Factorisation and Resummation for Jet Cross Sections Based on work with Thomas Becher (2309.17355)

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Introduction

Exclusive jet cross-sections Gaps between jets

- We are interested in cross sections of the form $\sigma\left(\boldsymbol{Q}_{0}\right) = \frac{1}{2\boldsymbol{Q}^{2}} \sum_{m=M}^{\infty} \prod_{i=1}^{m} \int \left[dp_{i}\right] \left|\mathcal{M}_{m}\left(\left\{\underline{p}\right\}\right)\right|^{2} \delta\left(\boldsymbol{Q}-E_{\mathrm{tot}}\right) \delta^{(d-1)}\left(\vec{p}_{\mathrm{tot}}\right) \Theta\left(\boldsymbol{Q}_{0}-2E_{\mathrm{out}}\right)$
- The energy veto $\Theta(Q_0 2E_{out})$ introduces non-global logarithms $\alpha_S \log\left(\frac{Q}{Q_0}\right) \sim 1$
- What does "out" mean?
 - Fixed cone cross section: "out" depends only on the hard scale dynamics
 - Sequential clustering: "out" also depends on the soft scale dynamics.

wist atts $2E_{\rm out} \leq Q_0$ Q_0 **Fixed** cone



Clustering Constraint

Figures adjusted from 1605.02737



Non-Global v.s. Clustering Logs



Due to correlated emissions.

CL

First emission changes gap for second emission

Due to uncorrelated emissions. Even exist in QED.



Non-Global and Clustering Logarithms (an incomplete history)

- NGLs first discovered by Dasgupta and Salam in 2001 (hep-ph/0104277)
- NLL NG resummation recently achieved. (GNOLE: 2111.02413, SCET: 2307.02283, PANSCALES: 2307.11142)
- LL Beyond leading color: (Weigert: hep-ph/0312050, Hatta,Ueda: 2011.04154, Plätzer et. al.: 1312.2448, 1802.08531,1905.08686)
- Resummation of Super Leading Logs (SLL): (Becher et. al. 2107.01212 and follow-up papers)
- Clustering Logarithms (CL): Discovered shortly after NGLs (Appleby, Seymour: hep-ph/ 0211426])
- Analysed in SCET: (R. Kelley, J.R. Walsh and S. Zuber: 1202.2361,1203.2923) A factorisation theorem for CL in SCET as a product of a hard and soft function was thought to be impossible

What does "out" mean?

- We run an inclusive k_T -type jet clustering on the partons $\{p_1, ..., p_n\}$, which yields the jet momenta $\{P_1, ..., P_{n_I}\}$.
- For each jet, decide whether it is "in" or "out", e.g.,
 - only the M hardest jets are "in" for M jet cross sections or (Such vetos are very common at the LHC)
 - only the jets which are in a cone with (half)-opening angle α around the thrust axis are "in"

• Then define
$$E_{\text{out}} = \sum_{j=1}^{n_{\text{J}}} P_j^0 \Theta_{\text{out}} \left(P_j \right)$$

k_T -type clustering algorithm

- 1. For a list of partons with momenta $\{p_1, ..., p_n\}$, determine the distances
 - $d_{ij} = \min(E_i^{2p}, E_j^{2p}) \frac{\Delta R_{ij}^2}{R^2}, \quad i \neq j \in \{1, \dots, n\}$ $d_i = E_i^{2p}, \quad i \in \{1, \ldots, n\},$ $p = 1: k_T$ p = 0: C/A $p = -1: Anti-k_T$
- 2. Find the minimum of the d_{ii} and d_i .
- and return to step 1.
- the list of particles, and return to 1.
- 5. Stop when no particles remain.

Determines the clustering distance Gives an approximate order in which things cluster

3. If it is a d_{ii} , combine the two partons into a single one with combined momentum $p_{ii} = p_i + p_i$

4. Otherwise, if the minimum is a d_i , declare the corresponding particle to be a jet, remove it from



Factorisation and Resummation

Factorisation Theorem

Factorisation for clustering:

It is convenient to have the hard particles ordered by energy

tering:
$$\sigma(Q,Q_0) = \sum_{m=M}^{\infty} \left\langle \mathcal{H}_m(\{\underline{n}\},\{\underline{z}\},Q,\mu) \otimes_{\underline{z}} \mathcal{S}_m(\{\underline{n}\},\{\underline{z}\},Q_0,\mu) \right\rangle \right\rangle$$
$$\mathcal{H}_m(\{\underline{n}\},\{\underline{z}\},Q) = \frac{1}{2Q^2} \left(\prod_{i=1}^m \int \frac{dE_i E_i^{d-3}}{\tilde{c}^{\epsilon}(2\pi)^2} \right) \widetilde{\mathcal{H}}_m(\{\underline{p}\}) \times (2\pi)^d \delta(Q - E_{\text{tot}}) \delta^{d-1}(\vec{p}_{\text{tot}}) \Theta_{\text{in}}(\{\underline{p}\}) \prod_{j=1}^m \delta\left(z_j - \frac{E_j}{E_{j-1}}\right)$$

$$\boldsymbol{\mathcal{S}}_{m}(\{\underline{n}\},\{\underline{\boldsymbol{z}}\},Q_{0}) = \sum_{X} \langle 0 \big| \boldsymbol{\mathcal{S}}_{1}^{\dagger}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}^{\dagger}(n_{m}) \big| X \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \theta \left(Q - \frac{2E_{\text{ot}}}{2E_{\text{ot}}} \right) \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \langle X \big| \boldsymbol{\mathcal$$

We need the energy fractions $z_i =$ simple product anymore

$$= \frac{E_i}{E_{i-1}}$$
 to solve Θ_{in} . Θ_{in} is not a





RG Evolution and Resummation Anomalous dimensions

The renormalised hard function satisfies an RGE:

$$\frac{d}{d\ln\mu}\mathcal{H}_m(\{\underline{n}\},\{\underline{z}\},Q,\mu) = -\sum_{l=M}^m \mathcal{H}_l(\{\underline{n}\},\{\underline{m}\},\{\underline{n}\},\underline{n}\},\{\underline{n}\},\{\underline{n}\},\{\underline{n}\},\underline{n}\},\{\underline{n}\},\{\underline{n}\},\{\underline{n}\},\underline{n}\},\{\underline{n}\},\underline{n}\},\{\underline{n}\},\underline{n}\},\underline{n}\},\{\underline{n}\},\underline{n}\},\underline{n}\},\{\underline{n}\},\underline$$

• The anomalous dimension is a matrix in multiplicity space

$$\boldsymbol{\Gamma}^{H} = \frac{\alpha_{s}}{4\pi} \begin{pmatrix} \boldsymbol{V}_{2} & \boldsymbol{R}_{2} & \boldsymbol{0} & \boldsymbol{0} & \dots \\ \boldsymbol{0} & \boldsymbol{V}_{3} & \boldsymbol{R}_{3} & \boldsymbol{0} & \dots \\ \boldsymbol{0} & \boldsymbol{0} & \boldsymbol{V}_{4} & \boldsymbol{R}_{4} & \dots \\ \boldsymbol{0} & \boldsymbol{0} & \boldsymbol{0} & \boldsymbol{V}_{5} & \dots \\ \vdots & \vdots & \vdots & \vdots & \ddots \end{pmatrix} + \dots$$

- R_m is obtained from the soft emission limit
- V_m is obtained from the soft gluon loop limit of $\mathscr{H}_m^{(1)}$

 $[\underline{z}], Q, \mu) \Gamma_{lm}^{H}(\{\underline{n}\}, \{\underline{z}\}, Q, \mu)$

of
$$\mathcal{H}_{m+1}^{(0)}$$

RG Evolution and Resummation Anomalous dimensions

• At NLO, the anomalous dimensions are given by

$$oldsymbol{V}_{m} = 2 \sum_{(ij)} \left(oldsymbol{T}_{i,L} \cdot oldsymbol{T}_{j,L} + oldsymbol{T}_{i,R} \cdot oldsymbol{T}_{j,R}
ight) \int \left[ds \ oldsymbol{R}_{m} = -4 \, \delta(oldsymbol{z}_{q}) \sum_{(ij)} oldsymbol{T}_{i,L}^{a} oldsymbol{T}_{j,R}^{\tilde{a}} W_{ij}^{q} \Theta_{\mathrm{in}} \left(oldsymbol{n}_{q}
ight) \ \mathrm{Strong \, energy \, ordering!}$$

 $oldsymbol{v}_m = oldsymbol{v}_m^{
m fc} \quad oldsymbol{r}_m = rac{\delta(z_q) r_m^{
m fc}}{m} \quad oldsymbol{d}_m = rac{\delta(z_{qr}) F(z_r)}{k}$

 $[\Omega_q] W^q_{ii}$

At NNLO the structure of the anomalous dimension gets more complicated:

- New and interesting ullet
- Contains 4-parton correlators \bullet
- Depends on details of clustering, e.g. WTA or E scheme

Parton Shower (@Leading Color)

• Shower time $t = \frac{\alpha_S}{4\pi} \log(\frac{Q}{Q_0})$

- Shower generates real emissions by randomly choosing dipoles and emission times according to V_m .
- Stops, once a new emission does not satisfy the "in"-condition.
- Angular integrals are done with the MC-sampling
- Energy integrals are trivial at LL due to the $\delta(z_i)$ term in \boldsymbol{R}_m
- The only additional difficulty related to the clustering is to determine the "in" condition for each new emission

Strongly Ordered Clustering

Example Situation for diet production Anti k_T C/A k_T 2 2 2 3 -2



Phase space, where the second emission would be in



3

LL Features

Clustering Effects With Jet Veto On Extra Jets









Effective Gap Area

- Note, if there is no gap then there is no veto and there are no large logs.
- unitarily.
- Cross section becomes independent of $t(Q_0)$

• With the clustering, the gap becomes smaller with each emission. At some shower time it should vanish completely and the shower should evolve

Effective Gap Area







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How good is the primary approximation?

Just ignoring the non-global effects due to "new" dipoles (pretending the gluons are photons) gets you within 10% of the correct result for k_{t} -clustering!

 $\Delta \eta$ 2.0

1.0

0.2

Note that 10% is also roughly the effect of subleading color or NLL corrections!

The table lists the ratio $(\Sigma_{\text{primary}}(t) - \Sigma_{\text{LL}}(t))/\Sigma_{\text{LL}}(t)$ at t = 0.07

anti- k_t [%] C/A[%] $k_t \, [\%]$ 32.0 ± 1.4 66.6 ± 1.5 9.1 ± 1.0 64.7 ± 1.0 17.8 ± 0.8 -4.7 ± 0.6 42.8 ± 0.6 3.9 ± 0.5 -1.2 ± 0.5



Reduction of NG Effects

The strong suppression of the gap fraction due to NGL is driven by collinear emissions into the gap: Without clustering,



collinear emissions soon

At shower times of $t \sim 0.07$ roughly 10% of the gluons emitted into the gap are emitted with $0.3 < \cos \theta < 0.4$, i.e. $66^{\circ} < \theta < 73^{\circ}$

The plots show at which angle from the emitting dipole gluons are radiated into the gap.



Reduction of NG Effects

The strong suppression of the gap fraction due to NGL is driven by collinear emissions into the gap:



The plots show at which angle from the emitting dipole gluons are radiated into the gap.





Conclusion

- Presented a first factorisation theorem applicable to NG observables with clustering effects
 - Derived the 1-Loop anomalous dimension
 - Simplified sequential clustering algorithms at LL
- LL result was implemented in a parton shower. Our result agrees with results previously calculated with different methods. Using the shower we
 - analysed how the "effective gap" seen by emissions shrinks with larger t (smaller Q_0)

shed light on how clustering suppresses the importance of collinear emissions



Outlook

- calculate the two loop anomalous dimension to go to NLL
- expand our analysis to more general, possibly double logarithmic, observables (like jet masses)
- analyse the effect of subleading color
- look at hadron collider observables including also SLL

Back-up slides



Global, Non-Global, Clustering, Super-Leading What is what?

• All of these are logarithms of $\frac{Q}{Q_0} \gg 1$

Global	Non-Global	Super-leading	Clustering
Towers of $\alpha_S \log\left(\frac{Q}{Q_0}\right)$ expected from naive exponentiation of the fixed order result. We only need to consider the primary hard partons as emitters. (Concept does not really make sense beyond LL)	Even at LL, <u>non-abelian</u> strongly ordered emissions destroy the naive exponentiation starting from α_S^2 . With every additional emission one gets new dipoles that can again radiate and generate new "non-global" logs.	At hadron colliders, starting at α_S^3 and beyond LC, collinear singularities do no longer cancel exactly between real and virtual emissions due to <u>Glauber</u> exchanges. Starting from α_S^4 these effects are super-leading.	If the shape of the gap changes with every emission, then even <u>abelian</u> emissions do n exponentiate. Leading additional non-global lo $\operatorname{at} \alpha_S^2$.

In general, one has all of those and they mix. Instead of listing which types of logs exists for a given observable, one should rather state which logs are absent.



RG Evolution and Resummation

- The resummed cross section becomes $\sigma(Q_0) = \sum_{l=M}^{\infty} \left\langle \mathcal{H}_l\left(\{\underline{n}\}, \{\underline{z}\}, Q, \mu_h\right) \sum_{m \ge l} U_{lm}\left(\{\underline{n}\}, \{\underline{z}\}, Q, \mu_h\right) \right\rangle$
 - with the evolution kernel $U(\{\underline{n}\}, \{\underline{z}\}, \{\underline{z}\},$
- We implement this equation in a Parton shower with the shower time

$$\int_{\mu_s}^{\mu_h} \frac{d\mu}{\mu} \, \mathbf{\Gamma}^H = \int_{\alpha(\mu_s)}^{\alpha(\mu_h)} \frac{d\alpha}{\beta(\alpha)} \, \frac{\alpha}{4\pi} \, \mathbf{\Gamma}^{(1)} = \frac{1}{2\beta_0} \ln \frac{\alpha(\mu_s)}{\alpha(\mu_h)} \, \mathbf{\Gamma}^{(1)} = t \, \mathbf{\Gamma}^{(1)}$$

- Define $\mathcal{H}_m(t) \equiv \mathcal{H}_M(\{\underline{n}\}, \{\underline{z}\}, Q, \mu_h) \mathcal{U}$
- Iterative solution $\mathcal{H}_{M+1}(t) = \int_0^t dt' \mathcal{H}_M(t')$
- And combine everything as $\sigma_{LL}(t) =$
- At leading color, one can reformulate the solution as a parton shower (LL: Becher et. al.: 1803.07045,2006.00014, NLL: Becher, Schalch, Xu: 2307.02283)

$$\underline{z}, \mu_s, \mu_h) \otimes_{\underline{z}} \boldsymbol{\mathcal{S}}_m\left(\{\underline{n}\}, \{\underline{z}\}, Q_0, \mu_s\right)\right\rangle,$$

$$\mu_s, \mu_h) = \mathbf{P} \exp\left[\int_{\mu_s}^{\mu_h} \frac{d\mu}{\mu} \mathbf{\Gamma}^H(\{\underline{n}\}, \{\underline{z}\}, \mu)\right]$$

$$\mathcal{J}_{Mm}(\{\underline{n}\},\{\underline{z}\},\mu_h,\mu_s)$$

)
$$oldsymbol{R}_M \, e^{(t-t') oldsymbol{V}_{M+1}}$$

$$\sum_{n=2}^{\infty} \left\langle \mathcal{H}_m(t) \otimes_z \mathbf{1} \right
angle$$

Strongly Ordered Clustering

- Note: If the jet clustering on $\{p_1, \dots, p_m\}$ yields the jets $\{P_1, \dots, P_{n_n}\}$, then the clustering on $\{p_1, \ldots, p_m, p_{m+1}\}$ either
 - 1. yields the same jets $\{P_1, \ldots, P_{n_i}\}$

2. or
$$\{P_1, \dots, P_{n_J}, p_{m+1}\}$$

- In case 1., the "in" condition is satisfied
- In case 2., we only need to check the new jet
- How to simplify the clustering, taking into account the strung ordering?

Factorisation Theorem

Factorisation for fixed cones: $\int \sigma(Q, Q_0)$

$$\begin{split} &\Theta_{\mathrm{in}}(\{\underline{p}\}) = \Theta_{\mathrm{in}}(n_1)\Theta_{\mathrm{in}}(n_2)\dots \\ & \text{is very simple} \end{split} \quad \mathcal{H}_m(\{\underline{n}\}, \zeta) \end{split}$$

$$\boldsymbol{\mathcal{S}}_{m}(\{\underline{n}\},Q_{0}) = \sum_{X} \langle 0 \big| \boldsymbol{\mathcal{S}}_{1}^{\dagger}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}^{\dagger}(n_{m}) \big| X \rangle \langle X \big| \boldsymbol{\mathcal{S}}_{1}(n_{1}) \dots \boldsymbol{\mathcal{S}}_{m}(n_{m}) \big| 0 \rangle \theta \left(Q - 2E_{\text{out}} \right)$$

$$egin{aligned} & = \sum_{m=M}^{\infty} \left\langle \mathcal{H}_m(\{\underline{n}\},Q,\mu)\otimes \mathcal{S}_m(\{\underline{n}\},Q_0,\mu)
ight
angle \\ & Q) = rac{1}{2Q^2} \left(\prod_{i=1}^m \int rac{dE_iE_i^{d-3}}{ ilde{c}^\epsilon(2\pi)^2}
ight) \widetilde{\mathcal{H}}_m(\{\underline{p}\}) imes \\ & (2\pi)^d \delta(Q-E_{\mathrm{tot}}) \delta^{d-1}(ec{p}_{\mathrm{tot}}) \Theta_{\mathrm{in}}(\{\underline{p}\}) \end{aligned}$$



k_T -Clustering With Central Rapidity Gap

As a check, we compared with (Delenda, Appleby, Dasgupta, Banfi hep-ph/0610242) and reproduced their result.

Here and in the following, we always plot the gap fraction for diet production: $\Sigma(t)$ σ_{B}



Effect of k_r jet-clustering on the gap fraction for a fixed central rapidity gap of $\Delta \eta = 1$. In this set-up, emissions can never cluster with the primary jets.



Example Situation for diet production



Primary particles

- First emission "in"
- Second emission "in"
- Second emission "out"



Phase space, where the second emission would be "in"

Example Situation for diet production



Phase space, where the second emission would be in

Example Situation for diet production

Anti k_T



Take Away The "in" region for p_{m+1} is obtained by Anti k_T Putting a "circle" of radius R around every jet $\{P_1, ..., P_{n_I}\}$

No growth! (Like fixed cones)

Putting a "circle" of radius $\delta_i \leq R$ around every particle $\{p_1, \ldots, p_m\}$, where δ_i is the distance with which p_i became a jet or was clustered with a harder parton

C/A

K_T Putting a "circle" of radius R around every particle $\{p_1, ..., p_m\}$: Fast growth!

Steady growth!