

# Mesh Refinement in quasi-static codes

*making plasma acceleration simulations in collider-relevant parameters feasible (and cheap)*

Maxence Thévenet – DESY

*MPA – plasma acceleration*

Plasma acceleration is described by kinetic plasma dynamics

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# Plasma acceleration is described by kinetic plasma dynamics

$$\frac{\partial \mathbf{B}}{\partial t} = -\nabla \times \mathbf{E},$$

$$\frac{\partial \mathbf{E}}{\partial t} = \nabla \times \mathbf{B} - \mathbf{J},$$

$$\frac{d\mathbf{x}}{dt} = \mathbf{v},$$

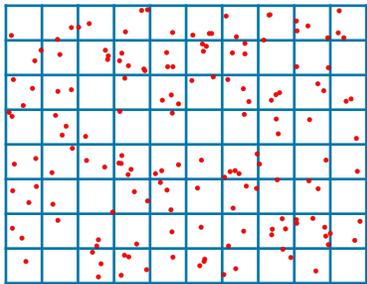
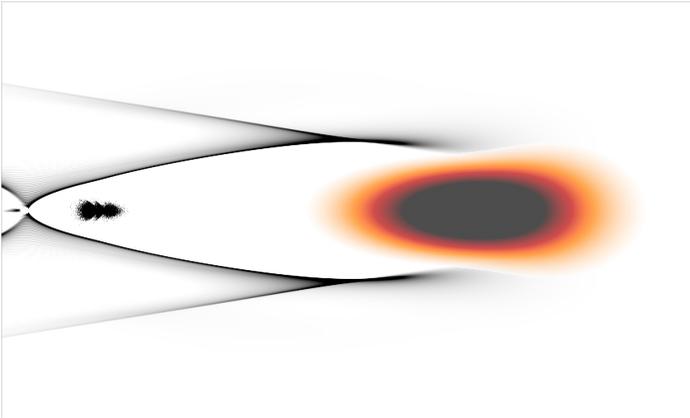
$$\frac{d(\gamma\mathbf{v})}{dt} = \frac{q}{m}(\mathbf{E} + \mathbf{v} \times \mathbf{B}),$$

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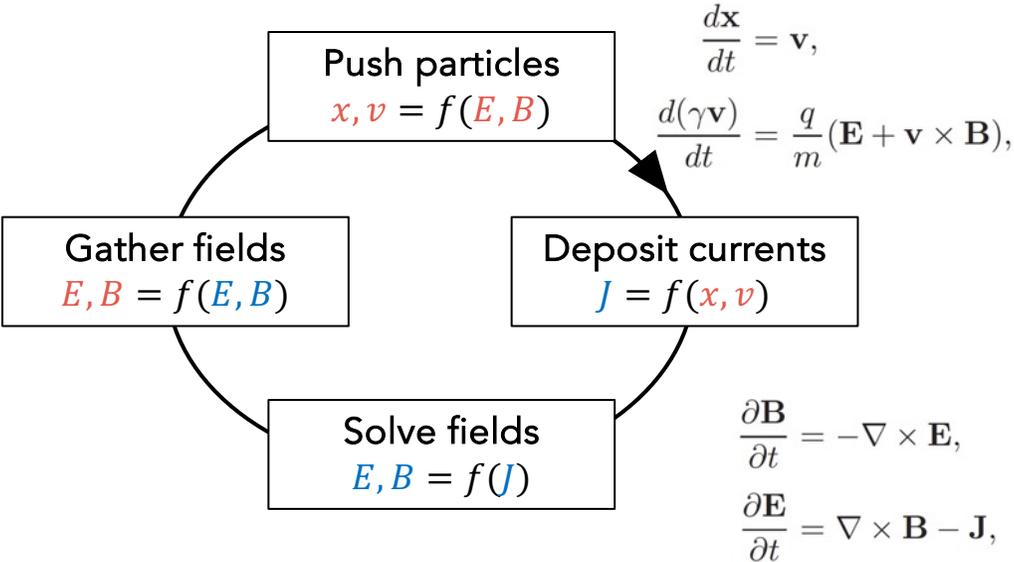
$$\frac{d\mathbf{x}}{dt} = \mathbf{v},$$
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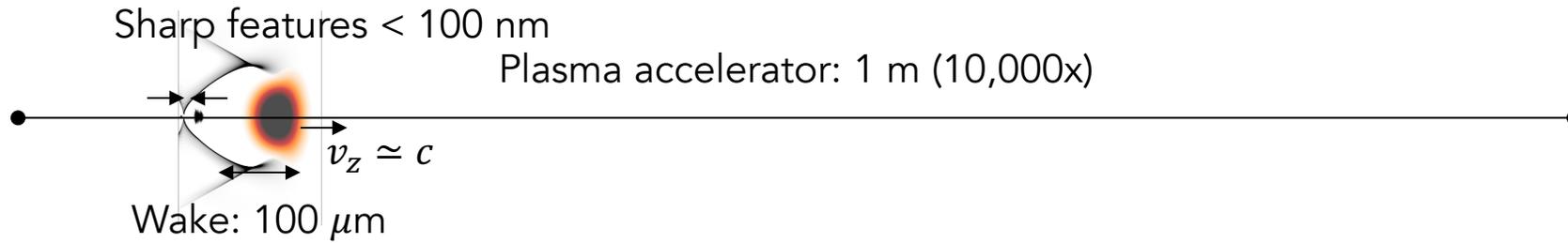


Regular mesh  
Macroparticles



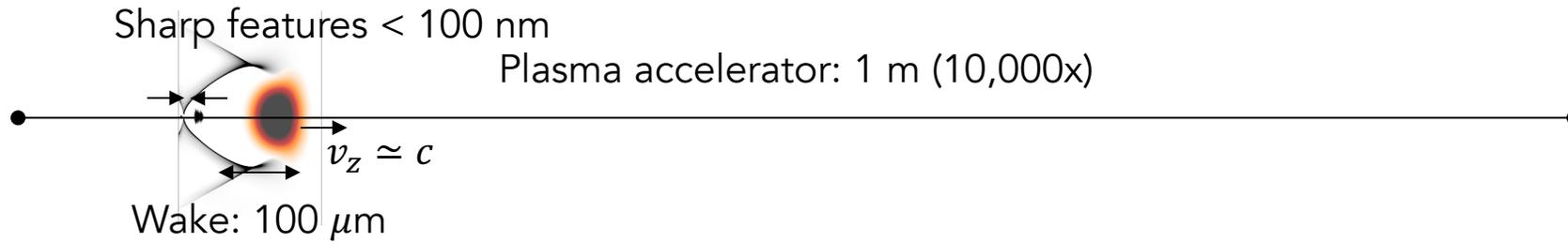
- *Lagrangian* description of plasma, *Eulerian* description of fields
  - Physics can be added
  - Time step limited by CFL condition:  $\Delta t \simeq \frac{\Delta z}{c}$
- 3D (EM) PIC simulations of plasma acceleration are very expensive

# Quasi-static approximation helps simulations of plasma acceleration



Problem: in PIC the CFL condition limits the time step to  $\Delta t < c\Delta z$

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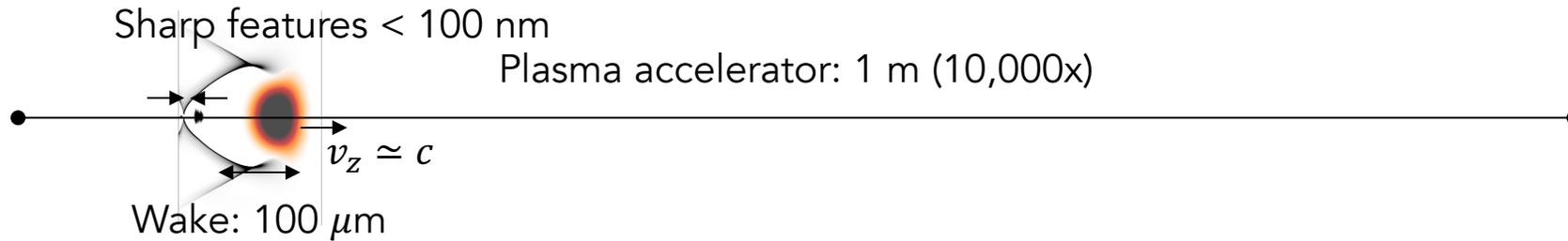


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## Two main methods for larger time steps

- **Boosted frame method** [[J.-L. Vay PRL 98, 130405 \(2007\)](#)]
  - Prone to Numerical Cherenkov Instability (NCI)
  - Mitigation methods exist [[R. Lehe et al., PRE 94 \(2016\)](#), [M. Kirchen et al., Phys. Plasmas 23 \(2016\)](#), [A. Pukhov JCP 418 \(2020\)](#)]

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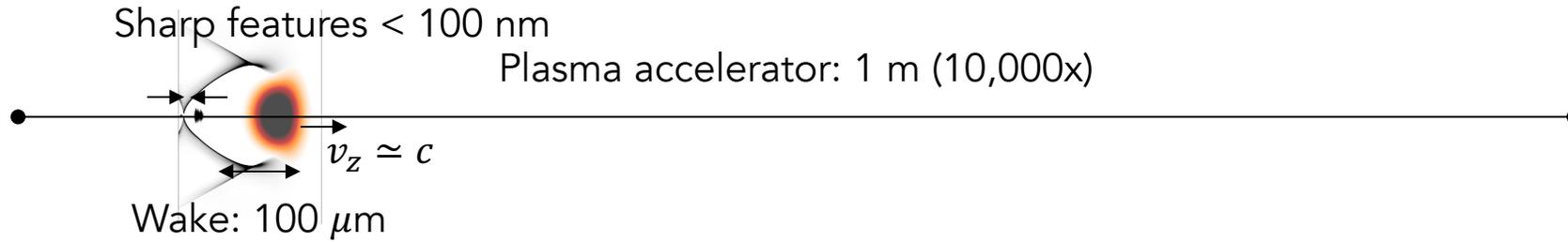


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- **Quasi-static particle-in-cell**
  - Beam & wake:  $\mathbf{v} \sim c\mathbf{e}_z$
  - Quasi-static approximation
    - No CFL condition, large time step for the beam
    - Cannot capture injection

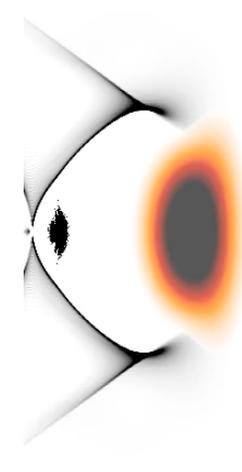
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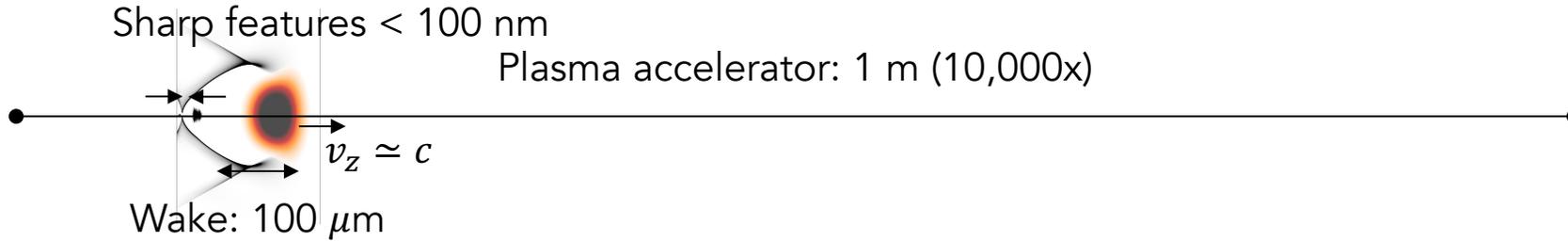
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$$\nabla_{\perp}^2 \psi = -\frac{1}{\epsilon_0} \left( \rho - \frac{1}{c} j_z \right)$$

$$E_x - c B_y = -\partial_x \psi$$

$$E_y + c B_x = -\partial_y \psi$$

$$\nabla_{\perp}^2 E_z = c\mu_0 (\partial_x j_x + \partial_y j_y)$$

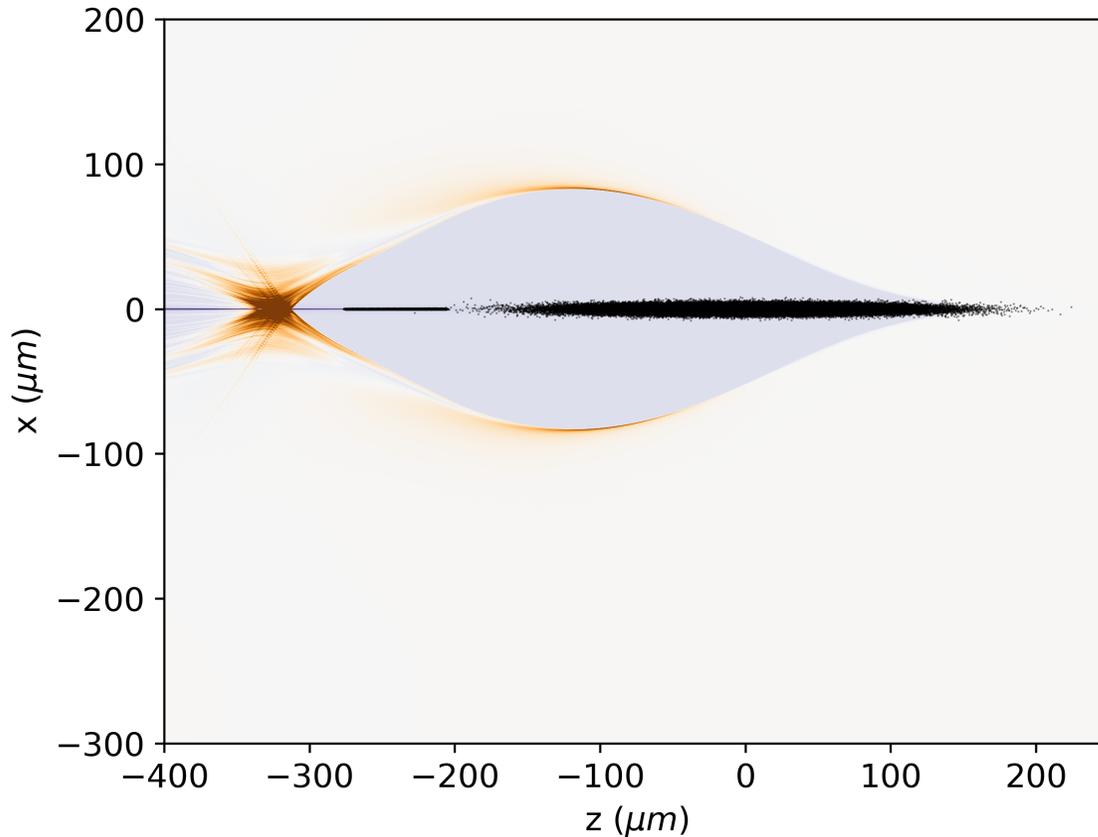
$$\nabla_{\perp}^2 B_x = \mu_0 (-\partial_y j_z + \partial_z j_y)$$

$$\nabla_{\perp}^2 B_y = \mu_0 (\partial_x j_z - \partial_z j_x)$$

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# Scale discrepancies can make simulations impractical or unfeasible

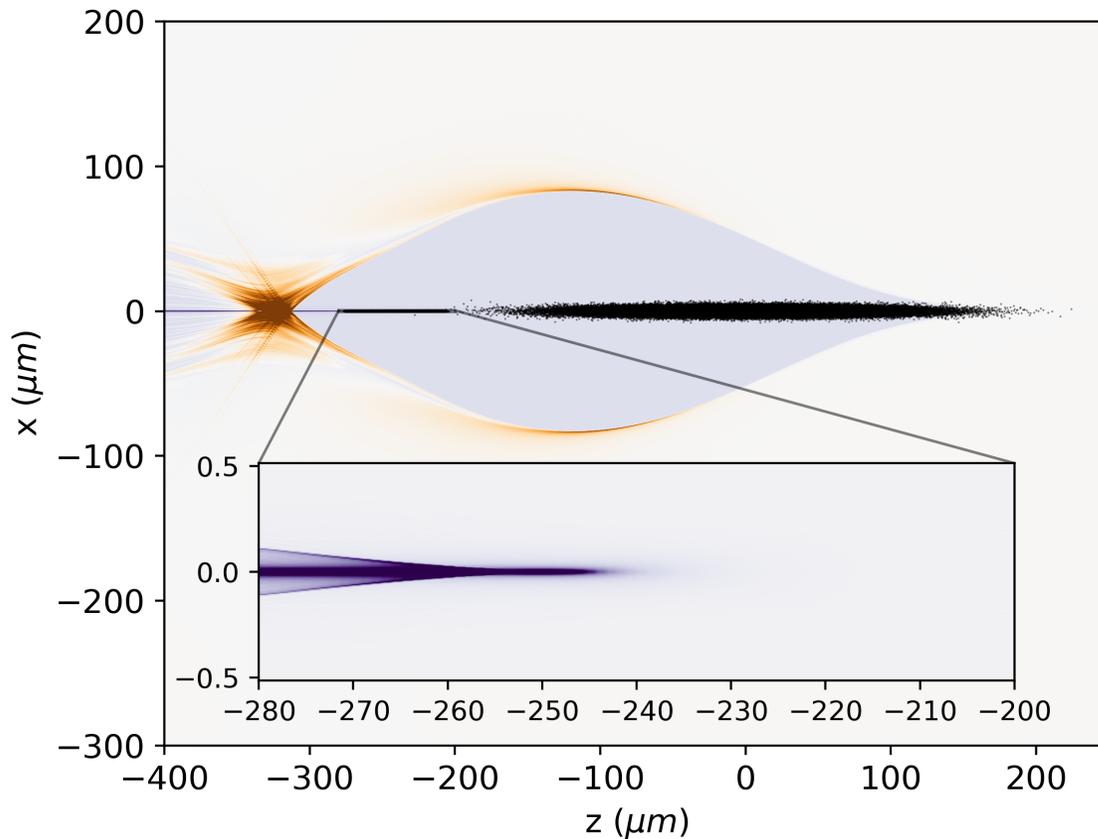
*Relevant for colliders, consistent with ESPP report*



- **Driver**  
 $Q = 2 \text{ nC}$ ,  $\epsilon_{x,y} = 10 \text{ }\mu\text{m}$ ,  $\mathcal{E} = 20 \text{ GeV}$ ,  $\Delta\mathcal{E} = 1\%$ ,  $L = 53 \text{ }\mu\text{m}$ ,  
matched
- **Witness**  
 $Q = 833 \text{ C}$ ,  $\epsilon_{x,y} = 135 \text{ nm}$ ,  $\mathcal{E} = 175 \text{ GeV}$ ,  $\Delta\mathcal{E} = 0.35\%$ ,  $L = 64 \text{ }\mu\text{m}$   
beam-loaded (SALAME), matched
- **Plasma**  $n_0 = 10^{16} \text{ cm}^{-3}$ ,  $r_b \approx 100 \text{ }\mu\text{m}$ , ion spike  $\approx 10 \text{ nm}$

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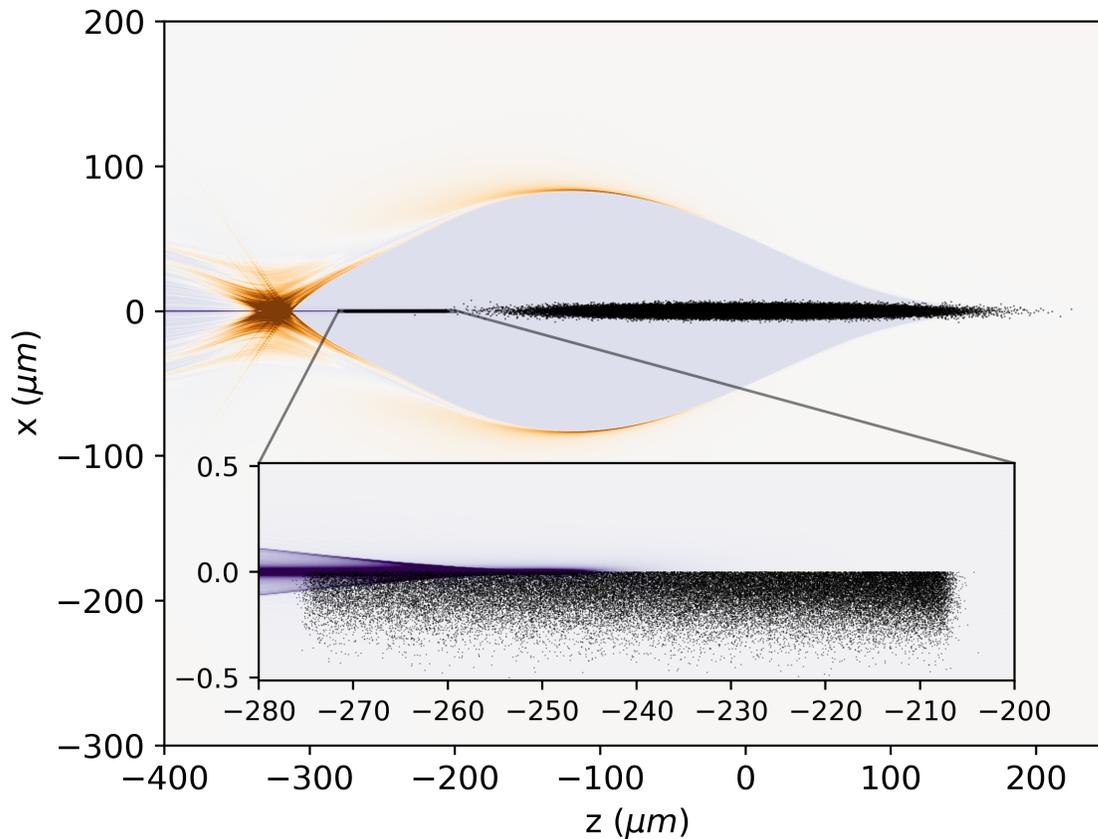
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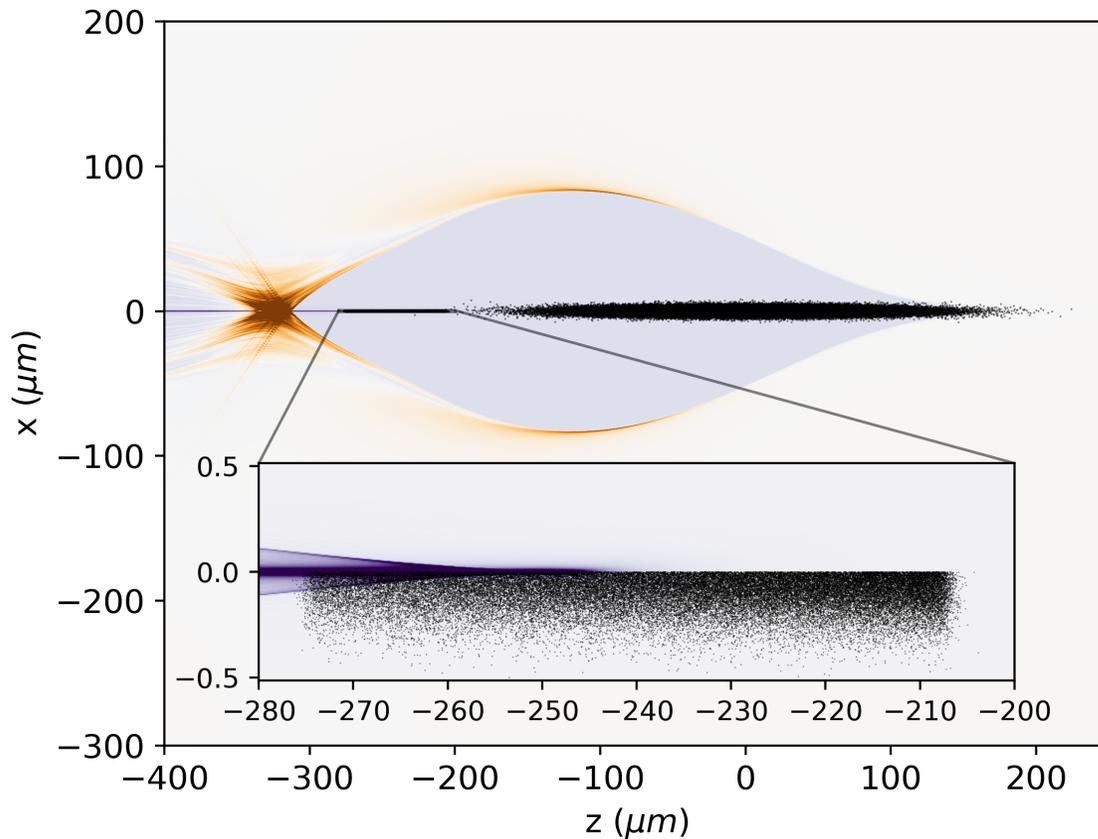
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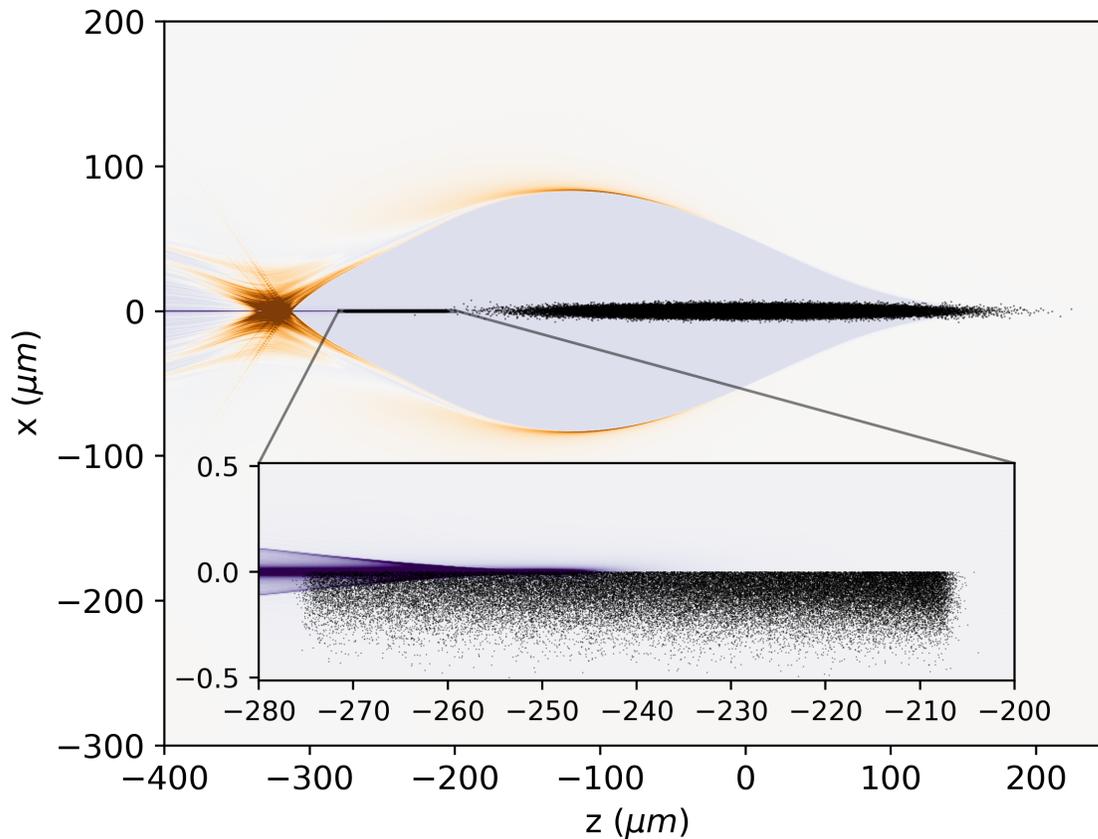


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Solutions exist (see presentation by J.-L. Vay)

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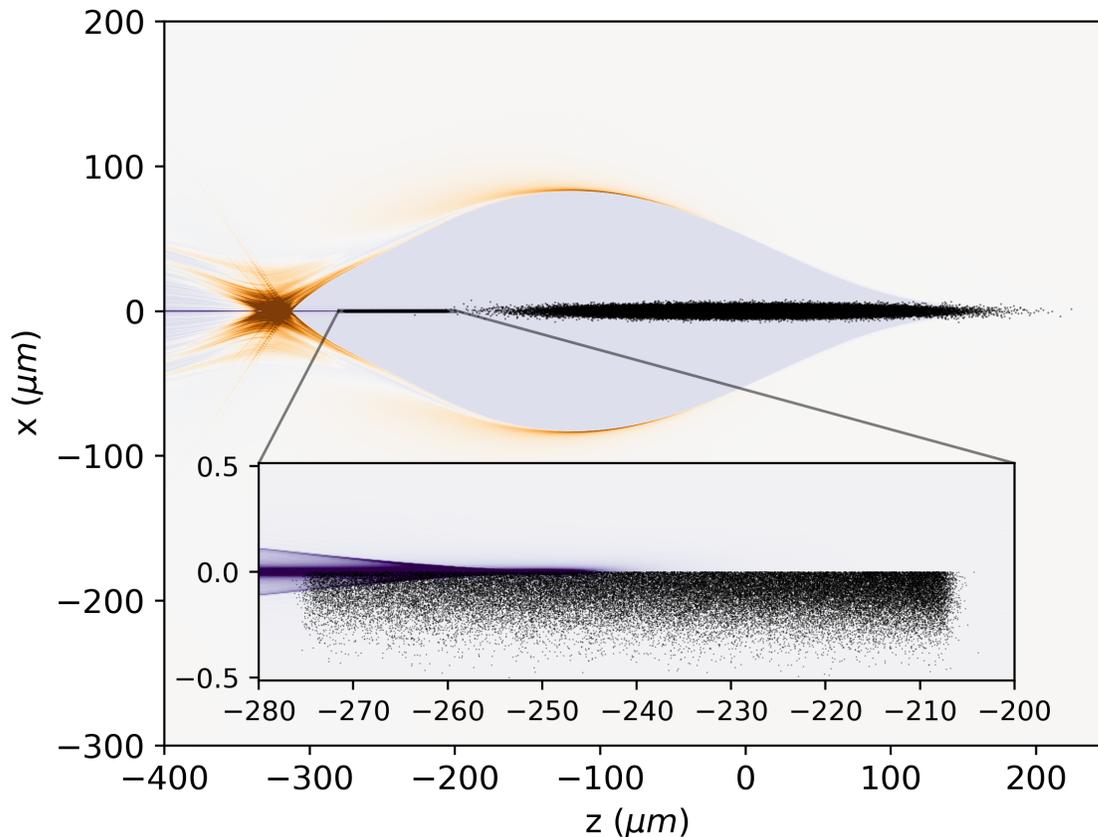


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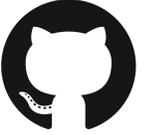
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- We will discuss mesh refinement in **two (open-source) codes**

HiPACE++

WakeT

# HiPACE++: 3D advanced quasi-static PIC on GPU

Beam-driven or laser-driven plasma acceleration



*Combine performance and usability*

- **Laptop to supercomputer** - CPUs/GPUs (powered by AMReX)
- **Open-source** - documented, openPMD, CI
- **Multi-physics** - lasers & beams, collisions, ionization, RR
- **Advanced methods** - explicit solver, in-situ diagnostics, two unit systems, SALAME, adaptive time step, etc.

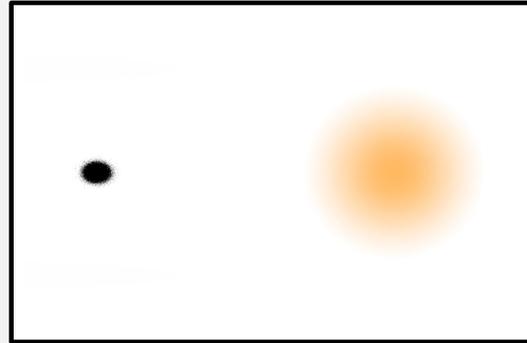


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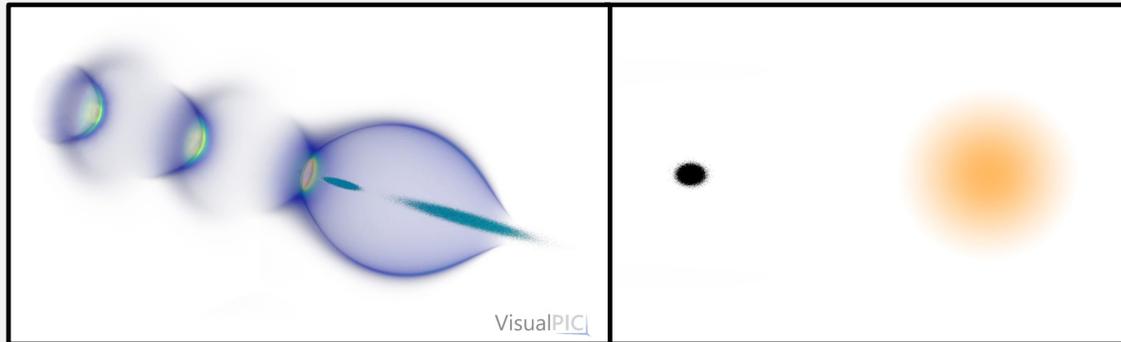


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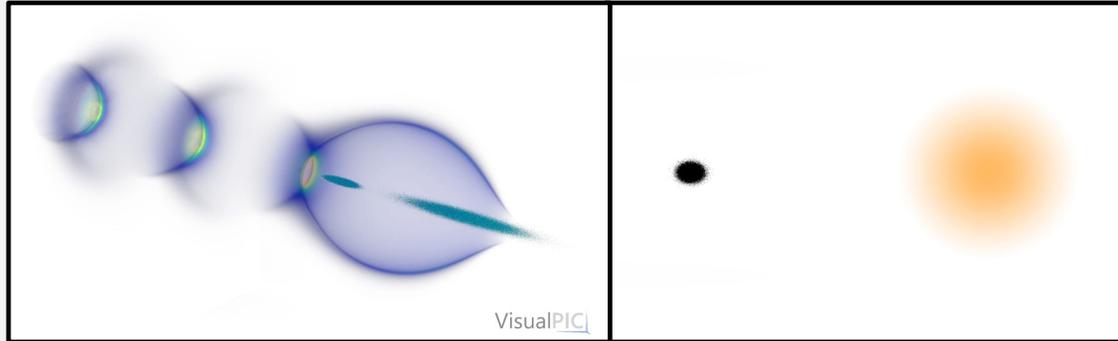


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Beam-driven or laser-driven plasma acceleration



	4 GPUs	1024 CPU cores
Runtime (seconds)	6	556
Cost (node-hours)	6	11900

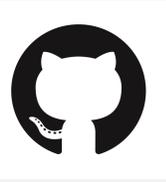
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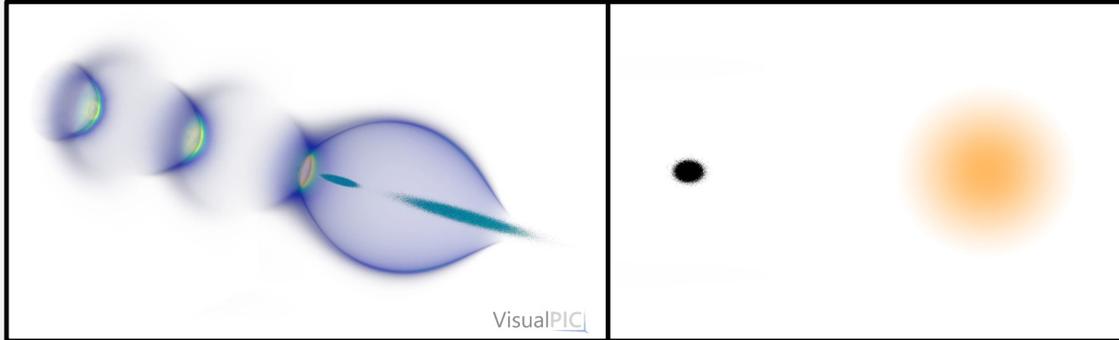


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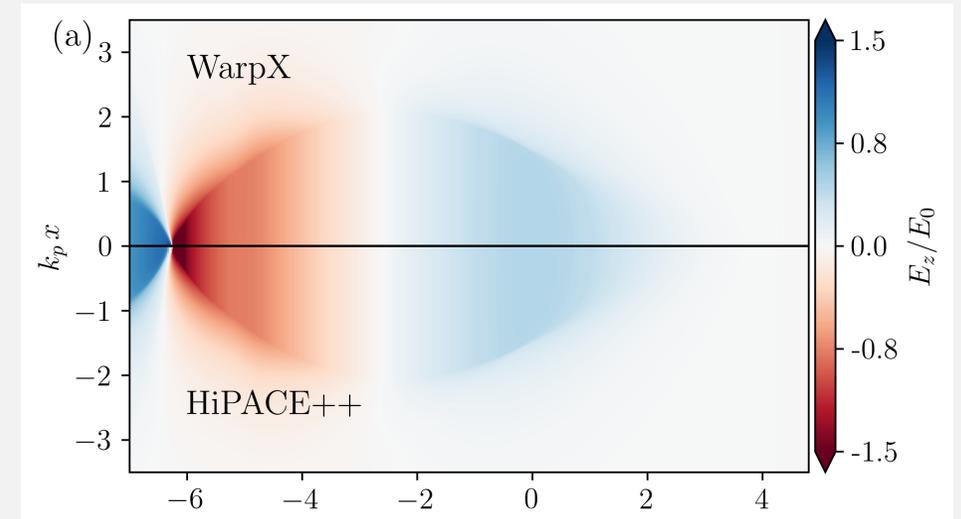
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# HiPACE++ – The Team

*Advanced algorithms and high-performance computing for fast and energy-efficient 3D simulations of plasma acceleration – for everyone*



Maxence Thévenet  
(lead)



Severin Diederichs



Alexander Sinn



Axel Huebl



Rémi Lehe



Jean-Luc Vay



Andrew Myers



Weiqun Zhang



Carlo Benedetti

**DESY – MPA**

**LBLN – AMP**



**LBLN – AMCR**

*AMReX developers*

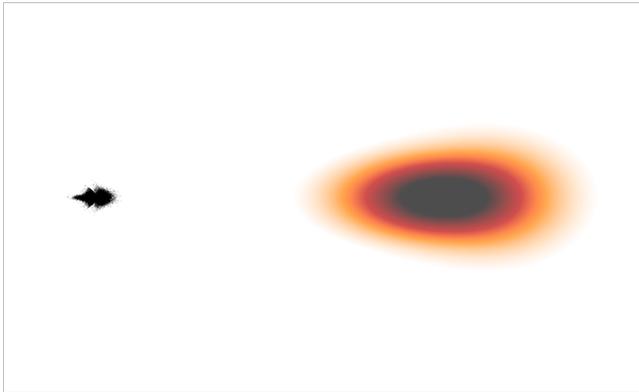
**LBLN – BELLA**

- Started mid-2020
- International project, open-source
- New contributors most welcome!

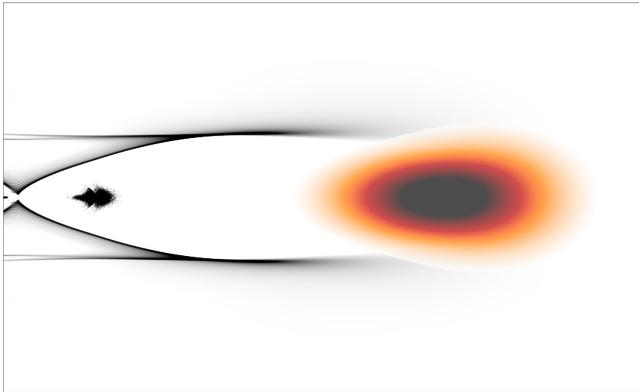


**BERKELEY LAB**

In QS PIC, plasma and laser/particle beams are treated differently

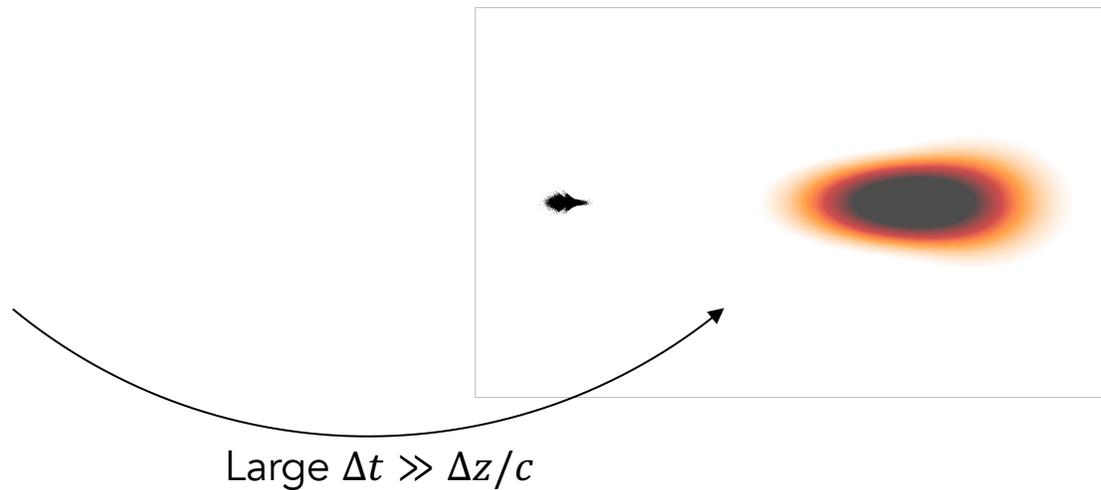


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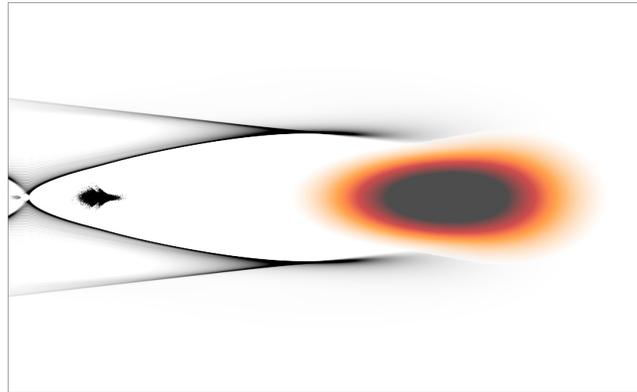
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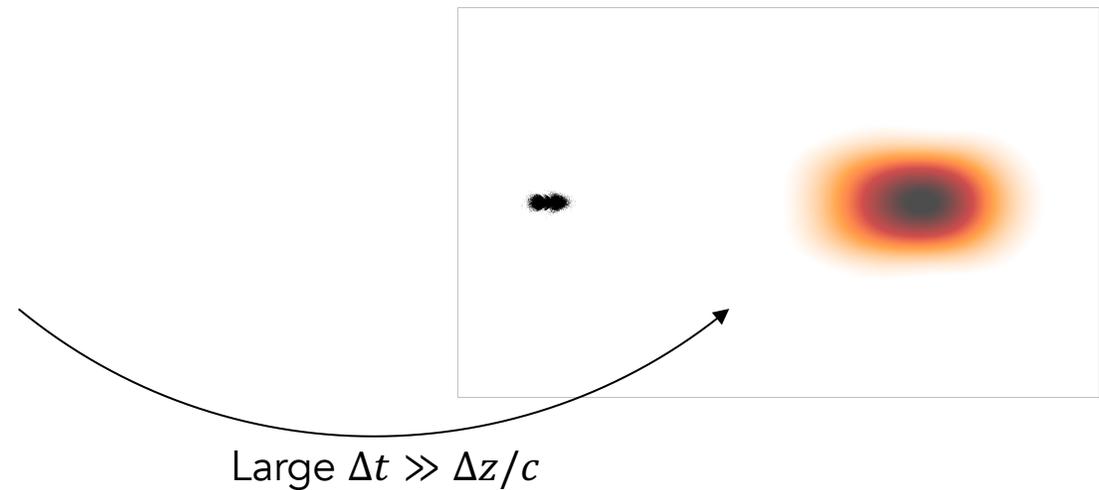
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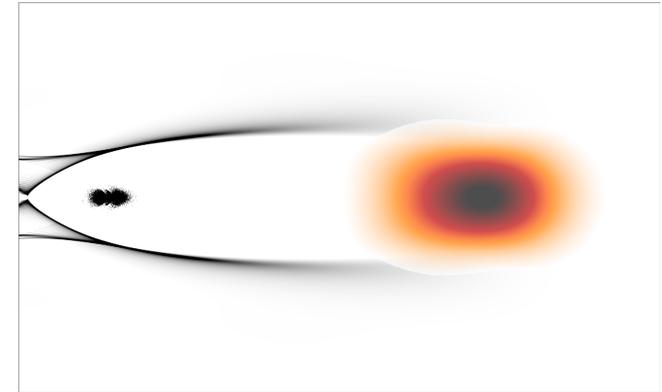
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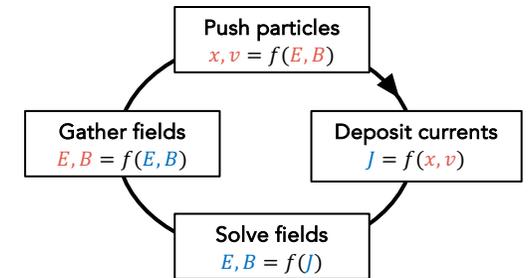
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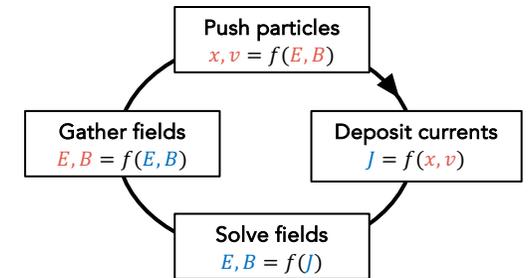
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The plasma response is computed with a swipe from head to tile

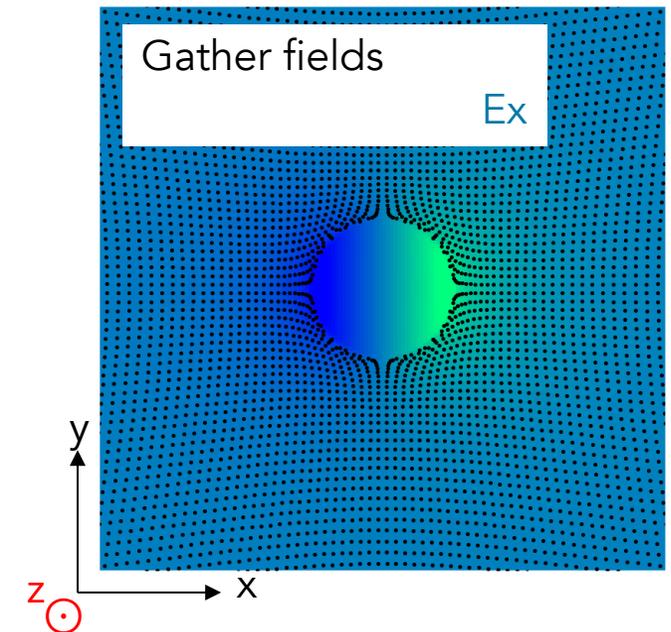
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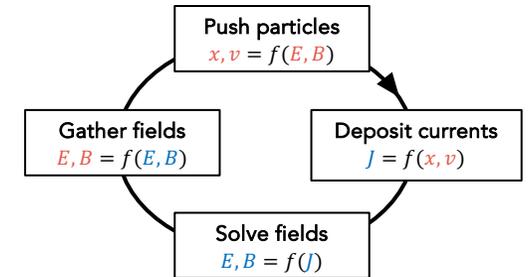
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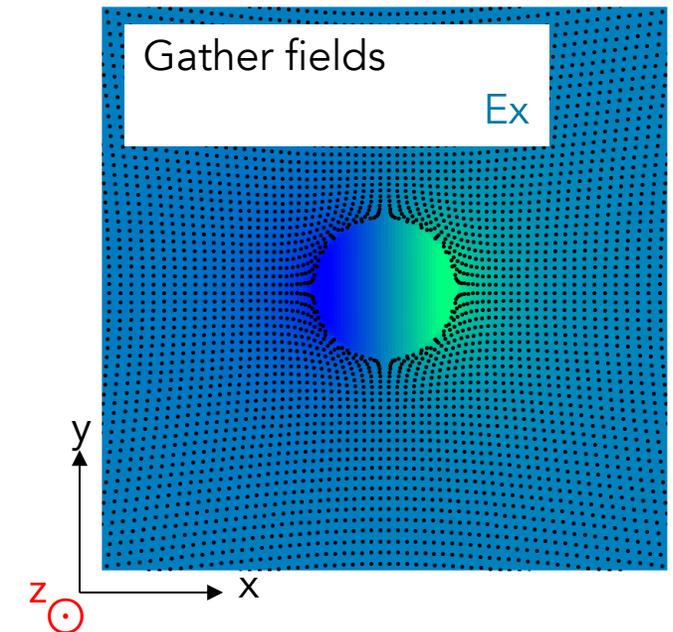
2D slice  
Field & particles



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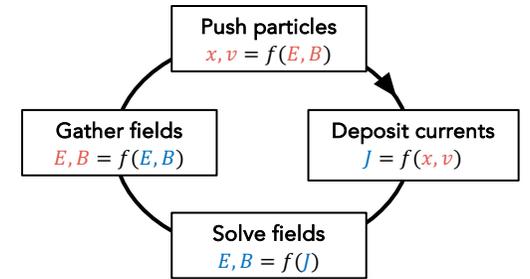
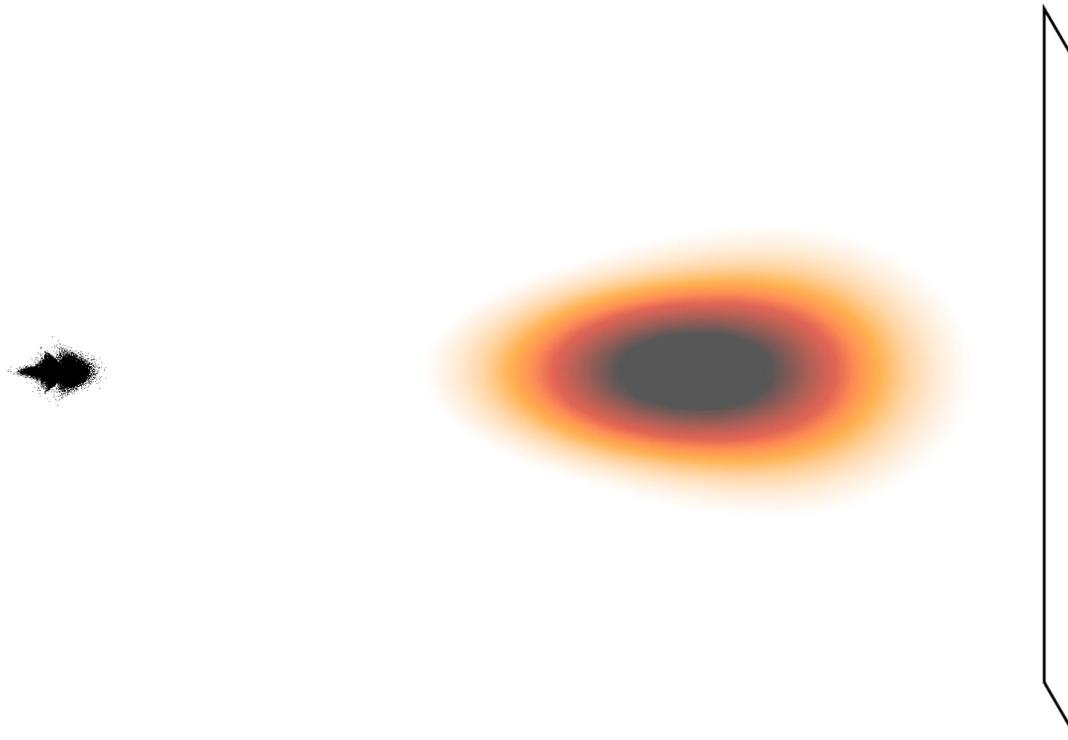


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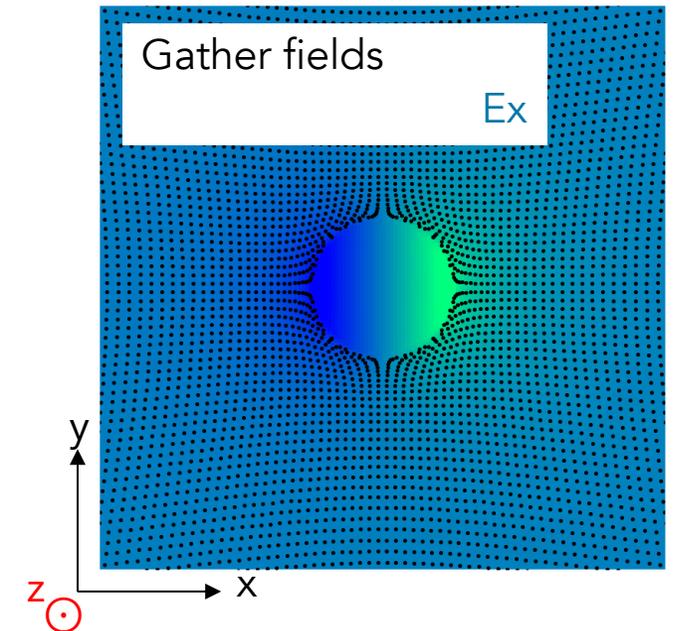


- All PIC operations occur on the 2D transverse domain
- Plasma particles are advanced in  $\zeta$  (z), not in time
- (specific to HiPACE++: beams and lasers also advanced in the swipe)
- A simulation does  $\mathbf{n}_t \times \mathbf{n}_z$  PIC iterations on domain  $\mathbf{n}_x \times \mathbf{n}_y$
- (EM PIC: does  $\mathbf{n}_t$  PIC iterations on domain  $\mathbf{n}_x \times \mathbf{n}_y \times \mathbf{n}_z$ )

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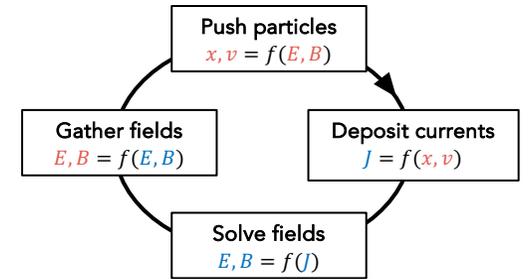
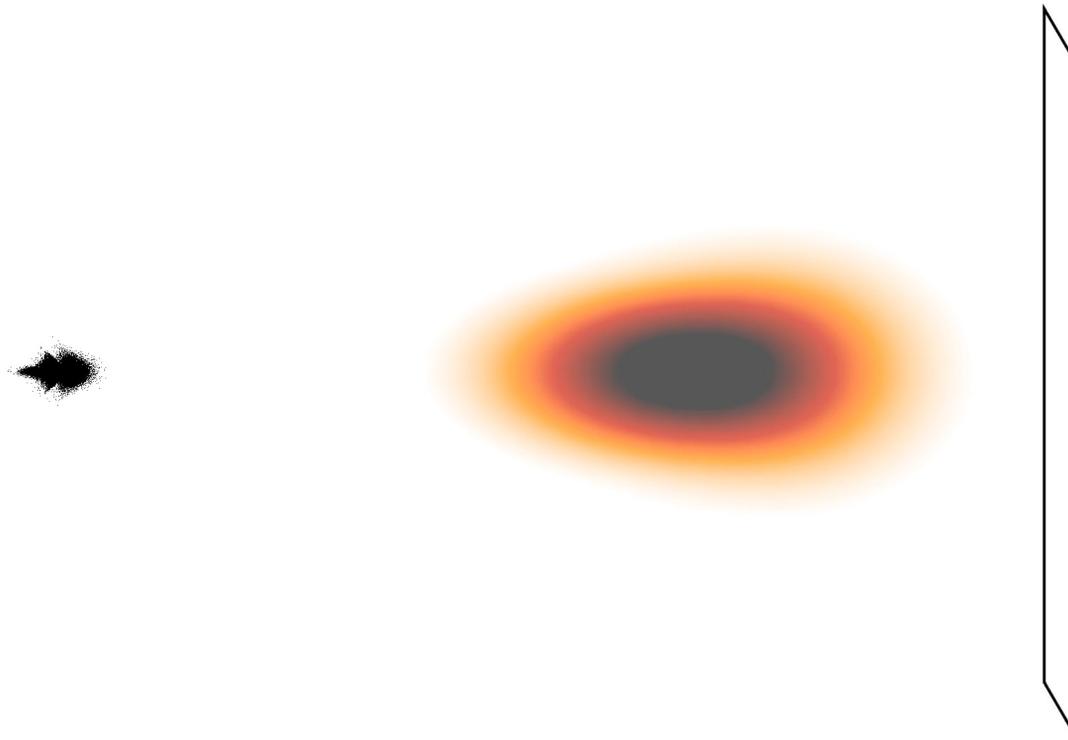


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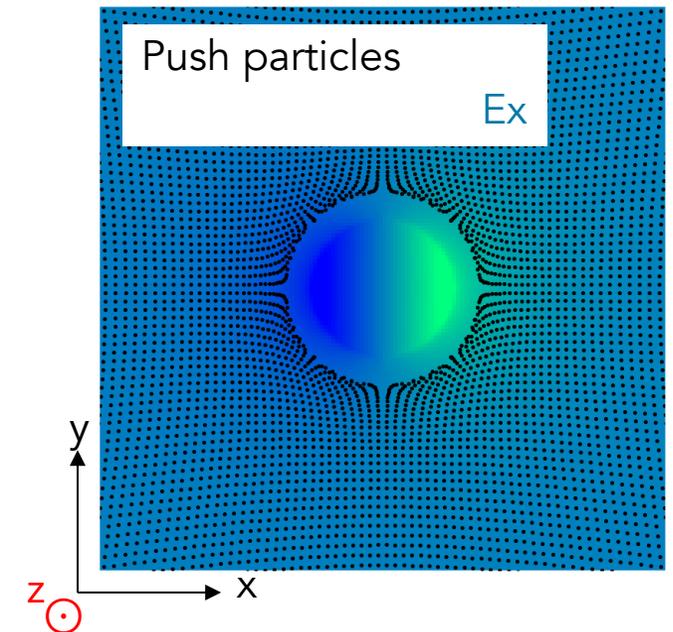


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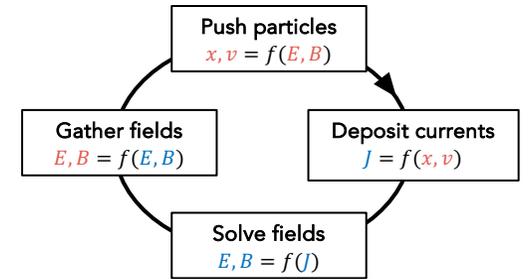
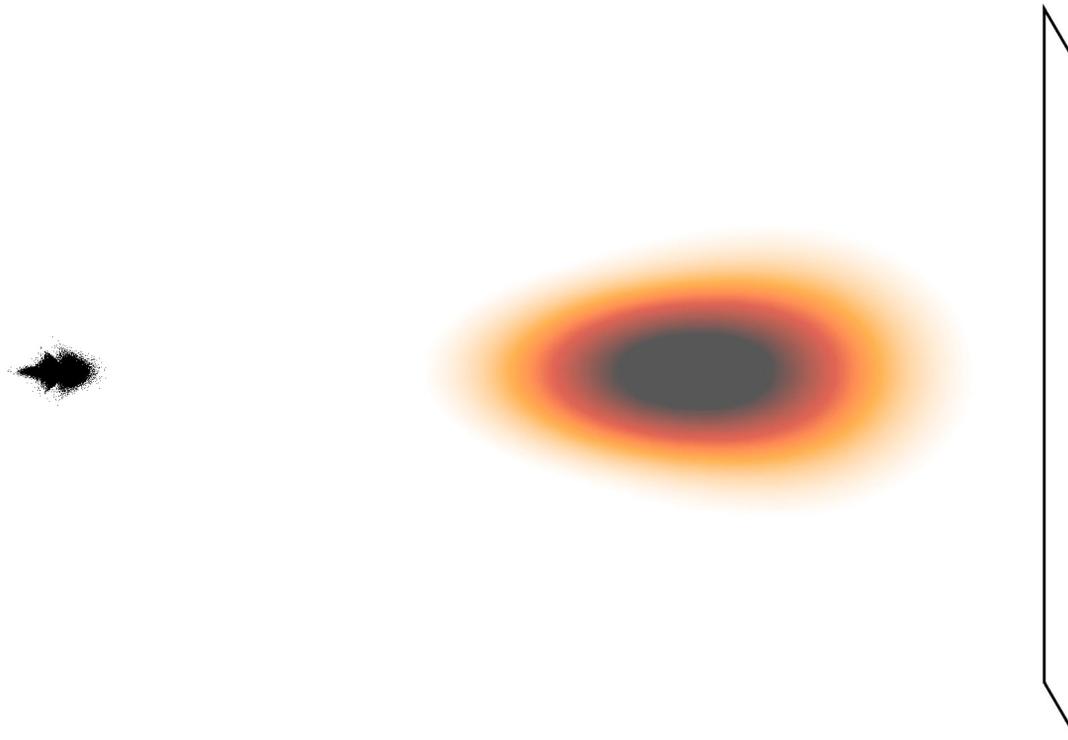


2D slice  
Field & particles

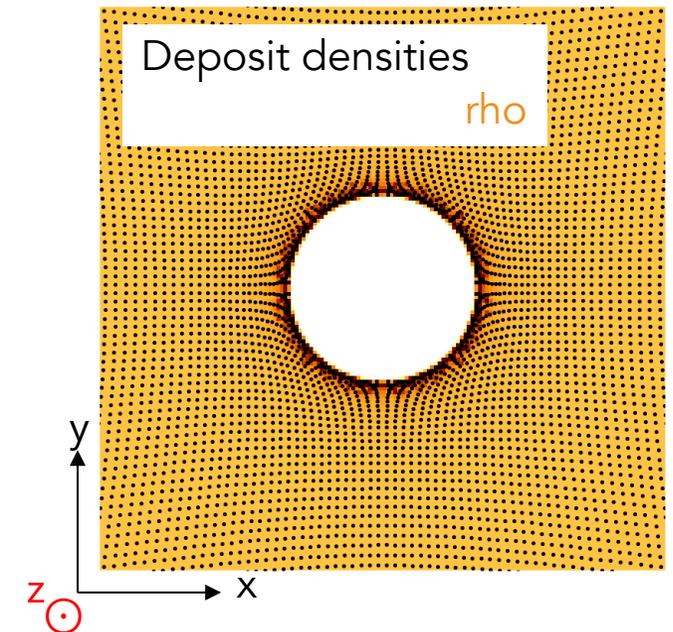


- All PIC operations occur on the 2D transverse domain
- Plasma particles are advanced in  $\zeta$  (z), not in time
- (specific to HiPACE++: beams and lasers also advanced in the swipe)
- A simulation does  $n_t \times n_z$  PIC iterations on domain  $n_x \times n_y$
- (EM PIC: does  $n_t$  PIC iterations on domain  $n_x \times n_y \times n_z$ )

# The plasma response is computed with a swipe from head to tile

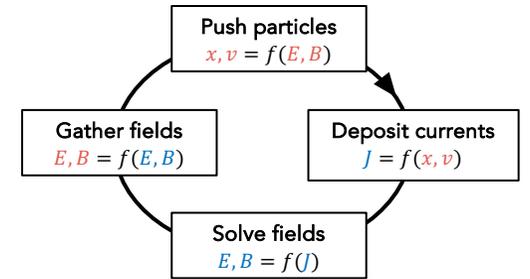
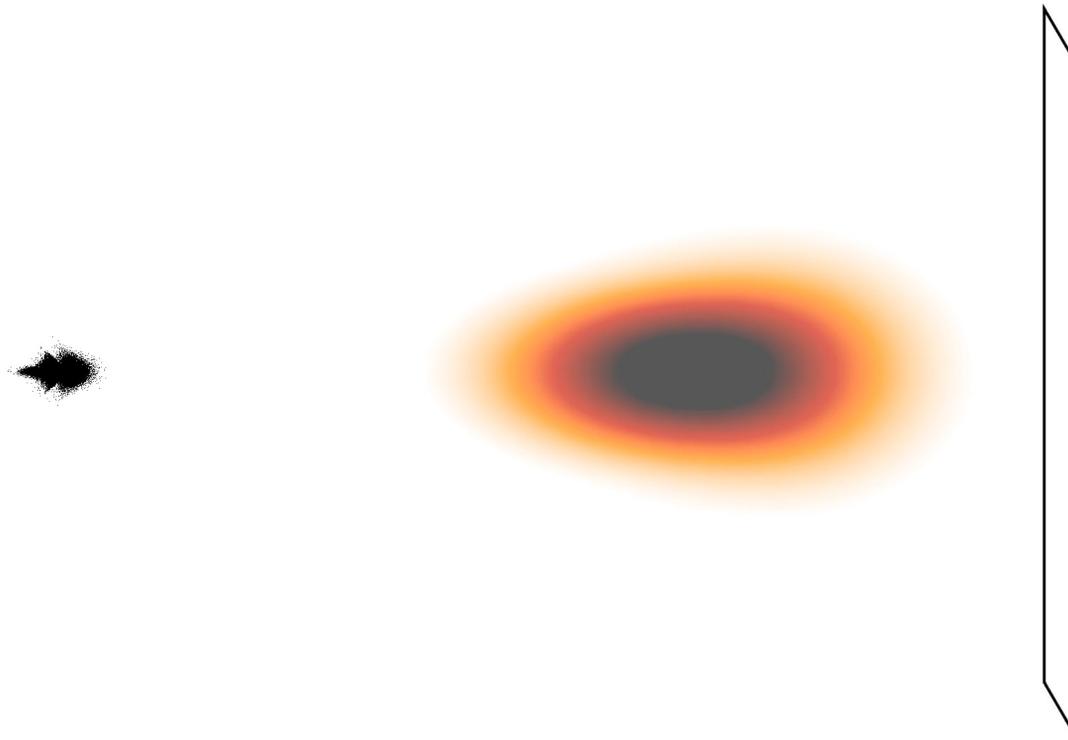


2D slice  
Field & particles

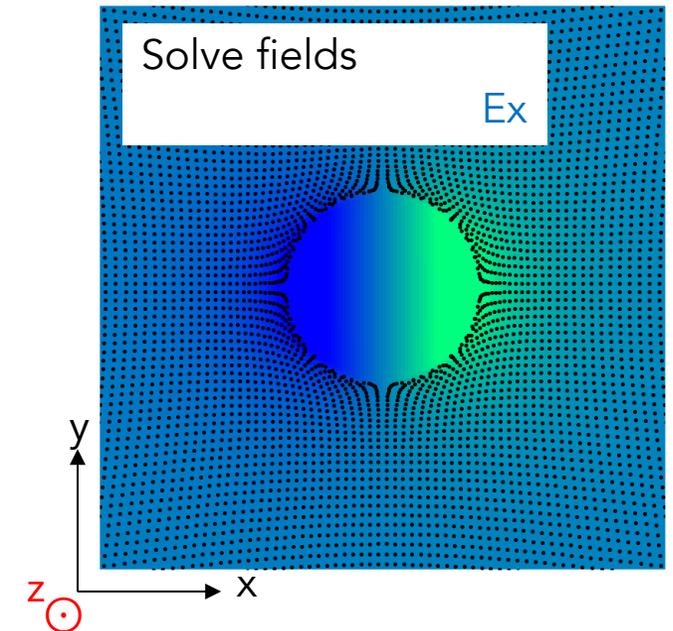


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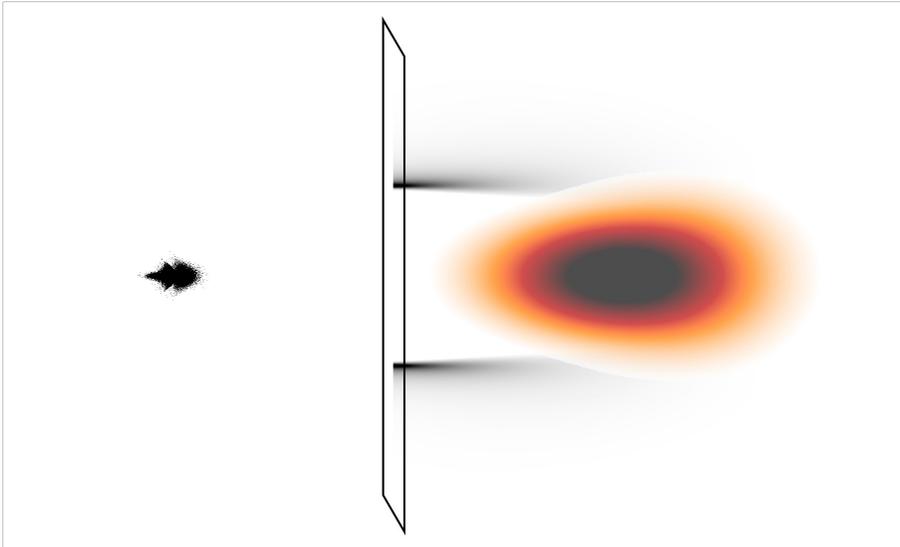


2D slice  
Field & particles



- All PIC operations occur on the 2D transverse domain
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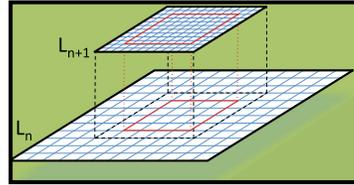
# Mesh Refinement in HiPACE++



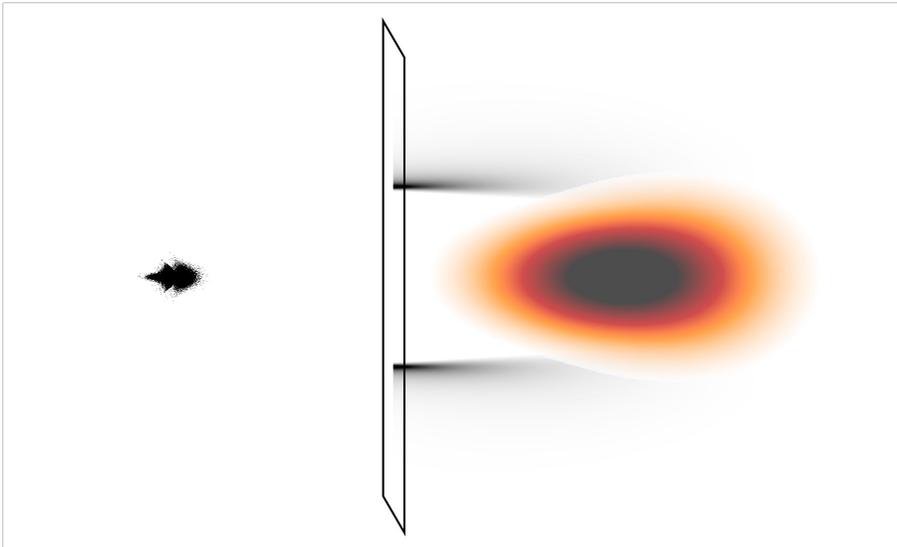
- Deposit densities (beam and plasma)  $\rho, \vec{J}, S_x, S_y$
- Solve fields ( $E_x - cB_y, E_y + cB_x, E_z \cdot B_z$ ) and  $(B_x \cdot B_y)$
- Advance plasma particles by 1 slice ( $-\Delta\zeta$ )
- Advance beam particles by 1 time step ( $+\Delta t$ )

# Mesh Refinement in HiPACE++

➤ MR in electrostatic PIC



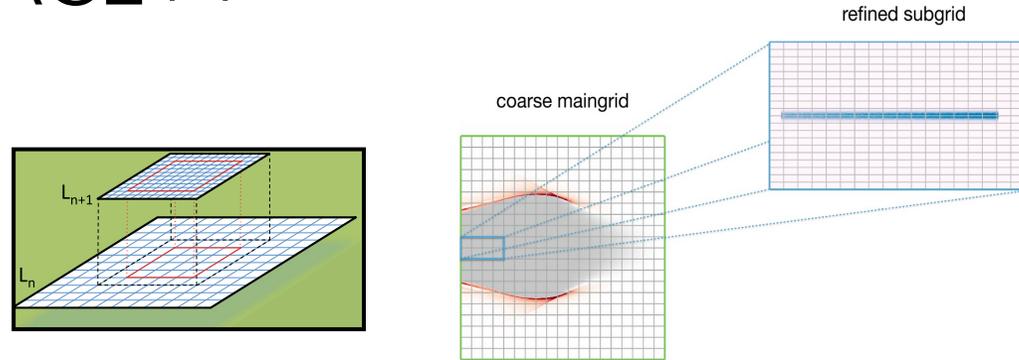
J.-L. Vay et al., Comput. Sci. & Disc. 5, 014019 (2012)



- Deposit densities (beam and plasma)  $\rho, \vec{J}, S_x, S_y$
- Solve fields ( $E_x - cB_y, E_y + cB_x, E_z \cdot B_z$ ) and  $(B_x \cdot B_y)$
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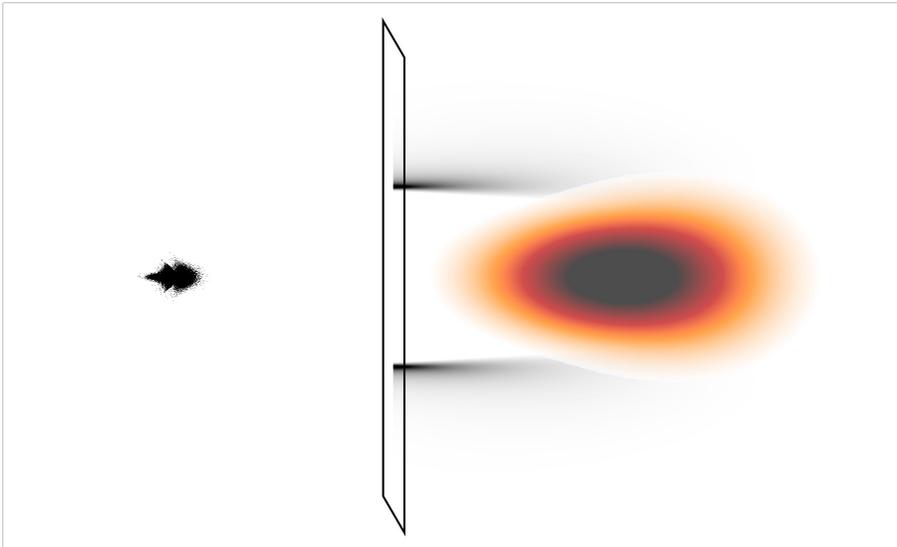
# Mesh Refinement in HiPACE++

- MR in electrostatic PIC
- MR with quasi-static PIC, no crossing



J.-L. Vay et al., Comput. Sci. & Disc. 5, 014019 (2012)

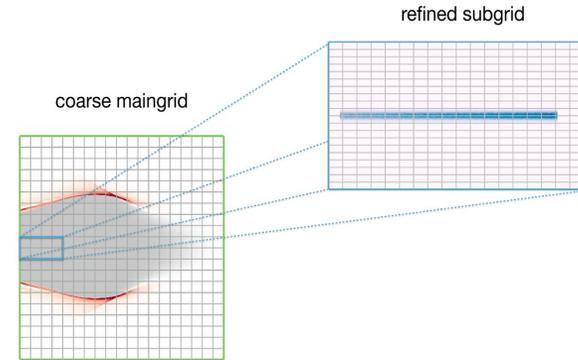
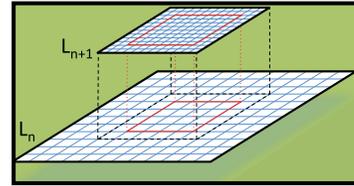
T. J. Mehrling et al., IEEE, AAC (2018)



- Deposit densities (beam and plasma)  $\rho, \vec{J}, S_x, S_y$
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# Mesh Refinement in HiPACE++

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- MR with quasi-static PIC, no crossing



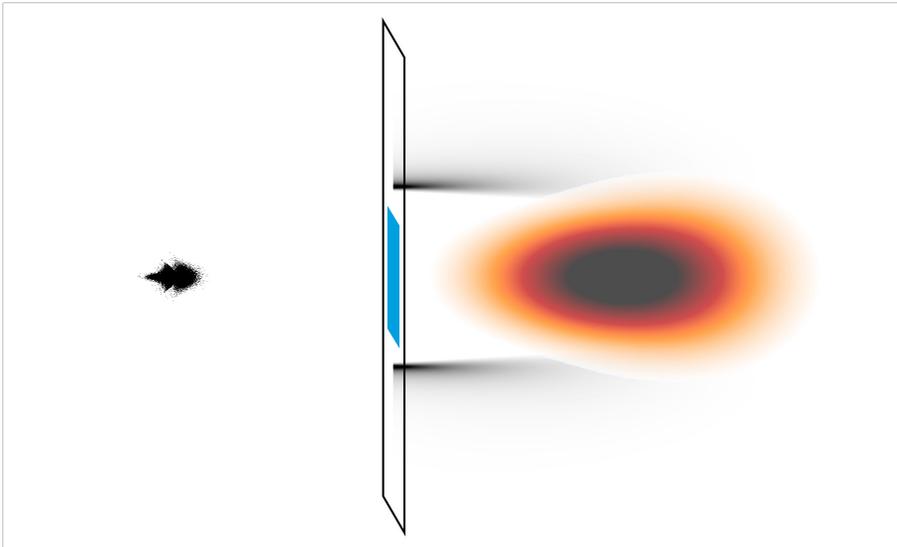
Severin  
Diederichs



Alexander  
Sinn

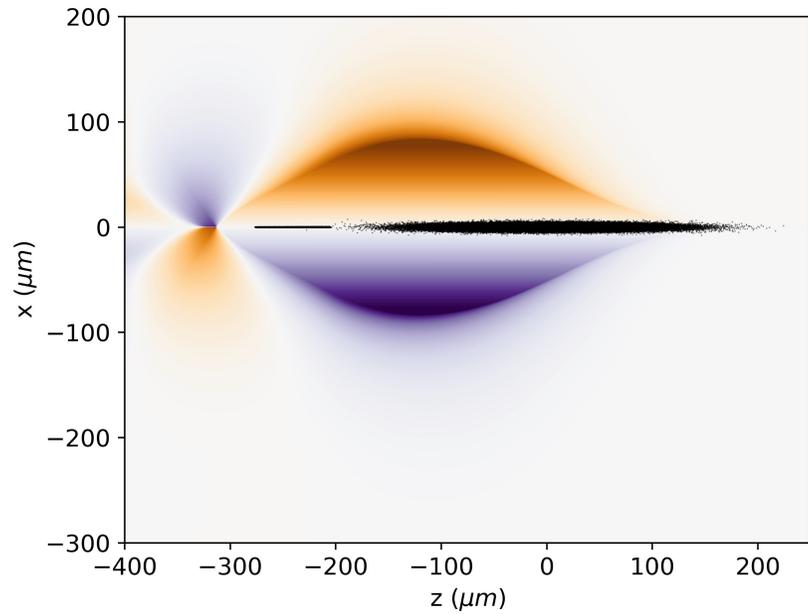
J.-L. Vay et al., Comput. Sci. & Disc. 5, 014019 (2012)

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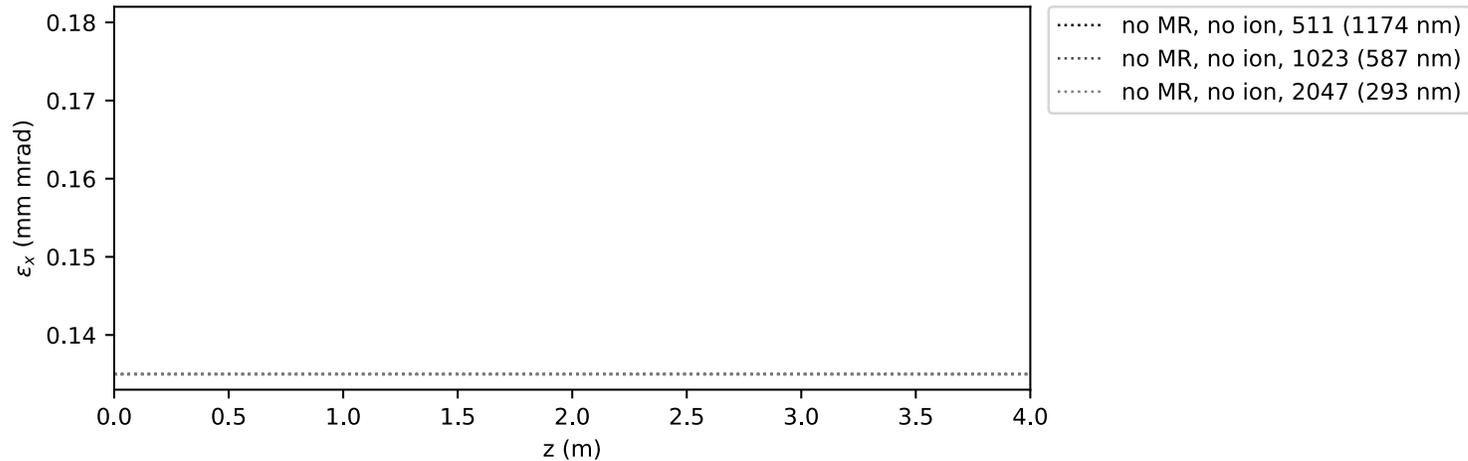


- Deposit densities (beam and plasma)  $\rho, \vec{J}, S_x, S_y$   
on all levels
- Solve fields ( $E_x - cB_y, E_y + cB_x, E_z \cdot B_z$ ) and ( $B_x \cdot B_y$ )  
BC on fine patch, solve, Interpolate in ghost cells
- Tag by level
- Advance plasma particles by 1 slice ( $-\Delta\zeta$ )
- Advance beam particles by 1 time step ( $+\Delta t$ )

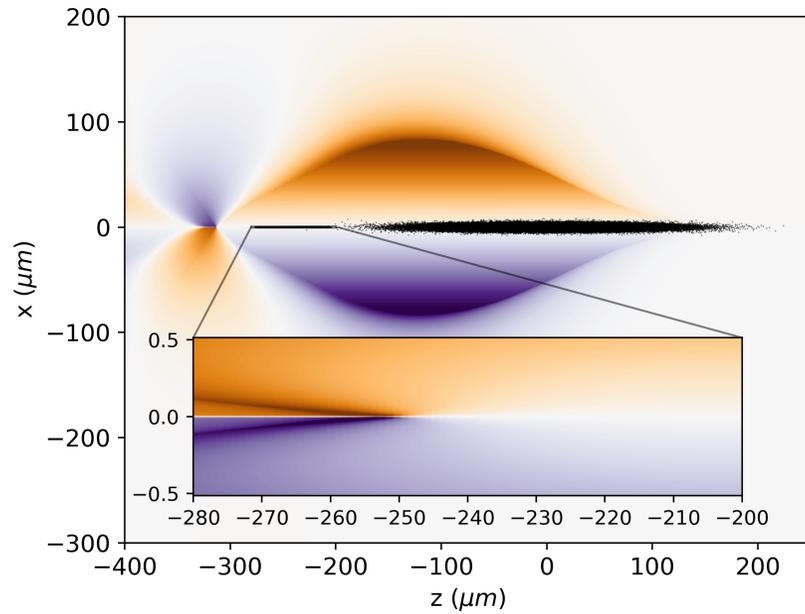
# Converged simulations in collider-relevant range are ~~feasible~~ cheap



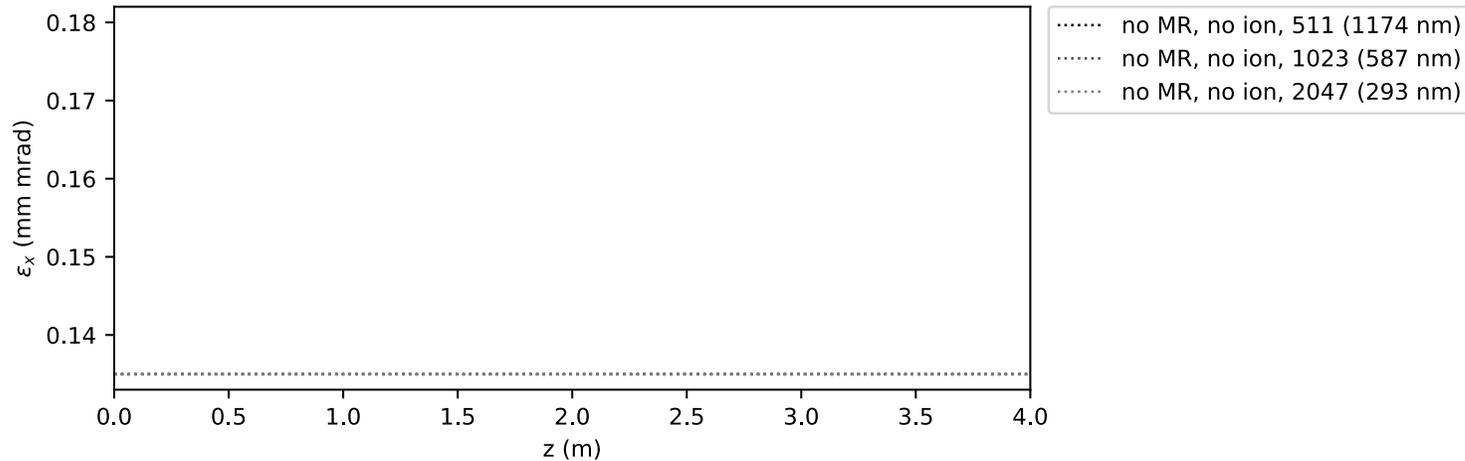
Projected emittance x



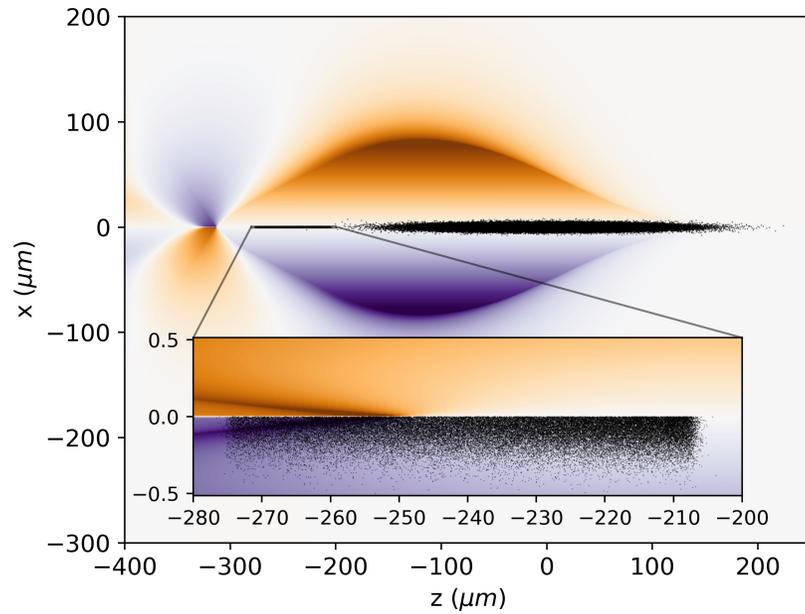
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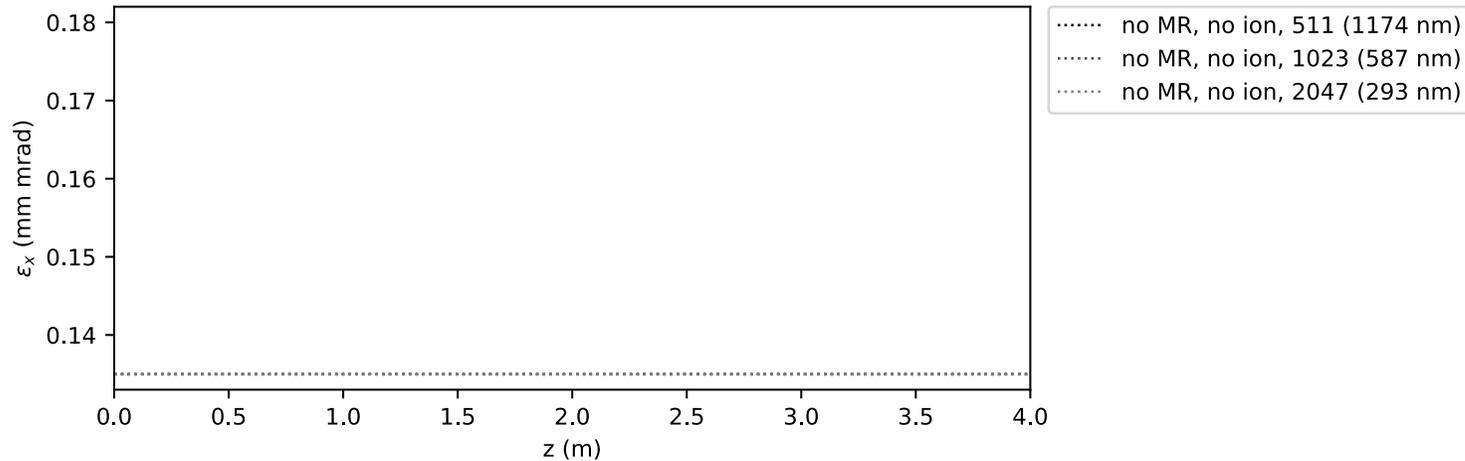
Projected emittance x



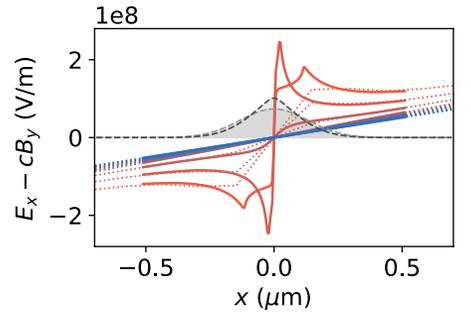
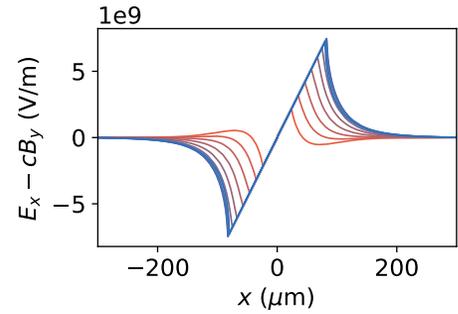
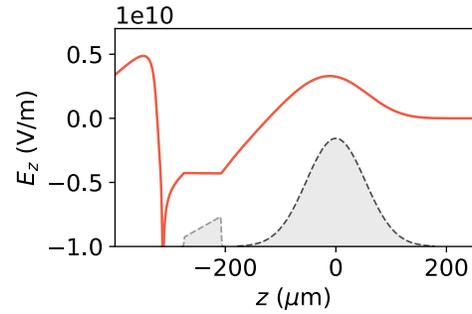
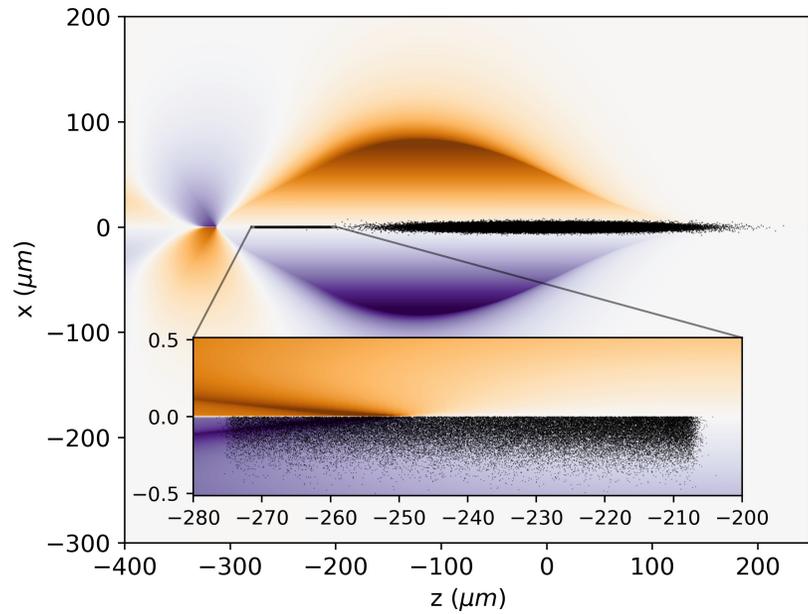
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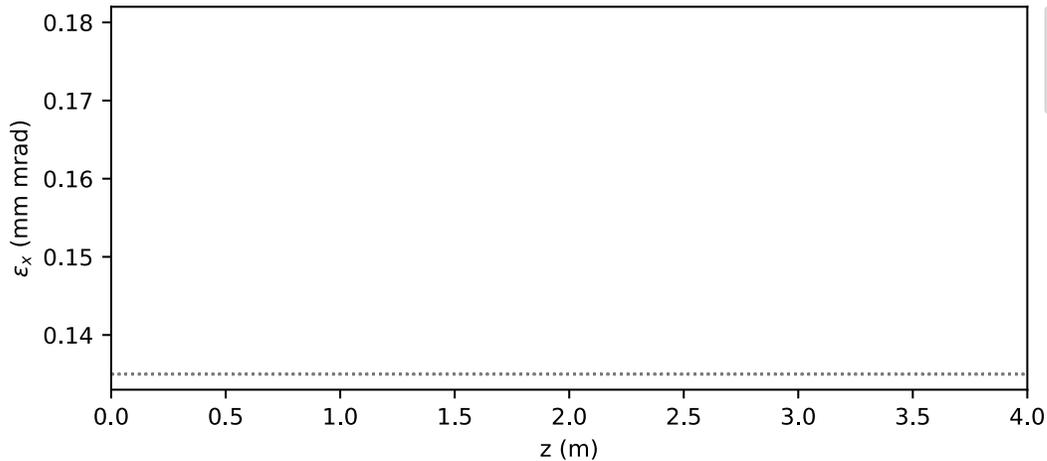
Projected emittance x



# Converged simulations in collider-relevant range are ~~feasible~~ cheap

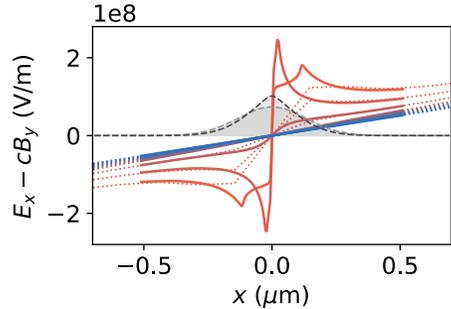
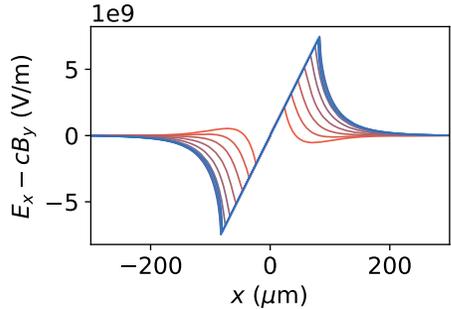
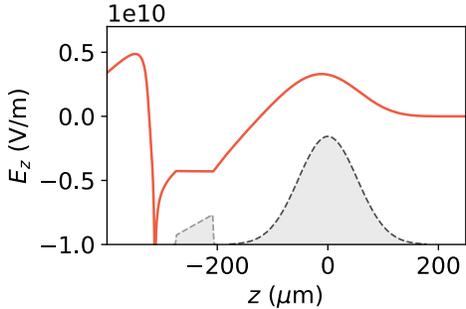
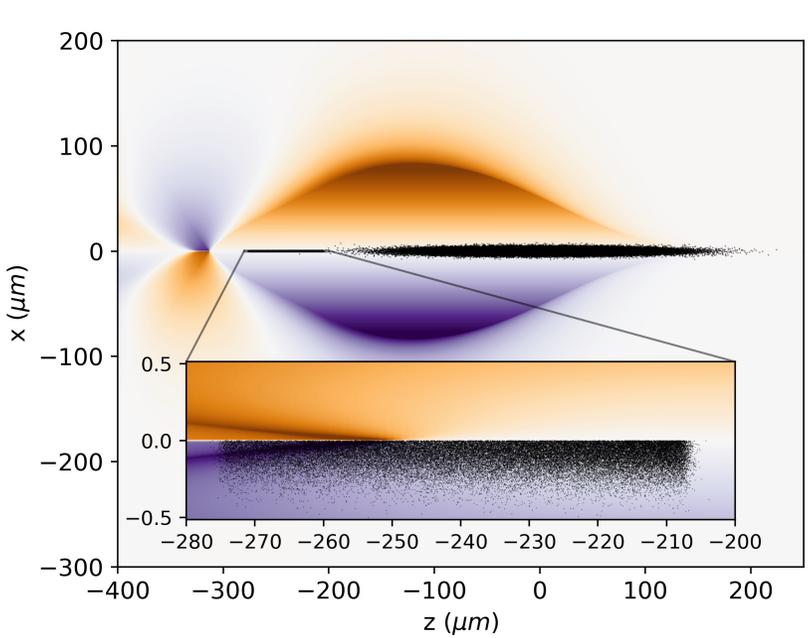


Projected emittance x

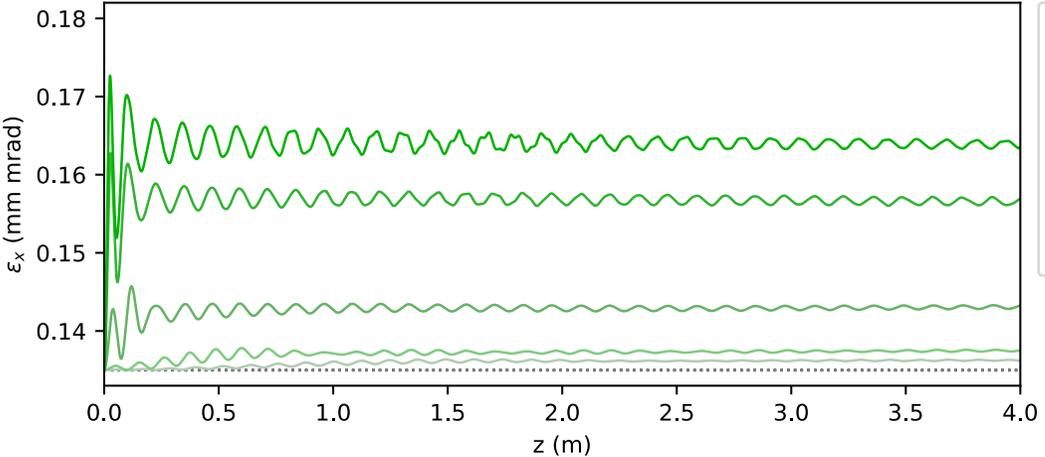


- ..... no MR, no ion, 511 (1174 nm)
- ..... no MR, no ion, 1023 (587 nm)
- ..... no MR, no ion, 2047 (293 nm)

# Converged simulations in collider-relevant range are ~~feasible~~ cheap

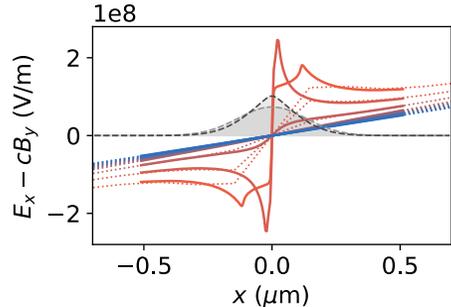
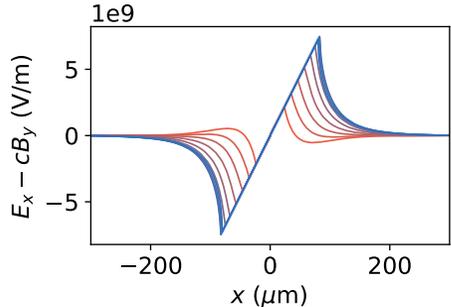
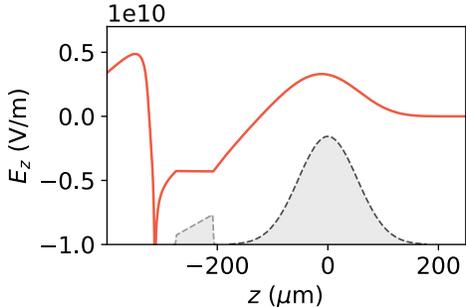
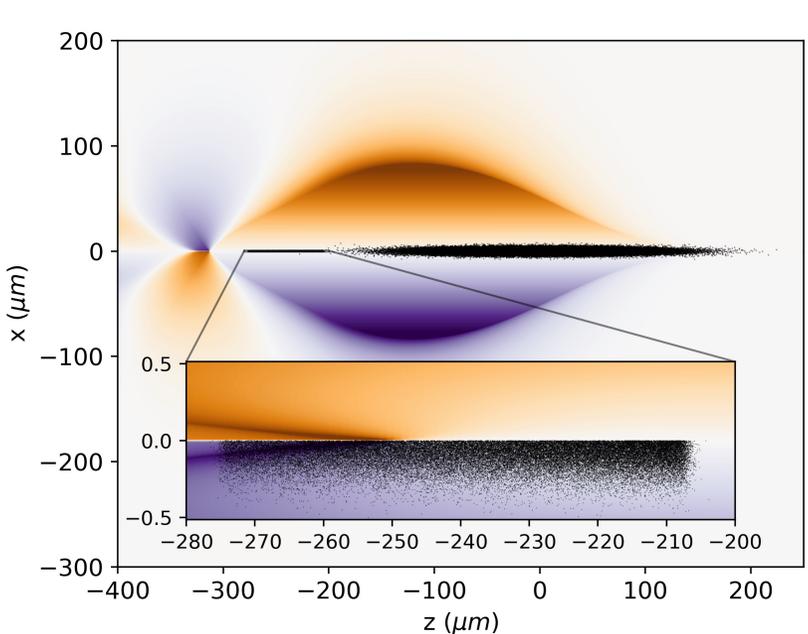


Projected emittance x

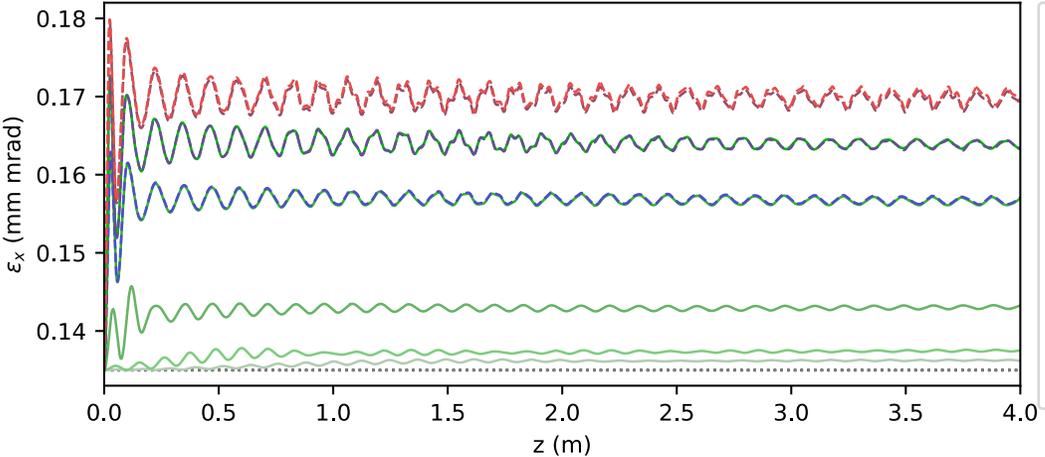


- ..... no MR, no ion, 511 (1174 nm)
- ..... no MR, no ion, 1023 (587 nm)
- ..... no MR, no ion, 2047 (293 nm)
- no MR, ion, 511 (1170 nm)
- no MR, ion, 1023 (587 nm)
- no MR, ion, 2047 (293 nm)
- no MR, ion, 4095 (147 nm)
- no MR, ion, 8191 (73 nm)

# Converged simulations in collider-relevant range are ~~feasible~~ cheap

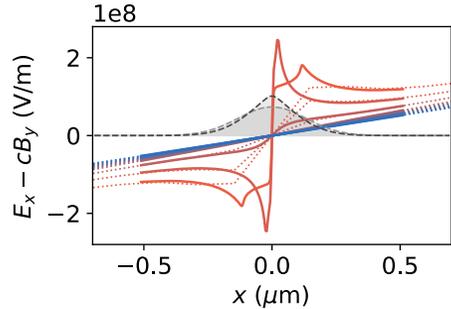
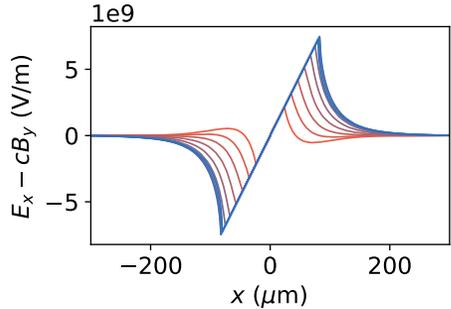
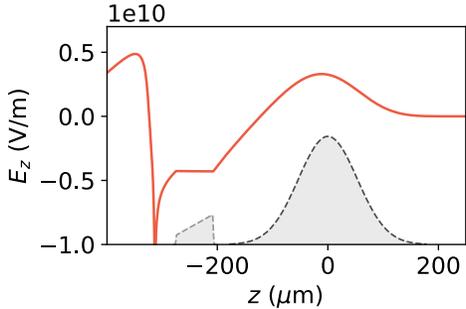
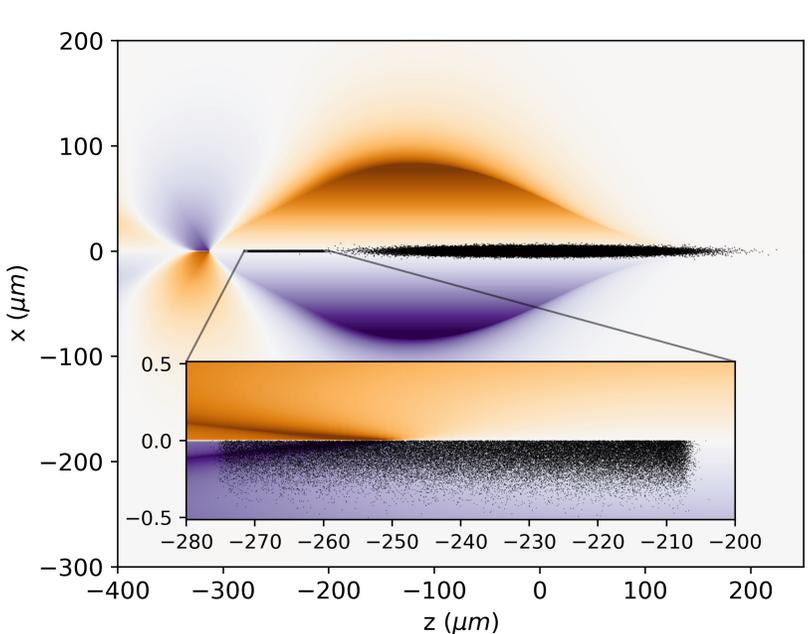


Projected emittance x

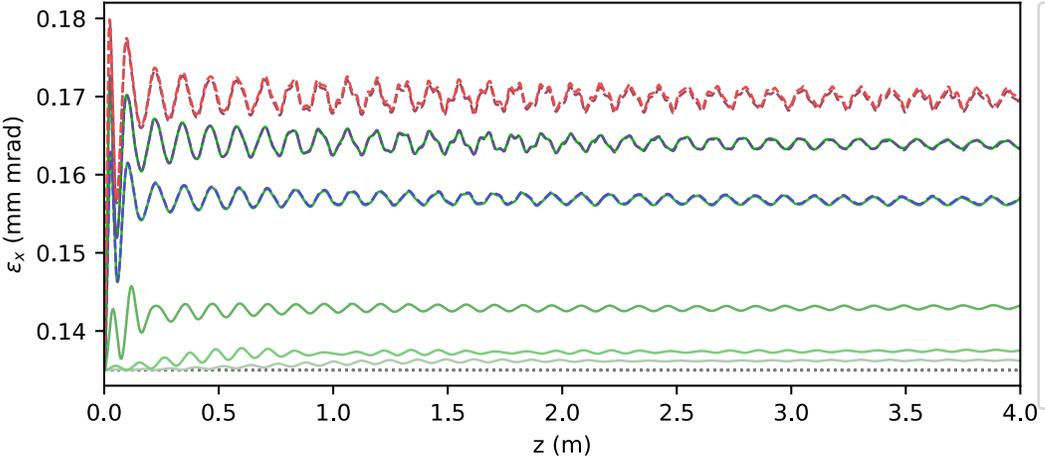


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- ..... no MR, ion, 2047 (293 nm)
- ..... no MR, ion, 4095 (147 nm)
- ..... no MR, ion, 8191 (73 nm)
- - - MR, ion, 11 (147 nm)
- - - MR, ion, 22 (83 nm)
- - - MR, ion, 88 (18 nm)
- - - MR, ion, 352 (5 nm)

# Converged simulations in collider-relevant range are ~~feasible~~ cheap



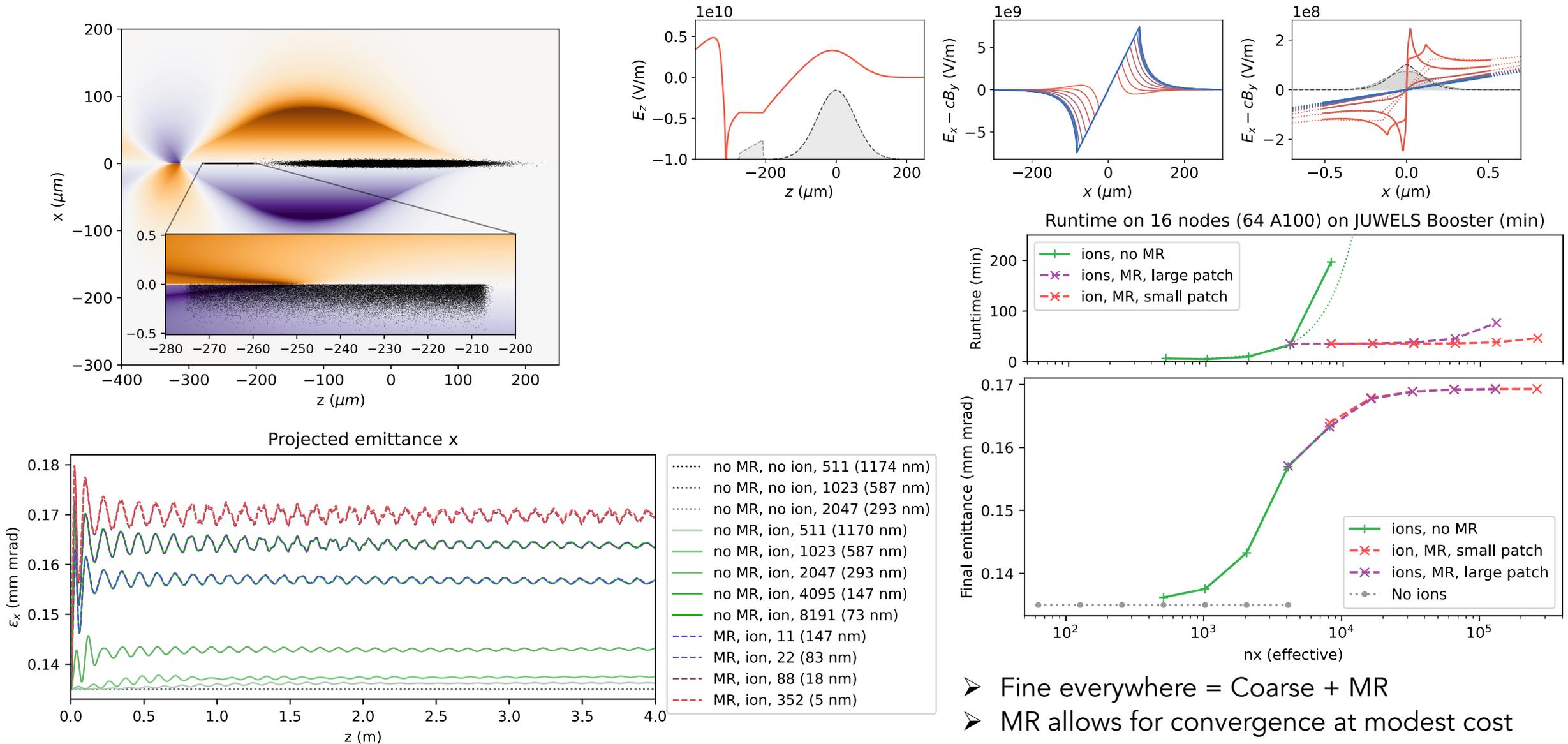
Projected emittance x



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- ..... no MR, ion, 511 (1170 nm)
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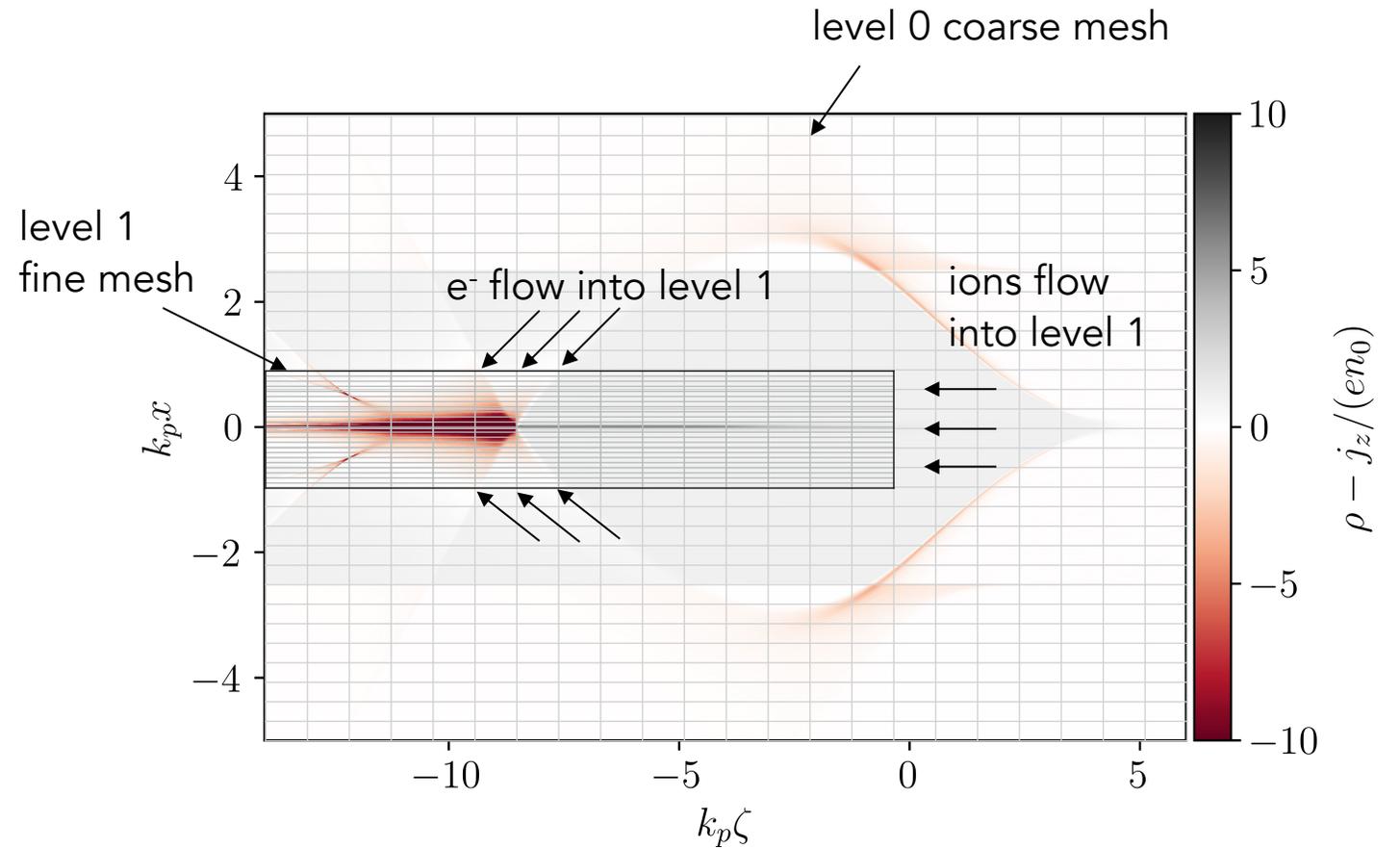
- Fine everywhere = Coarse + MR
- MR allows for convergence at modest cost

# Converged simulations in collider-relevant range are ~~feasible~~ cheap

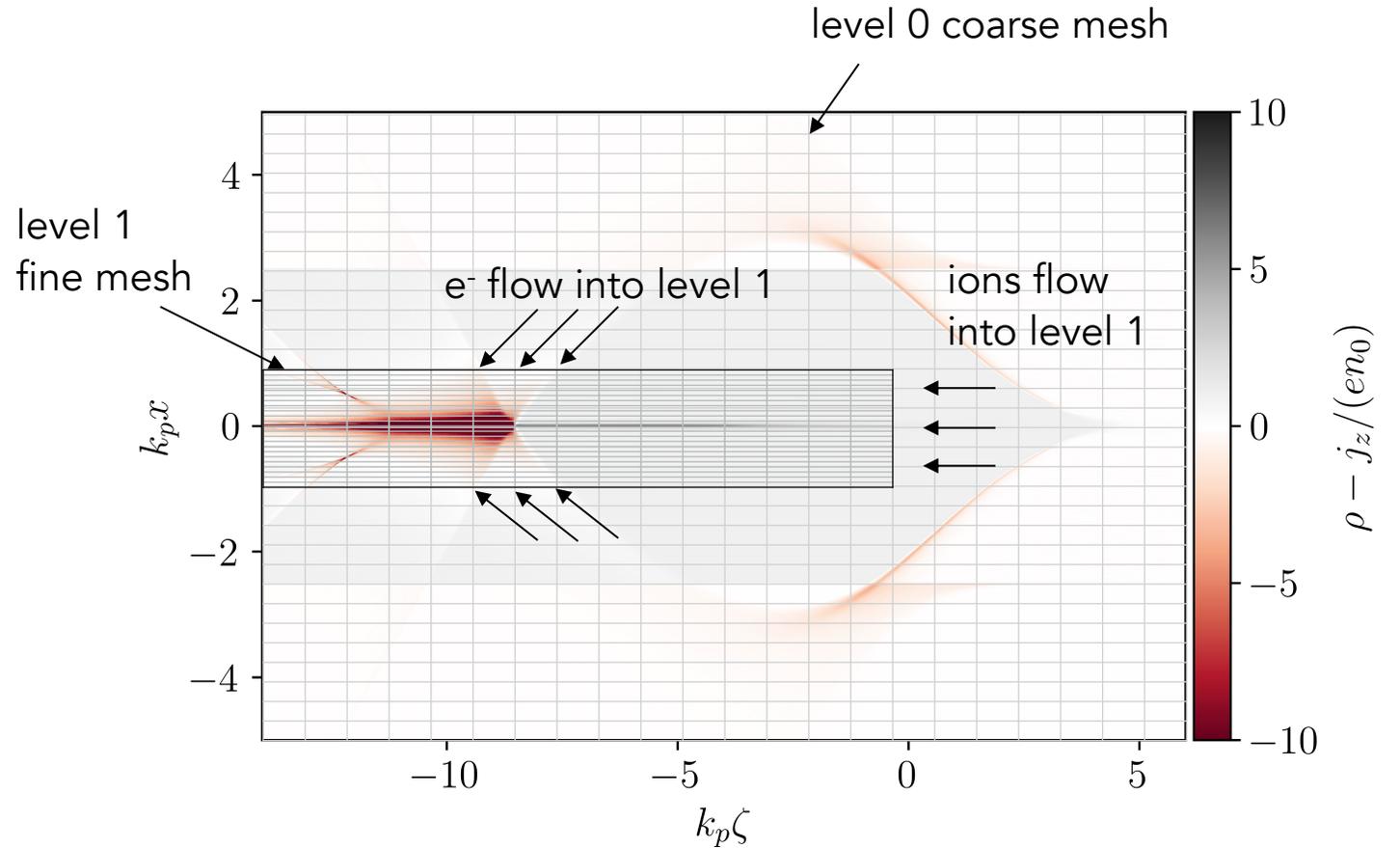
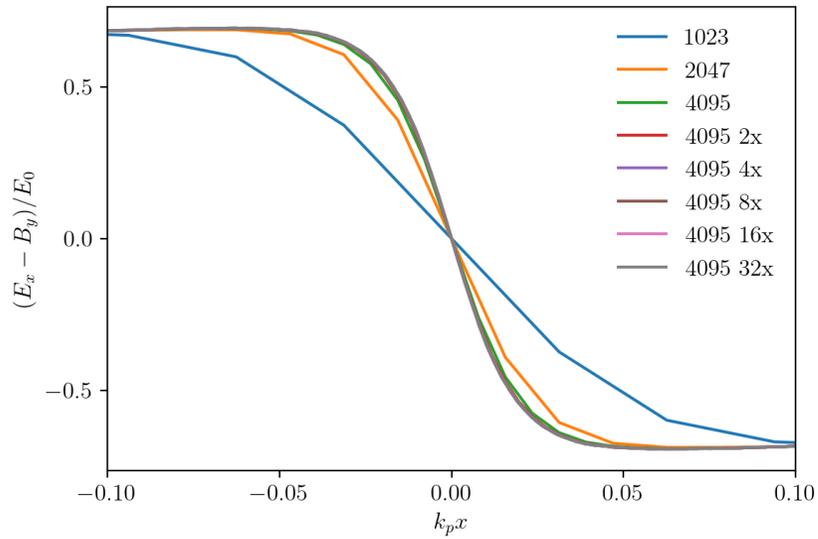


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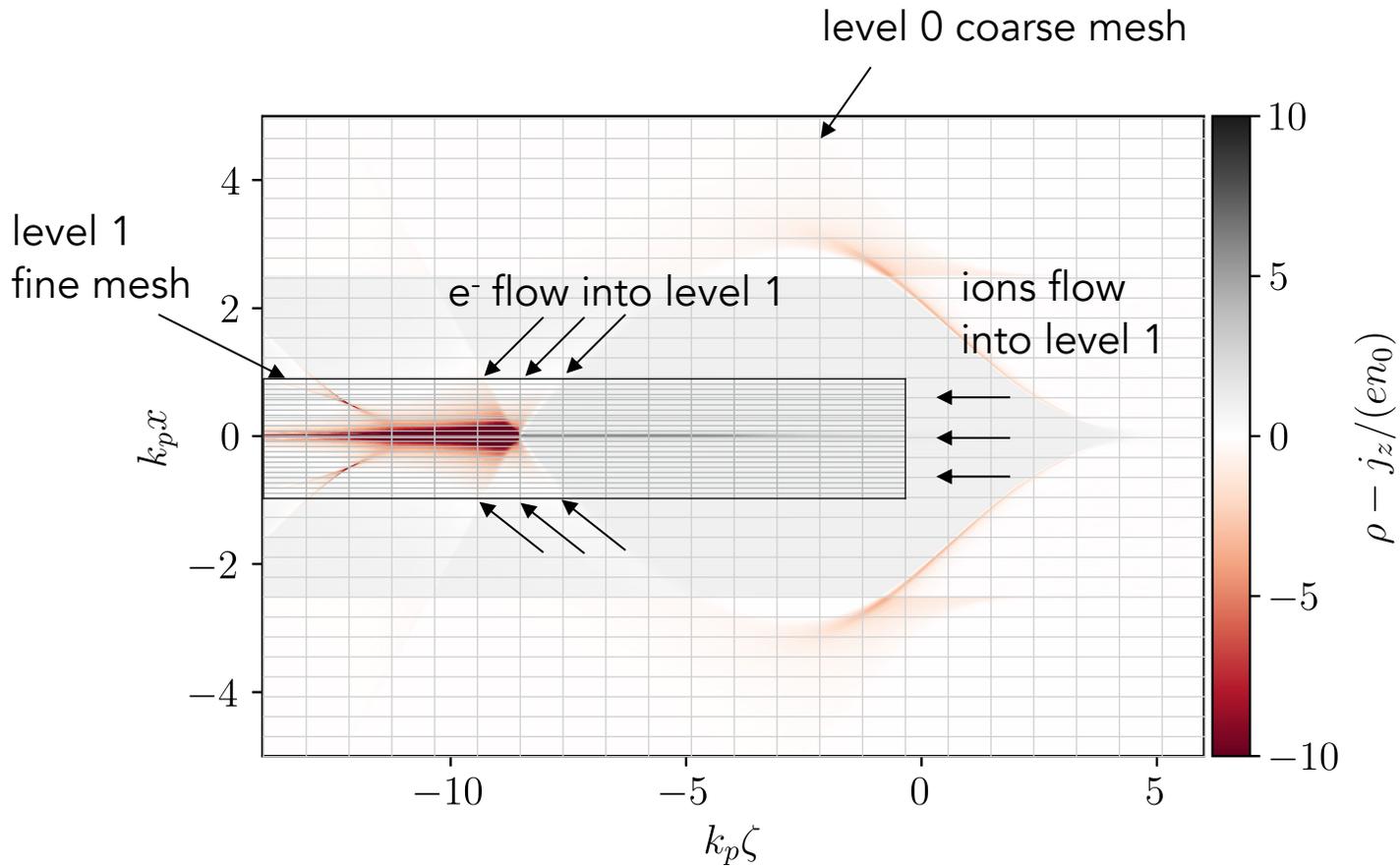
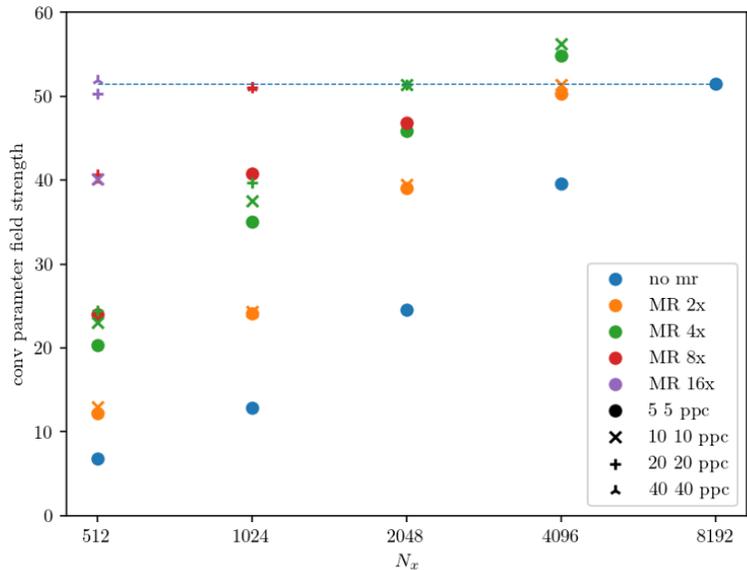
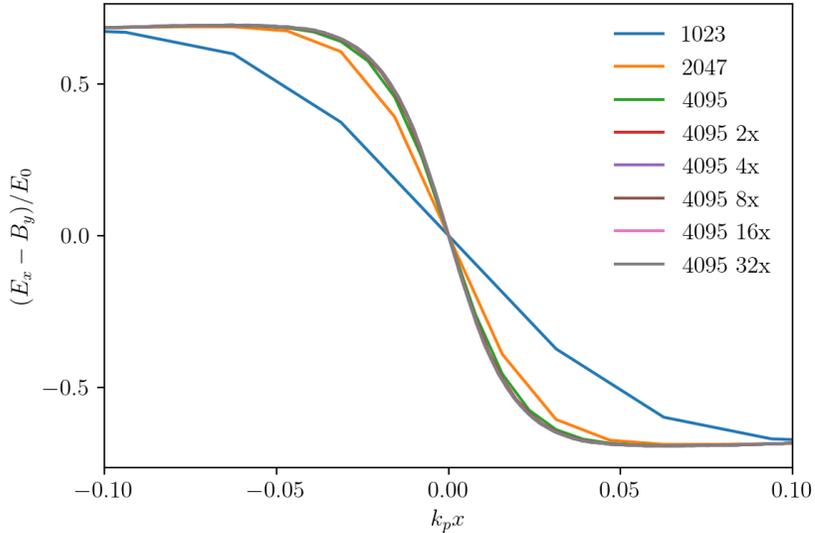
# Challenging positron acceleration simulations benefit from MR



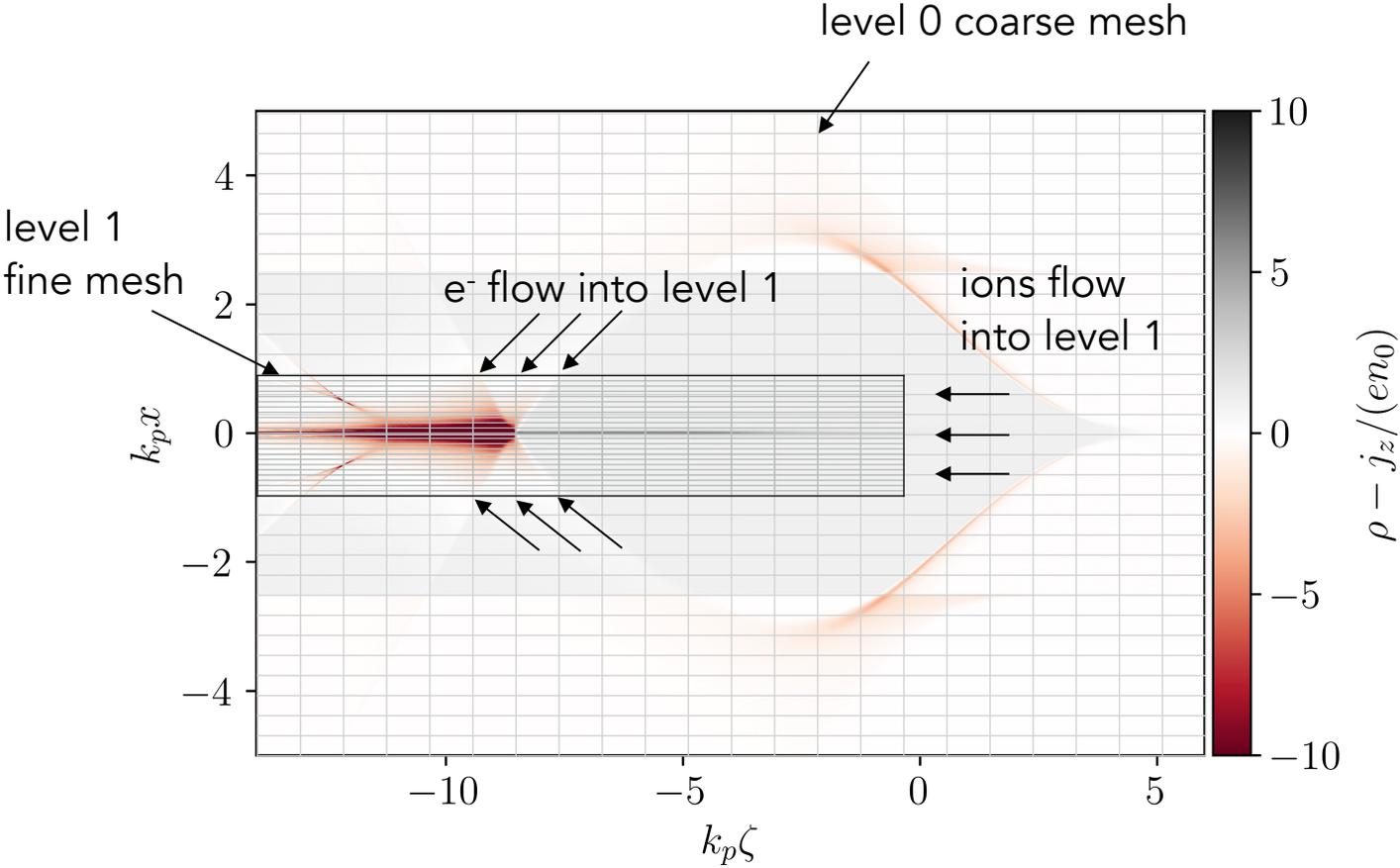
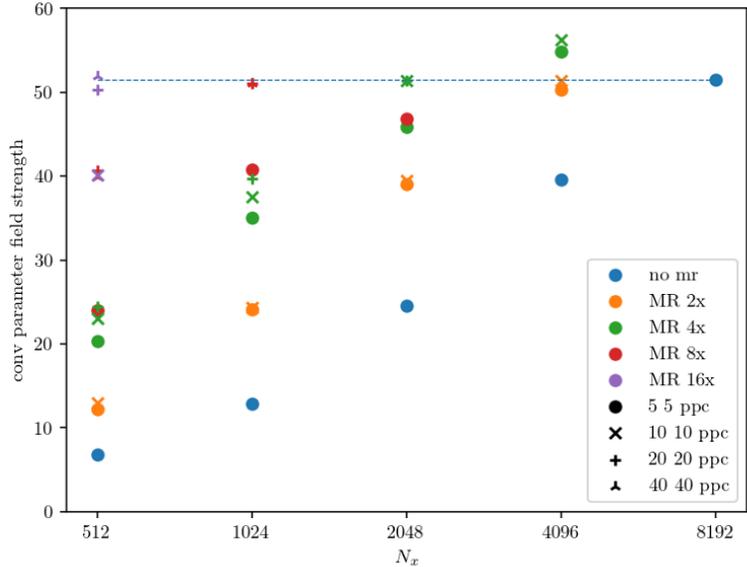
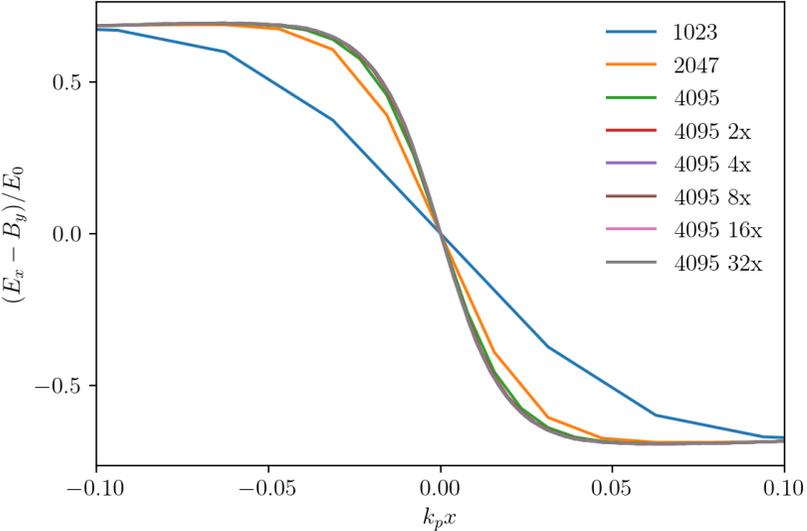
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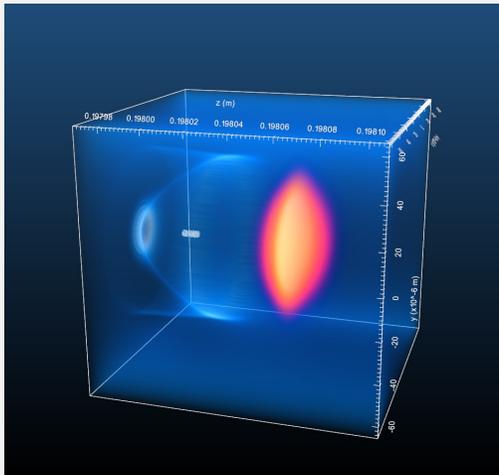


- Coarse resolution + MR = fine resolution everywhere
- MR allows for convergence at modest cost

# Wake-T: multi-stage axisymmetric simulations on a laptop

## Wakefield particle Tracker [1]

- 2D (RZ) axisymmetric, quasi-static
- Particle beam or laser pulse drivers [2]
- Gridless model based on explicit solver [3]
- Python, open-source, openPMD
- Beam optics



→ Multi-stage simulations within second/minutes on a laptop

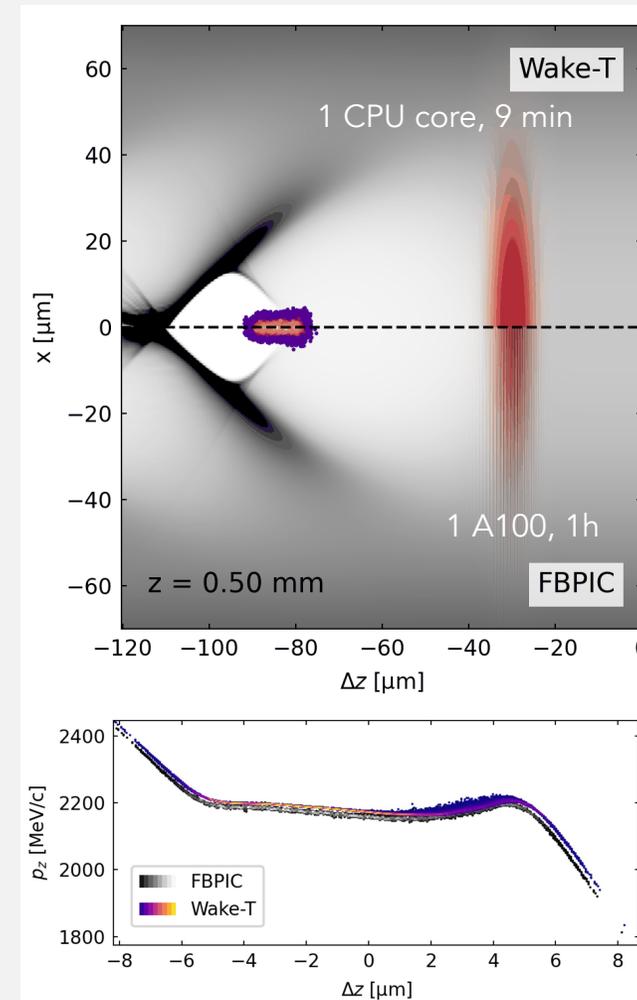
<https://github.com/AngelFP/Wake-T>

<https://wake-t.readthedocs.io>

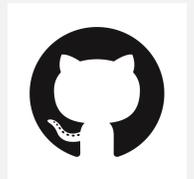
[1] A. Ferran Pousa et al., J. Phys.: Conf. Ser. (2019)

[2] C. Benedetti et al., PPCF 60 014002 (2018)

[3] P. Baxevanis and G. Stupakov, PRAB 21 (2018)



Ángel Ferran Pousa

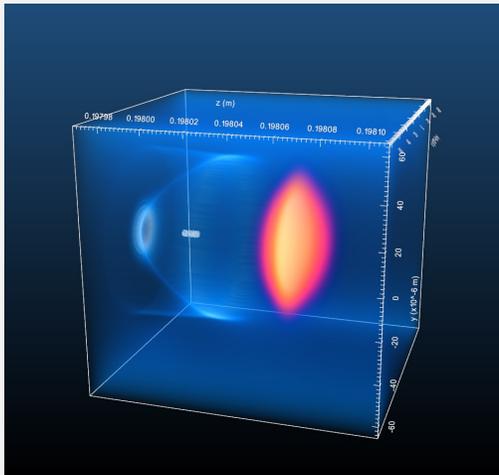


WakeT

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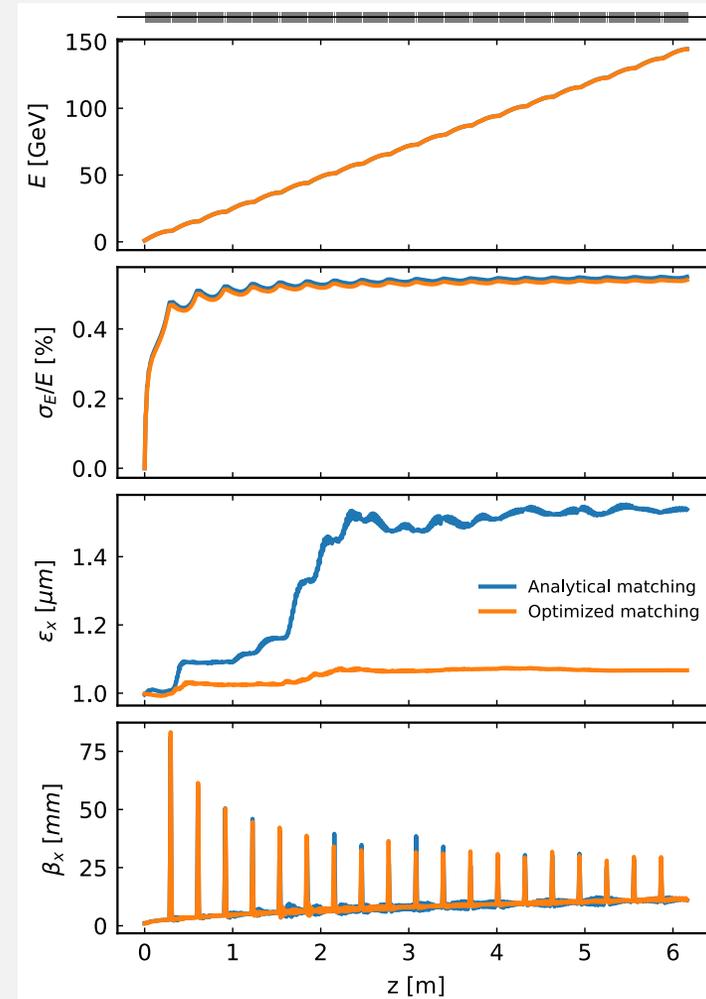
<https://github.com/AngelFP/Wake-T>

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[1] A. Ferran Pousa et al., J. Phys.: Conf. Ser. (2019)

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A. Ferran Pousa, IPAC 2023

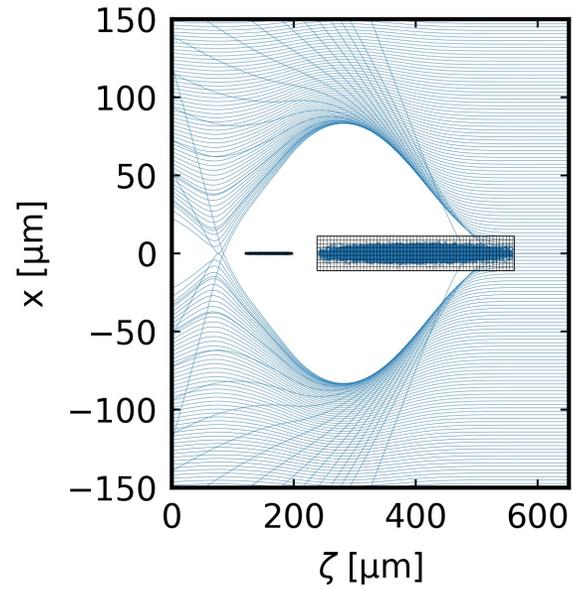


Ángel Ferran Pousa

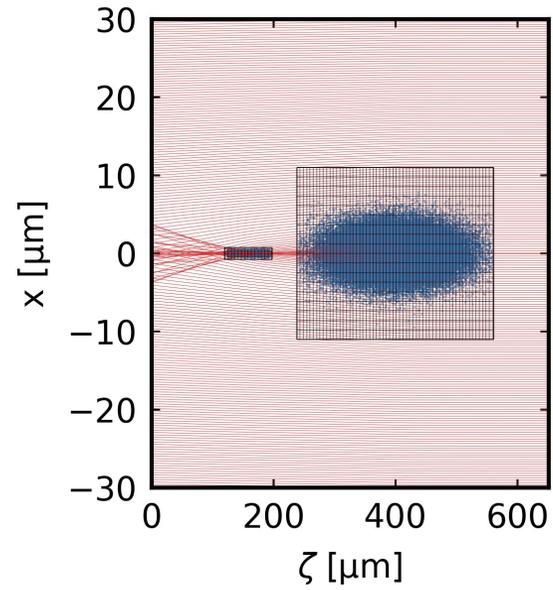
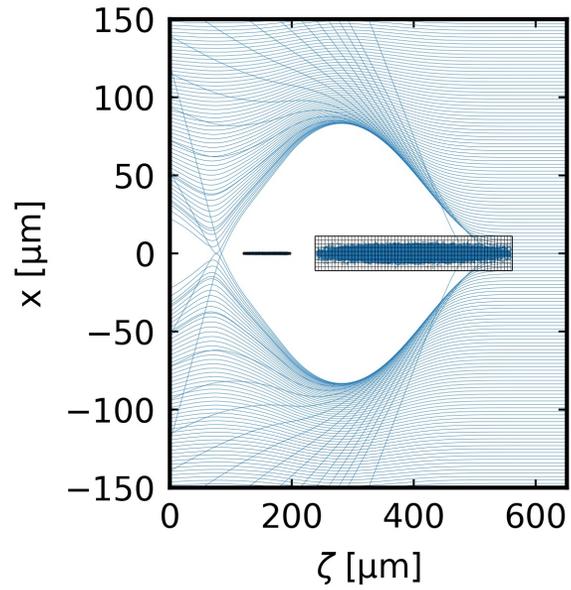


WakeT

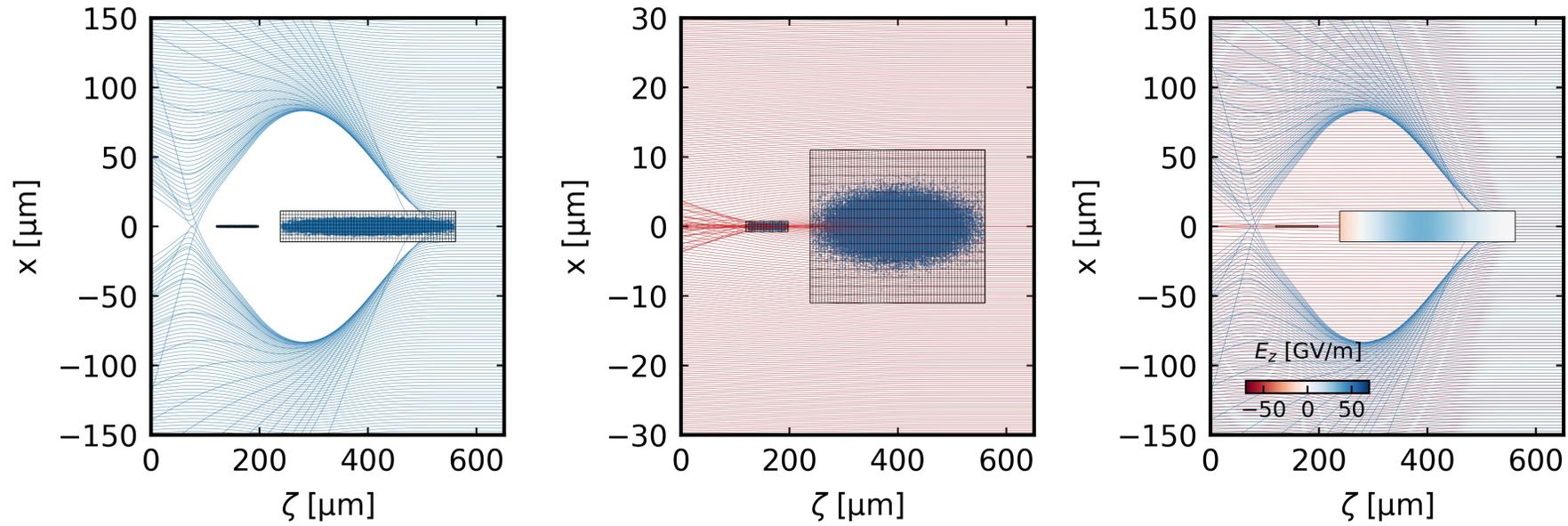
# Wake-T: an adaptive grid in a gridless method



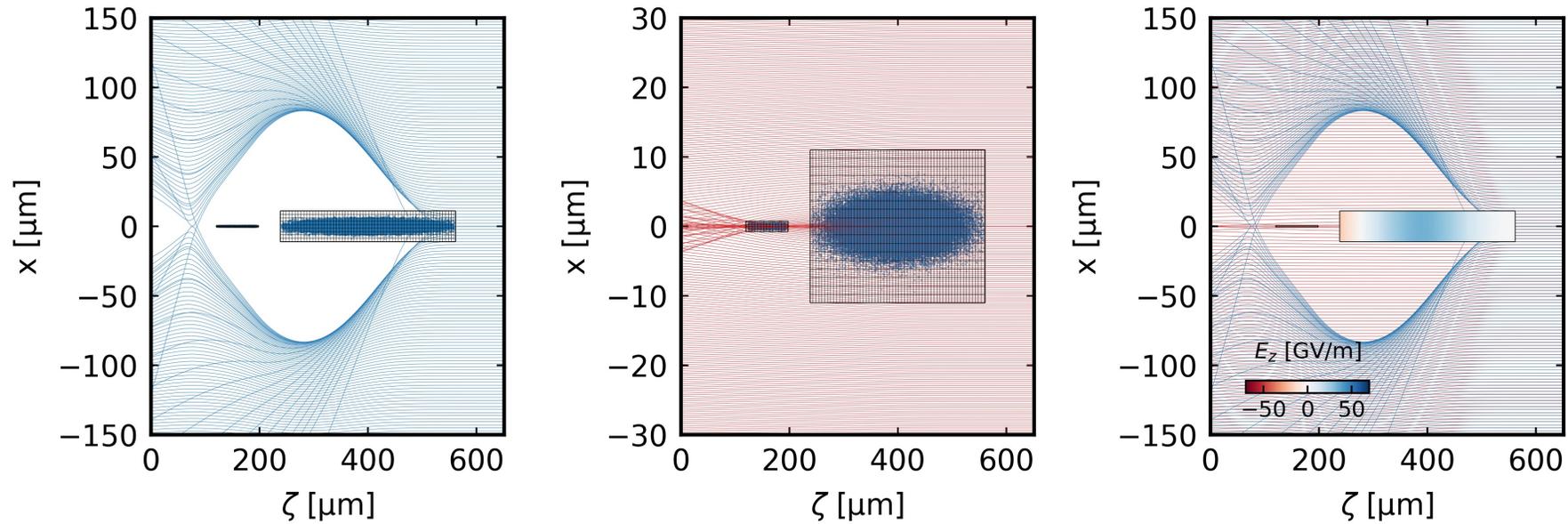
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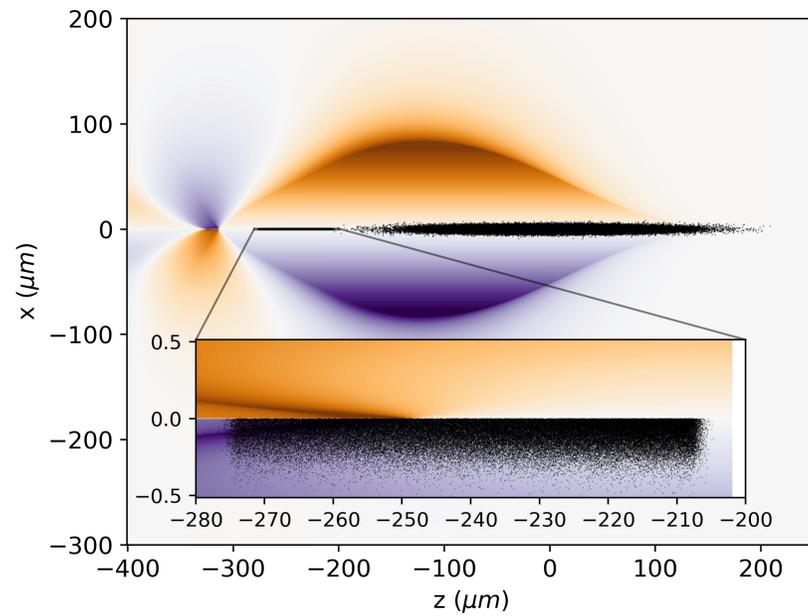


# Wake-T: an adaptive grid in a gridless method

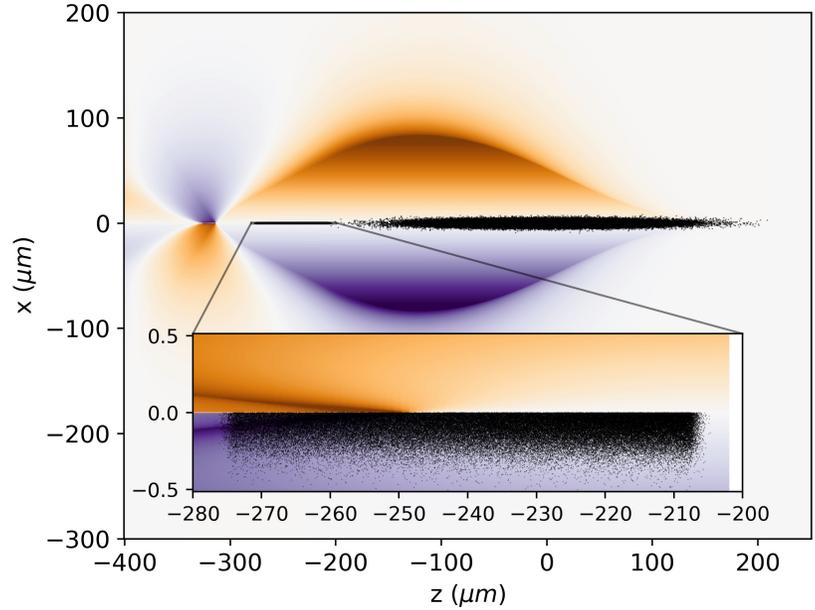


- Plasma advance does not need a grid
- Beam advance uses an adaptive grid

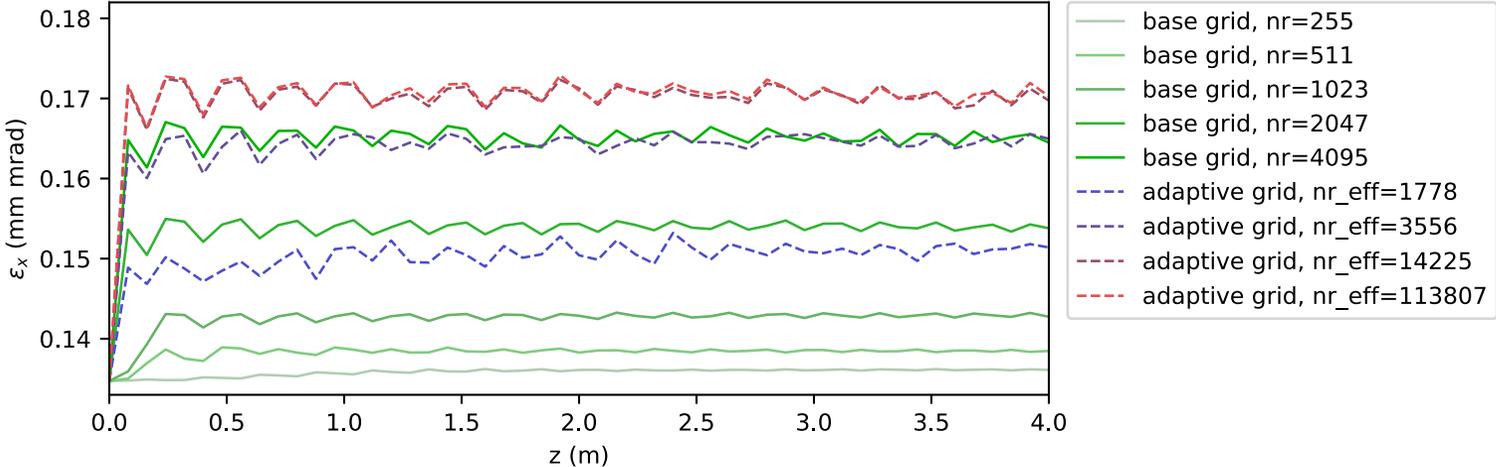
# Realistic simulations of collider parameters on a laptop w/ Wake-T



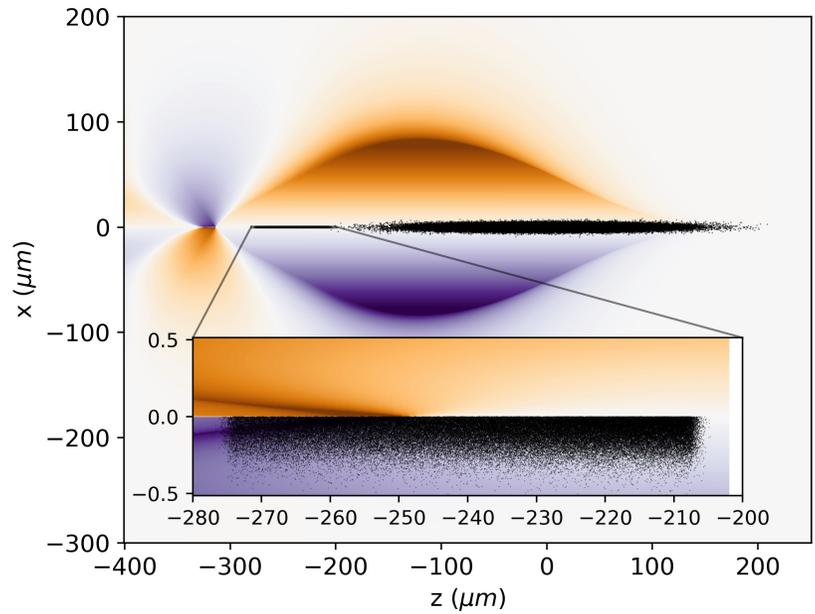
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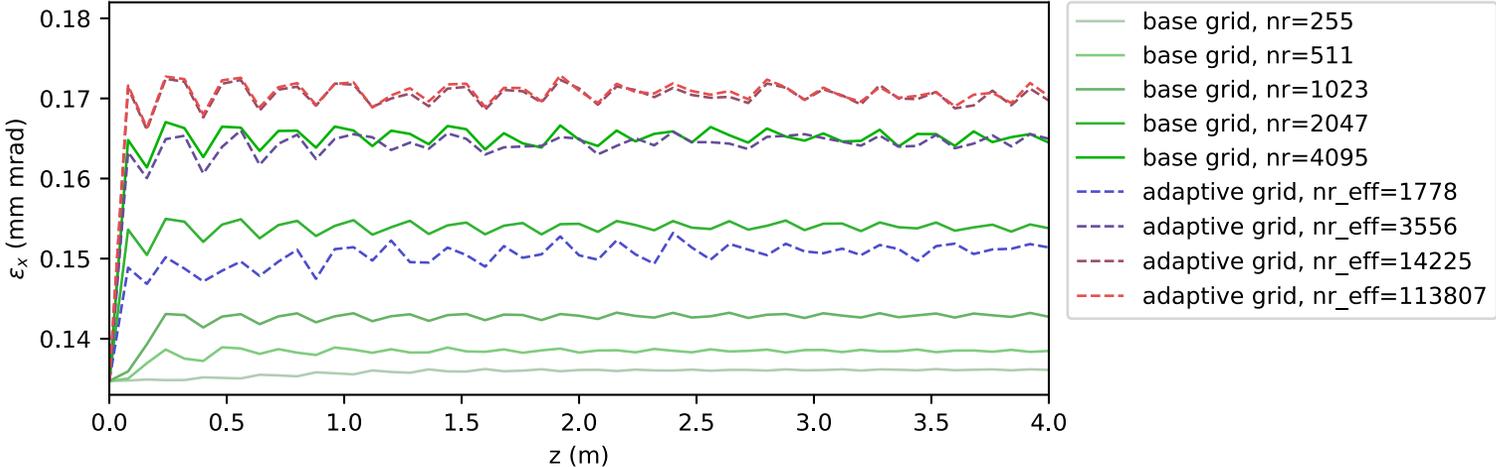
Projected emittance x



# Realistic simulations of collider parameters on a laptop w/ Wake-T

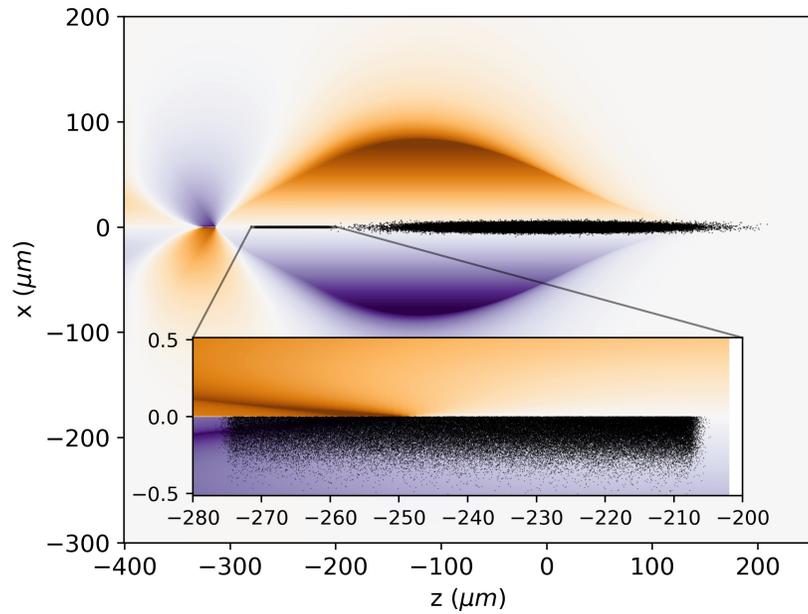


Projected emittance x

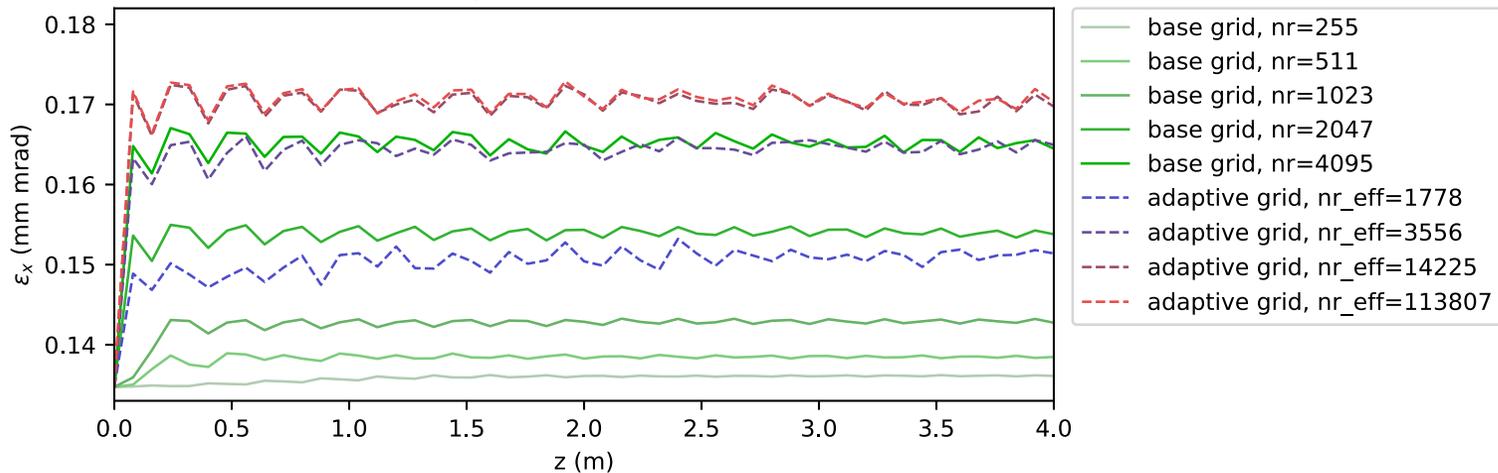


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- MR allows for convergence at modest cost

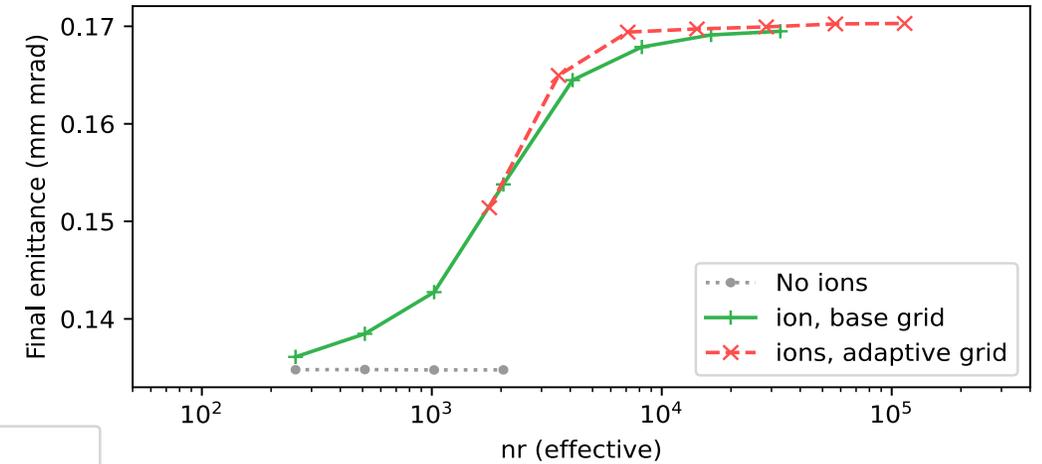
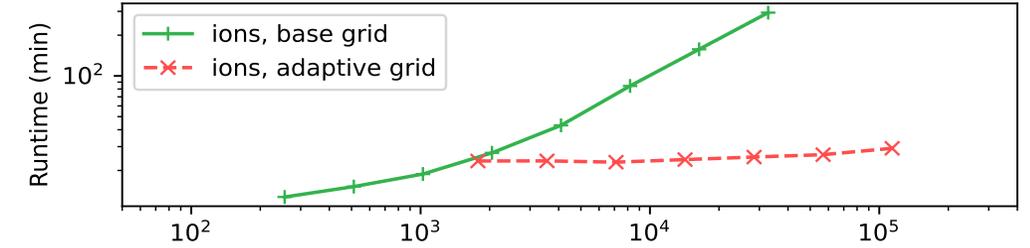
# Realistic simulations of collider parameters on a laptop w/ Wake-T



Projected emittance x

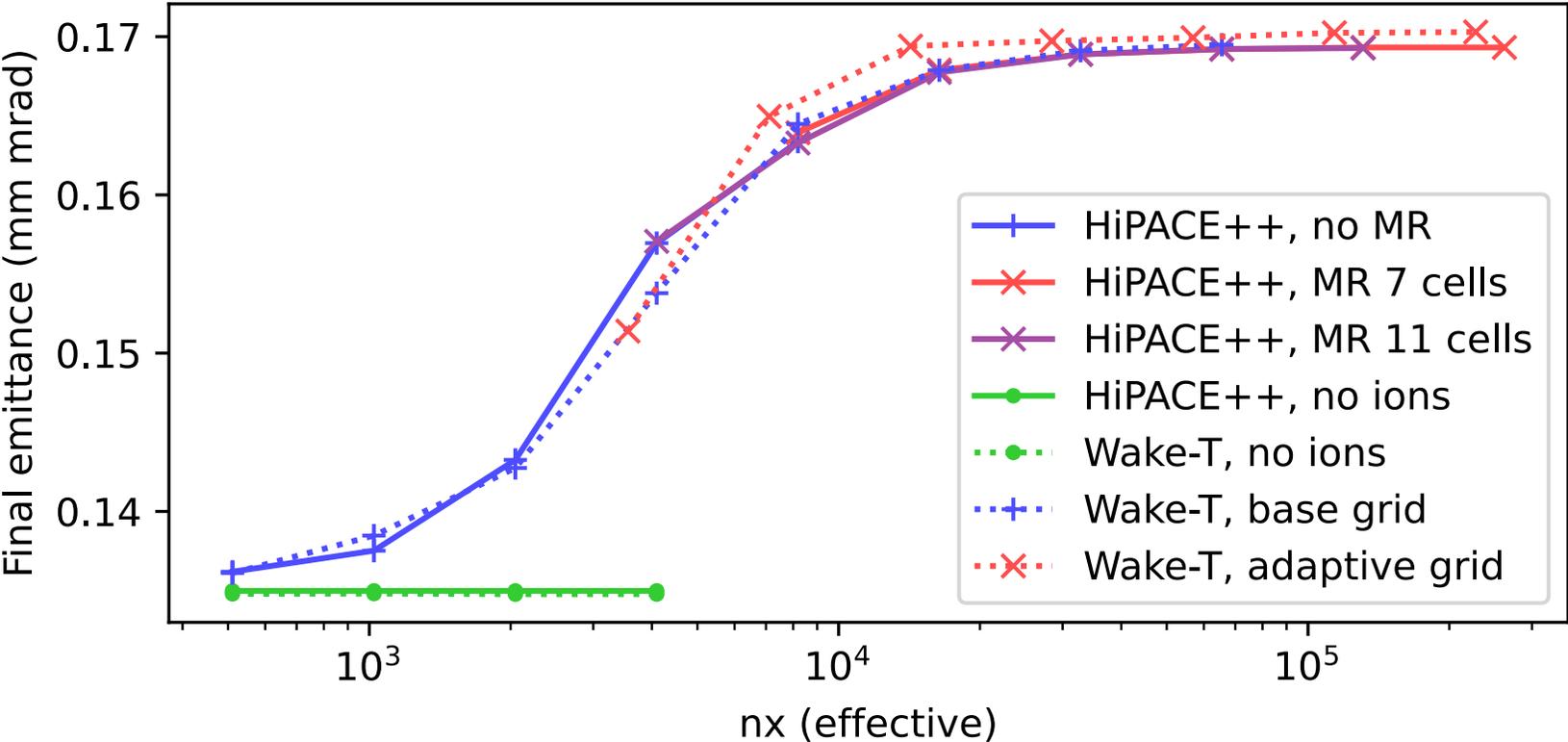


Runtime on 1 standard CPU core (min)



- Adaptive grid = fine resolution everywhere
- MR allows for convergence at modest cost

# HiPACE++ and Wake-T converge to the same (?) result



## Conclusion

- We implemented mesh refinement in HiPACE++ and adaptive grid in Wake-T.
- This allows for converged simulations in collider-relevant parameters.
- Full-physics realistic simulations are very affordable.

## Perspective

- Simplify usage of mesh refinement.
- Address low-hanging fruits for performance optimization.
- Interact with the community towards realistic simulations of collider design.

## Acknowledgements



Severin Diederichs, Ángel Ferran Pousa, Alexander Sinn



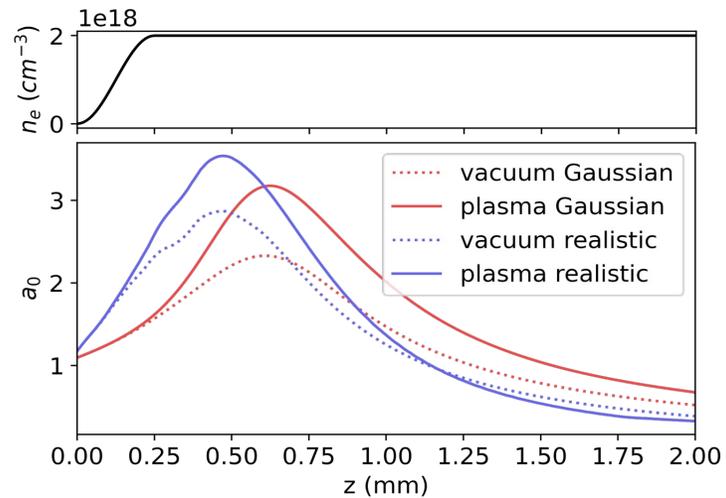
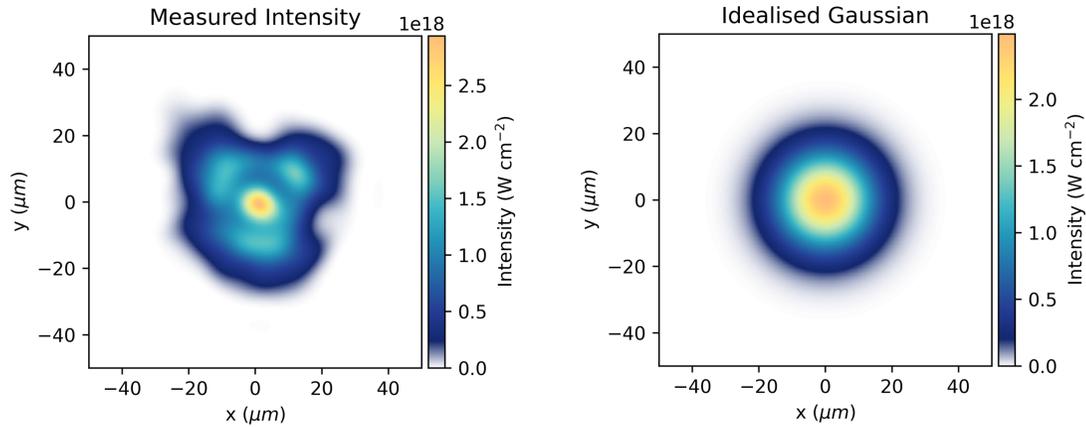
Carlo Benedetti, Axel Huebl, Rémi Lehe, Andrew Myers, Weiqun Zhang, Jean-Luc Vay

Wait, wait, two more slides!

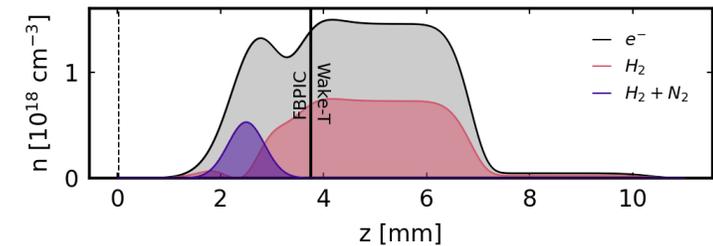
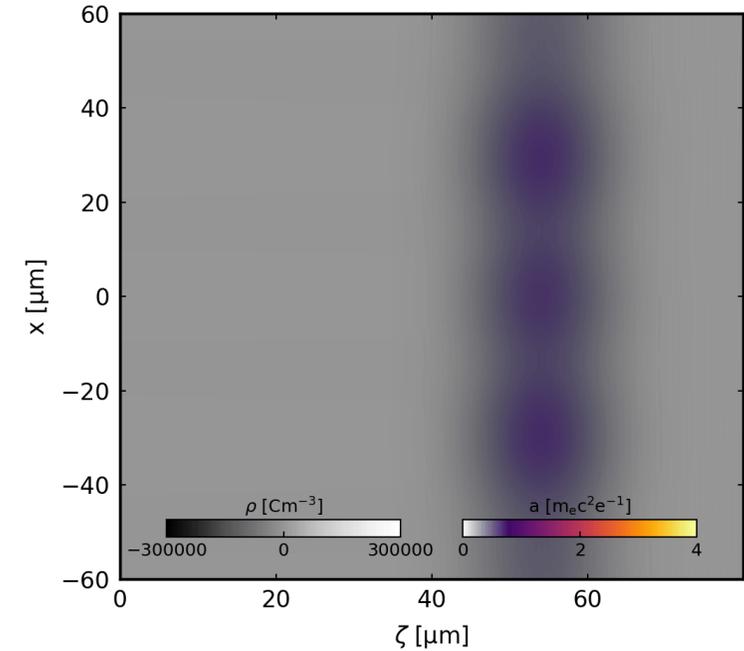


# LASY: LAsEr manipulations made eaSY

## From experiment to simulation



## From simulation to simulation

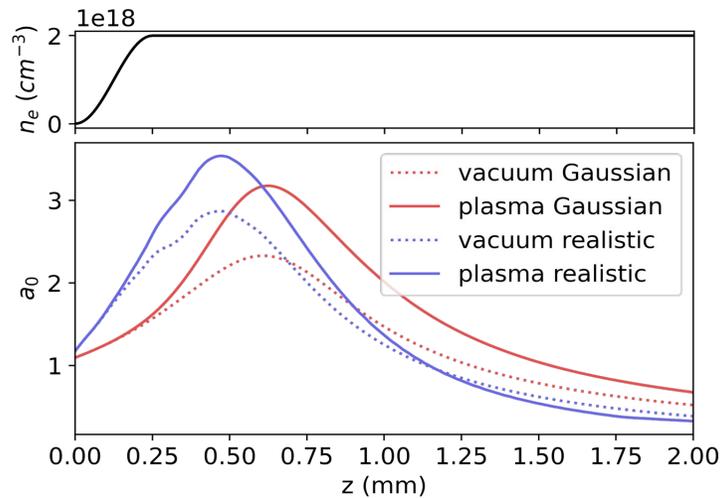
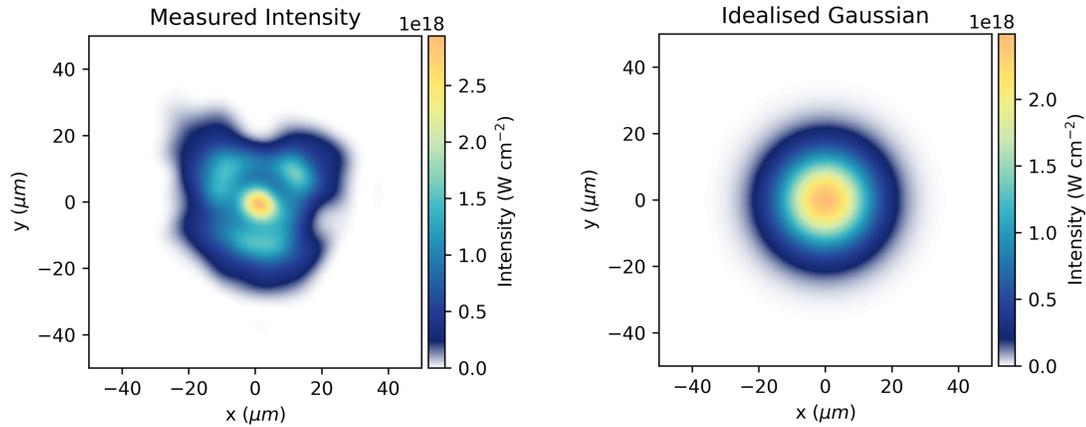


<https://github.com/LASY-org/LASY>

<https://lasydoc.readthedocs.io/en/latest/>

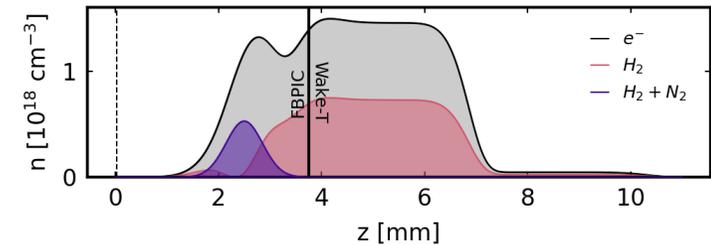
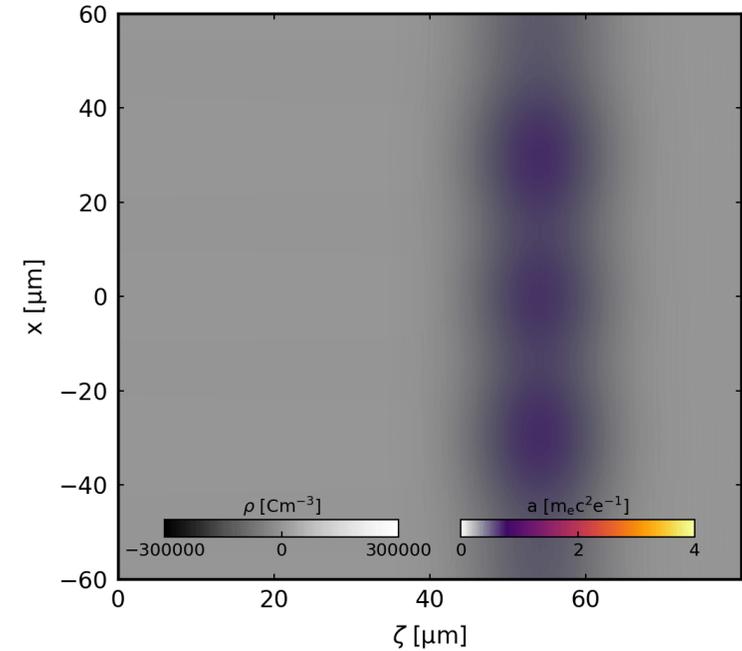
# LASY: LAsEr manipulations made eaSY

## From experiment to simulation



Come see poster #381 (yesterday)

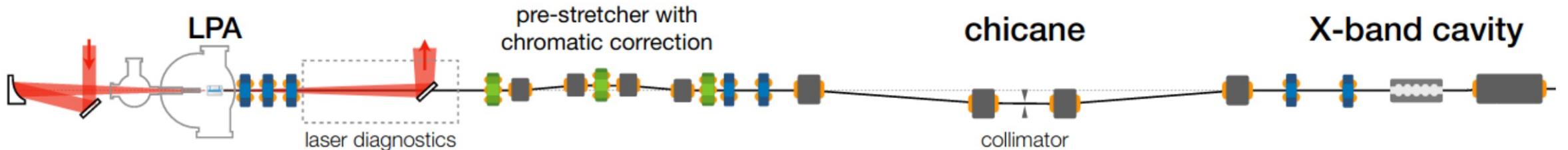
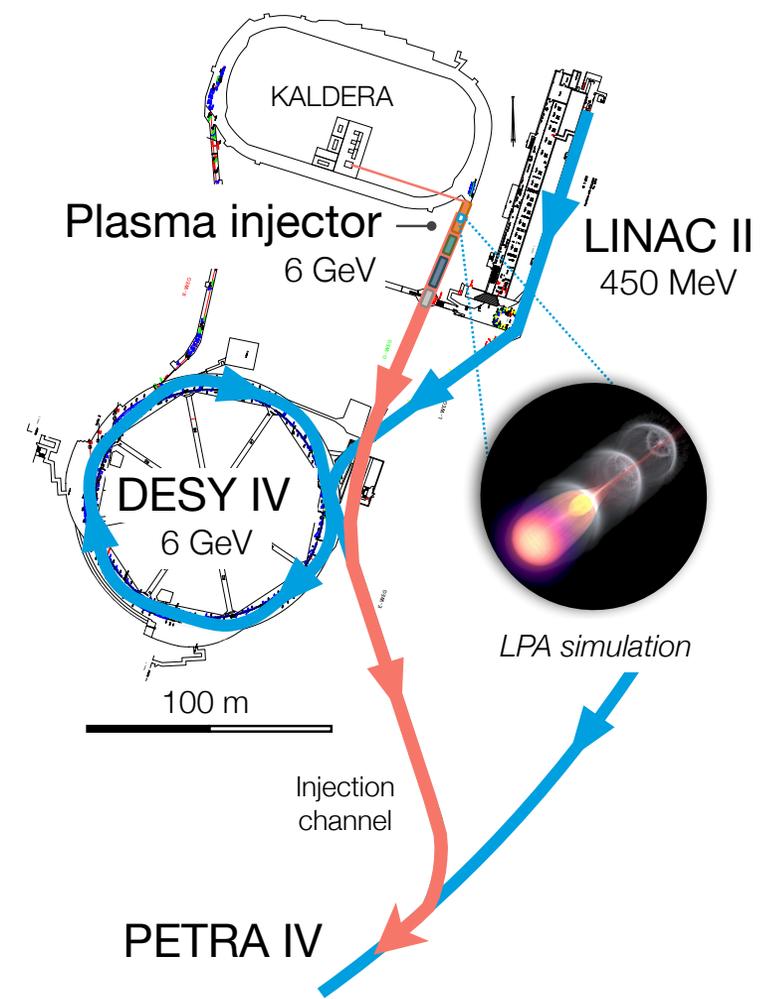
## From simulation to simulation



# A plasma injector for PETRA IV (PIP4)

## The team

I. Agapov, S. Antipov, R. Brinkmann, A. Ferran Pousa, S. J alas, L. Jeppe, M. Kirchen, W. P. Leemans, A. R. Maier, A. Martinez de la Ossa, J. Osterhoff, R. Shaloo, M. Thévenet, P. Winkler



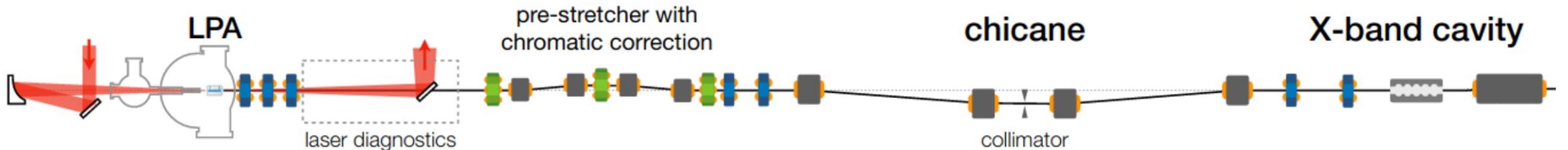
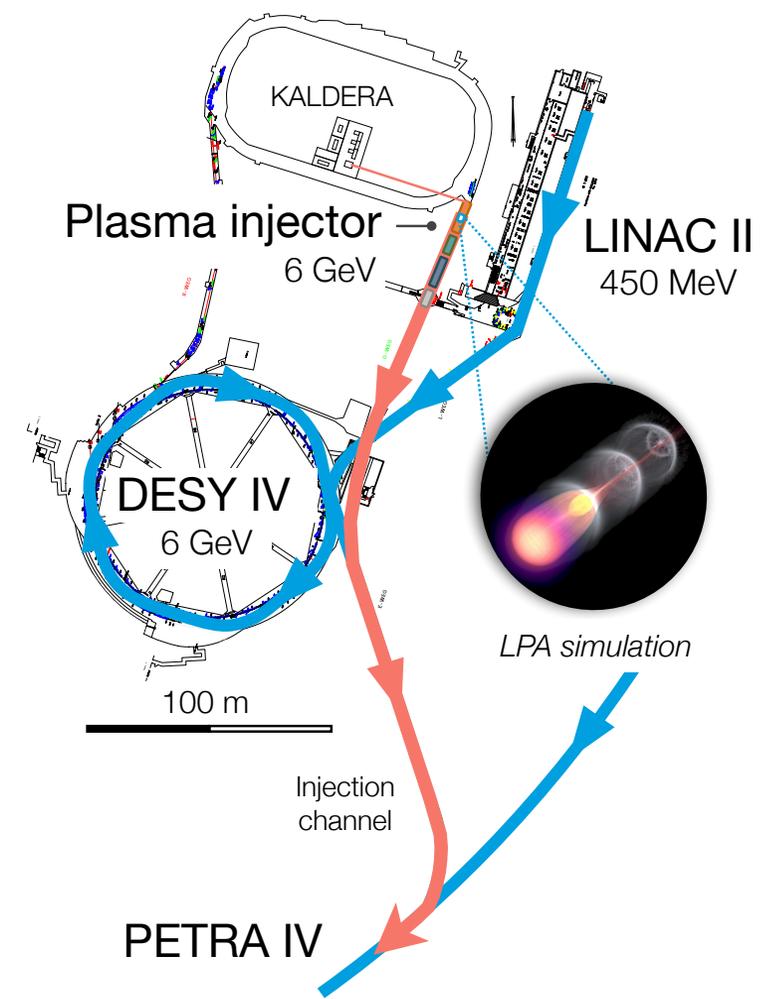
- [1] [https://www.desy.de/research/facilities\\_projects/petra\\_iv](https://www.desy.de/research/facilities_projects/petra_iv)
- [2] M. Kirchen et al. PRL 126.17 (2021); LUX PI: A. R. Maier
- [3] S. Antipov et al., 24, PRAB 111301 (2021)
- [4] A. Ferran Pousa et al. PRL 129, 094801 (2021)

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Come see poster #169 (today)



[1] [https://www.desy.de/research/facilities\\_projects/petra\\_iv](https://www.desy.de/research/facilities_projects/petra_iv)  
[2] M. Kirchen et al. *PRL* 126.17 (2021); LUX PI: A. R. Maier  
[3] S. Antipov et al., 24, *PRAB* 111301 (2021)  
[4] A. Ferran Pousa et al. *PRL* 129, 094801 (2021)

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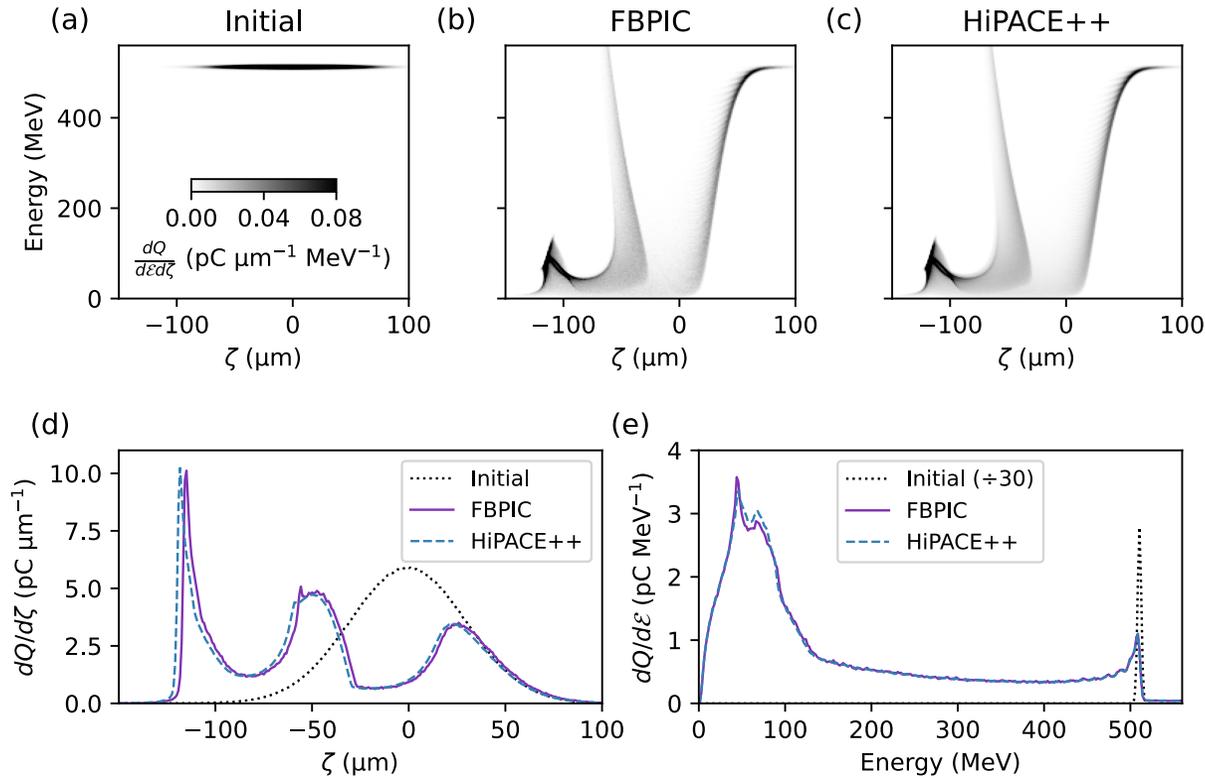


Carlo Benedetti, Axel Huebl, Rémi Lehe, Andrew Myers, Weiqun Zhang, Jean-Luc Vay

Thank you for your attention



# QS PIC even captures depletion



```
amr.n_cell = 4095 4095 3072
```

```
my_constants.Lramp = 0.025
my_constants.Lplateau = .3
my_constants.n0 = 3.7e22
```

```
max_step = 15000
hipace.max_time = (0.2+Lramp)/clight
diagnostic.output_period = 200
```

```
hipace.depos_order_xy = 2
hipace.dt = adaptive
hipace.nt_per_betatron = 10
hipace.dt_max = 1.e-13
```

```
geometry.coord_sys = 0 # 0: Cartesian
geometry.is_periodic = true true false # Is periodic?
geometry.prob_lo = -350.e-6 -350.e-6 -250.e-6 # physical domain
geometry.prob_hi = 350.e-6 350.e-6 110.e-6
```

```
beams.names = beam
```

```
beam.position_mean = 0. 0. 0.
beam.position_std = 15.e-6 15.e-6 30.e-6
beam.injection_type = fixed_weight
beam.num_particles = 10000000
beam.total_charge = 443.e-12
beam.u_mean = 0. 0. 1000.
beam.u_std = .7 .7 4.
```

```
plasmas.names = plasma
plasma.density(x,y,z) = "if(z>0, if(z<Lramp,n0*0.5*(1.-cos(pi*z/Lramp)),n0), 1.e-20)"
plasma.ppc = 1 1
plasma.element = electron
```

```
diagnostic.diag_type = xz
```

Figure 1: Longitudinal phase-space of the initial beam (a) and final beam from simulations using HiPACE++ (b) and FBPIC (c) along the co-moving variable  $\zeta = s - ct$ , with  $s$  being the longitudinal coordinate,  $t$  the time, and  $c$  the speed of light in vacuum. The longitudinal charge distribution (d) and the energy spectrum (e) show good agreement between the different PIC codes.

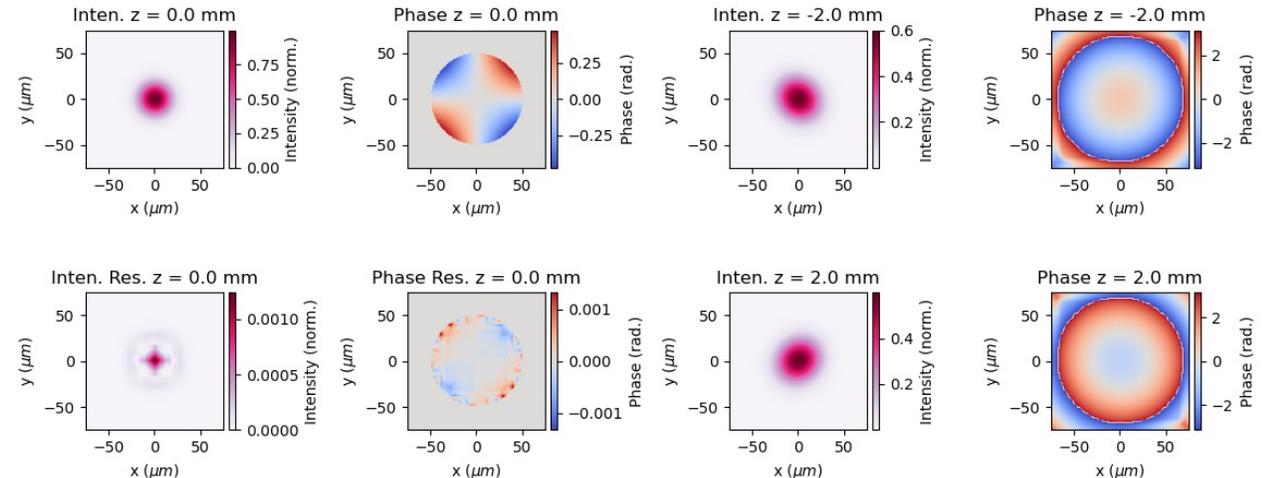
# LASY: LAsEr manipulation made eaSY

- Realistic/measured laser profiles are critical
- Workflow can be cumbersome, with efforts duplication
- LASY aims at making this easy
- Contributors from DESY, LBNL, LOA, CEA, and more

```
from lasy.laser import Laser
from lasy.profiles.gaussian_profile import GaussianProfile

profile = GaussianProfile(wavelength, pol, energy, w0, tau, t_peak)
laser = Laser(dim, lo, hi, npoints, gaussian)
laser.propagate(-100.e-6)
laser.write_to_file('laser_file')
```

- Written in Python
- Envelope model
- Support RZ (azimuthal modes) & XYZ
- Measured or analytic profiles
- Read/write openPMD standard, envelope or field
- Propagator powered by Axiprop (I. Andriyash)
- Utils (Gerchberg-Saxton algorithm, etc.)



[2] L. T. Dickson et al., Phys. Rev. Accel. Beams 25, 101301 (2022)

<https://github.com/LASY-org/LASY>  
<https://lasydoc.readthedocs.io/en/latest/>

Plasma acceleration is described by kinetic plasma dynamics

Plasma acceleration is described by kinetic plasma dynamics

# Plasma acceleration is described by kinetic plasma dynamics

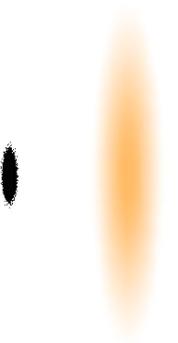
$$\frac{\partial \mathbf{B}}{\partial t} = -\nabla \times \mathbf{E},$$

$$\frac{\partial \mathbf{E}}{\partial t} = \nabla \times \mathbf{B} - \mathbf{J},$$

$$\frac{d\mathbf{x}}{dt} = \mathbf{v},$$

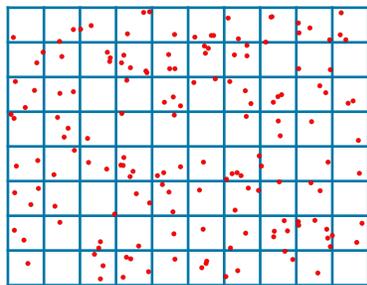
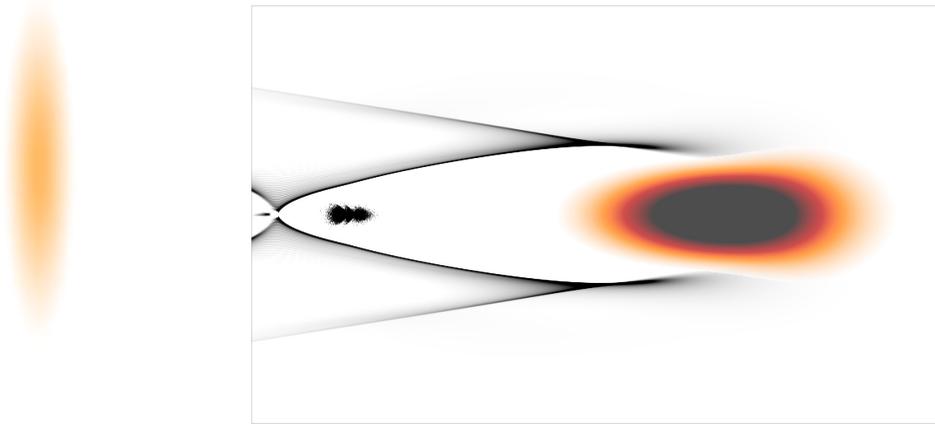
$$\frac{d(\gamma \mathbf{v})}{dt} = \frac{q}{m}(\mathbf{E} + \mathbf{v} \times \mathbf{B}),$$

# Plasma acceleration is described by kinetic plasma dynamics

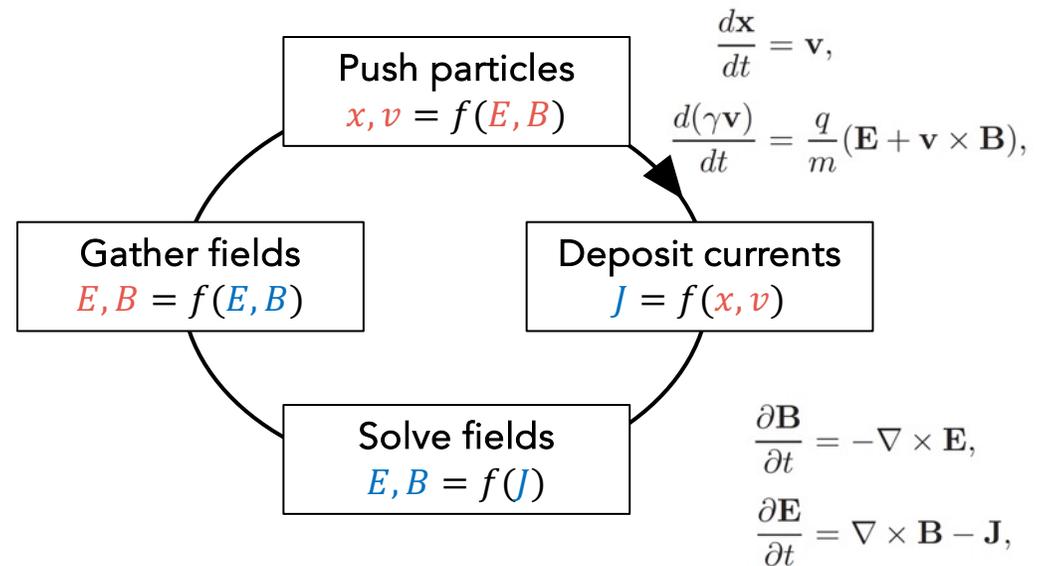

$$\frac{d\mathbf{x}}{dt} = \mathbf{v},$$
$$\frac{d(\gamma\mathbf{v})}{dt} = \frac{q}{m}(\mathbf{E} + \mathbf{v} \times \mathbf{B}),$$

$$\frac{\partial \mathbf{B}}{\partial t} = -\nabla \times \mathbf{E},$$
$$\frac{\partial \mathbf{E}}{\partial t} = \nabla \times \mathbf{B} - \mathbf{J},$$

# Plasma acceleration is described by kinetic plasma dynamics



Regular mesh  
Macroparticles



- *Lagrangian* description of plasma, *Eulerian* description of fields
  - Physics can be added
  - Time step limited by CFL condition:  $\Delta t \simeq \frac{\Delta z}{c}$
- 3D (EM) PIC simulations of plasma acceleration are very expensive

# Recent advances improved accuracy of the field solver

$$\nabla_{\perp}^2 \psi = -\frac{1}{\epsilon_0} \left( \rho - \frac{1}{c} j_z \right)$$

$$E_x - c B_y = -\partial_x \psi$$

$$E_y + c B_x = -\partial_y \psi$$

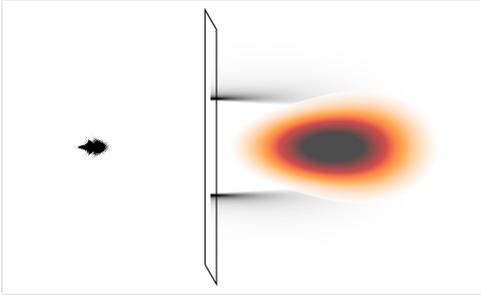
$$\nabla_{\perp}^2 E_z = c \mu_0 (\partial_x j_x + \partial_y j_y)$$

$$\nabla_{\perp}^2 B_x = \mu_0 (-\partial_y j_z + \partial_z j_y)$$

$$\nabla_{\perp}^2 B_y = \mu_0 (\partial_x j_z - \partial_z j_x)$$

$$\nabla_{\perp}^2 B_z = \mu_0 (\partial_y j_x - \partial_x j_y)$$

# Recent advances improved accuracy of the field solver



Source terms  $\partial_\zeta j_{x/y}$  are difficult to obtain

$$\nabla_\perp^2 \psi = -\frac{1}{\epsilon_0} \left( \rho - \frac{1}{c} j_z \right)$$

$$E_x - c B_y = -\partial_x \psi$$

$$E_y + c B_x = -\partial_y \psi$$

$$\nabla_\perp^2 E_z = c \mu_0 (\partial_x j_x + \partial_y j_y)$$

$$\nabla_\perp^2 B_x = \mu_0 (-\partial_y j_z + \partial_\zeta j_y)$$

$$\nabla_\perp^2 B_y = \mu_0 (\partial_x j_z - \partial_\zeta j_x)$$

$$\nabla_\perp^2 B_z = \mu_0 (\partial_y j_x - \partial_x j_y)$$

➤ **predictor-corrector solver: *the old one***

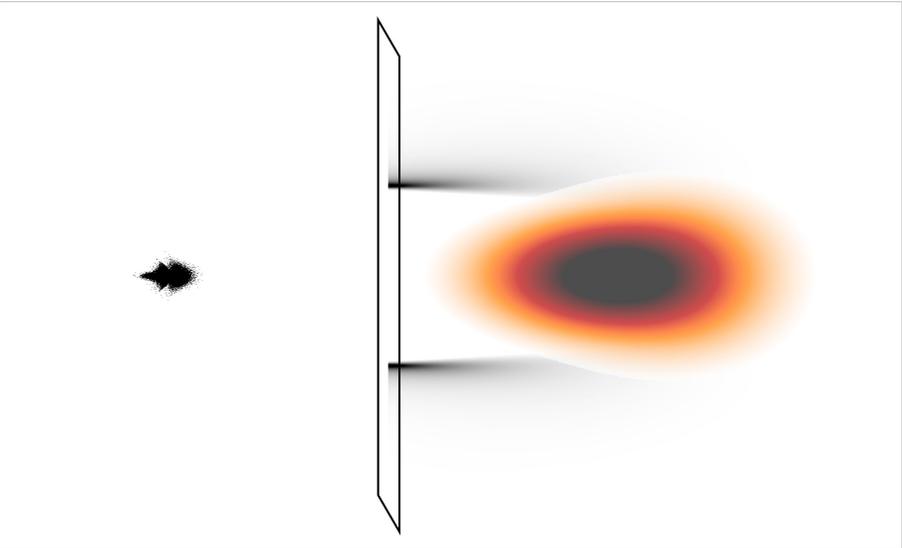
- [Mora & T. Antonsen, Phys. Plasmas (1997), W. An et al., JCP (2013)]
- Not very stable

➤ **explicit solver: *the new one***

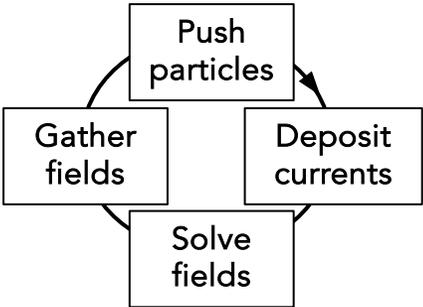
- [T. Wang et al., Phys. Plasmas (2017), P. Baxevanis & G. Stupakov, PRAB (2018), T. Wang, et al. PRAB 25.10 (2022)]
- Analytic integration of the source term
- Gives a screened Poisson equation, solved with multigrid solver

$$\nabla_\perp^2 B_\perp - \frac{n^*}{1 + \psi} B_\perp = -[e_z \times S]$$

# Mesh Refinement in HiPACE++

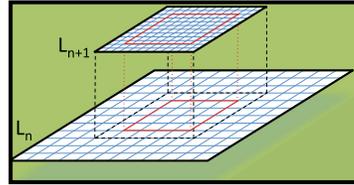


- Deposit beam and plasma densities  $\rho, \vec{J}$
- Solve Poisson fields  $(E_x - cB_y, E_y + cB_x, E_z \cdot B_z)$
- Deposit beam and plasma source terms  $S_x, S_y$
- Explicit solve  $(B_x, B_y)$
- Advance plasma particles by 1 slice  $(-\Delta\zeta)$
- Advance beam particles by 1 time step  $(+\Delta t)$

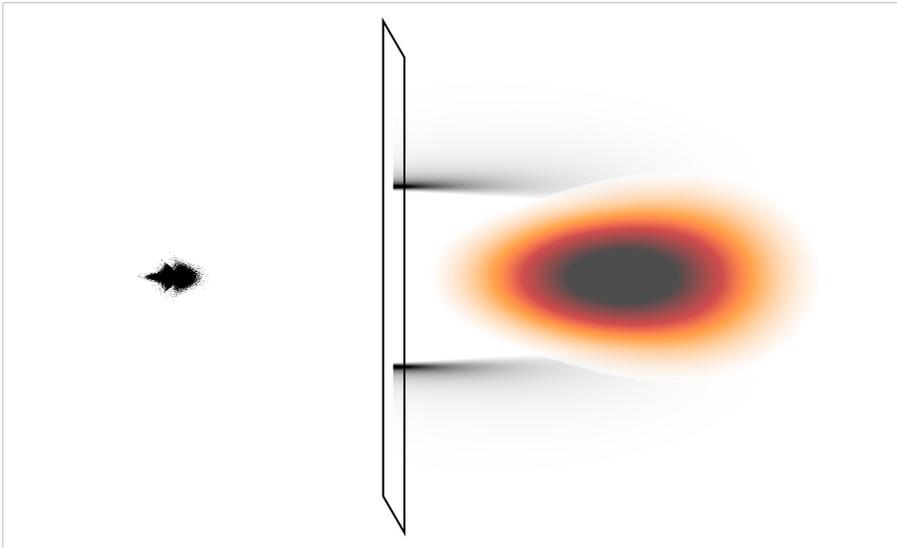


# Mesh Refinement in HiPACE++

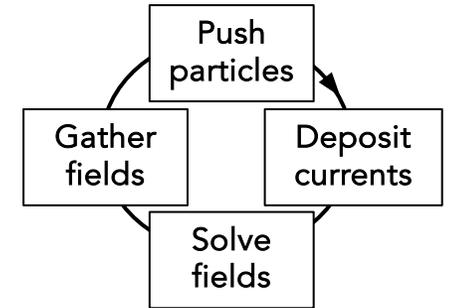
➤ MR in electrostatic PIC



J.-L. Vay et al., Comput. Sci. & Disc. 5, 014019 (2012)

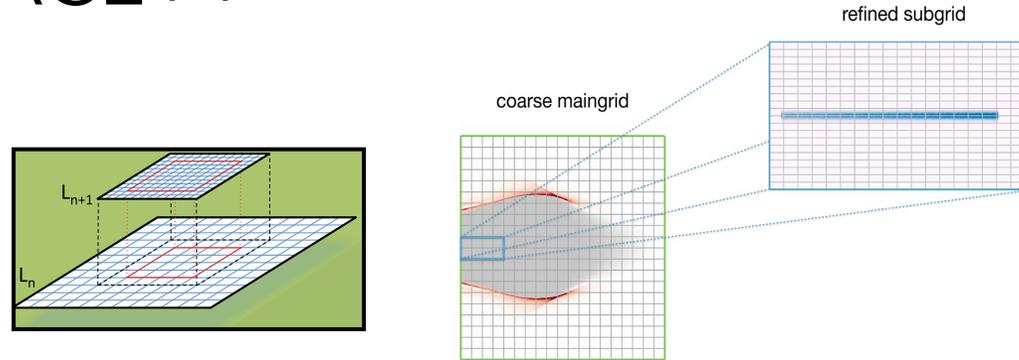


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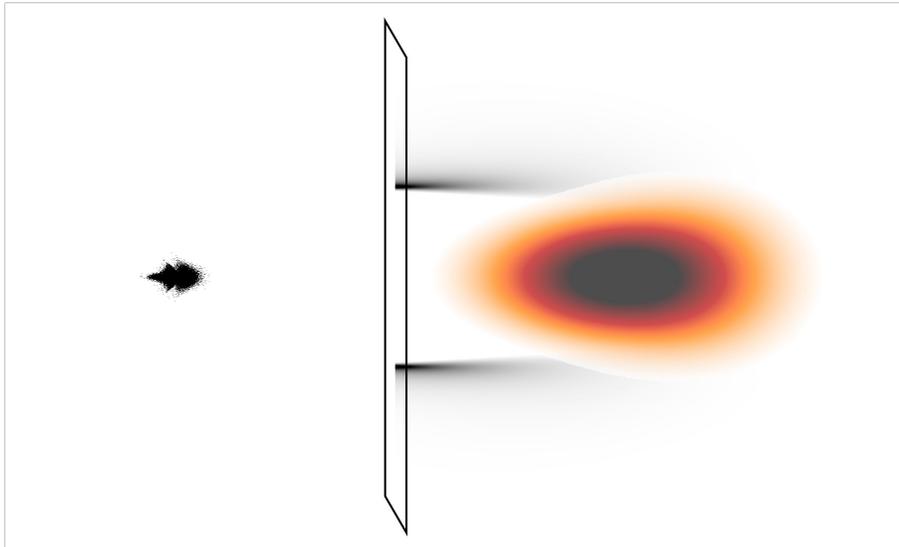
# Mesh Refinement in HiPACE++

- MR in electrostatic PIC
- MR with quasi-static PIC, no crossing

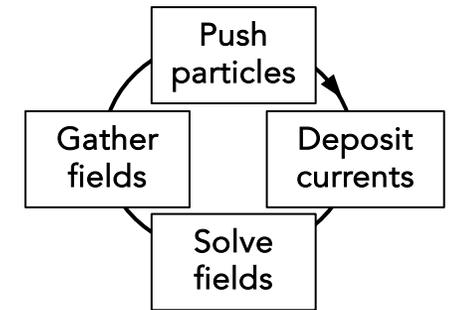


J.-L. Vay et al., Comput. Sci. & Disc. 5, 014019 (2012)

T. J. Mehrling et al., IEEE, AAC (2018)

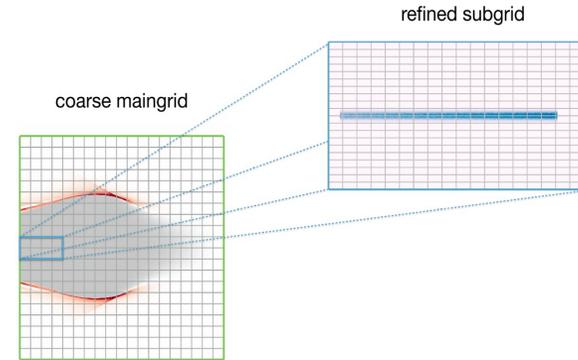
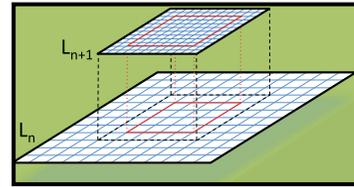


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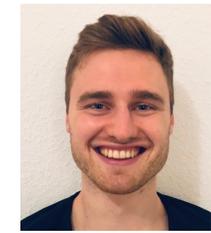
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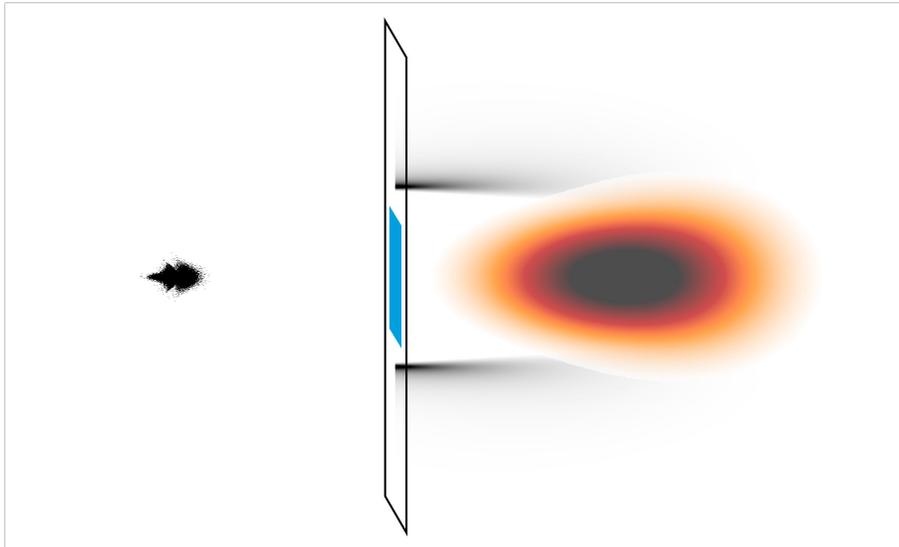
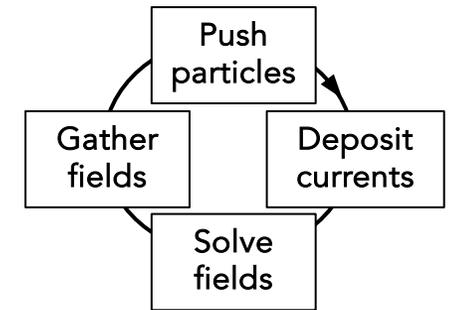
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Severin  
Diederichs

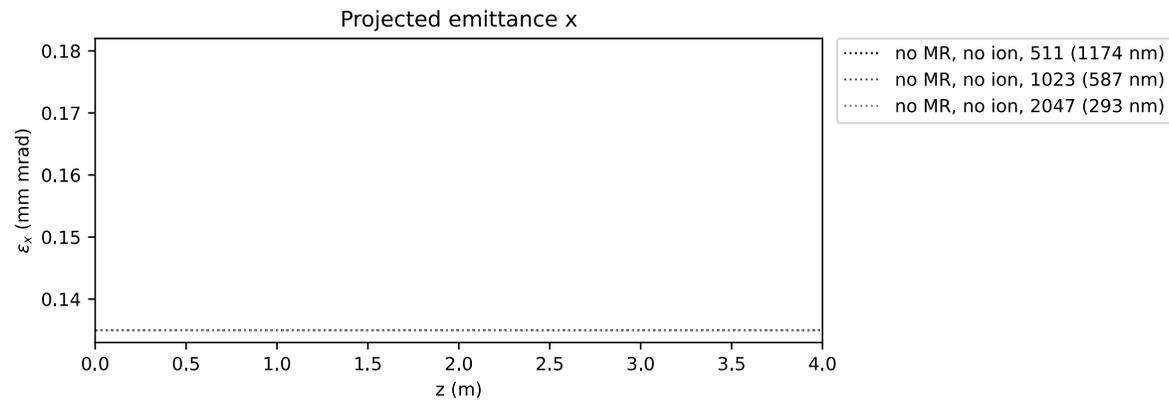
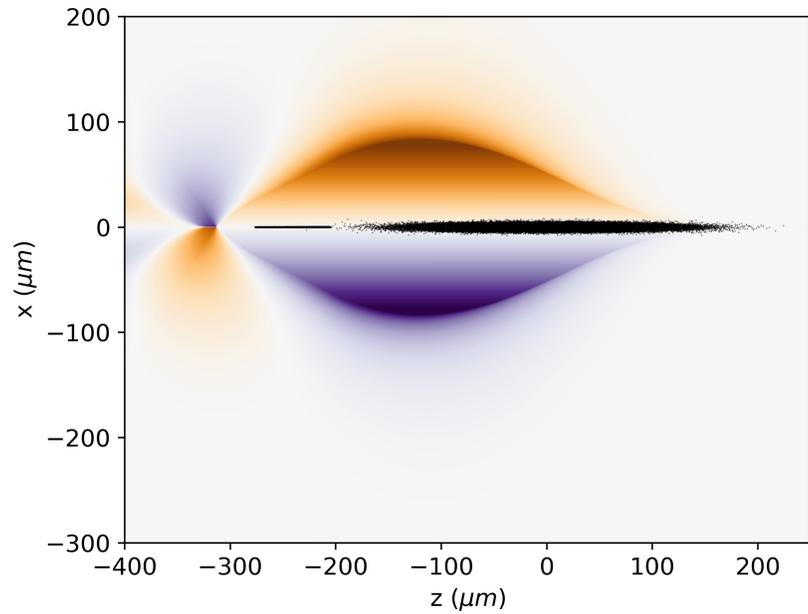


Alexander  
Sinn

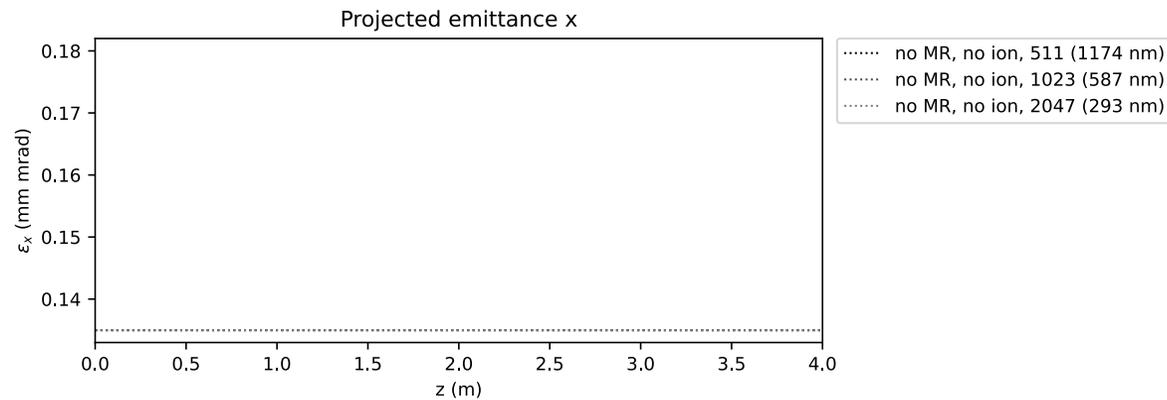
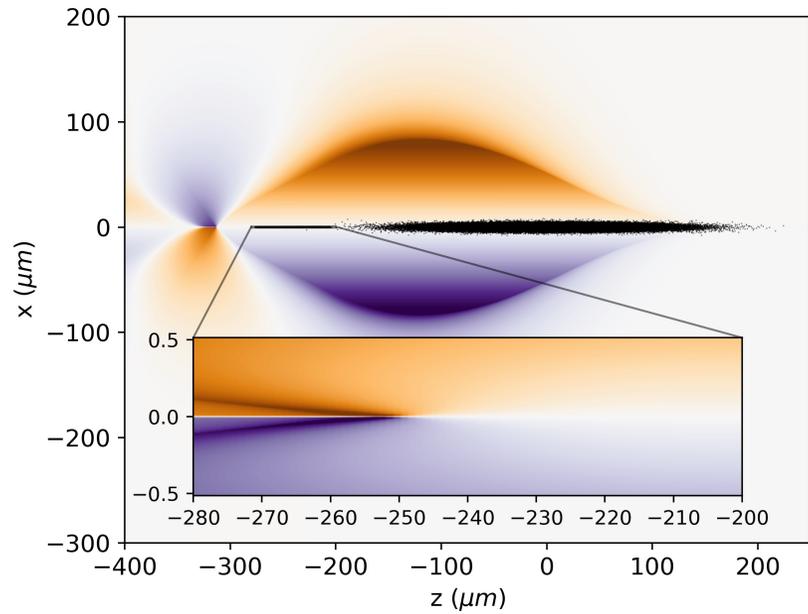


- Deposit beam and plasma densities  $\rho, \vec{j}$   
on all levels
- Solve Poisson fields ( $E_x - cB_y, E_y + cB_x, E_z \cdot B_z$ )  
BC on fine patch, solve, Interpolate in ghost cells
- Tag by level
- Deposit beam and plasma source terms  $S_x, S_y$   
on all levels
- Explicit solve ( $B_x, B_y$ )  
BC of source and B, solve
- Advance plasma particles by 1 slice ( $-\Delta\zeta$ )
- Advance beam particles by 1 time step ( $+\Delta t$ )

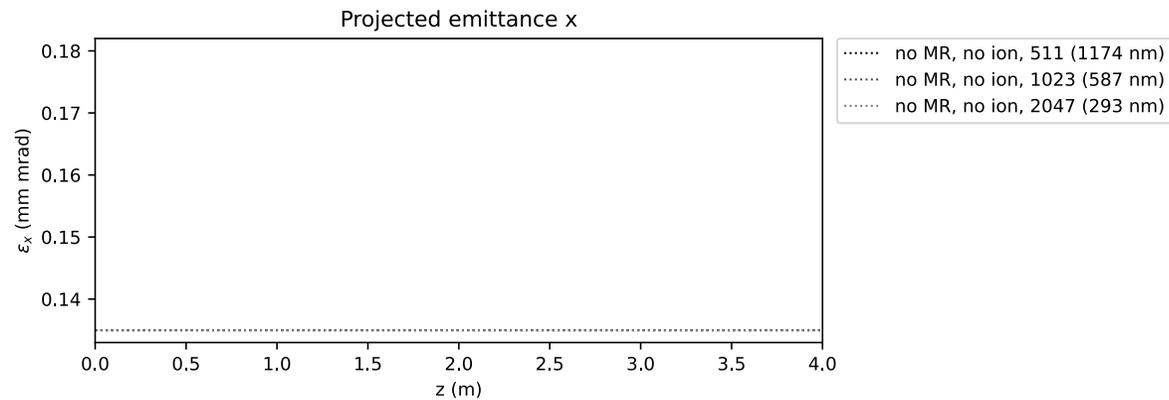
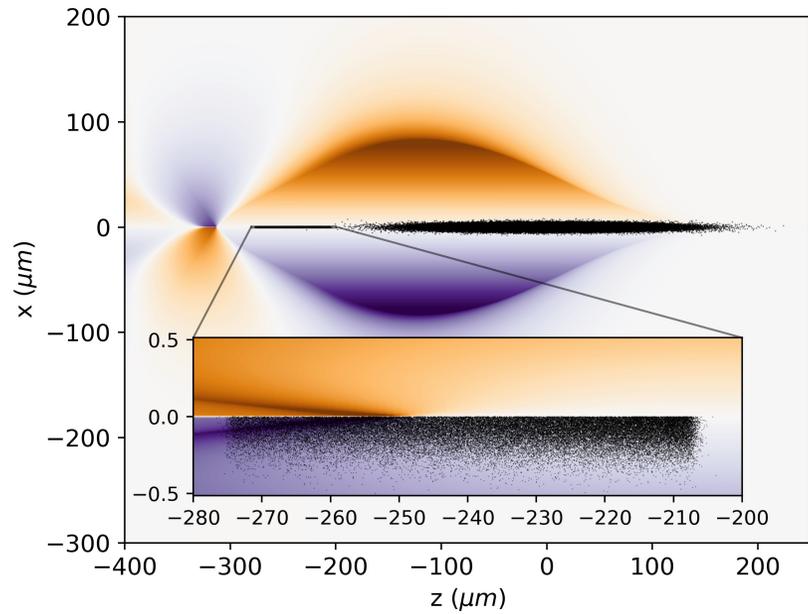
# Converged simulations in collider-relevant range are ~~feasible~~ cheap



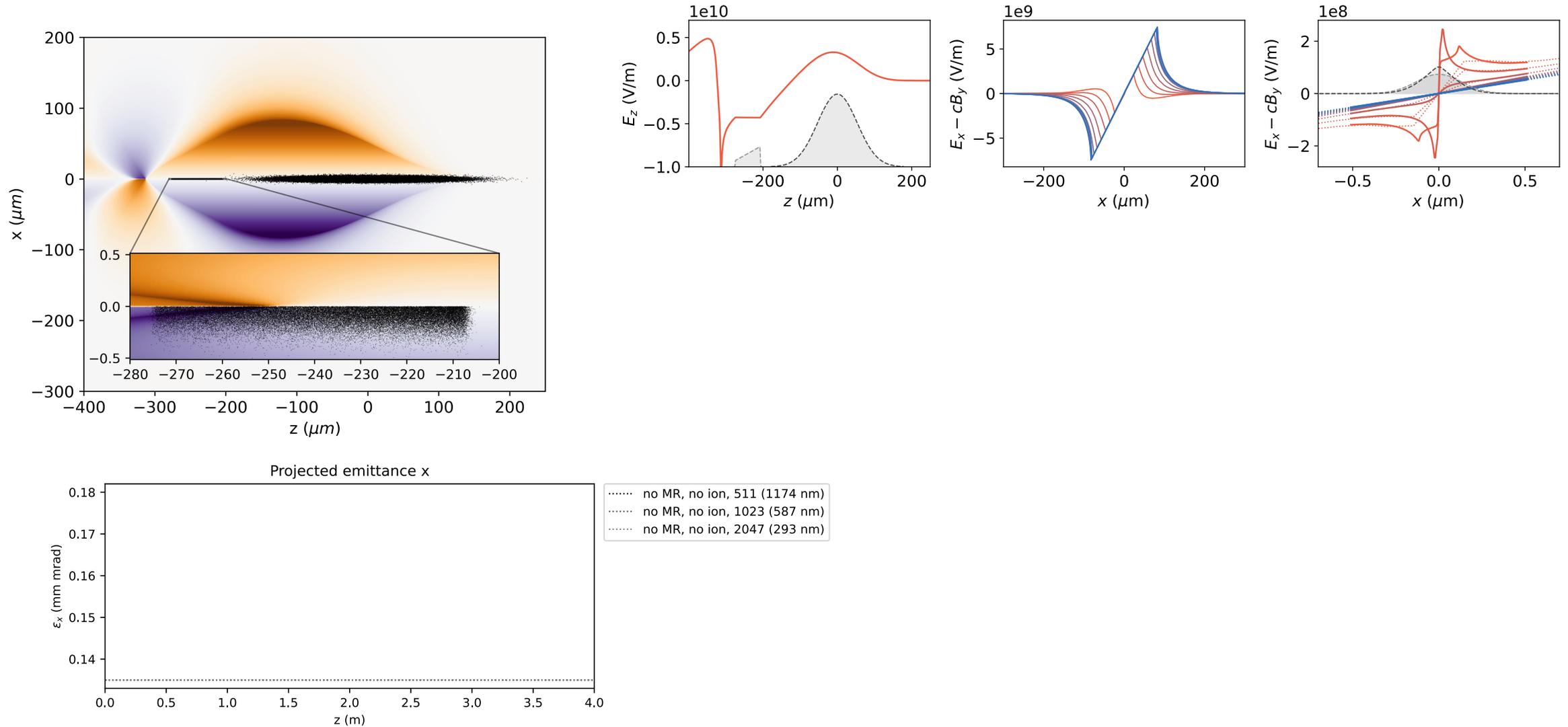
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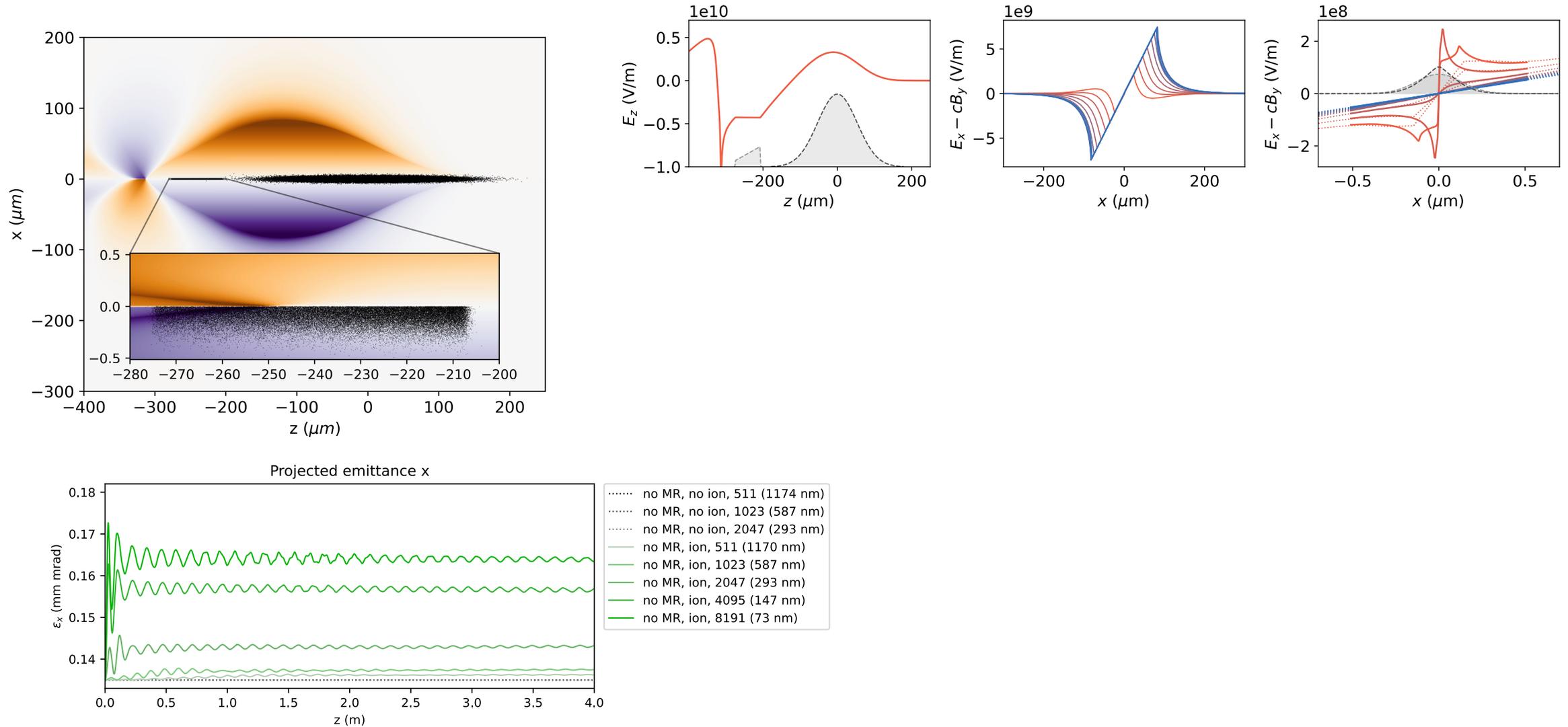
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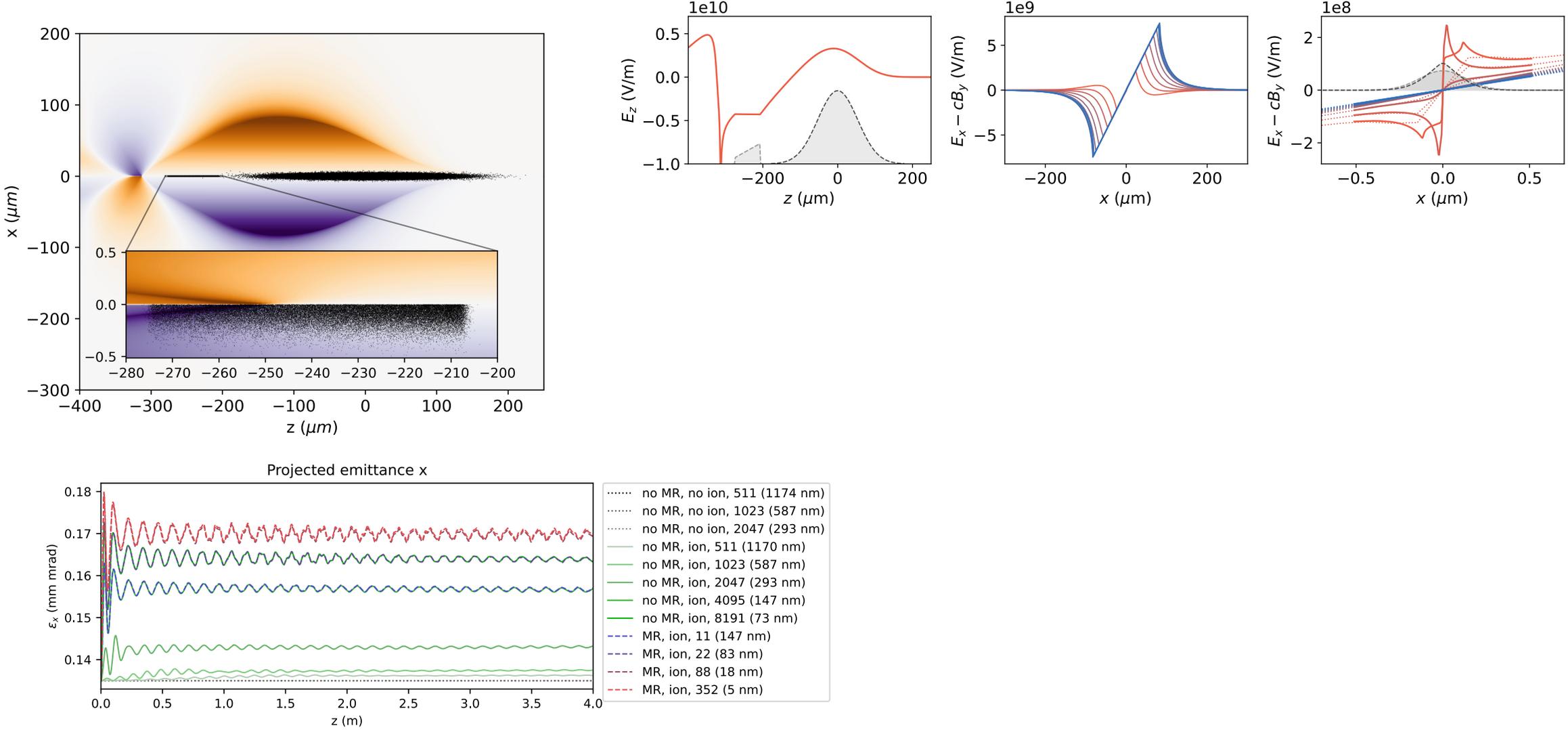
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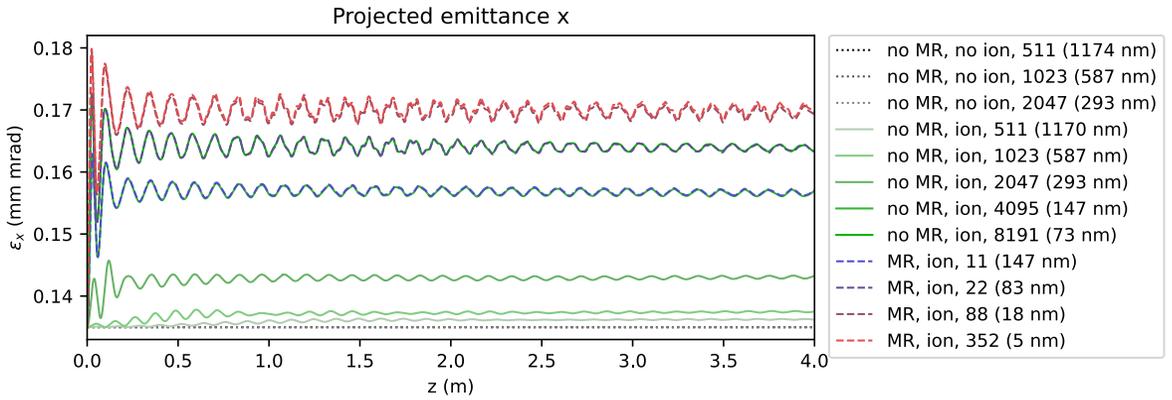
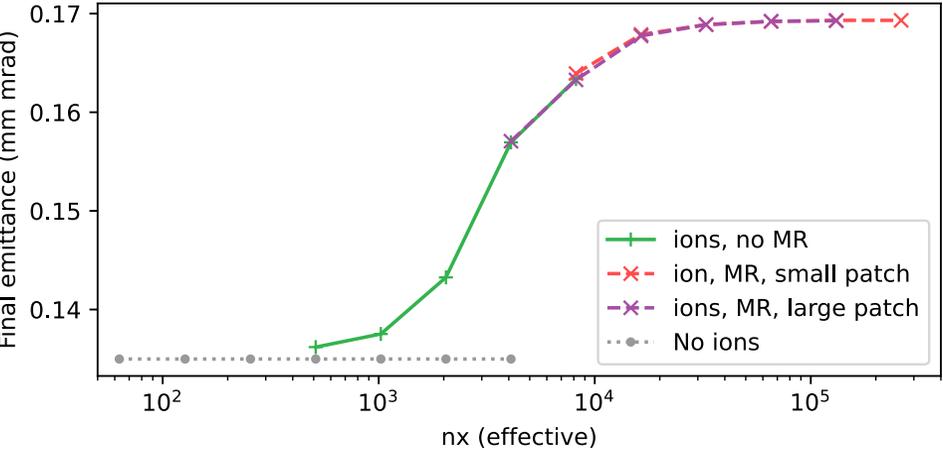
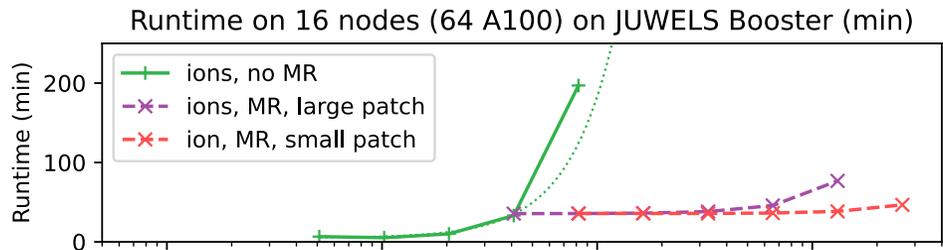
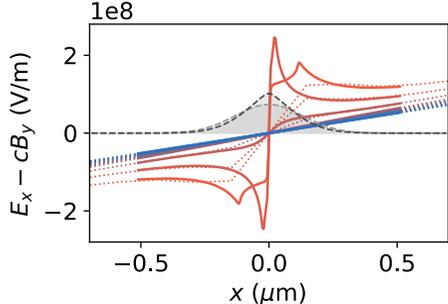
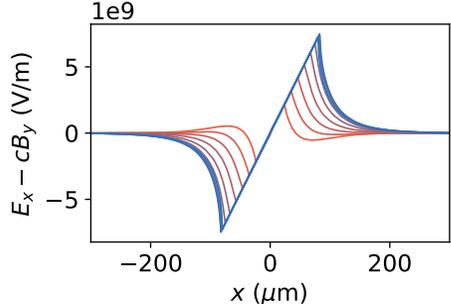
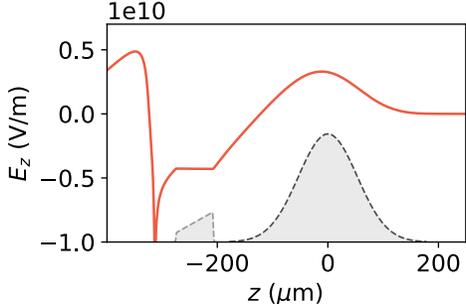
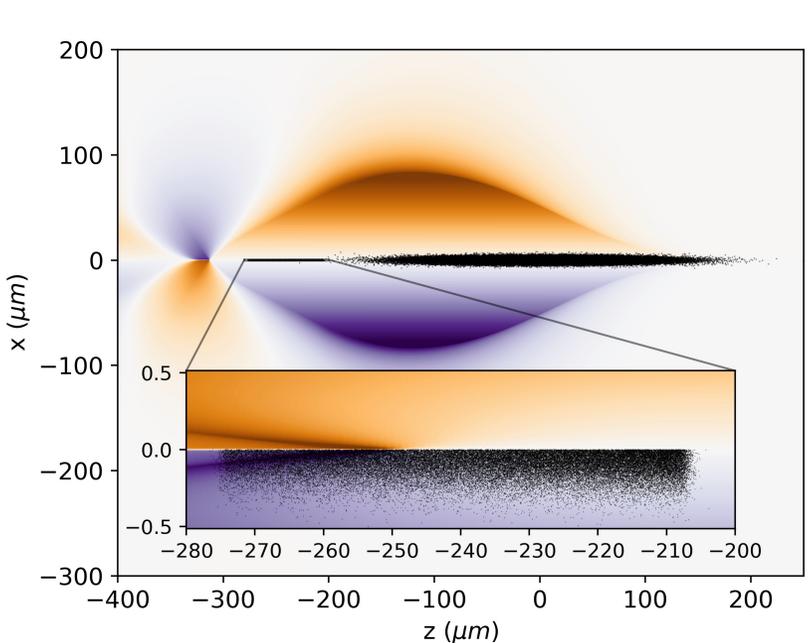
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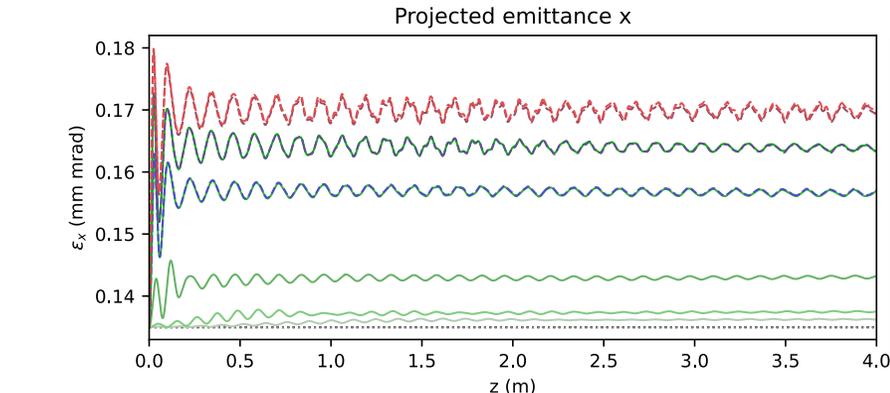
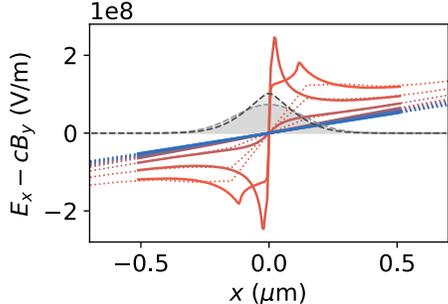
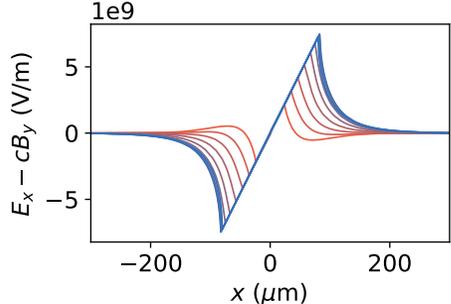
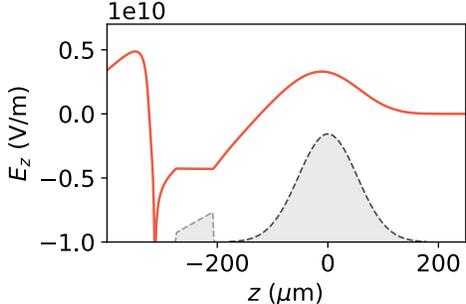
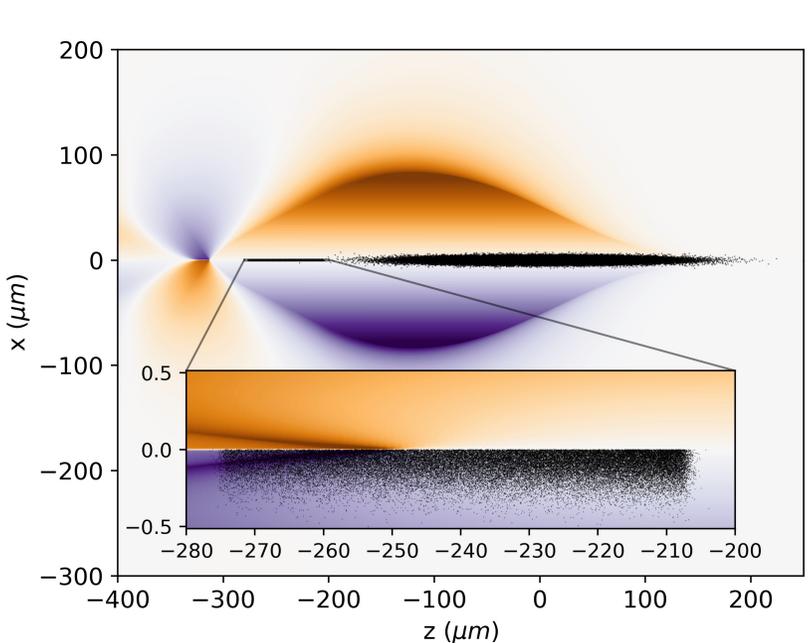
# Converged simulations in collider-relevant range are ~~feasible~~ cheap



# Converged simulations in collider-relevant range are ~~feasible~~ cheap

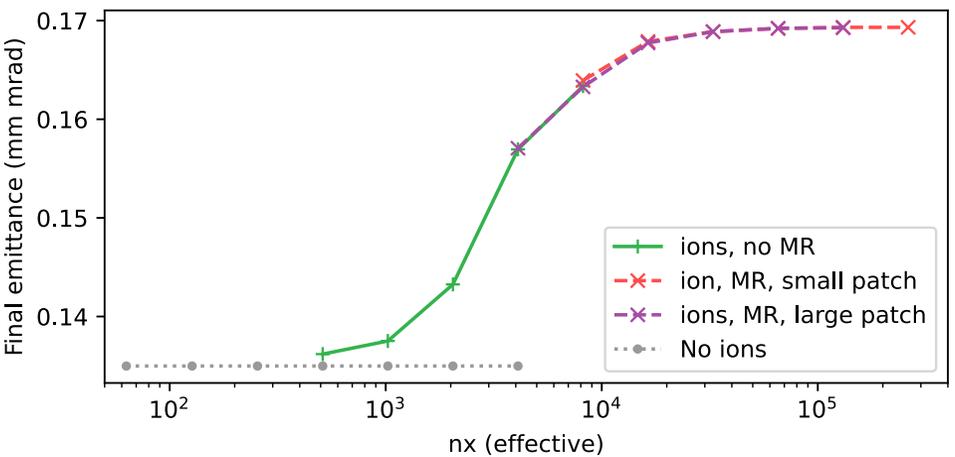
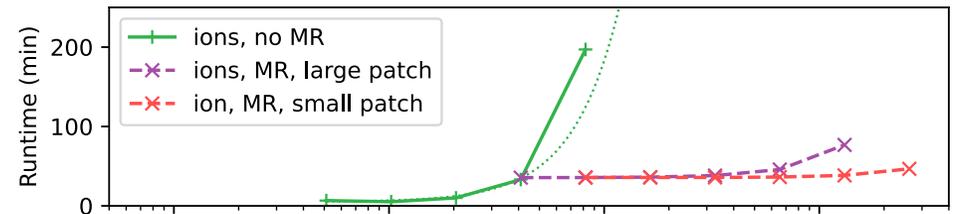


# Converged simulations in collider-relevant range are ~~feasible~~ cheap



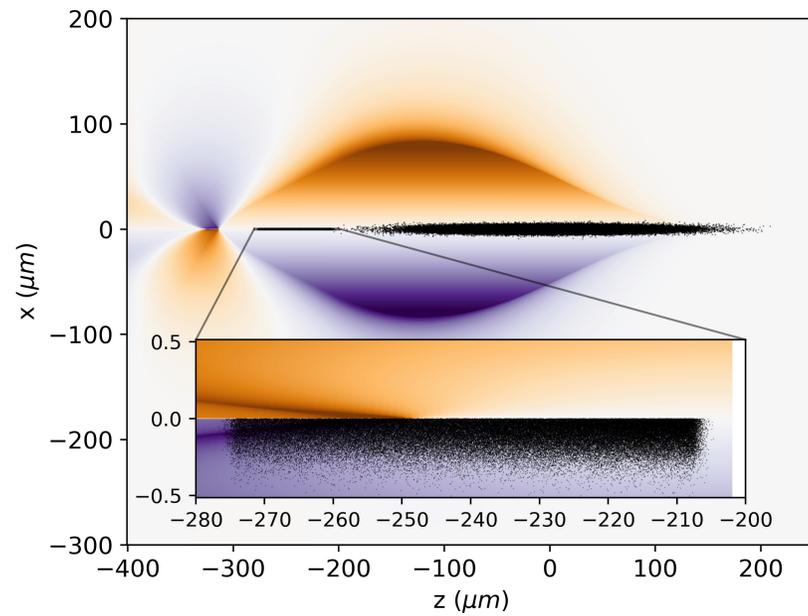
- ..... no MR, no ion, 511 (1174 nm)
- ..... no MR, no ion, 1023 (587 nm)
- ..... no MR, no ion, 2047 (293 nm)
- ..... no MR, ion, 511 (1170 nm)
- ..... no MR, ion, 1023 (587 nm)
- ..... no MR, ion, 2047 (293 nm)
- ..... no MR, ion, 4095 (147 nm)
- ..... no MR, ion, 8191 (73 nm)
- ..... MR, ion, 11 (147 nm)
- ..... MR, ion, 22 (83 nm)
- ..... MR, ion, 88 (18 nm)
- ..... MR, ion, 352 (5 nm)

Runtime on 16 nodes (64 A100) on JUWELS Booster (min)

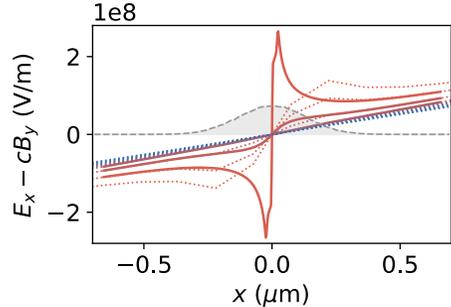
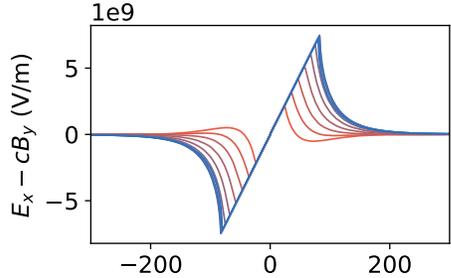
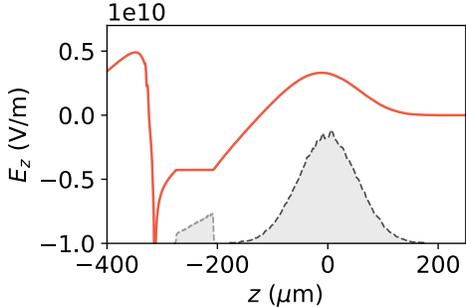
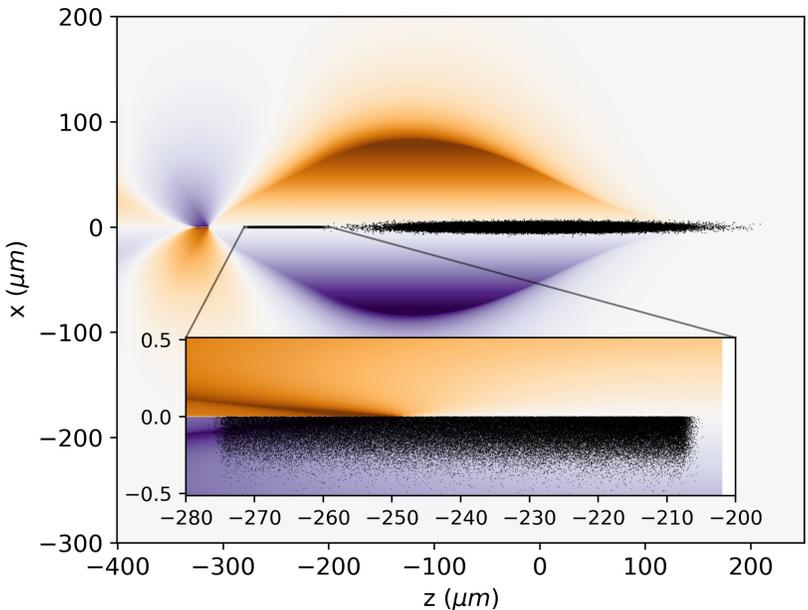


- Coarse resolution + MR = fine resolution everywhere
- MR allows for convergence at modest cost

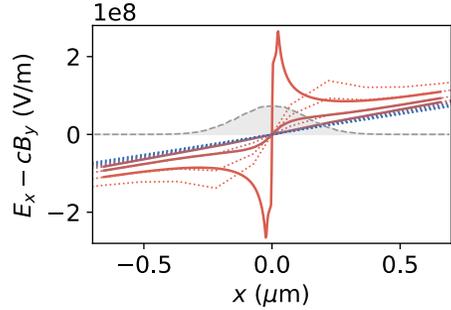
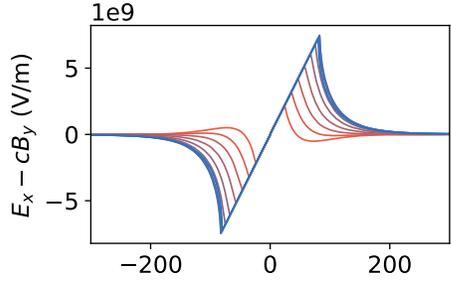
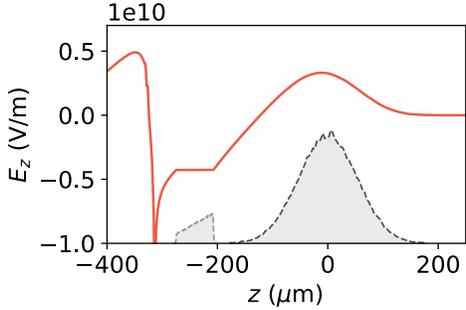
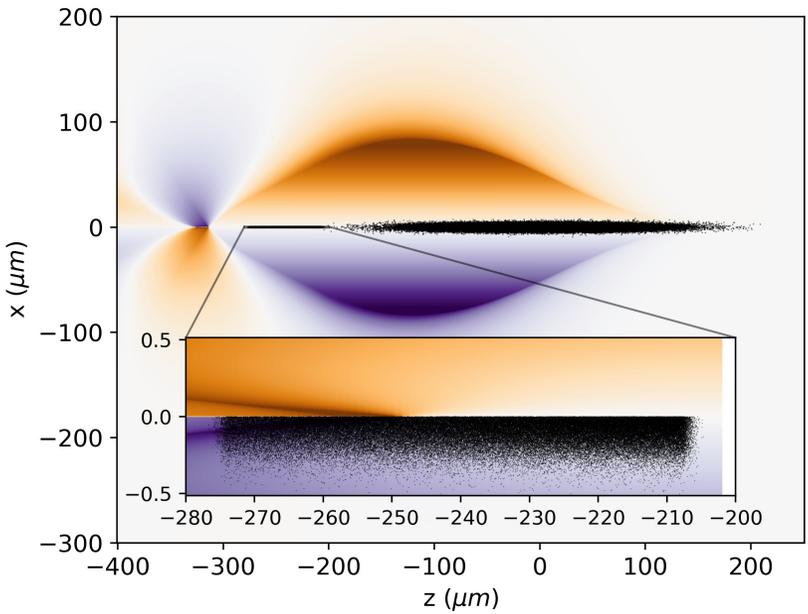
# Realistic simulations of collider parameters on a laptop w/ Wake-T



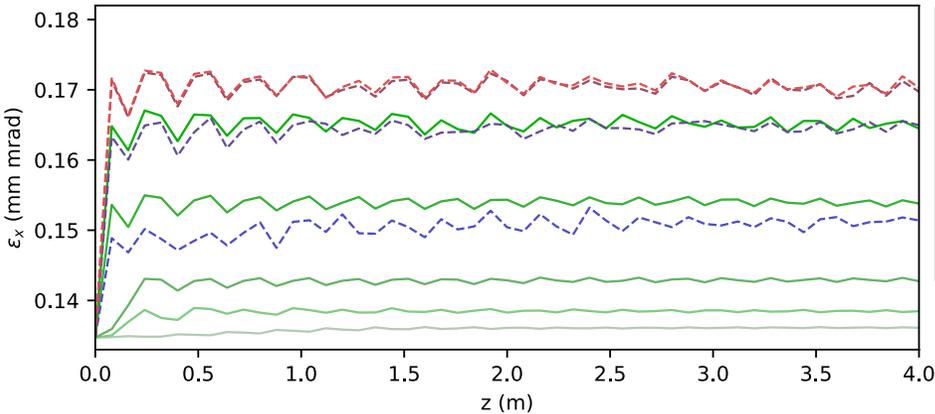
# Realistic simulations of collider parameters on a laptop w/ Wake-T



# Realistic simulations of collider parameters on a laptop w/ Wake-T

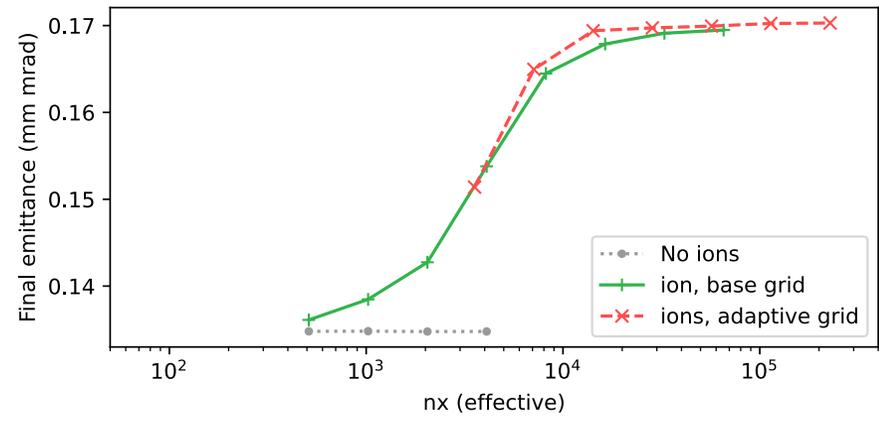
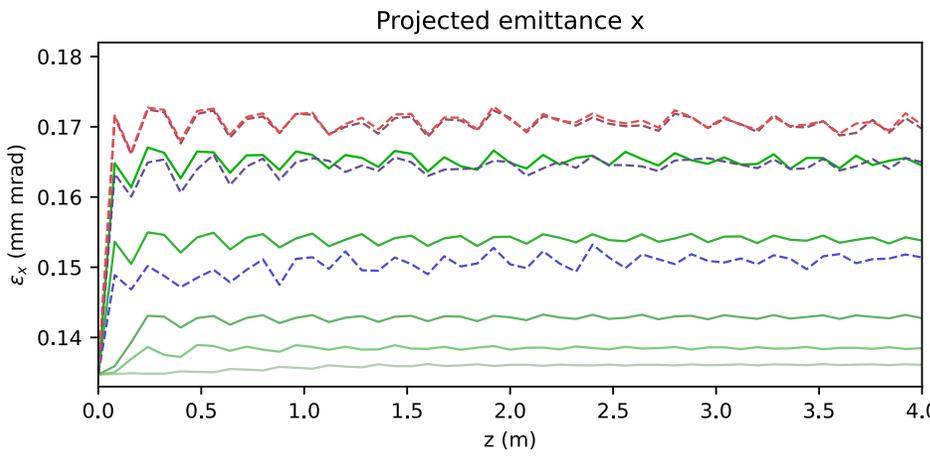
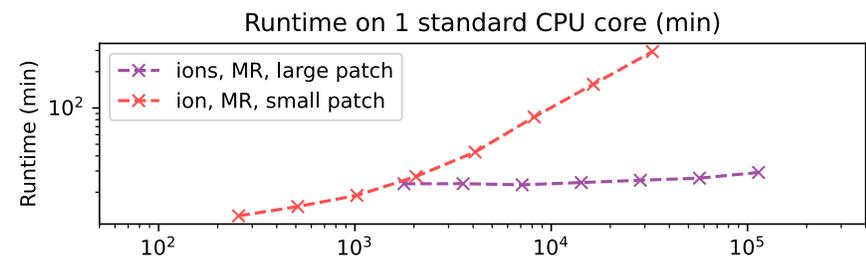
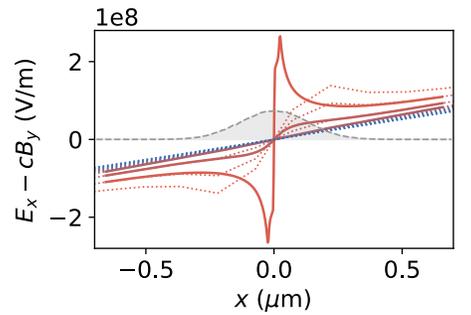
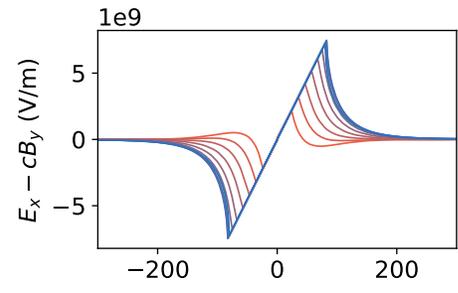
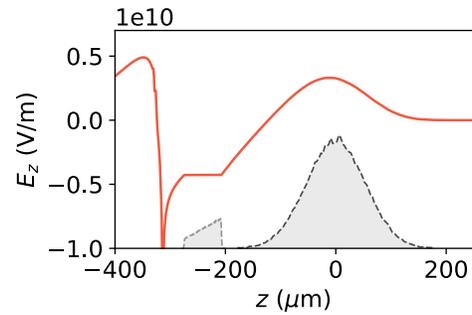
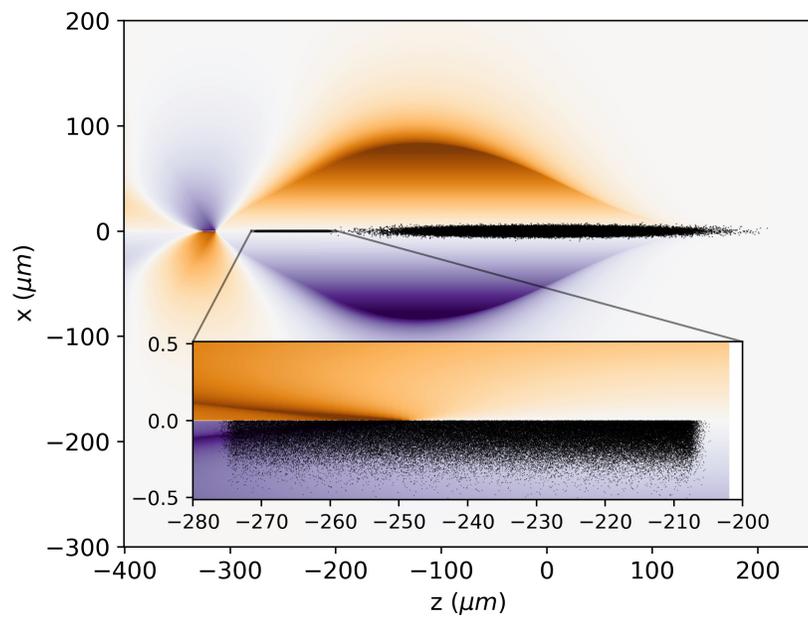


Projected emittance x

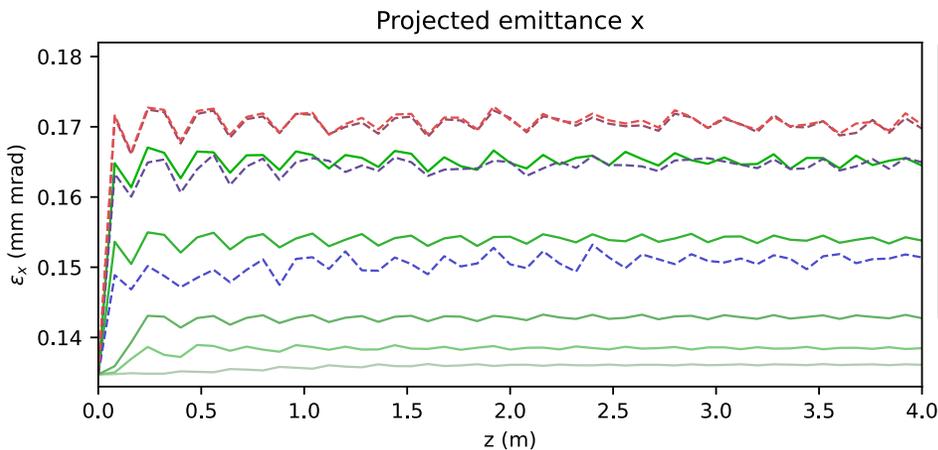
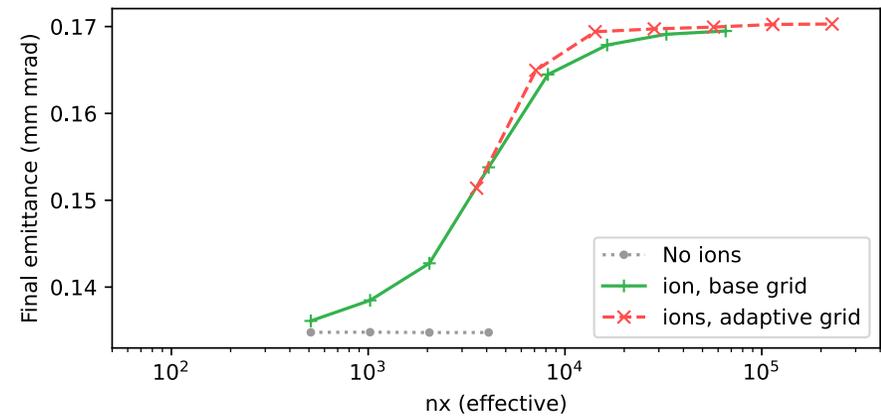
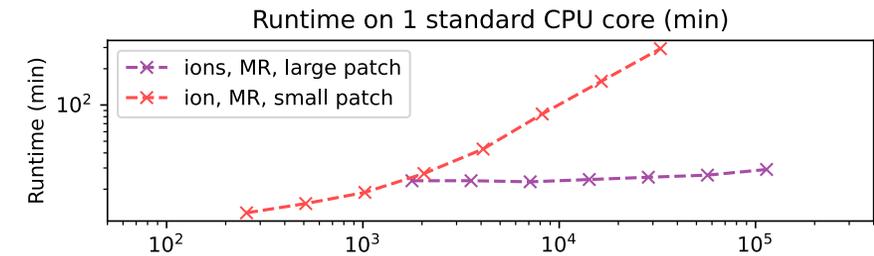
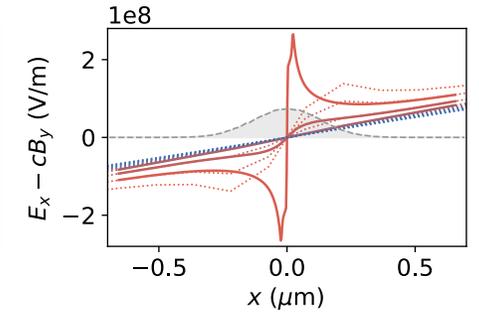
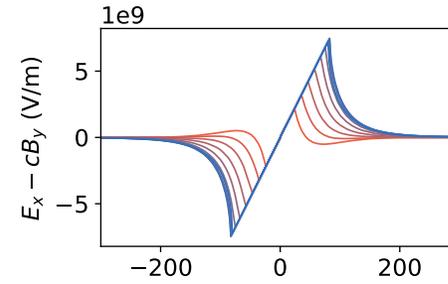
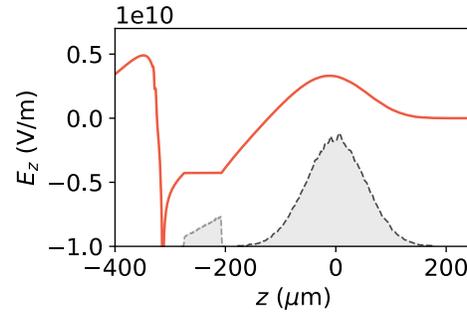
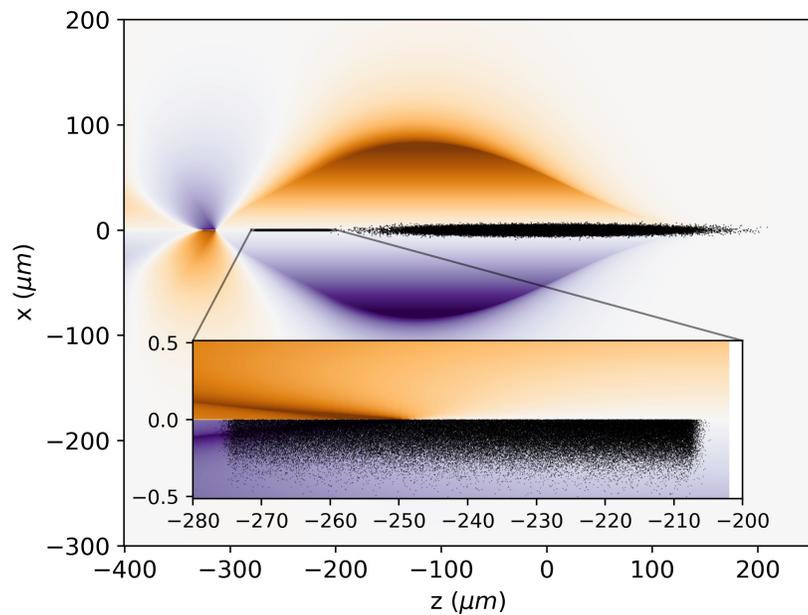


- base grid, nr=255
- base grid, nr=511
- base grid, nr=1023
- base grid, nr=2047
- base grid, nr=4095
- - - adaptive grid, nr\_eff=1778
- - - adaptive grid, nr\_eff=3556
- - - adaptive grid, nr\_eff=14225
- - - adaptive grid, nr\_eff=113807

# Realistic simulations of collider parameters on a laptop w/ Wake-T



# Realistic simulations of collider parameters on a laptop w/ Wake-T



- base grid, nr=255
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- base grid, nr=1023
- base grid, nr=2047
- base grid, nr=4095
- - - adaptive grid, nr\_eff=1778
- - - adaptive grid, nr\_eff=3556
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