



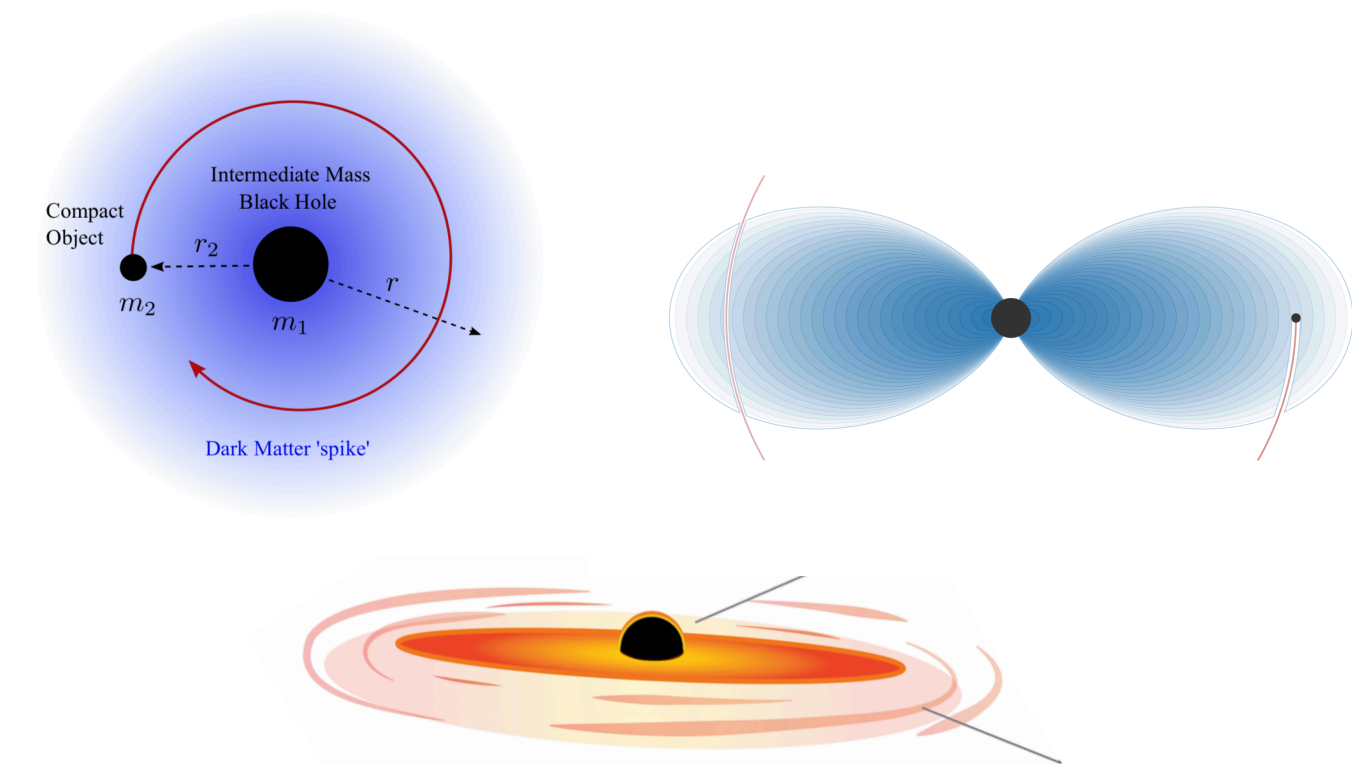
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# Searching for dark matter with gravitational waves

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Postdoc at University of Milano-Bicocca

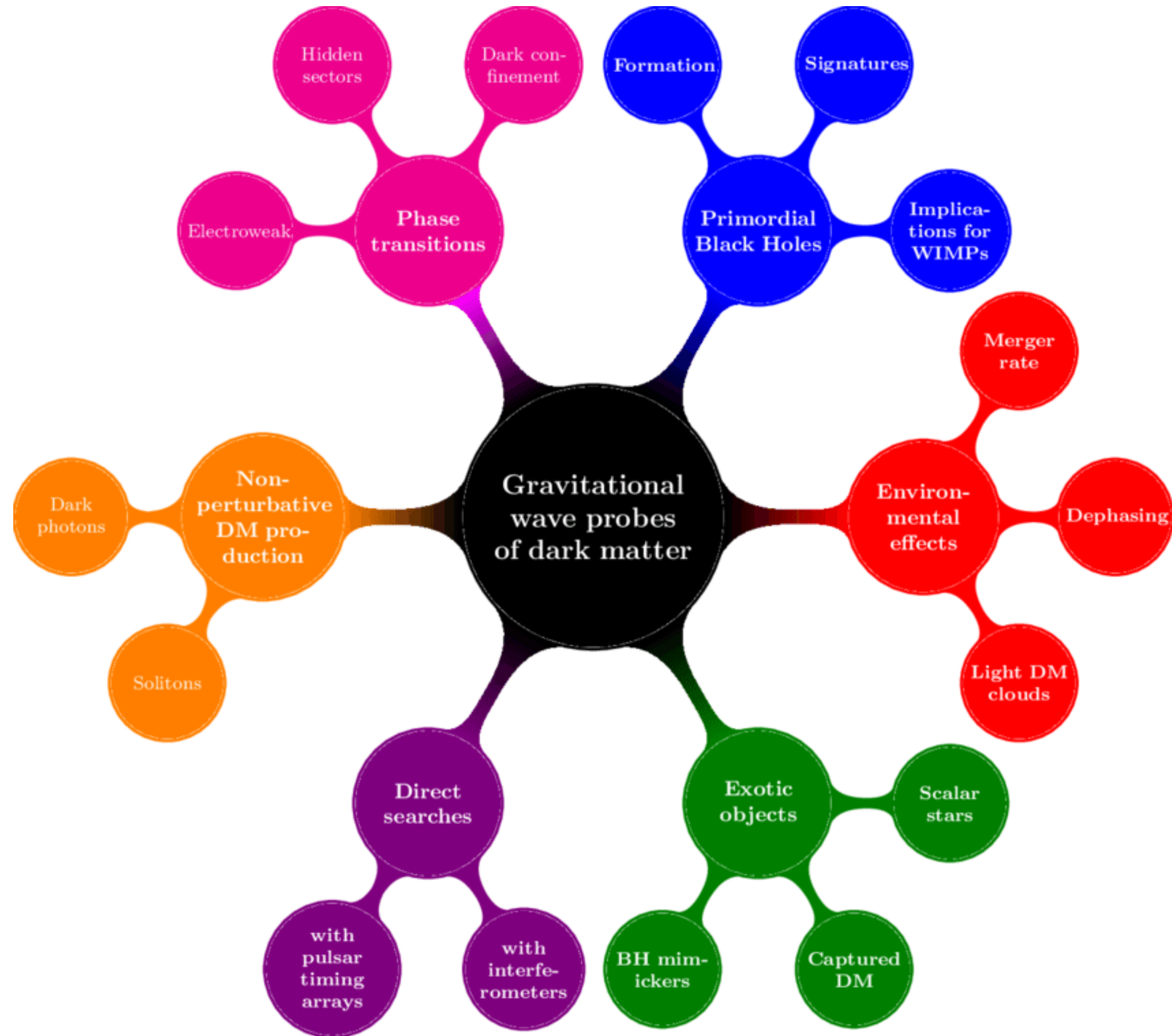
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with James Alvey, Gianfranco Bertone, Uddipta Bhardwaj, Adam Coogan, Daniele Gaggero, Bradley Kavanagh, Theophanes Karydas, Thomas Spiexsma and Giovanni Maria Tomaselli

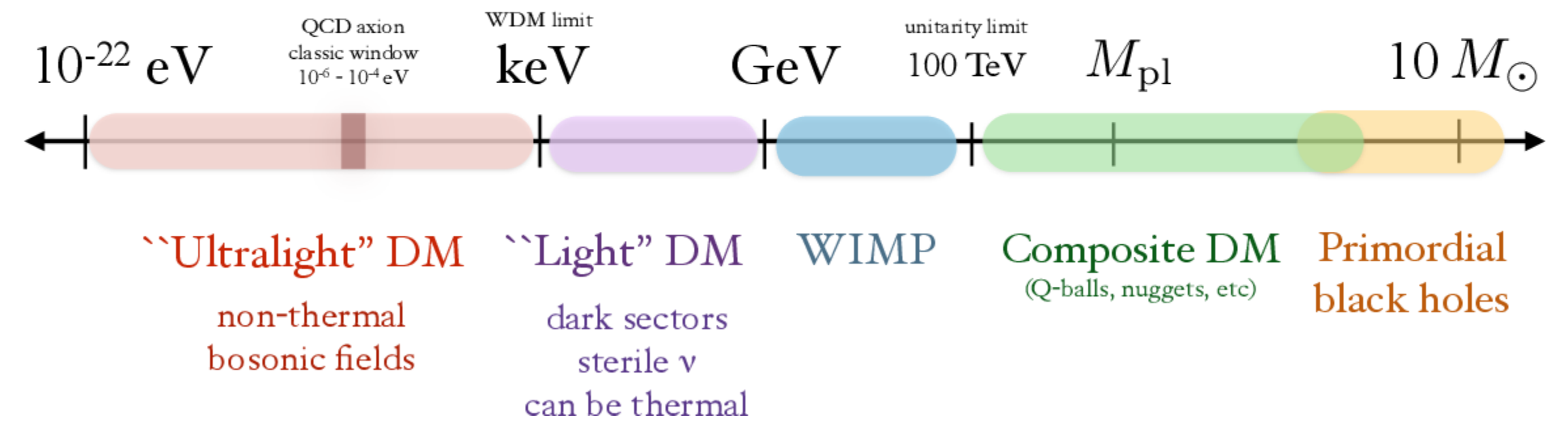
Based on Cole, P.S., Bertone, G., Coogan, A. *et al.* Distinguishing environmental effects on binary black hole gravitational waveforms, *Nature Astron.* 7 (2023) 8, 943-950 <https://doi.org/10.1038/s41550-023-01990-2>

# Wide mass range = wide range of probes



Bertone et al. 2020

## Mass scale of dark matter (not to scale)

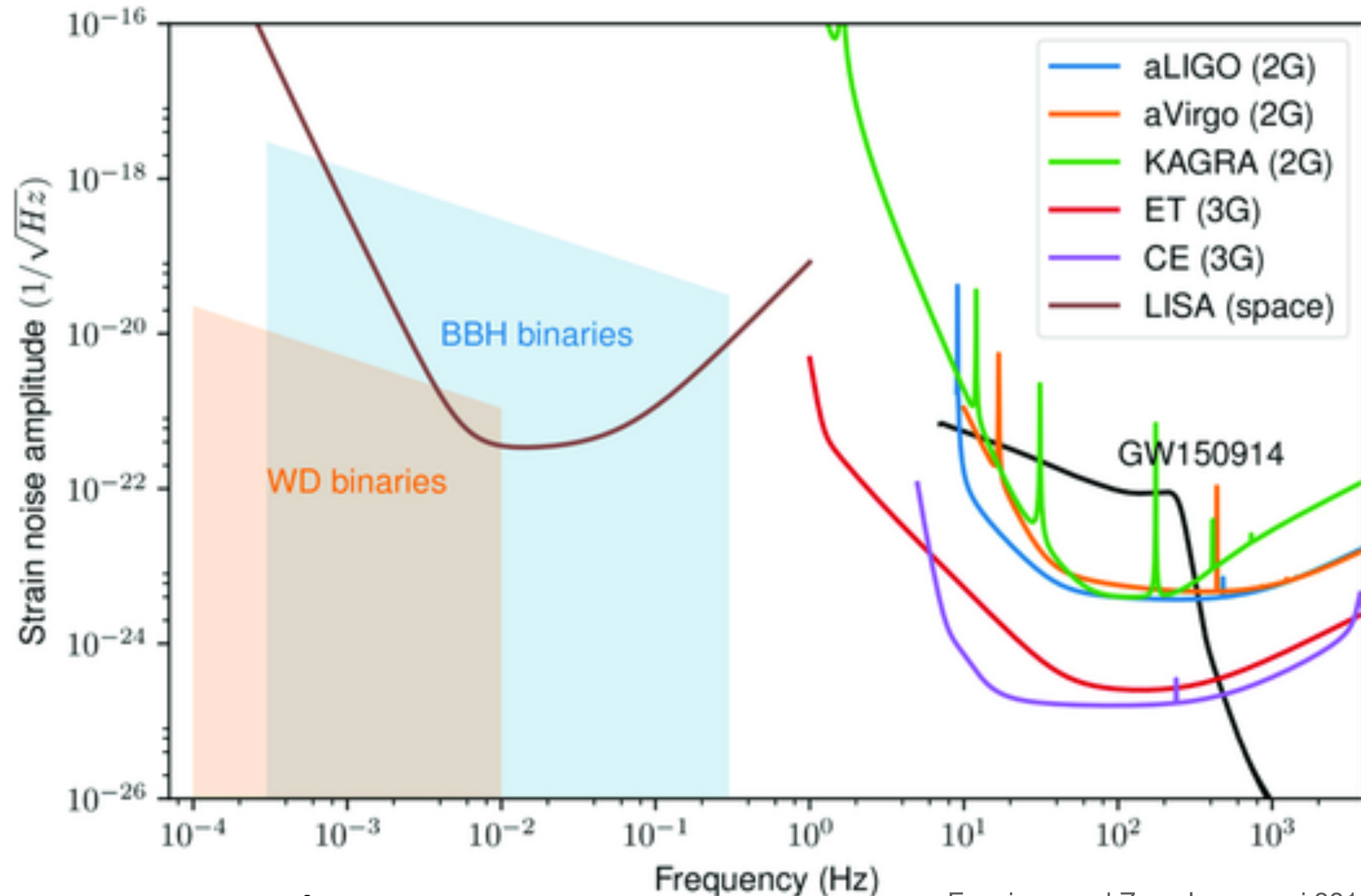


Lin 2019

# Vacuum or non-vacuum

Higher frequencies  
= smaller masses

- So far, all LIGO/Virgo/KAGRA binary black hole mergers have been detected and measured assuming that they occurred in vacuum
- OK for short duration signals (seconds - minutes for current detectors), but looking towards future interferometers, long duration signals may be affected by their environment

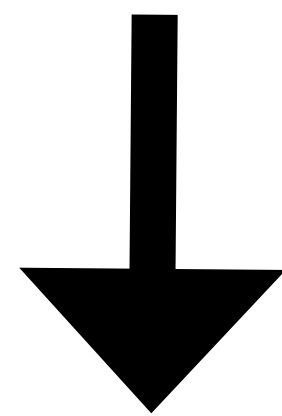


# Environmental effects

- Cause inspiral of black hole binary to either speed up or slow down with respect to vacuum case
- A dephasing accumulates, which alters the gravitational waveform from the binary's inspiral

Change in separation of the binary

$$\dot{r} = \dot{r}_{\text{GW}} + \dot{r}_{\text{env}}$$

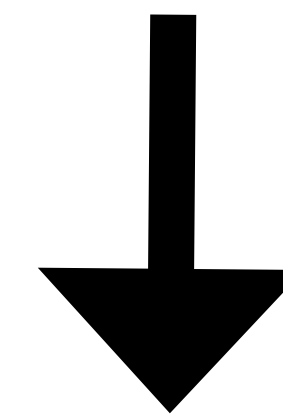


$$f(t) = \frac{1}{\pi} \sqrt{\frac{GM}{r(t)^3}}$$

Frequency evolution

Phase evolution

$$\Phi(f) = \int_f^{f_{\text{ISCO}}} \frac{dt}{df'} f' df'$$



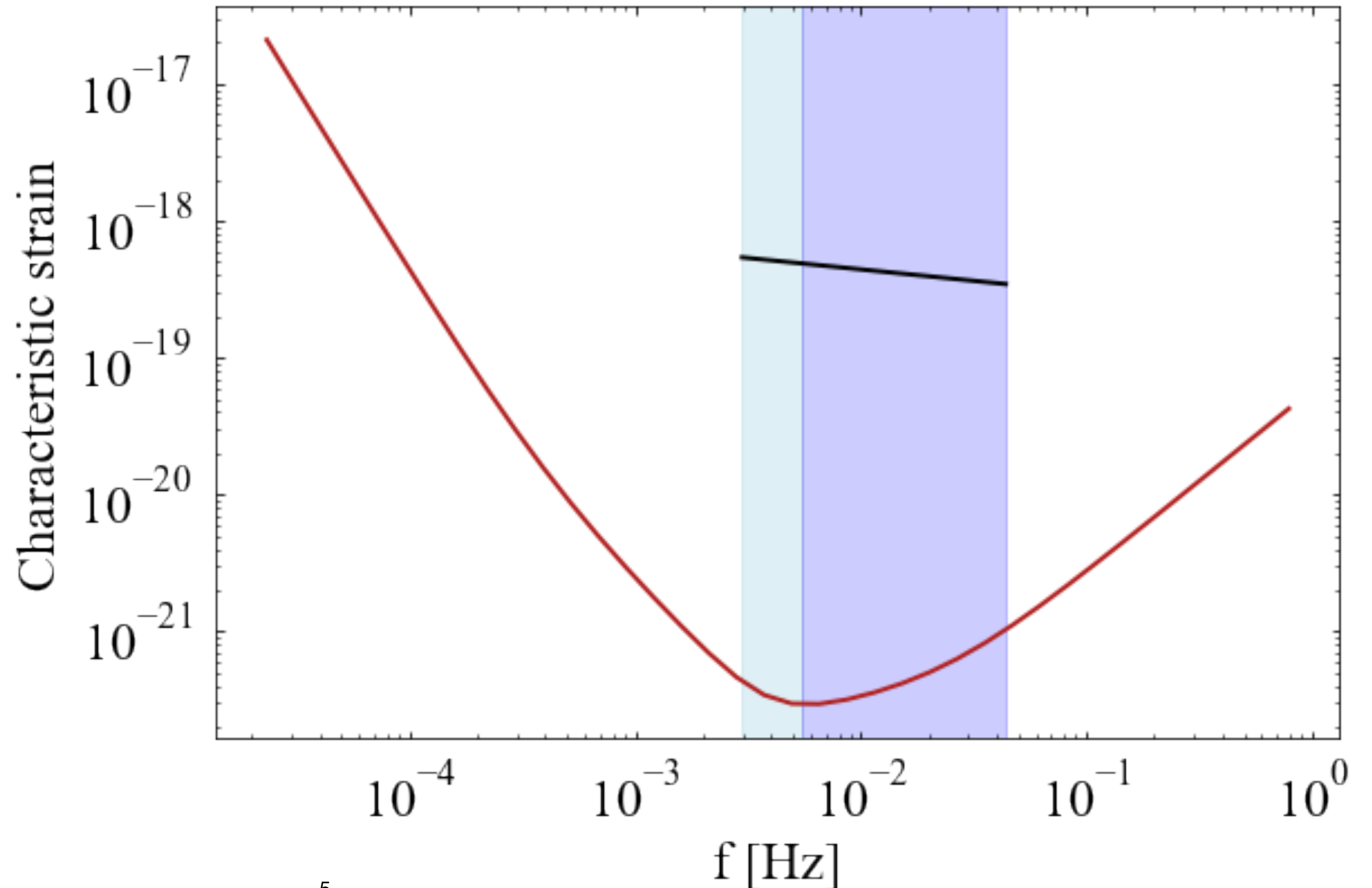
$$h_0(f) = \frac{1}{2} \frac{4\pi^{2/3} G_N^{5/3} \mathcal{M}^{5/3} f^{2/3}}{c^4} \sqrt{\frac{2\pi}{\ddot{\Phi}}}$$

Gravitational wave amplitude

# Extreme mass ratios

$$m_1 = 10^5 M_\odot, \quad m_2 = 10 M_\odot$$

- dephasing accumulates over thousands or millions of cycles
- small mass ratio  $q = \frac{m_2}{m_1} < 10^{-2.5}$  so that environment survives
- systems possible sources for LISA and Einstein Telescope/Cosmic Explorer

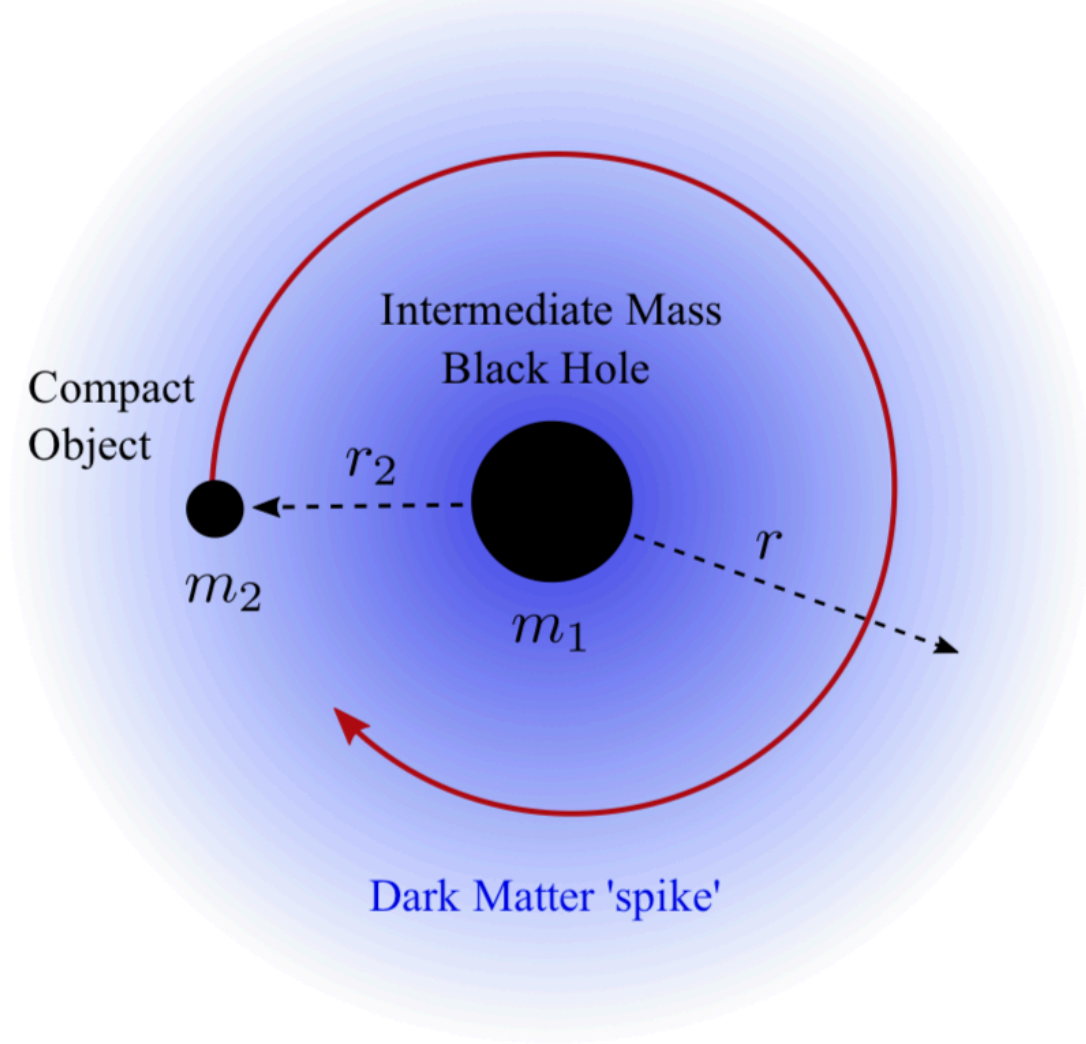


# Why should we care about environmental effects?

- We have a chance to learn about the environment itself (which could involve dark matter) via the dephasing in the waveform.
- If we search the data with the wrong ‘template’ we might miss the signal
- If we do parameter estimation with the ‘wrong’ parameters, we might come up with biased results

# Dark dress

Cold, collisionless dark matter

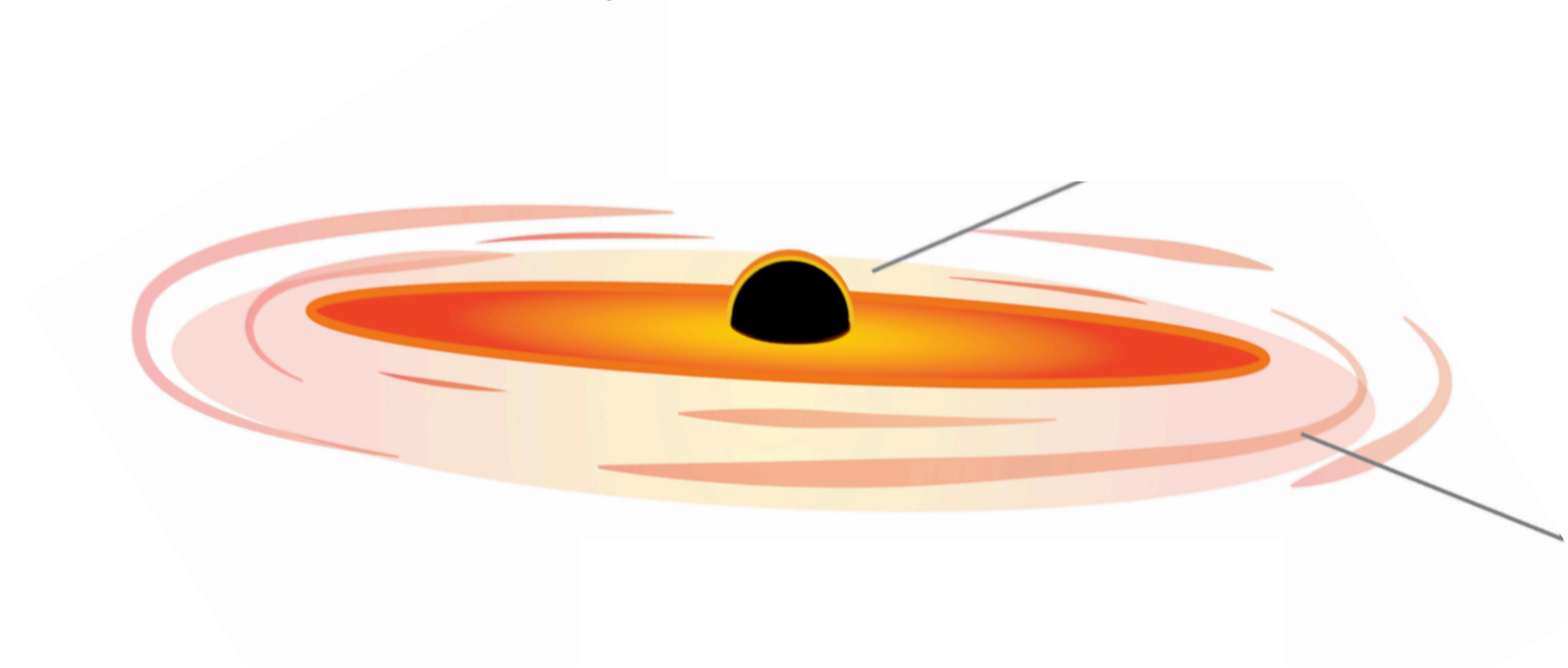


$$\rho(r) = \rho_6 \left( \frac{r_6}{r} \right)^{\gamma_s}$$

Eda et al. 2013, 2014  
Gondolo, Silk 1999  
Kavanagh et al. 2020  
Coogan et al. 2021

# Accretion disk

Baryonic matter



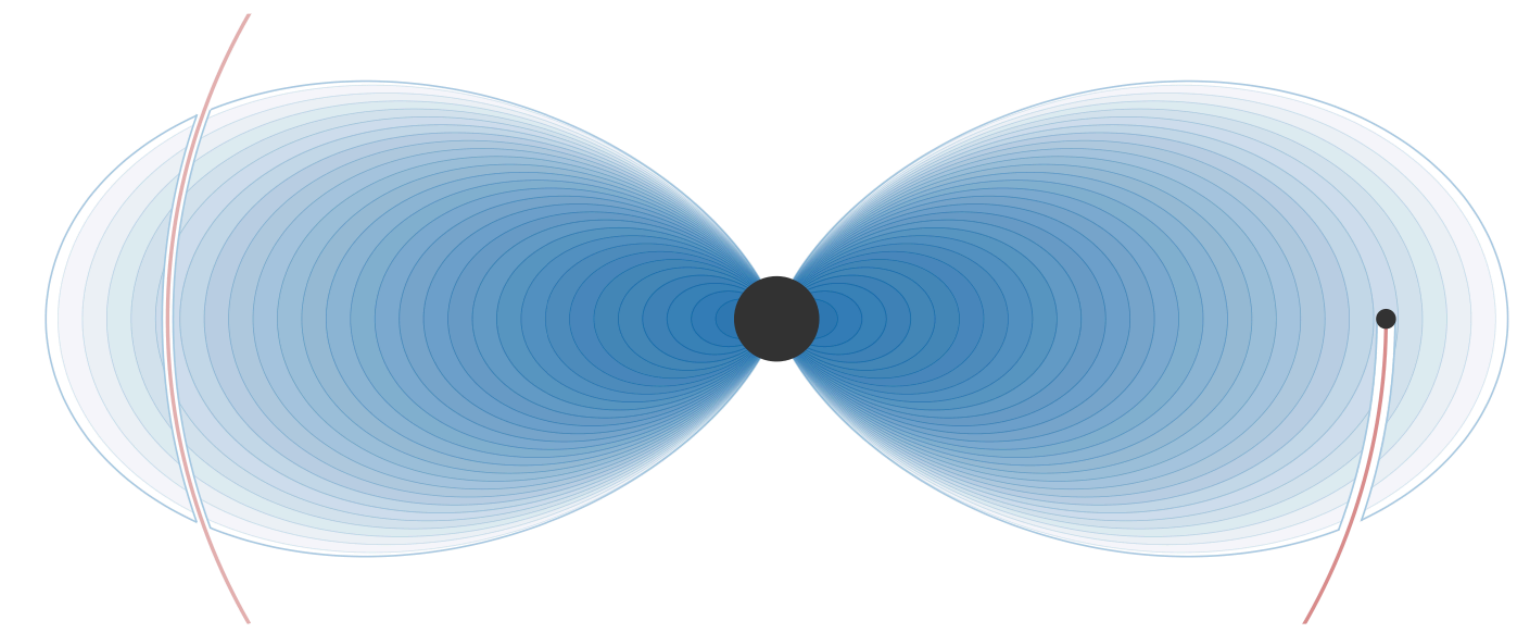
$$\Sigma(r) = \Sigma_0 \left( \frac{r}{r_0} \right)^{-1/2}$$

$$M = r/h$$

Goldreich & Tremaine 1980  
Tanaka 2002  
Derdzinski et al. 2020  
Speri et al. 2023

# Gravitational atom

Ultra-light bosons



$$\rho(\vec{r}) = M_c |\psi(\vec{r})|^2$$

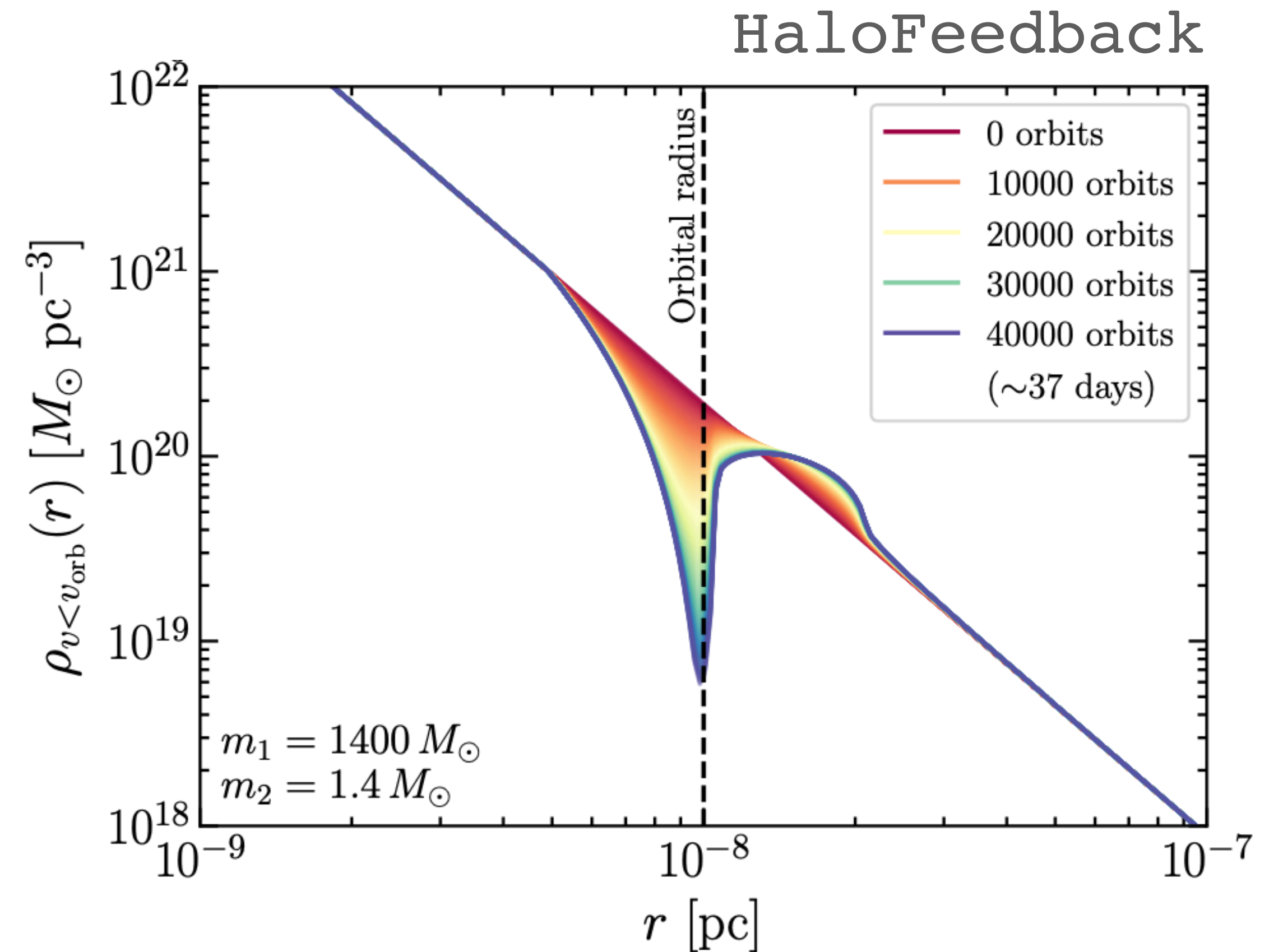
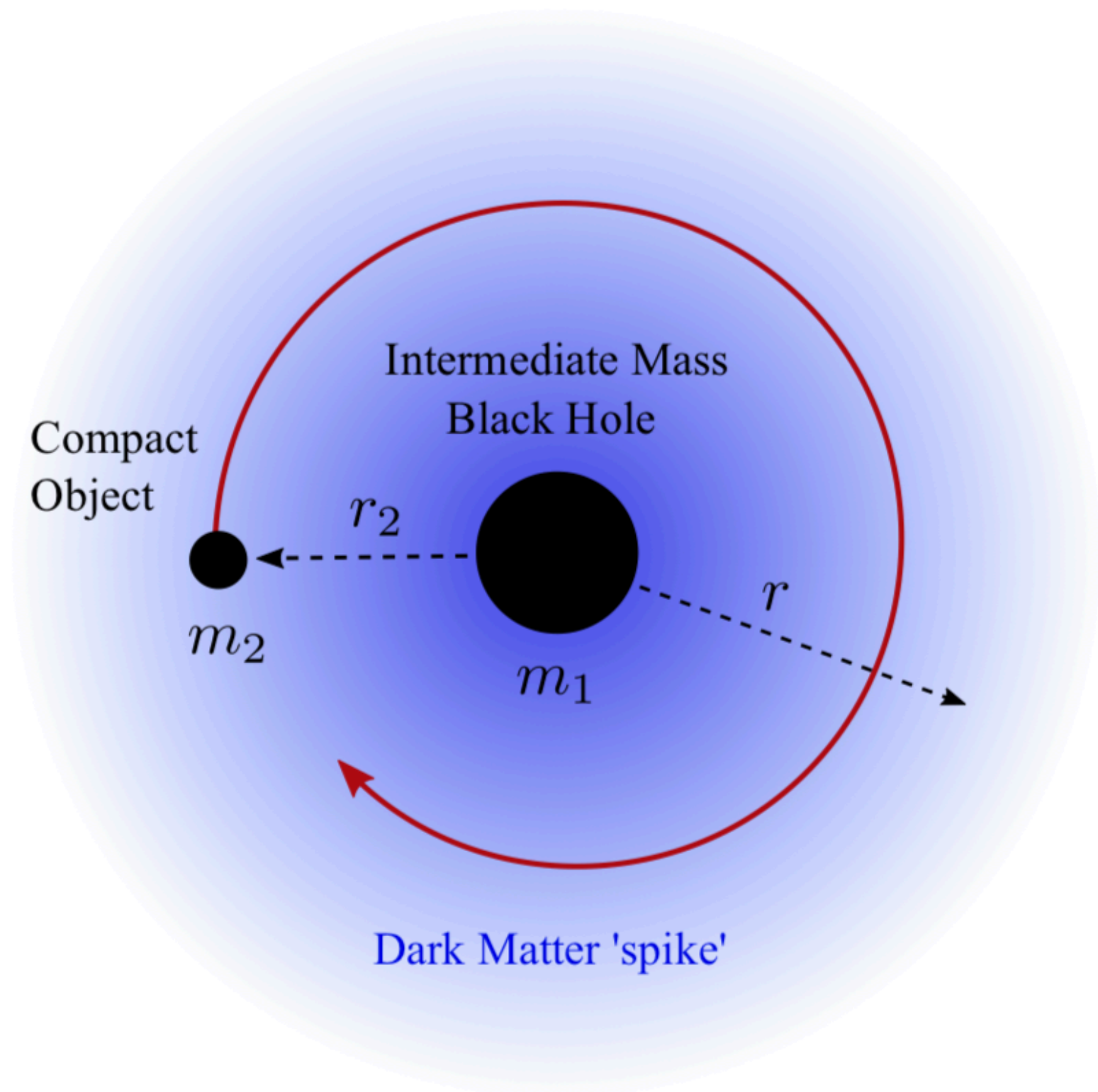
$$\alpha \equiv Gm_1\mu \ll 1$$

Mass of light scalar field  
( $10^{-10} - 10^{-20}$  eV)

Baumann et al. 2019  
Arvanitaki & Dubovsky 2010  
Bauman et al. 2021, 2022

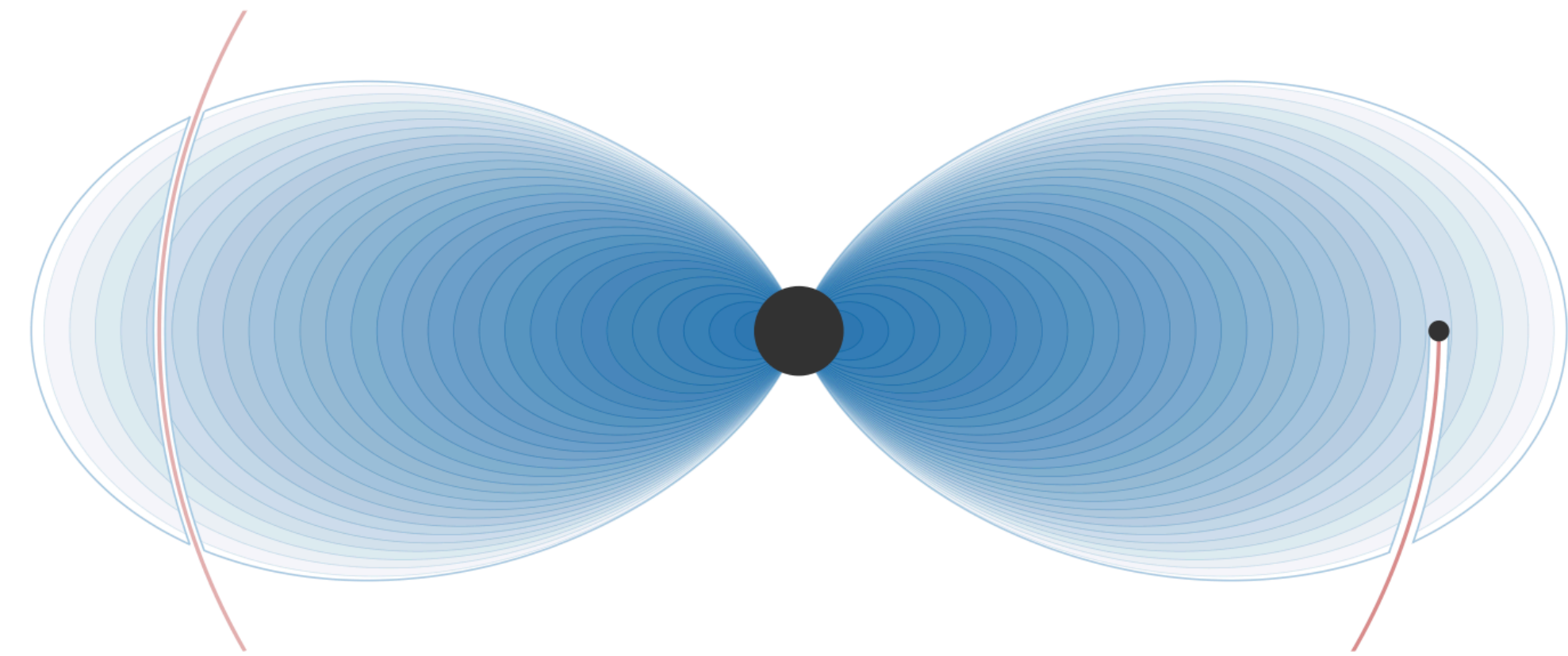
# Dynamical friction

$$\dot{r}_{\text{DF}} = - \frac{8\pi G_N^{1/2} m_2 \log \Lambda r_2^{5/2} \rho_{\text{DM}}(r_2, t) \xi(r_2, t)}{\sqrt{M} m_1}$$

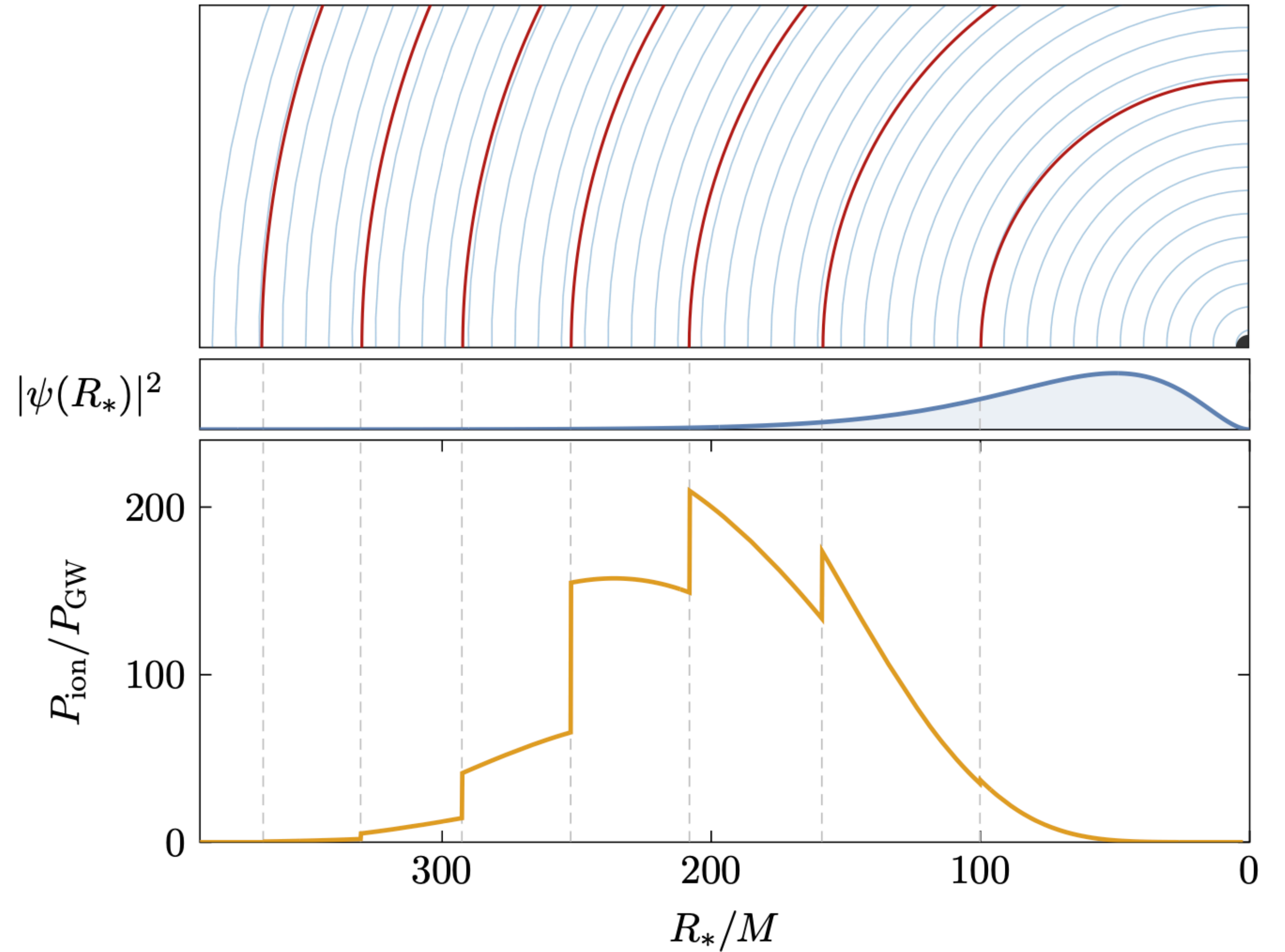




# Ionization



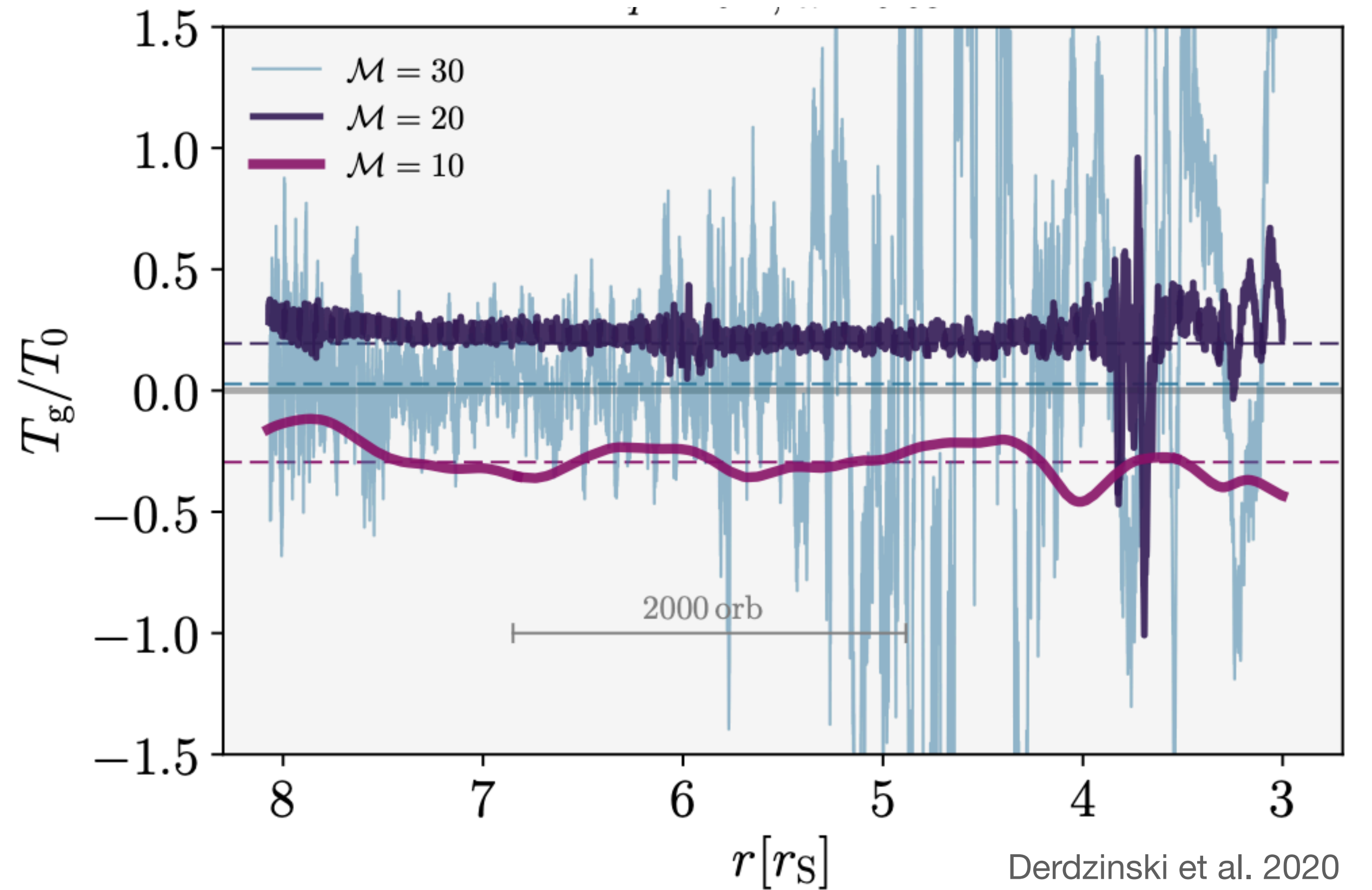
Perturber excites resonances in the cloud and it transitions from bound states to unbound states as the orbital frequency of the perturber hits the frequency of the energy difference between states



# Gas torques

$$\dot{r}_{\text{gas}} = \frac{\dot{L}_{\text{gas}} r^{1/2}}{2\sqrt{G(m_1 + m_2)m_2}}$$

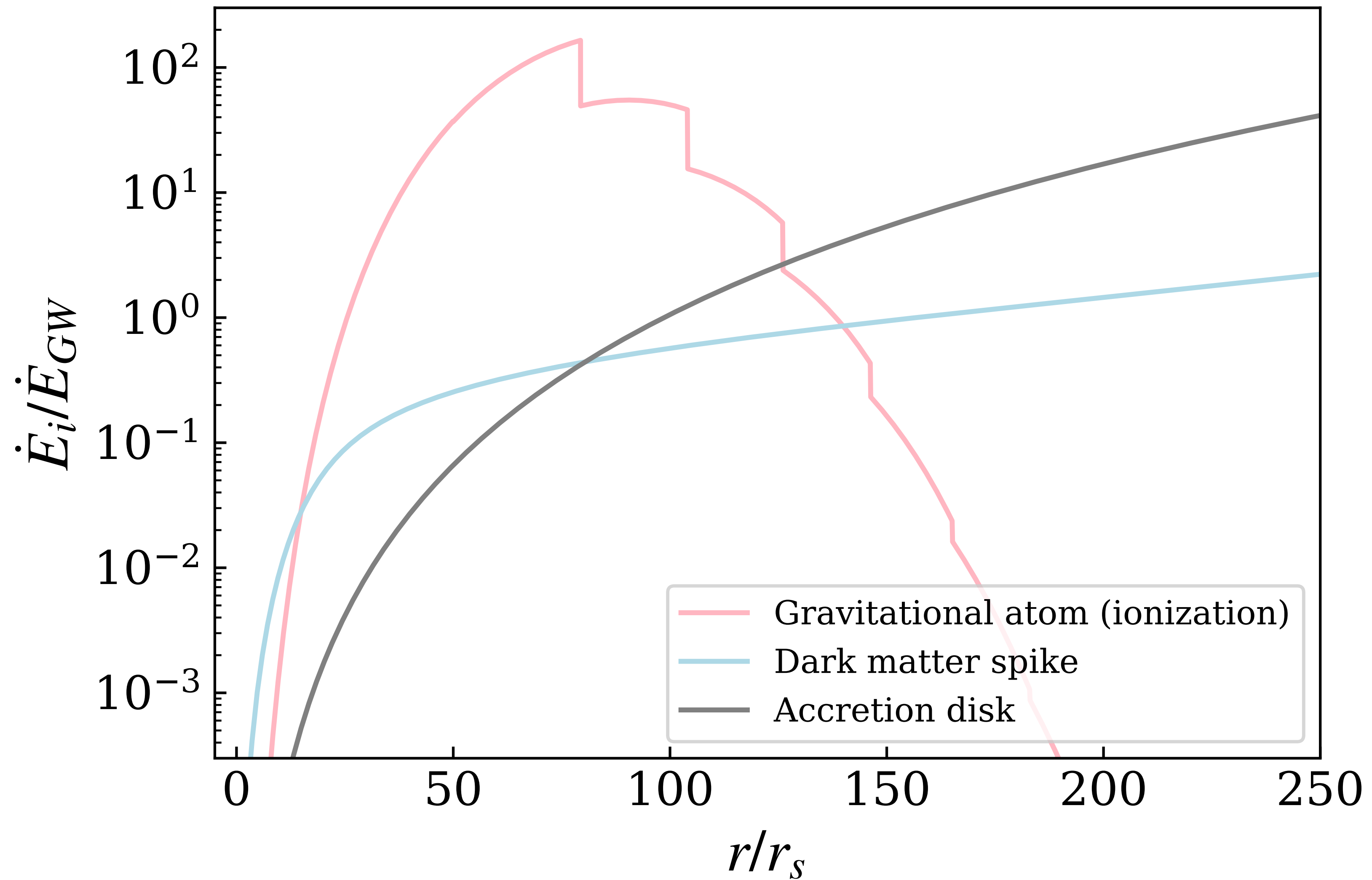
$$\dot{L}_{\text{gas}} = T_{\text{gas}} = \pm \Sigma(r)r^4\Omega^2q^2M^2$$



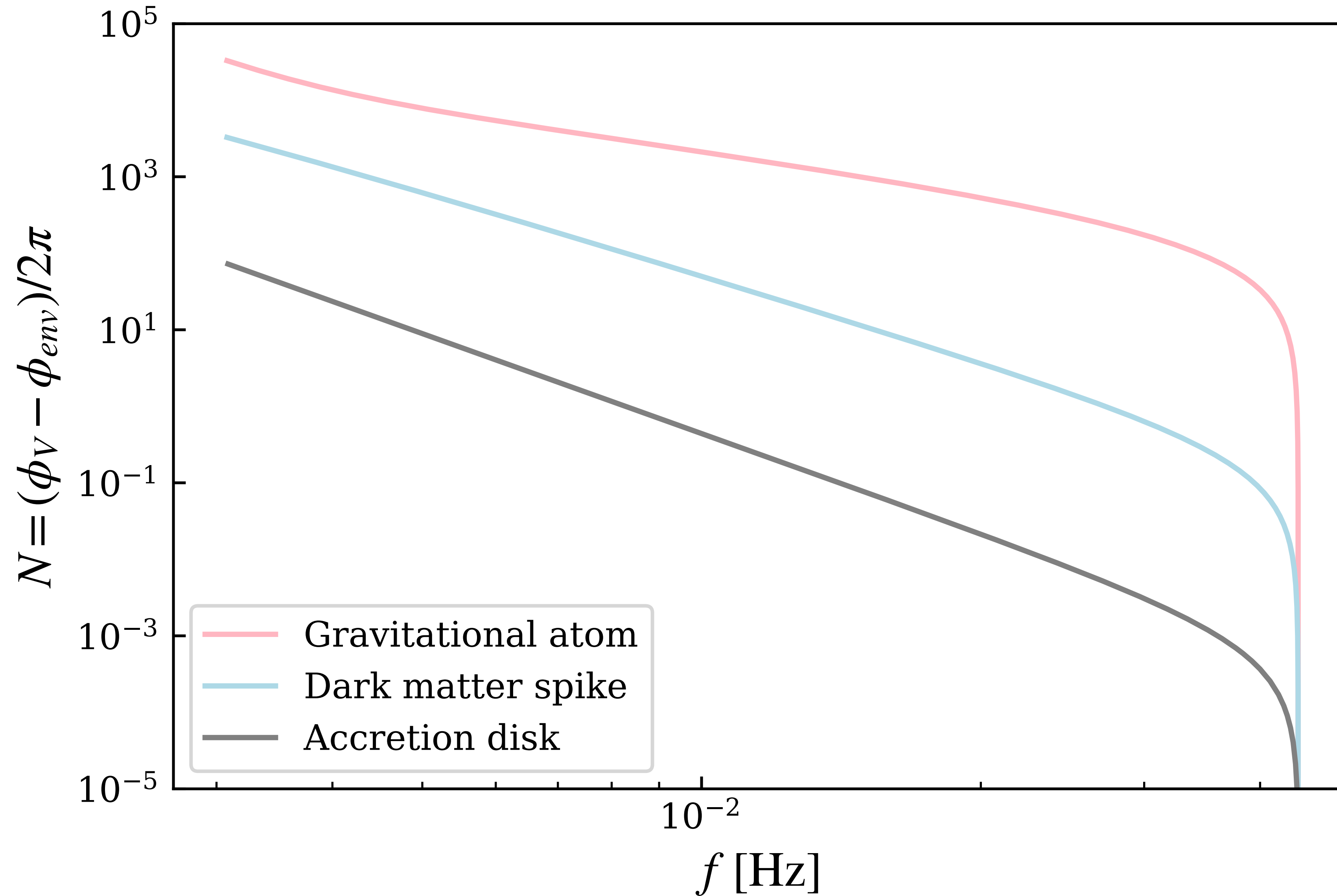
Assume gas in the disk is corotating with the companion object, which is orbiting in the plane of the disc.

Assume Mach number is locally constant, independent of  $r$ , i.e. locally isothermal.

# Energy losses



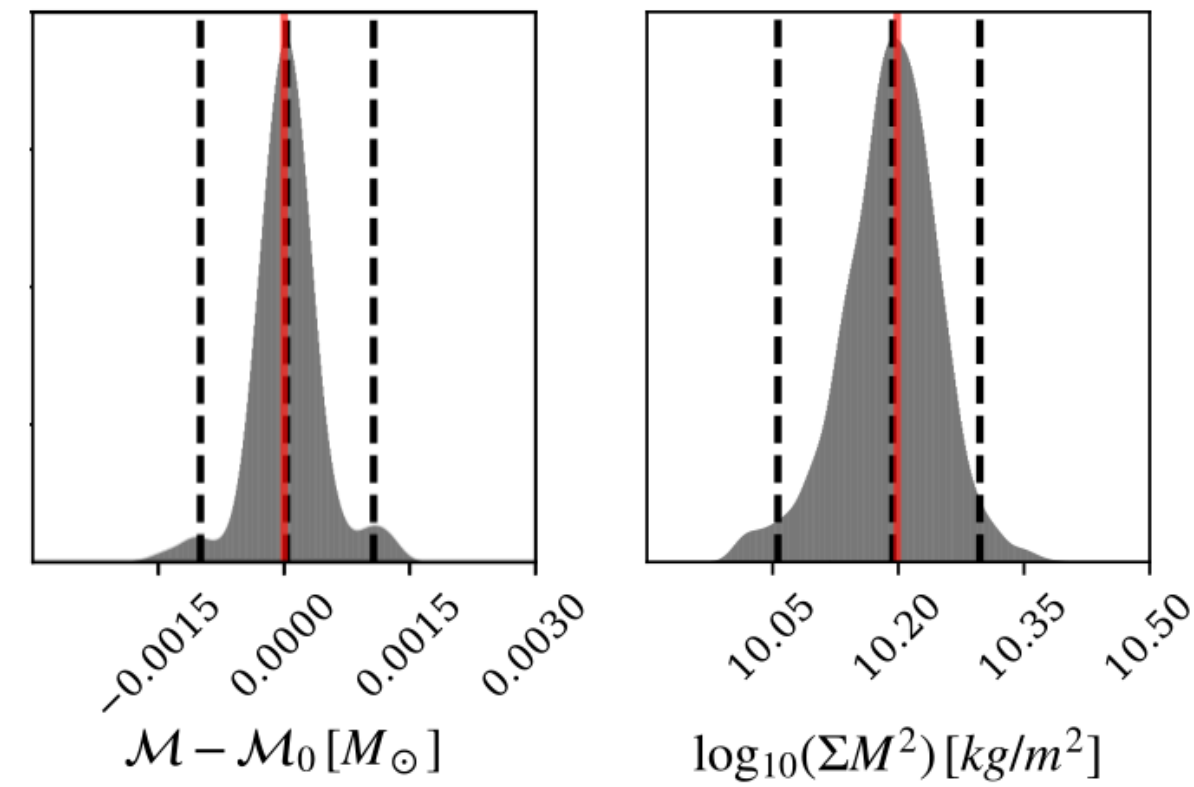
# Dephasing



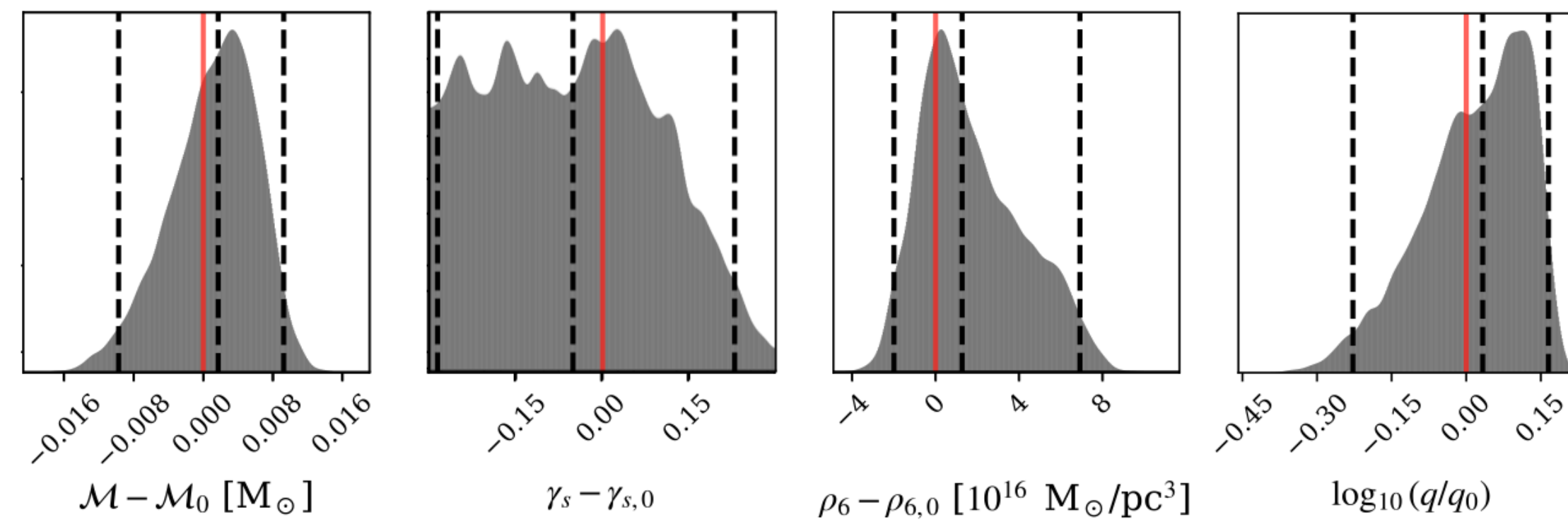
# Assuming we've detected a signal, can we measure the parameters?

## Parameter estimation with correct model

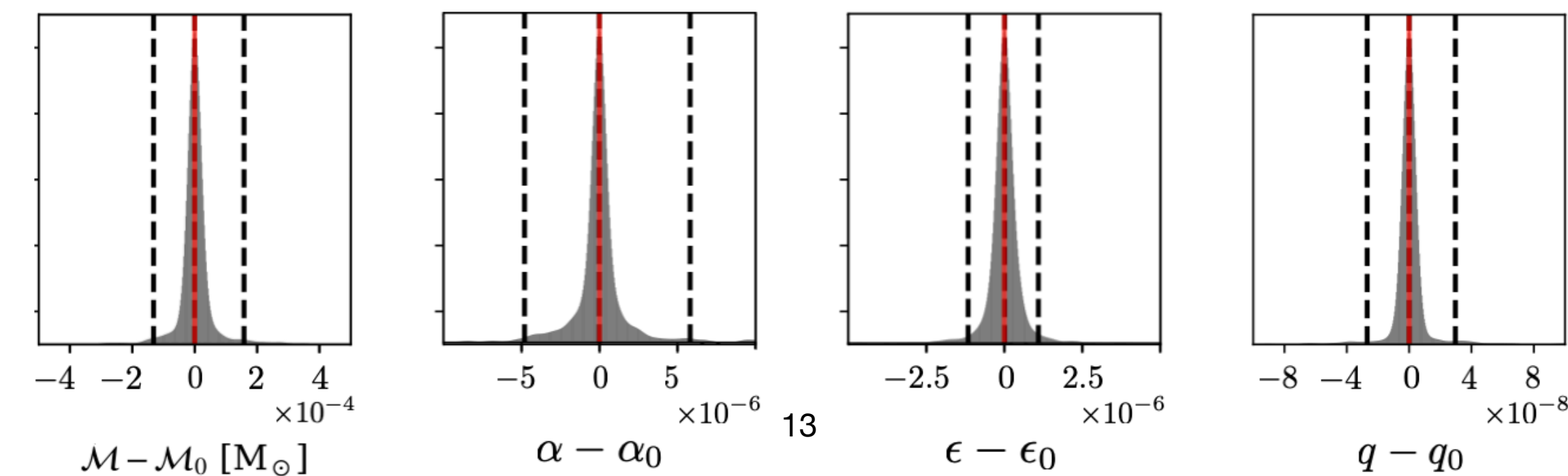
Accretion disk



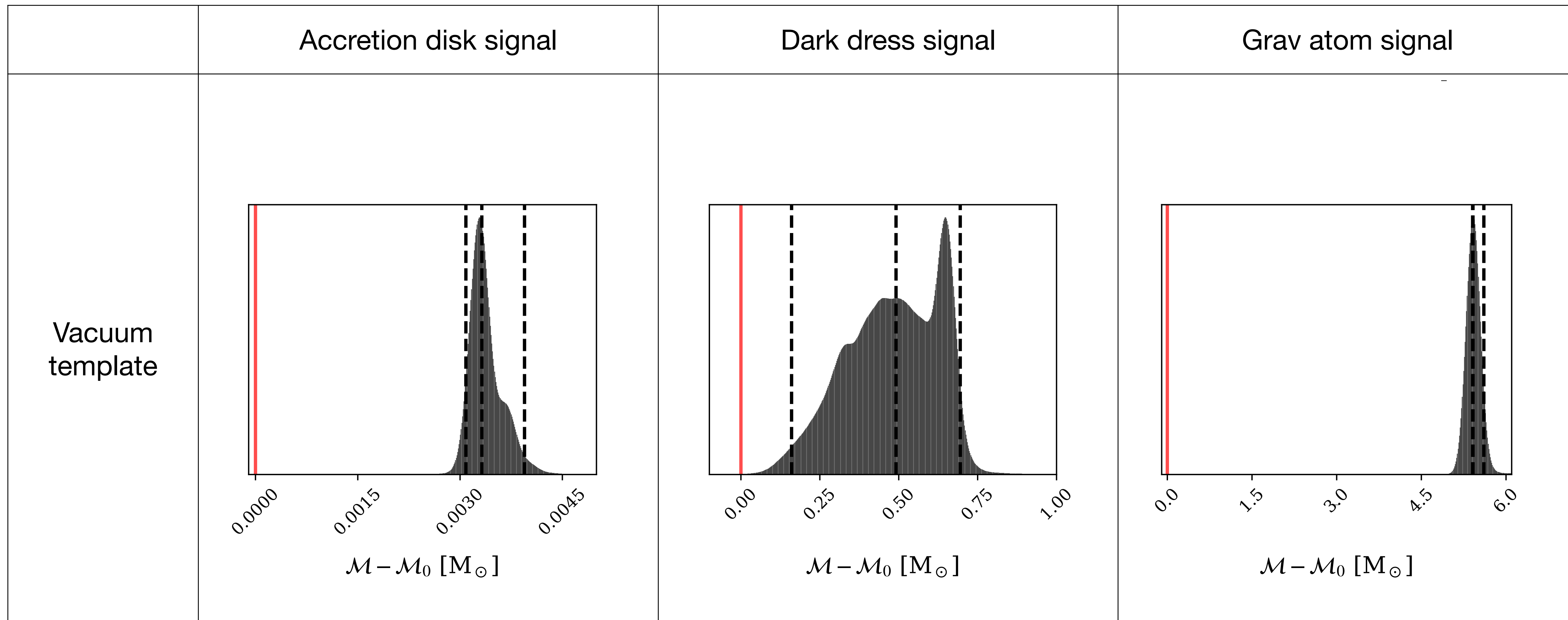
Dark dress



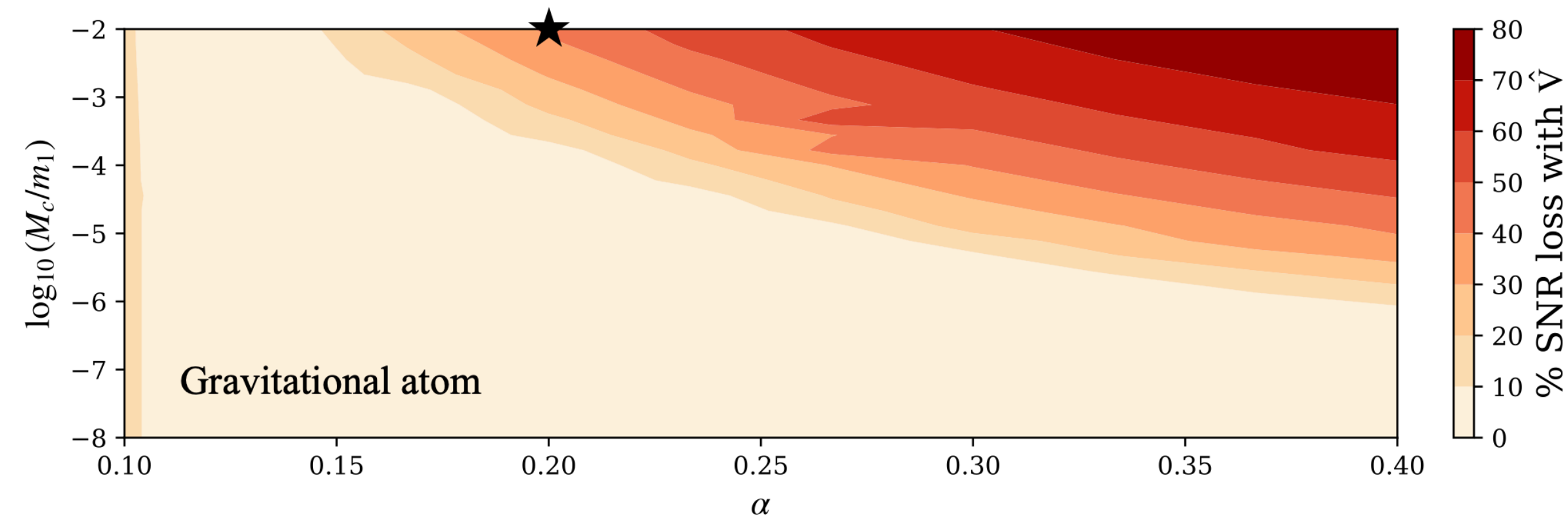
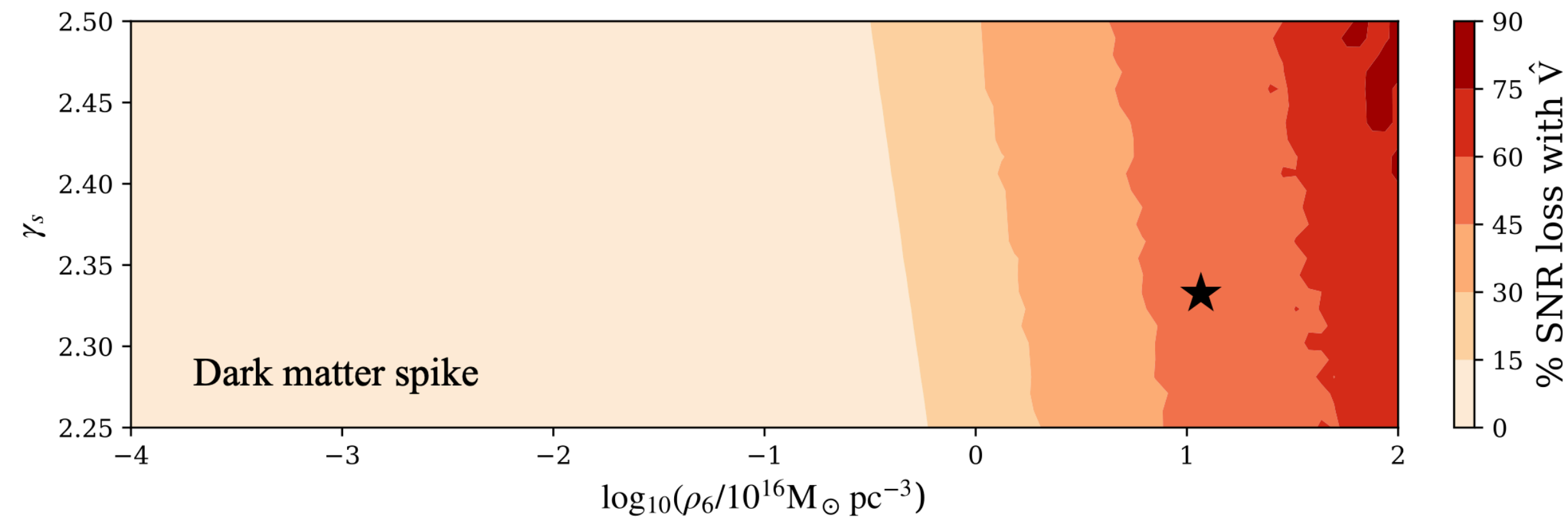
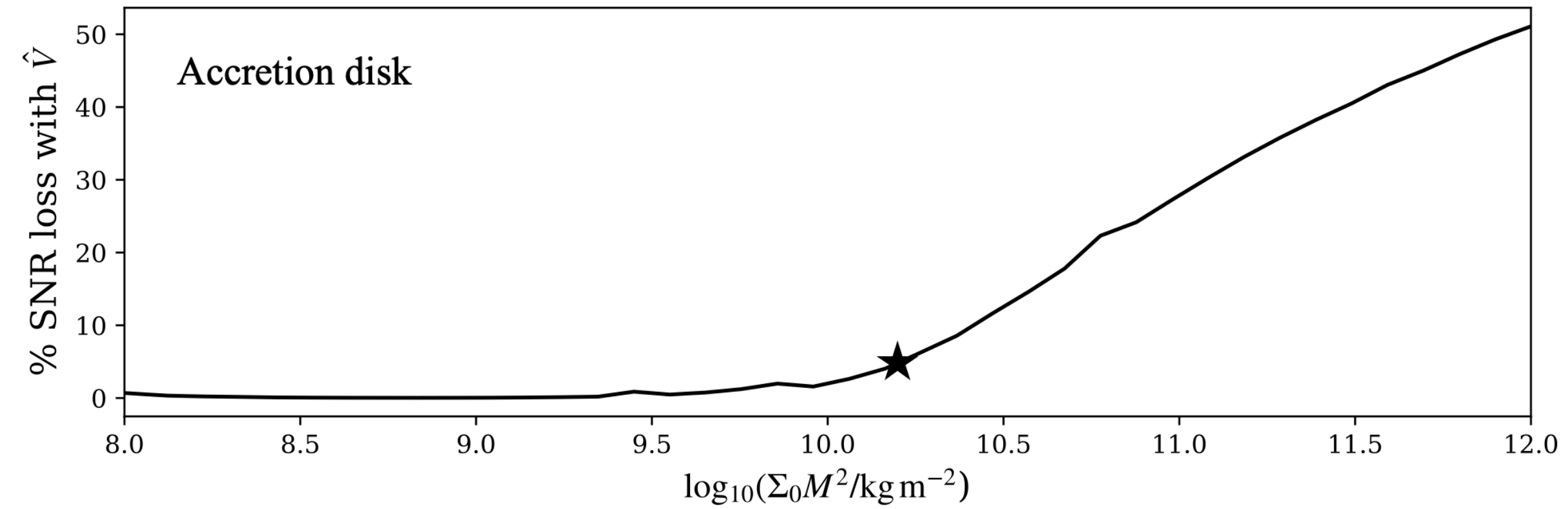
Gravitational atom



# Parameter estimation with vacuum waveform



# SNR loss: biased PE or miss signal entirely

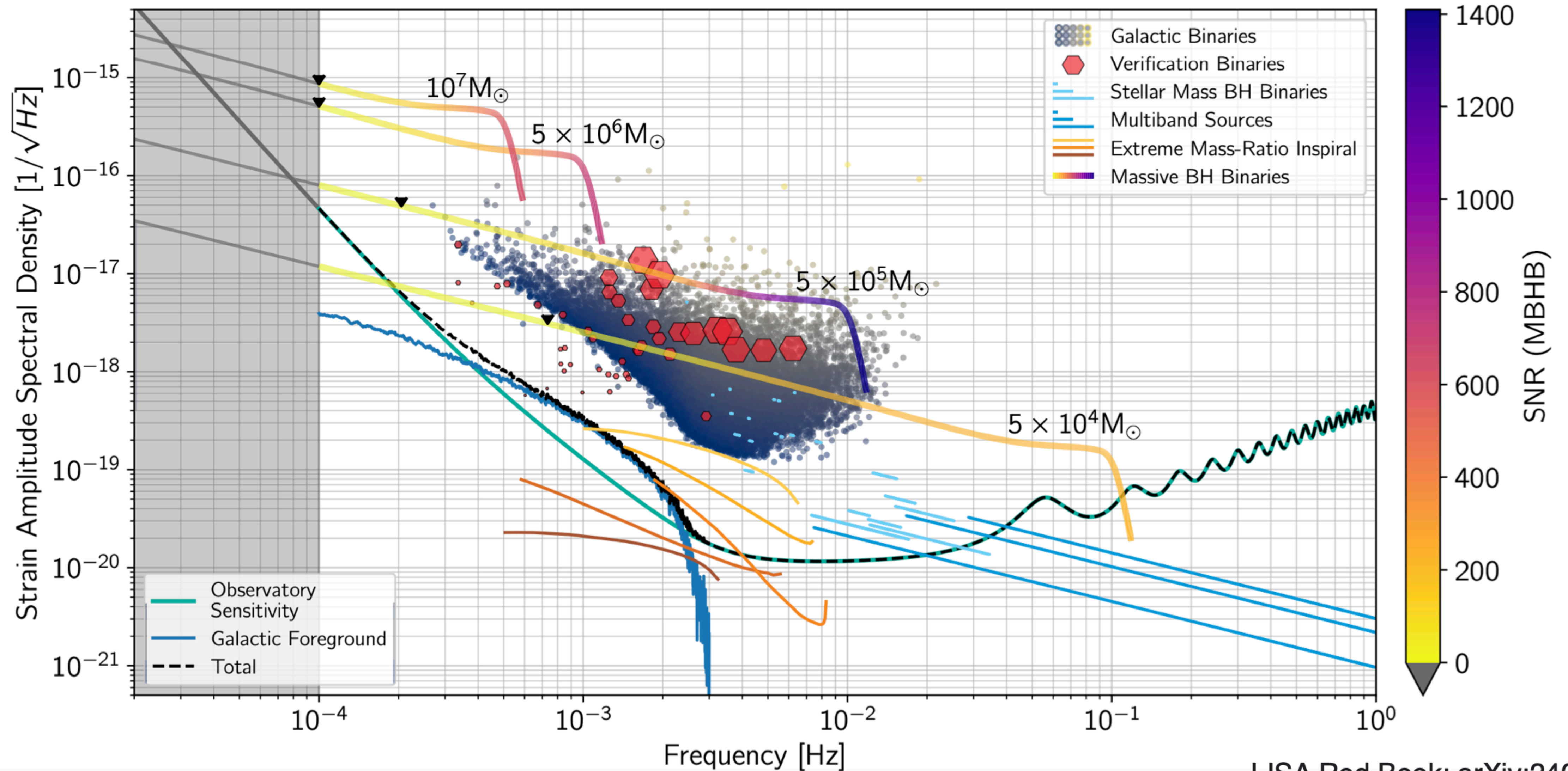


# Bayesian model comparison shows confident preference for correct model over any other environment

$\log_{10} \mathcal{B}$	Dark dress signal	Accretion disk signal	Gravitational atom signal
Vacuum template	34	6	39
Dark dress template	-	3	39
Accretion disk template	17	-	33
Gravitational atom template	24	6	-

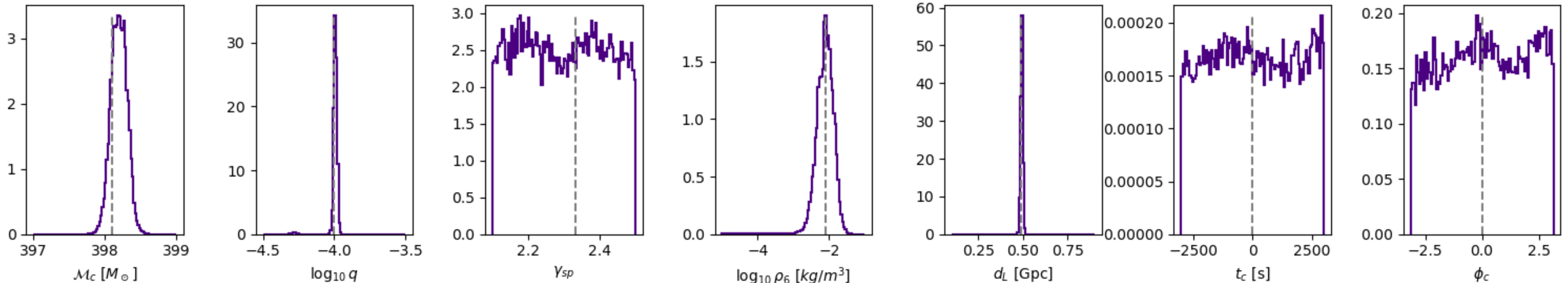
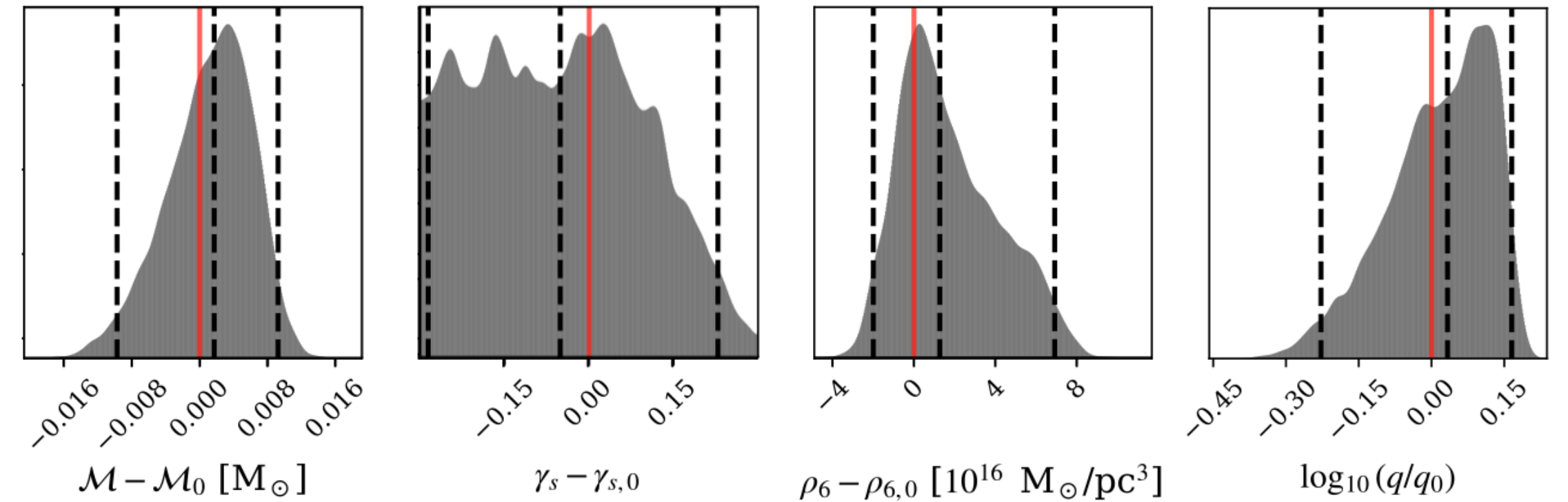


# Coping with real LISA data



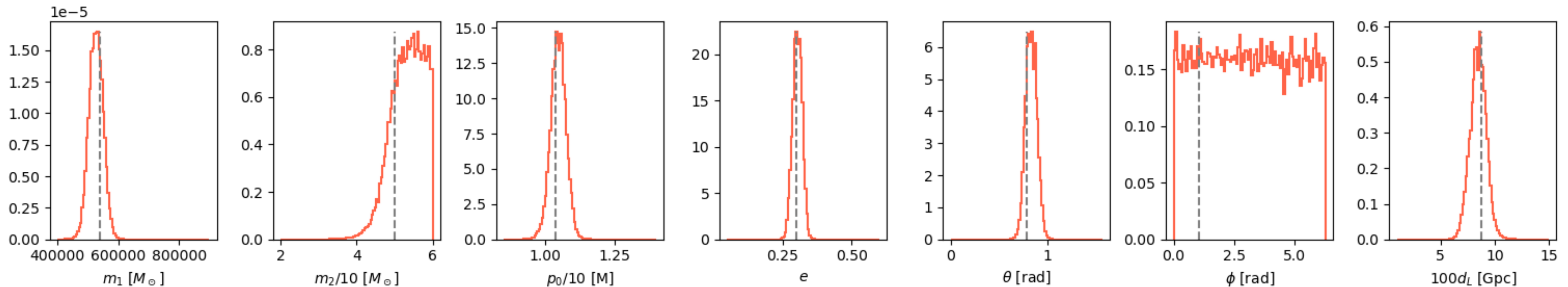
# Towards a realistic data analysis strategy

- Dark matter system as before, including extrinsic parameters and noise
- Using simulation-based inference, 30K simulations instead of 2million likelihood evaluations



# Towards a realistic data analysis strategy

- Aim to increase complexity of signal using Fast EMRI Waveforms (Katz et al. 2021)
- Preliminary results for Schwarzschild EMRI waveforms including the LISA response and noise



- Plan to fold in the dark matter effects to these higher order waveforms

# Conclusions

- There are many ways to probe the nature of dark matter with gravitational waves.
- LISA offers a particularly exciting avenue for searching for dark matter environments around extreme mass ratio inspirals.
- We need to include the possible presence of environments in our data analysis pipelines so that we don't miss the chance to measure the properties of dark matter, and to avoid unknown biases even for vacuum signals.
- Machine-learning tools may be a fruitful avenue for combating the complexity of the next generation of gravitational wave data.