

The population of Galactic supernova remnants in the TeV range

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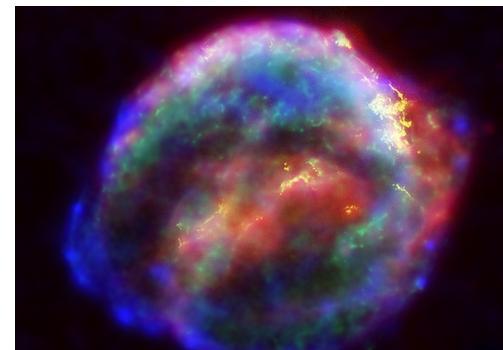


Image from [NASA](#)

Outline

- What are we looking for?
- SNR population model
- Properties of the SNR population investigated
- Results

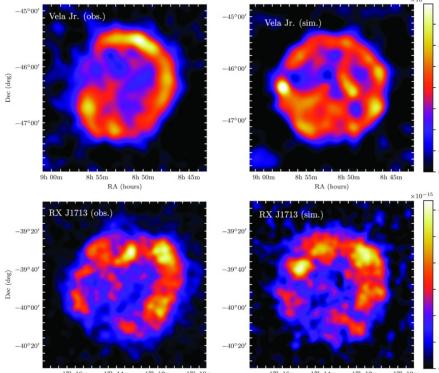
What are we looking for?

- SNRs produce gamma rays in the VHE (> 0.1 TeV) range but the details of this gamma-ray emission are not well understood.
- Questions to answer:
 - Can we describe the H.E.S.S. Galactic Plane Survey (HGPS) data?
 - What is the spectrum of accelerated particles?
 - What is the efficiency of particle acceleration?
 - Is the gamma-ray emission dominated by hadronic or leptonic origin?

What are we looking for?

Single SNR simulation

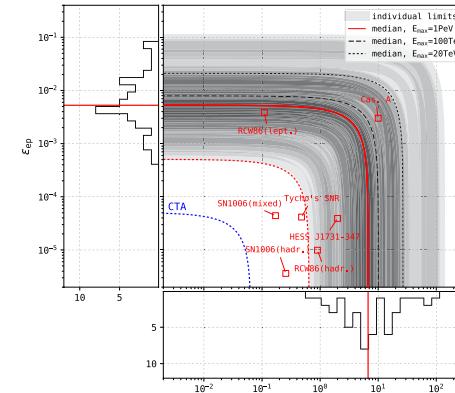
- Complicated modelling of the SNR
- Understanding the physical conditions and processes
- Only 1 SNR to compare to



[Pais et Pfrommer 2020](#)

Population simulation

- Simpler modelling of individual SNRs
- Reveal common properties of SNRs
- More SNRs for comparison



[HESS Collaboration 2018](#)

Gamma rays from SNRs

- Cosmic rays (CRs) are thought to be accelerated in SNR shocks
- The acceleration of CRs interacting with the interstellar medium can also produce gamma rays in the TeV range mainly via 2 mechanisms:

Hadronic

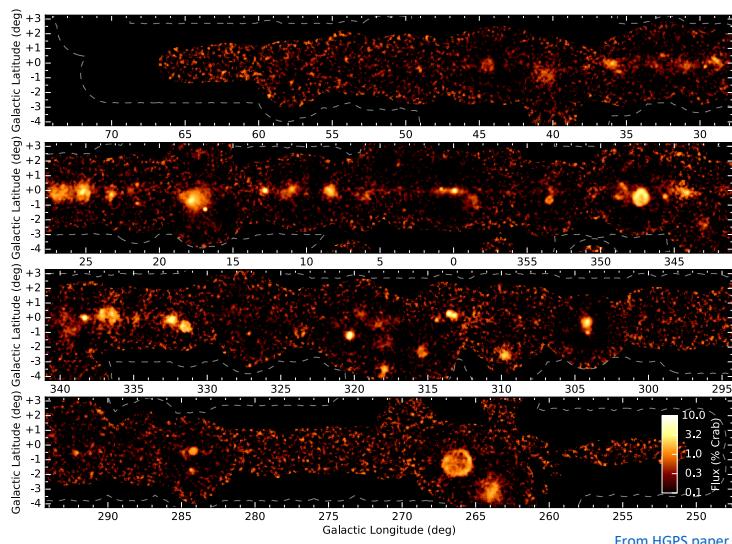
- Proton spectrum
- Pion decay

Leptonic

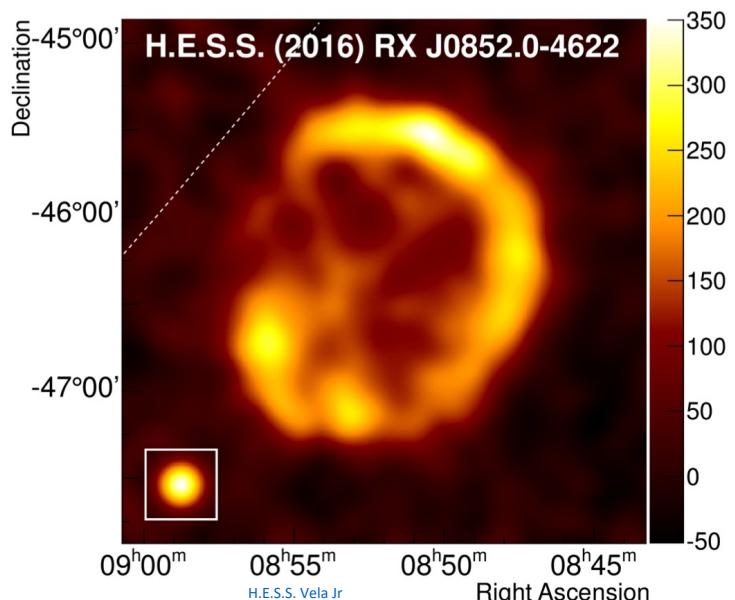
- Electron spectrum
- Inverse Compton

H.E.S.S. Galactic Plane Survey

- The High Energy Stereoscopic System (H.E.S.S.) performed a systematic survey of the Galactic plane (0.1 to 100 TeV)
- A total of 78 sources detected

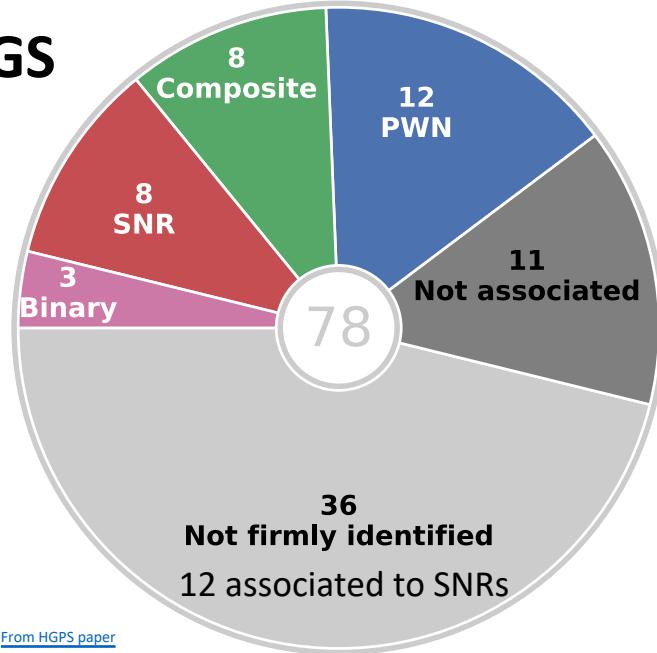


[From HGPS paper](#)



HGPS data

HPGS



Comparison

- Lower limit of 8
- Strict upper limit of 63 ($8 + 8 + 47$)
- Stringent upper limit of 28 ($8 + 8 + 12$)

SNR population model ingredients

- Physics of the supernova remnant
 - Evolution of the radius and velocity of the shock
 - Magnetic field amplification
 - Maximum energy of accelerated particles
- Distribution of sources and matter
 - Types of SNRs
 - Where in the Milky way
 - Ejecta mass and explosion energy distribution

Properties of the SNR population investigated

- Spectral index, α (4.0 to 4.4)
- Electron proton ratio, K_{ep} (10^{-2} to 10^{-5})
- Efficiency of gamma-ray production, η (1% to 10%)

Realisation of a single population

- Taking into account the HGPS sensitivity
- Gray shaded region is HGPS sensitivity for a source with luminosity, $L = 5 \times 10^{33} \text{ ph s}^{-1}$

Parameters:

$$\alpha = 4.3$$

$$K_{\text{ep}} = 10^{-3}$$

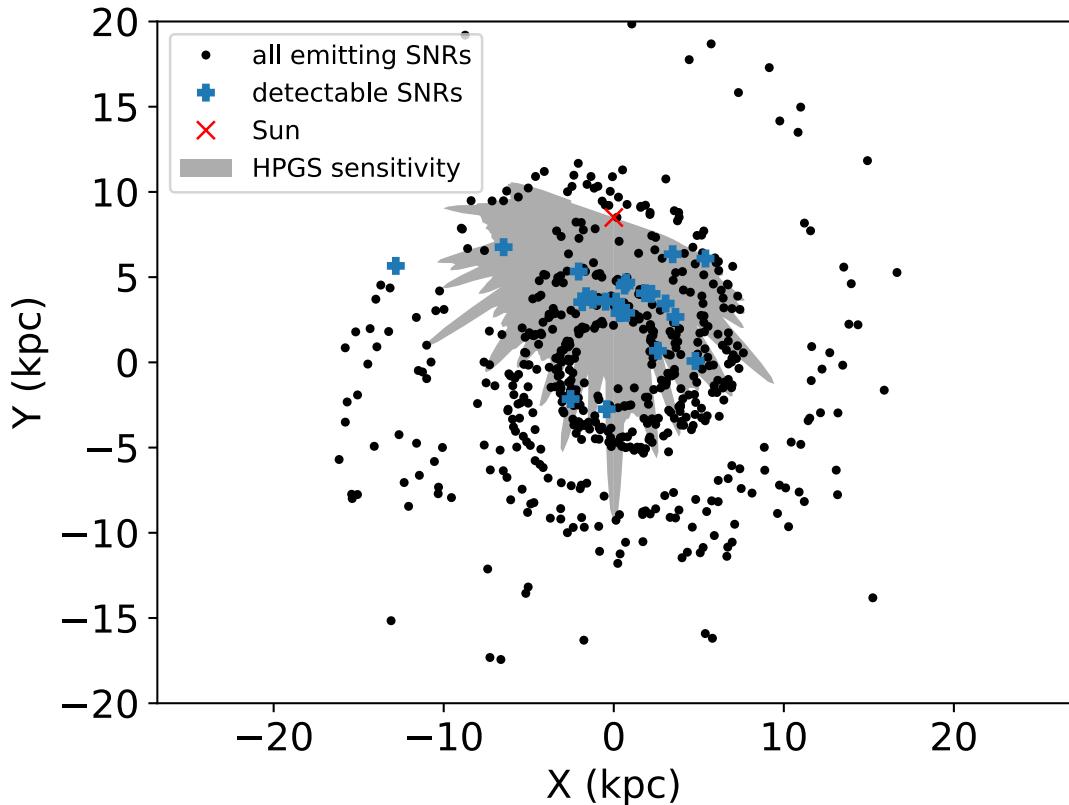
$$\eta = 0.07$$

$$S\text{T} = 20 \text{ kyr}$$

Steiman-Cameron distribution

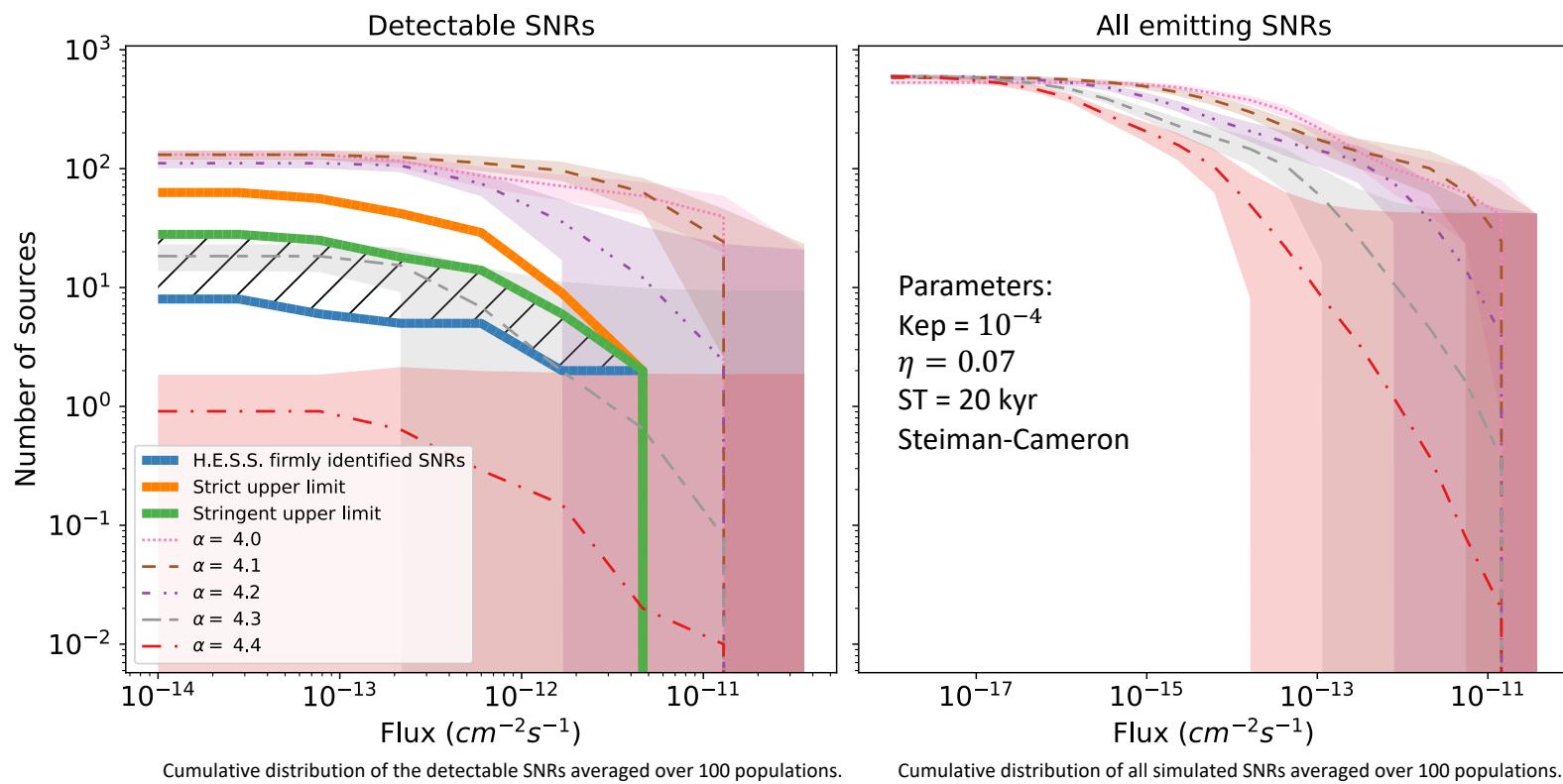
Shaded region:

$$L = 5 \times 10^{33} \text{ ph s}^{-1} (\sim 4 \times 10^{-11} \text{ TeV}^{-1} \text{ cm}^{-2} \text{ s}^{-1} \text{ at 1 kpc})$$



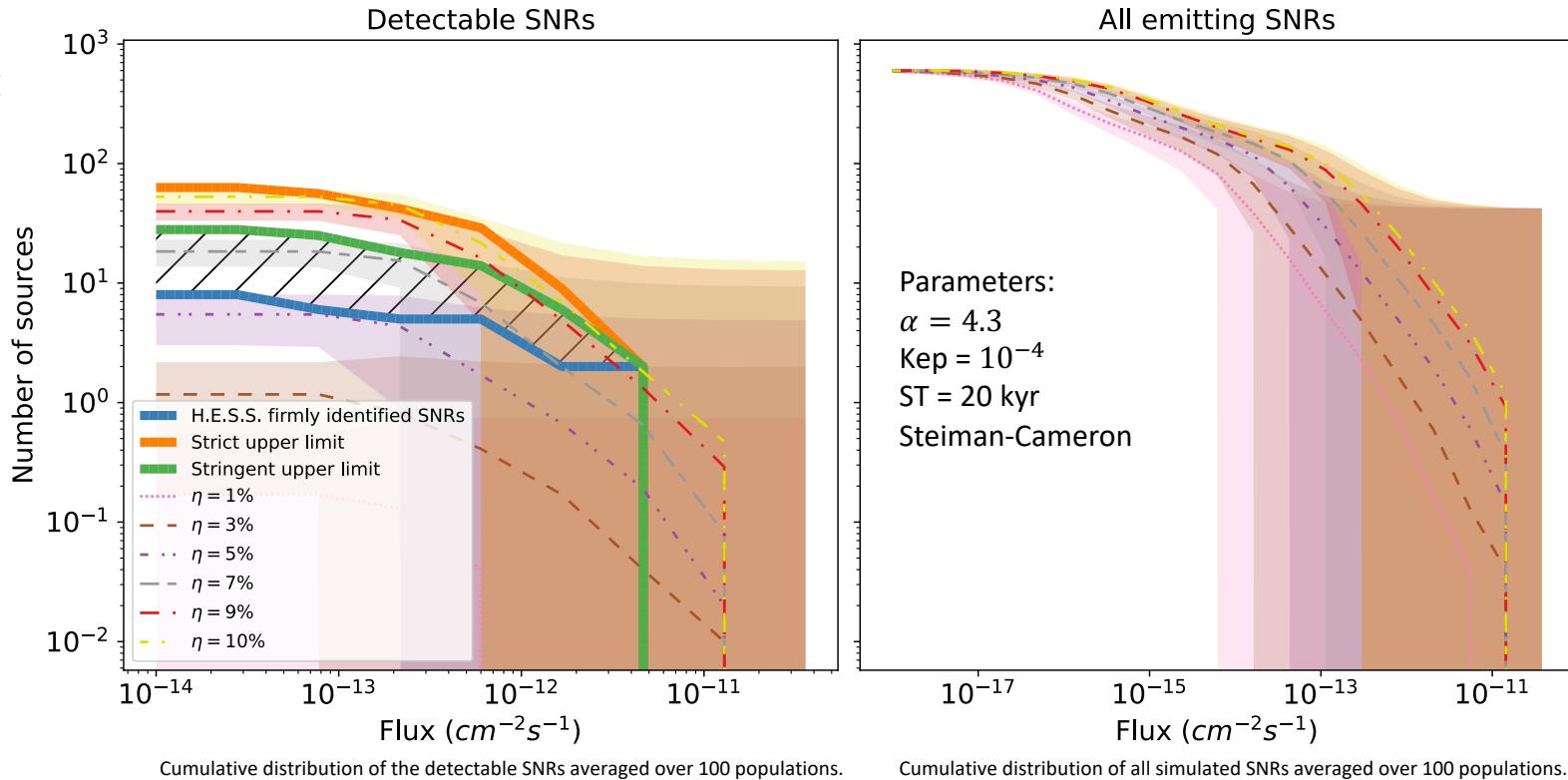
Results – Spectral Index

- Log-N log-S distributions
- Same no. of total SNRs
- Can't just draw a line at some flux to determine detectability
- Larger α means less detections



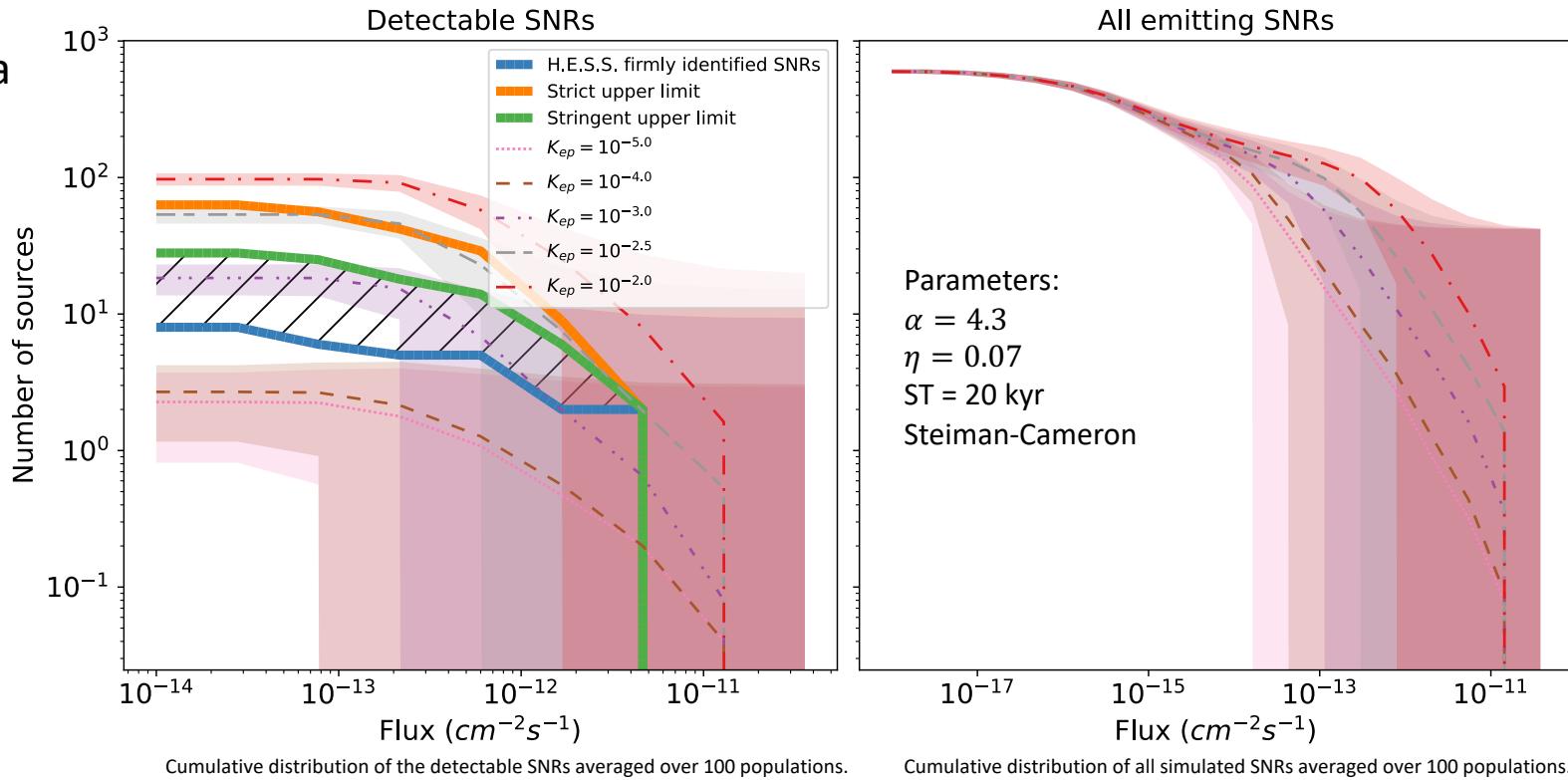
Results – Acceleration efficiency

- Illustrative parameter set remains the same
- $5\% < \eta < 10\%$ is within the strict limit
- Larger η means more detections



Results – Electron-proton ratio

- $K_{ep} = 10^{-2.5}$ is a possible but extremely unlikely case
- Larger K_{ep} means more detections

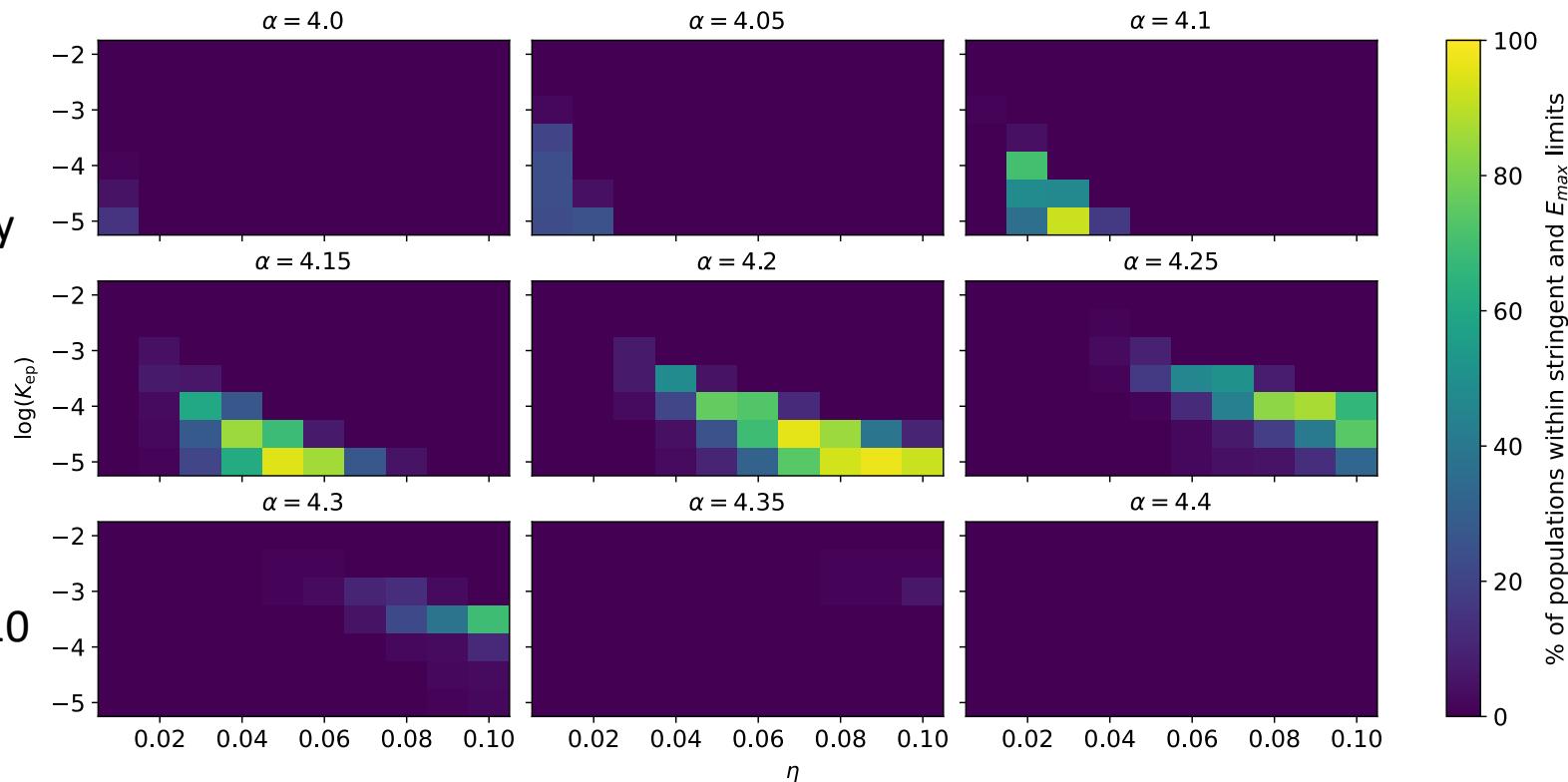


Systematic exploration of parameter space

- It's clear that by changing only one parameter at a time that there should be other combinations that work.
- We explored a large parameter space changing α , η and K_{ep} .
- Need populations with:
 - > 8 SNRs (firm detections)
 - < 28 SNRs (associated)
- Additional E_{max} criterion
- 8 firmly detected SNRs
 - $4 E_{max} > 10$ TeV
 - $2 E_{max} \sim 10$ TeV
 - $2 E_{max} < 10$ TeV

Results – Parameter exploration

- $\alpha < 4.1$ produces populations with too many detectable SNRs
- $\alpha > 4.3$ does not produce enough SNRs with $E_{max} > 10$ TeV



Best populations (>90% in agreement with HGPS)

- $K_{ep} \geq 10^{-4.5}$
- $4.1 \leq \alpha \leq 4.2$
- Hadronic ratio is not only dependant on K_{ep}
- SNRs dominated by emission from hadronic processes are typically younger and brighter than SNRs dominated by leptonic emission

Population Parameters			% compatible with HGPS	Hadronic Ratio	Mean No. detectable SNRs	Mean Had. Age (kyr)	Mean Lep. Age (kyr)	Mean Had. Dist. (kpc)	Mean Lep. Dist(kpc)
$\alpha = 4.2$	$K_{ep} = 10^{-5.0}$	$\eta = 0.09$	97	0.62	16.84	2.15	4.86	5.65	4.88
$\alpha = 4.2$	$K_{ep} = 10^{-4.5}$	$\eta = 0.07$	96	0.43	16.14	1.94	4.36	5.64	4.9
$\alpha = 4.15$	$K_{ep} = 10^{-5.0}$	$\eta = 0.05$	95	0.51	16.41	2.06	5.21	5.62	4.79
$\alpha = 4.2$	$K_{ep} = 10^{-5.0}$	$\eta = 0.08$	93	0.66	13.6	2	4.88	5.63	5.06
$\alpha = 4.1$	$K_{ep} = 10^{-5.0}$	$\eta = 0.03$	92	0.37	19.56	2.05	5.7	5.61	4.63
$\alpha = 4.2$	$K_{ep} = 10^{-5.0}$	$\eta = 0.1$	92	0.6	20.64	2.32	4.92	5.66	4.76

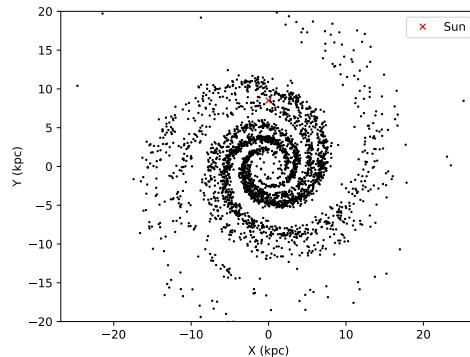
Summary

- Confronted SNR population model to HGPS, taking into account the multi-dimensional exposure for the first time.
- Explored a large parameter space but correlations prevent the identification of an optimal combination.
- Can exclude some parts off the parameter space:
 - $\alpha \lesssim 4.05$
 - $K_{ep} \gtrsim 10^{-2.5}$
 - $K_{ep} \sim 10^{-3}$ requires $\alpha \gtrsim 4.35$ and $\eta \lesssim 0.02$
- Realisations with $\gtrsim 90\%$ compatible:
 - $4.1 \lesssim \alpha \lesssim 4.2$
 - $10^{-5} \lesssim K_{ep} \lesssim 10^{-4.5}$
- Despite very low electron-proton ratios we still find many SNRs dominated by leptonic emission.
- The detectable SNRs are clearly a highly biased sample.
- Batzofin, et al. (2024), The population of Galactic supernova remnants in the TeV range, A&A, 687, A279, doi: [10.1051/0004-6361/202449779124](https://doi.org/10.1051/0004-6361/202449779124)

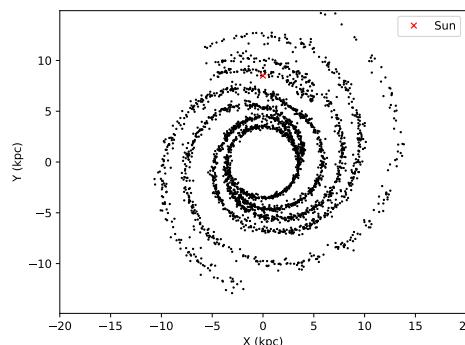
Backup slides

Source and matter distribution

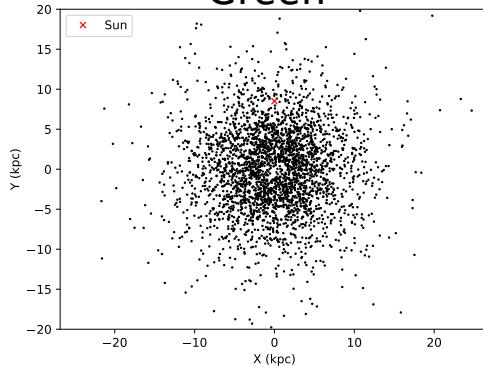
Steiman-Cameron



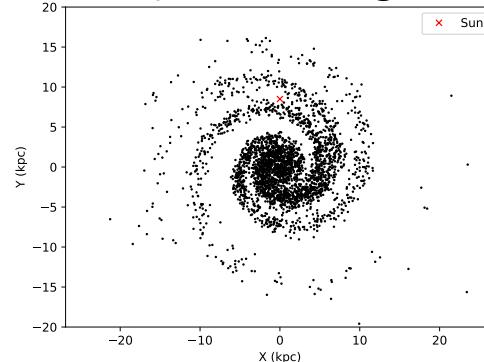
Reid



Green

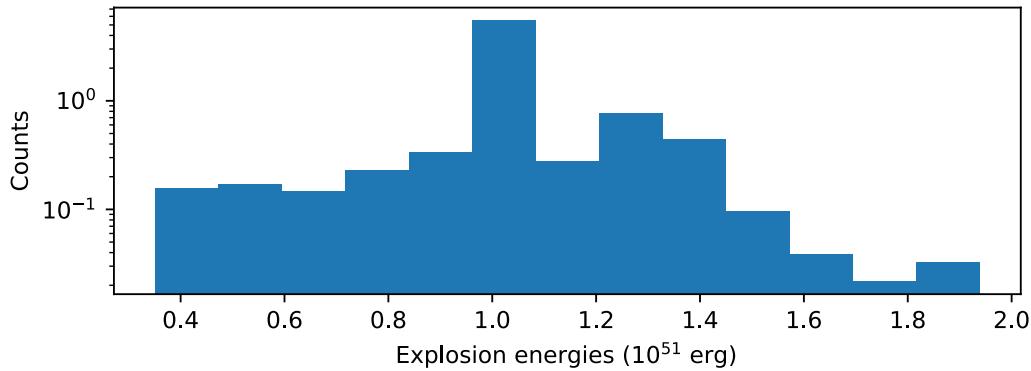
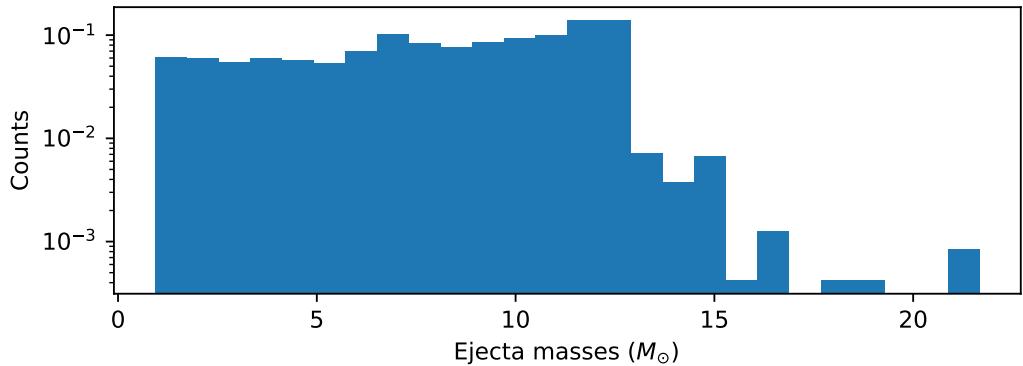


CAFG (Faucher-Giguere)



- Relative rates of supernovae:
 - Thermonuclear 32%
 - Core collapse 68%
- 3 supernovae per century
- Source distribution models
 - [Steiman Cameron](#) (ISM)
 - [Reid](#) (Massive stars)
 - [Green](#) (SNRs)
 - [CAFG](#) (Pulsars)
- Matter distribution follows an empirical model that closely matches the GALPROP code - [Shibata et al. 2010](#)

Distribution of masses and explosion energies of simulated SNRs



Distribution of mass and energy of explosion

Thermonuclear:

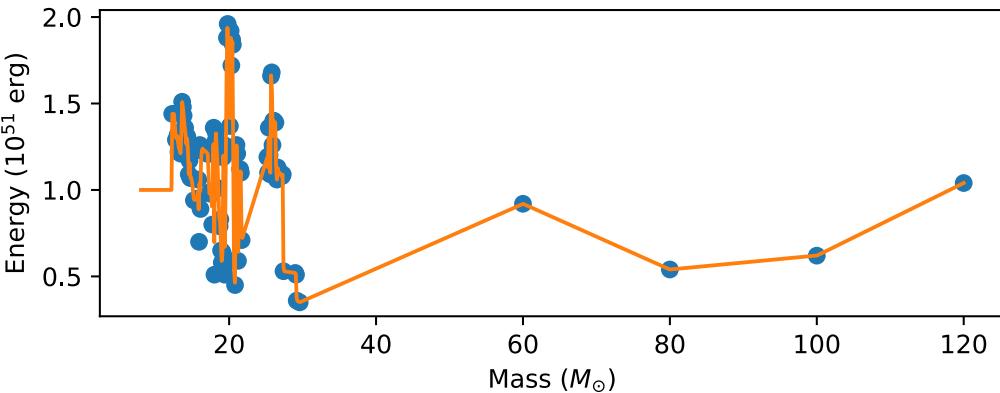
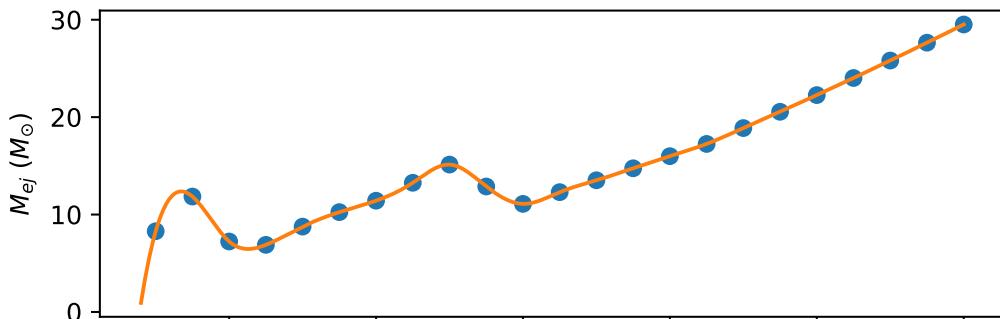
$$M_{ej} = 1.4 M_{\odot}$$

$$E_{SN} = 10^{51} \text{ erg}$$

Core collapse:

$$\text{Initial mass distribution } N \propto \int_8^{120} M_{\star}^{-2.3} dM_{\star}$$

E_{SN} interpolated from results obtained in [Sukhbold et al. 2016](#)



Supernova dynamics

- Place the SNR in the Milky way.
- Shock velocity and radius are determined at the age of the SNR, taking into account the density of the ISM.
- Magnetic field amplification:
 - initially from the growth of non-resonant streaming instabilities upstream of the shock - [Bell et al. 2013](#)
 - later resonant streaming instabilities - [Morlino & Caprioli 2012](#)
- Based on the shock and the magnetic field amplification we calculate the **maximum energy** of accelerated particles.
 - Determined by the growth of non-resonant streaming instabilities ([Bell](#)) - [Bell et al. 2013](#)
 - Determined by Hillas estimation ([Hillas](#))

Supernova dynamics

- $f_{CR}(p) = A \left(\frac{p}{m_p c} \right)^{-\alpha}$ Differential spectrum of accelerated particles
 - p is the momentum and α is the spectral index
 - The normalisation (A) is found by requiring the CR pressure to be some fraction, η_{CR} of the ram pressure at the shock location.
 - $\frac{1}{3} \int_{p_{min}}^{p_{max}} dp \, 4\pi p^2 f_{CR}(p) p v(p) = \eta_{CR} \rho v_{sh}^2$

{ Cosmic ray pressure } { Ram pressure }

SNR population model improvements

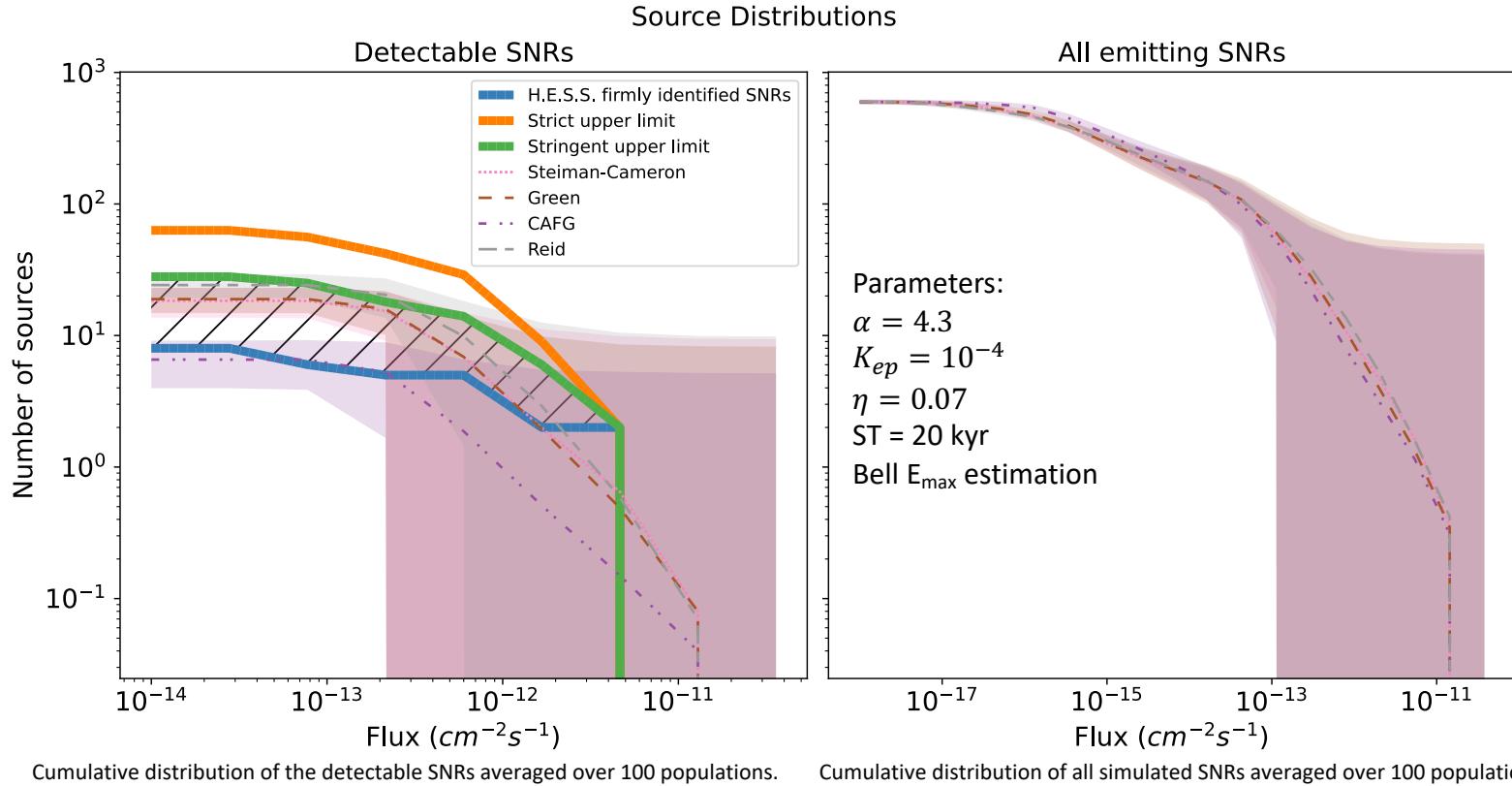
Expanding on the work done by [Cristofari et al.](#):

- Connection between ejecta masses and explosion energies
- Refined description of magnetic field amplification and corresponding maximum energy for protons and electrons
- Inclusion of diffusive shock reacceleration at SNR shocks
- Multiple prescriptions for the spatial distribution of SNRs in the Galaxy

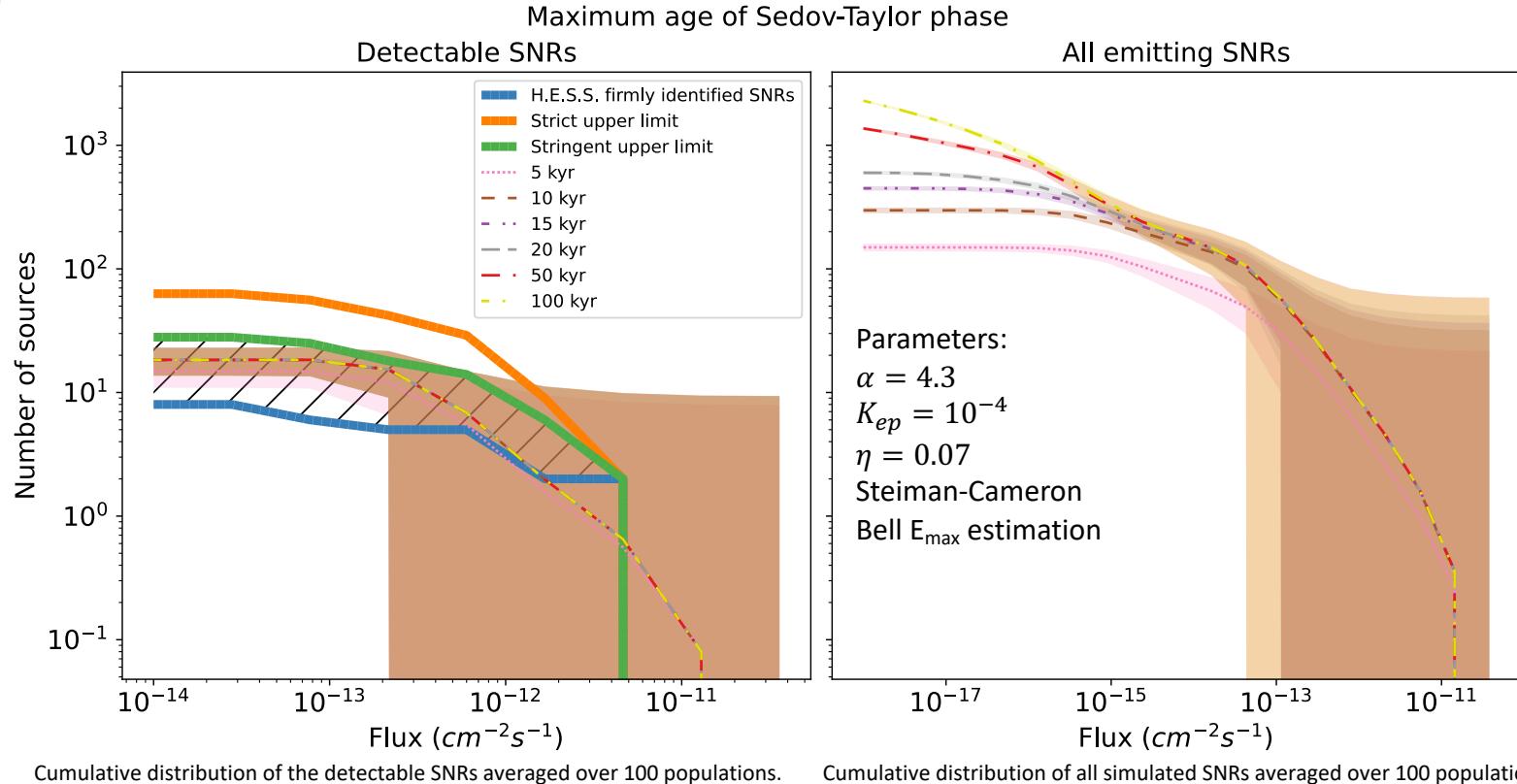
Emission from reaccelerated CRs - [Cristofari & Blasi \(2019\)](#)

- Galactic CRs reaccelerated at the SNR shock
 - Assume spectrum is the same as local interstellar spectrum
- $f_0^{seed}(p) = \alpha \int_{p_0}^p \frac{dp'}{p'} \left(\frac{p'}{p}\right)^\alpha f_\infty(p')$
 - $f_\infty(p)$ is the distribution function at upstream infinity of the seeds to be reaccelerated.
 - $p_0 = 10^{-2}$ GeV

Results – Spatial distribution

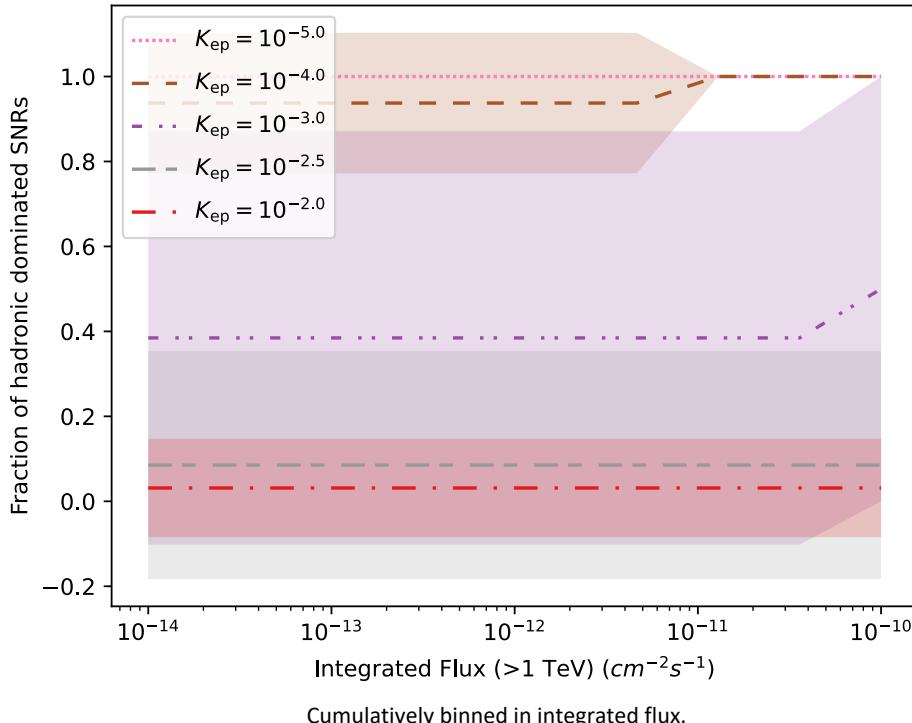


Results – Maximum length of Sedov-Taylor phase

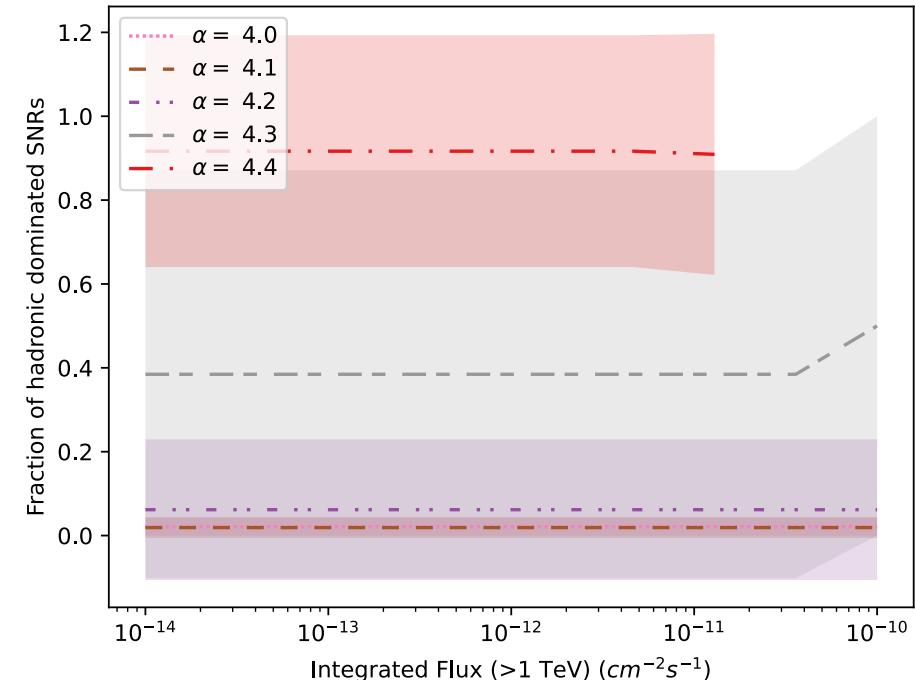


Ratio of detectable sources dominated by hadronic emission

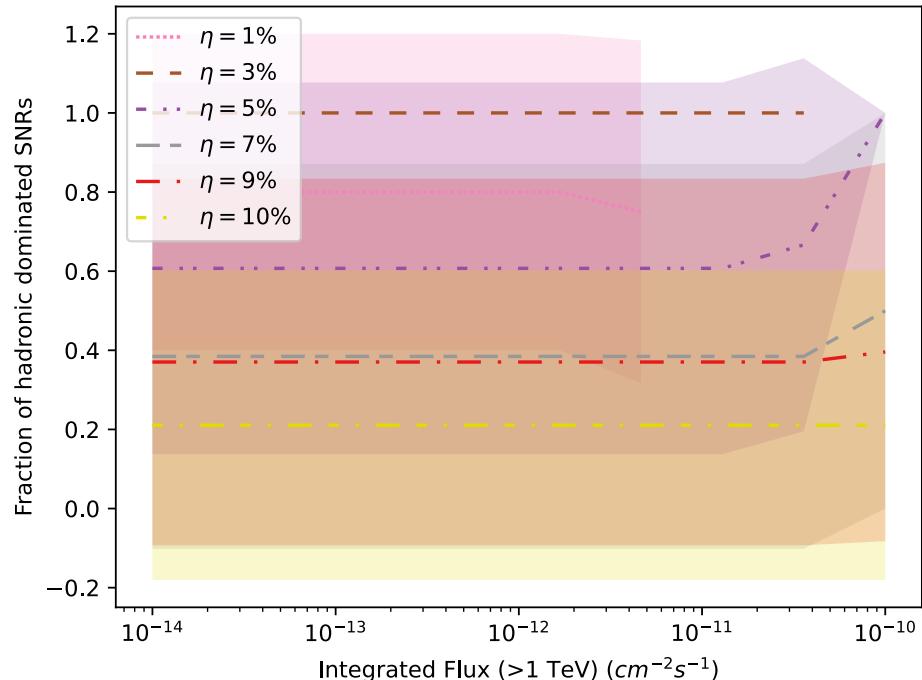
- As the electron-proton fraction increases the hadronic fraction decreases
- Is this the only property that changes the hadronic ratio?



Ratio of detectable sources dominated by hadronic emission

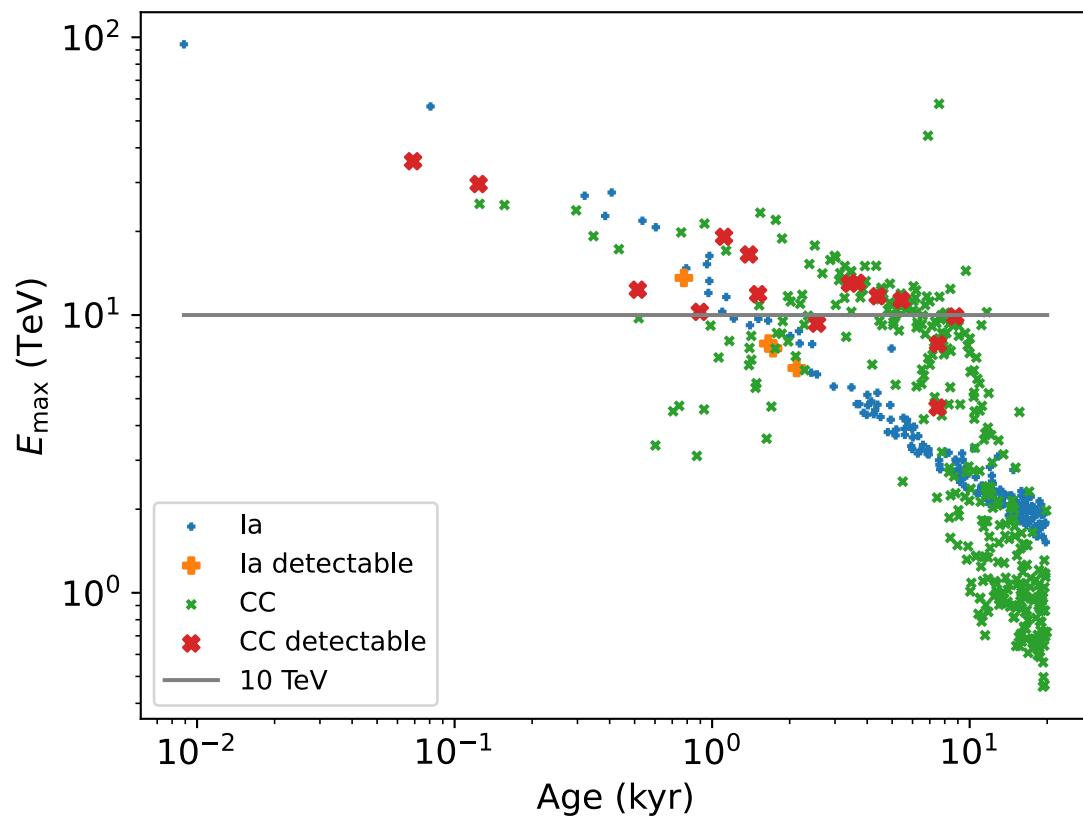


Cumulatively binned in integrated flux.



Cumulatively binned in integrated flux.

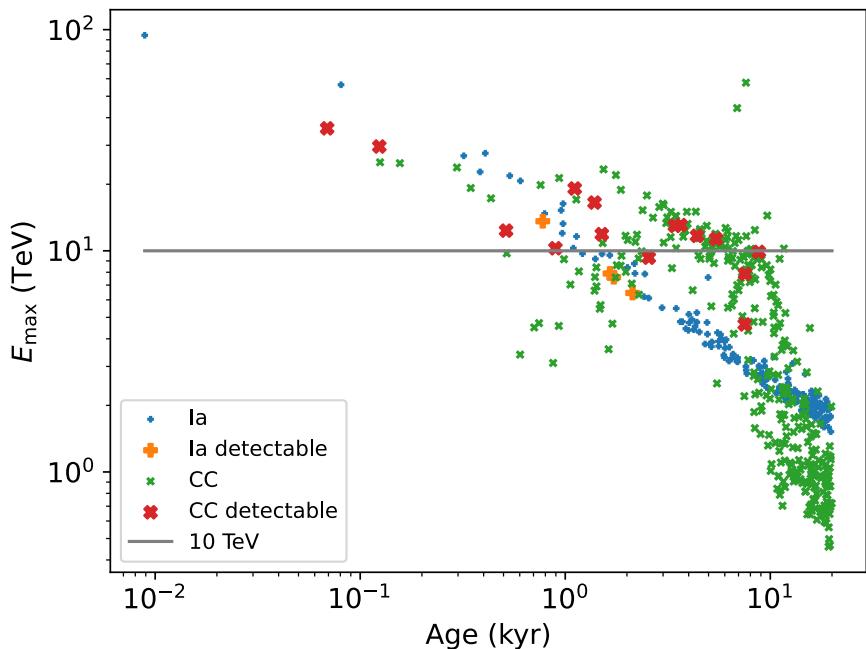
Additional E_{\max} criterion



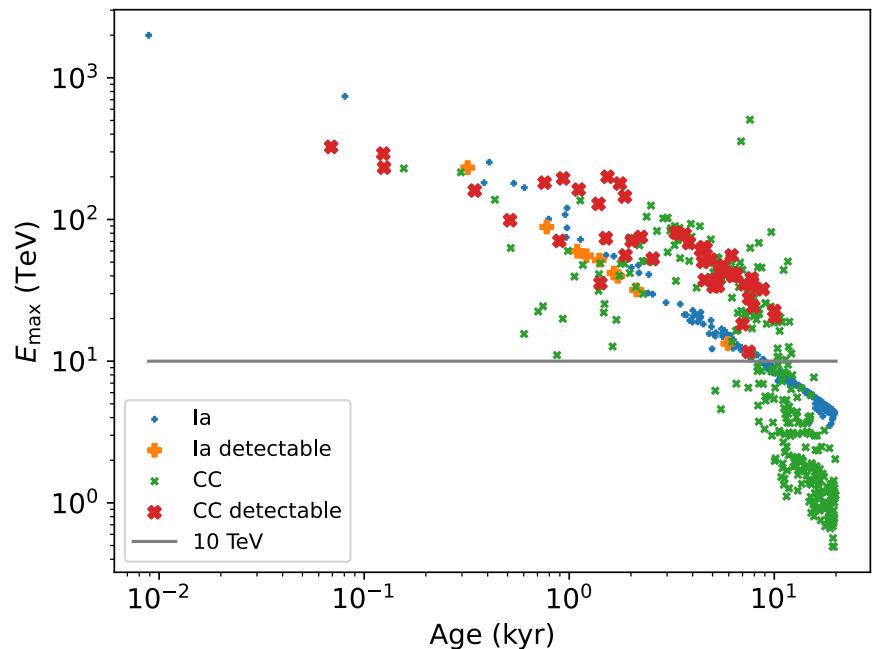
Maximum energy of particles

Parameters:
 $\alpha = 4.2$
 $K_{\text{ep}} = 10^{-5}$
 $\eta = 0.09$
 $ST = 20 \text{ kyr}$
 Steiman-Cameron

Bell

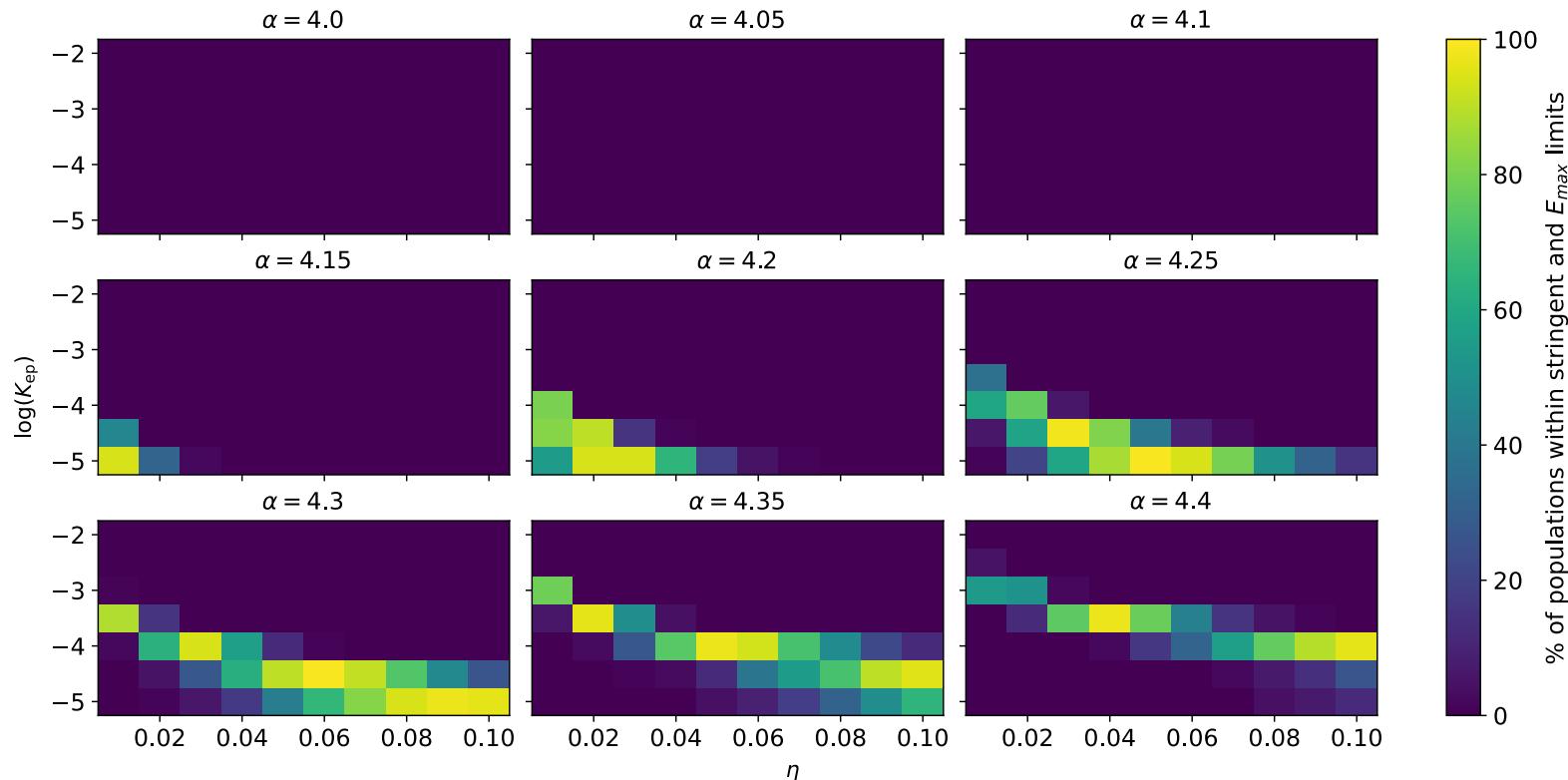


Hillas



Results – Parameter exploration (Hillas)

- $\alpha < 4.15$ and $K_{\text{ep}} > 10^{-3}$ means too many detectable SNRs
- None of the populations within the stringent are excluded by the E_{max} limit



Radius and luminosity distributions

