# Resonance-aware NLOPS matching for off-shell top-pair plus tW production with semileptonic decays

based on 2307.15653 (in collaboration with T. Jezo, S. Pozzorini)

# IK **University of Sussex**

Jonas M. Lindert



**UK Research** and Innovation

# HP2 Turin, 10th Sep 2024



# Resonanc for off-shell t

(in collab

# IK University of Sussex

# with top-pair and Wt production and decay NLO+PS predictions for



Turin, 10th Sep 2024

 $\overline{\phantom{a}}$ 

### Jonas M. Lindert

HP2 Buenos Aires, 8th September 2016



*work in collaboration with:*  T. Ježo*,* P. Nason, C. Oleari, S. Pozzorini *based on [Ježo, Nason; '15] & [Ježo, JML, Nason, Oleari, Pozzorini; '16]*



# The fate of the Universe



- $M_t/\text{GeV}$
- •top-mass measurements at the LHC via combination of different strategies: - total x-section, tt+jet, kinematic reconstruction, kinematic edges,….
- many techniques rely on kinematic information of top decay products
	- need realistic MC modelling

• Also: tt ubiquitous background, QCD laboratory, anomalous coupling, etc….

### *[ATLAS+CMS; arXiv:2402.08713]*



# @ NLO+PS



# Top-pair production and decay





# @ NLO+PS

# Top-pair production and decay

# NLO incl. off-shell/non-resonant/ interference effects

 $\boldsymbol{q}$ 

 $\overline{q}$ 



- •Consistent inverse-width expansion
- •Matrix-element based resonance histories
- Semi-leptonic decays

What's new? *[T. Jezo, JML, S. Pozzorini, [2307.15653](https://arxiv.org/abs/2307.15653)]*

# bb4l *[Jezo, JML, Nason, Oleari, Pozzorini, '16]*

Physics features:

- exact non-resonant / off-shell / interference / spin-correlation effects at NLO
- consistent NLO+PS treatment of top resonances, including quantum corrections to top propagators and off-shell top-decay chains thanks to POWHEG-BOX-RES
- unified treatment of top-pair and Wt production with interference at NLO
- access to phase-space regions with **unresolved b-quarks** and/or jet vetoes

### Resonance-unaware NLOPS matching in POWHEG and in the IR can control terms are controlled the IR can controlled through universal subtraction terms are c

### → Already at **NLO**: (B), radius integrated counterparts in the integrated counterparts

- FKS (and similar CS) subtraction does not preserve virtuality of intermediate resonances • FKS (and similar CS) subtraction does not preserve virtuality of in
	- Real (R) and Subtraction-term (S~B) with different virtuality of intermediate resonances  $(\Phi_{\mathbf{D}} \ \Phi_{\mathbf{D}}) \longleftrightarrow \Phi_{\mathbf{D}}^{(\alpha)}$  from FKS mannings  $k = 1$  $(\Phi_B, \Phi_{\rm rad}) \longleftrightarrow \Phi_{\rm R}^{(\alpha)}$  from FKS mappings
- IR cancellation spoiled

■ severe efficiency problem! Severe emeloney problem. efficiency problen  $\overline{\phantom{a}}$ 

- $\triangleright$  More severe problems at **NLO+PS**: **NLO+PS U**<br>
N∪ O⊥DC *<sup>B</sup>*(B) (B*, k*T) d(↵)
- in POWHEG: • in POWHEG:  $d\sigma = \bar{B}(\Phi_B) d\Phi_B \left[ \Delta(q_{\rm cut}) + \sum \Delta(k_{\rm T,c}) \frac{R_C \Phi_B}{R_G} \right]$

• also subsequent radiation by the **PS** itself reshuffles internal momenta and does in general not preserve the virtuality of intermediate resonances. Let us now discuss the problems that arise in the presence of resonances. The first subsequent radiation by the  $\bullet$  stock resinances internation rememerate and does in ediscion matrix elements in the soft and collinear limits in (2.2) the substantial collinear limits, the substantial collinear limits, the substantial collinear limits, the substantial collinear limits, the substantial col • also subsequent radiation by the PS itself reshuffles internal mon preserve the virtuality of intermediate resonances.

### $\Rightarrow$  expect uncontrollable distortion of important kinematic shapes!

and in each sector the IR cancellations are controlled through universal subtractions are controlled through universal subtractions are controlled through universal subtraction terms of  $\mathcal{L}$ 

Sudakov form-factor generated from uncontrollable R/B ratios: reador of the late of the sect series the sect section of the section of <sup>R</sup> )*/B*(B) and is unitarised through Sudakov form factors defined as

$$
\Delta\left(\Phi_B,p_\mathrm{T}\right)=\exp\left\{-\sum_{\alpha}\int_{k_\mathrm{T}>p_\mathrm{T}}\frac{R(\Phi_\mathrm{R}^{(\alpha)})}{B(\Phi_\mathrm{B})}\,\mathrm{d}\Phi_\mathrm{rad}^{(\alpha)}\right\}
$$

 $\mathbf{r}$ 



Rigorous solution to all these issues within POWHEG-BOX-RES according to *[Ježo, Nason; '15]*

Idea: *preserve invariant mass of intermediate resonances at all st* 

### ✓ **NLO**:

- Split phase-space integration into regions dominated by
- within a given resonance history modify FKS mappings, s that they *always* preserve intermediate resonances ⇒ R and S~B *always* with same virtuality of intermedent  $\Rightarrow$  IR cancellation restored

### ✓ **NLO+PS**:

- R and B related via modified FKS mappings
	- $\Rightarrow$  R/B ratio with fixed virtuality of intermediate resonances
	- $\Rightarrow$  Sudakov form-factor preserves intermediate resonances

### ✓ **PS**:

- pass information about resonance histories to the shower (via extension of LHE)
- tell PS to respect intermediate resonances (available in Pythia8)

*Lages!*  
\n
$$
\bar{B}_{h}(\Phi_{B}) = \omega_{h}^{(\text{hist})}(\Phi_{B}) \bar{B}(\Phi_{B})
$$
\na single resonance history  
\nsuch  
\n
$$
\omega_{h,c}(\Phi_{R}) = \rho_{h,c}(\Phi_{R}) \left[ \sum_{h' \in \mathcal{H}} \sum_{c' \in \mathcal{C}(h')} \rho_{h',c'}(c') \right]
$$
\nsuch  
\ndiate resonances  
\nd $\sigma = \sum_{h \in \mathcal{H}} \bar{B}_{h}(\Phi_{B}) d\Phi_{B} \left[ \Delta_{h}(q_{\text{cut}}) + \sum_{c \in \mathcal{C}(h)} \Delta_{h}(k_{\text{T},c}) \frac{R_{h,c}(\Phi_{R,c})}{B_{h}(\Phi_{B})} d\Phi_{\text{rad}} \right]$ 

# Resonance-aware NLOPS matching in POWHEG-RES







Key advantage I: Interplay between top-pair and Wt  $-4$   $-2$  0 2 4

 $\eta(t)$ 



Phys. Rev. Lett. 121 (2018) 152002

 $m_{b\ell}^{\text{minimax}} \equiv \min\{\max(m_{b_1\ell_1}, m_{b_2\ell_2}), \max(m_{b_1\ell_2}, m_{b_2\ell_1})\}$ 

For tt (double-resonant) at LO:  $m_{b\ell}^{\text{minimax}} < \sqrt{m_t^2 - m_W^2}$ 

- → sensitivity to off-shell effects/ tt-Wt interference beyond endpoint
- → measure top width *[Herwig, Jezo, Nachman, '19]*

"Probing the quantum interference between singly and doubly resonant top-quark production in pp collisions at  $\sqrt{s}$  = 13 TeV with the ATLAS detector"





# Interference effects between top-pair and Wt production

In traditional approach only hardest radiation is generated by POWHEG:

- $\blacktriangleright$  emission off decays are mostly generated by the shower.
- ‣ Multiple-radiation scheme: The full real matrix element is decomposed into a sum of terms
	- resonances.
	-

BUT: for top-pair (or single-top) production and decay, emission from production is almost

• keep hardest overall emission and additionally hardest emission from any of *n* decaying *. introduced in [Campbell, Ellis, Nason, Re; '15]* 

always the hardest. The first term in the square bracket corresponds to the probability that no radiation is



Key advantage II: Multiple-radiation scheme the wavailage in resource radiation serioris



Consistent inverse-width expansion at NLO  
\n
$$
[J_{PZO}, JML, Pozorini, 2307.15653]
$$
\nNNVA:  $d\sigma_{\text{prod}} \times d\sigma_{\text{prod}}$ , where  $\Gamma = \int_{\text{dec}} d\Gamma$  This hold to all orders!  
\n $\int_{\text{dec}} d\sigma_{\text{prod}} \times d\sigma_{\text{NLO}} = d\sigma_0 + d\sigma_1$ ,  $d\Gamma_{\text{NLO}} = d\Gamma_0 + d\Gamma_1$ ,  $\Gamma_{\text{NLO}} = \Gamma_0 + \Gamma_1$   
\n $\int_{\text{dec}} d\sigma_{\text{prod}}^{\text{NLO}} d\sigma_{\text{prod}} \times d\sigma_{\text{NLO}} = d\sigma_0 + d\sigma_1 - d\sigma_1 \frac{\Gamma_1}{\Gamma_{\text{NLO}}}$  spurious  
\nConsistent NLO expansion of NWA:  $d\sigma_{\text{NLO}} = d\sigma_0 + d\sigma_1$ ,  $d\Gamma_{\text{NLO}} = d\Gamma_0 + d\Gamma_1$ ,  $\frac{1}{\Gamma_{\text{NLO}}} \rightarrow \frac{1}{\Gamma_0} \left(1 - \frac{\Gamma_1}{\Gamma_0}\right)$   
\n $\int_{\text{dec}} d\sigma_{\text{prod}}^{\text{NLOexp}} d\sigma_{\text{prod}} \times d\sigma_{\text{NLO}} = d\sigma_0 + d\sigma_1$ 

$$
\sigma \frac{dI}{T}, \text{ where } \Gamma = \int_{\text{dec}} dT \qquad \text{This hold to all orders!}
$$
\n
$$
\int_{\text{dec}} d\sigma_{\text{prod} \times \text{dec}} = d\sigma
$$
\nVA:  $d\sigma_{\text{NLO}} = d\sigma_0 + d\sigma_1$ ,  $d\Gamma_{\text{NLO}} = d\Gamma_0 + d\Gamma_1$ ,  $\Gamma_{\text{NLO}} = \Gamma_0 + \Gamma_1$ \n
$$
\int_{\text{dec}} d\sigma_{\text{prod} \times \text{dec}}^{NLO} = d\sigma_0 + d\sigma_1 - d\sigma_1 \frac{\Gamma_1}{\Gamma_{\text{NLO}}}
$$
\nSolutions\n
$$
\int_{\text{dec}} d\sigma_{\text{prod} \times \text{dec}}^{NLO_{\text{exp}}} = d\sigma_0 + d\sigma_1, \qquad d\Gamma_{\text{NLO}} = d\Gamma_0 + d\Gamma_1, \quad \frac{1}{\Gamma_{\text{NLO}}} \to \frac{1}{\Gamma_0} \left(1 - \frac{\Gamma_1}{\Gamma_0}\right)
$$
\n
$$
\int_{\text{dec}} d\sigma_{\text{prod} \times \text{dec}}^{NLO_{\text{exp}}} = d\sigma_0 + d\sigma_1
$$

$$
\sigma \frac{dI}{\Gamma}, \text{ where } \Gamma = \int_{\text{dec}} d\Gamma \qquad \text{This hold to all orders!}
$$
\n
$$
\int_{\text{dec}} d\sigma_{\text{prod}A\text{dec}} = d\sigma
$$
\nVA:  $d\sigma_{\text{NLO}} = d\sigma_0 + d\sigma_1$ ,  $d\Gamma_{\text{NLO}} = d\Gamma_0 + d\Gamma_1$ ,  $\Gamma_{\text{NLO}} = \Gamma_0 + \Gamma_1$ \n
$$
\int_{\text{dec}} d\sigma_{\text{prod}A\text{dec}}^{NLO} = d\sigma_0 + d\sigma_1 - d\sigma_1 \frac{\Gamma_1}{\Gamma_{\text{NLO}}}
$$
\nSolutions\nof NWA:  $d\sigma_{\text{NLO}} = d\sigma_0 + d\sigma_1$ ,  $d\Gamma_{\text{NLO}} = d\Gamma_0 + d\Gamma_1$ ,  $\frac{1}{\Gamma_{\text{NLO}}} \rightarrow \frac{1}{\Gamma_0} \left(1 - \frac{\Gamma_1}{\Gamma_0}\right)$ \n
$$
\int_{\text{dec}} d\sigma_{\text{prod}A\text{dec}}^{NLO_{\text{exp}}} = d\sigma_0 + d\sigma_1
$$

Generalise to multiple resonances:  $d\sigma_{\rm prodxdec}^{\rm NLO_{exp}} = \left[ d\sigma_0 + \sum_{\tau} \sigma_{\tau}^2 \right]$  $\frac{r}{r}$ 

$$
d\sigma_{spurious} = d\sigma_{prod \times dec}^{NLO} - d\sigma_{prod \times dec}^{NLO_{exp}} = \delta \kappa_{sp}
$$

$$
\sum \left( d\sigma_0 \frac{d\Gamma_{r,1}}{d\Gamma_{r,0}} - d\sigma_0 \frac{\Gamma_{r,1}}{\Gamma_{r,0}} \right) + d\sigma_1 \left[ \left( \prod_{r \in \mathcal{R}} \frac{d\Gamma_{r,0}}{\Gamma_{r,0}} \right) \right]
$$

E.g.:  $\delta \kappa_{\text{spurious}}^{t\bar{t}+X} \simeq -2 \frac{d\sigma_1}{d\sigma_0} \frac{\Gamma_{t,1}}{\Gamma_{t,0}} \simeq +17\% \frac{d\sigma_1}{d\sigma_0}$ !  $_{\rm purious}\,{\rm d}\sigma_{\rm prod\times dec}^{\rm LO}$ 



Consistent inverse-width expansion at NLOPS

n ME

Start from fNLO in NWA: 
$$
d\sigma_{\text{prod,dec}}^{\text{NLO_{exp}}} = \left[ d\sigma_0 + \sum_r \left( d\sigma_0 \frac{d\Gamma_{r,1}}{d\Gamma_{r,0}} - d\sigma_0 \frac{\Gamma_{r,1}}{\Gamma_{r,0}} \right) + d\sigma_1 \right] \left( \prod_{r \in \mathcal{R}} \frac{d\Gamma_{r,0}}{\Gamma_{r,0}} \right)
$$
  
\n
$$
\left( + \text{fNLO for off-shell computation:} \quad d\sigma_{\text{off-shell}}^{\text{NLO_{exp}}} = \left( \prod_{r \in \mathcal{R}} \frac{\Gamma_{r,\text{NLO}}}{\Gamma_{r,0}} \right) \left[ d\sigma_{\text{off-shell}}^{\text{NLO}} - \left( \sum_{r \in \mathcal{R}} \frac{\Gamma_{r,1}}{\Gamma_{r,0}} \right) d\sigma_{\text{off-shell}}^{(0)} \right]
$$
\n
$$
\left( + \text{POWHEG for off-shell computation:} \quad \bar{B}_h(\Phi_B) \right|_{\text{exp}} = \left( \prod_{r \in \mathcal{R}} \frac{\Gamma_{r,\text{NLO}}}{\Gamma_{r,0}} \right) \left[ \bar{B}_h(\Phi_B) - \left( \sum_{r \in \mathcal{R}} \frac{\Gamma_{r,1}}{\Gamma_{r,0}} \right) B_h(\Phi_B) \right]
$$
\nuse  $\Gamma_{r,\text{NLO}}$  in  
\n
$$
R_{h,c}^{\text{(hard)}}(\Phi_R) \Big|_{\text{exp}} = \left( \prod_{r \in \mathcal{R}} \frac{\Gamma_{r,\text{NLO}}}{\Gamma_{r,0}} \right) R_{h,c}^{\text{(hard)}}(\Phi_R)
$$
\n
$$
\left. \frac{\sigma_{\text{bb41-s1}}}{\sigma_{\text{hvq+ST}}} \right|_{\text{no 1/Tt expansion}} = 1.074 \qquad \text{VS.} \qquad \left. \frac{\sigma_{\text{bb41-s1}}}{\sigma_{\text{hvq+ST}}} \right|_{\text{with 1/Tt expansion}} = 1.012
$$

# Matrix element-based resonance histories



*\*illustration courtesy of T. Jezo*





 $P_1 = B_{t\bar{t}}$  $P_2 = B_t w^+$ 

squared-ME in pole approximation

 $P_3 = B_{\bar{t}W^-}$ 

 $\left.\rho_{t\bar{t}}^{\mathrm{(hist)}}(\Phi_{\mathrm{B}})\right|_{\mathrm{ME}}=\left|\mathcal{A}_{t\bar{t}}\right|^{2}\quad\left.\rho_{\bar{t}W^{+}}^{\mathrm{(hist)}}(\Phi_{\mathrm{B}})\right|_{\mathrm{ME}}=\left|\mathcal{A}_{\bar{t}W^{+}}\right|^{2}\quad\left.\rho_{tW^{-}}^{\mathrm{(hist)}}(\Phi_{\mathrm{B}})\right|_{\mathrm{ME}}=\left|\mathcal{A}_{tW^{-}}\right|^{2}$ 



## Matrix element-based resonance histories





 $Q_{\text{off-shell}} = \max \left\{|Q_t - m_t|, |Q_{\bar{t}} - m_t|\right\} > 60\,\text{GeV} \,.$ 

Different resonance history projectors agree at <1% level!

## Matrix element-based resonance histories

Might open the door to tt vs tW separation. Similar to "matrix-element methods". However, remember: here separation at LO + Real [Kondo*, '88*]





$$
ME-based \t A_{\text{full}} = A_{t\bar{t}} + A_{\bar{t}W^+} + A_{tW^-} + A_{\text{rem}}
$$

$$
\text{Naive} \quad \rho_{t\bar{t}}^{(\text{hist})}(\Phi_{\text{B}})\Big|_{\text{naive}} = W_t(p_t)W_t(p_{\bar{t}}) \quad \rho_{\bar{t}W^{\pm}}^{(\text{hist})}(\Phi_{\text{B}})\Big|_{\text{naive}} = \frac{\chi m_t^2}{E_{\text{T},b}^2}W_t(p_{\bar{t}}) \quad W_t(p) = \frac{M_t^4}{(p^2 - M_t^2)^2 + \Gamma_t^2 M_t^2}
$$

$$
\mathsf{ME} \quad \begin{aligned}\n\rho_{t\bar{t}}^{(\text{hist})}(\Phi_{\text{B}})|_{\text{ME}} &= |\mathcal{A}_{t\bar{t}}|^2, \\
\rho_{\bar{t}W^{\pm}}^{(\text{hist})}(\Phi_{\text{B}})|_{\text{ME}} &= |\mathcal{A}_{\bar{t}W^{\pm}}|^2, \\
\rho_{\bar{t}W^{\pm}}^{(\text{hist})}(\Phi_{\text{B}})|_{\text{ME}'} &= |\mathcal{A}_{\bar{t}W^{\pm}}|^2 - |\mathcal{A}_{\bar{t}W^{\pm}}|^2 - |\mathcal{A}_{\bar{t}W^-}|^2 \\
\rho_{\bar{t}W^{\pm}}^{(\text{hist})}(\Phi_{\text{B}})|_{\text{ME}''} &= |\mathcal{A}_{\bar{t}W^{\pm}}|^2, \\
\rho_{\bar{t}W^{\pm}}^{(\text{hist})}(\Phi_{\text{B}})|_{\text{ME}'} &= |\mathcal{A}_{\bar{t}W^{\pm}}|^2, \\
\rho_{\bar{t}W^{\pm}}^{(\text{hist})}(\Phi_{\text{B}})|_{\text{ME}''} &= |\mathcal{A}_{\bar{t}W^{\pm}}|^2 - |\mathcal{A}_{\bar{t}W^{\pm}}|^2.\n\end{aligned}
$$



17

### Semi-leptonic tt  $Sami-lantonic  $t\bar{t}$$ ¯and *tW* production with semi-leponic decays, i.e.

 $pp\to \ell^\pm \nu_\ell jj b\bar{b}$ 

				$\bullet$ $\infty$
$\alpha_{\rm S}^n \alpha^m$	dominant subprocesses	type	order	
$\alpha_{\rm S}^4 \alpha^2$	$W^{\pm}b\bar{b}+2$ jets	$V+HF$	<b>NNLO</b>	
$\alpha_{\rm S}^3 \alpha^3$	tiny interference			
	$t\bar{t}+tWb$	$t\bar{t}+tW$	4FNS LO	
	$gq \rightarrow tq^{\prime}\bar{b} + 1$ jet	$t$ -chanel single-top	4FNS NLO	$\infty$
$\alpha_{\rm S}^2 \alpha^4$	$q\bar{q}' \rightarrow t\bar{b} + 2$ jets	s-chanel single-top	<b>NNLO</b>	
	$W^{\pm}Z$ + 2 jets with $Z \rightarrow b\overline{b}$	VV	<b>NNLO</b>	
	$W^{\pm} j j + 2 b$ -jets	<b>VBF</b>	<b>NNLO</b>	
$\alpha_{\rm S}^1 \alpha^5$	tiny interference			
$\alpha^6$	$W^{\pm} Z jj$ with $Z \rightarrow b\overline{b}$	<b>VBS</b>	LO	
	$W^{\pm} Z V$ with $Z \rightarrow b\bar{b}$ , $V \rightarrow jj$	VVV	LO	



 $pp \to \ell^{\pm} \nu_{\ell} q \bar{q}' b \bar{b}$ : [Denner, Pellen; '17]  $pp \to \ell^\pm \nu_\ell q \bar{q}^\prime$  $b\bar{b}$  : [Denner, Pellen; '17]



18

### Semi-leptonic tt Semi-leptonic tt





19

### <sup>493</sup> In this section we present the new bb4l-sl version of the bb4l generator, which is applicable to Semi-leptonic tt: DD41-si Semi-leptonic tt: bb4l-sl





### <sup>493</sup> In this section we present the new bb4l-sl version of the bb4l generator, which is applicable to Semi-leptonic tt: DD41-si Semi-leptonic tt: bb4l-sl







bb4l-sl vs. on-shell top-pair plus single-top



bb4l-sl vs. on-shell top-pair plus single-top







•Large differences between ST-DR and ST-DS in the tail of pTl

•bb4l agrees at O(1%) with ST-DS

bb4l-sl vs. on-shell top-pair plus single-top





- •Control of reconstructed top-mass crucial for top-mass measurements
- 

•Significantly smaller shower effects (and MEC) in bb4l-sl compared to hvq+ST

- ▶ Precision NLOPS predictions for off-shell tt+Wt crucial for top-mass measurements and backgrounds in searches.
- ‣ Resonance-aware matching mandatory
- ‣ Inverse-width expansion in off-shell fNLO and NLOPS computations ensures narrow-width limit. Numerical impact can be significant.
- ‣ Matrix-element based projectors indicate small remaining systematics in RES method.
- 
- 
- ▶ Semi-leptonic tt x decay available in **bb4l-sl** approximation (valid for  $|m_{j_1j_2} m_W|$  < 30 GeV) ‣ percent-level agreement of bb4l-sl with hvq+ST in inclusive phase-space ‣ Crucial shape-effects and reduced shower dependency with bb4l-sl

Conclusions

- exact non-resonant / off-shell / interference / spin-correlation effects at NLO
- unified treatment of top-pair and Wt production and  $\vert$  a with interference at NLO
	- access to phase-space regions with unresolved bquarks and/or jet vetoes
	- consistent NLO+PS treatment of top resonances, including quantum corrections to top propagators and off-shell top-decay chains

 $\sqrt{\frac{1}{2}}$ Standard POWHEG matching:

- $\left| \begin{array}{c} \alpha & \beta \end{array} \right|$  interference in the Postandard FKS/CS subtraction does • Standard FKS/CS subtraction does not preserve virtuality of intermediate resonances → R and B (~S) with different virtualities.
	- R/B enters POWHEG matching via generation of radiation and via Sudakov form-factor

 $\rightarrow$  uncontrollable distortions

- Separate process in *resonances histories*
- Modified FKS mappings that retain virtualities

## The resonance-aware bb4l generator [Jezo, JML, Nason, Oleari, Pozzorini, '16]

- 
- 





### Physics features:

Resonance-aware POWHEG matching: *[Jezo, Nason, '15]*