Electro-Optic Sampling for Bunch Length Measurement

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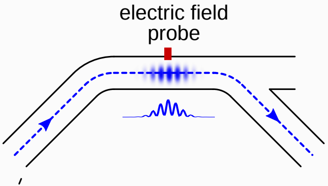
How to record the electron bunch shape ?

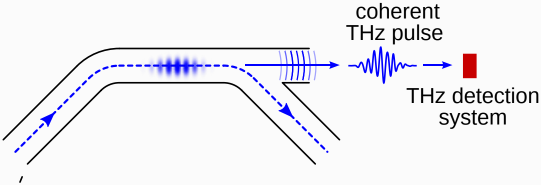
→ probe its electric field…

… in the near-field (NF)



- ☺/☹ crystal near the e- bunch
  - ☺ "very direct" measurement, access to the whole e-field
  - ☺ intense electric field

… or in the far-field (FF)



- ☺ detection far from the e- bunch
- ☺/☹ "high-pass" filter, only access to fast-evolving component
- ☹ less intense field (V-kV/cm)

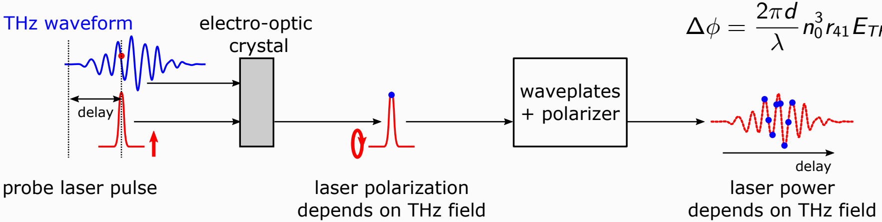
In both cases, need for:

(1) few ps/sub-ps resolution; (2) single-shot; (3) MHz+ acquisition rate

Electro-optic sampling of electric field: principle

Simple cross-correlation of the THz and optical pulses based on the **Pockels effect**:

- An external electric field modifies the refractive indexes of a birefringent crystal (EO crystal).
- The THz-induced birefringence is probed using a laser pulse.
- ▷ Multi-THz bandwidth obtained: limited by crystal speed and laser pulse duration.

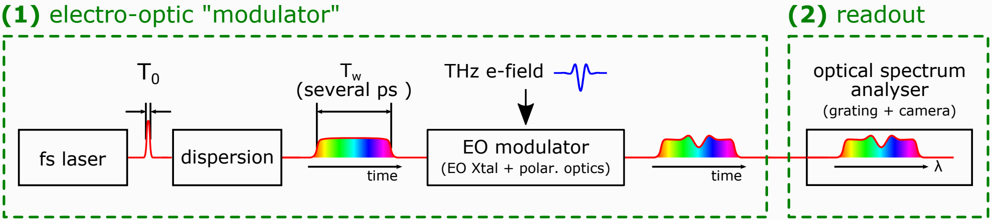


$$\Delta\phi = \frac{2\pi d}{\lambda} n_0^3 r_{41} E_{THz}$$

Free-propagating THz pulses (Time-domain spectroscopy, TDS): [Q. Wu & X.-C. Zhang, Appl. Phys. Lett. **67** (24), (1995)]
Scanned EO in accelerators: [Wilke et al., Phys. Rev. Lett. 88, 124801 (2002)], [Katayama et al., App. Phys. Lett. 100, 111112 (2012)]

Single-shot recording ? → using chirped laser pulses

Principle: time-to-wavelength mapping (aka **spectral decoding**)



First demonstration using OSA readout: [Z. Jiang & X.-C. Zhang, Appl. Phys. Lett., **72**, 1945 (1998)]

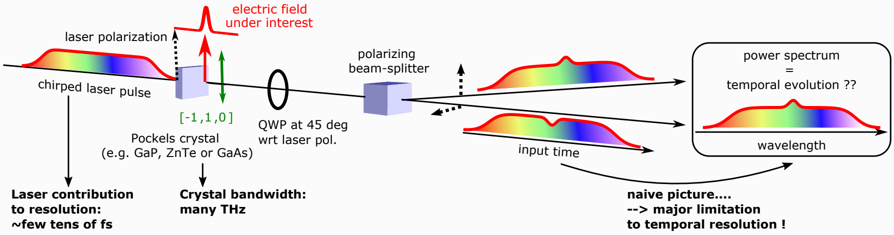
Applications in accelerators: [Müller et al., Phys. Rev. ST Accel. Beams 15, 070701 (2012)], [Hiller et al., IPAC'13, p. 500 (2013)]

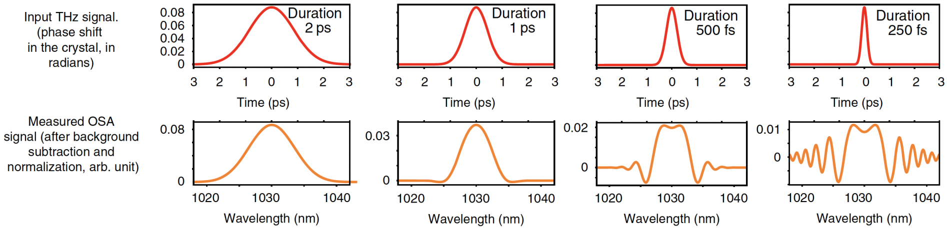
Potential applications:

- **Monitoring non-repetitive phenomena**, e.g. in accelerators
- **Time Domain Spectroscopy** in situations where scanning is unpractical:
  - for monitoring fast irreversible processes
  - for non linear THz science using high-power THz sources (with low repetition rate)

(20-year-old) Temporal resolution issue: the "time × bandwidth" limit (1)

Time-resolution limitation (20-year-old problem) [Sun, Jiang & Zhang, Appl. Phys. Lett. **73**, 2233 (1998)]



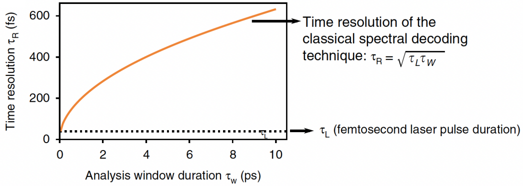


Temporal resolution issue: the "time × bandwidth" limit (2)

Time-resolution (assuming an infinitely fast crystal) [Sun, Jiang & Zhang, Appl. Phys. Lett. **73**, 2233 (1998)]

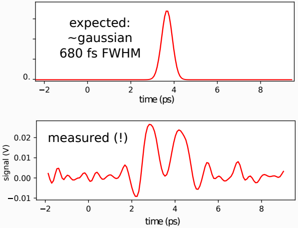
$$\tau = \sqrt{t_{laser} \times t_{window}}$$

Example: $t_{laser} = 100\ fs$, $t_{window} = 10\ ps$ $\rightarrow \tau = 1\ ps \gg t_{laser}$ ☹

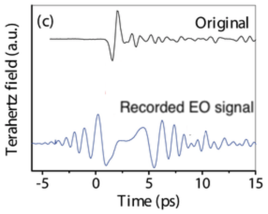


Examples of temporal resolution issue

- **at short timescales** e.g. e-bunch near field at EuXFEL

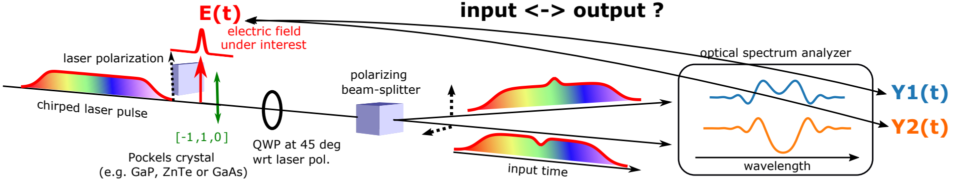


- **for long observation windows** e.g. TDS



[Murakami, doi: 10.5772/67195 (2017)]

A new point of view: calculation of Fourier-domain transfer functions



Derivation of the transfer functions

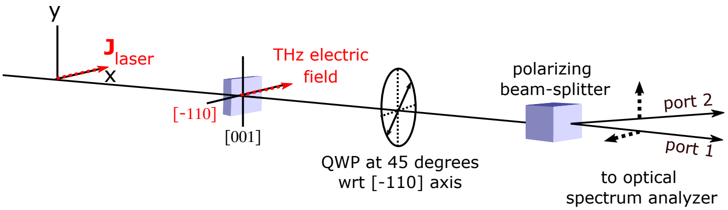
$$\text{Input field} \quad E(t) \quad \leftrightarrows \quad \tilde{E}(\Omega)$$
$$\text{Measurements} \quad Y_{1,2}(t) \quad \leftrightarrows \quad \tilde{Y}_{1,2}(\Omega) \approx H_{1,2}(\Omega) \times \tilde{E}(\Omega)$$

with $H_{1,2}(\Omega) = h_{1,2} \cos\left(B\Omega^2 + \phi_{1,2}\right)$, the transfer functions !

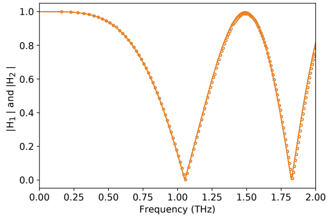
$h_{1,2}$, $\phi_{1,2}$ depend on the crystal and waveplates orientation, $B = 1/2C$ with $C = \partial\omega/\partial t$ the laser chirp.

calculation details in [Roussel et al., Light Sci Appl **11**, 14 (2022)]

"Classical" EO configuration



transfer functions



Transfer functions $H_{1,2}$ for the "classical" crystal & waveplates orientations

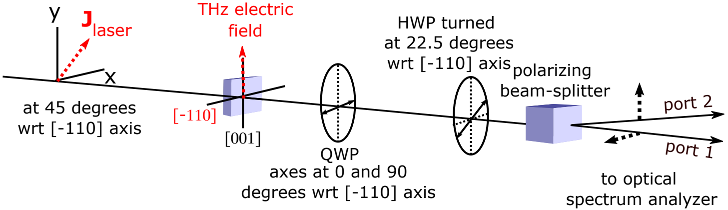
$$H_1(\Omega) = \cos\left(B\Omega^2\right)$$

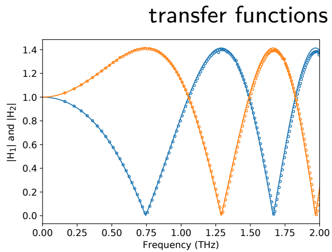
$$H_2(\Omega) = -\cos\left(B\Omega^2\right)$$

- clear existence of **zeros** at particular frequencies
  problem ill-posed → "deconvolution" impossible using one channel
- "classical" EO configuration: zeros of H_1 and H_2 at the same frequencies

→ find an other configuration to separate the zeros ?

Our strategy: Diversity Electro-Optic Sampling (DEOS)





Goal: interleave the zeros of transfer functions

$$H_1(\Omega) = \sqrt{2}\cos\left(B\Omega^2 + \frac{\pi}{4}\right)$$

$$H_2(\Omega) = -\sqrt{2}\cos\left(B\Omega^2 - \frac{\pi}{4}\right)$$

- in practice: crystal and waveplates orientation $\neq$ "classical" EO
- problem well-posed $\rightarrow$ "deconvolution" possible using the two channels

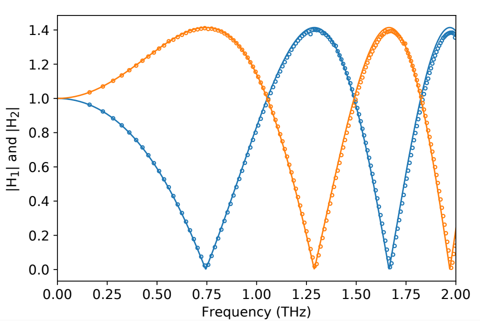
Algorithm for input field reconstruction: Maximum Ratio Combining (MRC)

Simple approach: retrieve the input field $\tilde{E}$ from the measured EO signals $\tilde{Y}_{1,2}$ using either

$$\tilde{E}_R(\Omega) = \frac{\tilde{Y}_1(\Omega)}{H_1(\Omega)} \quad \text{or} \quad \tilde{E}_R(\Omega) = \frac{\tilde{Y}_2(\Omega)}{H_2(\Omega)} \quad \text{depending on frequency } \Omega$$

Refined algorithm

Use a combination of the two EO signals $\tilde{Y}_{1,2}$ with **optimal** weights

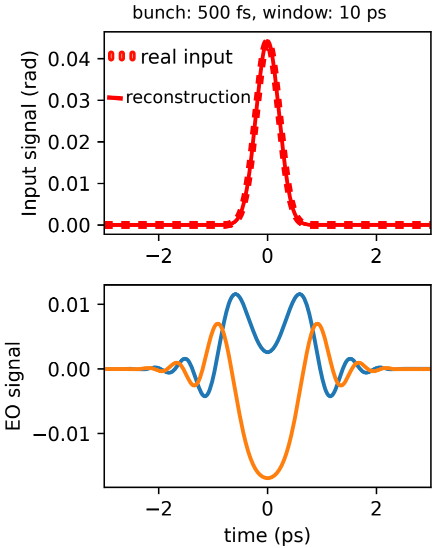


Maximum Ratio Combining (MRC) method:

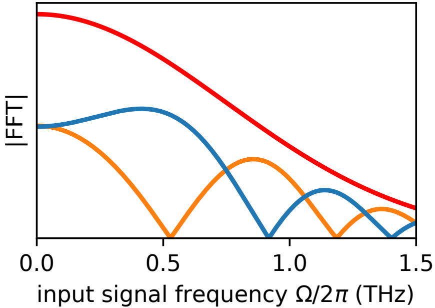
$$\tilde{E}_R = \frac{H_1 \tilde{Y}_1 + H_2 \tilde{Y}_2}{|H_1|^2 + |H_2|^2}$$

Inspired by: [Han, Boyraz & **Jalali**, Microwave Theory and Techniques, IEEE Transactions on **53**, 1404-1408 (2005)]

Reconstruction algorithm: numerical test

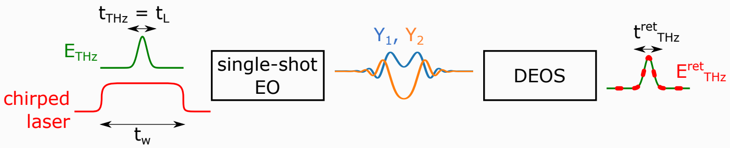


- ~~Old limitation~~ $\cancel{\tau = \sqrt{t_{laser} \times t_{window}}}$
- New resolution limit $\tau \sim t_{laser}$?
- Time window t_{window}: no limit (theoretically)

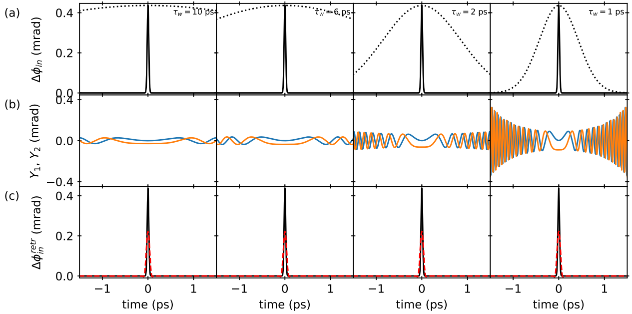


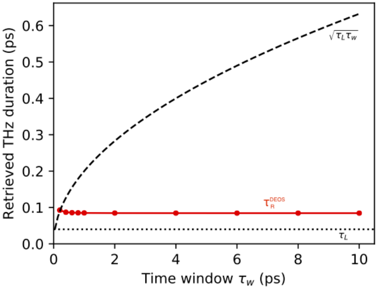
Time resolution of DEOS

Time resolution of DEOS: $\tau_R^{DEOS} \equiv \tau_{THz}^{retrieved}$ when $\tau_{THz} = \tau_L$



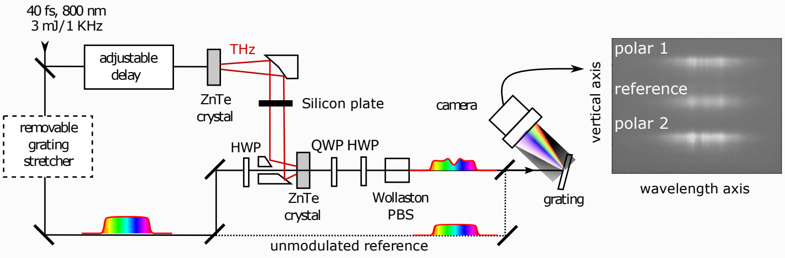
DEOS reconstruction versus time window τ_w:



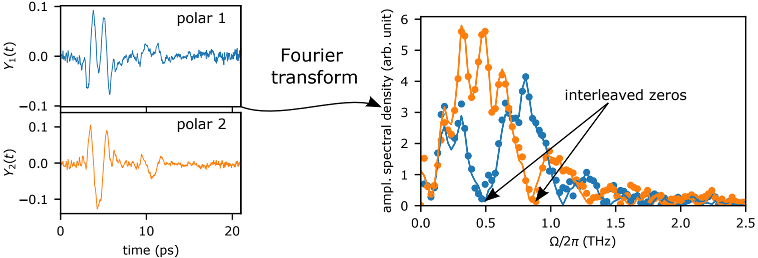


Experimental investigations using a table-top experiment

Terahertz signal generated by optical rectification of laser pulses

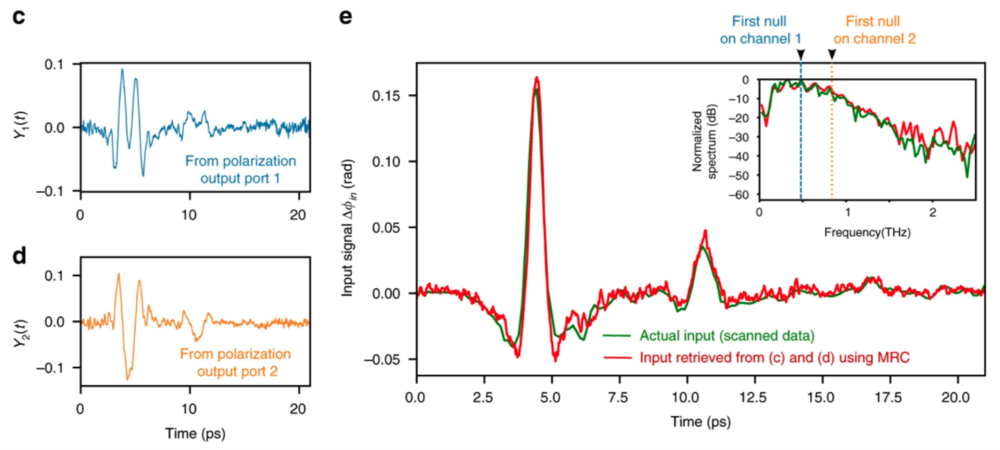


Computed EO signals:



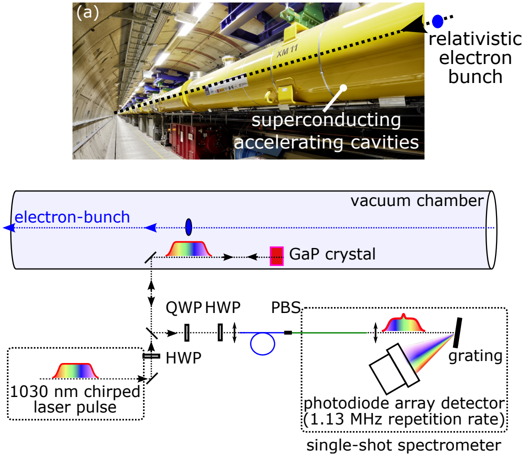
Comparison between DEOS and scanned EOS

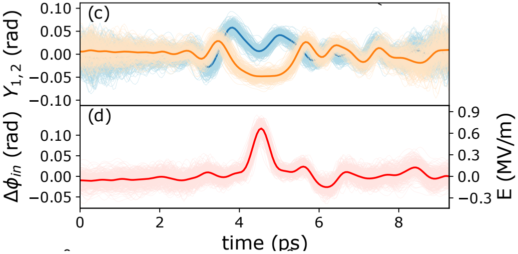
Reconstructed single-shot THz signal vs reference signal (obtained with scanned EOS)



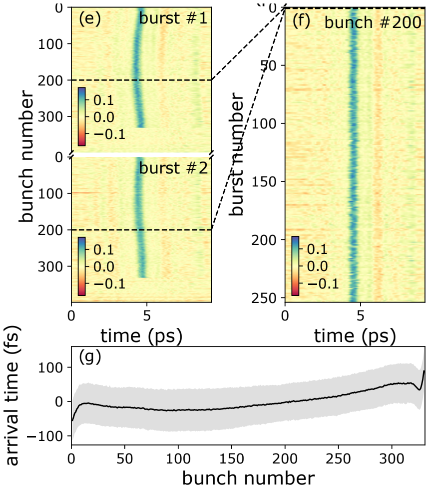
[Roussel et al., Light Sci Appl **11**, 14 (2022)]

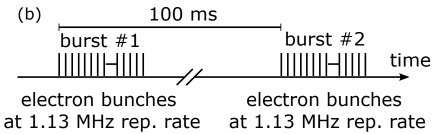
Studies of e-bunch shapes at the European XFEL





Preliminary results at the European XFEL





Train of 300 e-bunches over 250 bursts.

- bunch duration: $\sim$ 218 fs RMS
- arrival time jitter: $\sim$ 58 fs

Conclusion

Diversity Electro-Optic Sampling (DEOS)

- High temporal resolution (limited by laser and crystal) for arbitrary long windows.
- Table-top proof-of-principle tests + preliminary experiment at EuXFEL (DESY).

Related projects in machine physics

- PhLAM/DESY project: investigate DEOS + photonic time-stretch readout
- PhLAM/FERMI: TeraFERMI THz beamline (high power, low rep. rate source)
- PhLAM/KARA/SOLEIL (French-German ANR-DFG ULTRASYNC project).
- Feasibility studies at TELBE and FELBE.
- Advanced diagnostics for the European TWAC project (THz Waveguide Accelerating Cavity).

Other milestones

- High acquisition rate with photonic time-stretch readout.
- High sensitivity EOS.
- Cost reduction, using 1550 nm wavelength.

Fundings: CPER Photonics4Society, CEMPI, CNRS Momentum (METEOR), ANR/DFG (ULTRASYNC), EIC Pathfinder (TWAC).