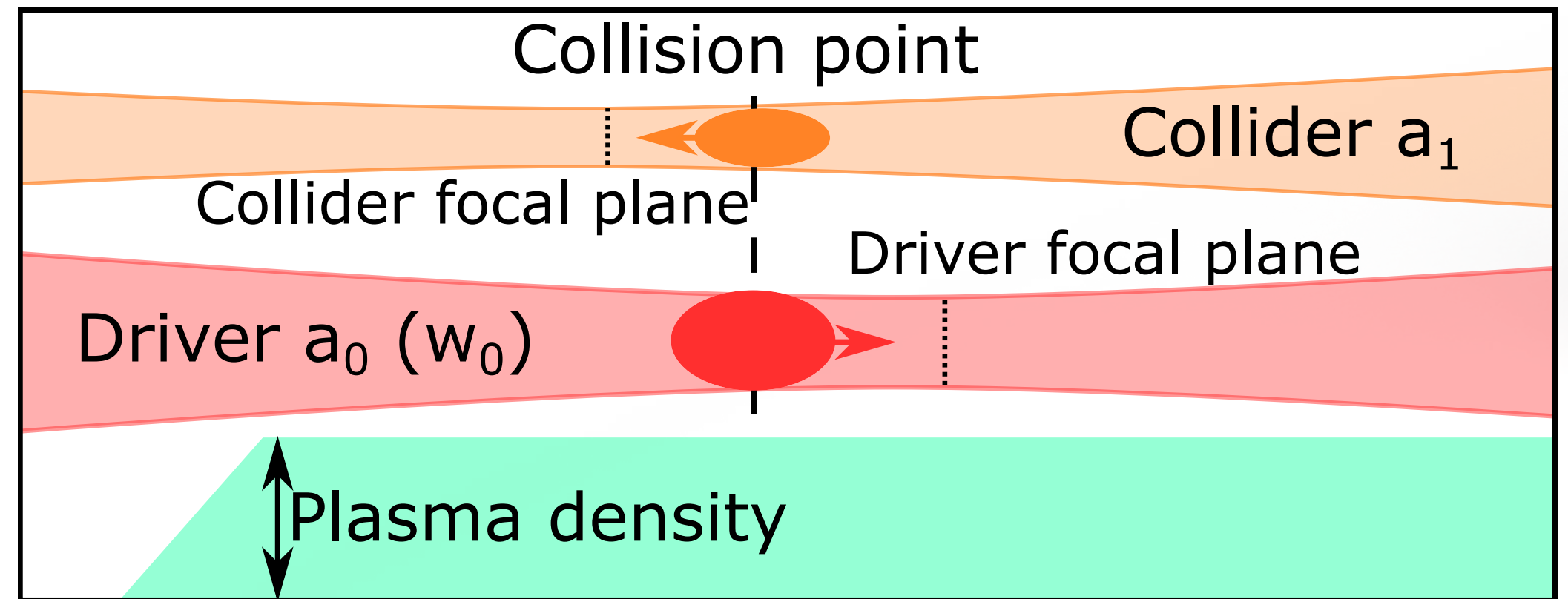
- > Without any optimisation, can get
 - > Highly polarised (>90%) beams
 - > Sub-micron emittance
 - > 6kA with 80% polarisation
- > Charge and polarisation interdependent
- > Extra charge injected with lowered polarisation



Colliding pulse scheme is highly optimisable

High amount of easily controllable degrees of freedom enable precision tuning and optimisation

- > Using OPTIMAS⁽¹⁾ library for Bayesian Optimisation, varying
 - > Collider a_1
 - > Driver a_0/w_0 with fixed $P=100$ TW
 - > Focal plane of the lasers
 - > Collision point in plasma
 - > Plasma density

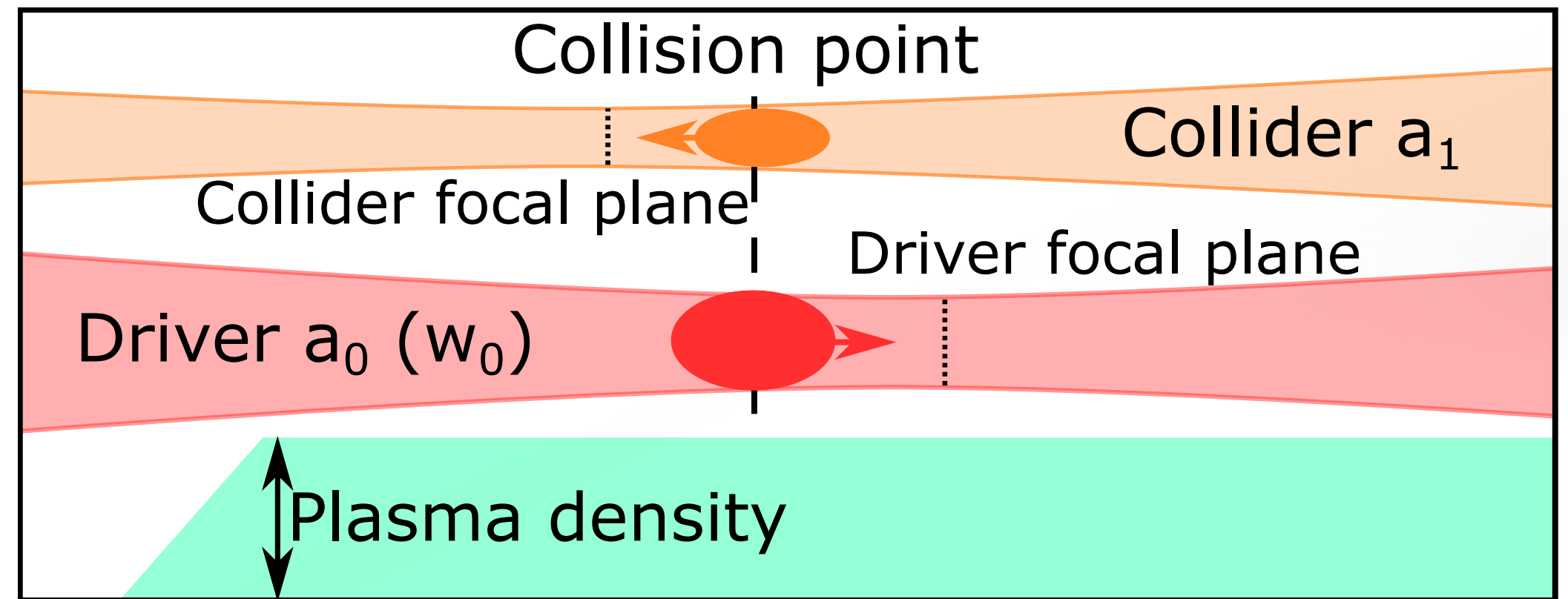


⁽¹⁾A. F. Pousa et al, PRAB **26**, 084601 (2023)

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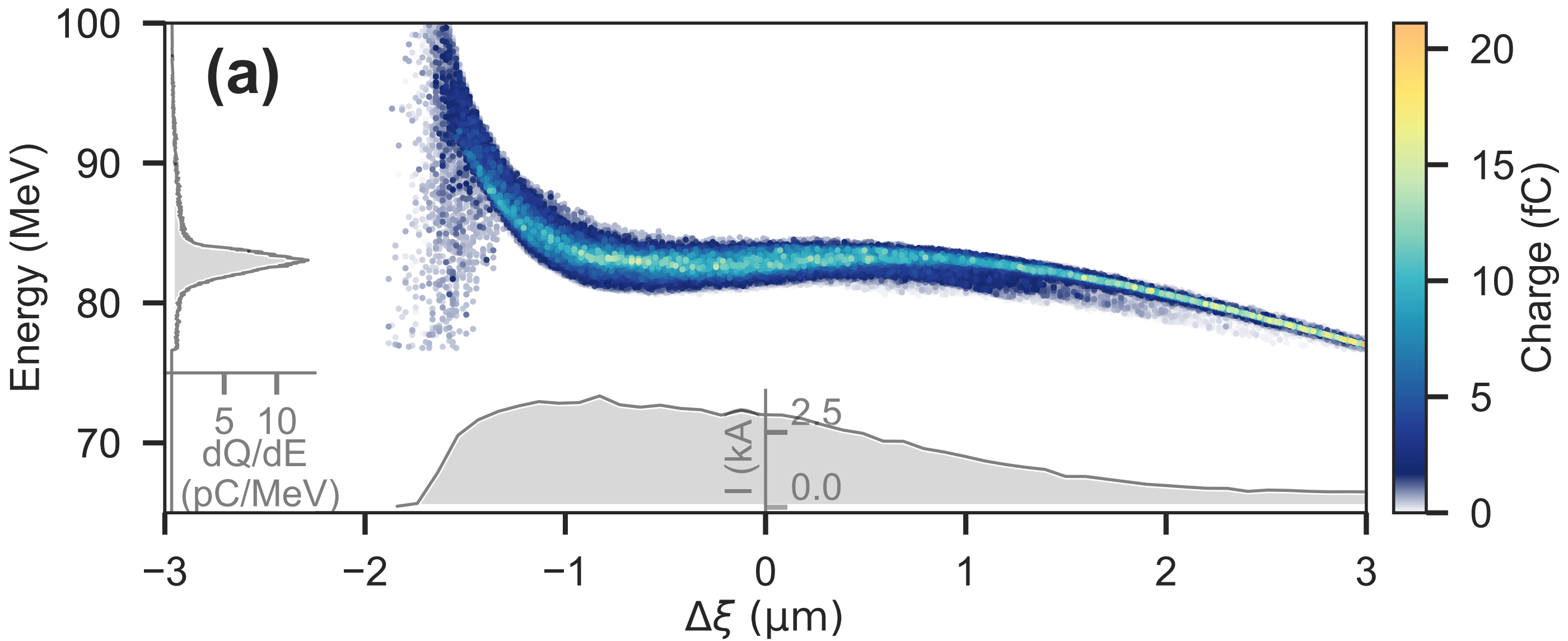


$$f = \frac{\sqrt{QE_m}}{\Delta E(1 - P)}$$

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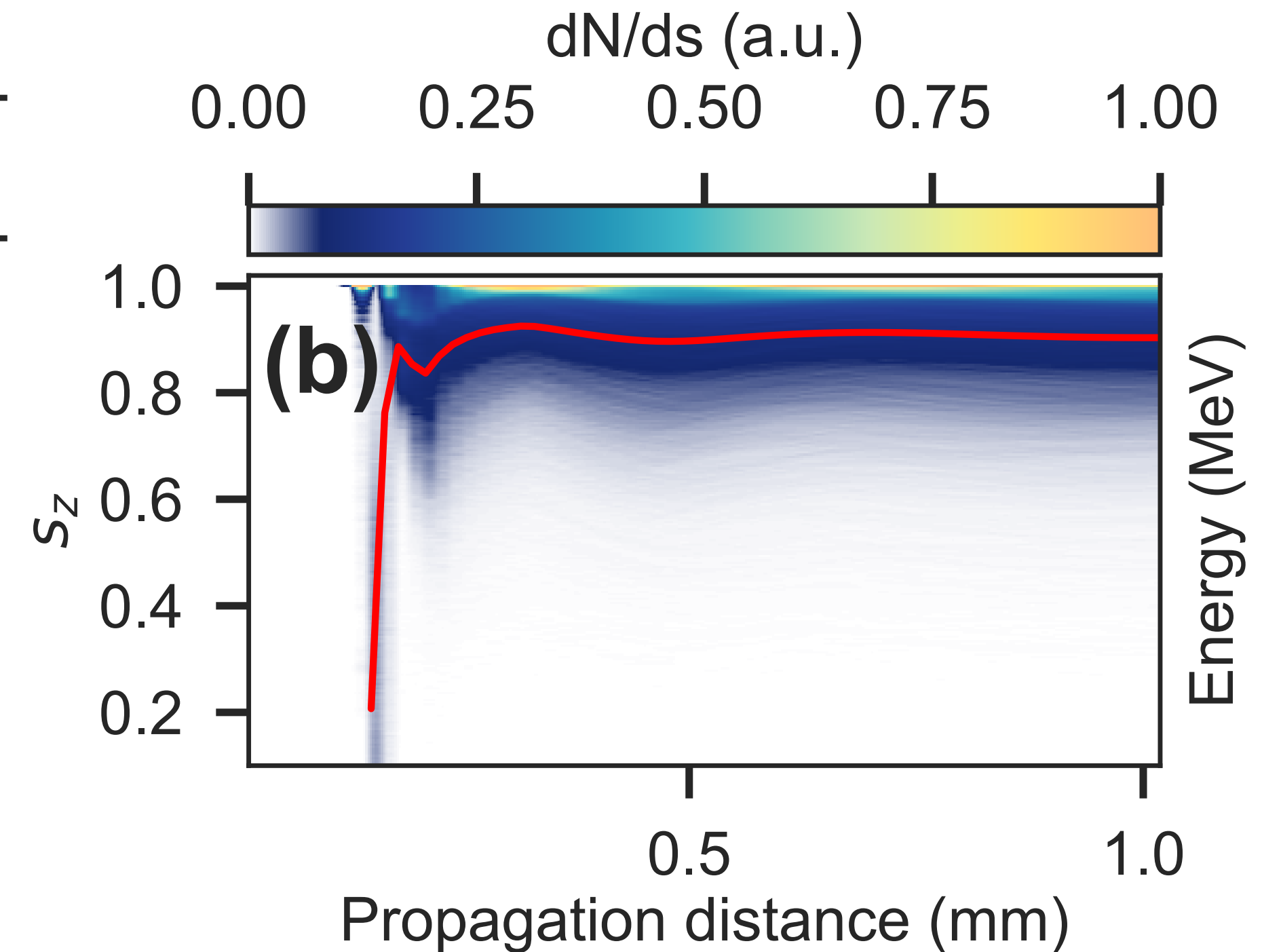
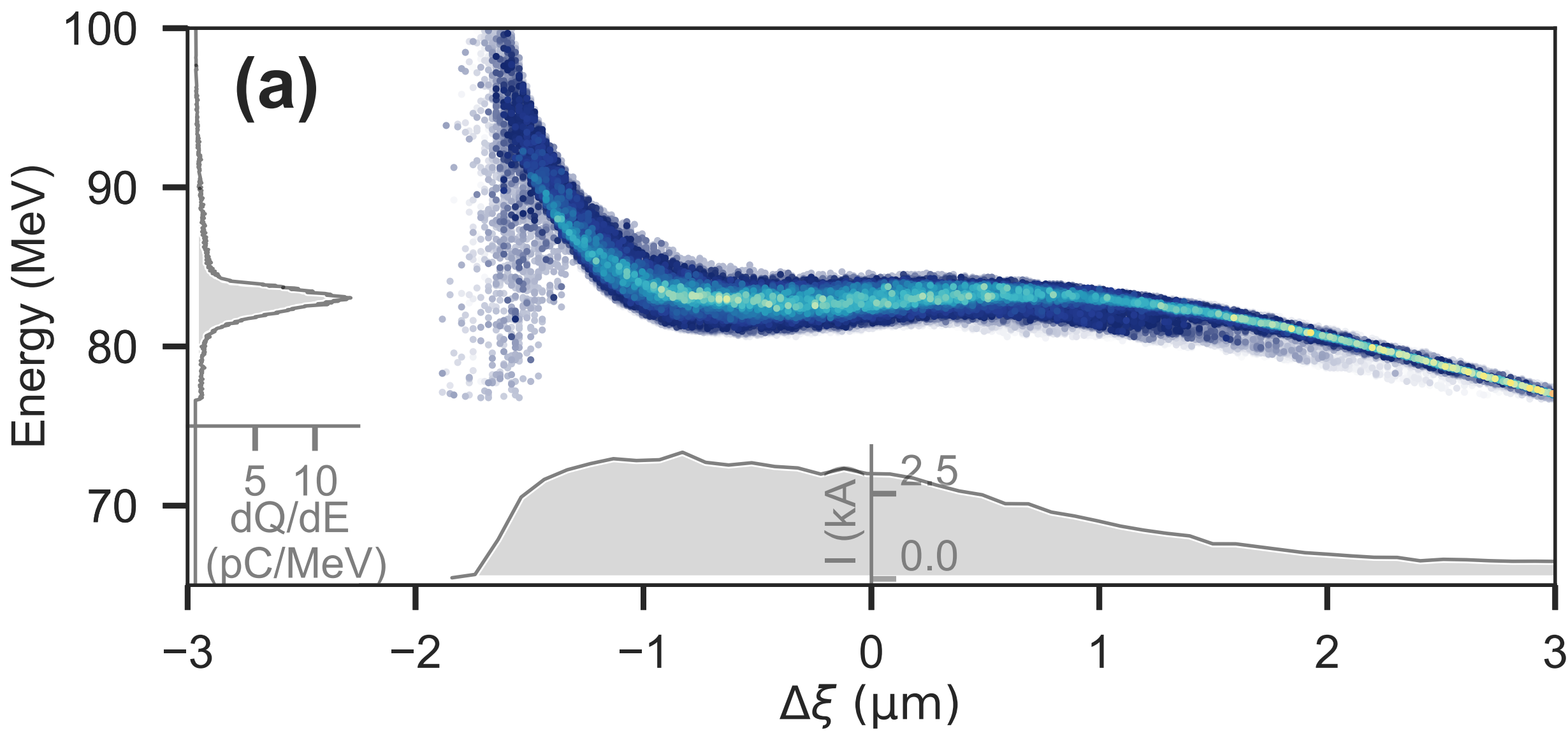
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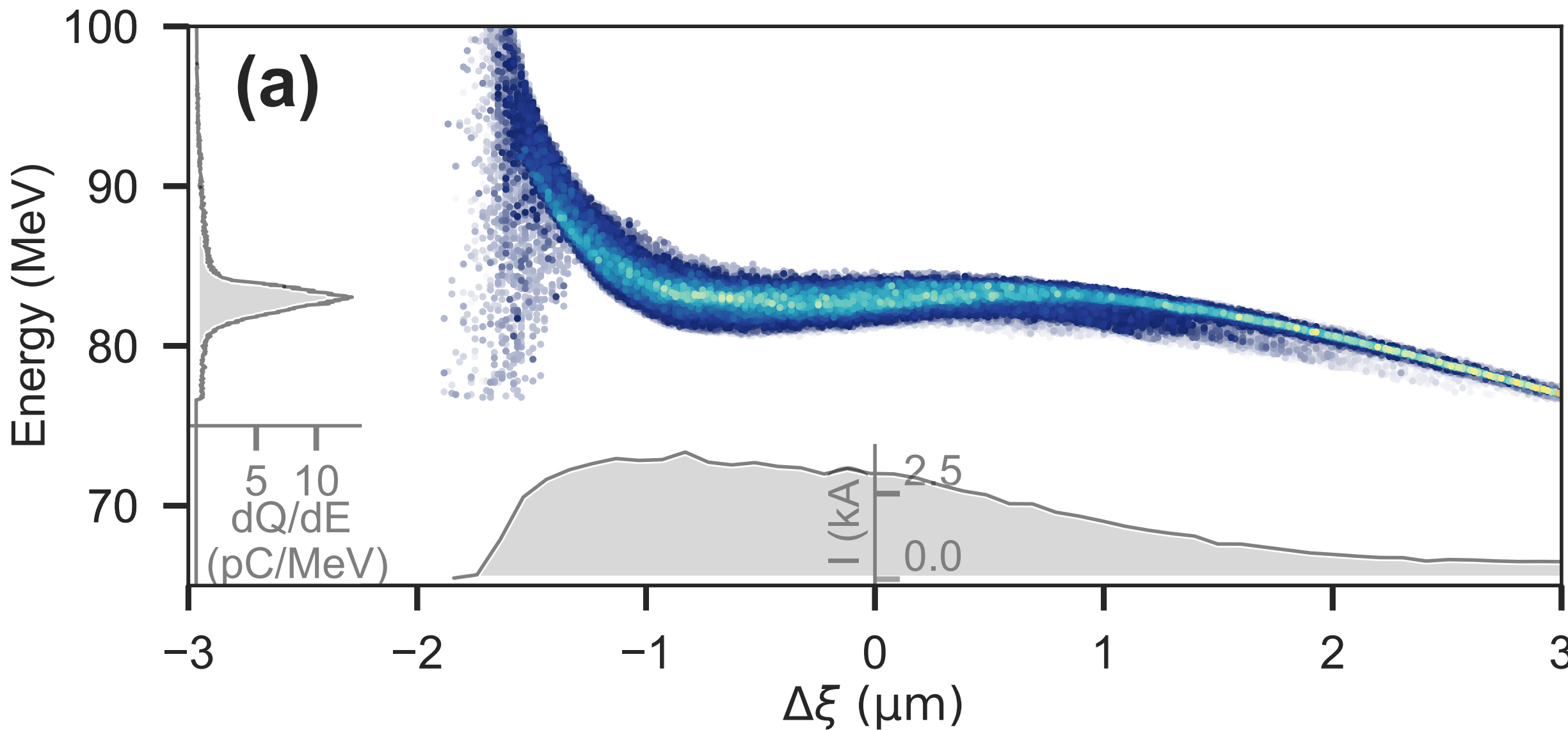
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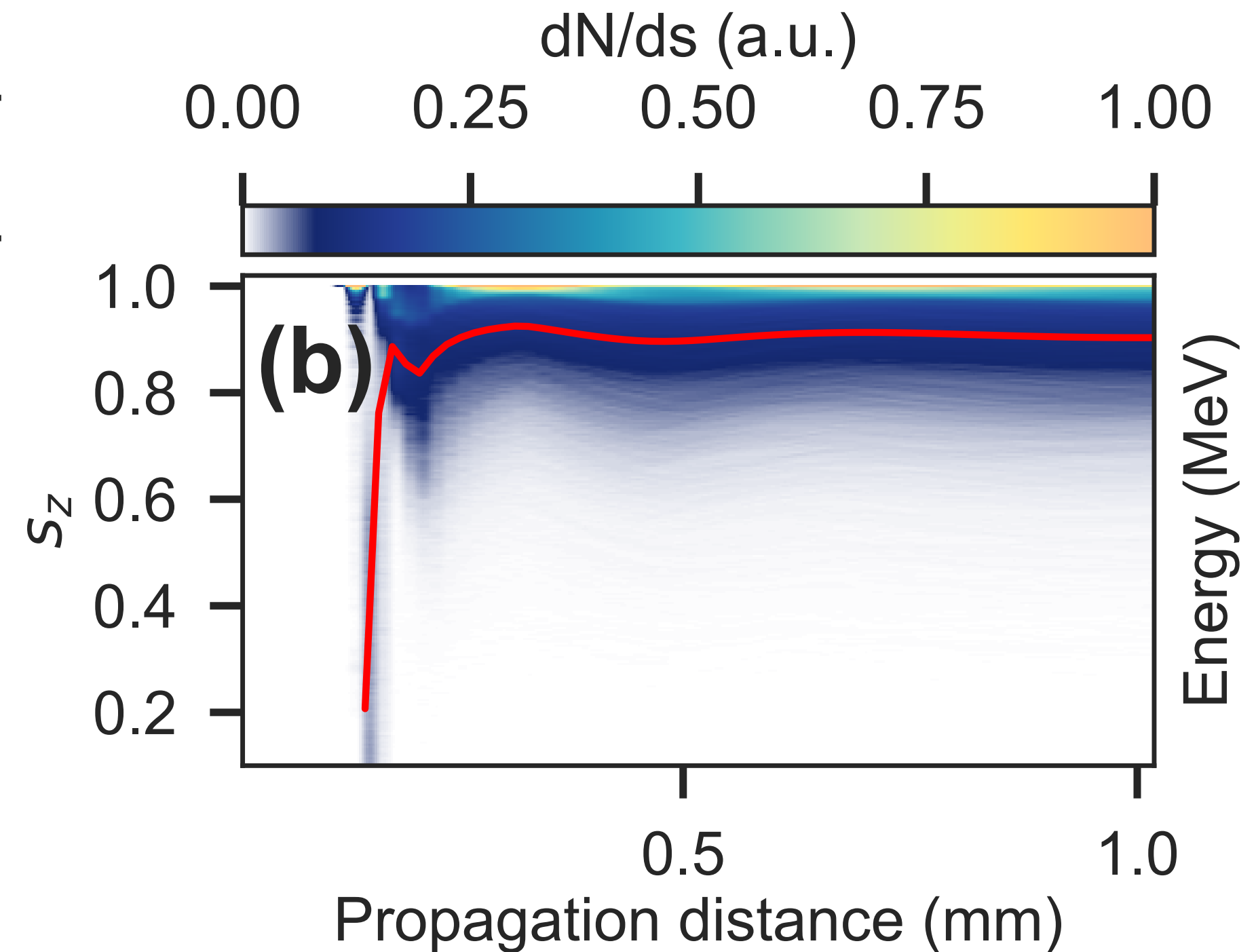


Colliding pulse scheme is highly optimisable

High amount of easily controllable degrees of freedom enable precision tuning and optimisation



Beam parameter	Value	Unit
Mean energy	85.2	MeV
Energy spread (rms)	4.4	%
Peak current	3.6	kA
Bunch duration (rms)	3.8	fs
Charge	31.8	pC
Normalized emittance, x plane	0.90	mm mrad
Normalized emittance, y plane	0.84	mm mrad
Spin polarization	0.90	

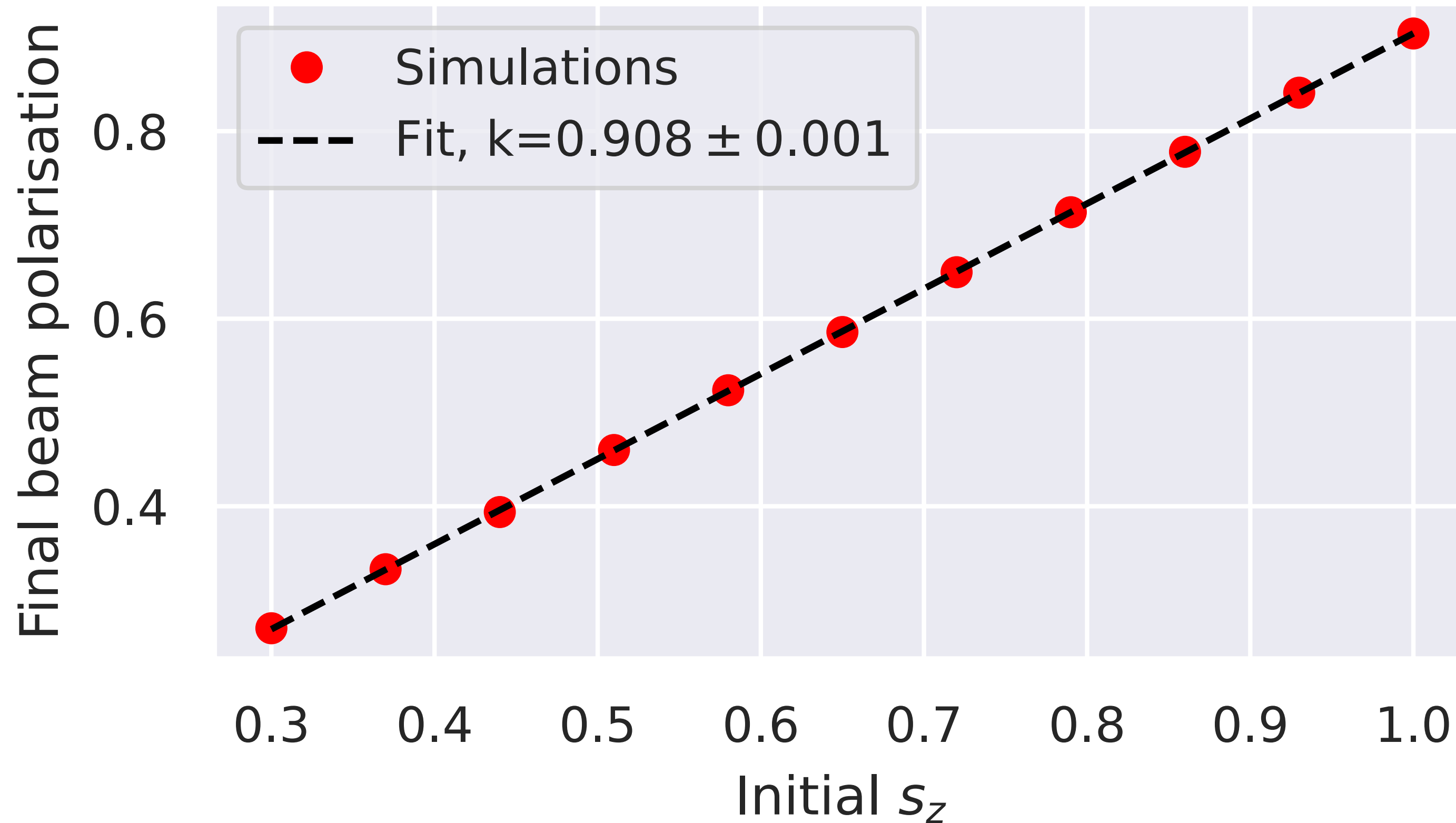


Optimised depolarisation enables first demonstrations

Isn't 100% pre-polarisation a little too optimistic?

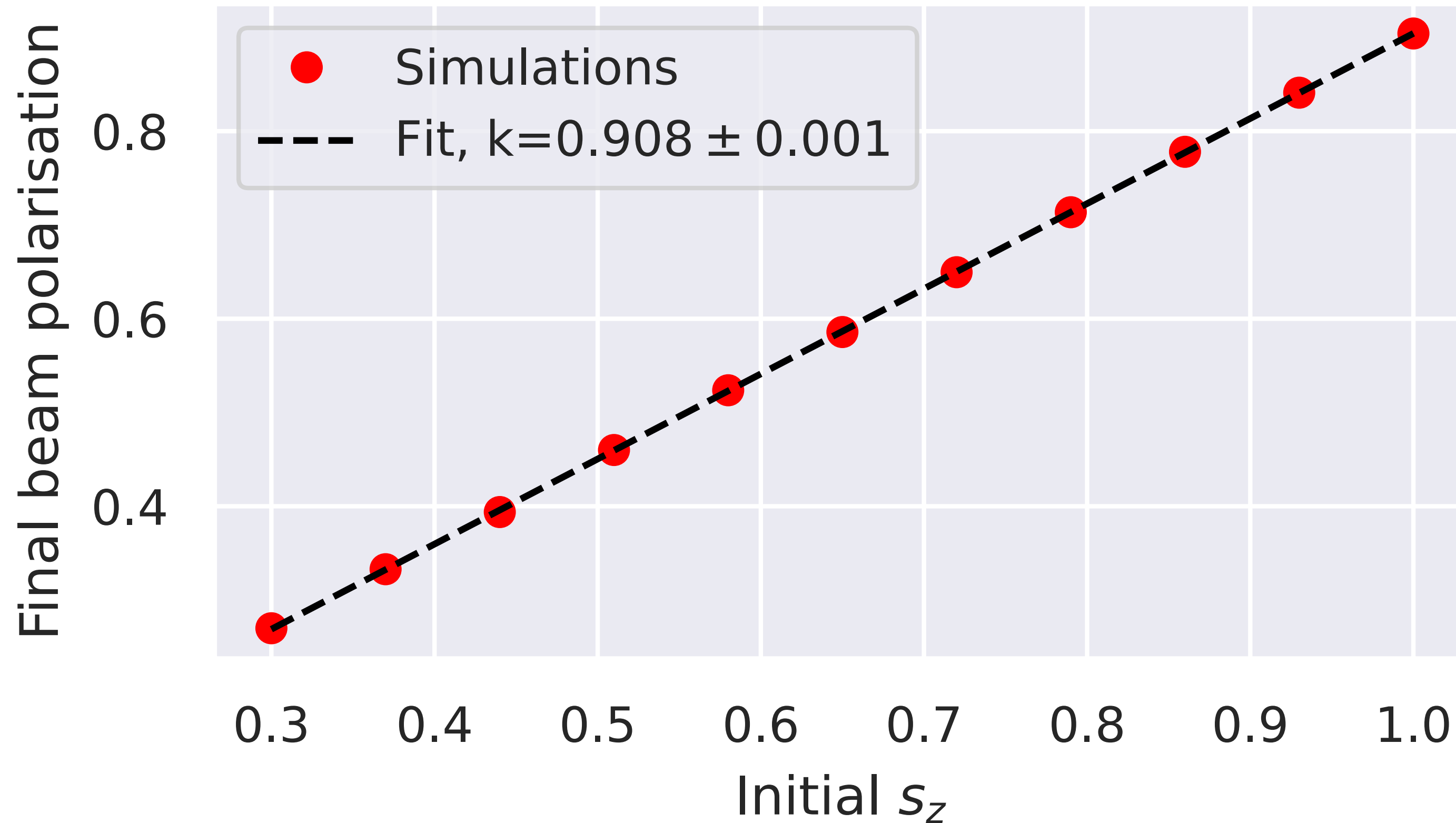
Optimised depolarisation enables first demonstrations

Lowered pre-polarisation simply leads to lower final polarisation



Optimised depolarisation enables first demonstrations

Lowered pre-polarisation simply leads to lower final polarisation



Enables first demo experiments with lower initial pre-polarisation giving detectable polarisation!

Colliding pulse injection for high-quality polarised beams

Realistic pathway to polarised laser-plasma accelerators

- > LPA-based polarised electron sources possible based on pre-polarisation technique
- > Colliding pulse injection enables
 - > High overall polarisation
 - > High-quality beam generation
 - > Wide tunability and many tuning knobs for optimisation
- > The polarised colliding pulse scheme highly advantageous for near-term experiments!

