

# Searching for evidences of Exotic Compact Objects from the spin distribution of compact binary coalescences

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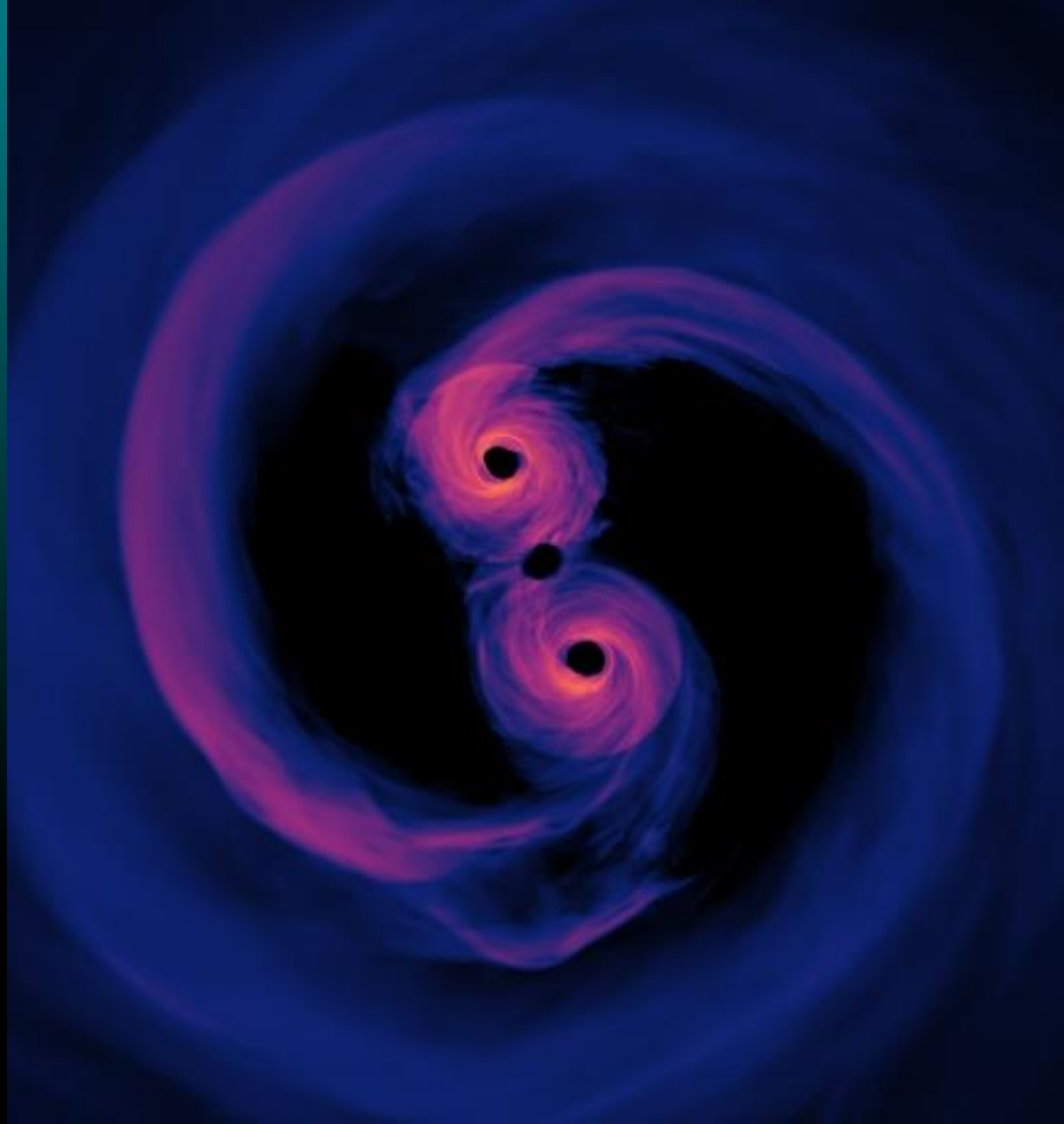
In collaboration with:

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Elisa Maggio (AEI, Potsdam)

**GraSP, 25/10/2023**

**Pisa**



# Outline of the work

## RATIONALE

- ✓ **Gravitational waves (GWs)** from **compact binary coalescence (CBC)** represent a novel tool to investigate the **nature of compact objects**.
- ✓ **Exotic Compact Objects (ECOs)** could in principle be distinguished by **Black Holes (BHs)** through minor phenomenological effects, like the **ergoregion instability**.

## STRUCTURE OF THE WORK

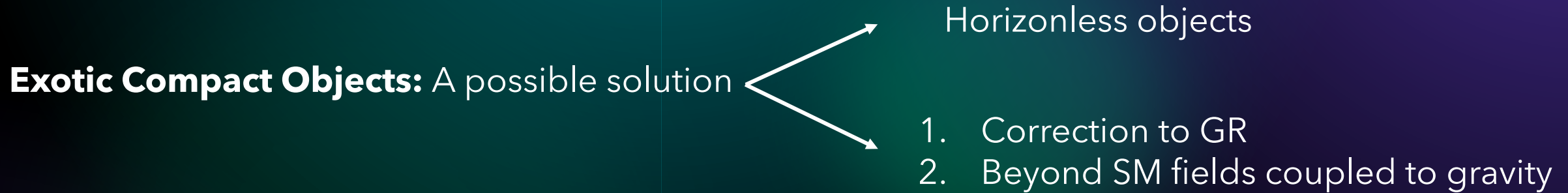
- 1. Hierarchical Bayesian inference** using GWs from the **population** of binary black holes (BBHs) of the **third observing run (O3)**.
- 2. Spins as figures of merit:** assume different spin distribution for populations of BHs and ECOs.
- 3. Assume firstly** a population of only ECOs, and **then a mixed** one.

*K. Ng et al. Phys. Rev. D 103, 063010 (2021)*

*K. Ng et al. Phys. Rev. D 126, 151102 (2021)*

# Why Exotic Compact Objects?

**Black holes** are fascinating objects but present theoretical controversies (curvature singularity, information loss paradox).



## CLASSIFIED BY

### Compactness

**Inverse** of the (possibly effective) **radius**, defined as:

$$r_0 = r_+(1 + \varepsilon)$$

With  $r_+$  Kerr horizon,  $\varepsilon$  **closeness parameter**.

**BH limit:**  $\varepsilon \rightarrow 0$

### Reflectivity

At **their** (possibly effective) **surface**

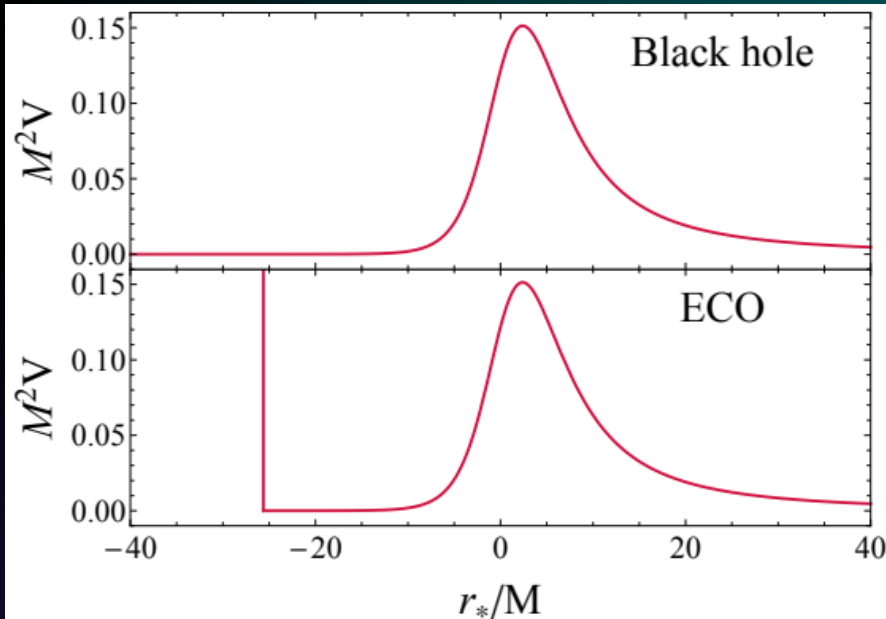
$$\mathcal{R}$$

In general complex and frequency dependent.

**BH limit:**  $\mathcal{R} \rightarrow 0$

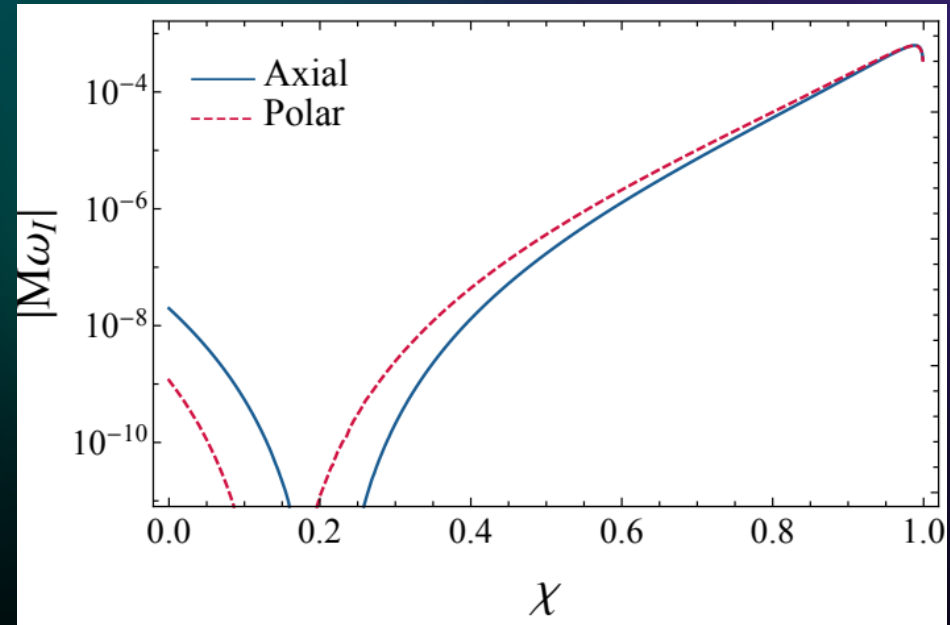
# The ergoregion instability (1/2)

Linear perturbations: 
$$\frac{d^2\Psi(r)}{dr_*^2} + [\omega^2 - V(r)]\Psi(r) = 0$$



**Potential governing the master equation:**

In the ECO case, the absence of the horizon at  $r_* \rightarrow -\infty$  implies a cavity, producing long-lived modes. Here  $\varepsilon = 10^{-6}$ .

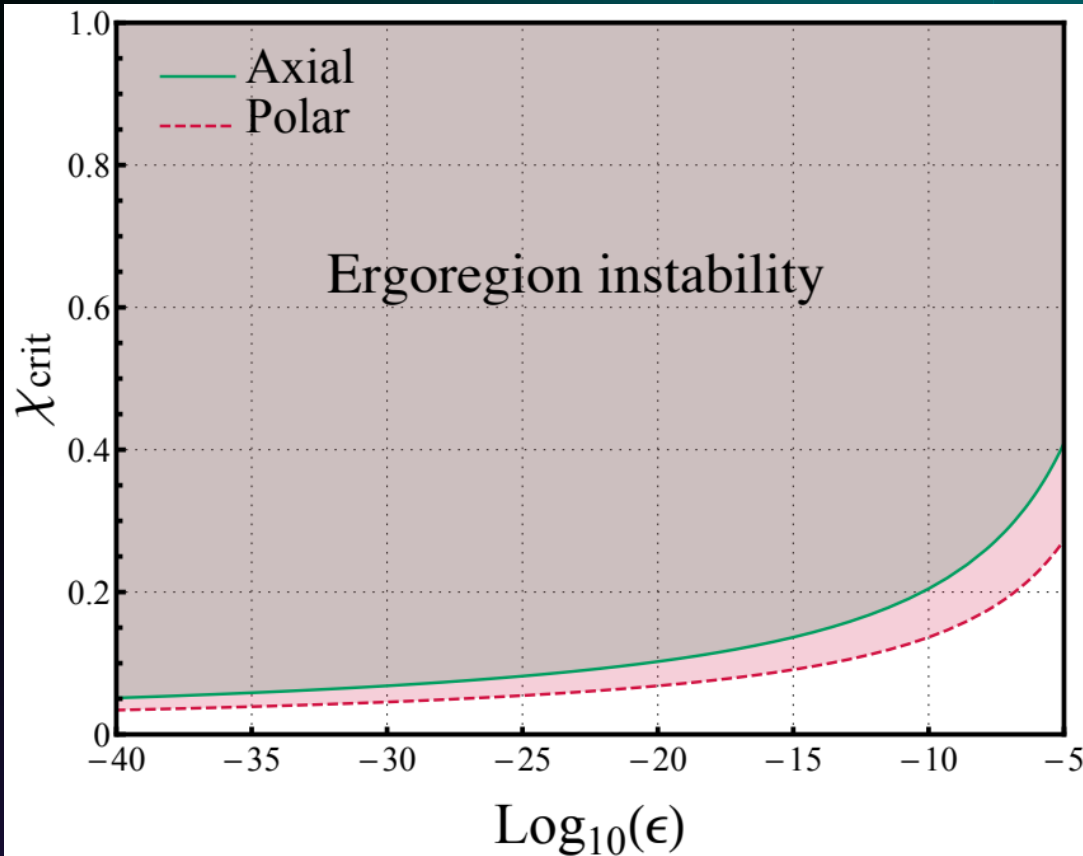


The imaginary frequency changes sign after a **critical spin**  $\chi_{crit}$ : presence **of unstable modes**

Here  $\varepsilon = 10^{-6}$  and  $|\mathcal{R}|^2 = 1$

*E. Maggio, P. Pani, G. Raposo, Springer (2021)*

# The ergoregion instability (2/2)



Behaviour of  $\chi_{crit}$  with the closeness parameter for a perfectly reflecting ECO  $|\mathcal{R}|^2 = 1$

Credit: E. Maggio, PhD Thesis, 2022

- ✓ For a **perfectly reflecting ECO** one can find the relation  $\chi_{crit}(\epsilon)$  by **imposing**  $\omega_R \simeq \omega_I \simeq 0$  :

$$\chi_{crit}(\epsilon) \propto \frac{1}{\log_{10} \epsilon}$$

- ✓ The spin **decays** till it reaches the **critical value**
- ✓ The **time of instability** is defined as:

$$\tau_{ins} \equiv \frac{1}{\omega_I} \in (5,7) \left( \frac{M}{10 M_{\odot}} \right) sec$$

Where the **lower (upper)** bounds are for **polar (axial)** GW perturbations.

# Gravitational-wave population inference

If **multiple GWs** from CBC events are **collected**, it's **crucial** to estimate **collective properties** of the **population** of compact objects.

Some of the **frequent questions** one tries to **answer** could be:

- How are distributed the masses/spins of the population of binary black holes/neutron stars? Are there peaks/gaps in the spectrum? Is it what we expect theoretically?
- Are there evidences of different classes of objects (our task)?
- Are we able to handle selection effects, namely the fact we are biased to measuring mainly the most luminous events?

The **framework** employed for these scopes is the **hierarchical Bayesian inference**.

# Hierarchical Bayesian inference (1/2)

## Main quantities

- GW single-event parameters:  $\theta$
- Number of sources for unit  $\theta$ :
- 

$$\frac{dN_s}{d\theta} = N_s \cdot p_{pop}(\theta|\lambda)$$

- Pop. Hyperparameters:  $\Lambda = \{N_s, \lambda\}$

$N_s$ : total number of mergers for a given time and volume  
 $\lambda$ : shape parameters

- $p_{pop}(\theta|\lambda)$ : fraction of the population with parameters  $\theta$ , given  $\lambda$ .

## Handling selection effects:

Fraction of detectable events with respect total ones:

$$\frac{N_s^\uparrow}{N_s} = \int d\theta p_{pop}(\theta|\lambda) p(\rho^\uparrow|\theta)$$

$p(\rho^\uparrow|\theta)$ : probability for a source with  $\theta$  to be over detection threshold (like SNR or FAR).

*I. Mandel, W. Farr, J. Gair, MNRAS 486 (2019)*  
*S. Vitale, D. Gerosa, W. Farr, S. Taylor, Springer (2021)*

# Hierarchical Bayesian inference (2/2)

## Further assumptions:

1.  $N_{tr}$  source events collected.
2. **Constant** source rate:  $\frac{dN_s}{dt} \simeq const$

## Final goal

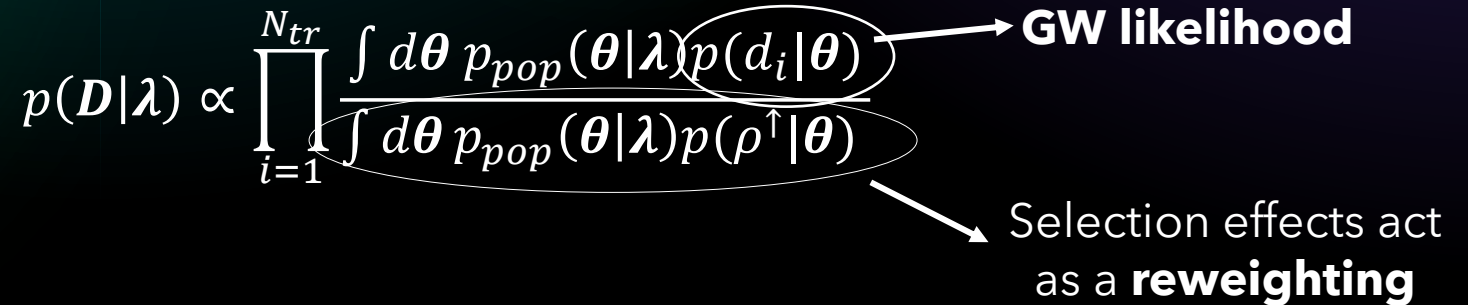
Find the posterior distribution on  $\Lambda$  given the set of detected sources  $\mathbf{D} = \{d_i\}_{i=1, \dots, N_{tr}}$ :

$$p(\boldsymbol{\lambda}|\mathbf{D}) \propto p(\mathbf{D}|\boldsymbol{\lambda})p(\boldsymbol{\lambda})$$

After **marginalizing** over  $N_s$ , assuming a  $1/N_s$  prior.

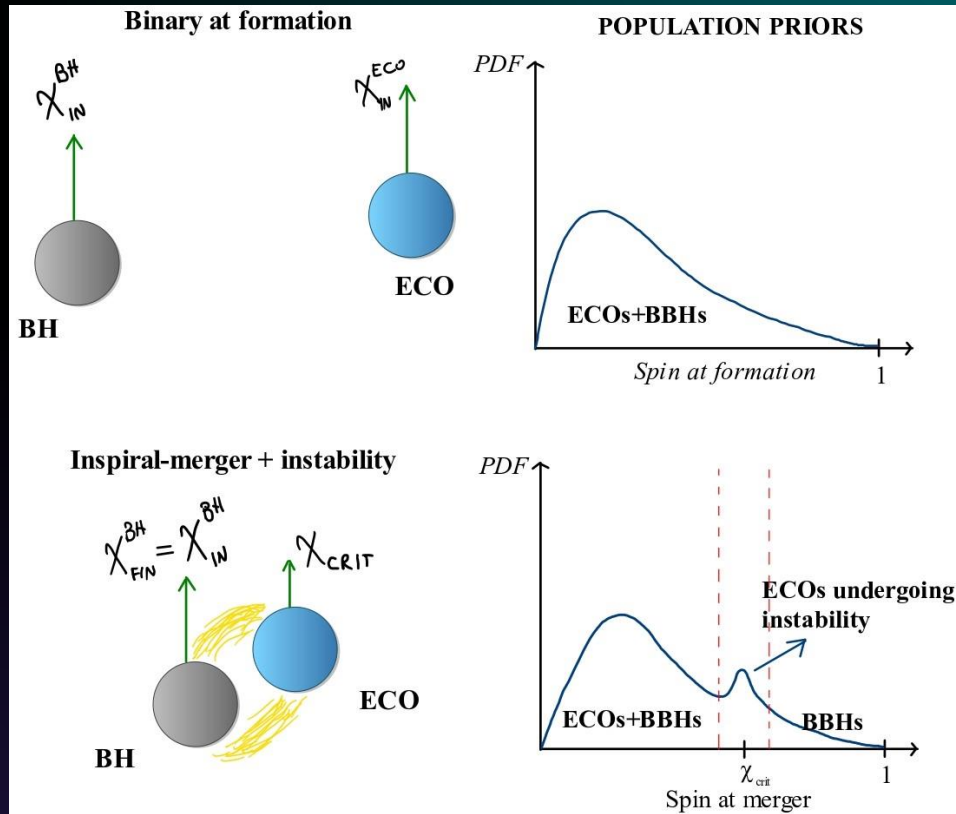
## Computing the hyperlikelihood:

$$p(\mathbf{D}|\boldsymbol{\lambda}) \propto \prod_{i=1}^{N_{tr}} \frac{\int d\boldsymbol{\theta} p_{pop}(\boldsymbol{\theta}|\boldsymbol{\lambda}) p(d_i|\boldsymbol{\theta})}{\int d\boldsymbol{\theta} p_{pop}(\boldsymbol{\theta}|\boldsymbol{\lambda}) p(\rho^\uparrow|\boldsymbol{\theta})}$$





# Spin population distribution employed



Since  $T(\text{inst}) \ll T(\text{inspiral})$ , we assume that an ECO would reach  $\chi_{crit}$  almost immediately after formation.

## SPINS AT FORMATION

**Beta distribution** for both ECOs and BBHs

## SPIN AT MERGER (THE ONES MEASURED)

- **Beta** with a **gaussian peak** on  $\chi_{crit}$  for **ECOs**
- **Unchanged** for **BHs** (again Beta)

$$p_{pop}^{tot}(\chi|\Lambda, f_{eco}) = f_{eco} p_{pop}^{ECO}(\chi|\Lambda) + (1 - f_{eco}) p_{pop}^{BBH}(\chi|\Lambda)$$

$$\left\{ \begin{array}{l} p_{pop}^{BBH}(\chi|\Lambda) = \beta(\chi|\alpha, \beta) \\ p_{pop}^{ECO}(\chi|\Lambda) = \lambda_{eco} \beta(\chi|\alpha, \beta) \Theta(\chi_{crit} - \chi) + (1 - \lambda_{eco}) \mathcal{N}(\chi|\chi_{crit}, \sigma) \end{array} \right.$$

$f_{eco}$ : fraction of ECOs included in the shape parameters  $\lambda$

# Simulations and main results

- ❖ Simulations carried out with **ICAROGW** (S. Mastrogiovanni *et al.* arXiv:2305.17973), a Python software for GW population inference.
- ❖ We performed **three** different simulations on O3 BBH events:
  1. Assuming a population of **100%** ECOs (BHs), namely  $f_{eco} = 1$  ( $f_{eco} = 0$ );
  2. Assuming **mixed** population,  $f_{eco}$  free parameter to infer.
- ❖ We computed the Bayes factor for the various combinations:

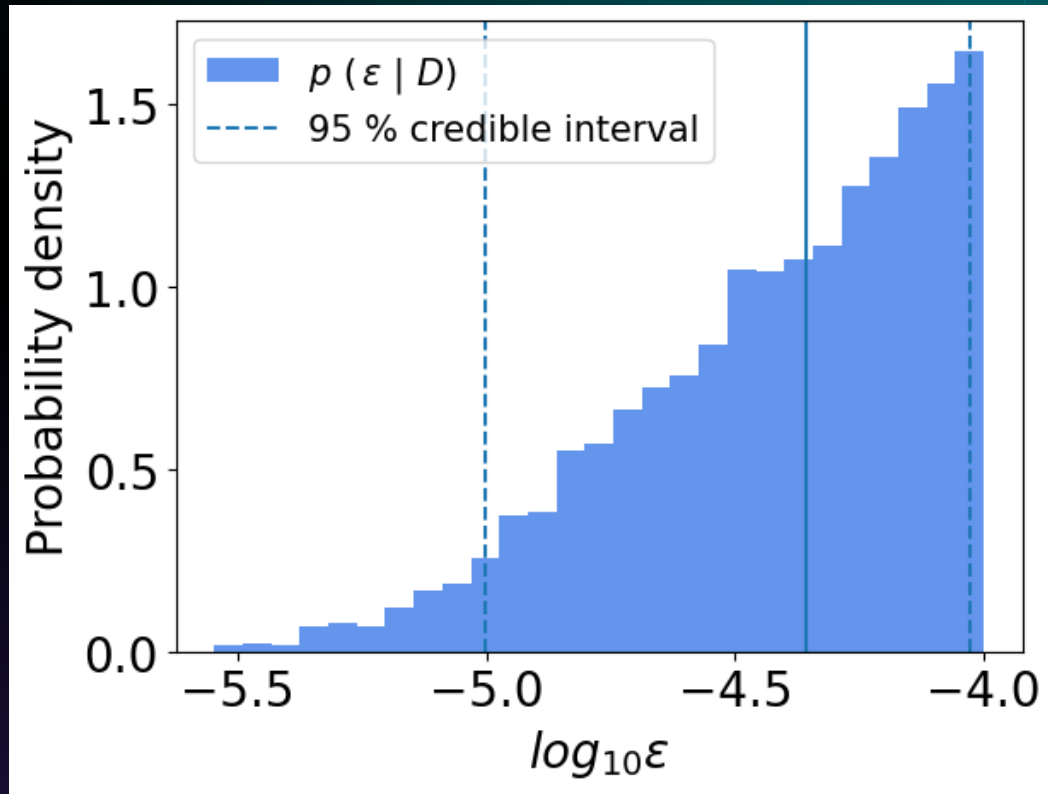
$$K = \frac{p(\mathbf{D}|i)}{p(\mathbf{D}|j)}, \quad \text{with } i, j \in (BBH, ECO, MIXTURE).$$

$$K(mix / BBH) = 3.8$$

$$K(mix / ECO) = 5.4$$

$$K(BBH / ECO) = 1.4$$

# Population of 100% ECOs



## PRIOR FOR $\epsilon$

Log-Uniform in  $[10^{-40}, 10^{-4}]$

## MAIN MESSAGE

- We can put a **lower limit** on  $\epsilon$  in the case of  $f_{eco} \equiv 1$ : this is  $\epsilon \simeq 10^{-5}$ .
- **Too low values would not explain** some **high-spin events** of the GWTC-3 catalog, if only ECOs are assumed.

Marginalized posterior for the closeness parameter  $\epsilon$ .

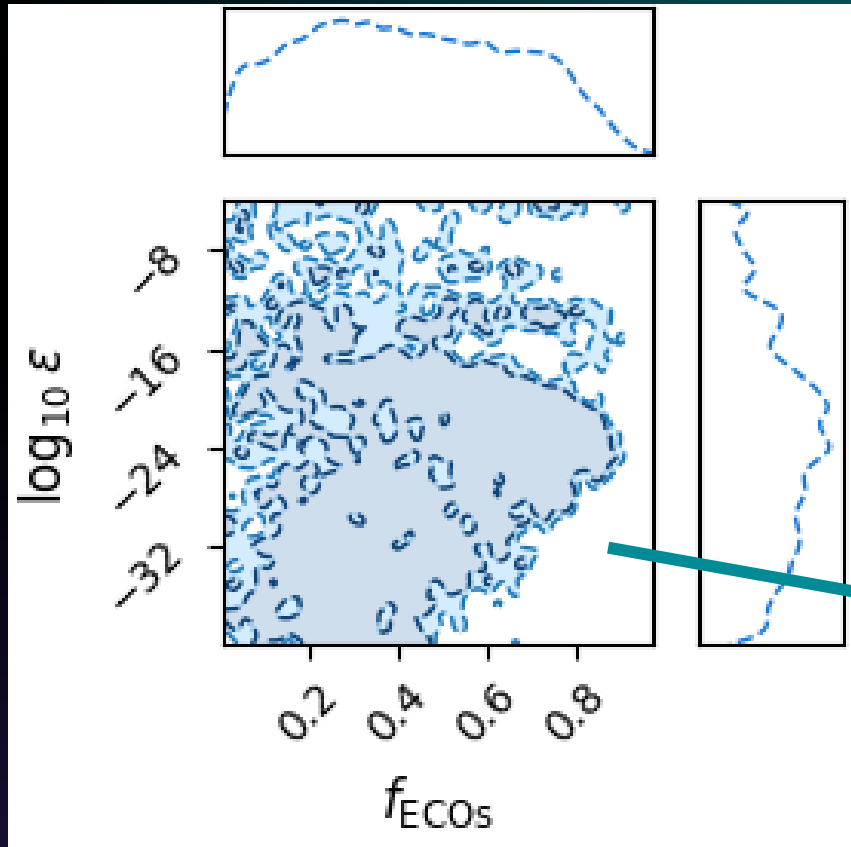
## An example of event of the catalog with high spin evidence

Event	$M$ ( $M_{\odot}$ )	$\mathcal{M}$ ( $M_{\odot}$ )	$m_1$ ( $M_{\odot}$ )	$m_2$ ( $M_{\odot}$ )	$\chi_{\text{eff}}$	$D_L$ (Gpc)	$z$	$M_f$ ( $M_{\odot}$ )	$\chi_f$	$\Delta\Omega$ (deg <sup>2</sup> )	SNR
GW190408_181802	43.0 <sup>+4.2</sup> <sub>-3.0</sub>	18.3 <sup>+1.9</sup> <sub>-1.2</sub>	24.6 <sup>+5.1</sup> <sub>-3.4</sub>	18.4 <sup>+3.3</sup> <sub>-3.6</sub>	-0.03 <sup>+0.14</sup> <sub>-0.19</sub>	1.55 <sup>+0.40</sup> <sub>-0.60</sub>	0.29 <sup>+0.06</sup> <sub>-0.10</sub>	41.1 <sup>+3.9</sup> <sub>-2.8</sub>	0.67 <sup>+0.06</sup> <sub>-0.07</sub>	150	15.3 <sup>+0.2</sup> <sub>-0.3</sub>
GW190412	38.4 <sup>+3.8</sup> <sub>-3.7</sub>	13.3 <sup>+0.4</sup> <sub>-0.3</sub>	30.1 <sup>+4.7</sup> <sub>-5.1</sub>	8.3 <sup>+1.6</sup> <sub>-0.9</sub>	0.25 <sup>+0.08</sup> <sub>-0.11</sub>	0.74 <sup>+0.14</sup> <sub>-0.17</sub>	0.15 <sup>+0.03</sup> <sub>-0.03</sub>	37.3 <sup>+3.9</sup> <sub>-3.8</sub>	0.67 <sup>+0.05</sup> <sub>-0.06</sub>	21	18.9 <sup>+0.2</sup> <sub>-0.3</sub>
GW190413_052954	58.6 <sup>+13.3</sup> <sub>-9.7</sub>	24.6 <sup>+5.5</sup> <sub>-4.1</sub>	34.7 <sup>+12.6</sup> <sub>-8.1</sub>	23.7 <sup>+7.3</sup> <sub>-6.7</sub>	-0.01 <sup>+0.29</sup> <sub>-0.34</sub>	3.55 <sup>+2.27</sup> <sub>-1.66</sub>	0.59 <sup>+0.29</sup> <sub>-0.24</sub>	56.0 <sup>+12.5</sup> <sub>-9.2</sub>	0.68 <sup>+0.12</sup> <sub>-0.13</sub>	1500	8.9 <sup>+0.4</sup> <sub>-0.7</sub>
GW190413_134308	78.8 <sup>+17.4</sup> <sub>-11.9</sub>	33.0 <sup>+8.2</sup> <sub>-5.4</sub>	47.5 <sup>+13.5</sup> <sub>-10.7</sub>	31.8 <sup>+11.7</sup> <sub>-10.8</sub>	-0.03 <sup>+0.25</sup> <sub>-0.29</sub>	4.45 <sup>+2.48</sup> <sub>-2.12</sub>	0.71 <sup>+0.31</sup> <sub>-0.30</sub>	75.5 <sup>+16.4</sup> <sub>-11.4</sub>	0.68 <sup>+0.10</sup> <sub>-0.12</sub>	730	10.0 <sup>+0.4</sup> <sub>-0.5</sub>
GW190421_213856	72.9 <sup>+13.4</sup> <sub>-9.2</sub>	31.2 <sup>+5.9</sup> <sub>-4.2</sub>	41.3 <sup>+10.4</sup> <sub>-6.9</sub>	31.9 <sup>+8.0</sup> <sub>-8.8</sub>	-0.06 <sup>+0.22</sup> <sub>-0.27</sub>	2.88 <sup>+1.37</sup> <sub>-1.38</sub>	0.49 <sup>+0.19</sup> <sub>-0.21</sub>	69.7 <sup>+12.5</sup> <sub>-8.7</sub>	0.67 <sup>+0.10</sup> <sub>-0.11</sub>	1200	10.7 <sup>+0.2</sup> <sub>-0.4</sub>
GW190424_180648	72.6 <sup>+13.3</sup> <sub>-10.7</sub>	31.0 <sup>+5.8</sup> <sub>-4.6</sub>	40.5 <sup>+11.1</sup> <sub>-7.3</sub>	31.8 <sup>+7.6</sup> <sub>-7.7</sub>	0.13 <sup>+0.22</sup> <sub>-0.22</sub>	2.20 <sup>+1.58</sup> <sub>-1.16</sub>	0.39 <sup>+0.23</sup> <sub>-0.19</sub>	68.9 <sup>+12.4</sup> <sub>-10.1</sub>	0.74 <sup>+0.09</sup> <sub>-0.09</sub>	28000	10.4 <sup>+0.2</sup> <sub>-0.4</sub>
GW190425	3.4 <sup>+0.3</sup> <sub>-0.1</sub>	1.44 <sup>+0.02</sup> <sub>-0.02</sub>	2.0 <sup>+0.6</sup> <sub>-0.3</sub>	1.4 <sup>+0.3</sup> <sub>-0.3</sub>	0.06 <sup>+0.11</sup> <sub>-0.05</sub>	0.16 <sup>+0.07</sup> <sub>-0.07</sub>	0.03 <sup>+0.01</sup> <sub>-0.02</sub>	-	-	10000	12.4 <sup>+0.3</sup> <sub>-0.4</sub>
GW190426_152155	7.2 <sup>+3.5</sup> <sub>-1.5</sub>	2.41 <sup>+0.08</sup> <sub>-0.08</sub>	5.7 <sup>+3.9</sup> <sub>-2.3</sub>	1.5 <sup>+0.8</sup> <sub>-0.5</sub>	-0.03 <sup>+0.32</sup> <sub>-0.30</sub>	0.37 <sup>+0.18</sup> <sub>-0.16</sub>	0.08 <sup>+0.04</sup> <sub>-0.03</sub>	-	-	1300	8.7 <sup>+0.5</sup> <sub>-0.6</sub>
GW190503_185404	71.7 <sup>+9.4</sup> <sub>-8.3</sub>	30.2 <sup>+4.2</sup> <sub>-4.2</sub>	43.3 <sup>+9.2</sup> <sub>-8.1</sub>	28.4 <sup>+7.7</sup> <sub>-8.0</sub>	-0.03 <sup>+0.20</sup> <sub>-0.26</sub>	1.45 <sup>+0.69</sup> <sub>-0.63</sub>	0.27 <sup>+0.11</sup> <sub>-0.11</sub>	68.6 <sup>+8.8</sup> <sub>-7.7</sub>	0.66 <sup>+0.09</sup> <sub>-0.12</sub>	94	12.4 <sup>+0.2</sup> <sub>-0.3</sub>
GW190512_180714	35.9 <sup>+3.8</sup> <sub>-3.5</sub>	14.6 <sup>+1.3</sup> <sub>-1.0</sub>	23.3 <sup>+5.3</sup> <sub>-5.8</sub>	12.6 <sup>+3.6</sup> <sub>-2.5</sub>	0.03 <sup>+0.12</sup> <sub>-0.13</sub>	1.43 <sup>+0.55</sup> <sub>-0.55</sub>	0.27 <sup>+0.09</sup> <sub>-0.10</sub>	34.5 <sup>+3.8</sup> <sub>-3.5</sub>	0.65 <sup>+0.07</sup> <sub>-0.07</sub>	220	12.2 <sup>+0.2</sup> <sub>-0.4</sub>
GW190513_205428	53.9 <sup>+8.6</sup> <sub>-5.9</sub>	21.6 <sup>+3.8</sup> <sub>-1.9</sub>	35.7 <sup>+9.5</sup> <sub>-9.2</sub>	18.0 <sup>+7.7</sup> <sub>-4.1</sub>	0.11 <sup>+0.28</sup> <sub>-0.17</sub>	2.06 <sup>+0.88</sup> <sub>-0.80</sub>	0.37 <sup>+0.13</sup> <sub>-0.13</sub>	51.6 <sup>+8.2</sup> <sub>-5.8</sub>	0.68 <sup>+0.14</sup> <sub>-0.12</sub>	520	12.9 <sup>+0.3</sup> <sub>-0.4</sub>
GW190514_065416	67.2 <sup>+18.7</sup> <sub>-10.8</sub>	28.5 <sup>+7.9</sup> <sub>-4.8</sub>	39.0 <sup>+14.7</sup> <sub>-8.2</sub>	28.4 <sup>+9.3</sup> <sub>-8.8</sub>	-0.19 <sup>+0.29</sup> <sub>-0.32</sub>	4.13 <sup>+2.65</sup> <sub>-2.17</sub>	0.67 <sup>+0.33</sup> <sub>-0.31</sub>	64.5 <sup>+17.9</sup> <sub>-10.4</sub>	0.63 <sup>+0.11</sup> <sub>-0.15</sub>	3000	8.2 <sup>+0.3</sup> <sub>-0.6</sub>
GW190517_055101	63.5 <sup>+9.6</sup> <sub>-9.6</sub>	26.6 <sup>+4.0</sup> <sub>-4.0</sub>	37.4 <sup>+11.7</sup> <sub>-7.6</sub>	25.3 <sup>+7.0</sup> <sub>-7.3</sub>	0.52 <sup>+0.19</sup> <sub>-0.19</sub>	1.86 <sup>+1.62</sup> <sub>-0.84</sub>	0.34 <sup>+0.24</sup> <sub>-0.24</sub>	59.3 <sup>+9.1</sup> <sub>-8.9</sub>	0.87 <sup>+0.05</sup> <sub>-0.07</sub>	470	10.7 <sup>+0.4</sup> <sub>-0.6</sub>
GW190519_153544	106.6 <sup>+13.5</sup> <sub>-14.8</sub>	44.5 <sup>+6.4</sup> <sub>-7.1</sub>	66.0 <sup>+10.7</sup> <sub>-12.0</sub>	40.5 <sup>+11.0</sup> <sub>-11.1</sub>	0.31 <sup>+0.20</sup> <sub>-0.22</sub>	2.53 <sup>+1.83</sup> <sub>-0.92</sub>	0.44 <sup>+0.25</sup> <sub>-0.14</sub>	101.0 <sup>+12.4</sup> <sub>-13.8</sub>	0.79 <sup>+0.07</sup> <sub>-0.13</sub>	860	15.6 <sup>+0.2</sup> <sub>-0.3</sub>
GW190521	163.9 <sup>+39.2</sup> <sub>-23.5</sub>	69.2 <sup>+17.0</sup> <sub>-10.6</sub>	95.3 <sup>+28.7</sup> <sub>-18.9</sub>	69.0 <sup>+22.7</sup> <sub>-23.1</sub>	0.03 <sup>+0.32</sup> <sub>-0.39</sub>	3.92 <sup>+2.19</sup> <sub>-1.95</sub>	0.64 <sup>+0.28</sup> <sub>-0.28</sub>	156.3 <sup>+36.8</sup> <sub>-22.4</sub>	0.71 <sup>+0.12</sup> <sub>-0.16</sub>	1000	14.2 <sup>+0.3</sup> <sub>-0.3</sub>
GW190521_074359	74.7 <sup>+7.0</sup> <sub>-4.8</sub>	32.1 <sup>+3.2</sup> <sub>-2.5</sub>	42.2 <sup>+5.9</sup> <sub>-4.8</sub>	32.8 <sup>+5.4</sup> <sub>-6.4</sub>	0.09 <sup>+0.10</sup> <sub>-0.13</sub>	1.24 <sup>+0.40</sup> <sub>-0.57</sub>	0.24 <sup>+0.07</sup> <sub>-0.10</sub>	71.0 <sup>+6.5</sup> <sub>-4.4</sub>	0.72 <sup>+0.05</sup> <sub>-0.07</sub>	550	25.8 <sup>+0.1</sup> <sub>-0.2</sub>
GW190527_092055	59.1 <sup>+21.3</sup> <sub>-9.8</sub>	24.3 <sup>+9.1</sup> <sub>-4.2</sub>	36.5 <sup>+16.4</sup> <sub>-9.0</sub>	22.6 <sup>+10.5</sup> <sub>-8.1</sub>	0.11 <sup>+0.28</sup> <sub>-0.28</sub>	2.49 <sup>+2.48</sup> <sub>-1.24</sub>	0.44 <sup>+0.34</sup> <sub>-0.20</sub>	56.4 <sup>+20.2</sup> <sub>-9.3</sub>	0.71 <sup>+0.12</sup> <sub>-0.16</sub>	3700	8.1 <sup>+0.3</sup> <sub>-0.9</sub>
GW190602_175927	116.3 <sup>+19.0</sup> <sub>-15.6</sub>	49.1 <sup>+9.1</sup> <sub>-8.5</sub>	69.1 <sup>+15.7</sup> <sub>-13.0</sub>	47.8 <sup>+14.3</sup> <sub>-17.4</sub>	0.07 <sup>+0.25</sup> <sub>-0.24</sub>	2.69 <sup>+1.79</sup> <sub>-1.12</sub>	0.47 <sup>+0.25</sup> <sub>-0.17</sub>	110.9 <sup>+17.7</sup> <sub>-14.9</sub>	0.70 <sup>+0.10</sup> <sub>-0.14</sub>	690	12.8 <sup>+0.2</sup> <sub>-0.3</sub>
GW190620_030421	92.1 <sup>+18.5</sup> <sub>-13.1</sub>	38.3 <sup>+8.3</sup> <sub>-6.5</sub>	57.1 <sup>+16.0</sup> <sub>-12.7</sub>	35.5 <sup>+12.2</sup> <sub>-12.3</sub>	0.33 <sup>+0.22</sup> <sub>-0.25</sub>	2.81 <sup>+1.68</sup> <sub>-1.31</sub>	0.49 <sup>+0.23</sup> <sub>-0.20</sub>	87.2 <sup>+16.8</sup> <sub>-12.1</sub>	0.79 <sup>+0.08</sup> <sub>-0.15</sub>	7200	12.1 <sup>+0.3</sup> <sub>-0.4</sub>
GW190630_185205	59.1 <sup>+4.6</sup> <sub>-4.8</sub>	24.9 <sup>+2.1</sup> <sub>-2.1</sub>	35.1 <sup>+6.9</sup> <sub>-5.6</sub>	23.7 <sup>+5.2</sup> <sub>-5.1</sub>	0.10 <sup>+0.12</sup> <sub>-0.13</sub>	0.89 <sup>+0.56</sup> <sub>-0.37</sub>	0.18 <sup>+0.10</sup> <sub>-0.07</sub>	56.4 <sup>+4.4</sup> <sub>-4.6</sub>	0.70 <sup>+0.05</sup> <sub>-0.07</sub>	1200	15.6 <sup>+0.2</sup> <sub>-0.3</sub>
GW190701_203306	94.3 <sup>+12.1</sup> <sub>-9.5</sub>	40.3 <sup>+5.4</sup> <sub>-4.9</sub>	53.9 <sup>+11.8</sup> <sub>-8.0</sub>	40.8 <sup>+8.7</sup> <sub>-12.0</sub>	-0.07 <sup>+0.23</sup> <sub>-0.29</sub>	2.06 <sup>+0.76</sup> <sub>-0.73</sub>	0.37 <sup>+0.11</sup> <sub>-0.12</sub>	90.2 <sup>+11.3</sup> <sub>-8.9</sub>	0.66 <sup>+0.09</sup> <sub>-0.13</sub>	46	11.3 <sup>+0.2</sup> <sub>-0.3</sub>
GW190706_222641	104.1 <sup>+20.2</sup> <sub>-13.9</sub>	42.7 <sup>+10.0</sup> <sub>-7.0</sub>	67.0 <sup>+14.6</sup> <sub>-16.2</sub>	38.2 <sup>+13.6</sup> <sub>-13.3</sub>	0.28 <sup>+0.26</sup> <sub>-0.29</sub>	4.42 <sup>+2.59</sup> <sub>-1.93</sub>	0.71 <sup>+0.32</sup> <sub>-0.27</sub>	99.0 <sup>+18.3</sup> <sub>-13.5</sub>	0.78 <sup>+0.09</sup> <sub>-0.18</sub>	650	12.6 <sup>+0.2</sup> <sub>-0.4</sub>
GW190707_093326	20.1 <sup>+1.9</sup> <sub>-1.3</sub>	8.5 <sup>+0.6</sup> <sub>-0.5</sub>	11.6 <sup>+3.3</sup> <sub>-1.7</sub>	8.4 <sup>+1.4</sup> <sub>-1.7</sub>	-0.05 <sup>+0.10</sup> <sub>-0.08</sub>	0.77 <sup>+0.38</sup> <sub>-0.37</sub>	0.16 <sup>+0.07</sup> <sub>-0.07</sub>	19.2 <sup>+1.9</sup> <sub>-1.3</sub>	0.66 <sup>+0.03</sup> <sub>-0.04</sub>	1300	13.3 <sup>+0.2</sup> <sub>-0.4</sub>
GW190708_232457	30.9 <sup>+2.5</sup> <sub>-1.8</sub>	13.2 <sup>+0.9</sup> <sub>-0.6</sub>	17.6 <sup>+4.7</sup> <sub>-2.3</sub>	13.2 <sup>+2.0</sup> <sub>-2.7</sub>	0.02 <sup>+0.10</sup> <sub>-0.08</sub>	0.88 <sup>+0.33</sup> <sub>-0.39</sub>	0.18 <sup>+0.06</sup> <sub>-0.07</sub>	29.5 <sup>+2.5</sup> <sub>-1.8</sub>	0.69 <sup>+0.04</sup> <sub>-0.04</sub>	14000	13.1 <sup>+0.2</sup> <sub>-0.3</sub>

CREDIT

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# Mixture model



Marginalized bidimensional posterior for the closeness parameter  $\epsilon$  and the fraction of ECOs, for a mixed population

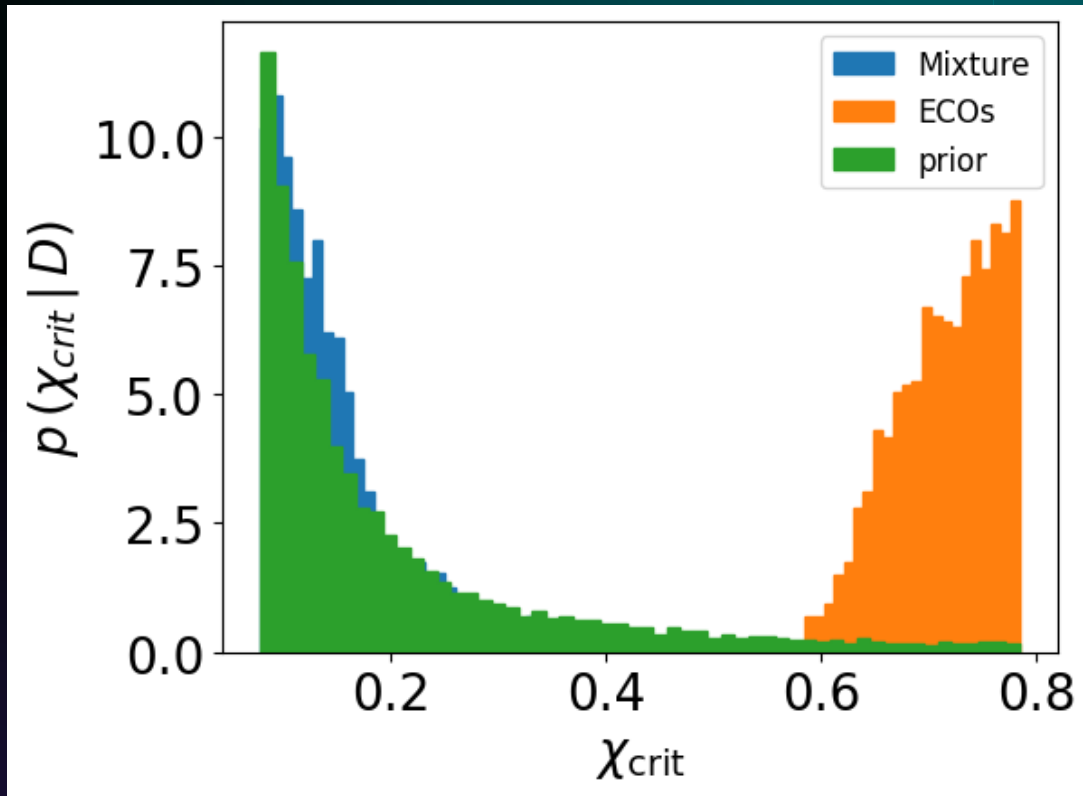
## GOAL

- We keep  $f_{eco}$  as a free parameter to infer to.
- Which **constraints** can we put on  $f_{eco}$  and  $\epsilon$  ?

We can **exclude** the **region** of **high-fraction, ultra-compact** ECOs ( $f_{eco} \simeq 1, \epsilon \ll 1$ ):

Particularly, no **more** than 60% of objects can be ECOs in the **ultra-compact region** ( $\epsilon < 10^{-30}$ )

# Implied distribution on $\chi_{crit}$



- **ONLY ECOs: shifted toward higher** values, recover high spin events
- **MIXTURE: dominated** by **prior** on  $\epsilon$ . High-spin events are handled by the possibility of being a BH.

Posterior distribution mapped on  $\chi_{crit}(\epsilon)$  for the two models, compared with the prior, that reflects the log-uniform prior on  $\epsilon$ .

# Probability of being a certain object (1/2)

- **Suppose** we have a new astrophysical event: what is the probability that this is an ECO (BBH)?
- What we know? The previous events with which we computed the posterior on population parameters
- We basically want to compute the following:

$$P(ECO|\mathbf{D}, d) = \int P(\boldsymbol{\lambda}|\mathbf{D}) \left[ \int P(ECO|\boldsymbol{\chi}, \boldsymbol{\lambda}) P(\boldsymbol{\chi}|d, \boldsymbol{\lambda}) d\boldsymbol{\chi} \right] d\boldsymbol{\lambda}$$

$\left\{ \begin{array}{l} \mathbf{D}: \text{all the previous data containing CBC events, used to compute the hyperposterior on } \boldsymbol{\lambda} \\ d: \text{data containing the new event} \end{array} \right.$

**We compute it for all the events of the catalog used for the analysis**

# Probability of being a certain object (2/2)

## Probability of being an ECO for each of the two objects of the O3 binaries

Event ID	$p_1(\text{ECO} D, d)$	$p_2(\text{ECO} D, d)$			
			GW191105_143521	$0.44^{+0.52}_{-0.42}$	$0.42^{+0.51}_{-0.40}$
GW190408_181802	$0.41^{+0.51}_{-0.40}$	$0.40^{+0.51}_{-0.39}$	GW191109_010717	$0.16^{+0.21}_{-0.16}$	$0.30^{+0.37}_{-0.29}$
GW190412	$0.25^{+0.43}_{-0.24}$	$0.32^{+0.41}_{-0.31}$	GW191127_050227	$0.29^{+0.37}_{-0.29}$	$0.36^{+0.43}_{-0.35}$
GW190413_134308	$0.35^{+0.43}_{-0.34}$	$0.39^{+0.47}_{-0.38}$	GW191129_134029	$0.43^{+0.52}_{-0.42}$	$0.42^{+0.50}_{-0.40}$
GW190421_213856	$0.38^{+0.48}_{-0.37}$	$0.39^{+0.47}_{-0.38}$	GW191204_171526	$0.36^{+0.51}_{-0.35}$	$0.36^{+0.47}_{-0.36}$
GW190503_185404	$0.39^{+0.50}_{-0.38}$	$0.39^{+0.46}_{-0.38}$	GW191204_171526	$0.36^{+0.51}_{-0.35}$	$0.36^{+0.47}_{-0.36}$
GW190512_180714	$0.44^{+0.52}_{-0.43}$	$0.40^{+0.51}_{-0.39}$	GW191215_223052	$0.38^{+0.48}_{-0.37}$	$0.40^{+0.48}_{-0.39}$
GW190513_205428	$0.41^{+0.50}_{-0.39}$	$0.38^{+0.47}_{-0.37}$	GW191216_213338	$0.43^{+0.54}_{-0.42}$	$0.42^{+0.51}_{-0.40}$
GW190517_055101	$0.02^{+0.03}_{-0.02}$	$0.33^{+0.42}_{-0.32}$	GW191222_033537	$0.41^{+0.50}_{-0.39}$	$0.40^{+0.49}_{-0.39}$
GW190519_153544	$0.23^{+0.29}_{-0.22}$	$0.32^{+0.39}_{-0.31}$	GW191230_180458	$0.39^{+0.46}_{-0.38}$	$0.37^{+0.47}_{-0.36}$
GW190521	$0.28^{+0.37}_{-0.28}$	$0.34^{+0.42}_{-0.33}$	GW200112_155838	$0.41^{+0.51}_{-0.40}$	$0.41^{+0.49}_{-0.40}$
GW190521_074359	$0.40^{+0.50}_{-0.39}$	$0.37^{+0.48}_{-0.36}$	GW200128_022011	$0.34^{+0.43}_{-0.33}$	$0.37^{+0.46}_{-0.36}$
GW190527_092055	$0.37^{+0.48}_{-0.36}$	$0.38^{+0.46}_{-0.37}$	GW200129_065458	$0.36^{+0.48}_{-0.36}$	$0.38^{+0.49}_{-0.37}$
GW190602_175927	$0.39^{+0.49}_{-0.38}$	$0.37^{+0.45}_{-0.36}$	GW200202_154313	$0.44^{+0.52}_{-0.43}$	$0.41^{+0.51}_{-0.40}$

The two probabilities  $p_1$  and  $p_2$  are referred to the two objects of the binary. The **high-spin events** of the catalog **can be recognized as black holes** (at least the primary object). The **heaviest** object of GW190517\_055101 is  $\sim 100\%$  a black hole.



# Conclusions

- If **all** the compact objects are **ECOs**, epsilon **cannot be** lower than  $10^{-5}$  at 95% credible interval. We **exclude** a population of ultra-compact exotic objects;
- If **mixed population**: no more than 60% of ECOs can be present if  $\varepsilon < 10^{-30}$  (namely ultra-compact objects);
- The **heaviest object of the GW190517\_055101** binary is  $\sim 100\%$  a BH with all the models we tried.

# What's next?

- Employ a **reflectivity-dependent** model.
- Analyse **simulated signals** from a mixed population, and study future **forecast**.
- **FOLLOW-UP PROJECT**: Check the presence of biases due to potential difference among BBH and ECO waveforms.

# Thanks for the attention !

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**Pisa**

