



# Calibration of a Magnet used for Hall Probes Calibration in Mu2e Experiment

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# Introduction

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- Mu2e is an experiment with the goal of determining conversion properties of muons to electrons
- The magnetic field of the Detector Solenoid must be mapped with a precision of better than  $10^{-4}$  T
- Hall Probes will be used to map the field (3D) and Nuclear Magnetic Resonance (NMR) Probes to determine the absolute field value



Hall Probes need to be calibrated in the intended measurement range at a known homogeneous magnetic field much better than  $10^{-4}$  T



# Introduction

## Calibration Magnet

Field **homogeneity** much better than  $10^{-4}$  T in a region of **2 cm x 2 cm**

Field **stability** over time

needed for the Hall Probes calibration

**Main goal:** Meet the magnetic field requirements

Hard constraint: a lot of factors decrease the field homogeneity and stability, compared to the ideal case.

Pole skewness  
Hysteresis  
Field saturation

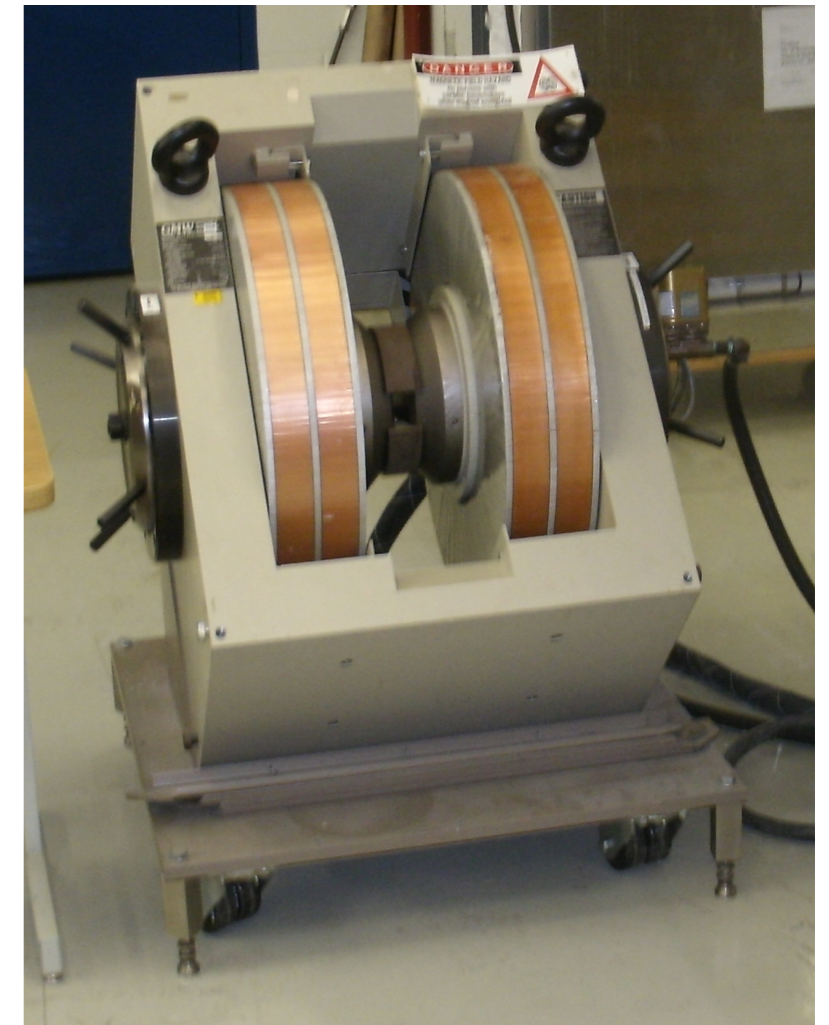
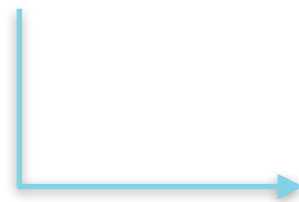
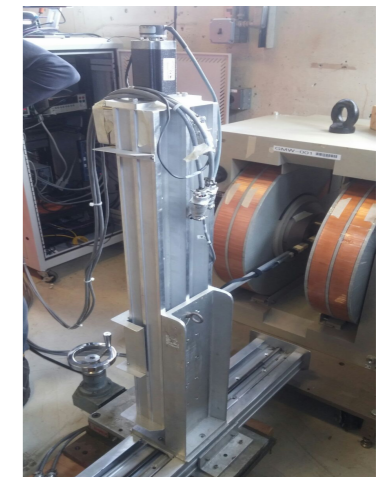
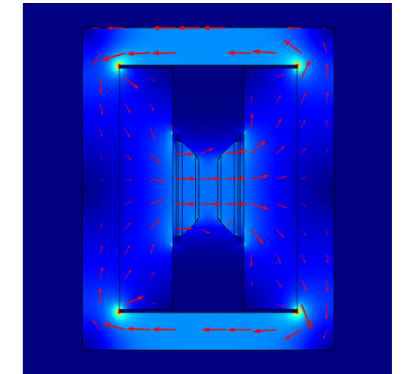
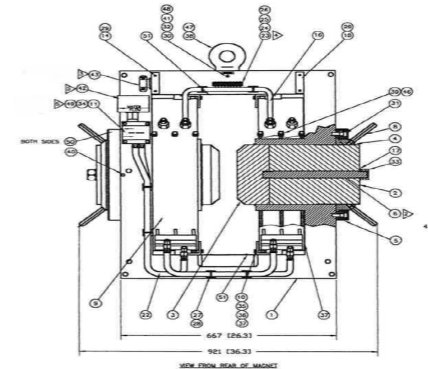


Fig.1. GMW 3474-140/280 250 mm Electromagnet.

# Introduction

How to reach the goal:

- ✓ Study the magnet design using the manual
- ✓ COMSOL simulations of the magnetic field generated by the magnet
- ✓ Field mapping using NMR Probes mounted on a 2 axis motion robot with LabVIEW interface.
- Shimming procedure to achieve a homogeneous field



- Shims are thin metal strips that adjust the field
- Iterative procedure

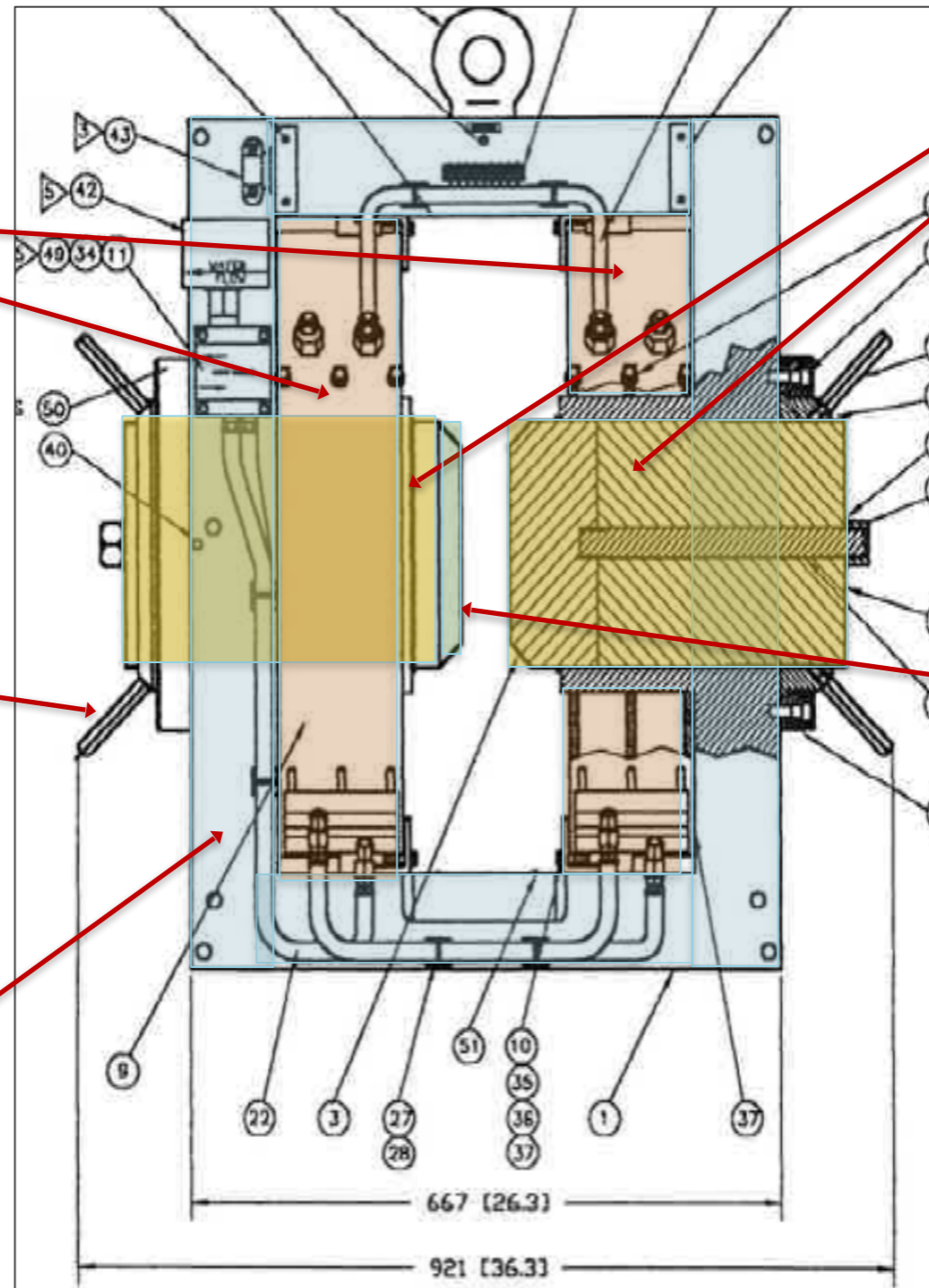


# Magnet Design

**Coils:**  
360 turns for each coil  
Coils are connected in parallel

**Handle**  
to adjust the pole gap in a range of 0 – 160 mm

**Yoke**



**Poles**  
250 mm diameter

**Pole cap**  
used to increase the magnetic field and the homogeneity

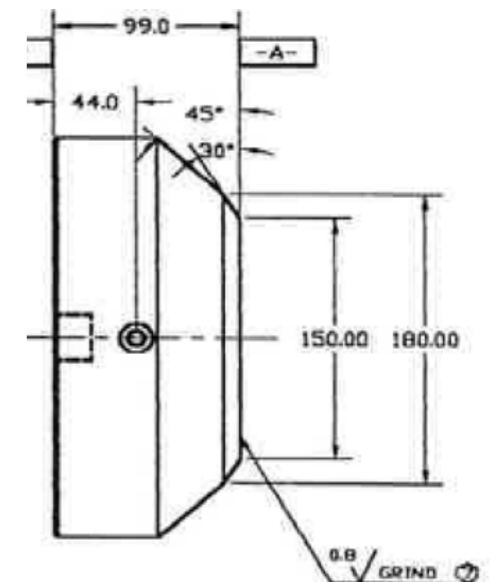


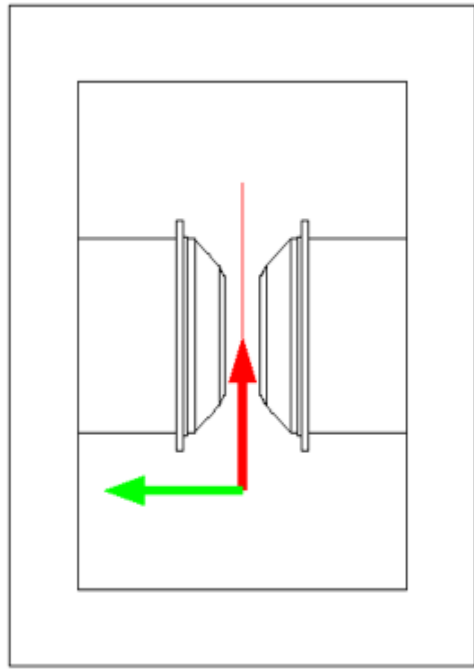
Fig.2. View from rear of magnet.

Fig.3. Pole Cap.

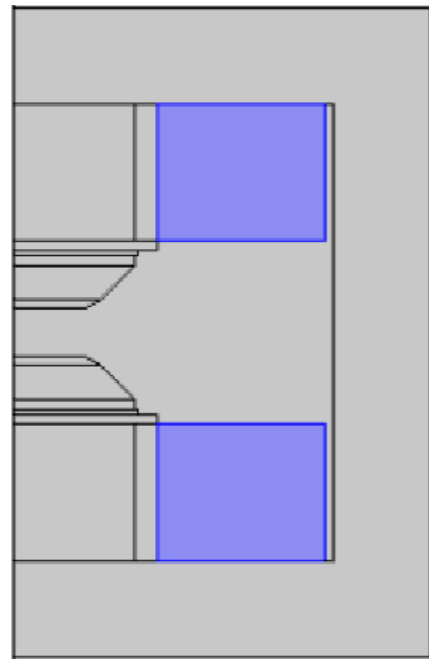
# COMSOL Simulations (Finite Element Method) - Models

## Models of the magnet

- 2D

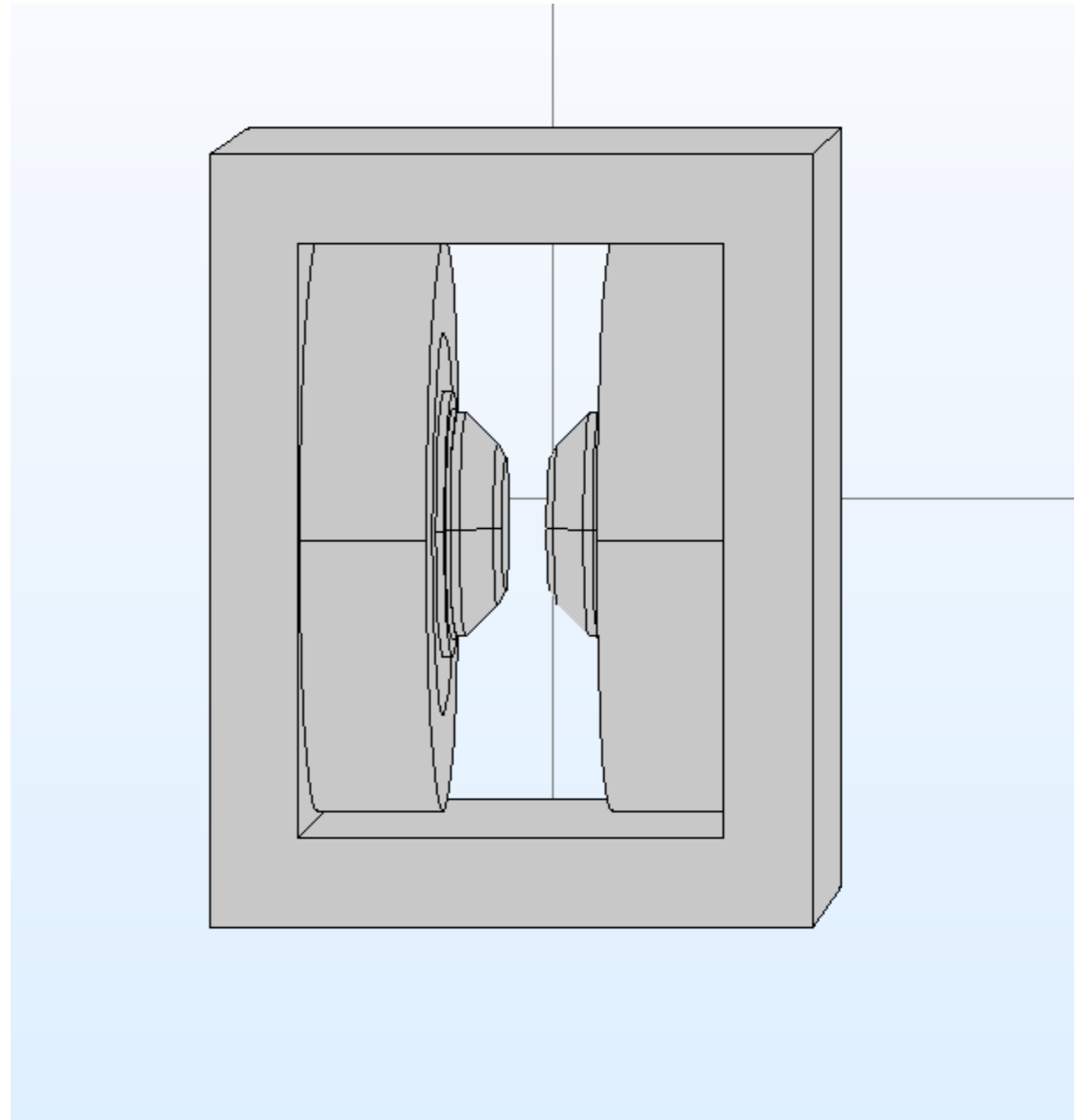


- 2D Axisymmetric



- more realistic **3D Model** →

- shape, dimensions and materials are taken from the manual





# COMSOL Simulations - Ideal Case

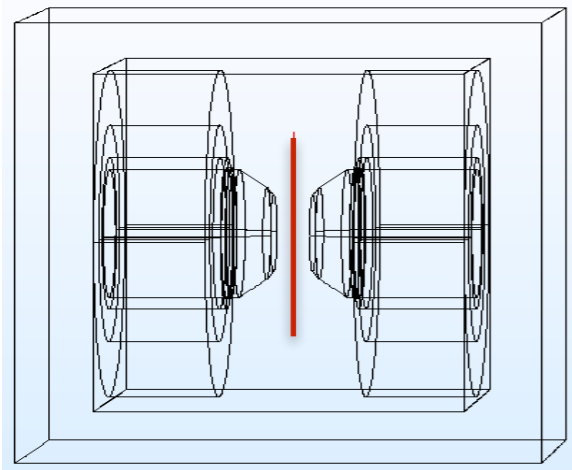
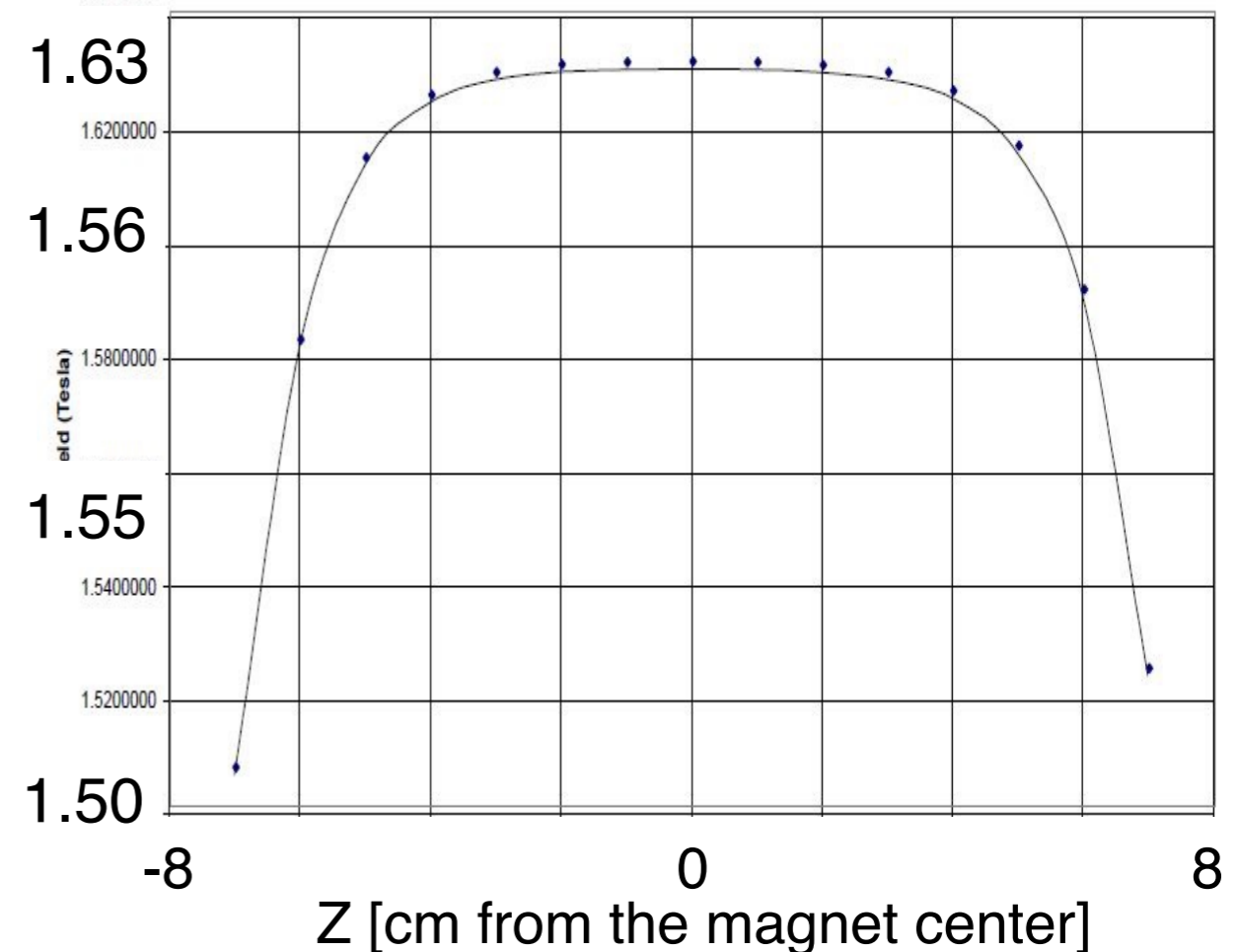
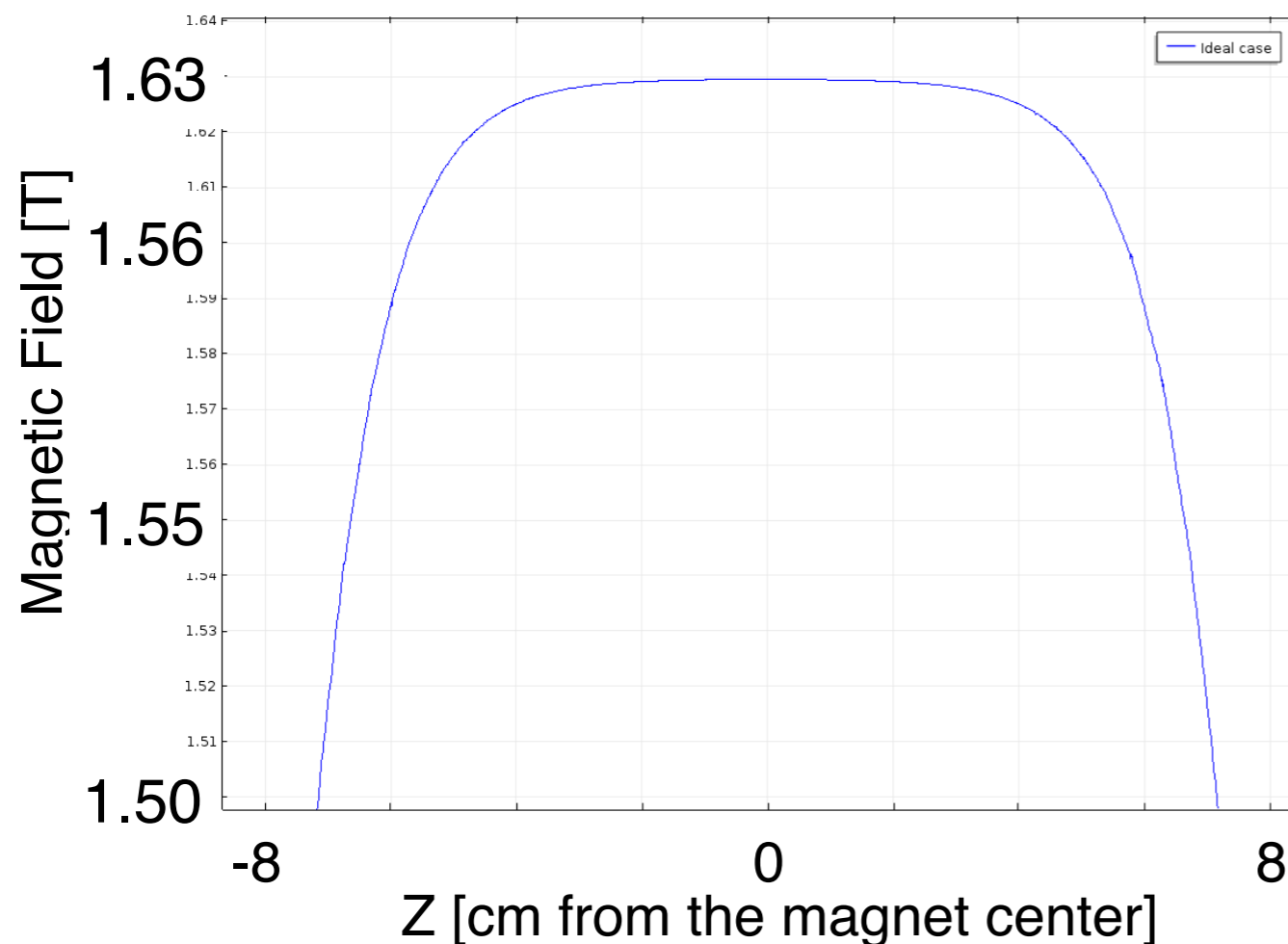


Fig.4. Z line.

Magnetic field along z direction line  
in the magnet center

COMSOL Simulation

Datasheet of the magnet



# COMSOL Simulations – Ideal case Vs poles skewed

Field along Z line in the magnet center. Ideal case Vs poles skewed

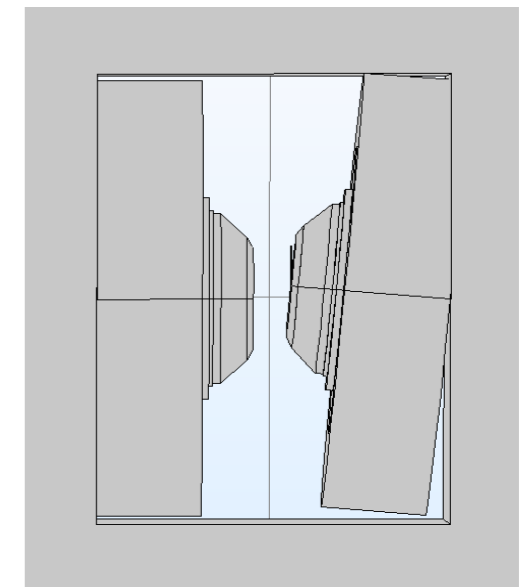
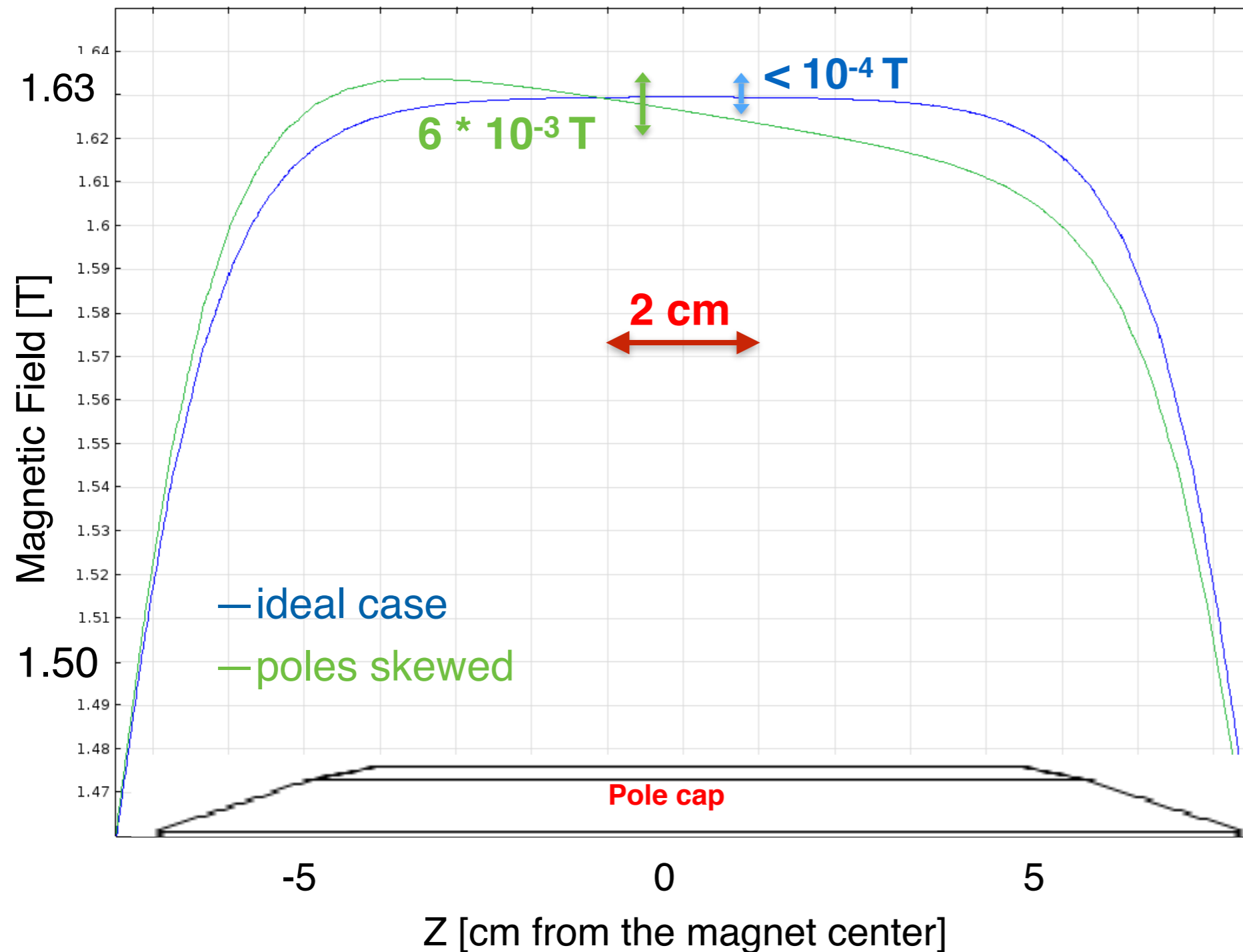
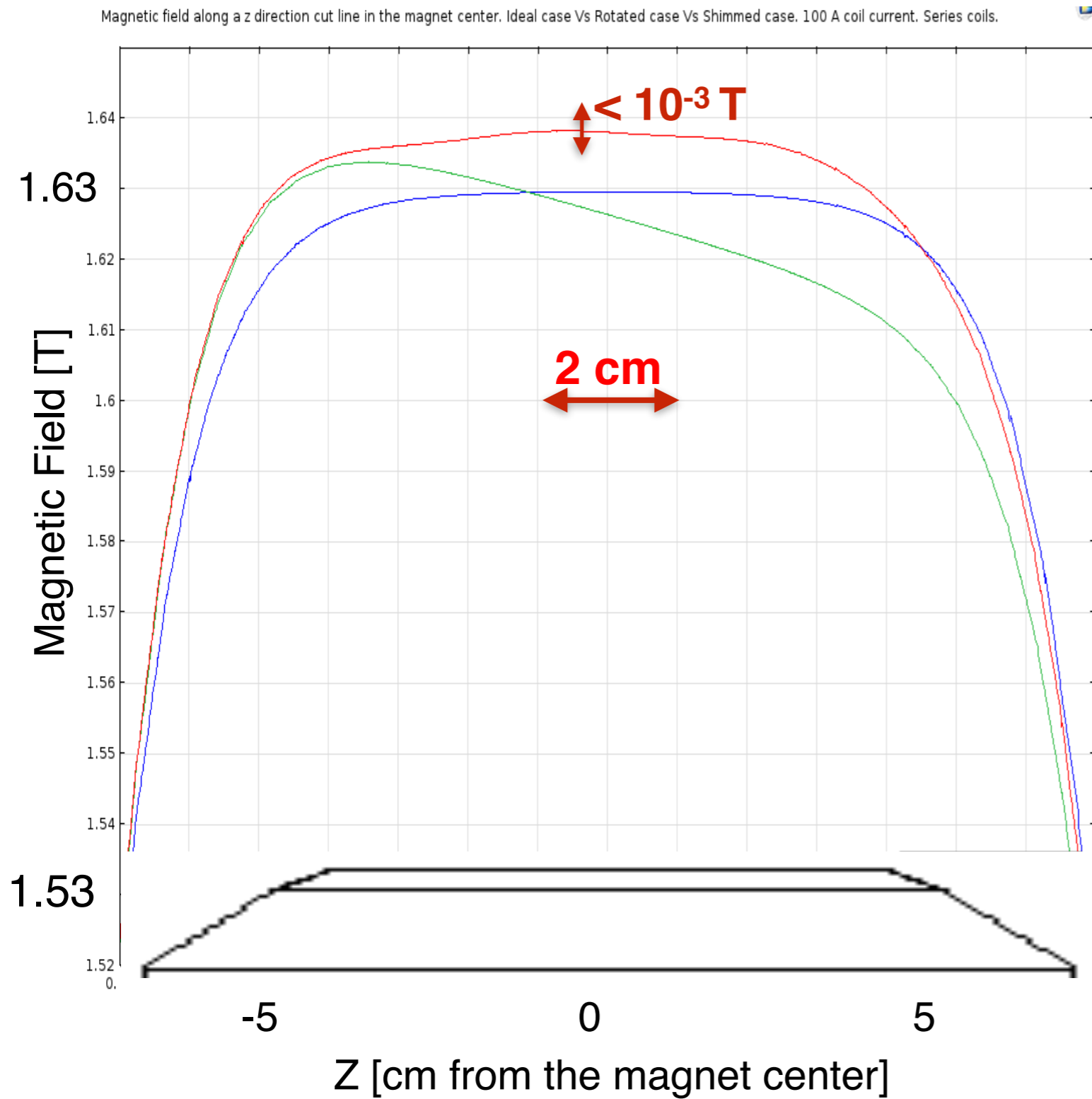


Fig.5. Pole skewness.

- Pole skewness decreases the field homogeneity to  $6 \times 10^{-3}$  T over 2 cm

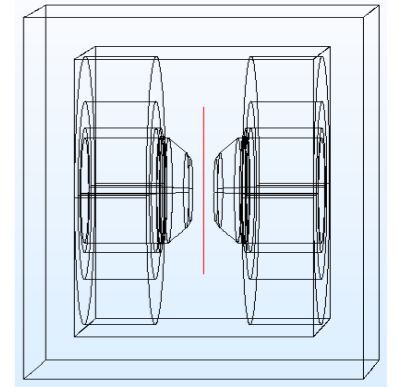


# COMSOL Simulations – Shimming (trial and error procedure)

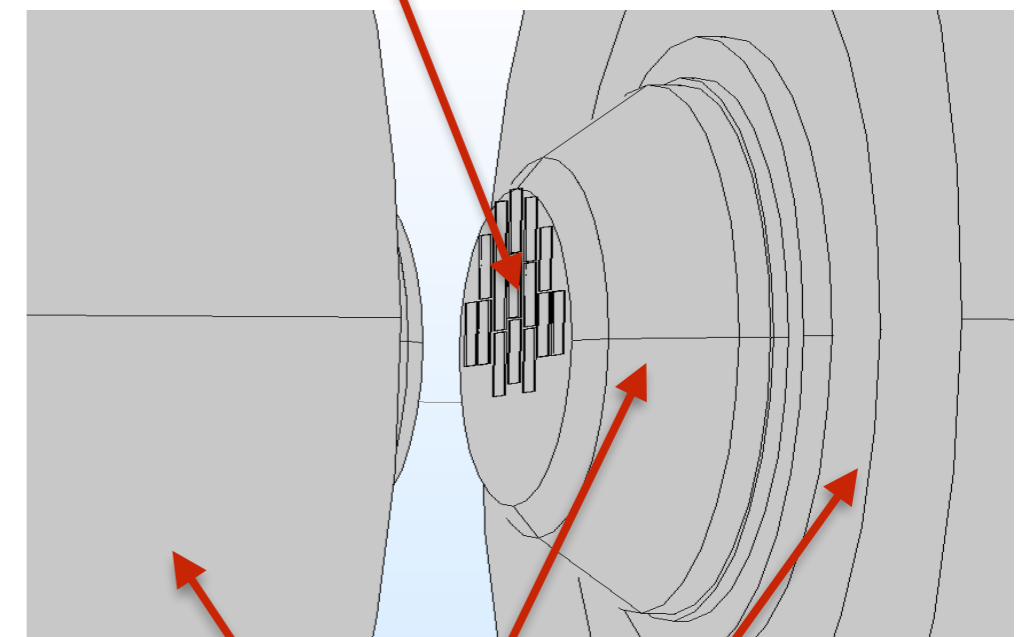


Field along Z line in the magnet center in the:

- ideal case
- poles skewed
- after shimming



**Shims**



Pole cap

Coils

# COMSOL Simulations – Summary

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Field homogeneity in the region of 2 cm in the magnet center:

- Ideal case:  $< 10^{-4}$  T
- With poles skewed:  $6 \cdot 10^{-3}$  T
- With Shimming:  $< 10^{-3}$  T



- The magnet can meet the requirement for the Hall Probe in the ideal case
- In non ideal conditions the homogeneity can be increased with shimming, decreasing the skew effect
- Simulations provide guidelines to how do the shimming



# Field Mapping - Instrumentation Setup

- **Magnetic Field mapping** using **NMR Probes** mounted on a **2 axis motion robot** with **LabVIEW** interface

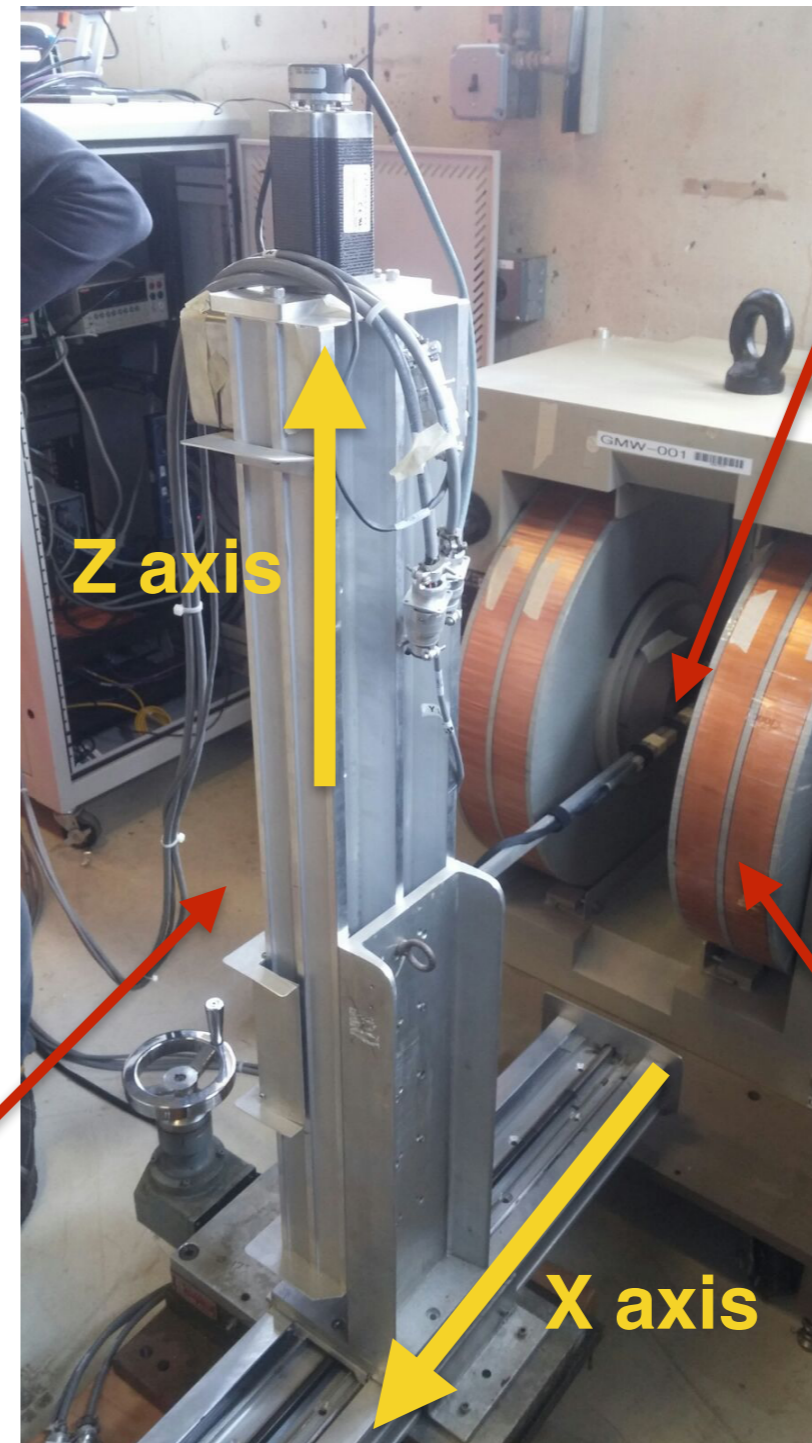


For Metrolab PT 2025:

NMR Probe #4  
range 0.7 - 2.1 T

NMR Probe #5  
range 0.35 - 1.05 T

Motion Robot



NMR Probe

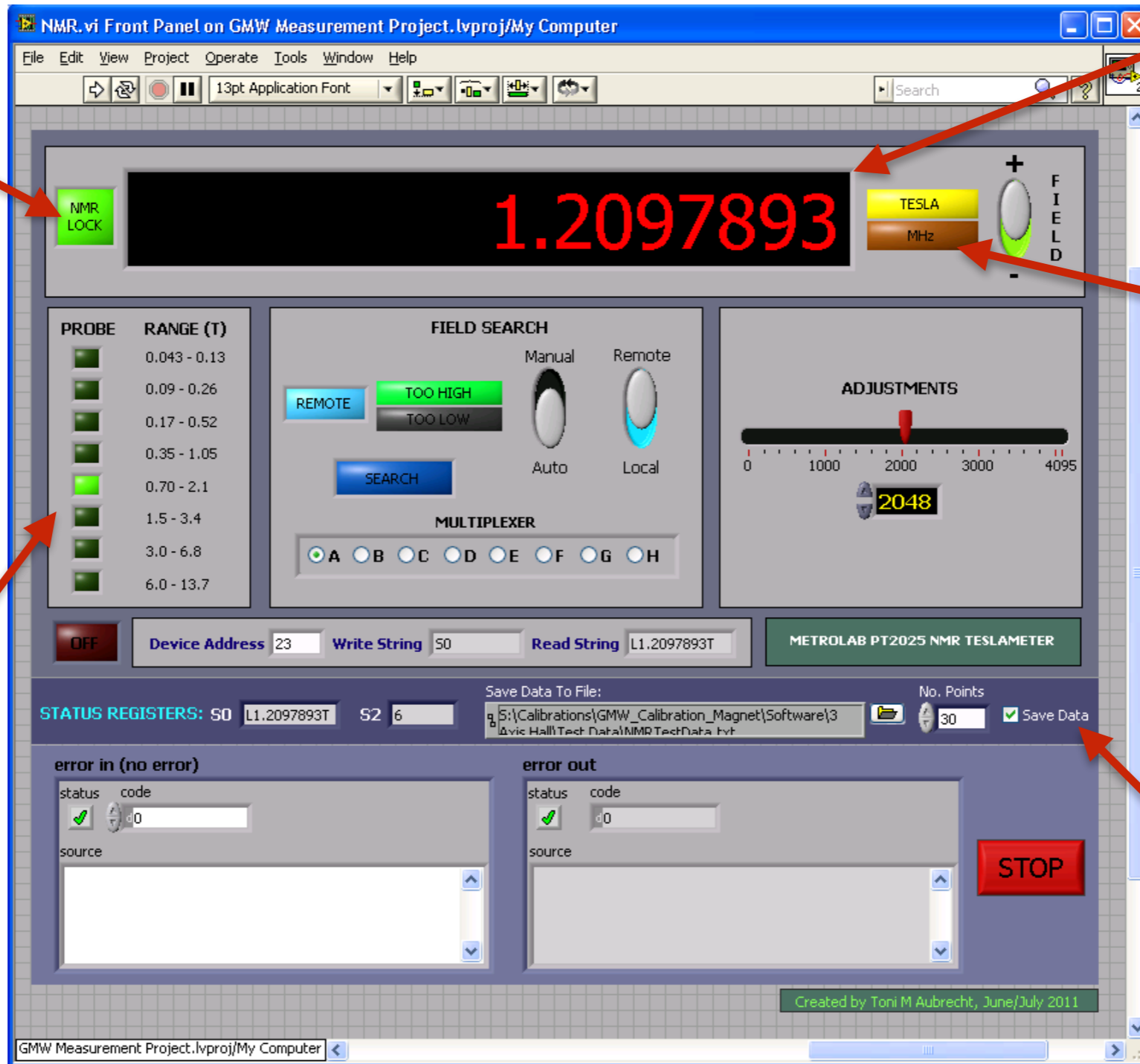
X axis

Electromagnet

# Field Mapping - LabVIEW interface - NMR Probes reading

Light indicates if the NMR “has lock” the field

Magnetic field measured value



Switch to read the field or the resonant frequency of the NMR Probe active sample

Lights indicate which probe is connected and its measurement range

Save the data in a spreadsheet file

# Field Mapping - LabVIEW interface - Robot Movement

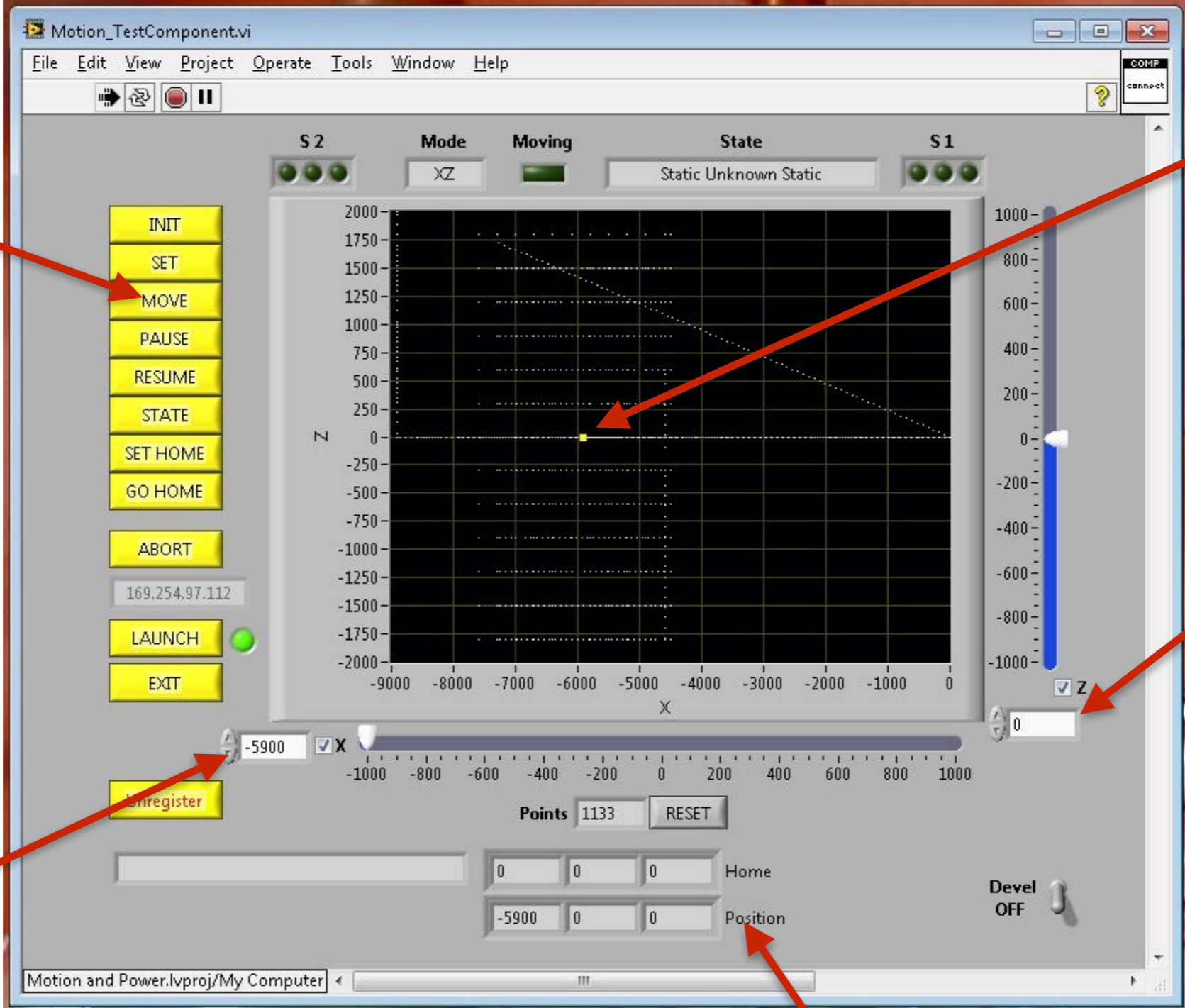
Button to move the robot

Actual robot position

Motor step along Z axis

Motor step along X axis

Robot position (x y z coordinates), relative to the home position





# Field Mapping - Instrumentation Setup



## Power Supply

- Manual supply current setting, using fixed steps

## Water cooling control panel



## DANFYSIK ULTRASTAB SATURN Current Transducer

- feedback current measurement for power supply control



# Field Mapping - Instrumentation Setup

## Multimeters

- to measure a voltage proportional to the power supply current



- Agilent 3458A Multimeter
- Precision of  $10^{-6}$  V



- Keithley Model 2001 Multimeter
- Precision of  $10^{-5}$  V

- to measure the power supply voltage

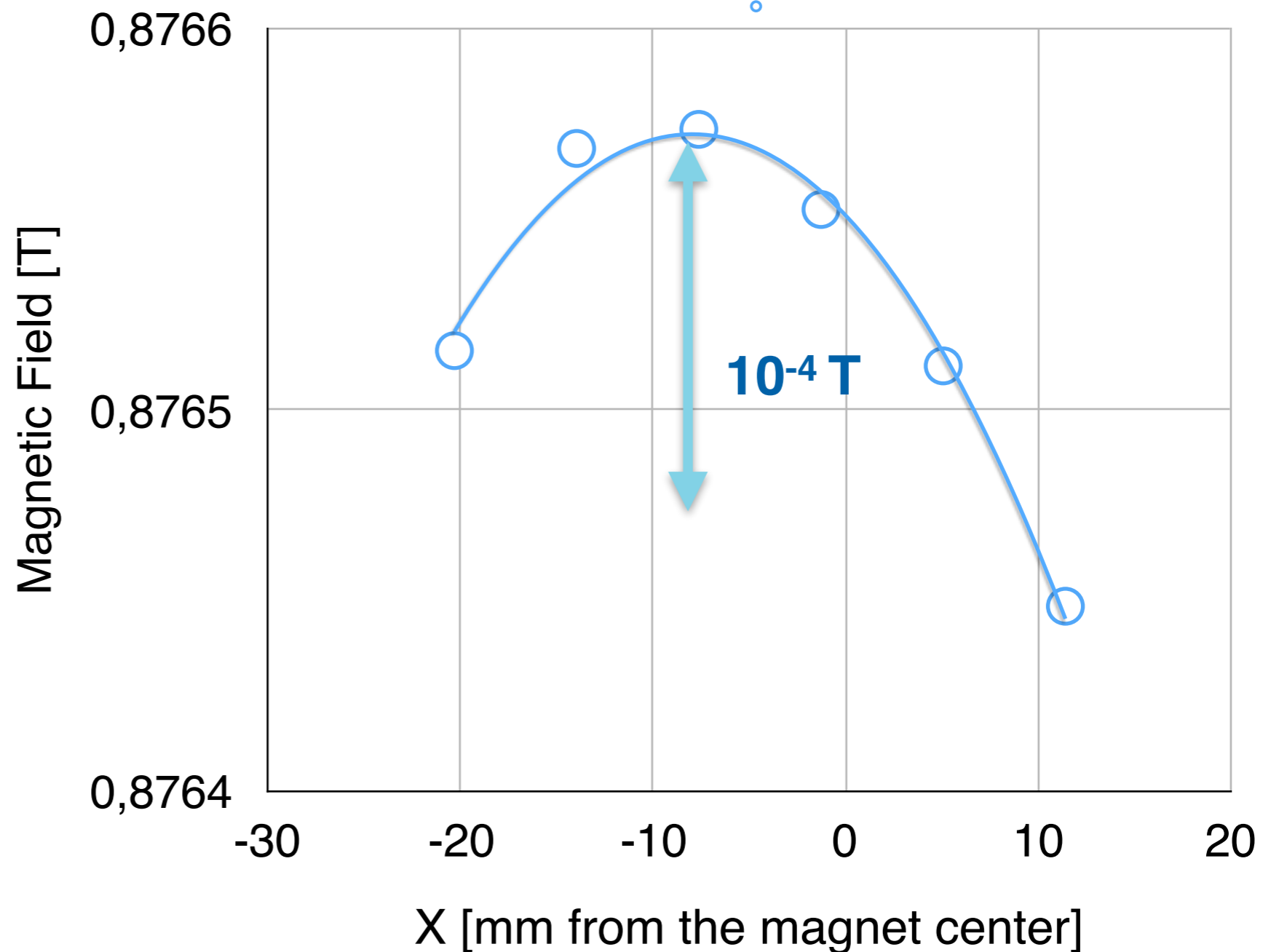


- Hp 3457 A
- Precision of  $10^{-4}$  V

# Field Mapping - Coarse 1D field Mapping

- Map resolution: 6.35 mm (step size 500 in X movement)
- The max field value is not in the magnet center
- Homogeneity of  $10^{-4}$  T
- Only a small region can be measured: Probe #5 is insensitive if gradient is larger than 250ppm/cm)

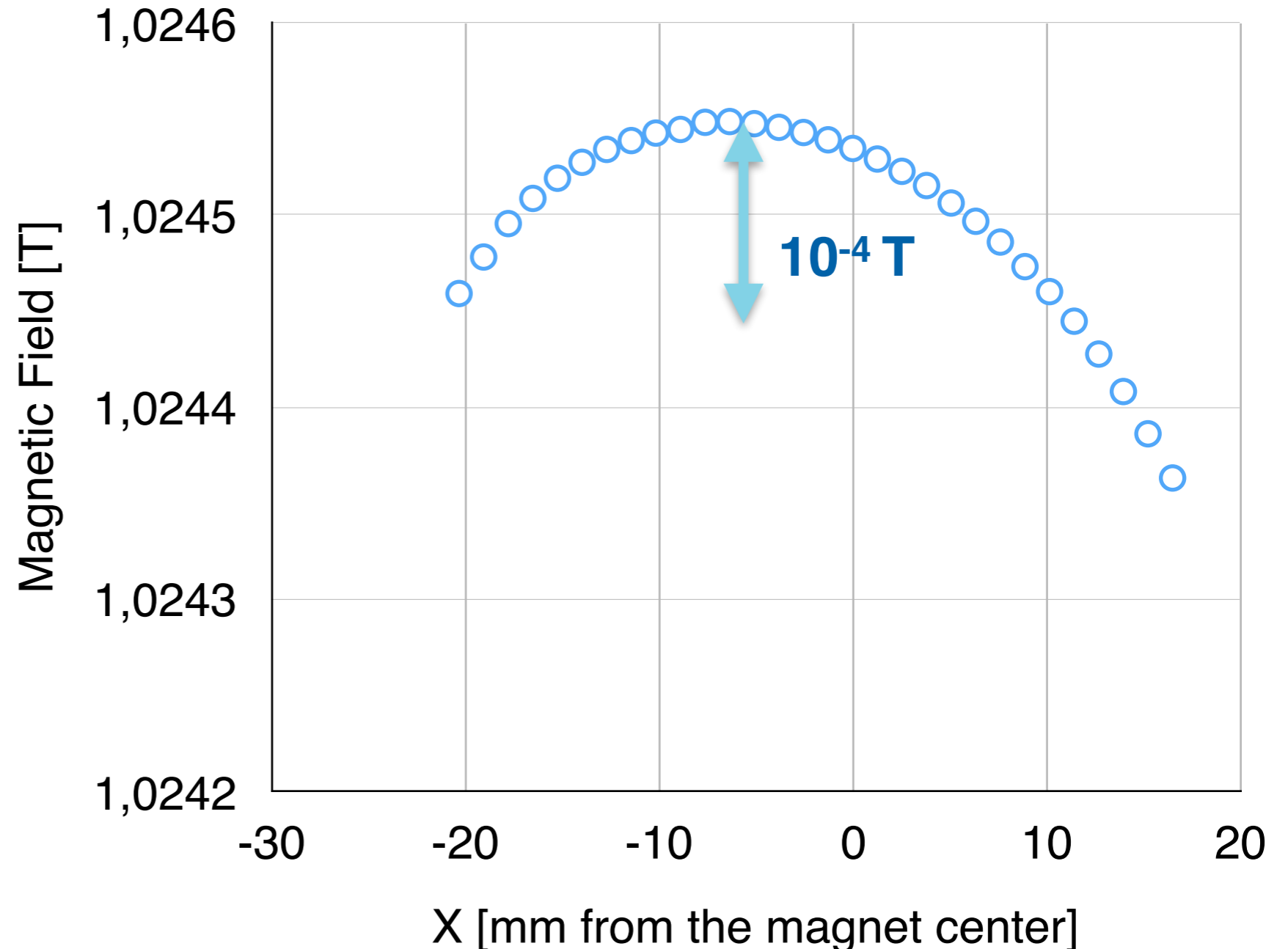
Field mapping along X axis ( $Z = 0$ ).  
100 A of Supply Current



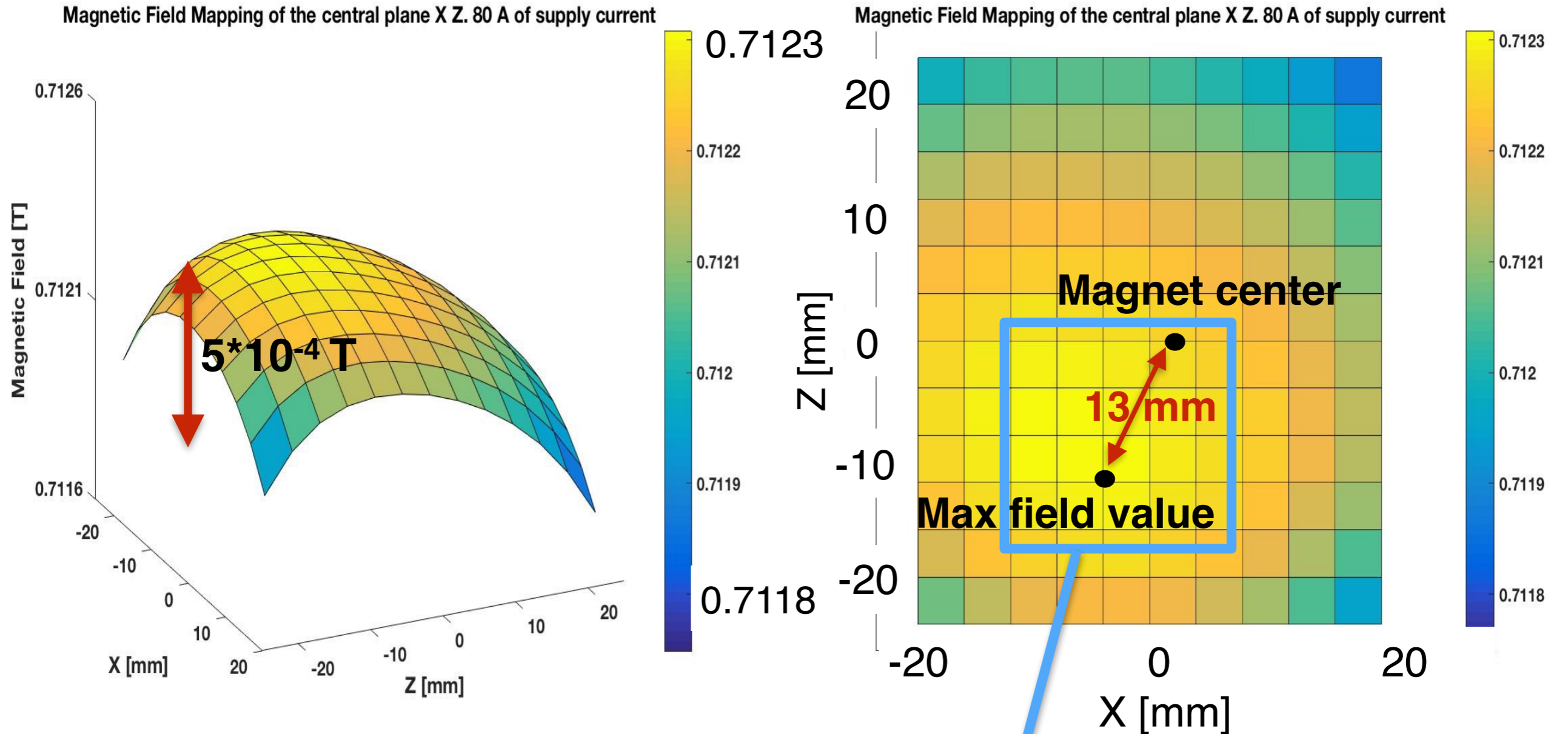
# Field Mapping - Finer 1D field Mapping

- Map resolution: 1.27 mm (step size 100 in X movement)
- The max field value is not in the magnet center
- Homogeneity of  $10^{-4}$  T
- Only a small region can be measured: Probe #5 is insensitive if gradient is larger than 250ppm/cm)

Field mapping along X axis ( $Z = 0$ ).  
120 A of Supply Current



# Field Mapping - 2D Field Mapping - 80 A

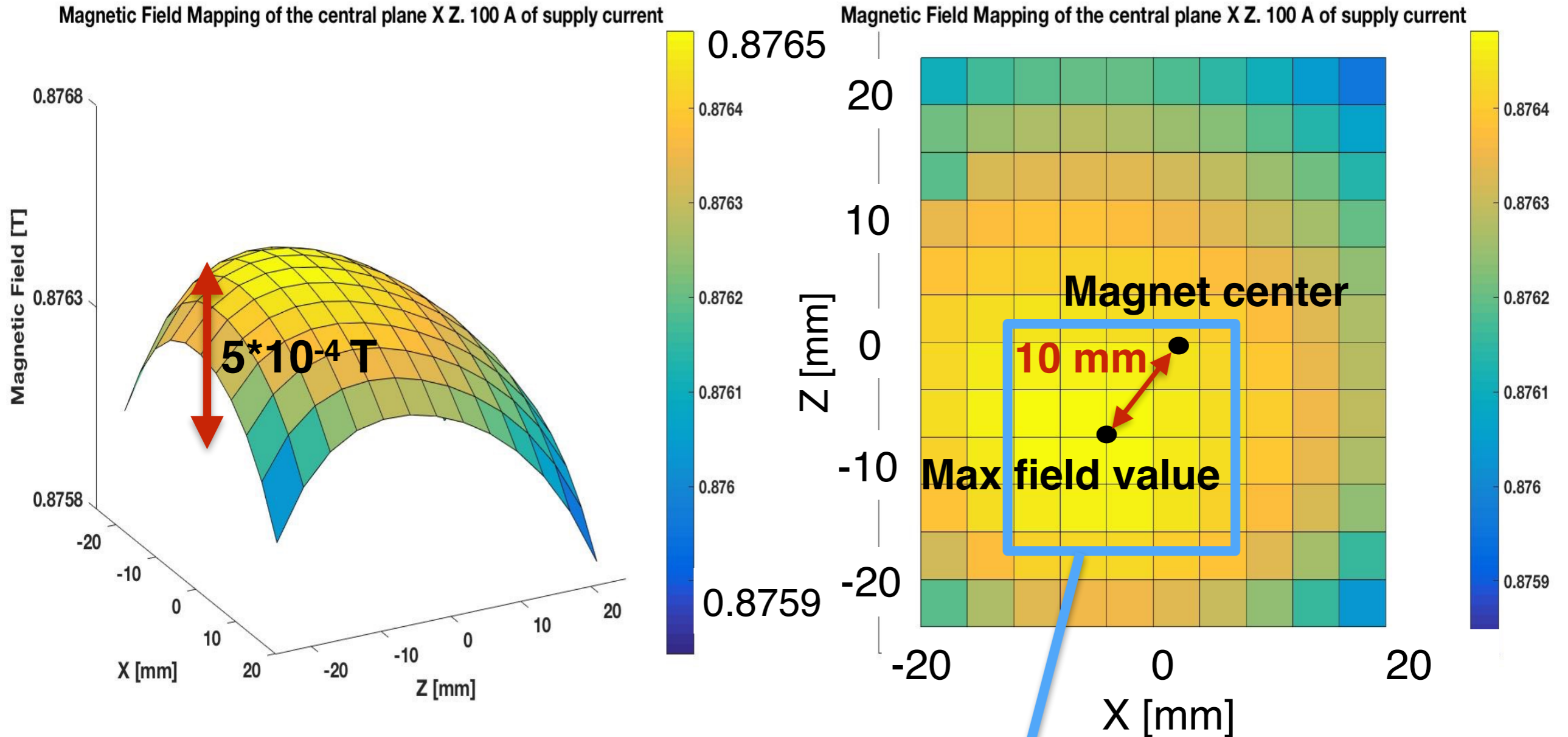


- Map resolution: 3.81 mm
- Supply current 80 A
- Field homogeneity

$5.6 \cdot 10^{-4} \text{ T}$  in the entire plane  
 $1.3 \cdot 10^{-4} \text{ T}$  in a  $2 \text{ cm} \cdot 2 \text{ cm}$  region



# Field Mapping - 2D Field Mapping - 100 A

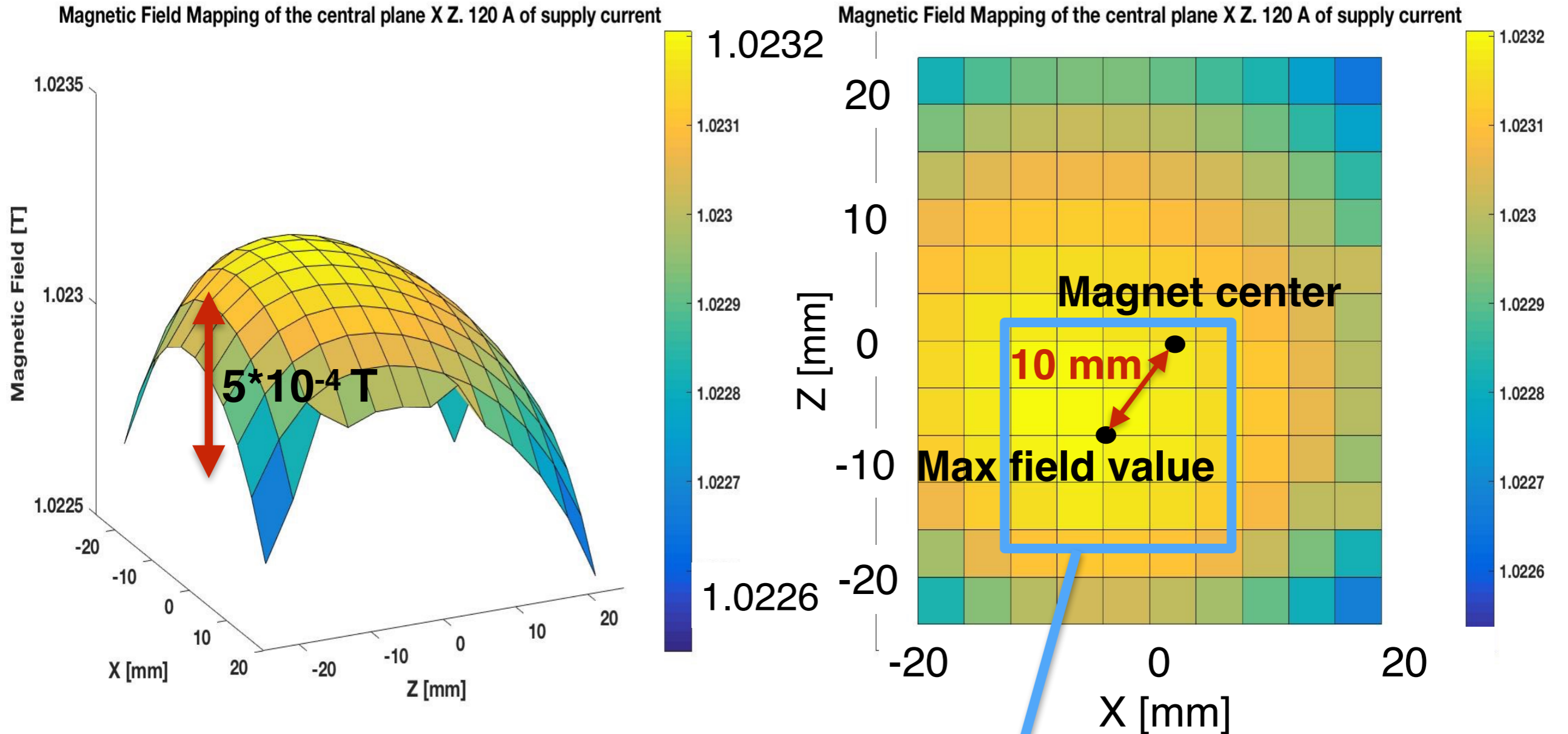


- Map resolution: 3.81 mm
- Supply current 100 A
- Field homogeneity

6.7 \* 10<sup>-4</sup> T in the entire plane

1.5 \* 10<sup>-4</sup> T in a 2 cm \* 2 cm region

# Field Mapping - 2D Field Mapping - 120 A



- Map resolution: 3.81 mm
- Supply current 120 A
- Field homogeneity
  - $7.0 \cdot 10^{-4}$  T in the entire plane
  - $1.4 \cdot 10^{-4}$  T in a  $2 \text{ cm} \cdot 2 \text{ cm}$  region

# Field Mapping - 2D Field Mapping - Spacers

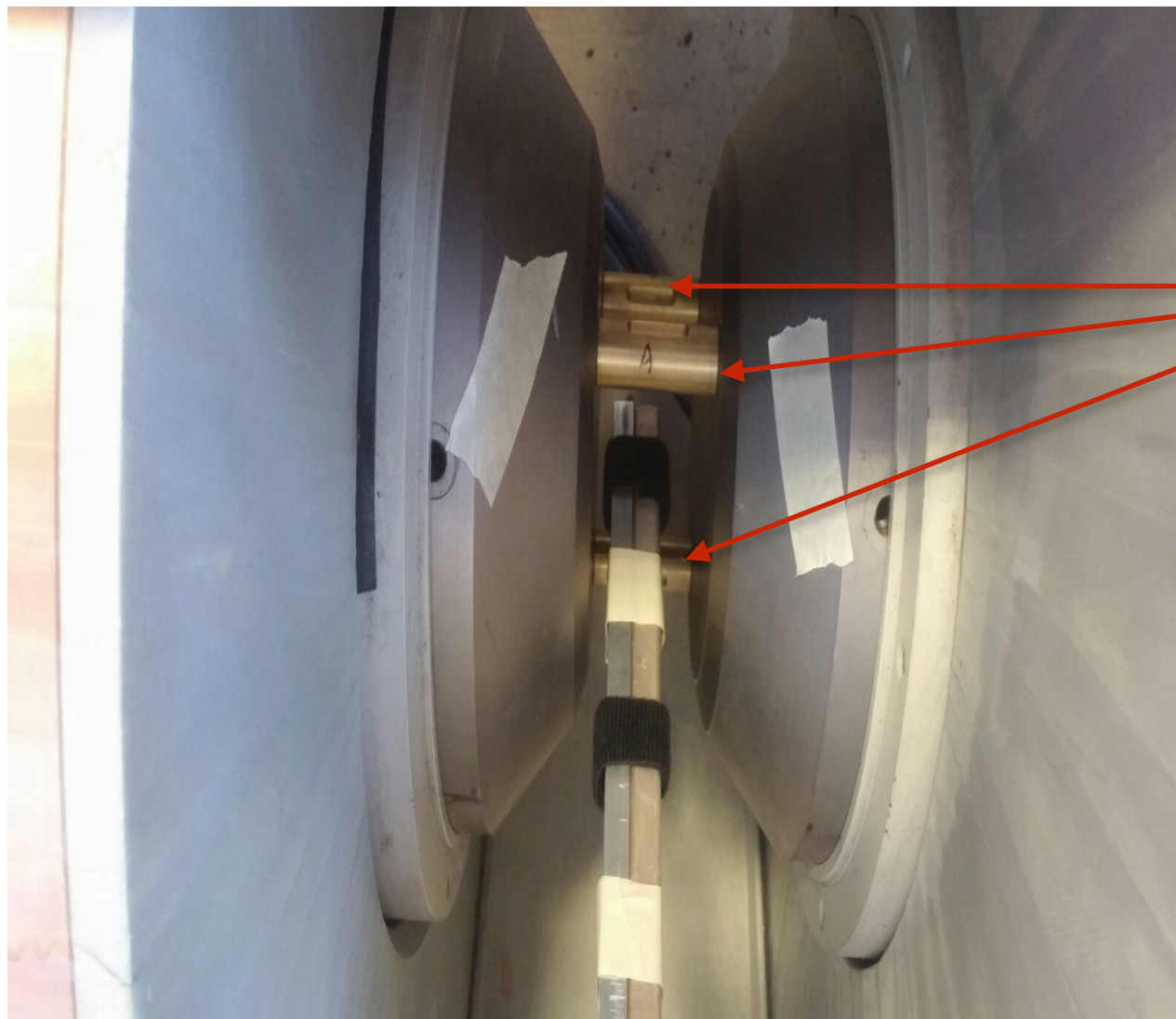
The maximum field value is not in the magnet center



The cause is pole skewness (measured about 1 mm)




Use **pole spacers** to align the poles and reduce the skewness



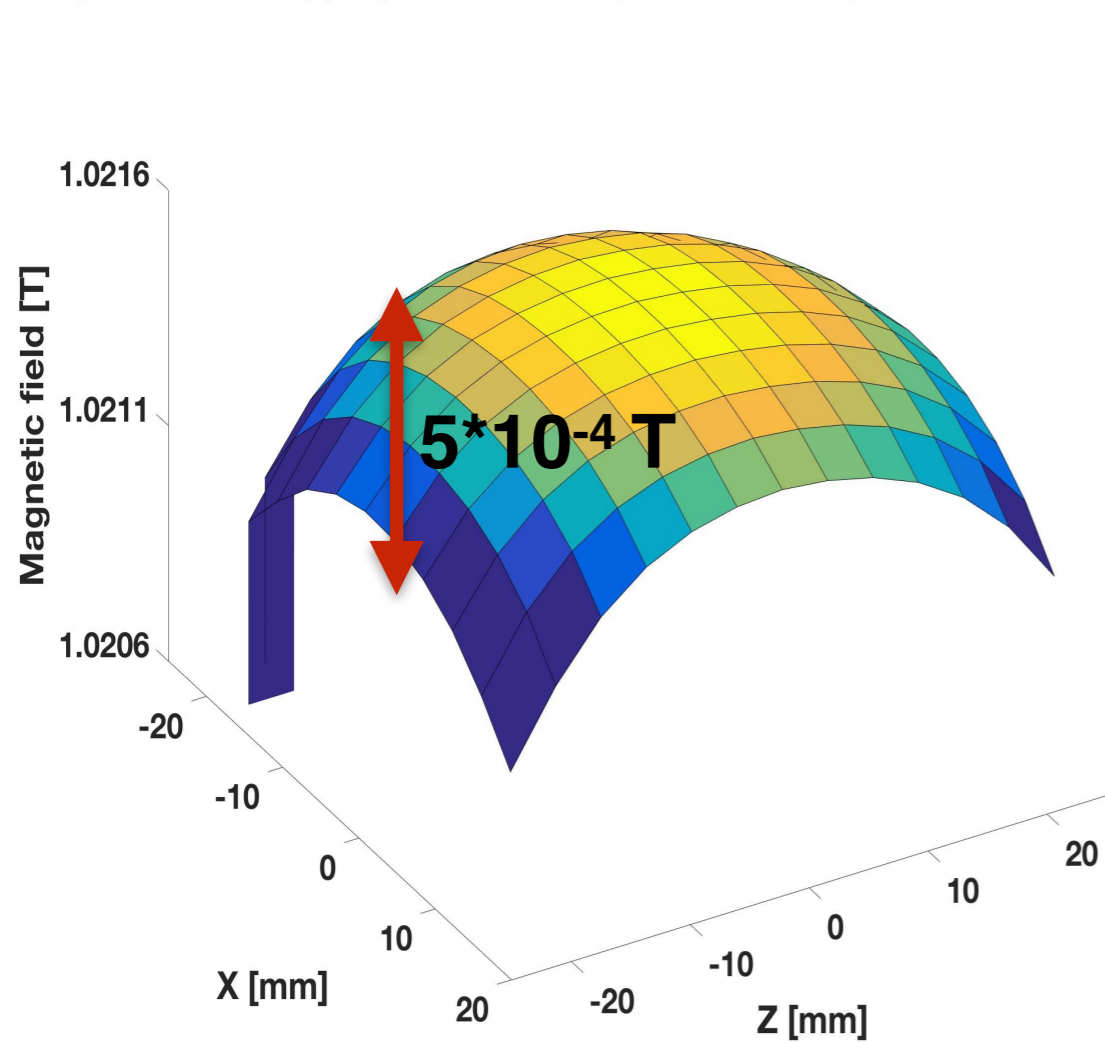
Pole spacers

## Results

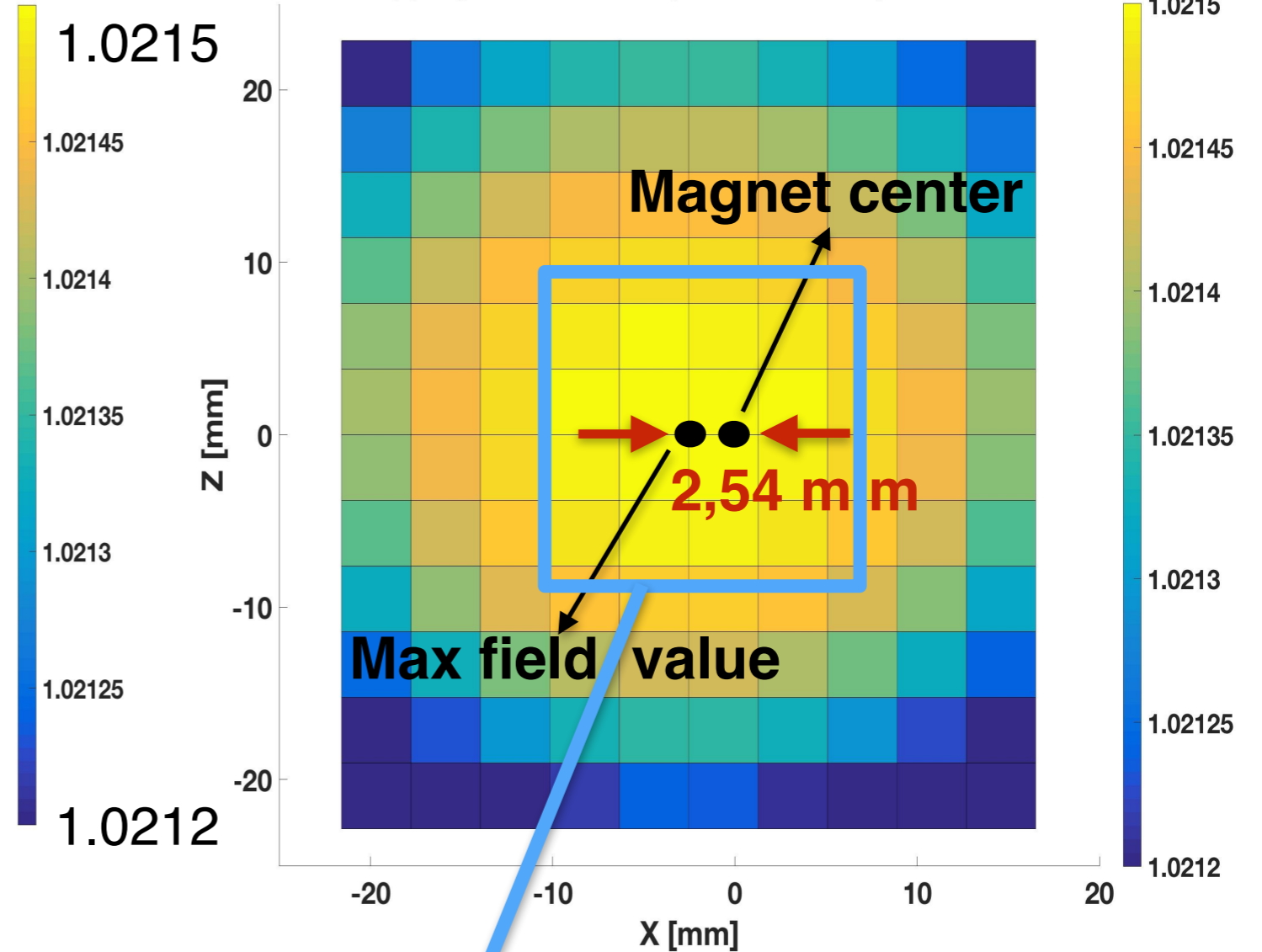
- The field is more **symmetric**
- **homogeneity increased** from  $1.4 \cdot 10^{-4}$  T to  $8.8 \cdot 10^{-5}$  T in the region of  $2 \cdot 2$  cm... 

# Field Mapping - 2D Field Mapping - Spacers

Magnetic field mapping of the central plane X Z with pole skewness correction



Magnetic field mapping of the central plane X Z with pole skewness correction



- Map resolution: 3.81 mm
- Supply current 120 A
- Field homogeneity

$6 \cdot 10^{-4}$  T in the entire plane  
 $8.8 \cdot 10^{-5}$  T in a 2 cm \* 2 cm region

Error on center position of the robot about 3 mm



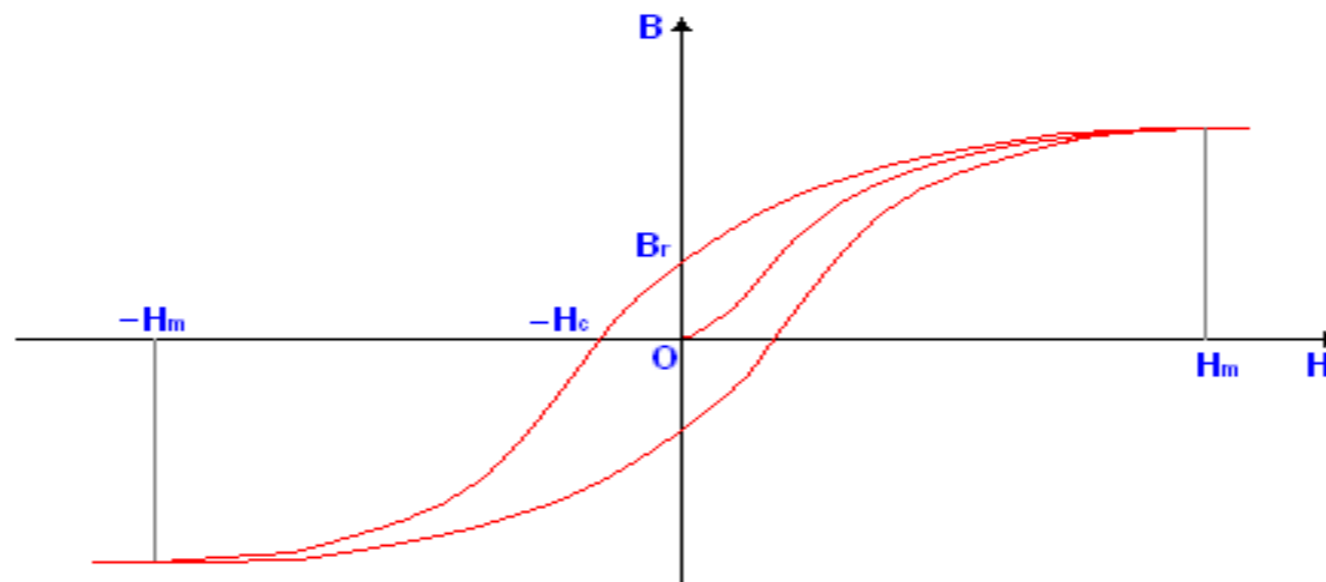
# Field Mapping - Magnetic Hysteresis

## Hysteresis

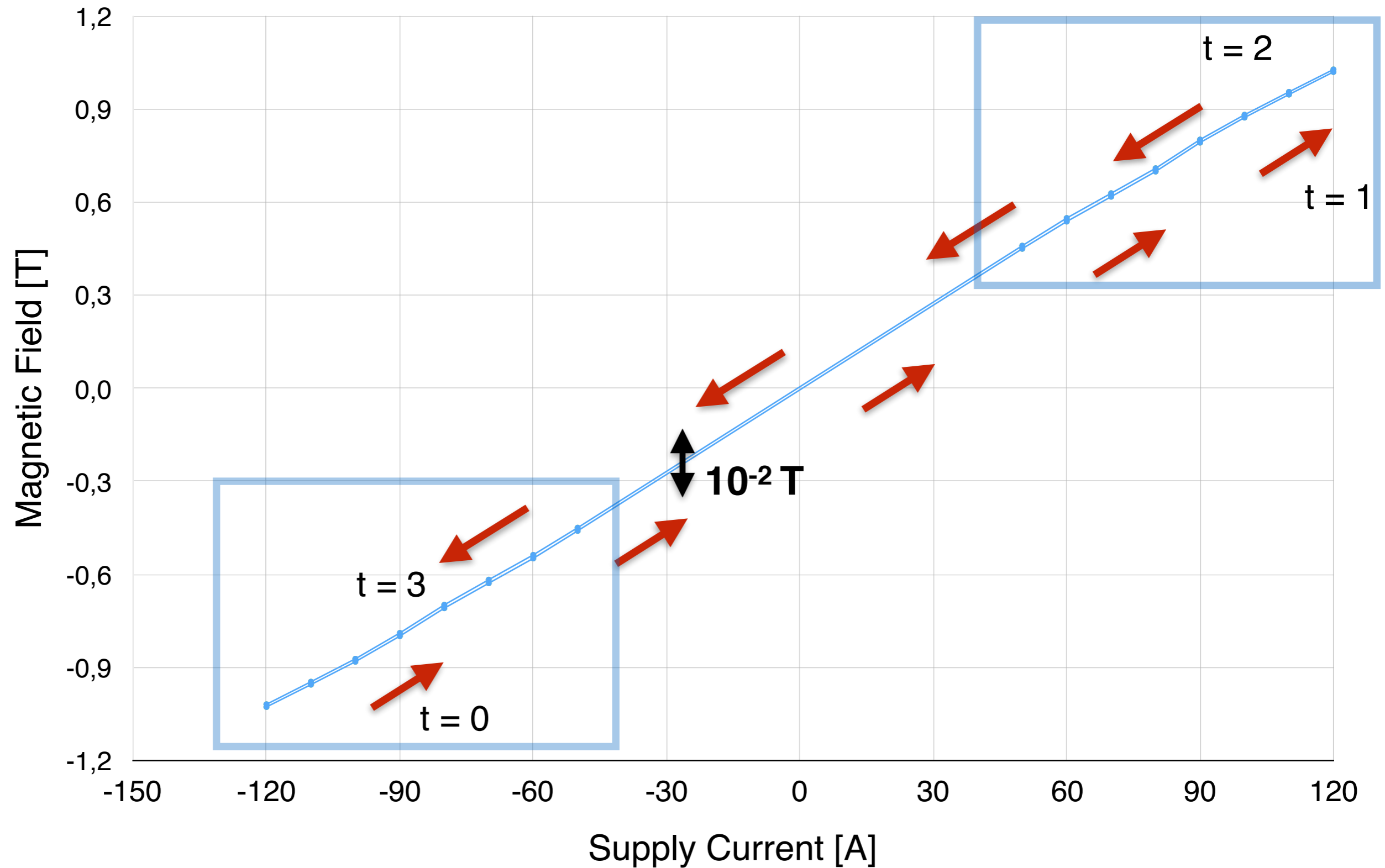
- System's dependence on the present and past input
- The history of the state assumed by the system affects the behavior of present state

## Explanation:

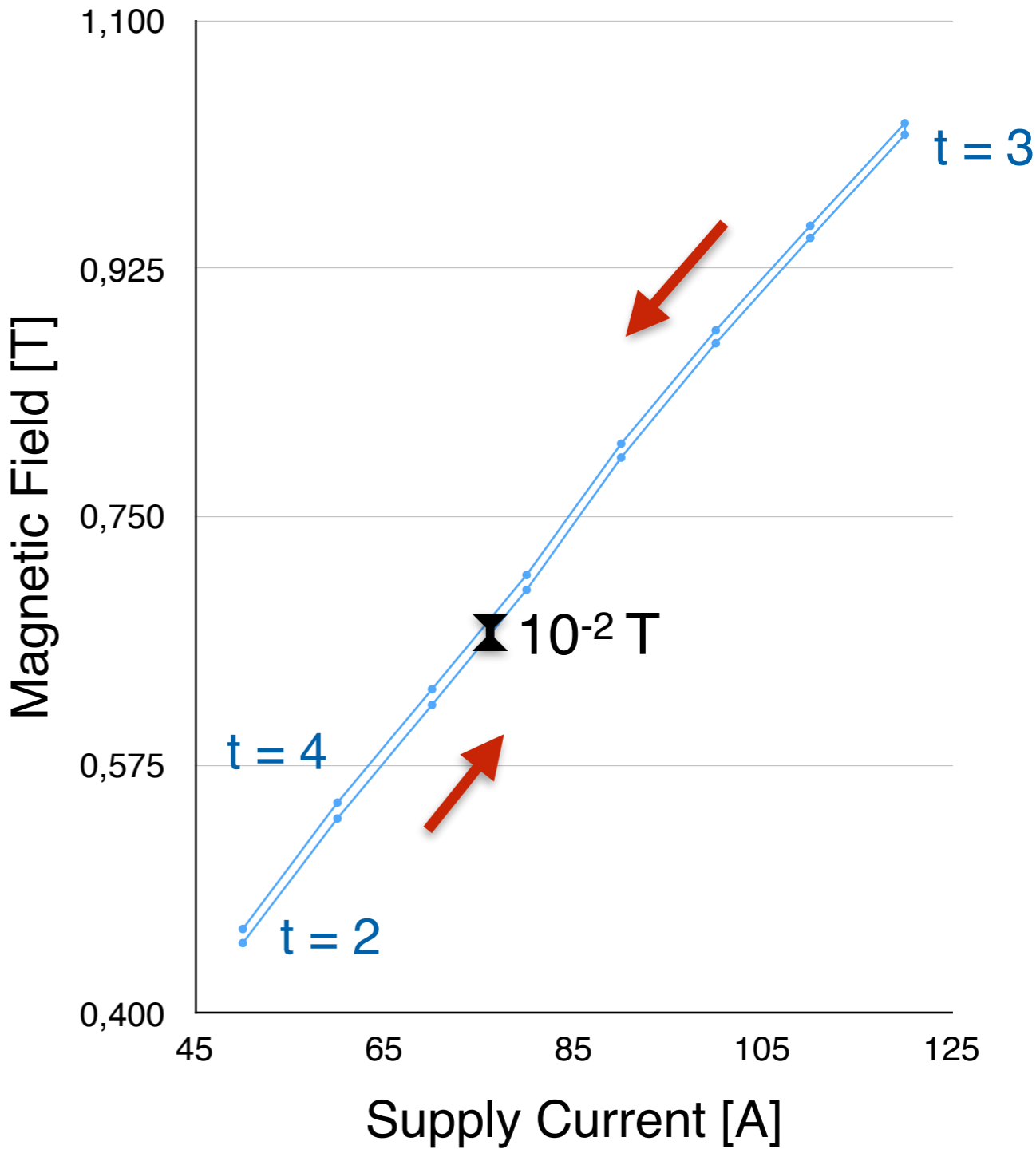
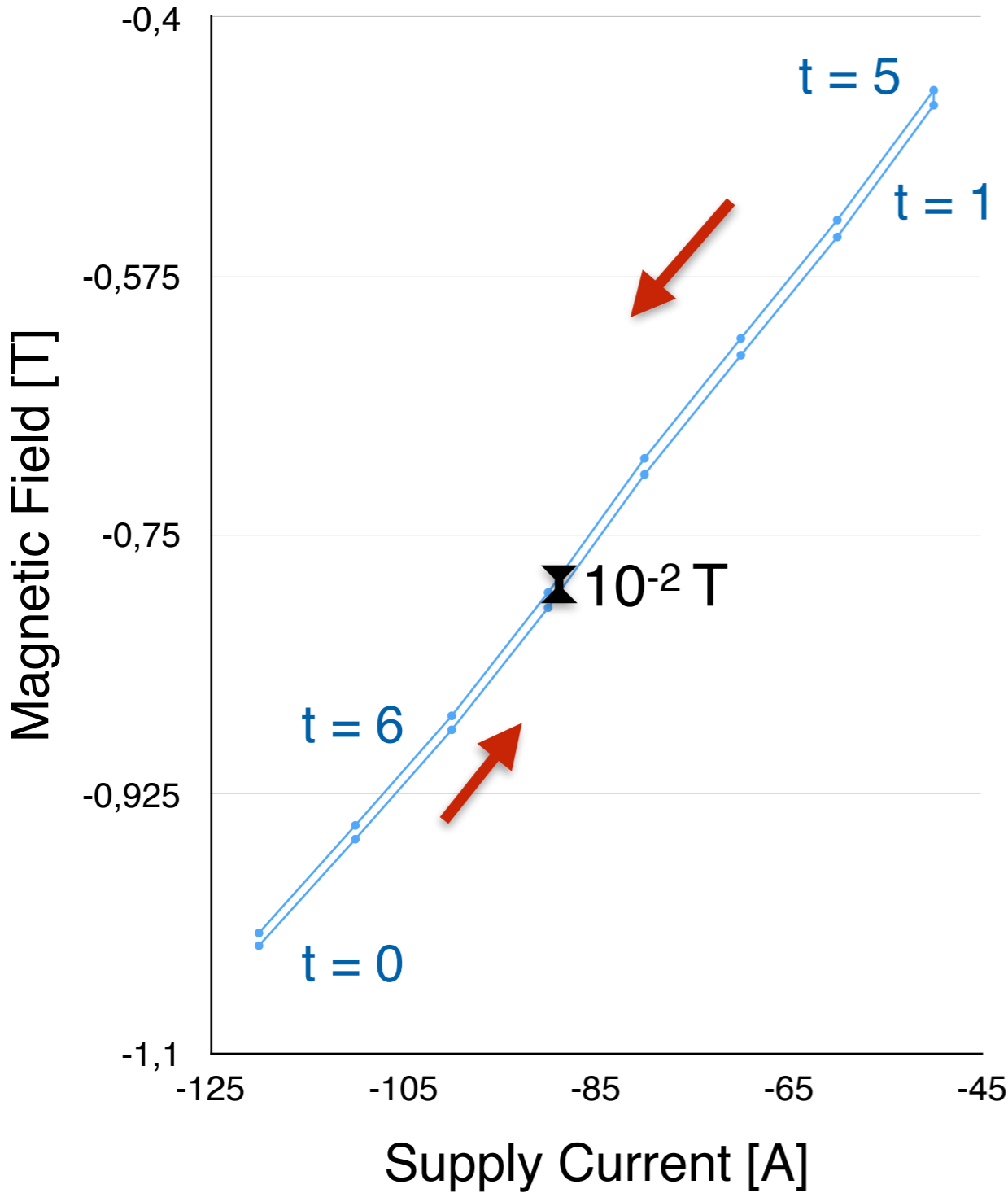
- When an external magnetic field is applied to a ferromagnetic material, the atomic dipoles align themselves with it
- When the field is removed, part of the alignment will be retained and the material hold a magnetization



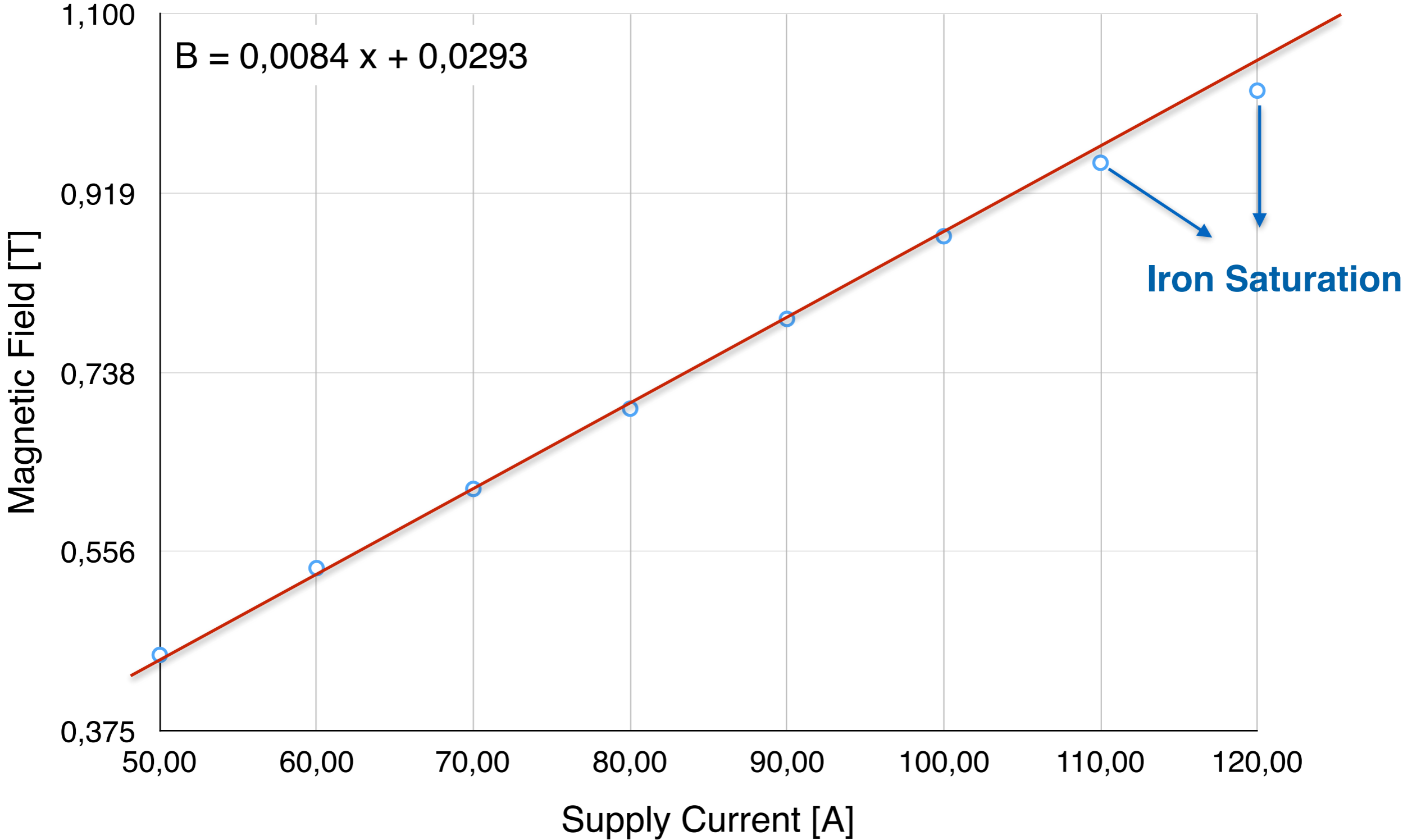
# Field Mapping - Magnetic Hysteresis



# Field Mapping - Magnetic Hysteresis



# Field Mapping - Field Vs Current plot





# Field Stability over time - 85 F

Several measurements of the field with 80 A of supply current



Stability of  $10^{-3}$  T

Degaussing



0 A



80 A



Degaussing

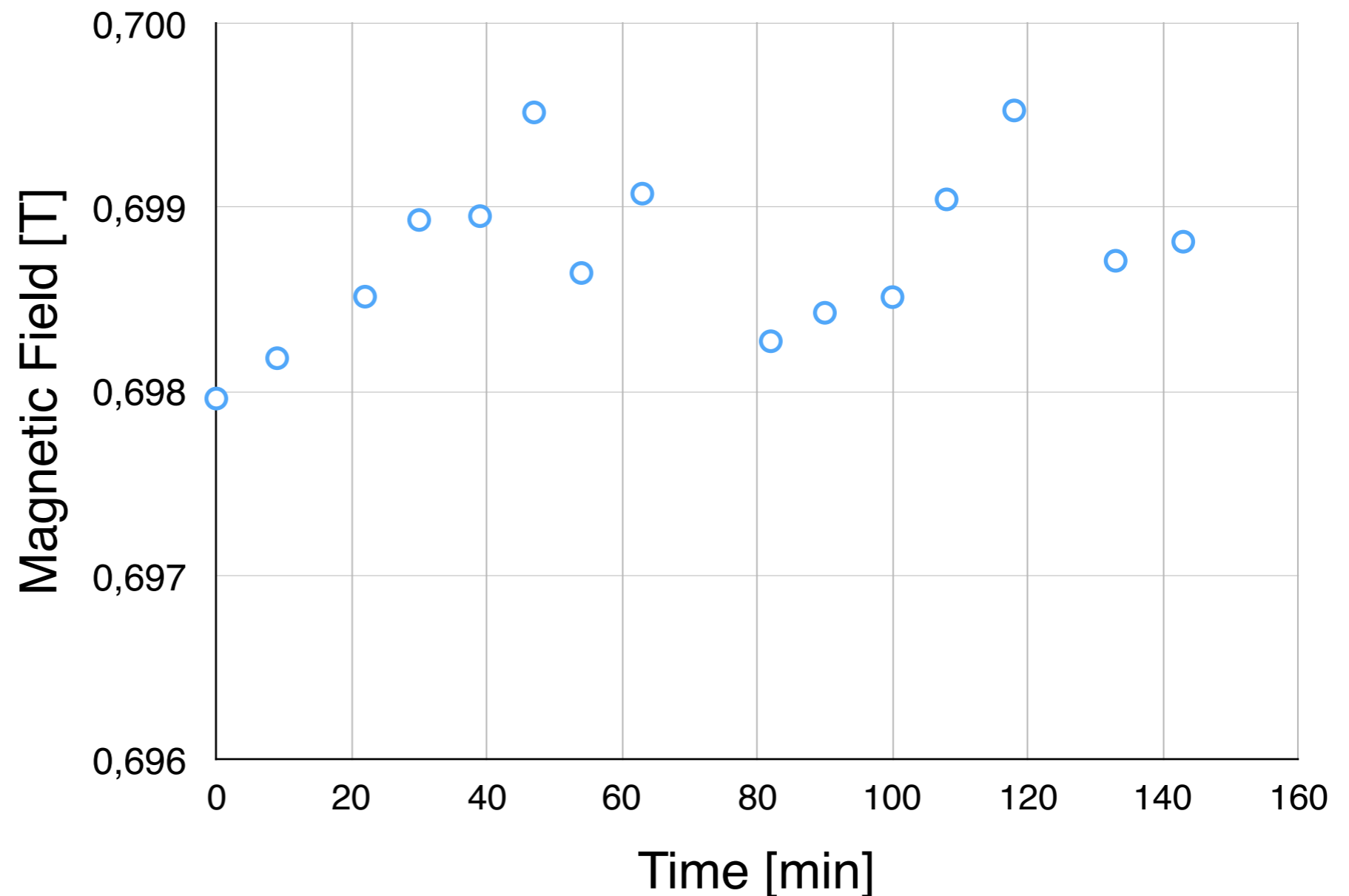


0 A



80

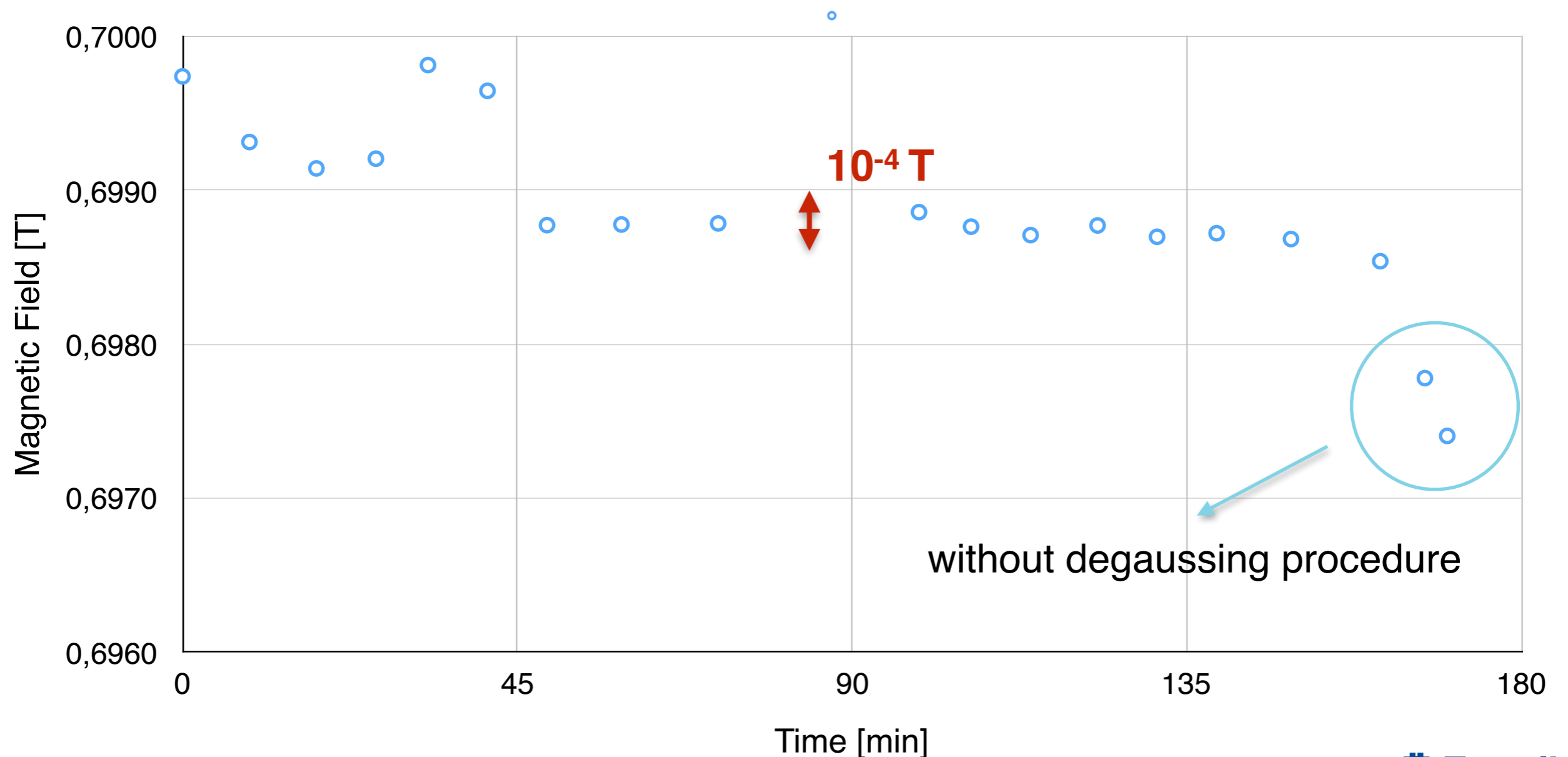
Magnetic Field Vs Time



# Field Stability over time - 100 F

- Increasing the temperature set point, the magnet goes in a more stable temperature condition
- Field stability goes up to  $10^{-4}$  T

Magnetic Field Vs Time with 80 A of Supply Current



# Field Mapping - Magnetic Hysteresis

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- Hysteresis can explain the field difference of  $10^{-3}$  T observed in two different days mapping
- However, there is still a variance in the field, which can be attributed to a variation in the power supply; increasing the set-point temperature helps to stabilize the power supply
- Lessons learned:
  - apply a degaussing procedure to loose previous memory of the magnet
  - Ramp to the desired current plateau slowly
  - Stabilize the power supply internal temperature
- We obtained a stability of  $10^{-4}$  in the final measurements

# Results

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- We can not go over  $10^{-4}$  T of field stability because the power supply stability is limiting the mapping
- With pole spacers the field homogeneity is increased from  $1.4 \cdot 10^{-4}$  T to  $8.8 \cdot 10^{-5}$  T in a 2 cm \* 2 cm region
- Shimming procedure can potentially increase the field homogeneity. Not done due to instability in power supply.
- Before the shimming procedure, one needs to work on stabilizing the power supply, not only do we need homogeneity over the mapped volume, but also over the time of the hall probe calibration to ensure repeatability of the measurement
- We are confident that one can achieve the value that meet the requirement for Hall Probe Calibration



# Skills learned

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## Safety

- Electrical safety
- Radiological safety

## Software

- Improvement of COMSOL (new electro static and temperature dependance)
- Basics of LabVIEW (write small program to read measurement values)

## Magnetic field

- Magnetic field measurements: how do NMR Probes and Hall Probes work, differences, and applications
  - How do a magnetic field test using advanced instruments
  - Analyze the acquired data, understand some data inconsistency and show the results
- 
- Interact with engineers, scientists and technicians at a national laboratory

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# Thank you for attention

- All nucleons, have the intrinsic quantum property of **spin**, determined by the *spin quantum number S*.

- **Angular momentum** associated with the spin has a quantized magnitude and orientation. The angular momentum component along a z axis is:

$$P_z = m\hbar$$

where  $\hbar$  is the reduced Planck constant and  $m$  is the *magnetic quantum number*, that can take the values from  $-S$  to  $S$  in integer steps.

- We consider atoms with  **$S = 1/2$**  because NMR Probes use the property of Hydrogen atoms whose have  $S = 1/2$ .
- A charge particle with spin property has a **magnetic moment**.

- The relation between the magnetic moment and the angular momentum is described by  $\gamma$ , the **gyromagnetic ratio**.

$$\mu_z = \gamma S_z = \gamma m \hbar.$$

- In an atom with  $S = 1/2$ ,  $m$  can take only 2 values (-1/2, 1/2): the atom have only two energy state, one with **parallel** magnetic momentum and the other **antiparallel**.

- Energy of a magnetic momentum in the presence of an external magnetic field:

$$E = -\boldsymbol{\mu} \cdot \mathbf{B}_0 = -\mu_z B_0 = -\gamma m \hbar B_0$$

$$\Delta E = \gamma \hbar B_0$$

- Parallel state is more stable than antiparallel state: a bigger number of atoms have a magnetic moment parallel with the external field and a smaller number are antiparallel



- When an external electromagnetic radiation of a frequency of

$$\nu_0 = \frac{\Delta E}{h} = \frac{\gamma B_0}{2\pi} \quad (\text{Larmor Frequency})$$

the atoms absorb energy and from the lower energy state they go in the higher energy state. Larmor frequency depends both on the external magnetic field and the material and is in the range of radio frequency

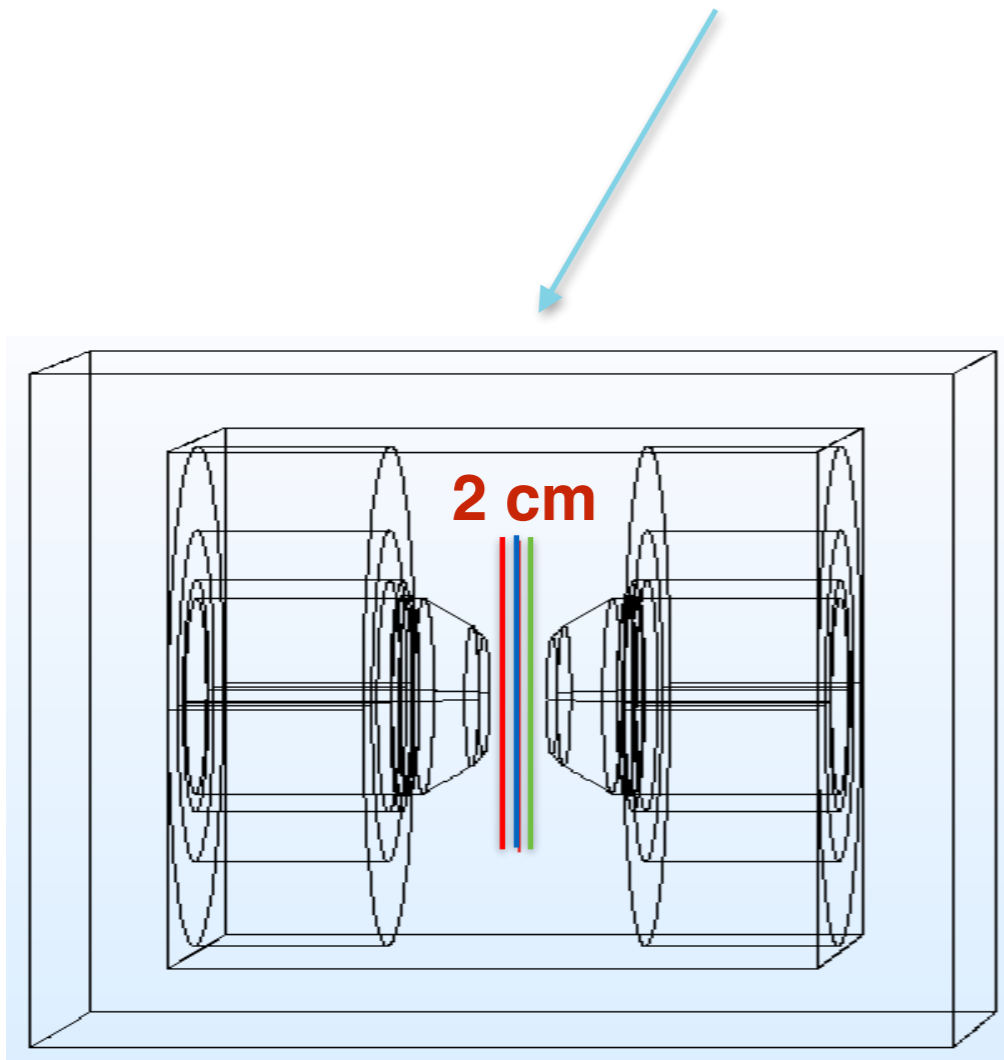
## How do NMR Probes work

- An active sample rich of hydrogen atoms is wound by radio frequency coils.
- If the sample is inside an external magnetic field and the coils generate an electromagnetic field at the sample Larmor Frequency, the atoms of the sample absorb energy, decreasing the quality factors of the coils.
- Measuring the attenuation of the radio frequency voltage amplitude across the coils, and amplifying this signal, the NMR Probe Electronic can detect the NMR signal.

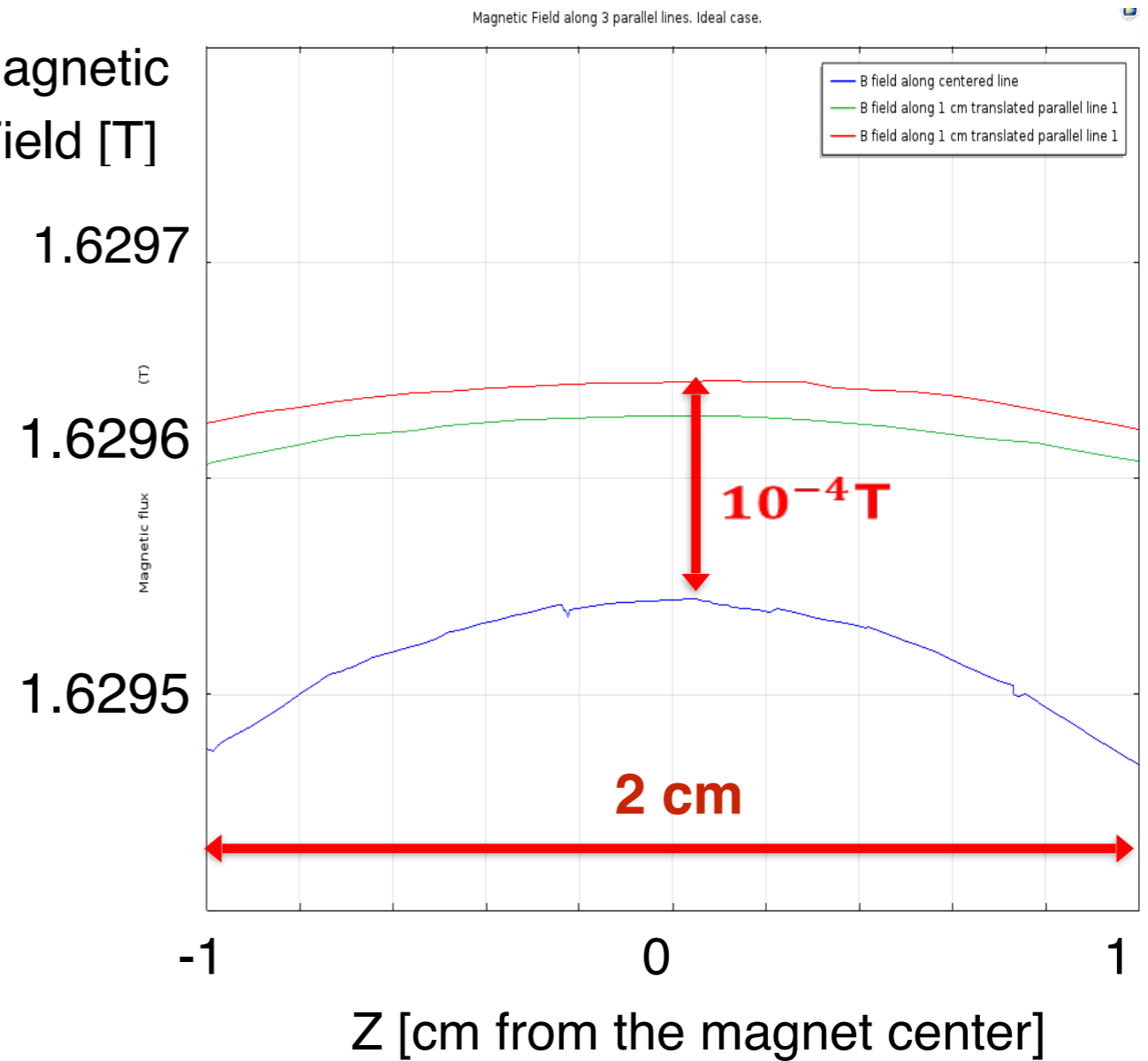
- Knowing the frequency at which the sample absorb energy, the external magnetic field can be calculate because there is a linear correlation between frequency and field.

# APPENDIX 2 - COMSOL Simulations - Ideal case

Magnetic Field along 3 parallel line in the magnet center



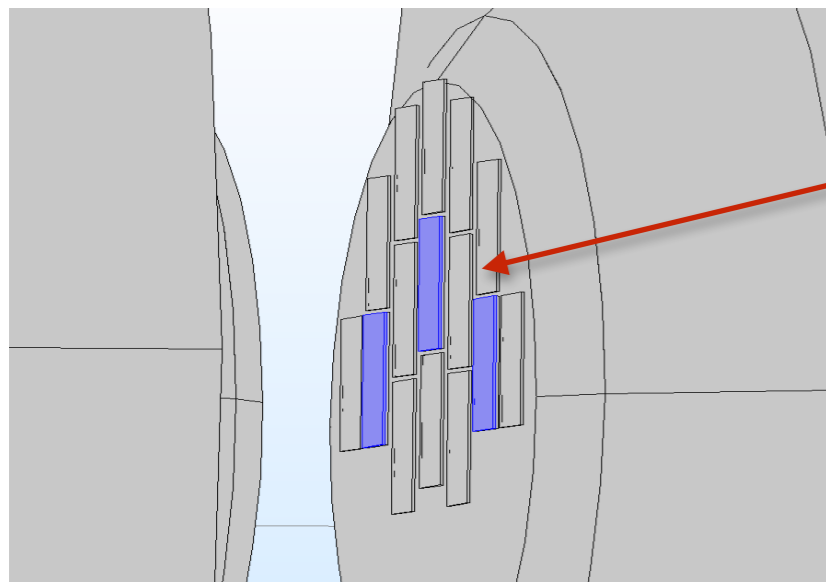
Magnetic Field [T]



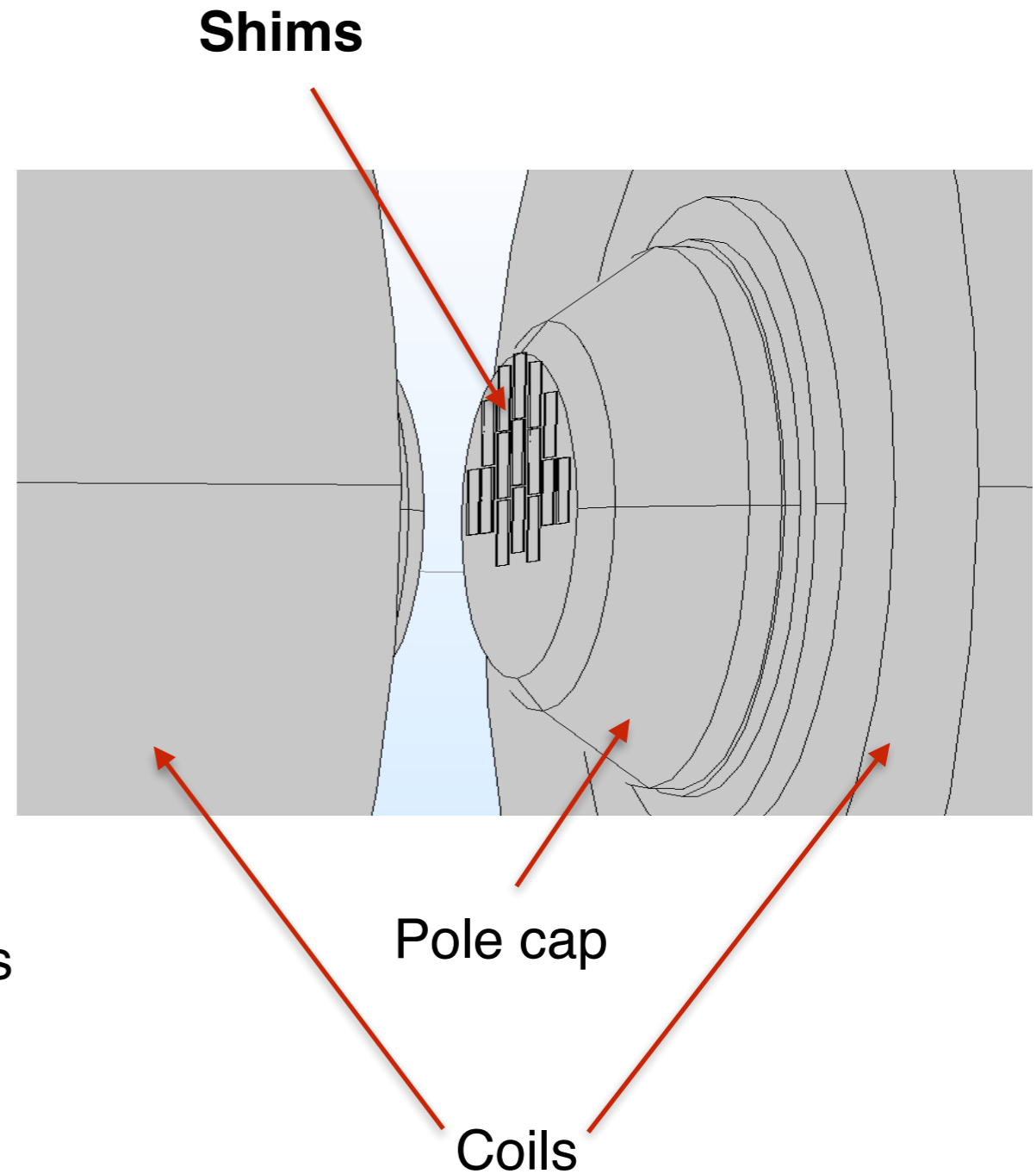
# APPENDIX 2 - COMSOL Simulations – Shimming

Shims used in the model:

- thin iron strips of  $430\ \mu\text{m} * 3\ \text{cm} * 1\ \text{cm}$
- added on the pole surface where poles are less closer due to skewness
- compensate the field in the region where it is smaller
- **Trial and error** procedure



Double shims



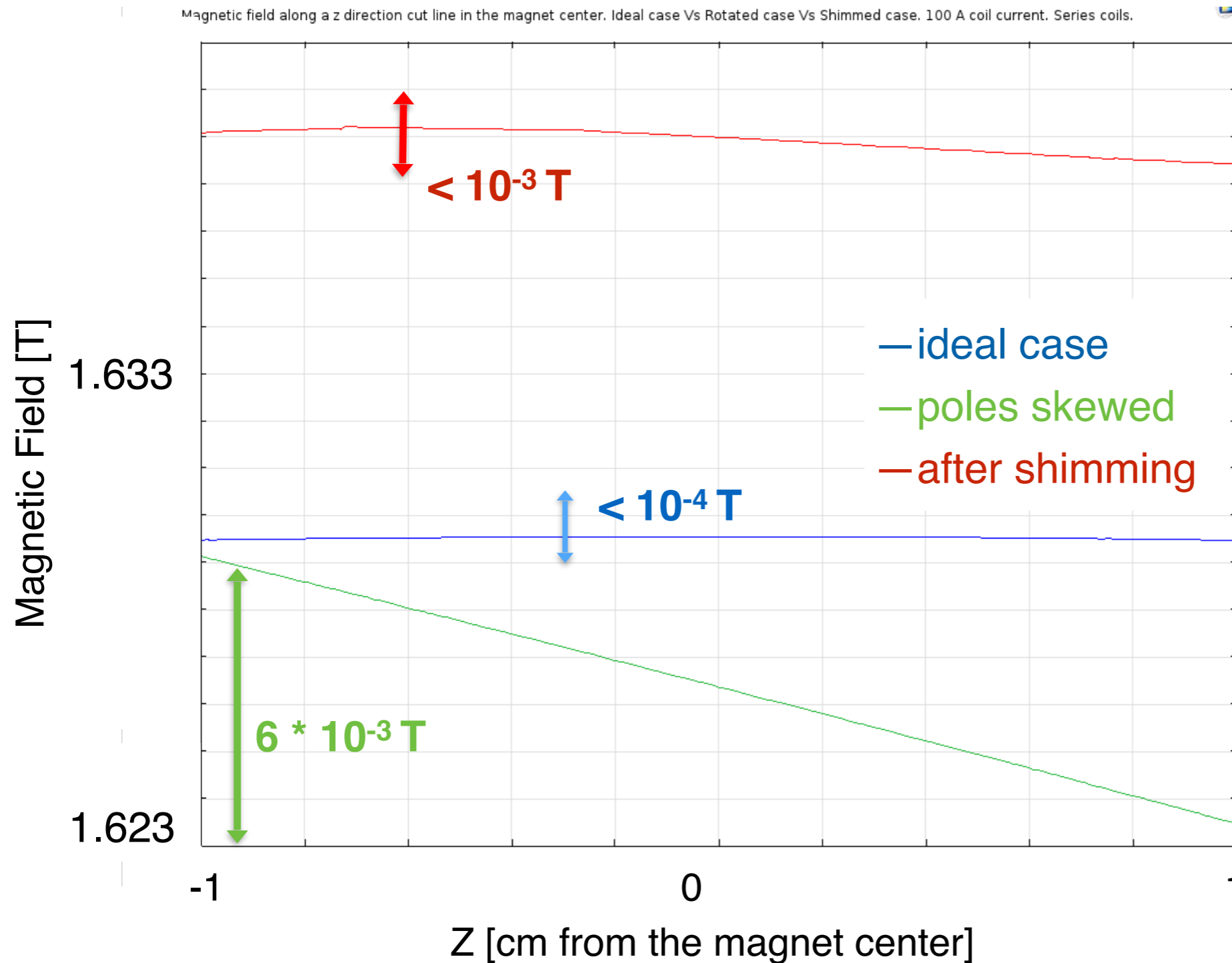
Shims

Pole cap

Coils



# APPENDIX 2 - COMSOL Simulations – Shimming



Field along Z line.  
Zoom in the region  
of 2 cm in the  
magnet center.

## Result:

- Shims increase the field homogeneity and compensate the pole skewness