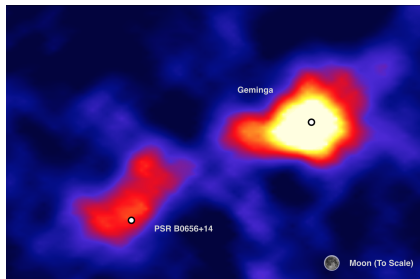


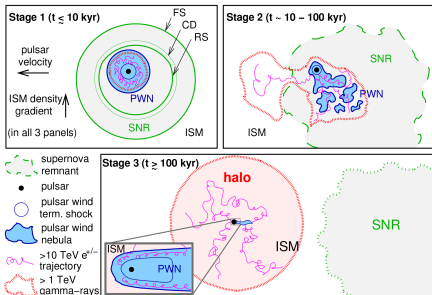
# The environment of pulsar halo progenitors

Lioni-Moana Bourguinat  
Carmelo Evoli, Pierrick Martin, Sarah Recchia

# TeV Halos



**Figure:** HAWC sky map of TeV emission from Geminga and its neighbour PSR B0656+14.  
Credits: HAWC Collaboration



**Figure:** Sketch of the main evolutionary stages of a pulsar wind nebula.  
Credits: Giacinti et al. (2020)

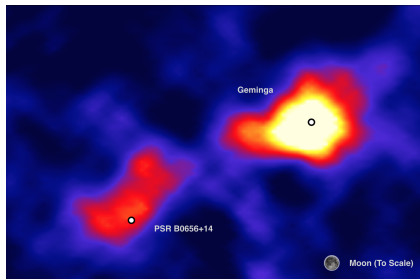


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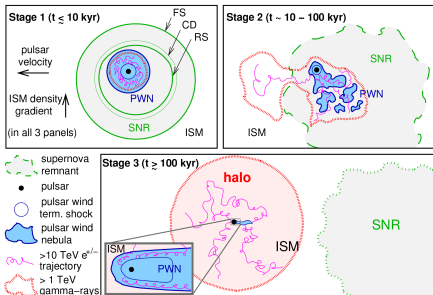


Figure: Sketch of the main evolutionary stages of a pulsar wind nebula.  
Credits: Giacinti et al. (2020)

## Standard assumption

Pulsar **outside** the SNR → Low diffusion coefficient problem [Abeysekera et al. (2017)]

## Theoretical explanations

- Cosmic-ray induced turbulence [[Evoli et al. \(2018\)](#), [Mukhopadhyay et al. \(2022\)](#)]
- **Environment induced turbulence** [[Fang et al. \(2019\)](#), [Schroer et al. \(2022\)](#)]

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Which medium are the leptons probing when we see a TeV halo?

**Where is the pulsar at a given age?**

## Method

Computation of the escape time from the SNR of a population of pulsars using a Monte Carlo approach for 3 models:

- ISM (interstellar medium)
- CSM (circumstellar medium)
- SB (superbubble)

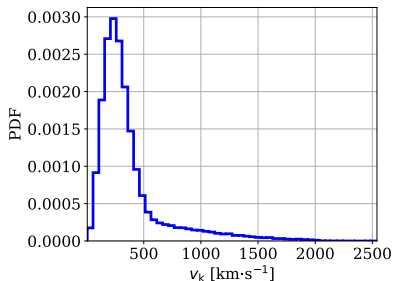
# Property of the pulsars: Kick velocity

## Kick velocity distribution

Taken from [Faucher-Giguère et al. \(2006\)](#), modulus of all components:

$$f(v_k^{x,y,z}) = w \mathcal{N}(v_k, \sigma = 160 \text{ km/s}) + (1 - w) \mathcal{N}(v_k, \sigma = 780 \text{ km/s}) \quad (1)$$

with  $w = 0.90$ .



**Figure:** PDF of the kick velocity of pulsars.



## Assumptions

- **Constant interstellar medium** around the CC SN
- Distributions of  $E_{\text{SN}}$  and  $n_{\text{ISM}}$

## Assumptions

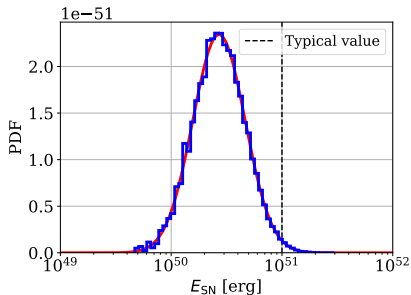
- **Constant interstellar medium** around the CC SN
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## SNR evolution

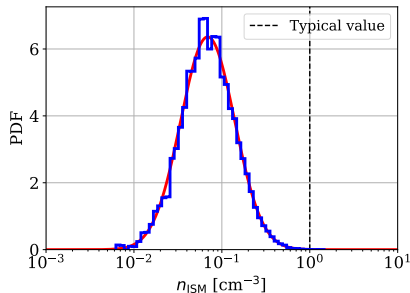
Analytical solutions following [Cioffi et al. \(1988\)](#), compared with the calculator by [Leahy and Williams \(2017\)](#):

- Sedov-Taylor phase
- Pressure-Driven Snowplough phase
- (Momentum Conserving Stage)
- Merger with the ISM

# ISM model: SN energy and ISM density



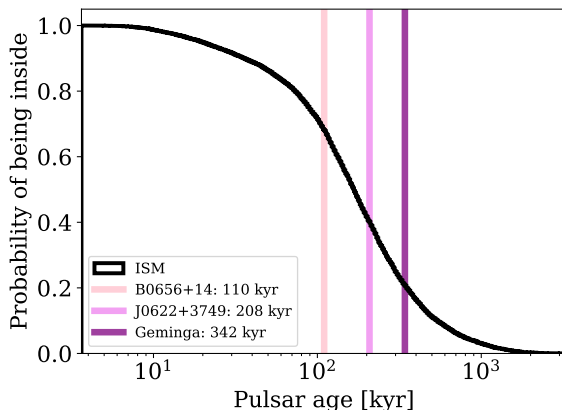
(a) Effective  $E_{\text{SN}}$  PDF,  $\mu = 2.7 \times 10^{50}$  erg,  $\sigma = 3.5$



(b) Effective  $n_{\text{ISM}}$  PDF,  $\mu = 0.069$   $\text{cm}^{-3}$ ,  $\sigma = 5.1$

**Figure:** Lognormal distributions, following [Leahy, Ransinghe, et al. \(2020\)](#). Computed by assuming a constant ISM density surrounding each of 43 SNe.

# ISM model: Escape time



**Figure:** Probability of pulsars being inside the **SNR** as a function of time for the **ISM** model. Characteristic ages of pulsars are orders of magnitude, taken from the catalog of [Manchester et al. \(2005\)](#).

## Assumptions

- CC SN happens in the **circumstellar medium** shaped by the progenitor

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## Process

- Pick a random **progenitor mass** from a Galactic Initial Mass Function (IMF),
- **Star properties** [Seo et al. (2018)],
- **Bubble properties** [Weaver et al. (1977), Härer et al. (2023)].

Neglecting post-MS phases for the wind and bubble structure.

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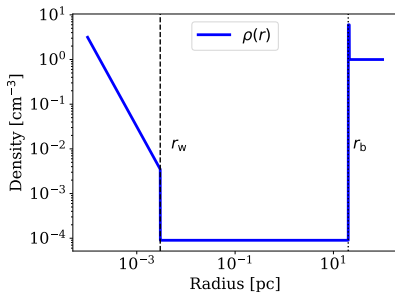


Figure: Density profile in the CSM, based on Weaver et al. (1977).

# CSM model: Comparing the shell mass and the SNR mass

Parameters for a star of

$$M_{\text{ZAMS}} = 8 M_{\odot}$$

- Bubble radius  $r_b = 20 \text{ pc}$ ,
- Surrounding ISM density of  $n_{\text{ISM}} = 1 \text{ cm}^{-3}$ ,
- Mass lost in winds  
 $\Delta M_{\text{MS}} = 0.1 M_{\odot}$  and  
 $\Delta M_{\text{RSG}} = 3.4 M_{\odot}$ ,
- Ejecta mass is  
 $M_{\text{ZAMS}} - \Delta M_{\text{MS}} - \Delta M_{\text{RSG}} -$   
 $M_{\text{pulsar}} = M_{\text{ej}} = 3.1 M_{\odot}$ ,
- Mass swept in the bubble by the SNR is the mass lost in winds.



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- Ejecta mass is  $M_{\text{ZAMS}} - \Delta M_{\text{MS}} - \Delta M_{\text{RSG}} - M_{\text{pulsar}} = M_{\text{ej}} = 3.1 M_{\odot}$ ,
- Mass swept in the bubble by the SNR is the mass lost in winds.

## Computations

$$M_{\text{shell}} = \frac{4\pi}{3} \rho_{\text{ISM}} r_b^3 = 755 M_{\odot} \quad (2)$$

Mass ratio:

$$\frac{M_{\text{shell}}}{M_{\text{ej}} + \Delta M} = 116 \quad (3)$$

**Shell stops the expansion** of the SNR

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**Shell stops the expansion** of the SNR

## Conclusion

**Boundary: bubble radius** instead of the SNR

## Assumptions

- Point-like cluster surrounded by a **superbubble** [Weaver et al. (1977)]
- Ambient density of  $n_{\text{ISM}} \sim 100 \text{ cm}^{-3}$  [Parizot et al. (2004)]
- The SNR is very fast and merges within the SB [Mac Low et al. (1988)]

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- The SNR is very fast and merges within the SB [Mac Low et al. (1988)]

## Process

Pick a **random cluster mass** following a cluster IMF [Portegies Zwart et al. (2010)].

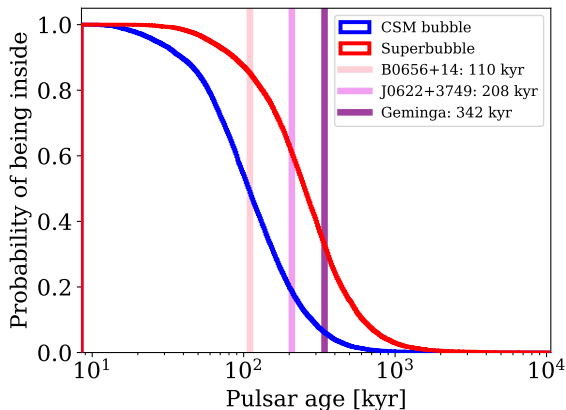
**Populate with stars** following the Galactic IMF.

Compute the **cluster luminosity** and SB radius [Weaver et al. (1977), Härer et al. (2023)].

Pick a **random massive star** and find the associated MS time [Seo et al. (2018)].

**Creation of a pulsar** at the MS time and propagation of both pulsar and SB radius.

# Comparing the probability of being inside the boundary



**Figure:** Probability of pulsars being inside the **bubble/SB** as a function of time for the **CSM/SB models** respectively.

# Some numbers

Pulsar	Age [kyr]	Inside (CSM, 4% <sup>1</sup> )	Inside (SB, 96% <sup>1</sup> )
B0656+14	110	49%	85%
J0622+3749	208	19%	61%
Geminga	342	6%	33%

---

<sup>1</sup>of O stars[de Wit et al. (2005)]

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## More on Geminga

Hints that Geminga is in a hot ionized medium:

- No  $H_{\alpha}$  lines in the near vicinity [Caraveo et al. (2003)]
- Proximity to Gemini  $H_{\alpha}$  Ring bubble [Knies et al. (2018)]

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## Main questions

Which medium are the leptons probing when we see a TeV halo?

Where is the pulsar at a given age?



## Main questions

Which medium are the leptons probing when we see a TeV halo?  
Where is the pulsar at a given age?

## Conclusions

- Typically assumed:  $\sim 50$  kyr and probe the ISM.
- We find instead a majority of  $\gtrsim 100$  kyr pulsars are inside the **CSM/SB**.
- Are Geminga and PSR B0656+14 in a **hot and turbulent** environment?
- How are CSM/SB connected to **TeV halos**?

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# CSM model

Theoretical framework for the SNR shock

## Time (Numerically integrated)

$$t(R_s) = \int_0^{R_s} \frac{1}{u_s(r)} dr \quad (4)$$

## Speed (Analytical)

$$u_s(R_s) = \frac{\gamma + 1}{2} \left[ \frac{2\alpha E_{SN}}{M^2(R_s) R_s^\alpha} \times \int_0^{R_s} r^{\alpha-1} M(r) dr \right] \quad (5)$$

with  $\alpha = 6(\gamma - 1)/(\gamma + 1)$ .

## Mass (Analytical)

$$M(r) = M_{ej} + 4\pi \int_0^r r'^2 \rho(r') dr' \quad (6)$$

# CSM model

## Density profile

The numbers (model from Weaver et al. (1977))

Wind region ( $R_s < r_w$ ):

$$\rho_w(R_s) = \frac{\dot{M}}{4\pi u_w R_s^2}$$

Bubble region ( $r_w < R_s < r_b$ ):

$$\rho_b(R_s) = \rho_b$$

Shell region ( $r_b < R_s < r_{\text{ISM}}$ ):

$$\rho_{\text{shell}} = \frac{M_{\text{shell}}}{V_{\text{shell}}} = \frac{\frac{4\pi}{3} r_b^3 \rho_{\text{ISM}}}{\frac{4\pi}{3} (r_{\text{ISM}}^3 - r_b^3)}$$

ISM region ( $r_{\text{ISM}} < R_s$ ):

$$\rho_{\text{ISM}} = 1 \text{ cm}^{-3}$$

# CSM model

Looking at all the distributions

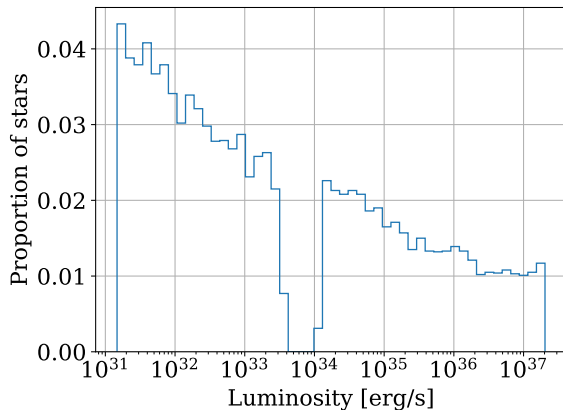


Figure: Luminosity distribution.

# CSM model

Looking at all the distributions

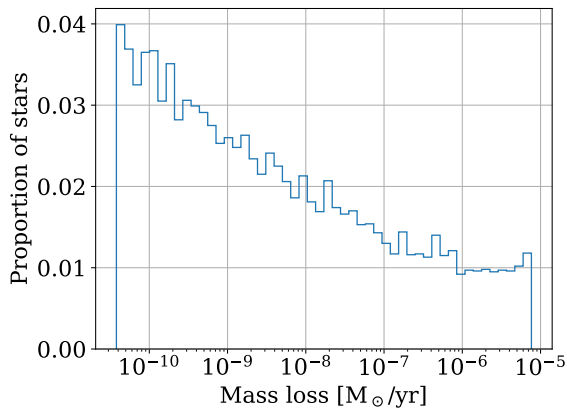


Figure: Mass loss distribution.



# CSM model

Looking at all the distributions

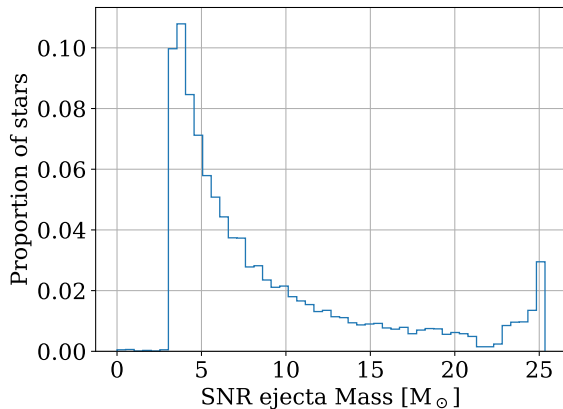


Figure: SNR ejecta mass distribution.

# CSM model

Looking at all the distributions

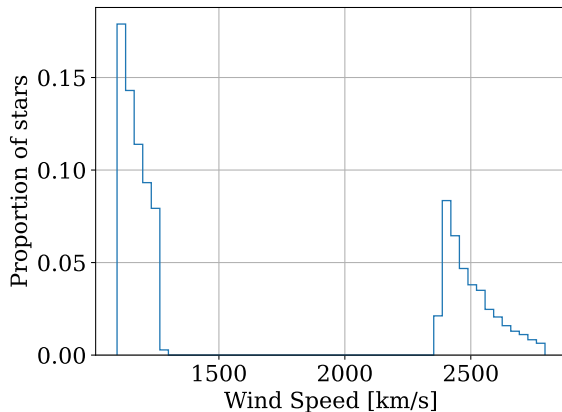


Figure: Wind speed distribution.

# CSM model

Looking at all the distributions

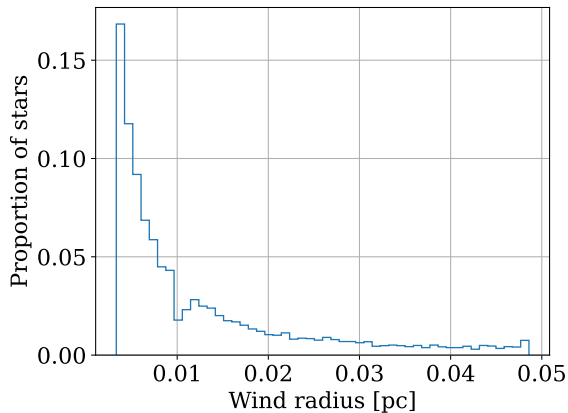
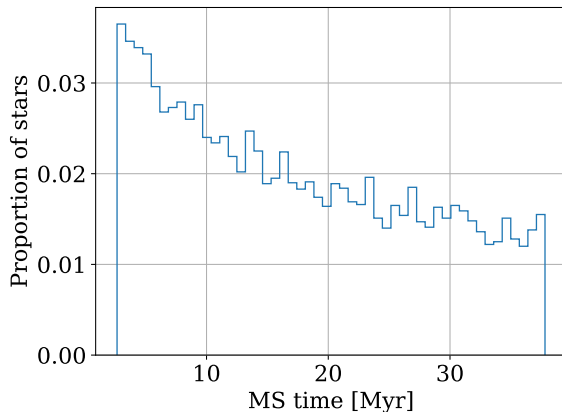


Figure: Wind radius distribution.

# CSM model

Looking at all the distributions



**Figure:** Main sequence time distribution.

# CSM model

Looking at all the distributions

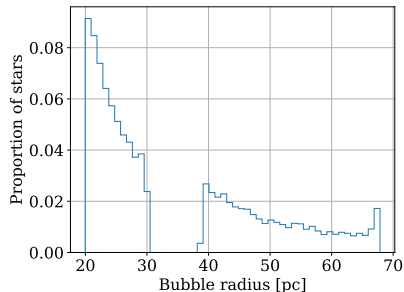


Figure: Bubble radius distribution.

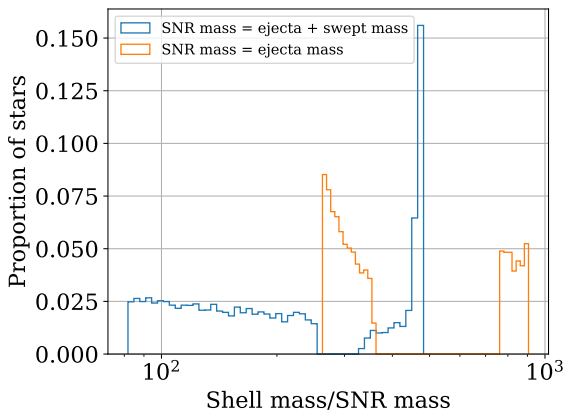
## Formula

From Weaver et al. (1977) and Härer et al. (2023):

$$r_b = 21 \text{ pc } \zeta_b^{1/5} L_{36}^{1/5} n_{\text{ISM},1}^{-1/5} t_6^{3/5} \quad (7)$$

# CSM model

Looking at all the distributions



**Figure:** Shell mass/SNR mass distribution. We show for both the ejecta mass and the swept mass. Naturally, the swept mass is higher than the ejecta mass, resulting in a lower (by less than an order of magnitude) ratio. The shape in two parts of the orange curve is linked to the shape of the bubble radius (which is the determining factor for the parameter).

# CSM model

## Density profile

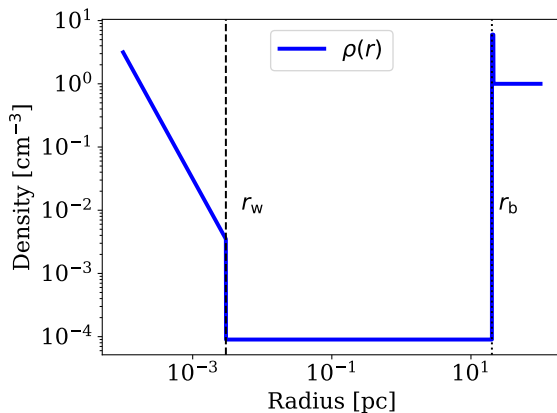
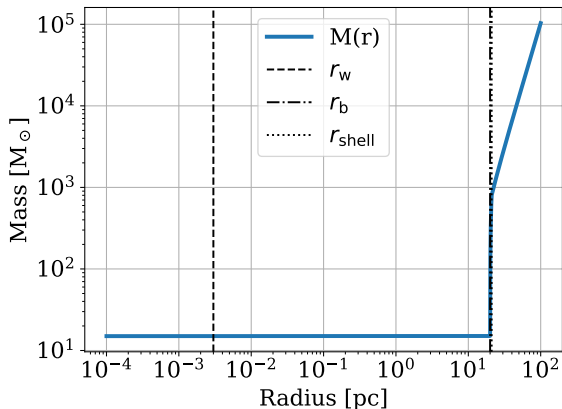


Figure: Density profile in the CSM, based on [Weaver et al. \(1977\)](#).

# CSM model

## Mass profile

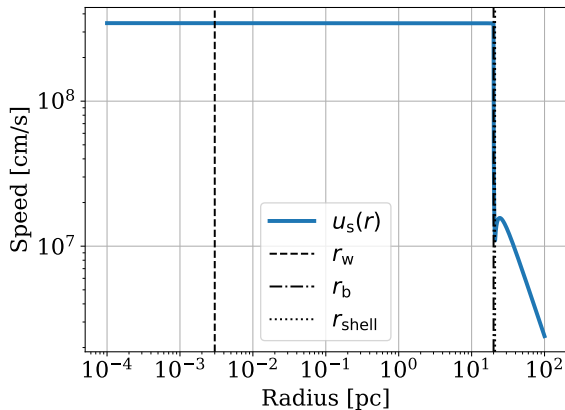


**Figure:** Accumulated mass profile in the CSM, analytically computed from the density profile



# CSM model

## Speed profile



**Figure:** Accumulated speed profile in the CSM, analytically computed from the mass profile

### Radiative phase

$$t_{\text{rad}} = \frac{3}{2} \frac{k_b T}{n \Lambda(T)}$$

with  $\Lambda(T) = 1.6 \times 10^{-19} T^{-1/2}$  erg/cm<sup>3</sup>/s. We always go radiative when reaching the shell.

### Merger with the bubble shell

$$u_s(R_s) = \beta c_{\text{sound}}(T(R_s))$$

with  $\beta = 3$  and the speed of sound  $c_{\text{sound}}$  depending on the temperature profile found in [Weaver et al. \(1977\)](#). Since the SNR stops inside the shell, it merges there.

# SB model

Looking at all the distributions

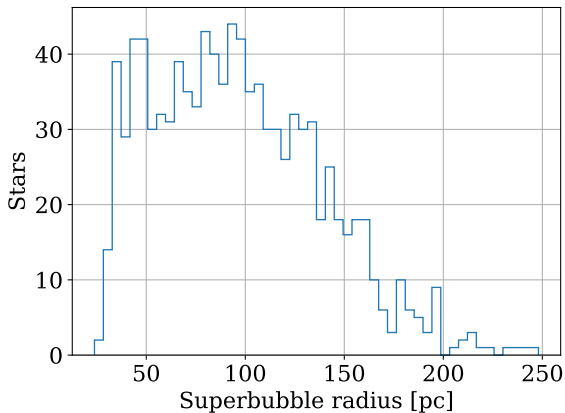
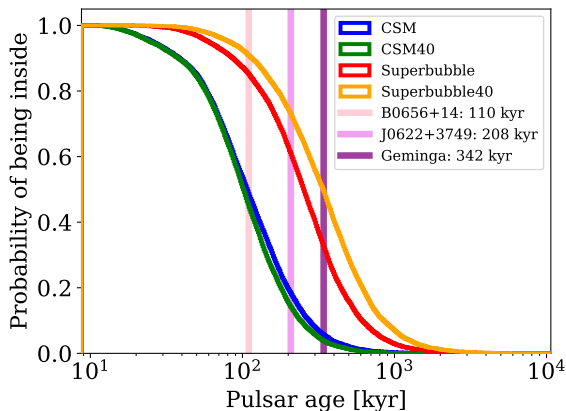


Figure: Superbubble radius distribution.

# Comparing the probability of being inside the boundary

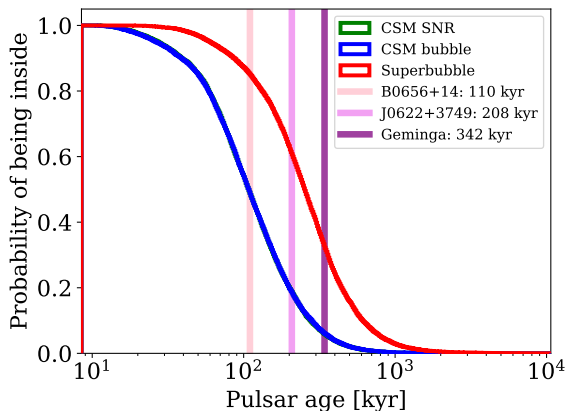
Changing the maximum star mass



**Figure:** Probability of pulsars being inside the bubble/SB as a function of time for the CSM/SB models respectively. Two curves are added by changing the maximum mass of massive stars that create pulsars from 150  $M_{\odot}$  to 40  $M_{\odot}$  following [Sukhbold et al. \(2016\)](#).

# Comparing the probability of being inside the boundary

Special case: exiting the SNR inside the bubble



**Figure:** Probability of pulsars being inside the bubble/SB as a function of time for the CSM/SB models respectively. The green curve corresponds to the escape time of pulsars from the SNR inside the CSM.