

Coherence of confined matter in lattice gauge theories at the mesoscopic scale

Enrico C. Domanti, Paolo Castorina, Dario Zappalà, Luigi Amico

QuantHEP Conference, Bari, September 2023



Outline

➤ Motivation

- Introduction to one dimensional \mathbb{Z}_2 lattice gauge theory

➤ Results

- Implementation on a ring pierced by a synthetic magnetic flux
- Ground state current
- Single meson dynamics in the ring

➤ Conclusions

Motivation

High energy physics

- Gauge theories are at the basis of our understanding of fundamental interactions
- Lattice gauge theories as tools for studying high-energy phenomena:
 - Confinement, string breaking, etc.

Low energy physics

- High T_c superconductors
- Spin liquids
- Topology

Quantum simulation of LGTs

ARTICLES

<https://doi.org/10.1038/s41567-019-0649-7>

nature
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Floquet approach to \mathbb{Z}_2 lattice gauge theories with ultracold atoms in optical lattices

Christian Schweizer^{1,2,3}, Fabian Grusdt^{3,4}, Moritz Berngruber^{1,3}, Luca Barbiero⁵, Eugene Demler⁶, Nathan Goldman⁵, Immanuel Bloch^{1,2,3} and Monika Aidelsburger^{1,2,3*}

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REPORT | QUANTUM SIMULATION



Thermalization dynamics of a gauge theory on a quantum simulator

ZHAO-YU ZHOU, GUO-XIAN SU, JAD C. HALIMEH, ROBERT OTT, HUI SUN, PHILIPP HAUKE, BING YANG, ZHEN-SHENG YUAN, JÜRGEN BERGES,

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Umberto Borla, Ruben Verresen, Fabian Grusdt, and Sergej Moroz
Phys. Rev. Lett. **124**, 120503 – Published 26 March 2020

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Federica M. Surace, Paolo P. Mazza, Giuliano Giudici, Alessio Lerose, Andrea Gambassi, and Marcello Dalmonte
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Quantum Coherence in LGTs at the mesoscopic scale

Goal: address properties of LGTs which emerge in quantum coherent systems at the mesoscopic scale.

Quantum technology to explore properties of coherent mesoscopic systems:

- Superconducting circuits
- Cold atoms: neutral atoms, long coherence times

'Roadmap on Atomtronics: State of the art and perspective', Amico, Birkel, Boshier *et al.*, AVS Quantum Science (2021).



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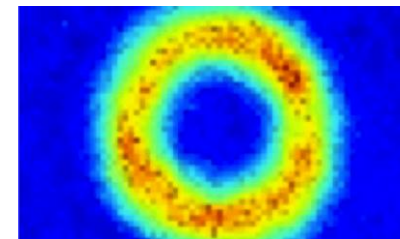
'Roadmap on Atomtronics: State of the art and perspective', Amico, Birkl, Boshier *et al.*, AVS Quantum Science (2021).

Probe of quantum coherence: Persistent Current

$$\mathcal{I}(\Phi) = -\frac{\partial \mathcal{F}(\Phi)}{\partial \Phi}$$

'Probing the BCS-BEC crossover with persistent currents', Pecci, Naldesi *et al.*, PRR (2021).

'Probe for bound states of SU(3) fermions and colour deconfinement', Chetcuti, Polo *et al.*, Communication Physics (2023).



JQI/NIST



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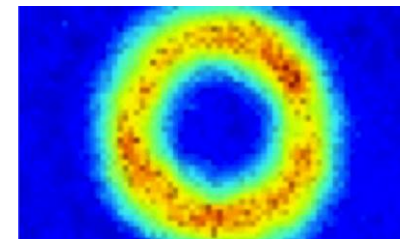
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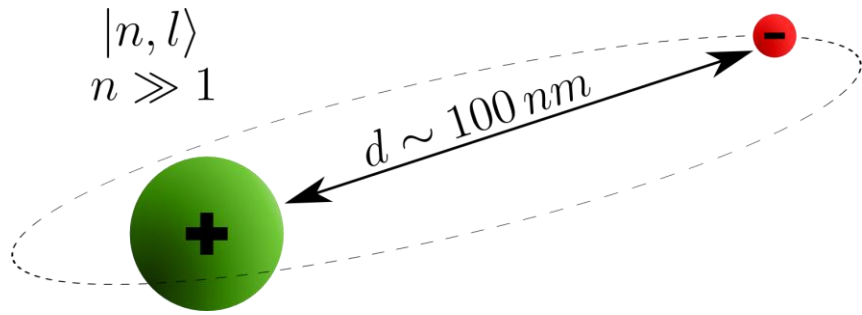


More recently:

- Rydberg atoms: coherent transport of excitations

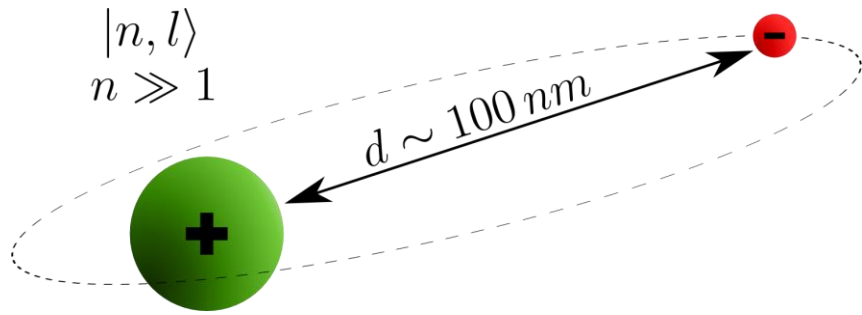
'Controlled flow of excitations in a ring-shaped network of Rydberg atoms', Perciavalle, Rossini *et al.*, PRA (2023).

Rydberg atoms

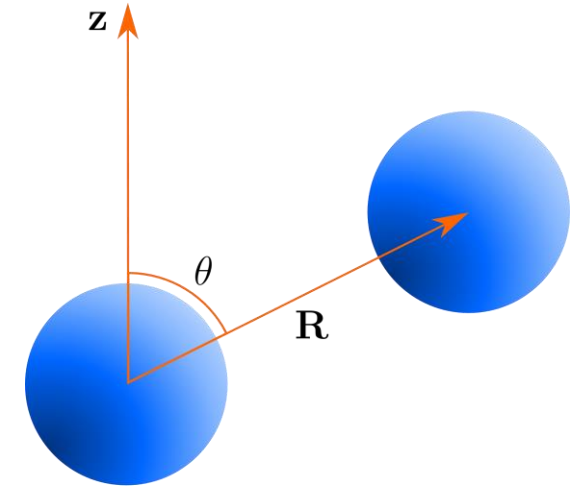


D. Barredo, et al. 2015 *PRL* **114**, 113002
S. Ravets, et al. 2015 *PRA* **92**, 020701(R)
A. Browaeys & T. Lahaye 2020 *Nature Physics* **16**, 132-142

Rydberg atoms

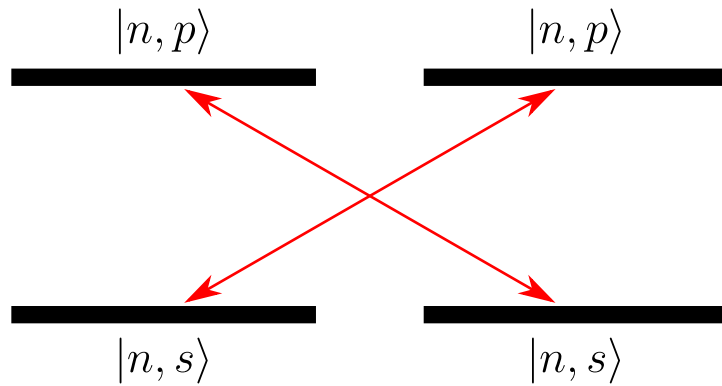
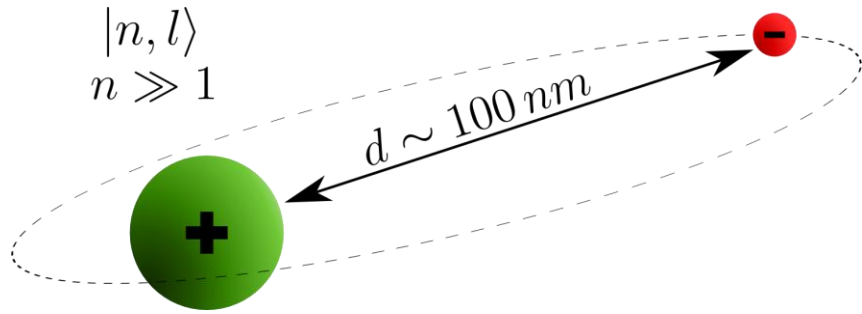


$$V_{dd} = \frac{\mathbf{p}_1 \cdot \mathbf{p}_2 - 3(\mathbf{p}_1 \cdot \mathbf{n})(\mathbf{p}_2 \cdot \mathbf{n})}{R^3}$$



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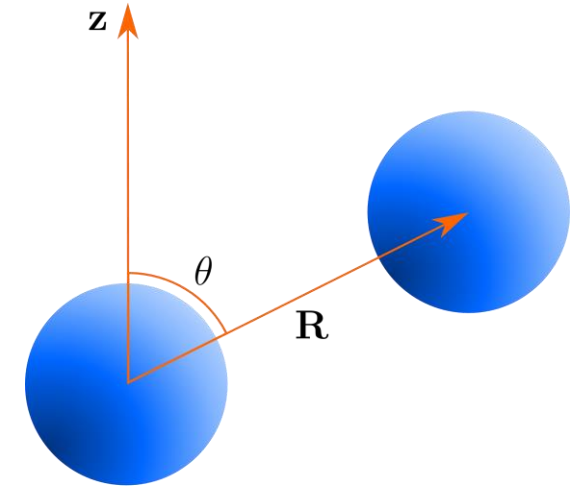
Rydberg atoms



$$\mathcal{H}_{XY} = \sum_{i \neq j} \frac{C_3(\theta_{ij})}{R_{ij}^3} \sigma_i^+ \sigma_j^-$$

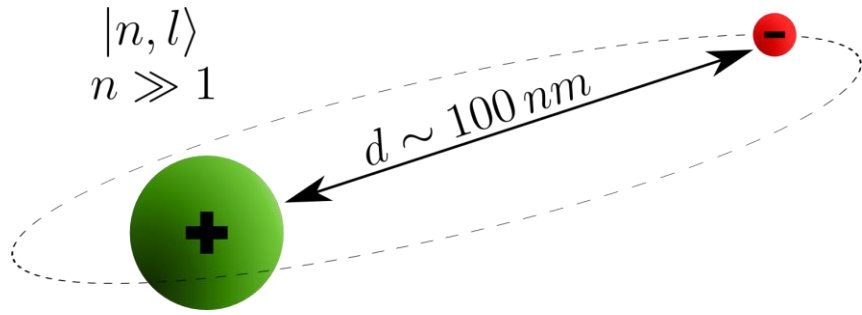
$$C_3(\theta) = C_3 (1 - 3 \cos^2 \theta)$$

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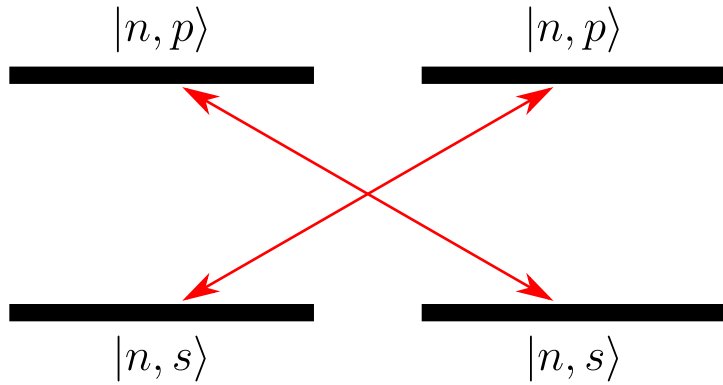
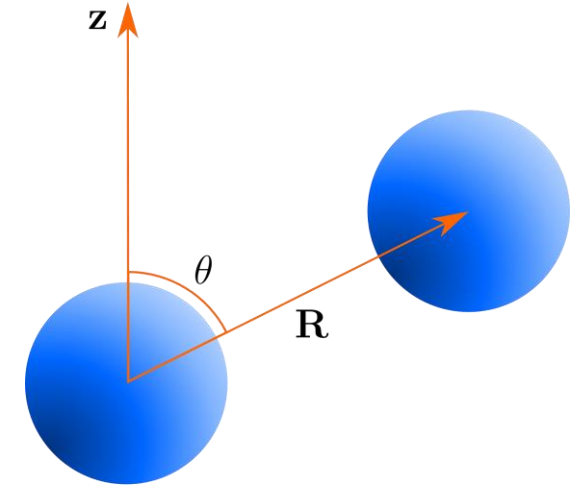


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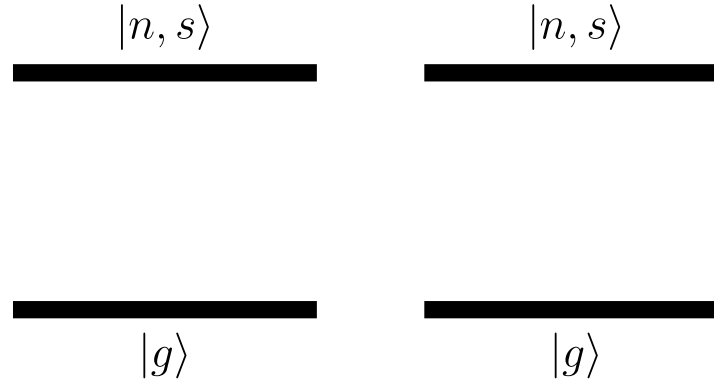


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Gauge theories

Lattice Gauge Theories

(Hamiltonian approach)

Gauge theories

$$S(\psi, A) = \int d^d x \mathcal{L}(\psi(x), A(x))$$

QED

$$\mathcal{L} = \bar{\psi}(i\gamma^\mu(\partial_\mu - ieA^\mu) - m)\psi - \frac{1}{4}F_{\mu\nu}F^{\mu\nu}$$

The action is invariant under local gauge transformations.

$$A_\mu(x) \rightarrow A_\mu(x) + \partial_\mu \Lambda(x)$$

$$\psi(x) \rightarrow e^{ie\Lambda(x)}\psi(x)$$

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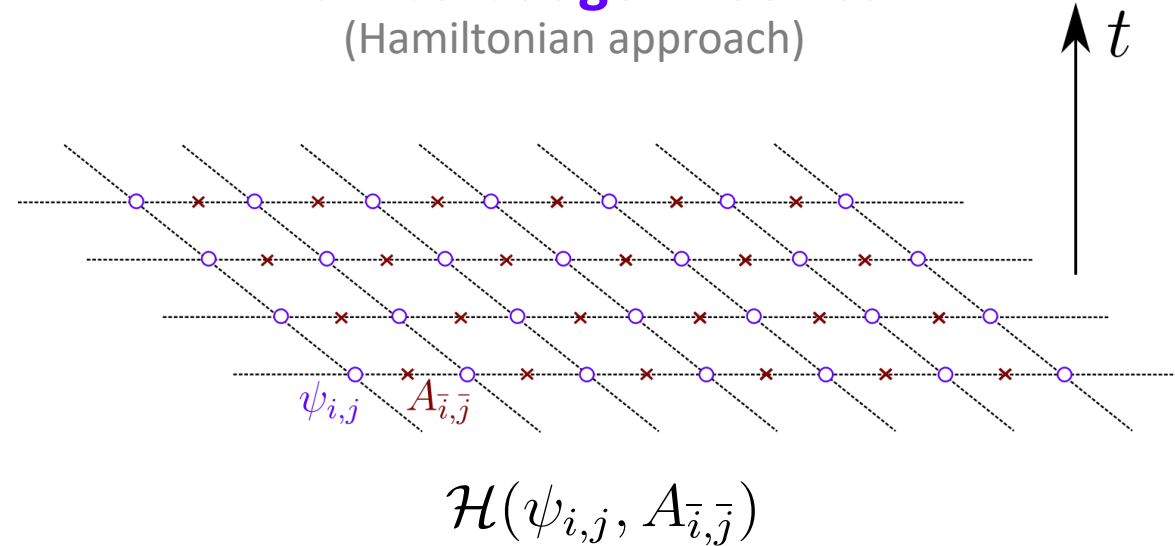
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The Hamiltonian commutes with the generators of local gauge transformations, at each site of the lattice:

$$[\mathcal{H}, G_{i,j}] = 0$$

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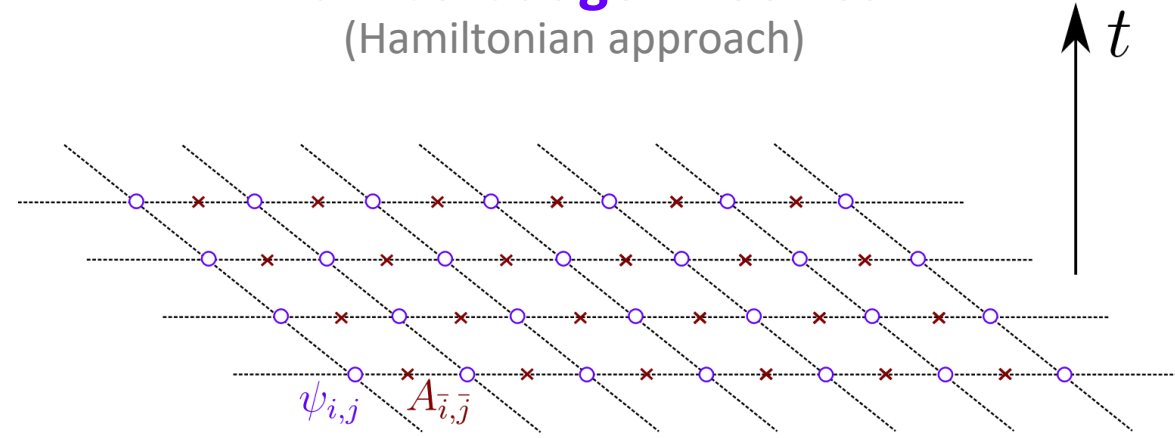
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Lattice Gauge Theories

(Hamiltonian approach)



$$\mathcal{H}(\psi_{i,j}, A_{i,j})$$

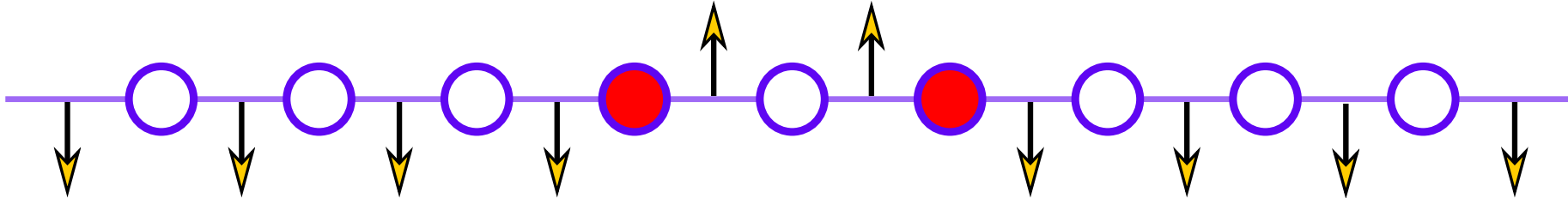
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$$\mathcal{H} = \left(\begin{array}{c} \boxed{} \\ \phantom{\boxed{}} \\ \phantom{\phantom{\boxed{}}} \\ \phantom{\phantom{\phantom{\boxed{}}}} \\ \phantom{\phantom{\phantom{\phantom{\boxed{}}}} \\ \phantom{\phantom{\phantom{\phantom{\phantom{\boxed{}}}} \\ \phantom{\phantom{\phantom{\phantom{\phantom{\phantom{\boxed{}}}} \end{array} \right) \text{GAUGE SECTORS}$$

\mathbb{Z}_2 Lattice gauge theory

$$\mathcal{H} = \sum_j \left[w(c_j^\dagger \sigma_{j+\frac{1}{2}}^x c_{j+1} + h.c.) + \frac{\tau}{2} \sigma_{j+\frac{1}{2}}^z \right]$$

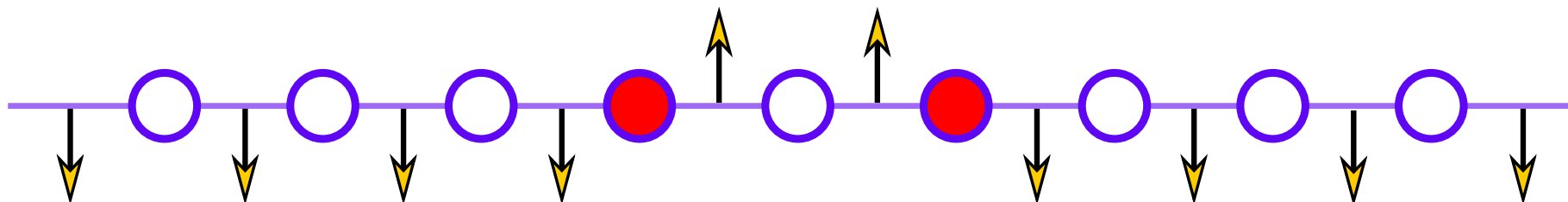


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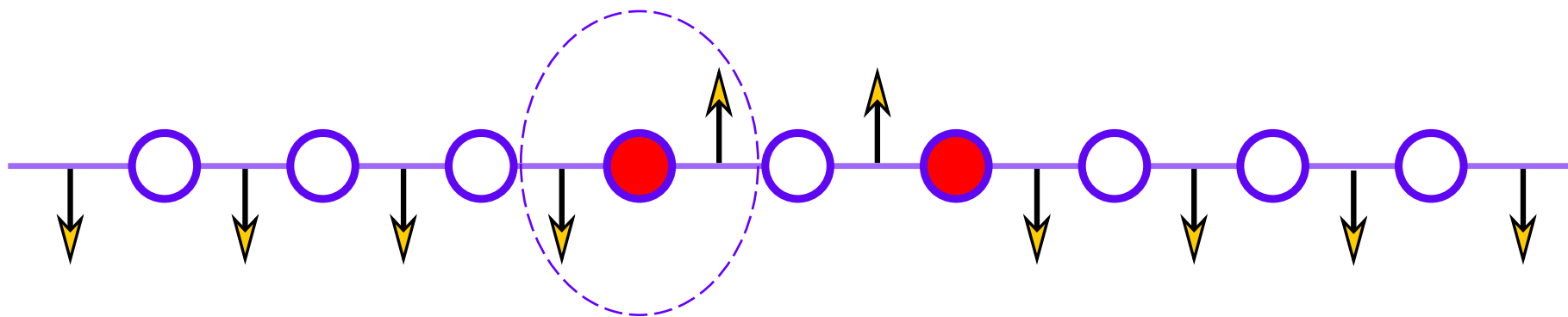
Fermionic operators

Gauge variables



\mathbb{Z}_2 Lattice gauge theory

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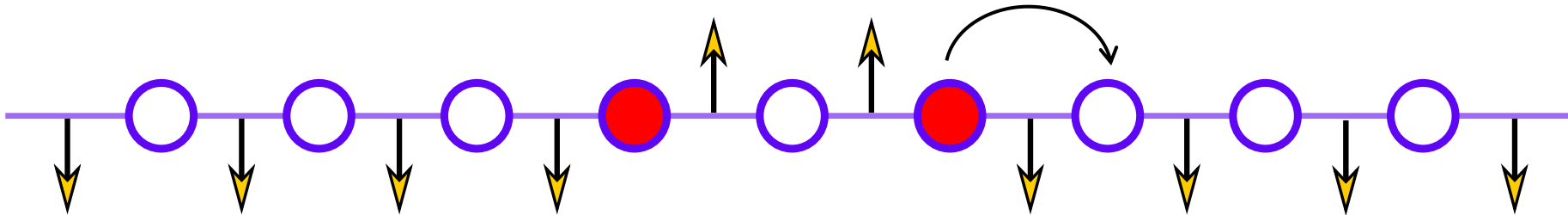
Gauge Constraints: Gauss Law

$$G_j = \sigma_{j-1/2}^z (-1)^{n_j} \sigma_{j+1/2}^z = 1 \forall j$$

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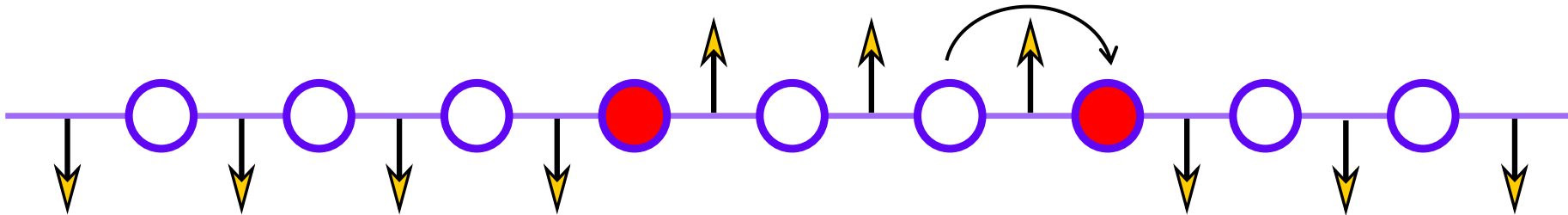
Gauge invariant hopping



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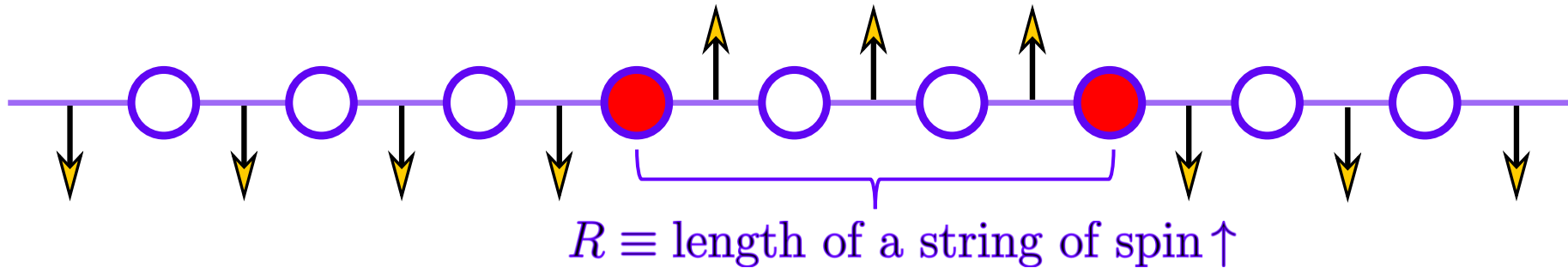
↓
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String tension /
electric field term



$$V(R) = \tau R$$

CONFINING POTENTIAL

➤ Motivation

- Introduction to one dimensional \mathbb{Z}_2 lattice gauge theory

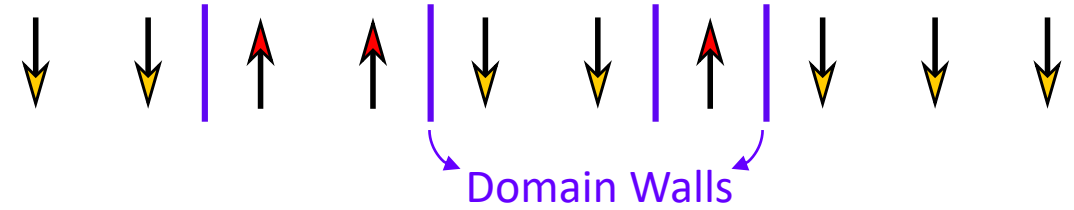
➤ Results

- Implementation on a ring pierced by a synthetic magnetic flux
- Ground state current
- Single meson dynamics in the ring

Implementation on a ring pierced by a synthetic magnetic field

In a **fixed gauge sector**, a \mathbb{Z}_2 Lattice Gauge Theory dynamics can be mapped in an Ising model in transverse & longitudinal fields

$$\mathcal{H} = \sum_j \left[-(m/2) s_j^z s_{j+1}^z + w s_j^x + (\tau/2) s_j^z \right]$$



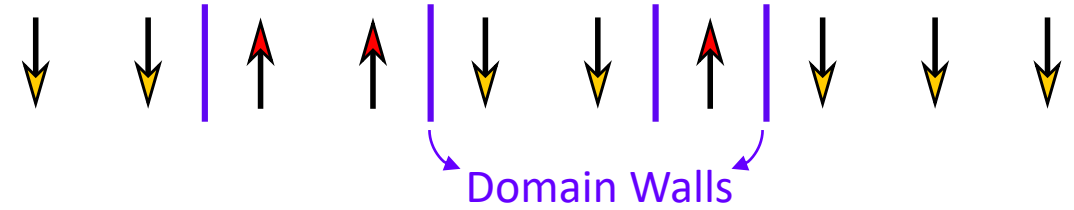
U. Borla, et al. - SciPost Phys. 10, 148 (2021)

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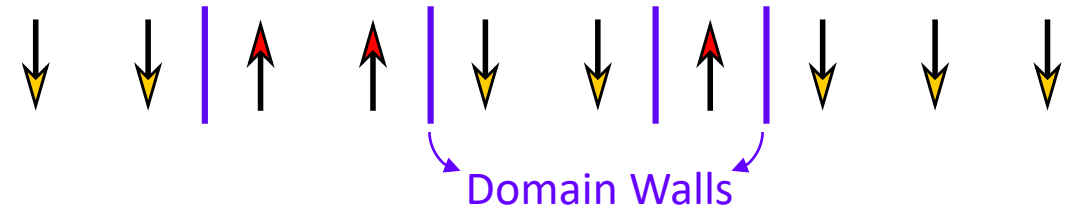
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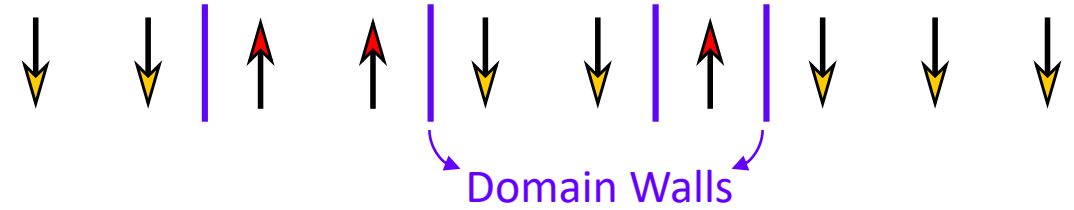
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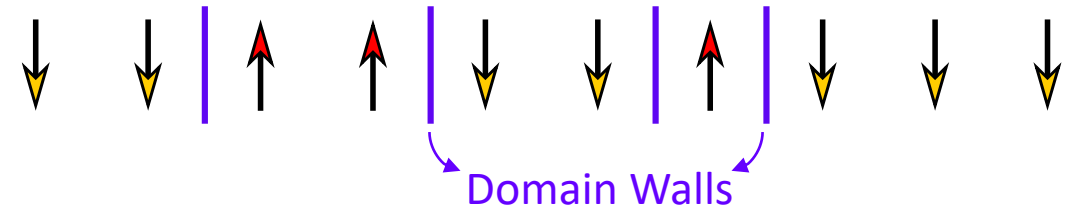
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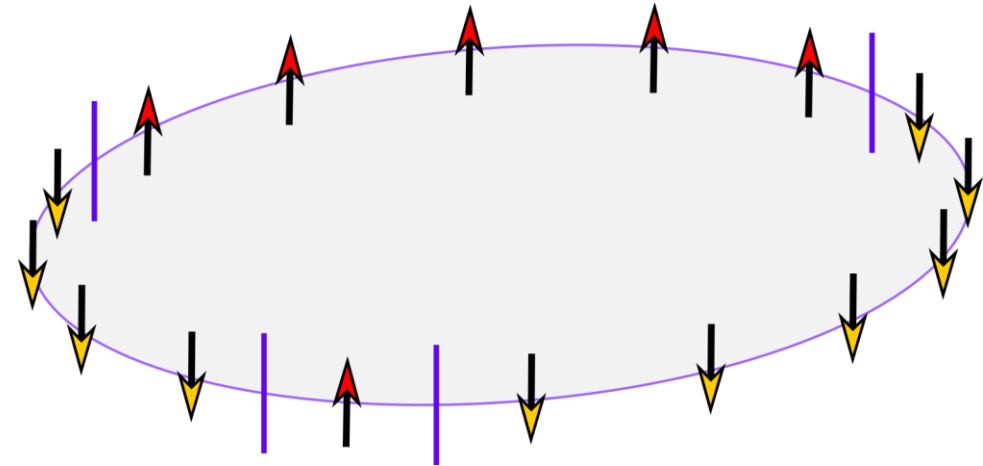
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Floquet engineering → Synthetic magnetic flux

$$\mathcal{H} = \mathcal{H}_0 + \mathcal{H}_{drive}(t)$$

$$\mathcal{H}_0 = \sum_j \left[(\tau/2) s_j^z + w s_j^x + (-1)^j V s_j^z s_{j+1}^z \right]$$

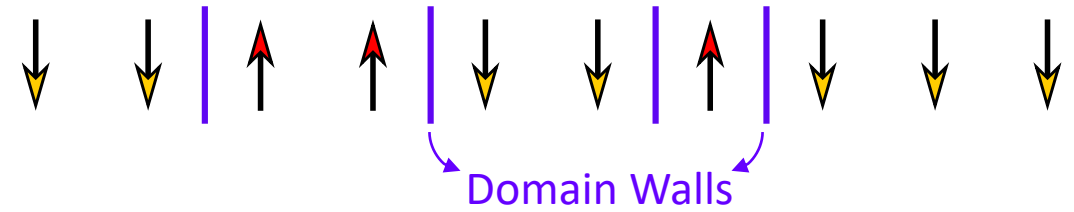
$$\mathcal{H}_{drive}(t) = \sum_j (A/2) \cos(\Omega t + (-1)^j \varphi) s_j^z$$



Implementation on a ring pierced by a synthetic magnetic field

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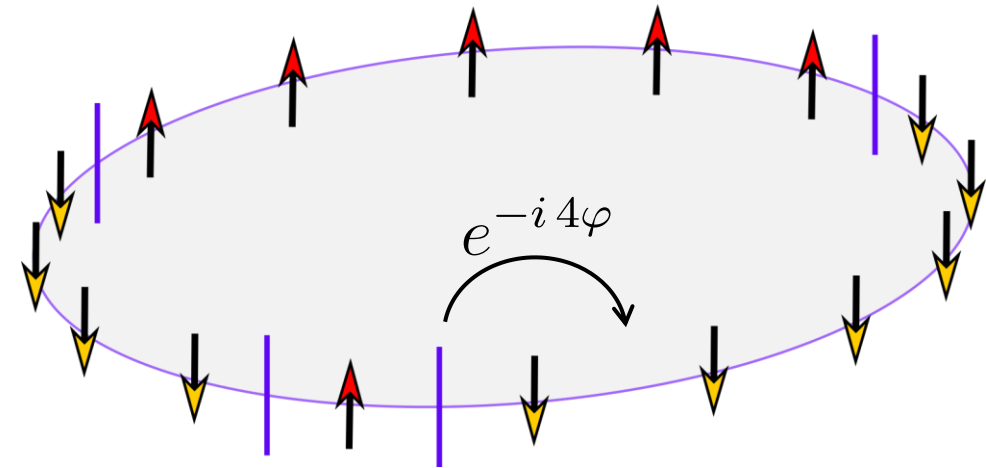
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$$\mathcal{H}_{drive}(t) = \sum_j (A/2) \cos(\Omega t + (-1)^j \varphi) s_j^z$$



$$\mathcal{H}_{\text{eff}} = \sum_j \tilde{w} (e^{i(2\pi/L)(\Phi/\Phi_0)} c_j^\dagger c_{j+1} + h.c.) \sigma_{j+1/2}^x + (\tau/2) \sigma_{j+1/2}^z$$

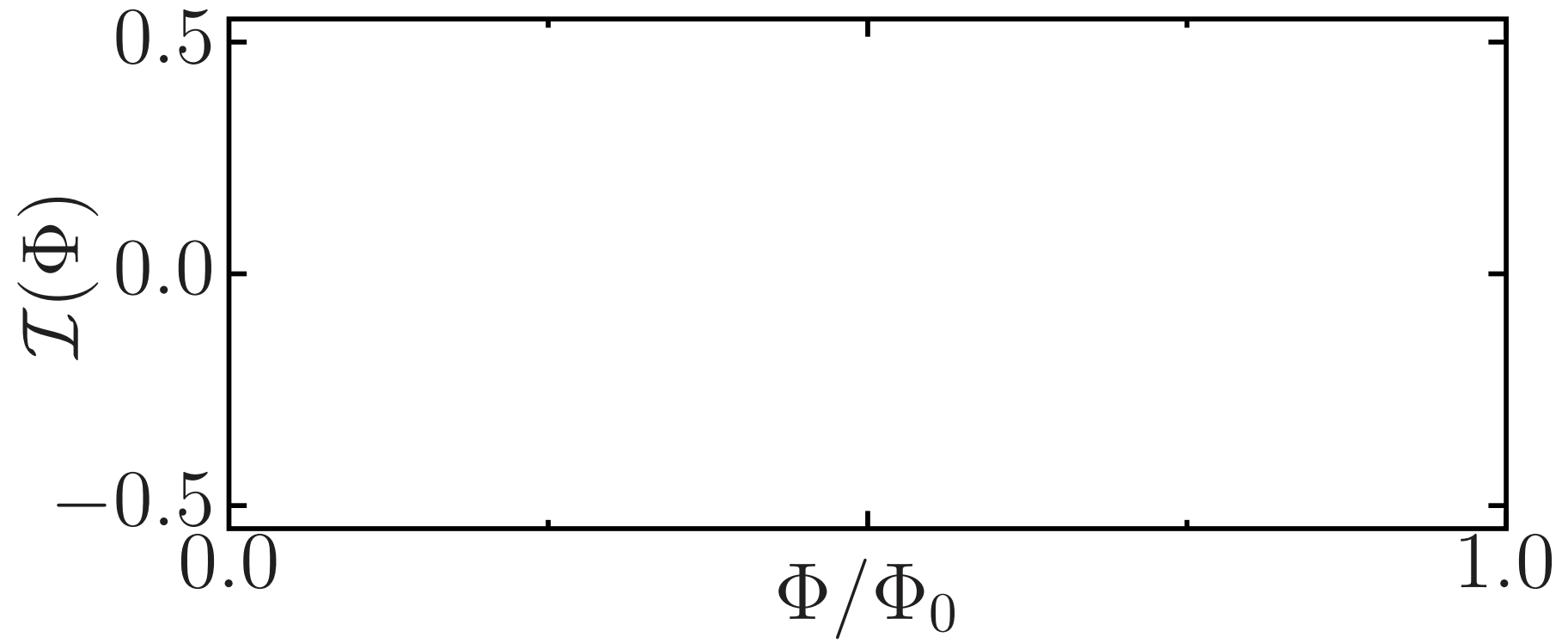
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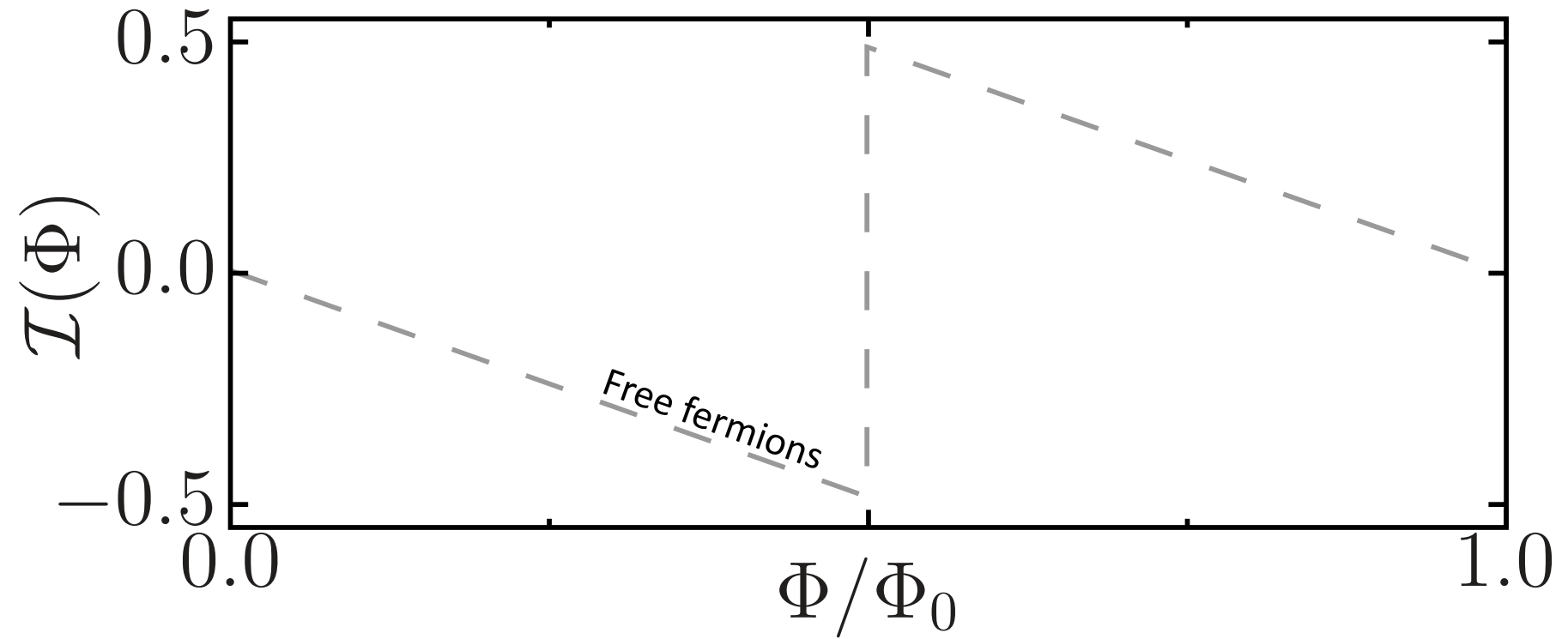
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- **Ground state current**
- Single meson dynamics in the ring

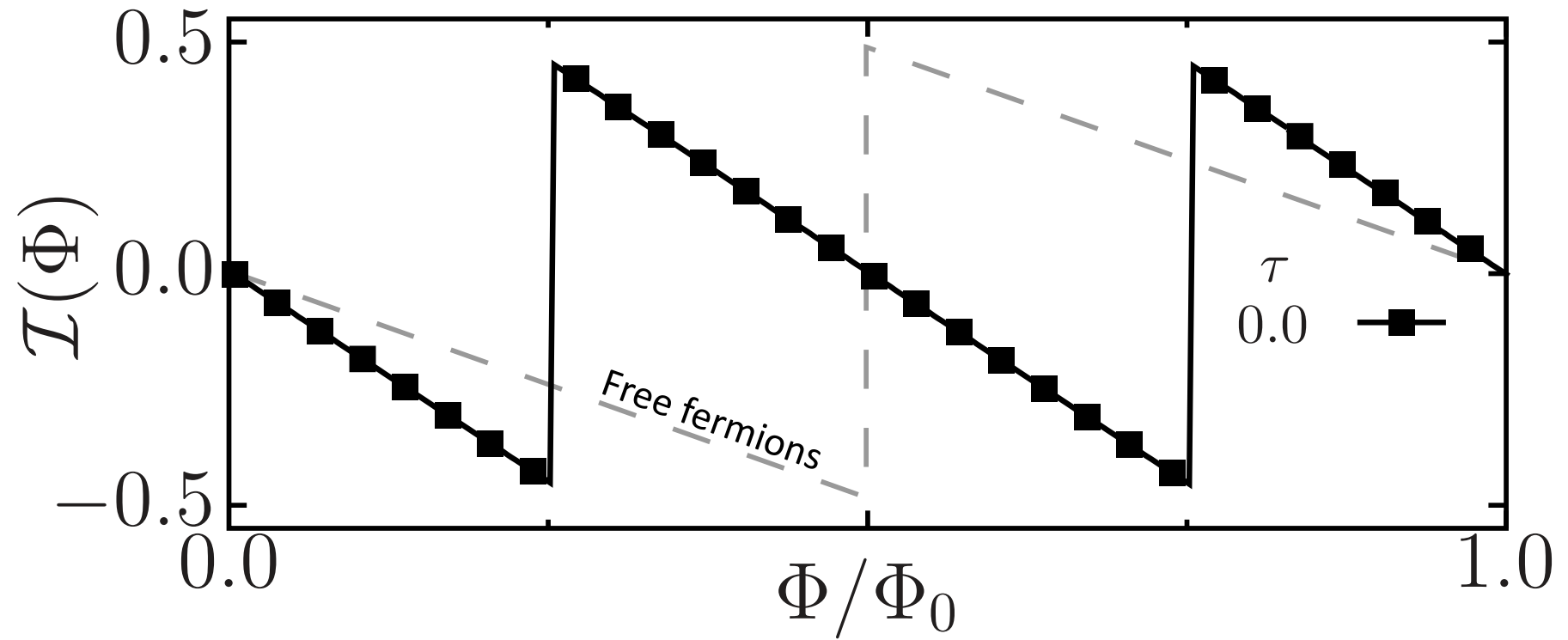
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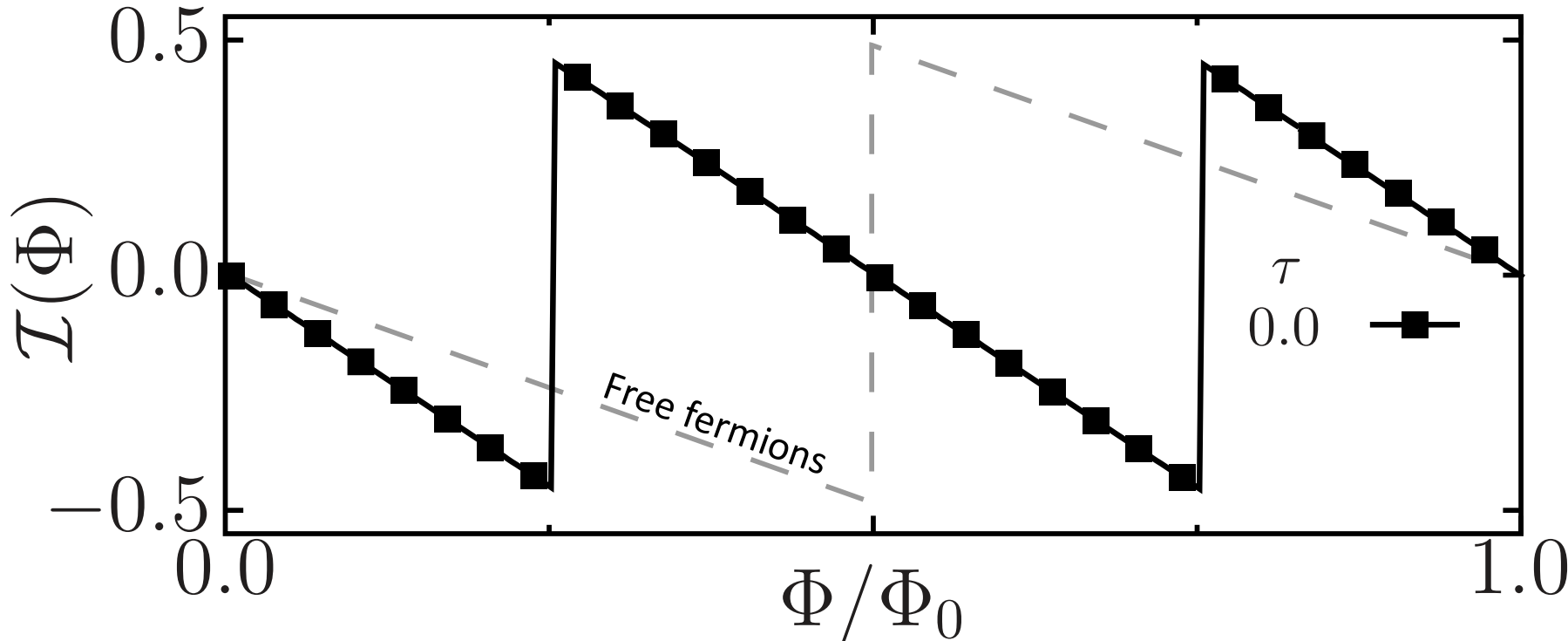
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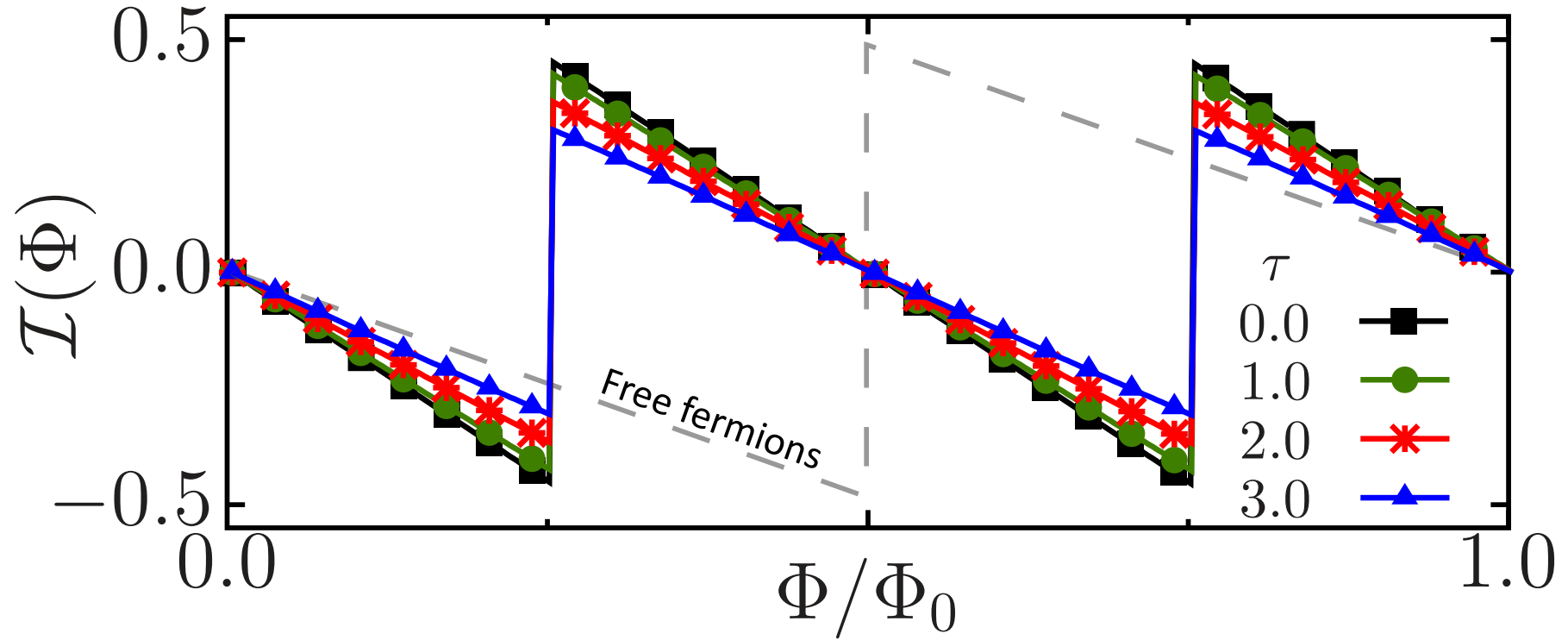
Symmetry at $\tau = 0$

$$W = \prod_{\text{ring}} \sigma_{j+\frac{1}{2}}^x$$

\mathbb{Z}_2 Flux – adds to the total phase acquired by particles circulating the ring

$$\mathcal{H} = \left(\begin{array}{l} W = 1 \\ \text{Free fermions} \\ \Phi_{\text{TOT}} = \Phi \end{array} \right) \left(\begin{array}{l} W = -1 \\ \text{Free fermions} \\ \Phi_{\text{TOT}} = \Phi + \pi \end{array} \right)$$

Ground state current



The symmetry is broken for $\tau \neq 0$

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➤ Motivation and introduction

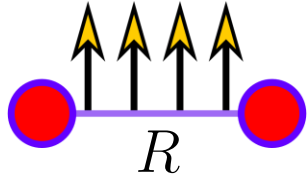
- Introduction to one dimensional \mathbb{Z}_2 lattice gauge theory

➤ Results

- Implementation on a ring pierced by a synthetic magnetic flux
- Ground state current
- **Single meson dynamics in the ring**

Exact solution of the two-particle problem on the ring with flux

Exact solution of the two-particle problem on the ring with flux



$$\Psi_E(s, R) = \mathcal{N} e^{iKs} \chi_E(\boxed{K}, R)$$

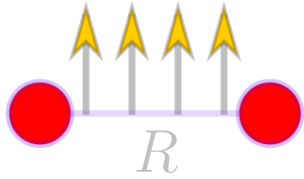
Center of mass momentum $K = \frac{2\pi}{L} n$

$$2w \cos \left(\frac{K}{2} + \frac{2\pi\Phi}{L\Phi_0} \right) [\chi(R+1) + \chi(R-1)] + \tau R \chi(R) = E \chi(R)$$

Wannier-Stark equation

G. H. Wannier – Rev. Mod. Phys. (1962)

Exact solution of the two-particle problem on the ring with flux



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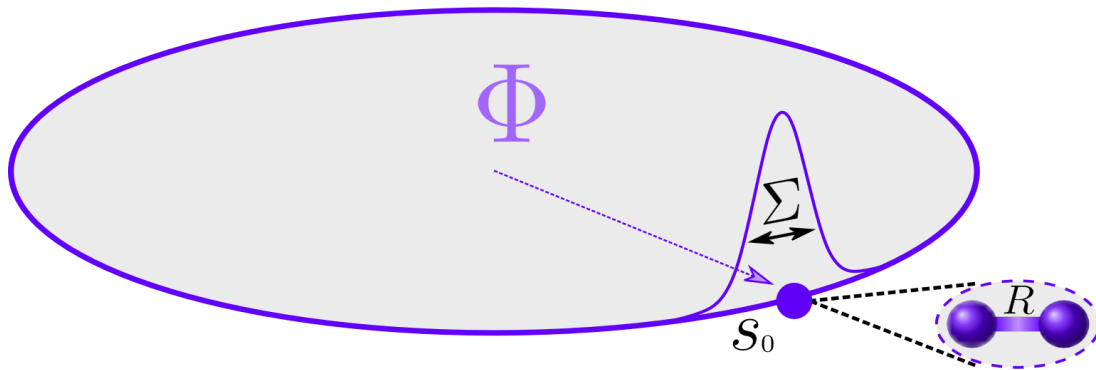
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Quench dynamics



$$\Phi = 0 \rightarrow \Phi \neq 0$$

$$\psi_0(s, R) = e^{-(s-s_0)^2/(2\Sigma^2)} \boxed{\Psi_{E_0}(s, R)}$$

$\boxed{\Sigma}$ → gaussian width

$\boxed{\Psi_{E_0}(s, R)}$
↓
lowest energy eigenstate

Quench dynamics

	CENTER OF MASS DYNAMICS	STRING DYNAMICS	CURRENT DYNAMICS
$\Sigma \rightarrow 2$	$P(s, t)$	$P(R, t)$	$\langle \psi(t) \mathcal{I} \psi(t) \rangle$
$\Sigma \rightarrow 0$			

Quench dynamics

CENTER OF MASS DYNAMICS

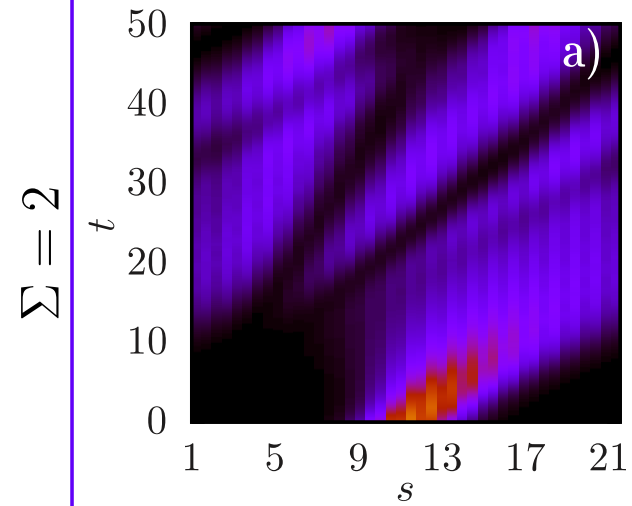
$$P(s, t)$$

STRING DYNAMICS

$$P(R, t)$$

CURRENT DYNAMICS

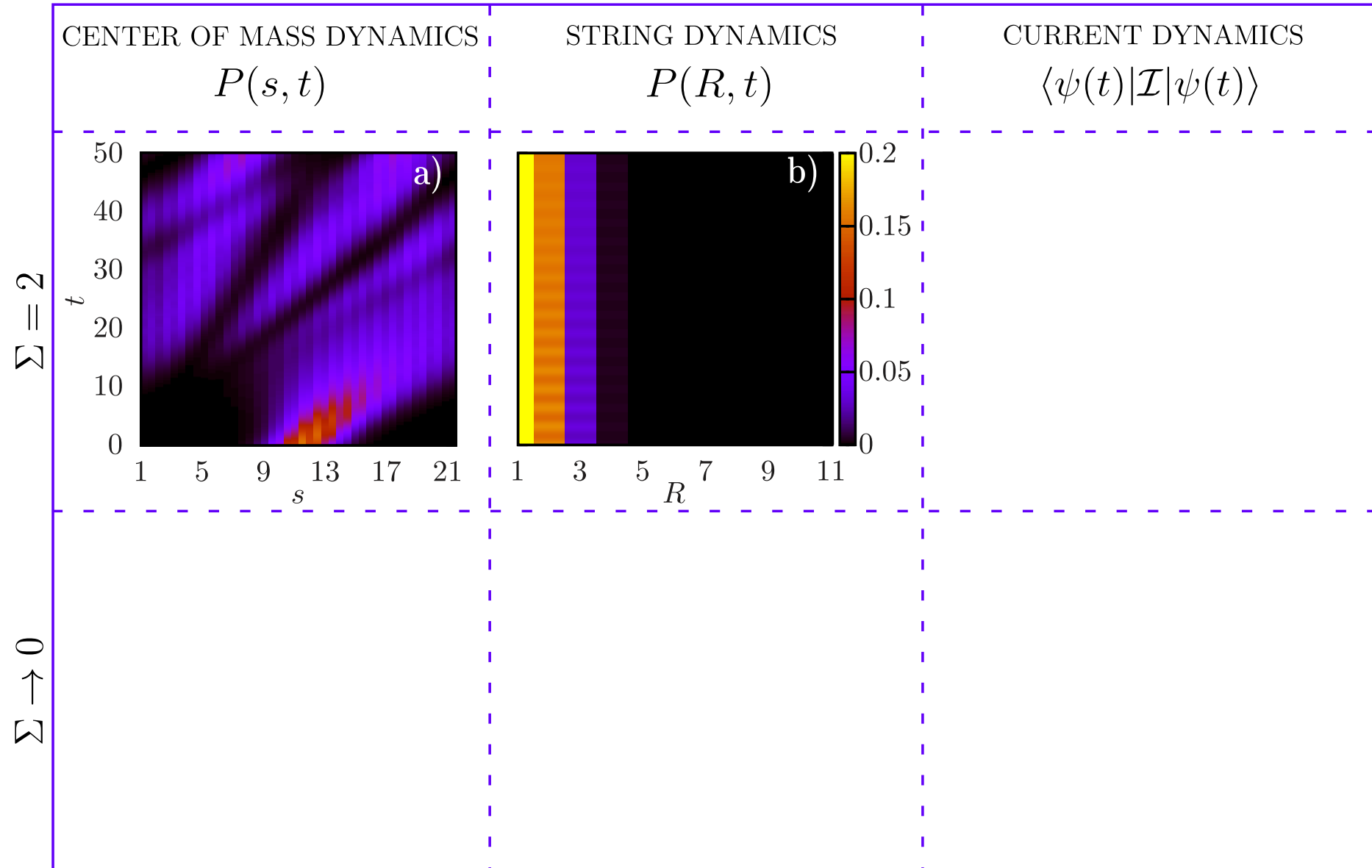
$$\langle \psi(t) | \mathcal{I} | \psi(t) \rangle$$



- Directional motion

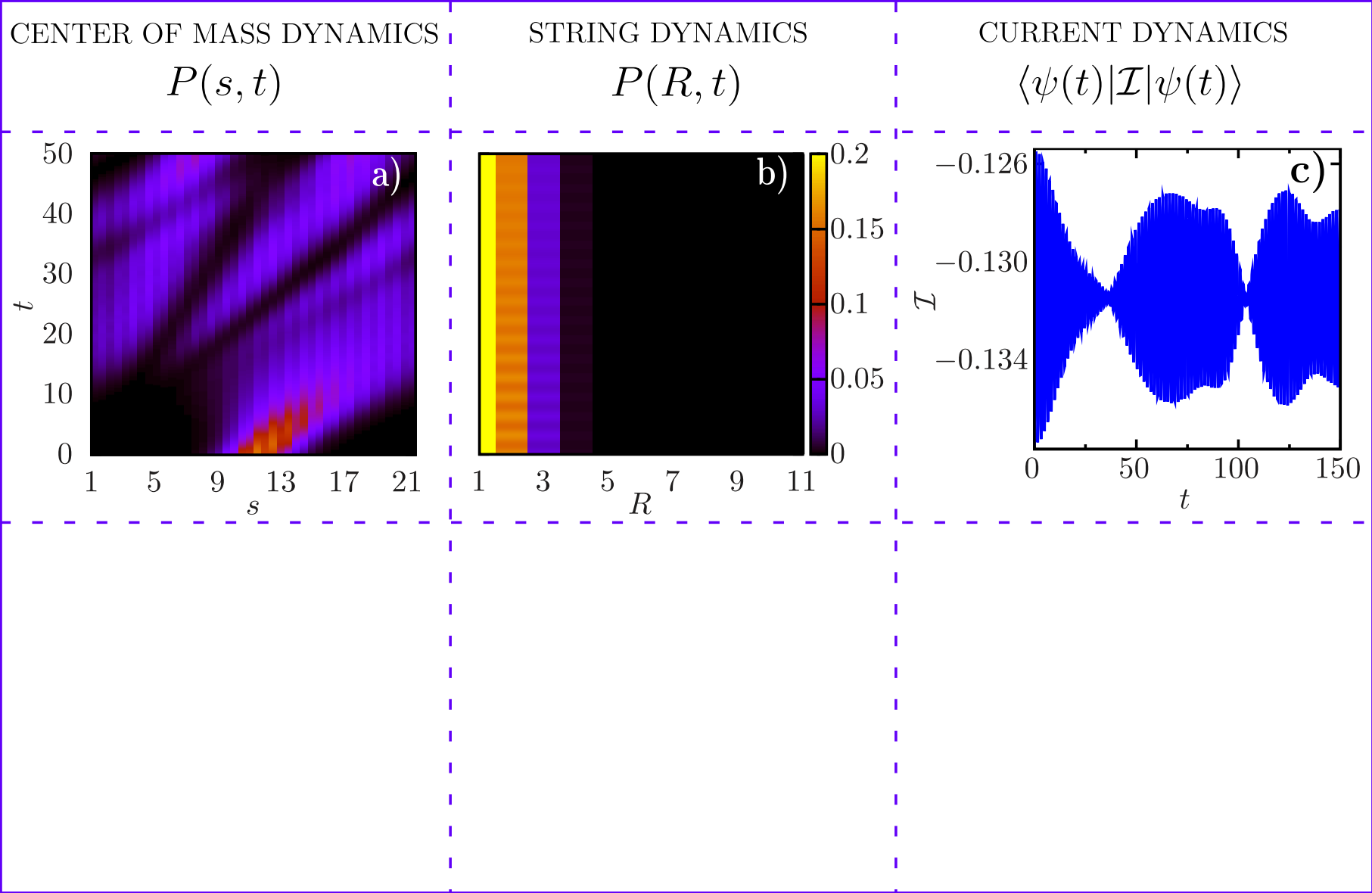
$\Sigma \rightarrow 0$

Quench dynamics



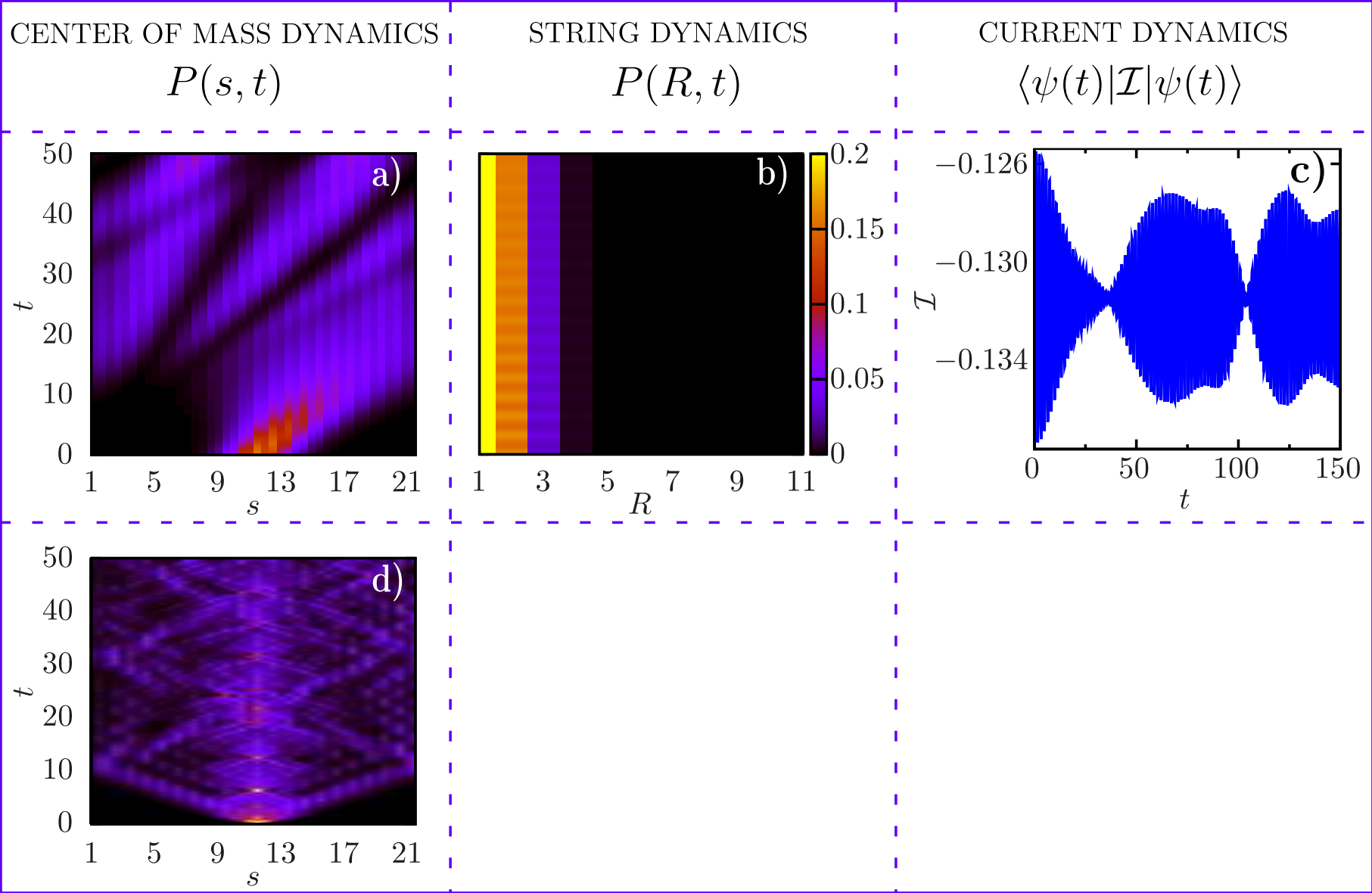
- Directional motion
- Suppressed string oscillations

Quench dynamics



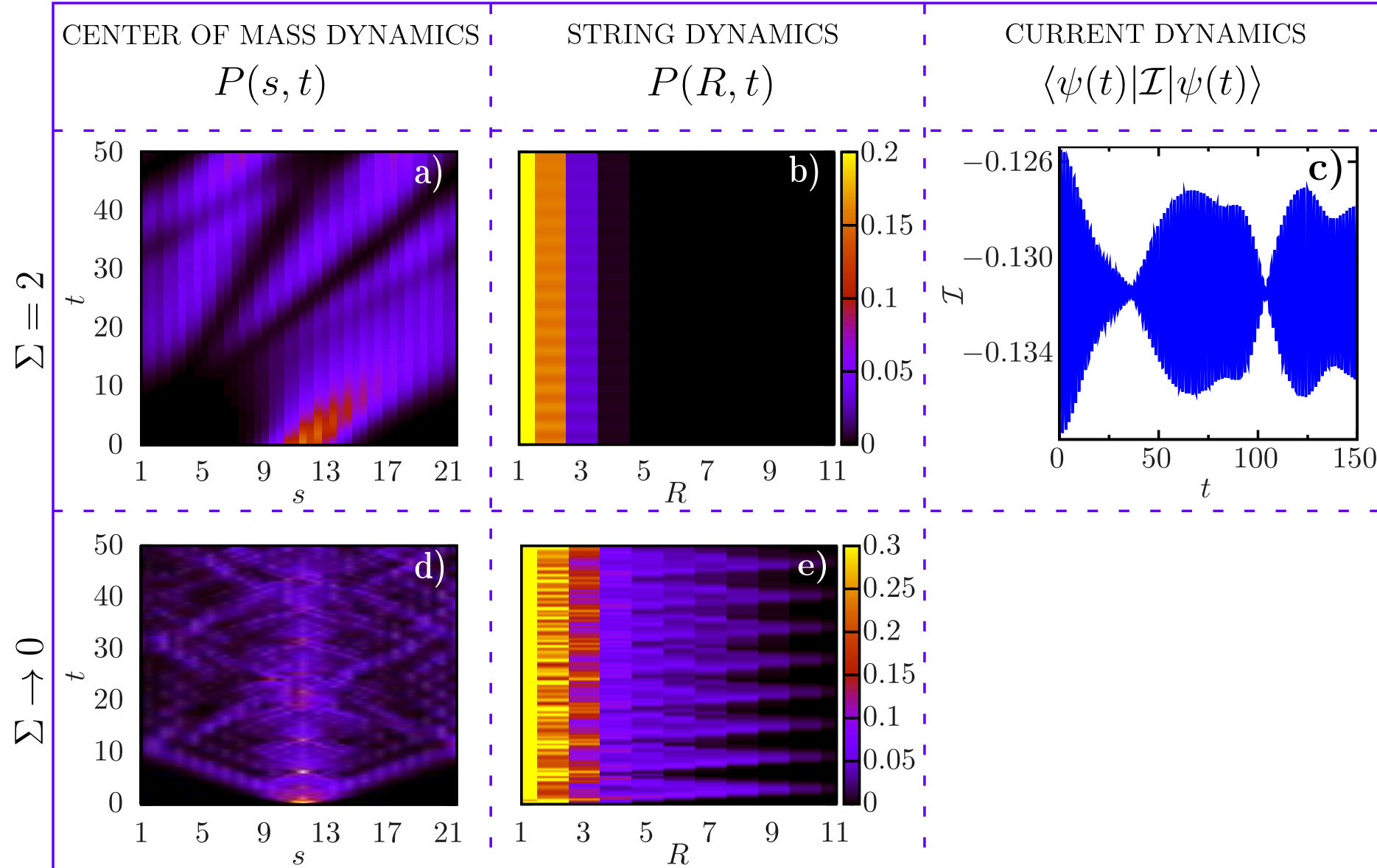
- Directional motion
- Suppressed string oscillations
- \mathcal{I} oscillates around a finite value \mathcal{I}_0

Quench dynamics



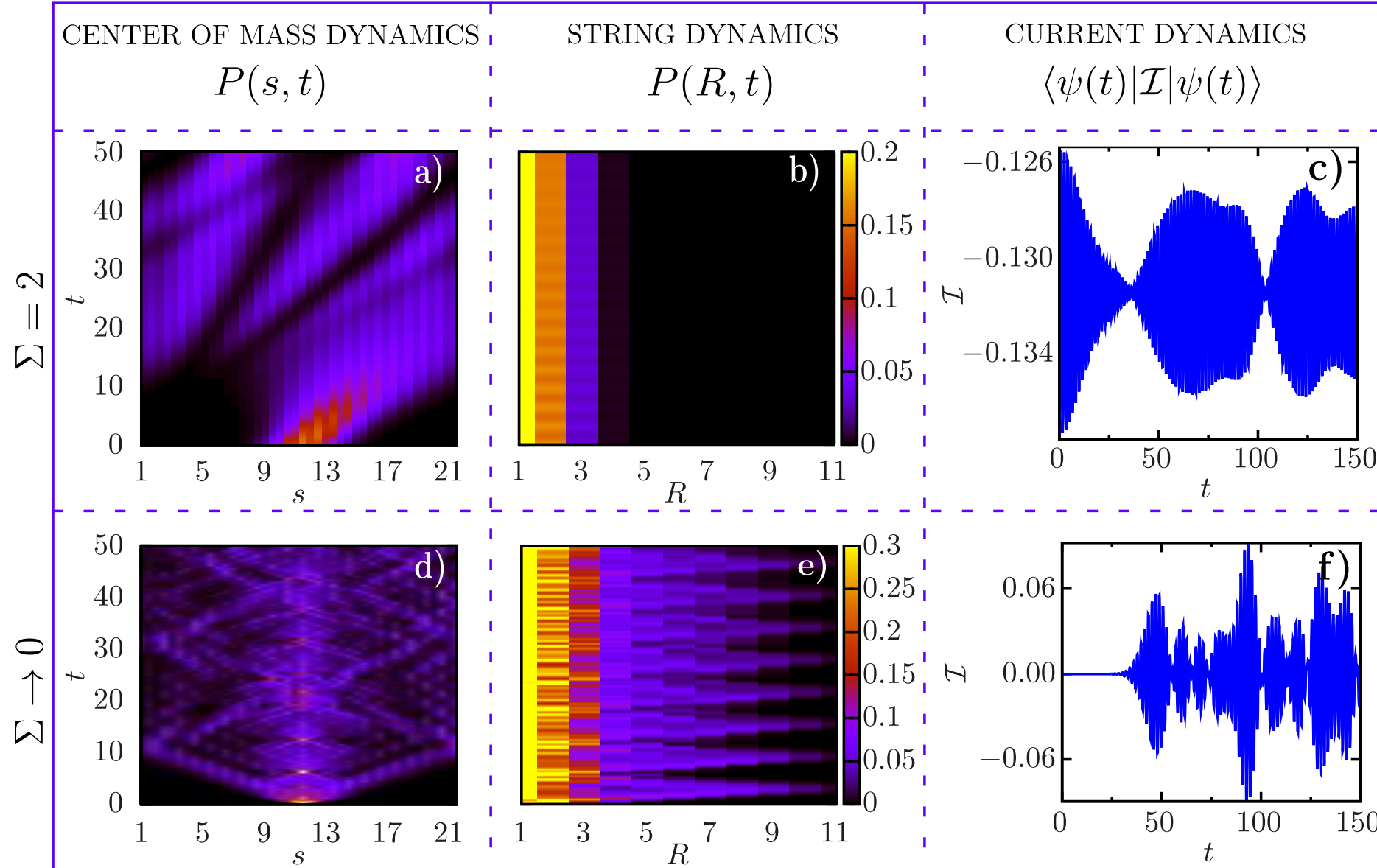
- Directional motion
- Suppressed string oscillations
- \mathcal{I} oscillates around a finite value \mathcal{I}_0
- Non-directional motion

Quench dynamics



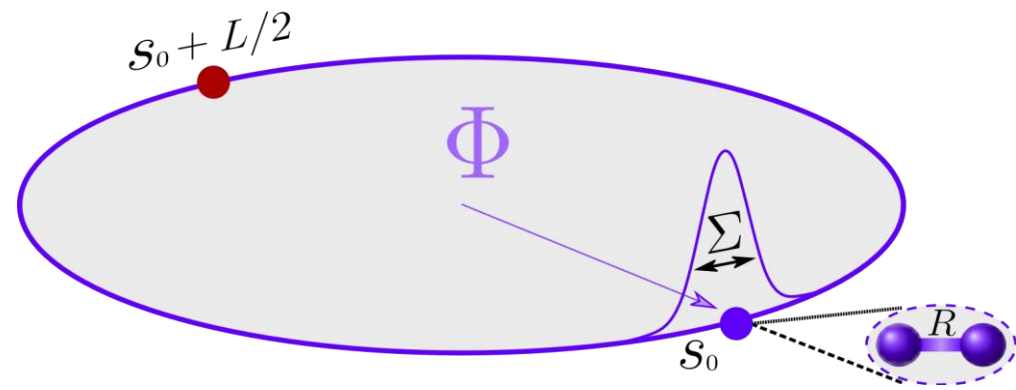
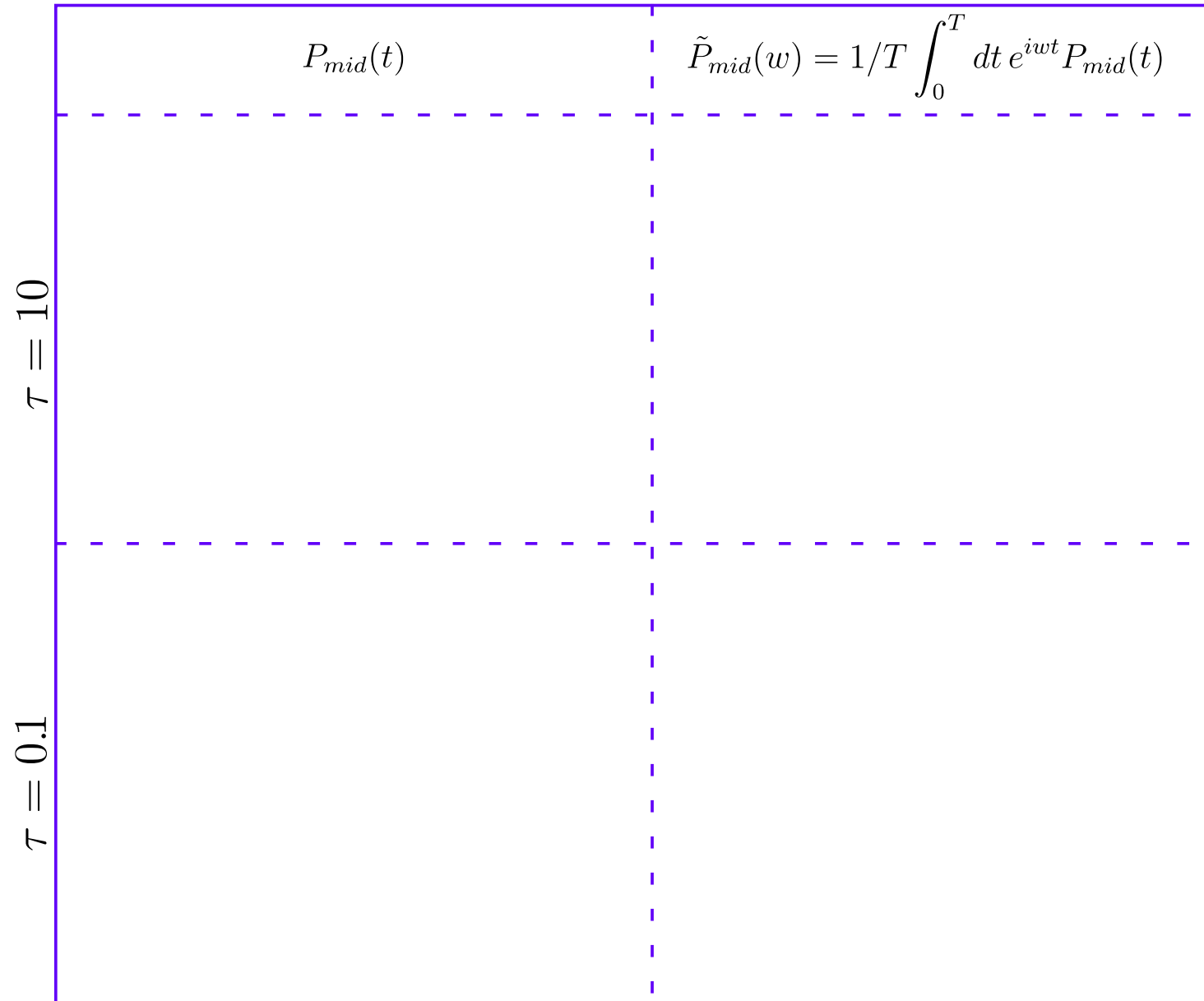
- Directional motion
- Suppressed string oscillations
- \mathcal{I} oscillates around a finite value \mathcal{I}_0
- Non-directional motion
- Broad string oscillations

Quench dynamics



- Directional motion
 - Suppressed string oscillations
 - \mathcal{I} oscillates around a finite value \mathcal{I}_0
-
- Non-directional motion
 - Broad string oscillations
 - \mathcal{I} is zero on average

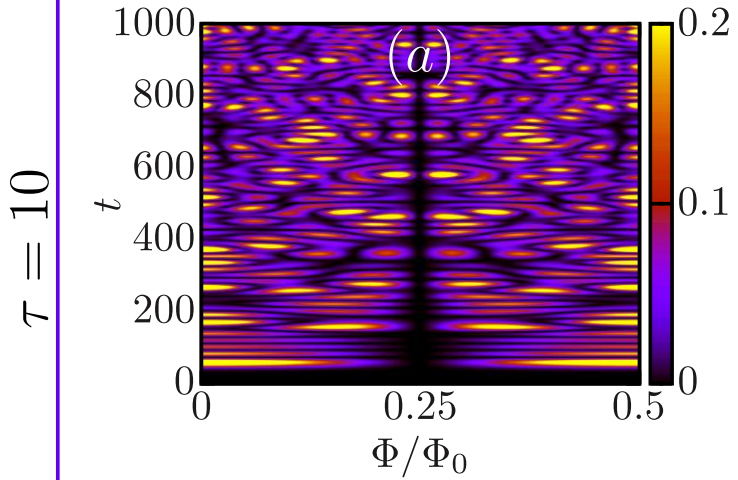
Aharonov-Bohm effect



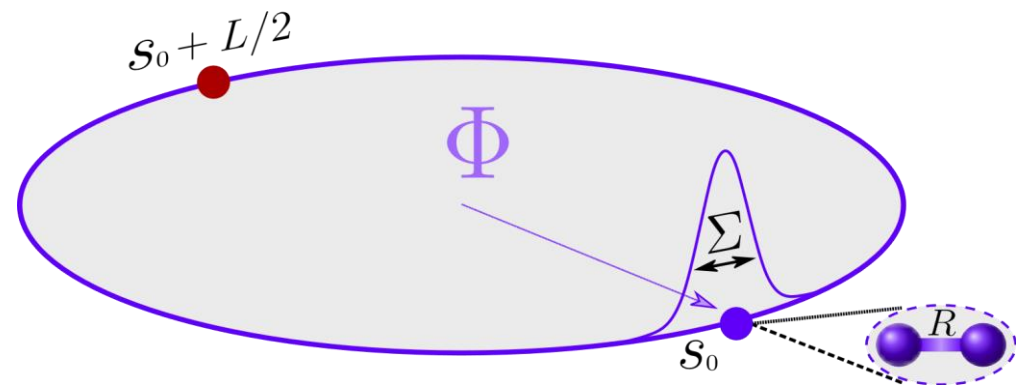
Aharonov-Bohm effect

$P_{mid}(t)$

$$\tilde{P}_{mid}(w) = 1/T \int_0^T dt e^{iwt} P_{mid}(t)$$



$\tau = 0.1$

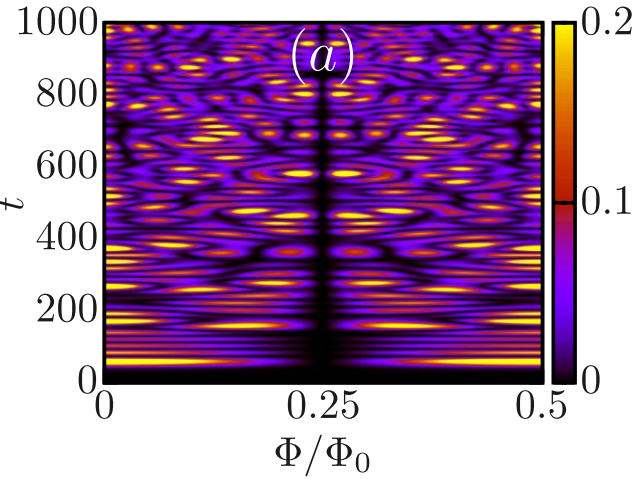


Aharonov-Bohm effect

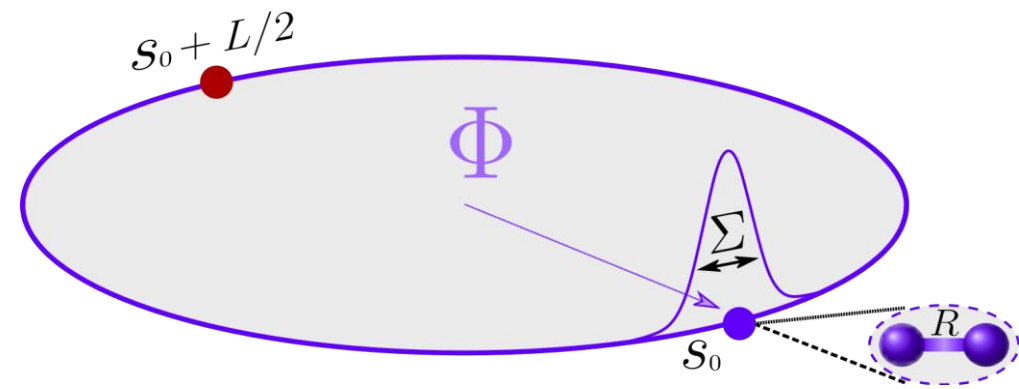
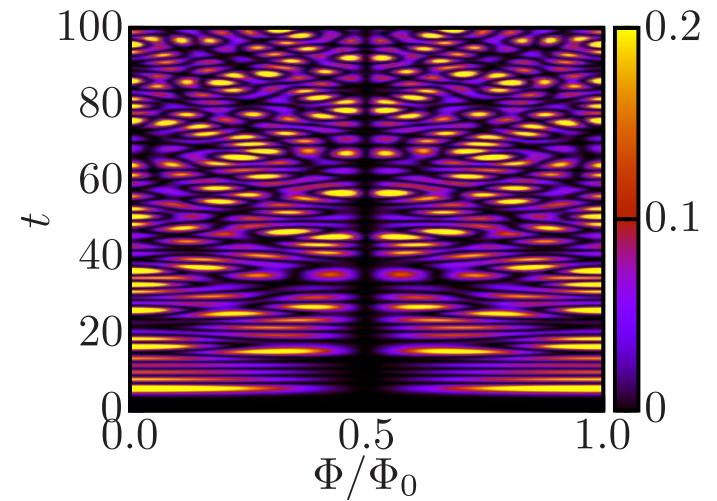
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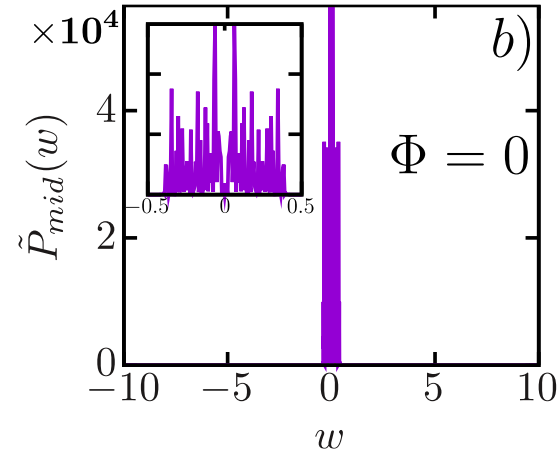
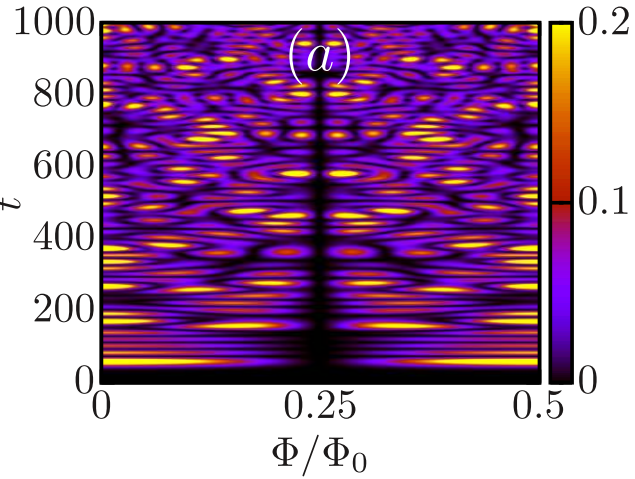
- Effectively single particle Aharonov – Bohm effect
- Slow dynamics

Aharonov-Bohm effect

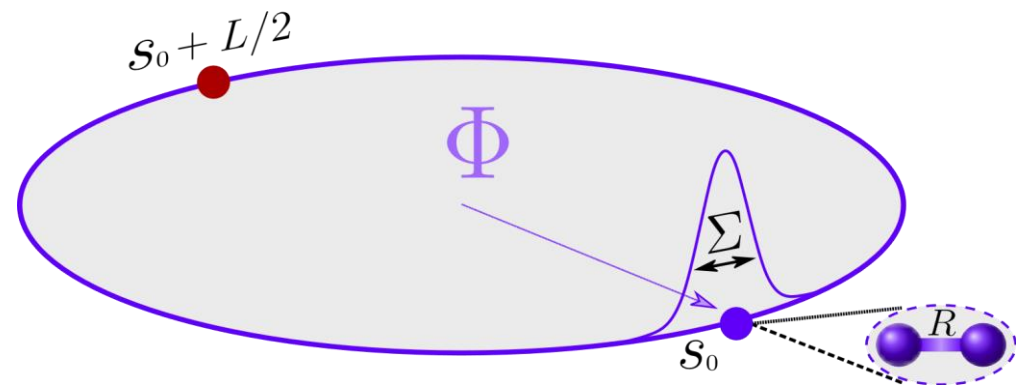
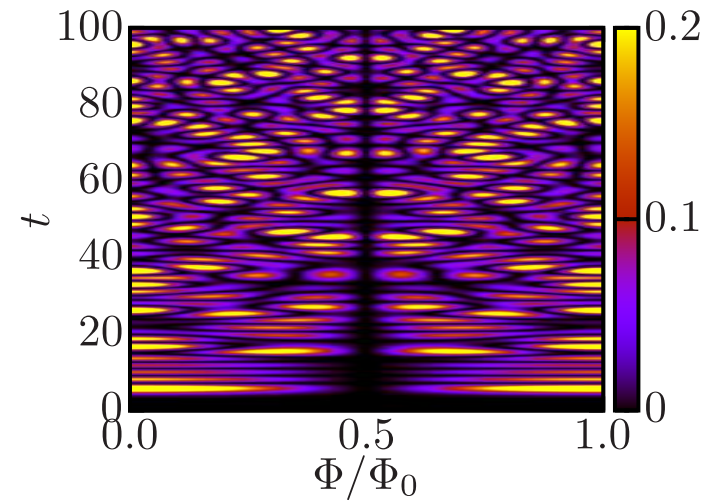
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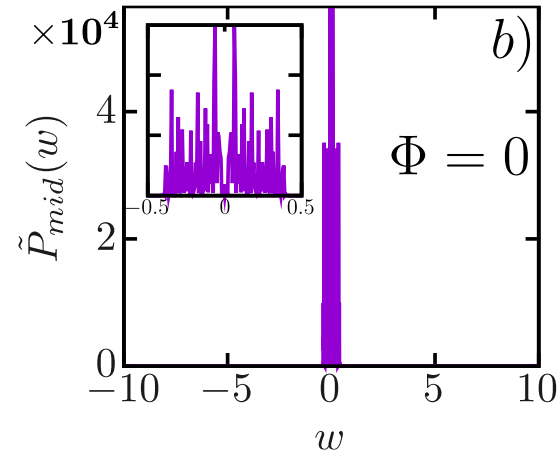
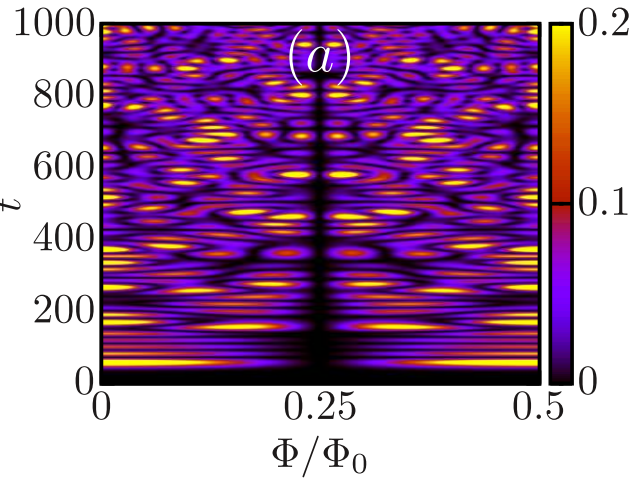
- Effectively single particle Aharonov – Bohm effect
- Slow dynamics
- Narrow frequency distribution

Aharonov-Bohm effect

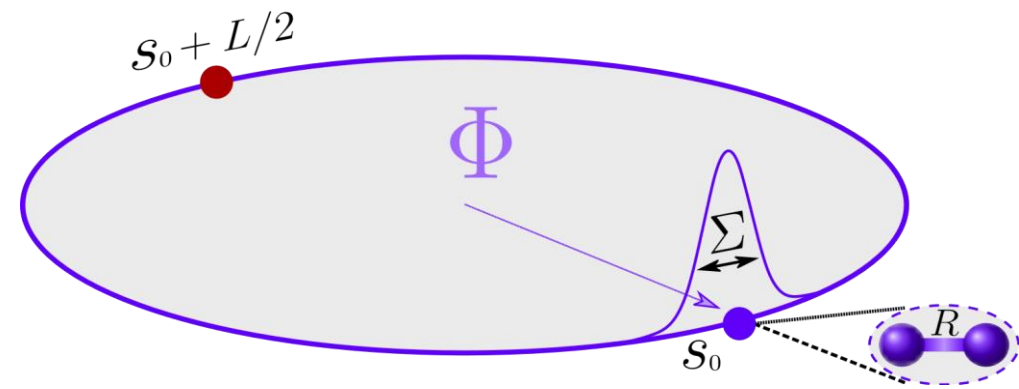
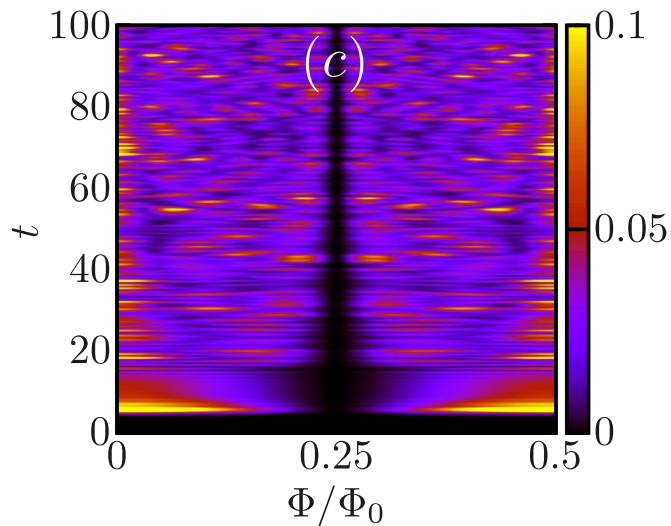
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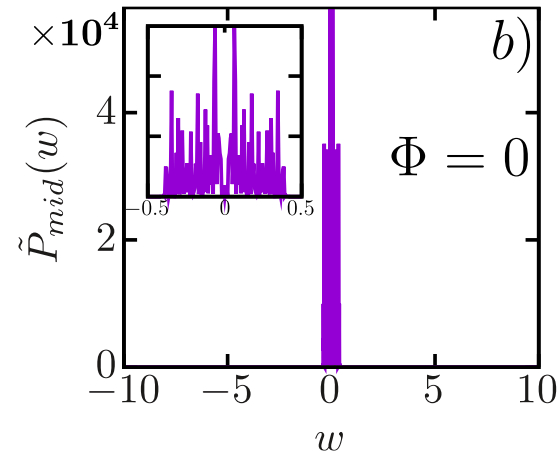
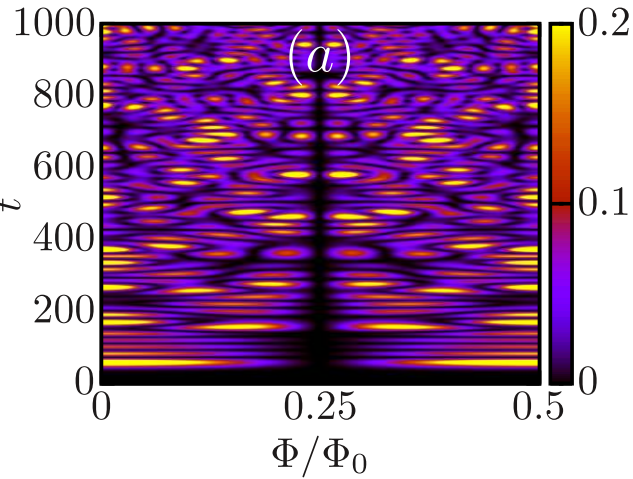
- Effectively single particle Aharonov – Bohm effect
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- Aharonov – Bohm oscillations combine with the string dynamics

Aharonov-Bohm effect

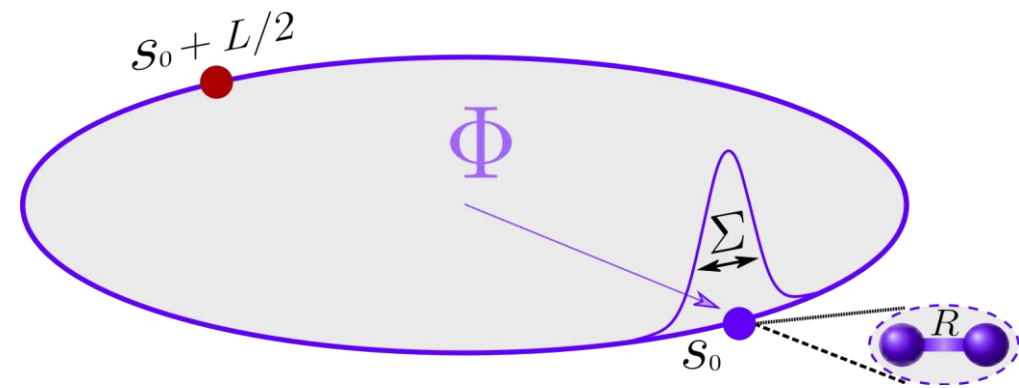
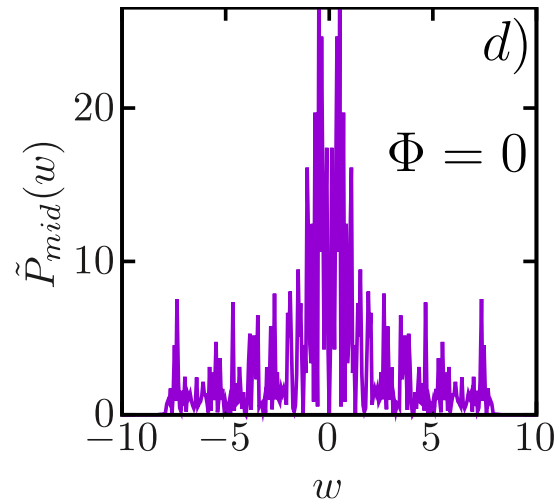
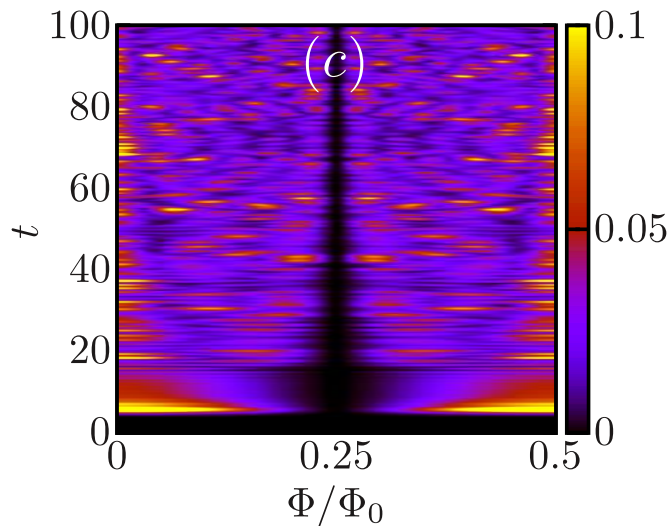
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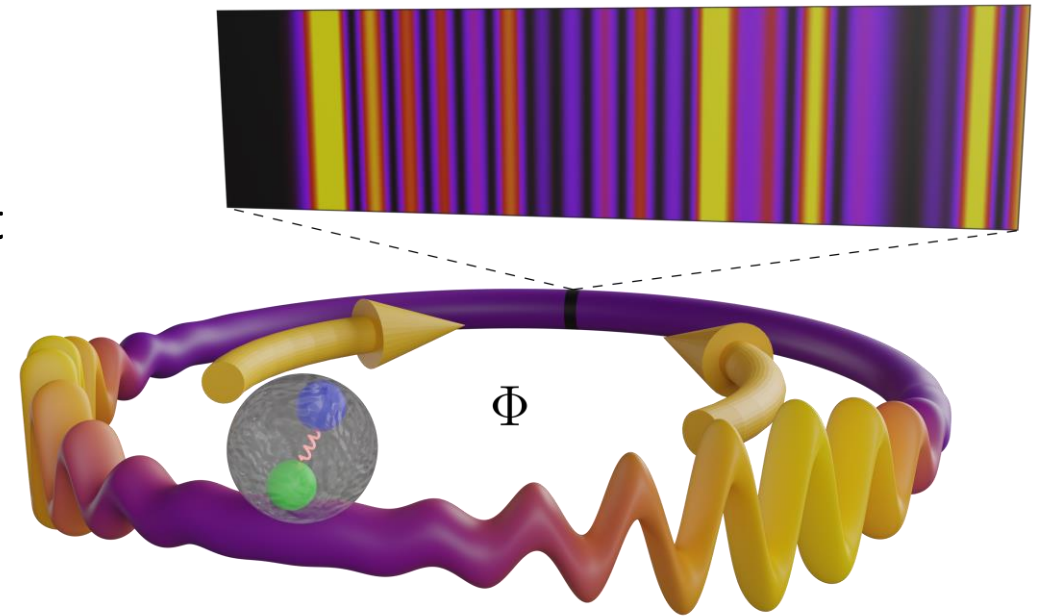
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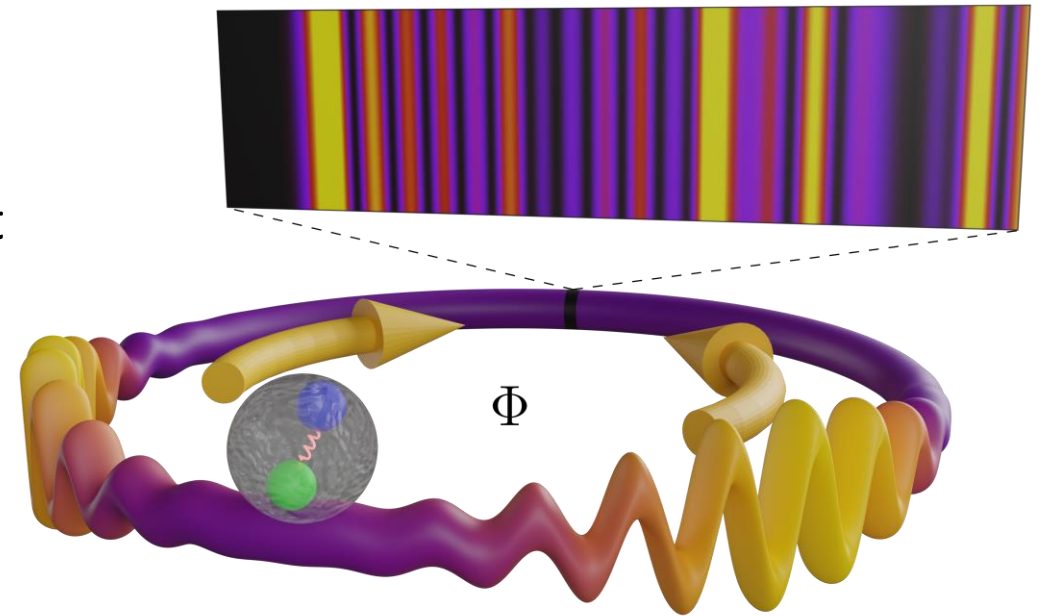
Summary

- We proposed an implementation of a synthetic magnetic flux in a Z2 LGT via Floquet engineering
- We studied coherence properties of the theory
 - Fractionalization of the ground state current
 - Flux driven dynamics of a single meson
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- Future directions
 - Extension to other LGTs
 - Scattering with localized potential barriers in the ring



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Thank you for your attention!