



# Recent progress in the modeling of laser wakefield acceleration

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# Acknowledgements

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## **Smilei development team**

A. Beck, G. Bouchard, M. Grech, M. Lobet, F. Pérez, C. Prouveur,  
T. Vinci

## **EARLI Project**

D. F. G. Minenna, L. Batista, B. Cros, C. Simon-Boisson, S.  
Bethuys, B. Bolzon, A. Jeandet, S. Marini, I. Moulanier, P. A. Phi  
Nghiem, N. Pichoff, S. Ricaud, and C. Simon

## **AWAKE Project**

P. Muggli, E. Gschwendter, J. Farmer



# Outline

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- Motivation: multi-stage laser wakefield acceleration (LWFA)
- Reconstruction of the laser field -> Realistic simulations
- Fast modelling of LWFA: envelope modeling
  - adding ionization
  - adding perfectly matched layer boundary conditions
  - reducing the effects of Numerical Cherenkov radiation
- Fast PIC modelling: Smilei on GPU
- Fast dataset generation, optimization



# Motivation: multi-stage LWFA



# Multi-stage laser wakefield acceleration: let's start from 2 stages

~100 MeV, ~ some mm

>10 GeV, ~ 1-10 cm



Plasma stage #1



Plasma stage #2

Laser pulse #1

Laser pulse #2



# Multi-stage laser wakefield acceleration: let's start from 2 stages

~100 MeV, ~ some mm

>10 GeV, ~ 1-10 cm



Plasma stage #1



Plasma stage #2

Laser pulse #1

Laser pulse #2

## Modeling:

- Fluid simulation of plasma formation
- PIC simulation of injection and acceleration

## Challenges:

- Long simulation
- Numerical Cherenkov radiation
- Realistic simulations

## Modeling:

- Beam dynamics simulation for beam transport

## Challenges:

- Interface between PIC codes

## Modeling:

- Fluid simulation of channel formation
- PIC simulation of injection and acceleration

## Challenges:

- Even longer simulation
- Numerical dephasing
- Boundary conditions
- Numerical Cherenkov radiation
- Realistic simulations

Addressed  
in this talk

F. Massimo, EAAC23



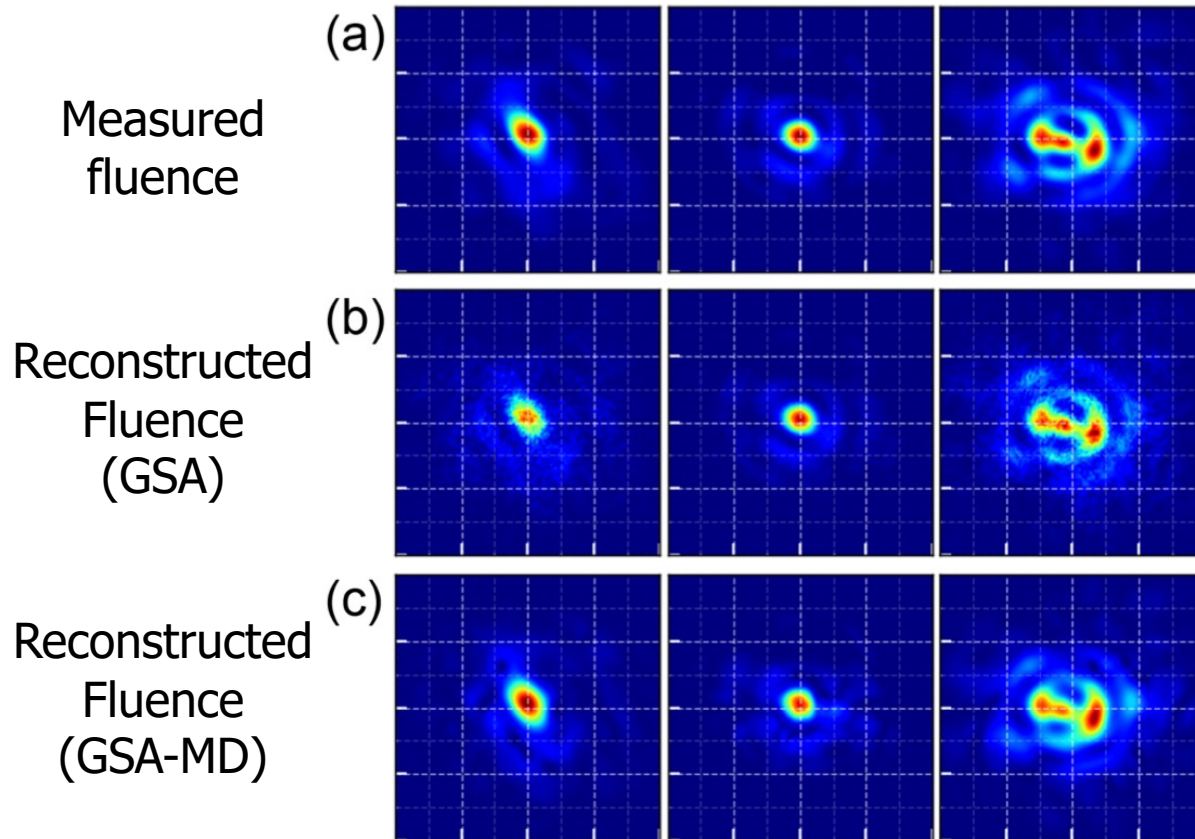
# Reconstruction of the laser field $\rightarrow$ realistic simulations



# Gerchberg-Saxton algorithm with modes decomposition (GSA-MD)



I. Moulanier et al., J. Opt. Soc. Am. B 40, 9, 2450-2461 (2023)



See I. Moulanier's poster!





# A deeper physical understanding with GSA-MD+PIC simulations



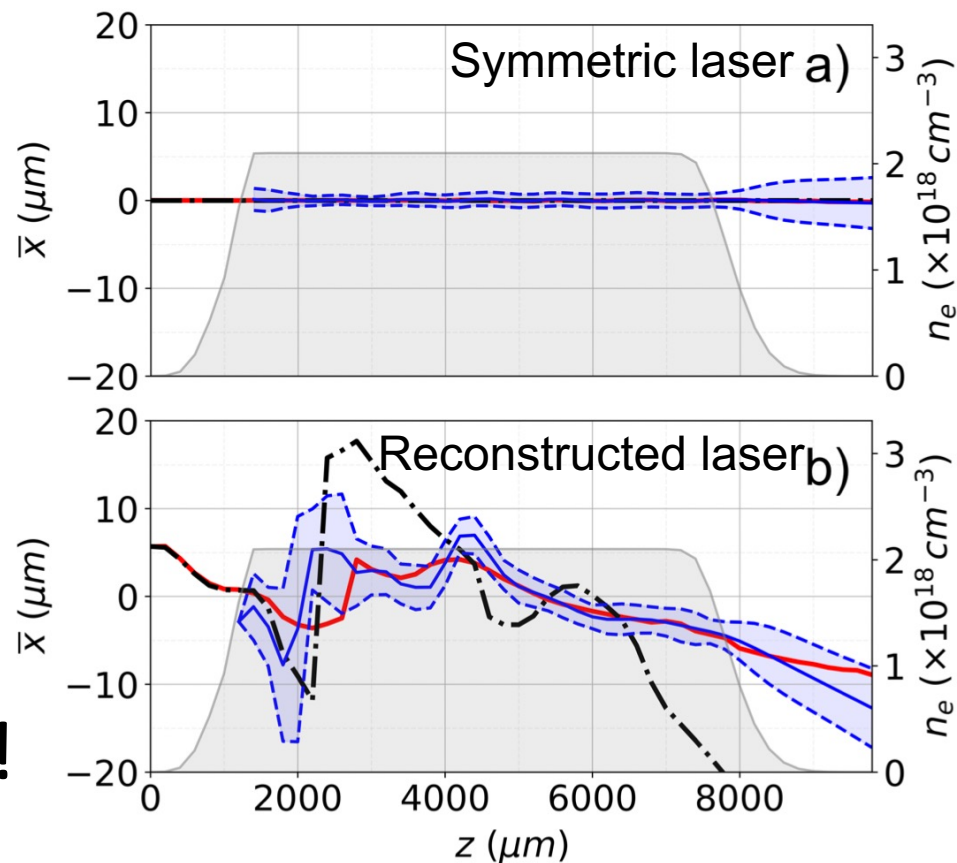
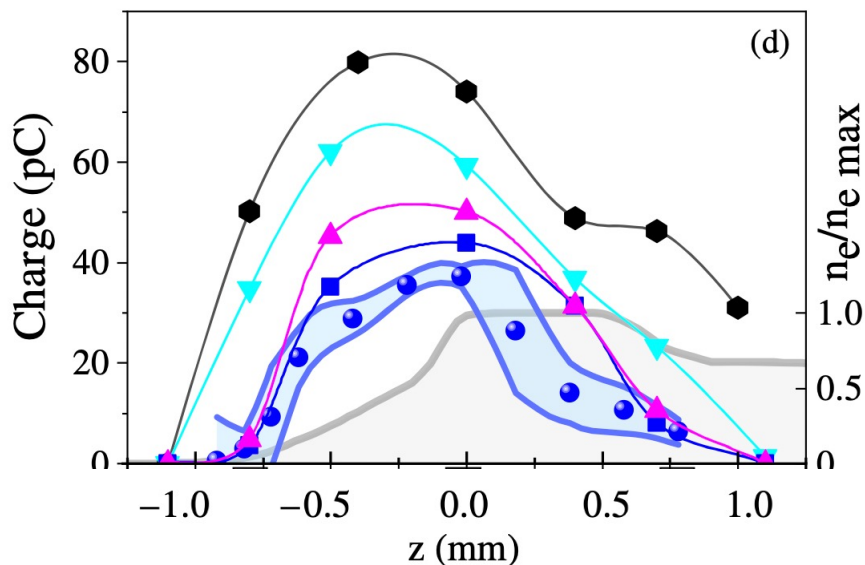
L. Dickson et al., Phys. Rev. Accel. Beams **25**, 101301 (2023)

I. Moulanier et al, Phys. Plasmas **30** (2023) 5, 053109

Experiment

Ideal laser simulation

Realistic laser simulation



See I. Moulanier's poster!



# Fast modeling of LWFA: envelope modeling and Smilei on GPU



# Smilei)

A collaborative, open source  
multi-purpose Particle in Cell code

<https://smileipic.github.io/Smilei/index.html>

## User-friendly

- online: documentation, tutorials
- Python input/output
- quick visualisation library
- teaching platform
- bi-annual training workshop

## High Performance

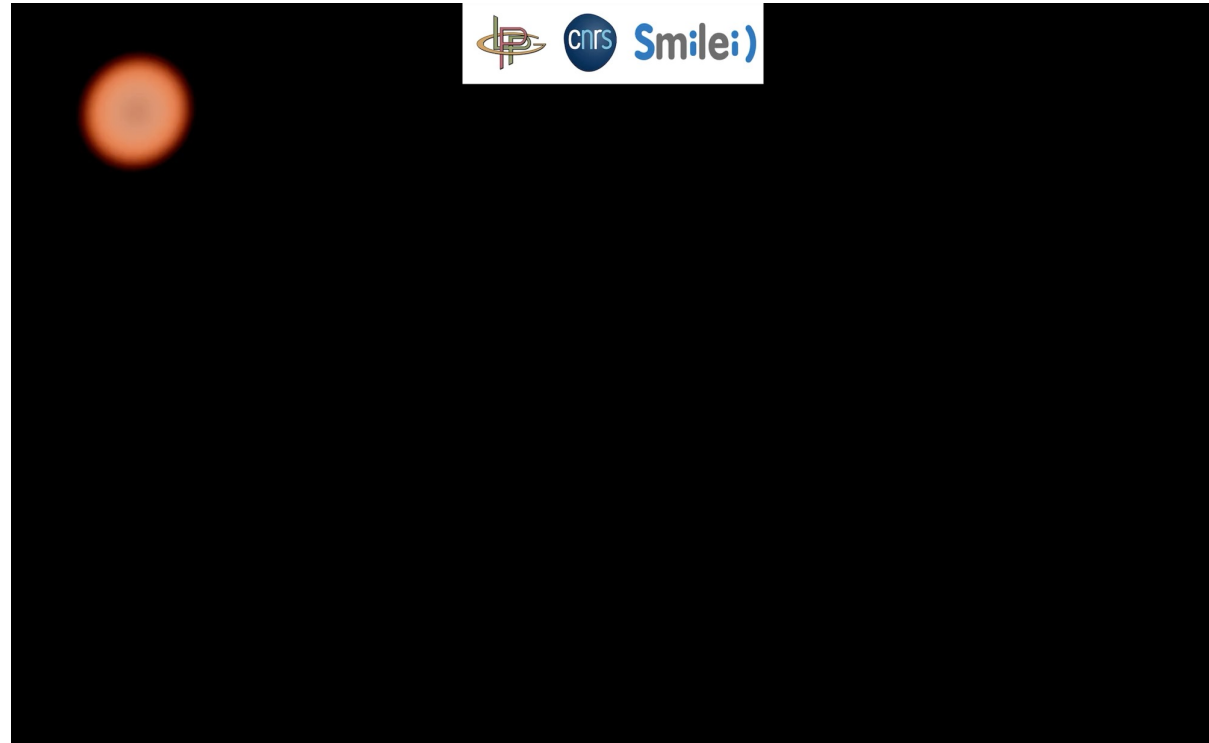
- MPI + OpenMP parallelization
- dynamic load balancing
- adaptive vectorization
- macro-particle merging

## Multi-physics

- 1D, 2D, 3D, quasi-3D geometries
- ionization, collisions
- strong-field QED
- laser envelope model
- envelope relativistic ADK ionization
- relativistic beam field initialization
- B-TIS3 anti-Cherenkov interpolation

## High quality

- developers: experts of physics and HPC
- continuously benchmarked
- GitHub bug reporting
- OpenPMD standard

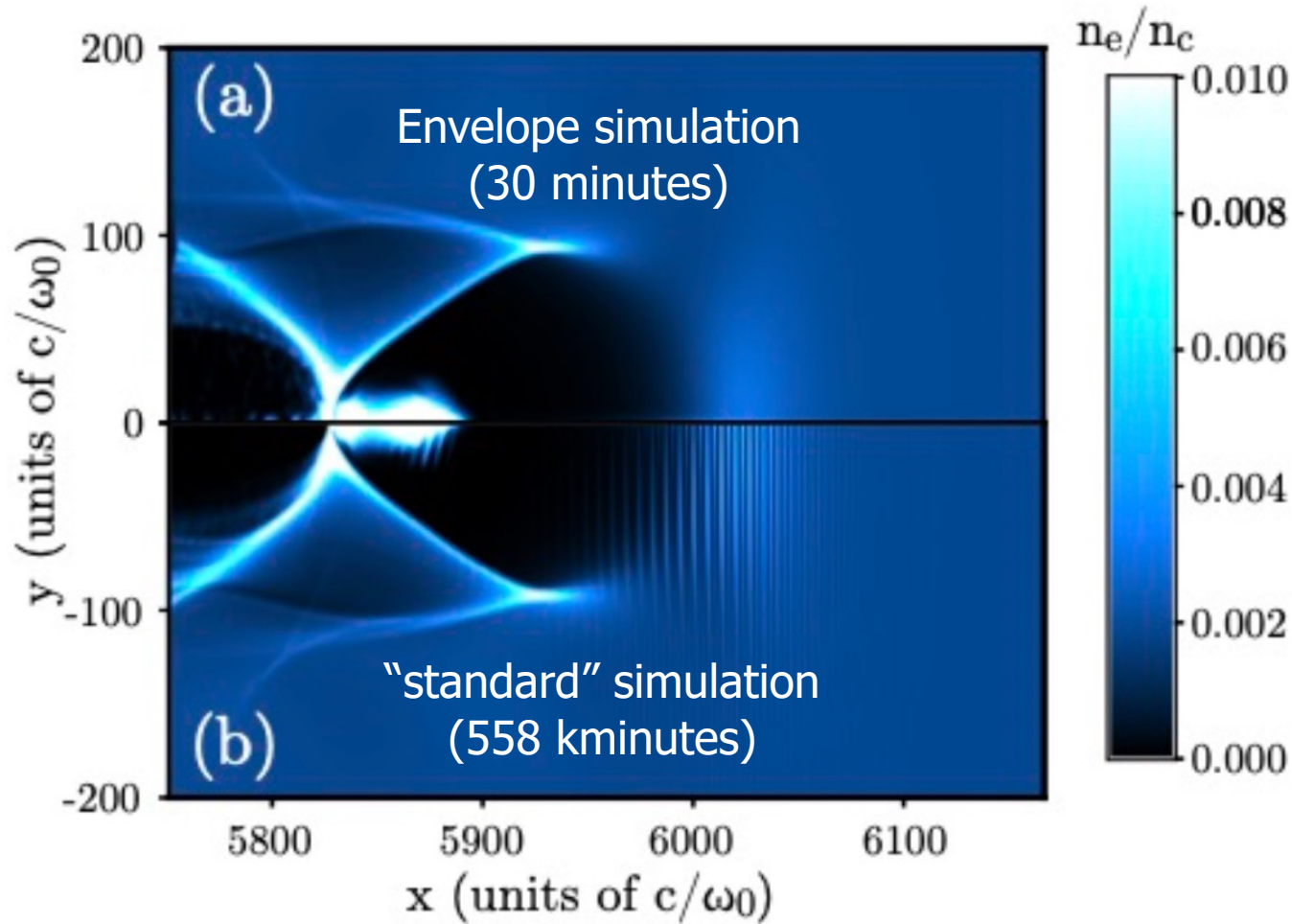


**Next Smilei Workshop: Prague, 8-10 Nov 2023**

<https://indico.math.cnrs.fr/event/9577/>

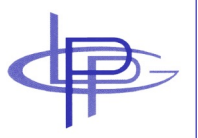


# Fast ionization modeling through a laser envelope model



F. Massimo et al., Phys. Rev. E **102**, 033204 (2023)

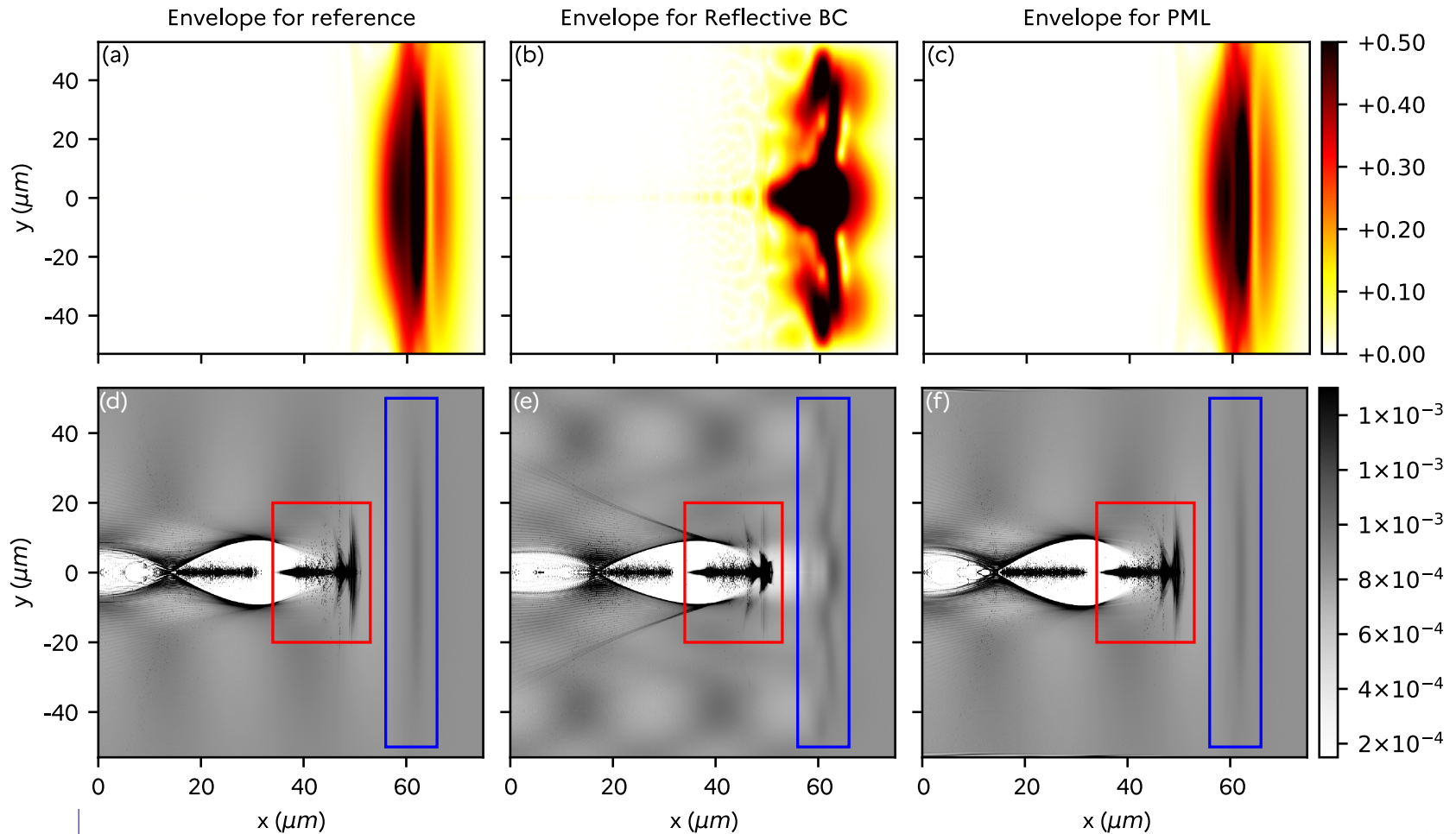
F. Massimo, EAAC23



# Envelope modeling: adding perfectly matched layers



G. Bouchard et al., in preparation (2023)

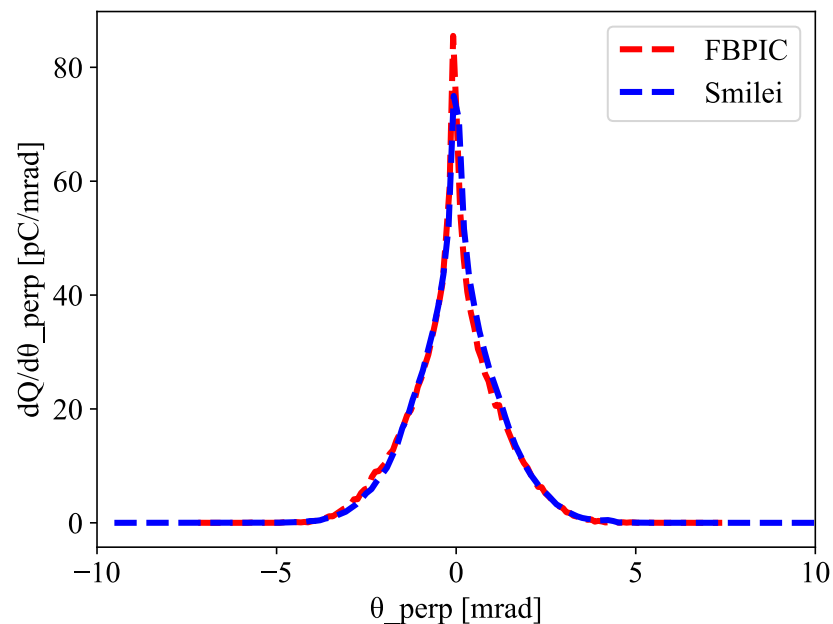
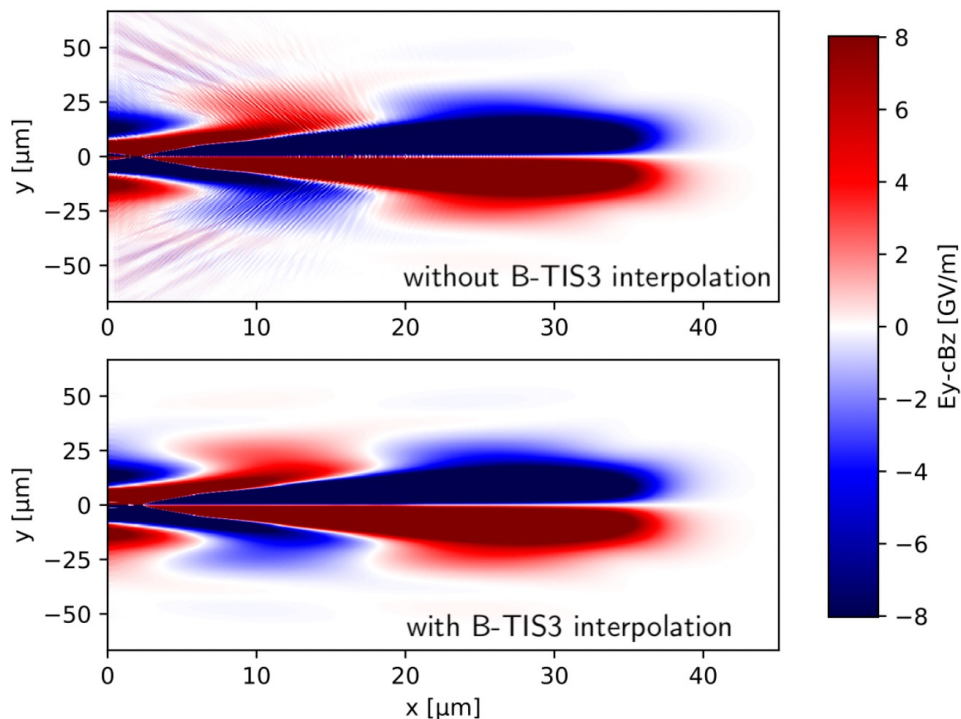


# Envelope modeling: reducing the effects of numerical Cherenkov Radiation

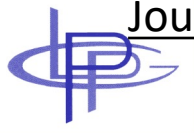


No spectral solver is used!

Divergence and emittance  
With and without a spectral code  
after 7 mm of propagation



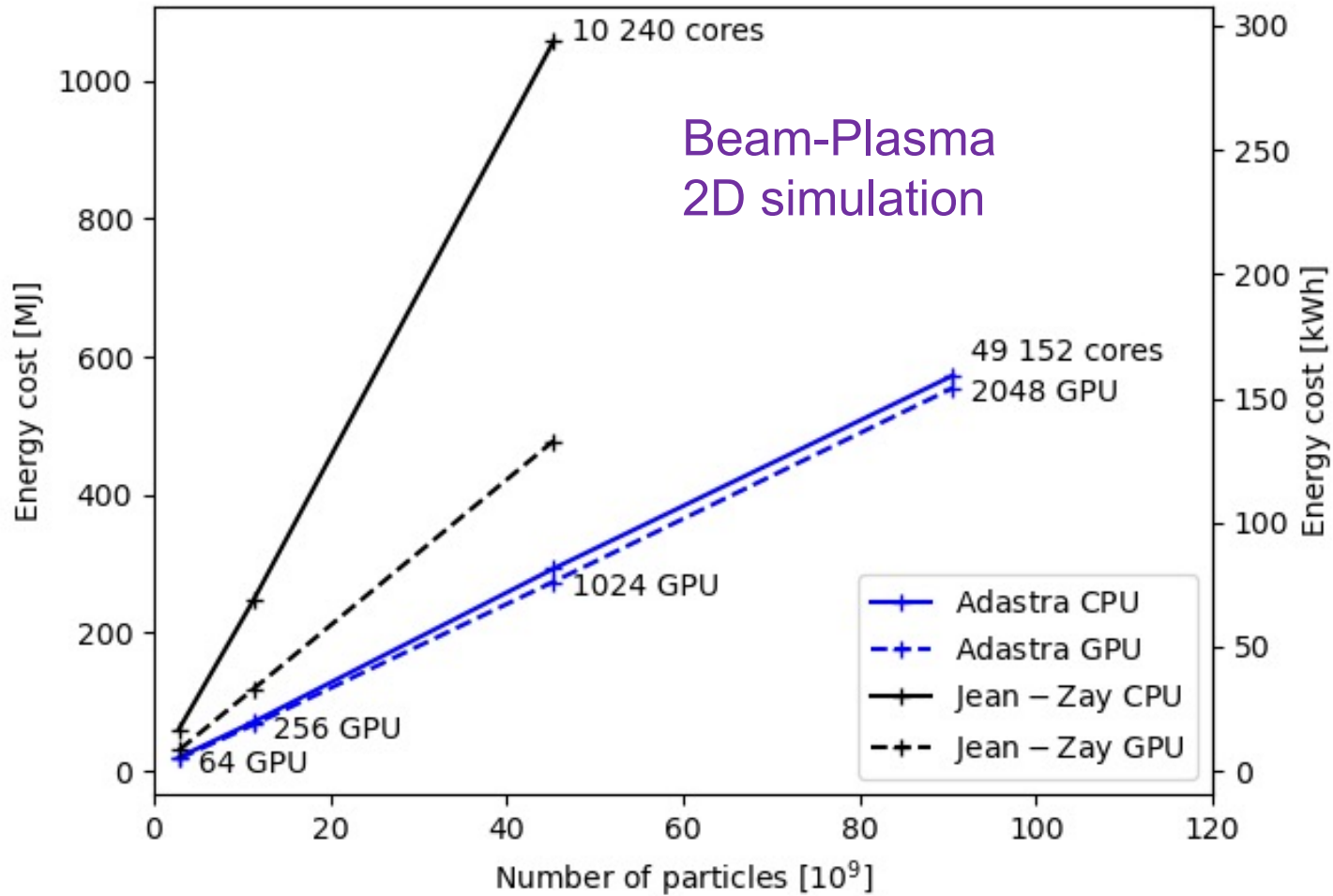
B-TIS3 scheme from  
P.-L. Bourgeois and X. Davoine,  
Journal of Plasma Physics 89 , 2 (2023)



# Quick simulations: Smilei porting on GPU is ongoing



First release with initial GPU features planned for November



# Fast dataset generation, optimization

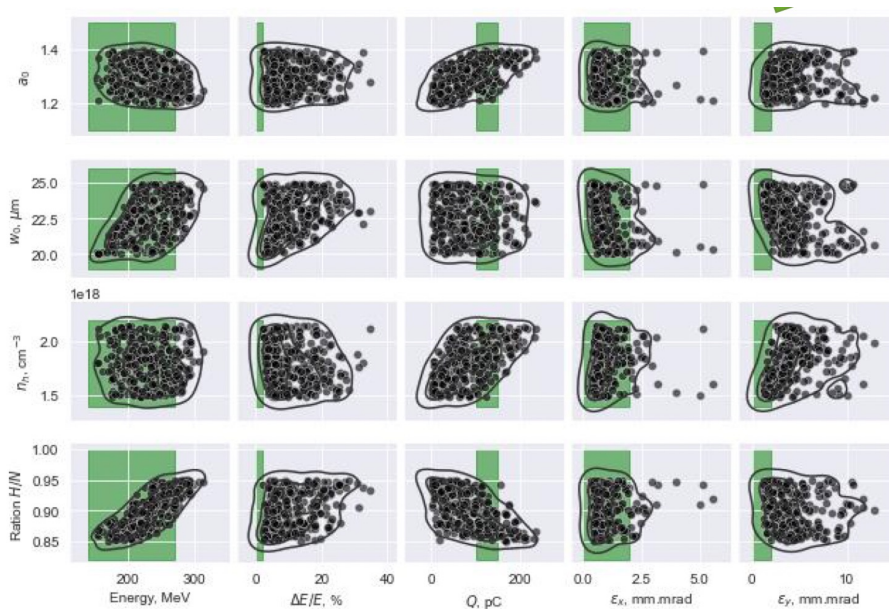




# Random scan dataset generation for machine learning

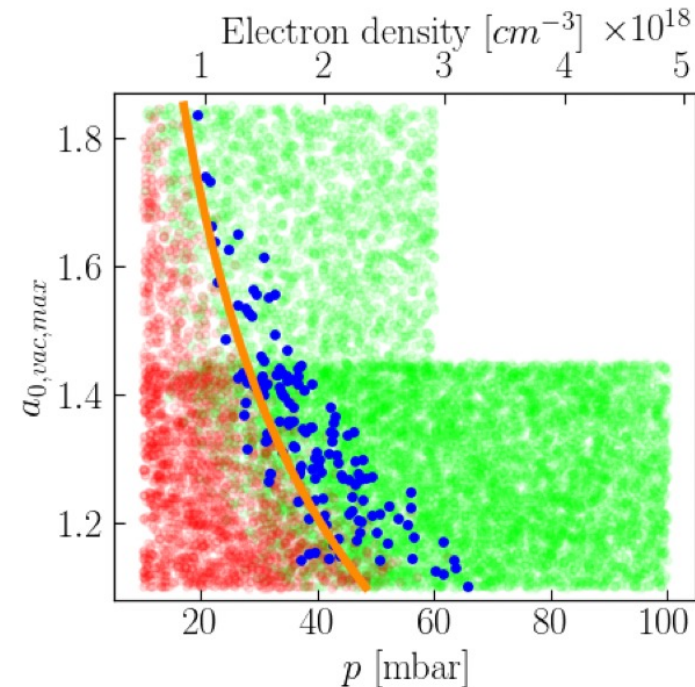


D. Minenna et al.,  
EuroNNAc Special Topics Workshop  
(2022)



See S. Marini's poster!

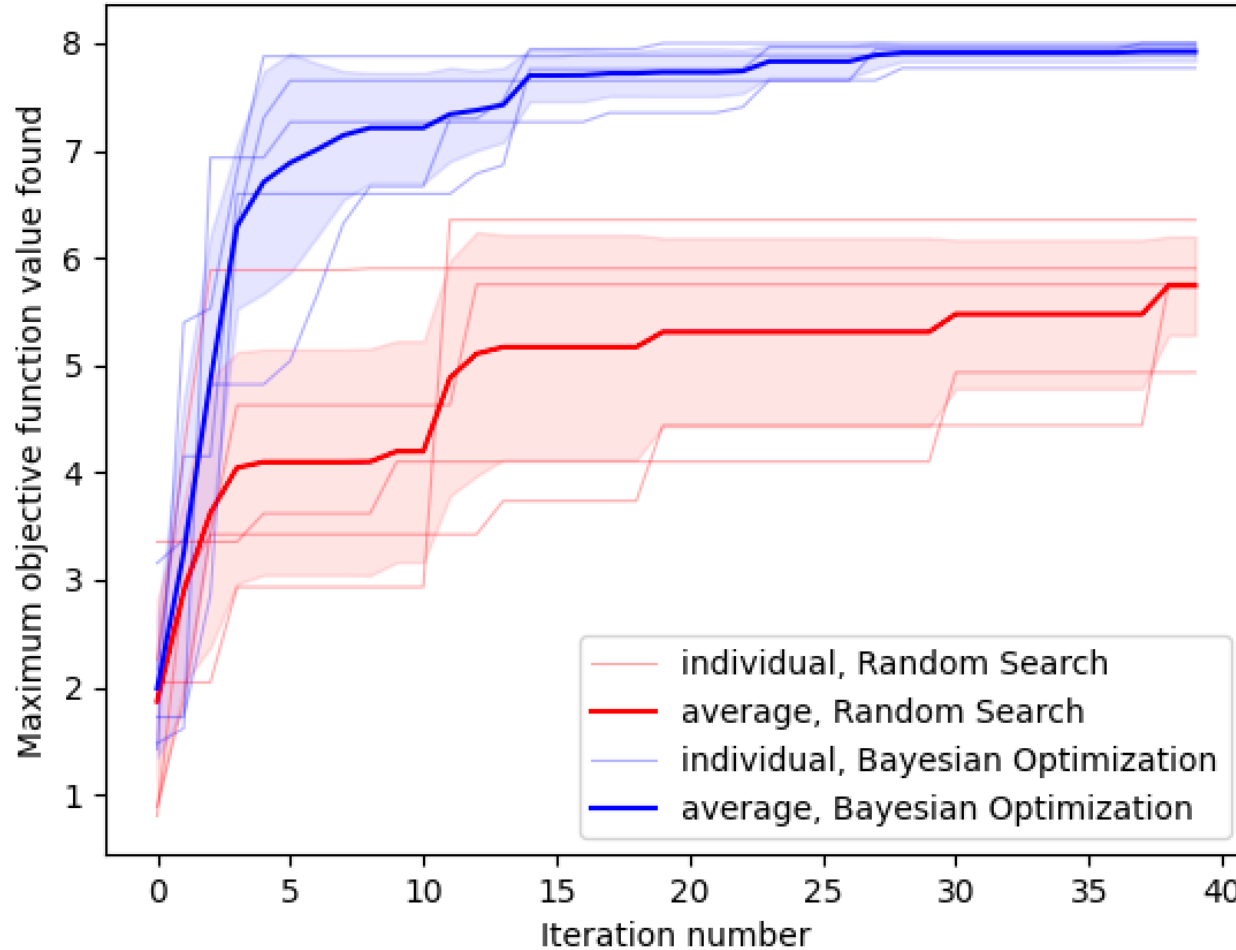
P. Drobniak et al.,  
Phys. Rev. Accel. Beams (2023)



See V. Kubytsky's poster!



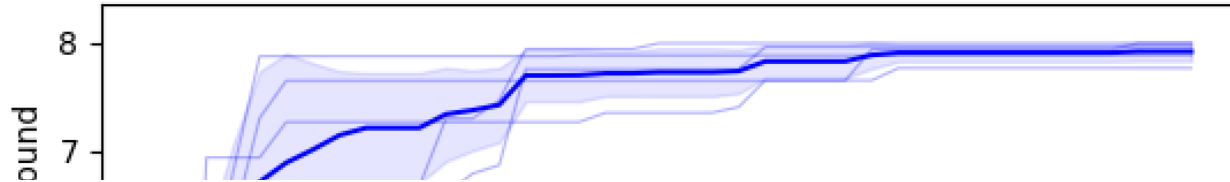
# Comparison optimization methods possible with fast simulations



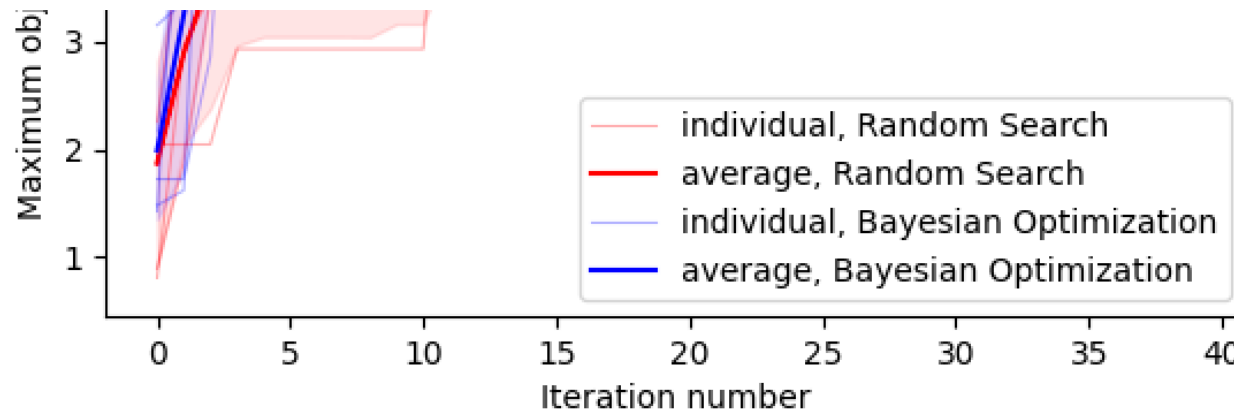
Same optimized function ( $\sqrt{Q} * E / \Delta E$ ) from S. J alas et al, PRL 2020



# Comparison optimization methods possible with fast simulations



How do BO compares with performances of other algorithms?  
E.g. genetic algorithms, CMA-ES  
Are we neglecting other efficient techniques?



Same optimized function ( $\sqrt{Q} * E / \Delta E$ ) from S. Jalas et al, PRL 2020



# Conclusions

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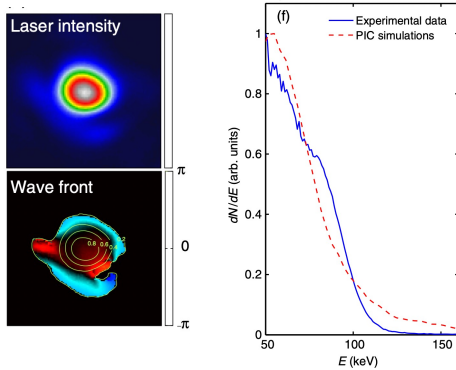
- Multistage LWFA offers considerable modeling challenges
- Combinations of different techniques will be necessary to face these challenges
- Recent progress in realistic simulation: GSA-MD, study of asymmetries effects
- Envelope modeling can be one of the techniques to have fast simulations
- Recent progress in envelope modeling: ionization, PML (available in Smilei)
- Non spectral scheme B-TIS3 to reduce effects of numerical Cherenkov radiation is compatible with envelope modeling (available in Smilei)
- GPU porting of Smilei advances, LWFA features in progress
- Quick simulations allow to generate datasets for ML, compare optimization methods



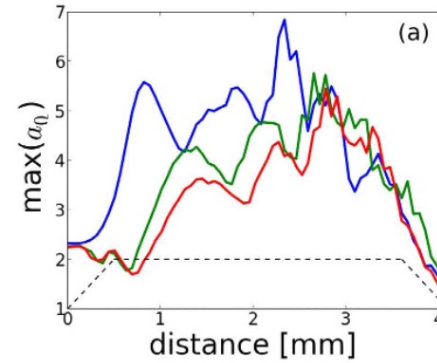
# Additional slides



# Laser field and LWFA experiment reconstruction: some results in the literature

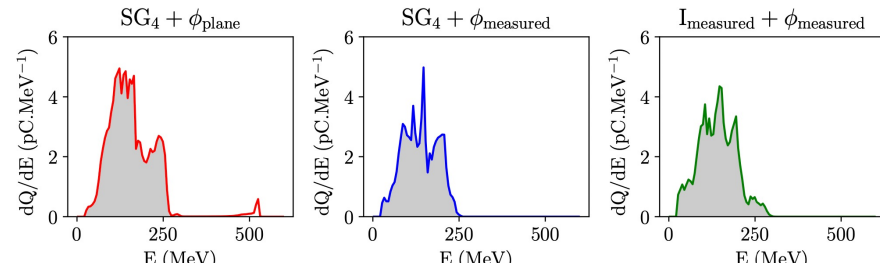


Beaurepaire, B. et al,  
Phys. Rev. X **5**, 031012 (2015)

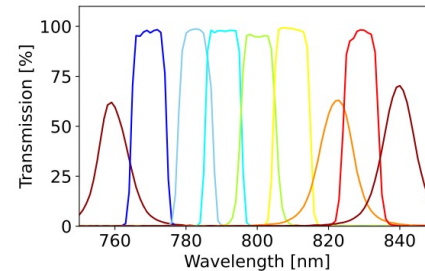
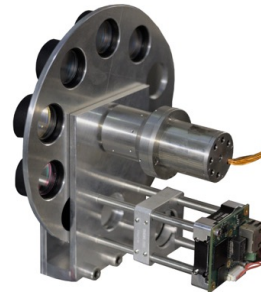


J. Ferri et al,  
Sc. Reports **6**,27846 (2016)

I. Zemzemi and A. Beck,  
arXiv 2304.09020 (2023)



N. Weiße al,  
arXiv 2303.01360 (2023)





# Smilei) 4th Smilei user & training workshop

8–10 Nov 2023 @ ELI beamlines & CTU Europe/Prague timezone

<https://indico.math.cnrs.fr/event/9577/>



# Envelope ionization model (1)



- ADK ionization rate averaged over optical cycles  
(M. Chen et al., J. Comput. Phys. 2013)
- Initialization of electron transverse momenta after ionization  
(P. Tomassini et al., Phys. Plasmas 2017)

$$\mathbf{p}_{\perp} - \mathbf{A}_{\perp} = \text{const} \longrightarrow \mathbf{p}_{\perp} = \mathbf{A}_{\perp} - \mathbf{A}_{\perp, t_{\text{ioniz}}}$$

$$|\mathbf{p}_{\perp, 0}| = \begin{cases} p_{\text{pol}, 0} \leftarrow N(0, \sigma_{p_{\perp}}) & \text{Linear Polarization} \\ |\tilde{A}|/\sqrt{2} & \text{Circular Polarization} \end{cases} \longrightarrow \text{C. B. Schroeder et al., Phys. Rev Accel. Beams (2014)}$$

Accurate description in non-relativistic regime ( $a_0 < 1$ )





# Envelope ionization model (2)



- ADK ionization rate averaged over optical cycles  
(M. Chen et al., J. Comput. Phys. 2013)
- Initialization of electron transverse momenta after ionization  
(P. Tomassini et al., Phys. Plasmas 2017)
- Initialisation des impulsions longitudinales des électrons  
(F. Massimo et al., Phys. Rev. E 2020)

$$p_x = \frac{|\mathbf{p}_\perp|^2}{2} = \frac{1}{2} |\mathbf{A}_\perp - \mathbf{A}_{\perp, t_{\text{ioniz}}}|^2$$



$$p_{x,0} = \begin{cases} |\tilde{A}|^2/4 + p_{\text{pol},0}^2/2 \\ |\tilde{A}|^2/2 \end{cases}$$

Accurate description  
also in relativistic regimes ( $a_0 > 1$ )



# Envelope ionization model (3)



Laser  
Pulse:

$a_0=2.5$   
(linear  
polarization

$\lambda_0=0.8 \mu\text{m}$

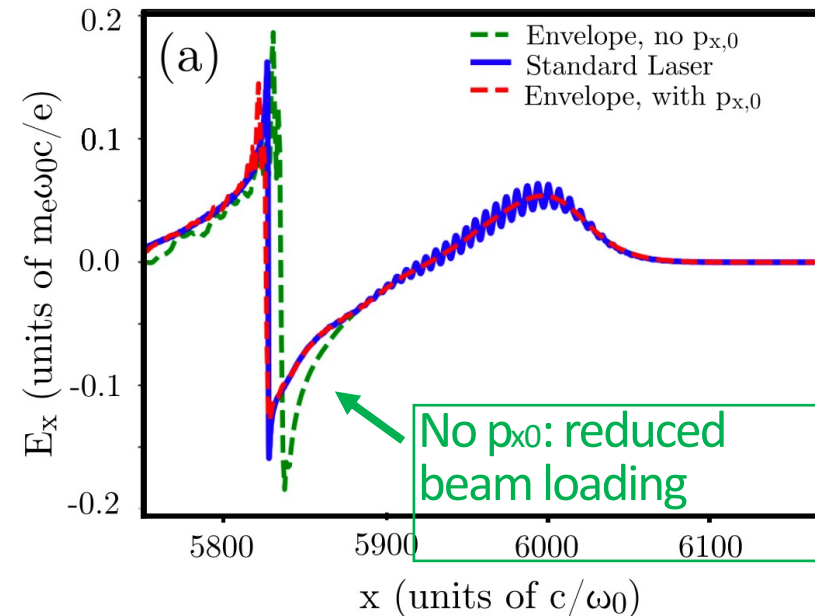
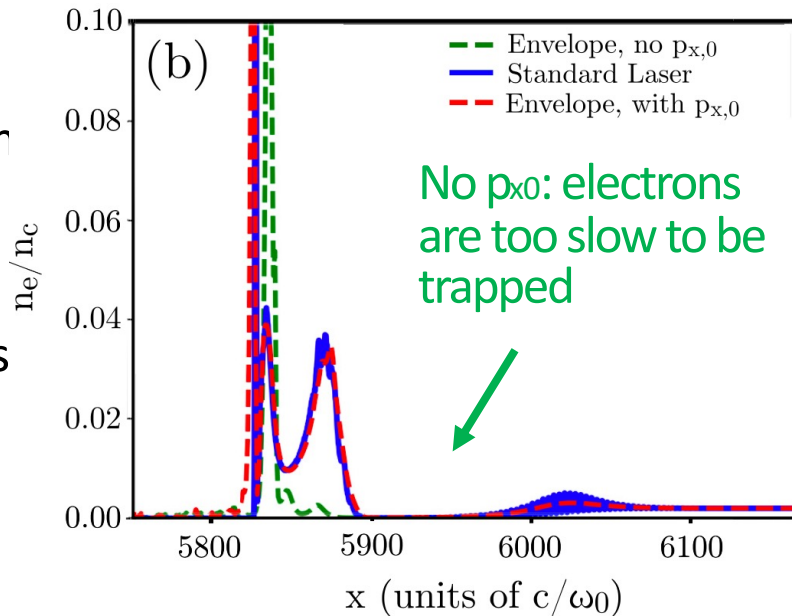
$w_0=19 \mu\text{m}$

$T_{\text{FWHM}}=33 \text{ fs}$

Gas target  
(99%He  
+1%N<sup>5+</sup>):

$n=3.4 \cdot 10^8 \text{ cm}^{-3}$

$L=800 \mu\text{m}$



F. Massimo et al., Phys. Rev E (2020)

F. Massimo, March 6th 2023, LPAW2023

