

NNLO+PS predictions for Z boson production in association with b -jets at the LHC

Vasily Sotnikov

University of Zurich

based on

Javier Mazzitelli, VS, Marius Wiesemann [[arXiv:2404.08598](https://arxiv.org/abs/2404.08598)]

**High Precision for Hard Processes (HP2 2024),
Turin (Italy)**

10th September 2024



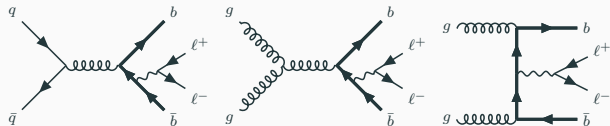
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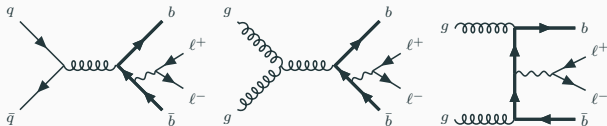
**Universität
Zürich**^{UZH}

Introduction

Motivation for $Zb\bar{b}$ production

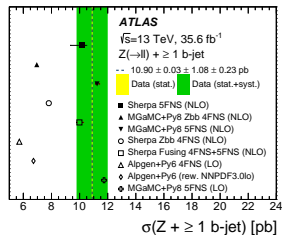


Motivation for $Zb\bar{b}$ production



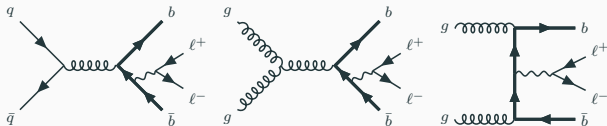
Phenomenological

- Important background to $ZH(bb)$ and BSM searches
- Precision benchmark of pQCD
- Sensitivity to heavy flavor scheme: 4FS vs 5FS



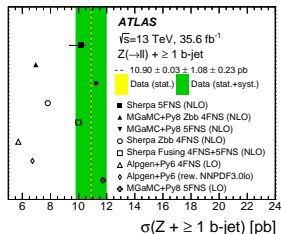
[JHEP 07 (2020) 44]

Motivation for $Zb\bar{b}$ production



Phenomenological

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Technical

- Matching NNLO QCD corrections for a genuine $2 \rightarrow 3$ QCD process to parton showers (PS) for the first time
- Extension of a NNLO+PS matching to a new class of processes
- Phenomenological application of one of the most complex two-loop amplitudes known

[JHEP 07 (2020) 44]

Theory

- NLO 5FS [Campbell, Ellis, Keith, Maltoni, Willenbrock '03]
- NLO 4FS [Febres Cordero, Reina, Wackerroth '08,'09] (see also [Campbell, Ellis, Keith '00])
- NLO+PS in MADGRAPH5_AMC@NLO [Frederix, Frixione, Hirschi, Maltoni, Pittau, Torrielli '11] (+ multi-jet merging in 5FS)
- NLO+PS in SHERPA [Krauss, Napoletano, Schumann '16] (+ multi-jet merging in 5FS)
- NLO+PS combination 4FS + 5FS [Höche, Krause, Siegert '19] (see also [Forte, Napoletano, Ubiali '18])
- NNLO in 5FS one b -jet [Gauld, Gehrmann-De Ridder, Glover, Huss, Majer '20]

This talk

First NNLO and NNLO+PS computation in 4FS

Theory

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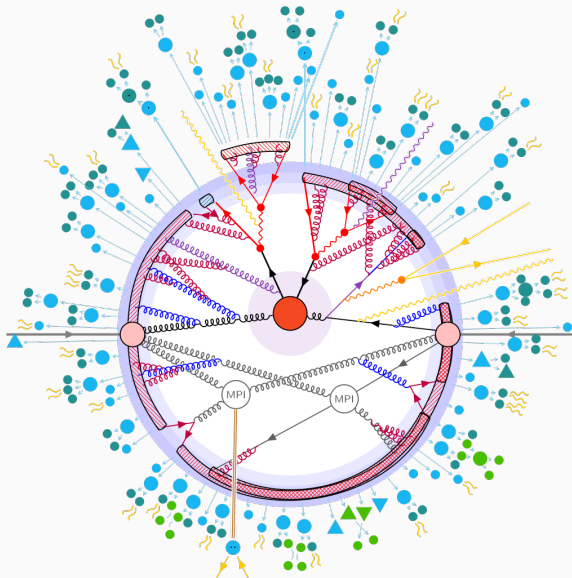
This talk

First NNLO and NNLO+PS computation in 4FS

LHC $\sqrt{s} = 13$ TeV measurements

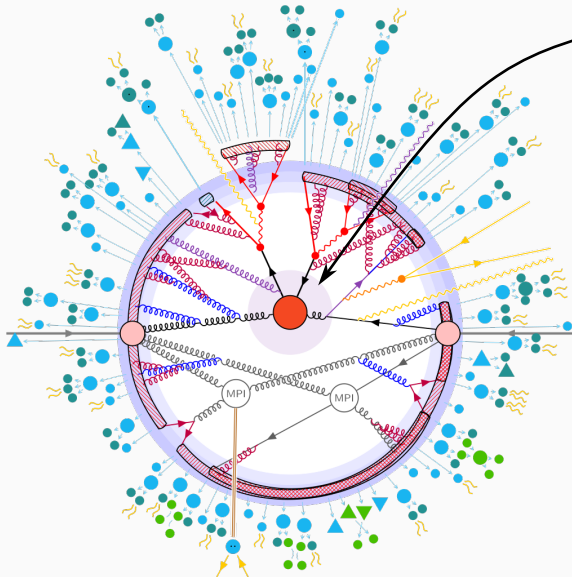
- [ATLAS, arXiv:2003.11960]
- [CMS, arXiv:2112.09659]
- [ATLAS, arXiv:2204.12355] (large R jets)
- [ATLAS, arXiv:2403.15093]

Hadron collisions



[Pythia manual]

Hadron collisions



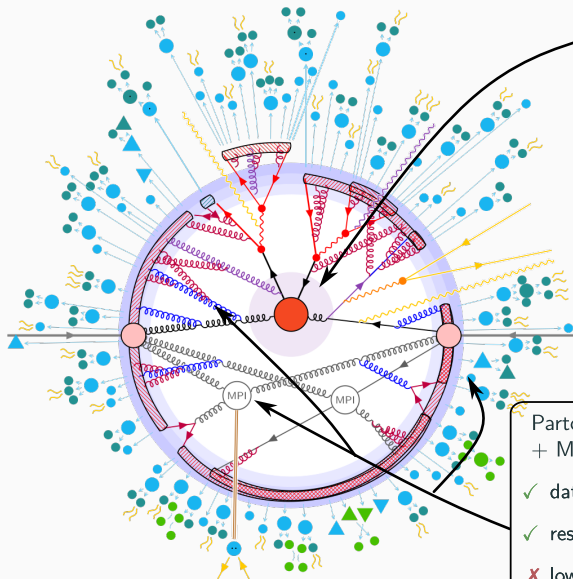
Hard interaction

✓ N^xLO precision

✗ no "events"

[Pythia manual]

Hadron collisions



Hard interaction

✓ N^{\times} LO precision

✗ no "events"

Parton shower (PS)
+ MPI, hadronization

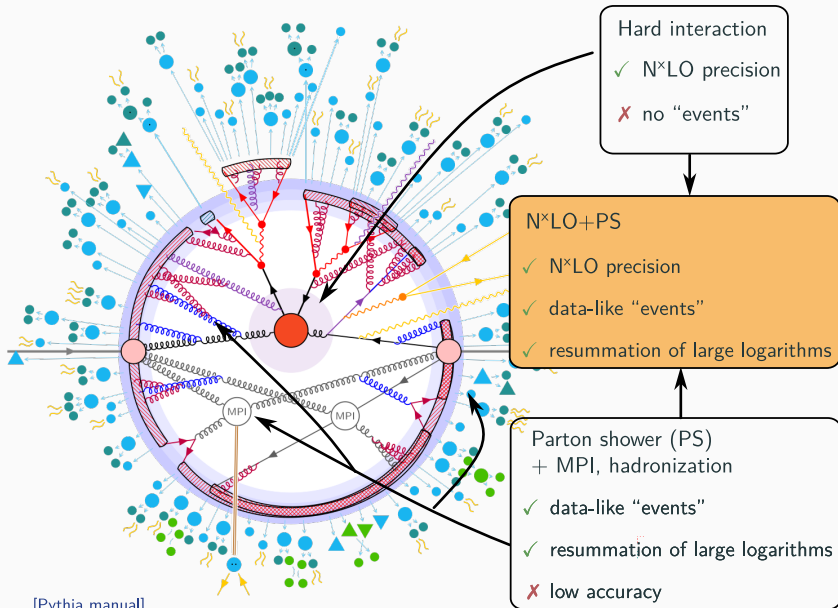
✓ data-like "events"

✓ resummation of large logarithms

✗ low accuracy

[Pythia manual]

Hadron collisions



[Pythia manual]

Computational setup

Computational setup

MiNNLO_{PS} method

MiNNLO_{PS} for color singlet production

[Monni, Nason, Re, Wiesemann, Zanderighi '19] [Monni, Re, Wiesemann '20]

Step 1: q_T resummation formula

Consider color singlet production $pp \rightarrow F + X$

$$\frac{d\sigma_F^{\text{res}}}{d\Phi_F dq_T} \sim \frac{d}{dq_T} \left\{ e^{-S} H(C \otimes f)(C \otimes f) \right\}$$

- Differential in Born phase space Φ_F and q_T
- N³LL resummation is NNLO accurate upon integration over q_T

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Step 2: match to Fj @ NLO

$$d\sigma = d\sigma_F^{\text{res}} + [d\sigma_{Fj}]_{\text{f.o.}} - [d\sigma_F^{\text{res}}]_{\text{f.o.}}$$

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Pull out Sudakov exponent, expand to α_s^3 :

$$d\sigma^{\text{MiNNLO}} \sim e^{-S} \left(d\sigma_{Fj}^{(1)} (1 + S^{(1)}) + d\sigma_{Fj}^{(2)} + D^{(3)} \right)$$

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(F and Fj NLO "merged")

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Note: e^{-S} exponentially suppresses $q_T \rightarrow 0 \implies$ NNLO subtraction

MiNNLO_{PS} for color singlet production

[Monni, Nason, Re, Wiesemann, Zanderighi '19] [Monni, Re, Wiesemann '20]

Step 3: upgrade POWHEG Fj @ NLO generator

$$d\sigma_{Fj}^{\text{pwg}} = d\Phi_{Fj} \tilde{B}^{Fj} \times \left\{ \Delta_{\text{pwg}}(p_T^{\text{min}}) + d\Phi_{\text{rad}} \Delta_{\text{pwg}}(p_{T,\text{rad}}) \frac{R_{Fj}}{B_{Fj}} \right\}$$
$$\tilde{B}_{Fj} \sim \frac{d\sigma_{Fj}^{\text{NLO}}}{d\Phi_{Fj}}$$

- Generates events in Φ_{Fj} distributed according to \tilde{B}^{Fj}
- Replace $\tilde{B}^{Fj} \rightarrow \frac{d\sigma^{\text{MiNNLO}}}{d\Phi_{Fj}}$, such that $\int dq_T \frac{d\sigma_{Fj}}{d\Phi_{Fj}}$ is NNLO accurate

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MiNNLO_{PS} accuracy

- **NNLO** for inclusive observables (differential in Φ_F)
- Resummation from parton shower (PS) preserved (e.g. LL in p_T)
- No unphysical scales

Extension to heavy quark pair (+singlet) production

$$pp \rightarrow Q\bar{Q} + F$$

Resummation structure more complex

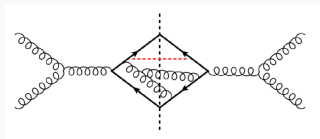
[Zhu, Li, Li, Shao, Yang '12] [Catani, Grazzini, Torre '14]

$$d\sigma_F^{\text{res}} \sim \frac{d}{dq_T} \left\{ e^{-S} H(C \otimes f)(C \otimes f) \right\} \rightarrow$$
$$d\sigma_{Q\bar{Q}}^{\text{res}} \sim \frac{d}{dq_T} \left\{ e^{-S} \left[\text{Tr}[\mathbf{H}\Delta] (C \otimes f)(C \otimes f) \right]_{\phi} \right\}$$

- Additional radiative factor Δ of soft origin [Catani, Devoto, Grazzini, Mazzitelli '23]
- Cast into a sum of color-singlet-like contributions to connect to MINNLO_{PS} formalism [Mazzitelli, Monni, Nason, Re, Wiesemann, Zanderighi '20]
- Explicit integration of (subtracted) soft current required (up to 4-fold numerical integration)

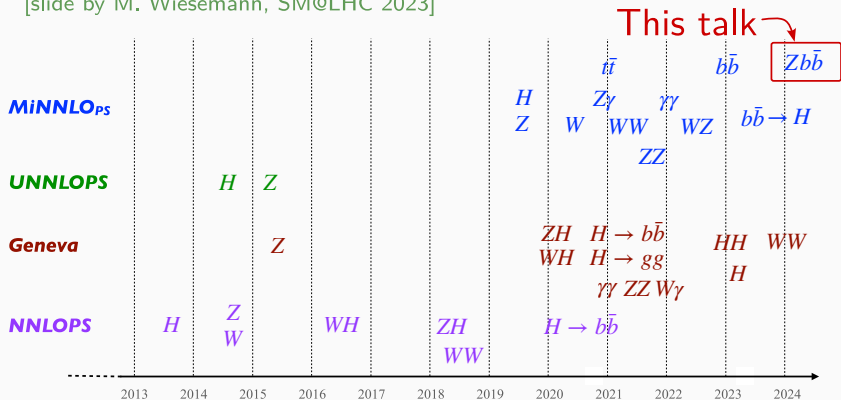
SHARK

[Devoto, Mazzitelli, in preparation]



NNLO+PS timeline

[slide by M. Wiesemann, SM@LHC 2023]



Computational setup

Two-loop corrections

Two-loop hard function

$$e^{-S} \left[\text{Tr}[\mathbf{H}\Delta] (C \otimes f)(C \otimes f) \right]_{\phi} \quad \longrightarrow \quad H = \frac{\langle \mathcal{R} | \bar{\mathbf{h}}^{\dagger} \bar{\mathbf{h}} | \mathcal{R} \rangle}{|\mathcal{M}^{(0)}|^2}, \quad |\mathcal{R}\rangle = \mathbf{Z}^{-1} |\mathcal{M}\rangle,$$
$$\bar{\mathbf{h}} = 1 + \mathcal{O}(\alpha_s)$$

- Operator $\mathbf{Z}^{-1} = 1 + \mathcal{O}(\alpha_s)$ absorbs IR divergences [Becher, Neubert '09]
- Two-loop corrections contribute to hard-virtual function H through $2 \text{Re} \langle \mathcal{R}^{(0)} | \mathcal{R}^{(2)} \rangle$
- Need five-point two-loop amplitudes for $q\bar{q} \rightarrow Zb\bar{b}$, $gg \rightarrow Zb\bar{b}$ with **massive b** , currently **out of reach** [see Bayu's talk]

Scale hierarchy $m_b \ll \mu_h \implies$ **factorization** [Mitov, Moch '06]:

$$|\mathcal{M}\rangle = \mathcal{F} |\mathcal{M}_0\rangle + \mathcal{O}\left(\frac{m_b}{\mu_h}\right), \quad \mathcal{F}^{(l)} = \sum_{i=0}^{2l} f_i \log\left(\frac{m_b}{\mu_R}\right)^i$$
$$|\mathcal{M}\rangle^{(2)} = \mathcal{F}^{(2)} |\mathcal{M}_0^{(0)}\rangle + \mathcal{F}^{(1)} |\mathcal{M}_0^{(1)}\rangle + |\mathcal{M}_0^{(2)}\rangle$$

Intuition: $1/\epsilon$ poles in 5FS scheme ($|\mathcal{M}_0\rangle$) related to $\log \frac{m_b}{\mu_R}$ power in 4FS ($|\mathcal{M}\rangle$) via “massification”.

Application to NNLO $Wb\bar{b}$ production [Buonocore, Devoto, Kallweit, Mazzitelli, Rottoli, Savoini '22]

Small m_b expansion

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Recently extended to include contributions from **closed b loops** [Wang, Xia, Yang, Ye '23]:

$$\mathcal{F} |\mathcal{M}_0\rangle \rightarrow \mathcal{F}' \mathbf{S} |\mathcal{M}_0\rangle,$$

$\mathbf{S} = 1 + \mathbf{S}^{(2)}$ soft function (operator in color space) with additional $\log \frac{m_b}{\mu_R}$ contributions.

[see Guoxing's talk]

$$|\mathcal{M}\rangle = \mathcal{F} \mathbf{S} |\mathcal{M}_0\rangle$$

$$|\mathcal{M}(\epsilon)\rangle = \mathcal{F}(\epsilon) \mathbf{S}(\epsilon) |\mathcal{M}_0(\epsilon)\rangle$$

- Factorization formulated for **divergent quantities**
- Higher orders in ϵ required in $|\mathcal{M}_0(\epsilon)\rangle$, (e.g. 1-loop to ϵ^2 for NNLO)
- Modern analytic methods compute **finite remainders** $|\mathcal{R}\rangle = \mathbf{Z}^{-1} |\mathcal{M}\rangle$ directly

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Finite formulation

Multiply by $\mathbf{Z}_{m_b \ll \mu_h}^{-1}$ and insert $1 = \mathbf{Z}_0 \mathbf{Z}_0^{-1}$:

$$|\mathcal{R}_{m_b \ll \mu_h}\rangle = \mathbf{Z}_{m_b \ll \mu_h}^{-1} \mathcal{F} \mathbf{S} \mathbf{Z}_0 |\mathcal{R}_0\rangle = \bar{\mathcal{F}} \bar{\mathbf{S}} |\mathcal{R}_0\rangle$$

$\bar{\mathcal{F}}$, $\bar{\mathbf{S}}$ **finite**, $\bar{\mathcal{F}}$ diagonal in color space

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Evaluate 2-loop contribution as

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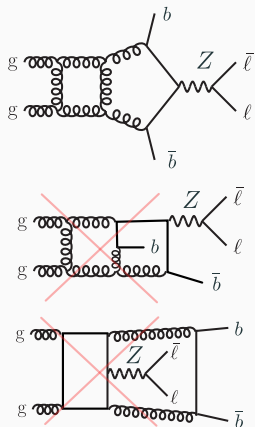
$\log(m_b)$ terms

Further approximations

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Massless two-loop $pp \rightarrow Z b \bar{b}$ process simpler, still on the cutting edge. We evaluate $\text{Re} \left\langle \mathcal{R}_0^{(0)} \left| \mathcal{R}_0^{(2)} \right. \right\rangle$ based on analytic results [Abreu, Febres Cordero, Ita, Klinkert, Page, VS '21] [Chicherin, VS, Zoia '21]

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Further approximations

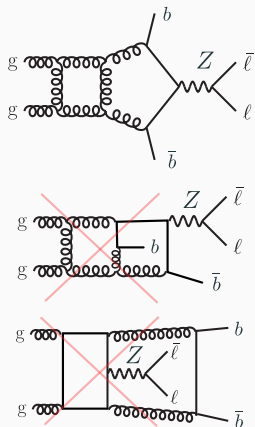
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Finite $\bar{\mathcal{F}}$ formulation \implies further approximations only in $\text{Re} \left\langle \mathcal{R}_0^{(0)} \left| \mathcal{R}_0^{(2)} \right. \right\rangle$.

No approximations in log-enhanced terms (very important!)



Computational setup

Implementation

Implementation

- Extension of MINNLO_{PS} to $Q\bar{Q} + F$ processes implemented within POWHEG-BOX-RES
- Some contributions to \mathbf{D} evaluated by **numerical integration** (requires some care!)
[Devoto, Mazzitelli, in preparation]
- PYTHIA for QCD, QED showers, MPI, hadronization
- OPENLOOPS for tree and one-loop amplitudes, including color- and spin-correlated

Massless two-loop corrections

Numerical code based on analytic results [Abreu, Febres Cordero, Ita, Klinkert, Page, VS '21], one-mass pentagon functions in PentagonFunctions++ [Chicherin, VS, Zoia '21]

- ⚠ **Challenging numerics:** huge expressions $\mathcal{O}(1\text{Gb}) \implies$ high memory usage, elaborate numerical stability checks and rescue through higher precision
- Noticeable fraction of total CPU time for two-loop contributions

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SOON: new “simplified” analytic form [de Laurentis, Ita, Page, VS, in preparation]:

17× faster, 11× less memory

Phenomenology

Inclusive cross sections

	σ_{total} [pb]	ratio to NLO
NLO+PS	$32.21(0)^{+16.4\%}_{-13.4\%}$	1.000
MI _{NLO} '	$22.33(1)^{+28.2\%}_{-17.9\%}$	0.693
MI _{NNLO} _{PS}	$50.58(4)^{+16.8\%}_{-12.2\%}$	1.588

- $\sqrt{s} = 13$ TeV,
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- $\log m_b$ -enhanced contributions from closed b loops small (larger in CMS fiducial region)

Comparison to CMS measurement

Compare to CMS $\sqrt{s} = 13$ TeV complete Run 2 data [Phys. Rev. D 105 (2022) 092014]

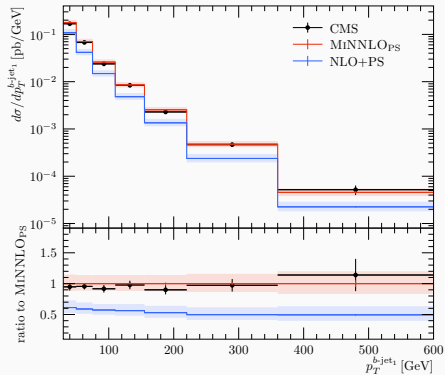
- Unfolded to fiducial region
- Backgrounds ($t\bar{t}, Z + \text{jets}$) subtracted by MC simulations

σ_{fiducial} [pb]	$Z + \geq 1$ b -jet	$Z + \geq 2$ b -jets	
NLO+PS	4.08 ± 0.66	0.44 ± 0.08	• Hadronization, MPI included
MINNLO _{PS}	6.72 ± 0.91	0.79 ± 0.10	• Apply experimental definition of b -jets (at the level of hadrons)
NLO+PS (5FS) [CMS]	7.03 ± 0.47	0.77 ± 0.07	
CMS	6.52 ± 0.43	0.65 ± 0.08	

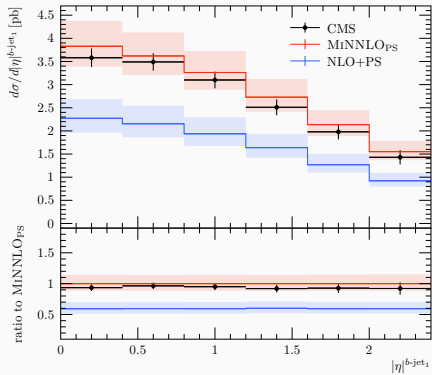
- Tension between NLO+PS(4FS) and data lifted upon inclusion of NNLO
- Excellent agreement between MINNLO_{PS} and NLO+PS(5FS)

Differential distributions: 1- b -jet

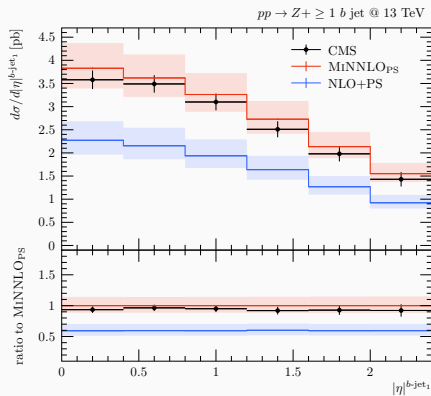
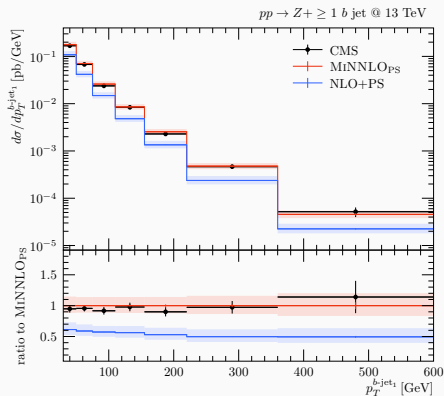
$pp \rightarrow Z + \geq 1 b \text{ jet @ 13 TeV}$



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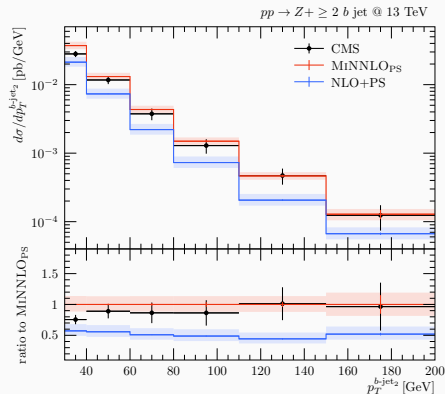
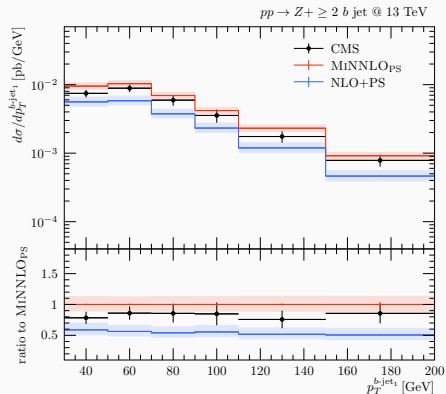


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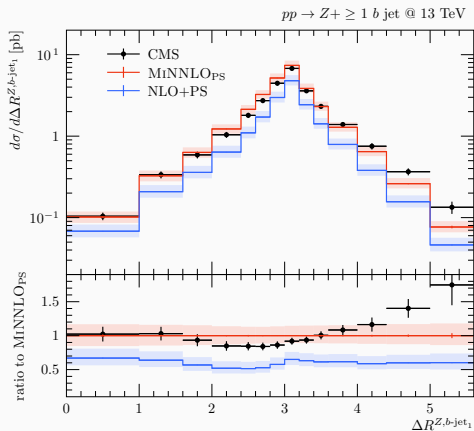
- NLO+PS fails to describe normalization
- $p_T^{b\text{-jet}_1}$ shape significantly corrected
- MiNNLO_{PS} predictions in remarkable agreement with data
- Theory uncertainty still larger than experimental in most bins

Differential distributions: 2- b -jet



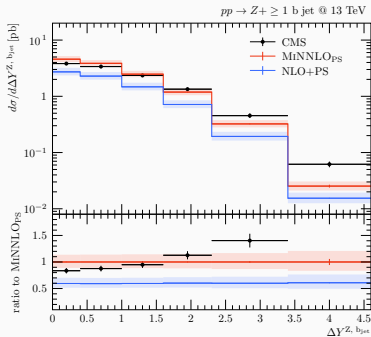
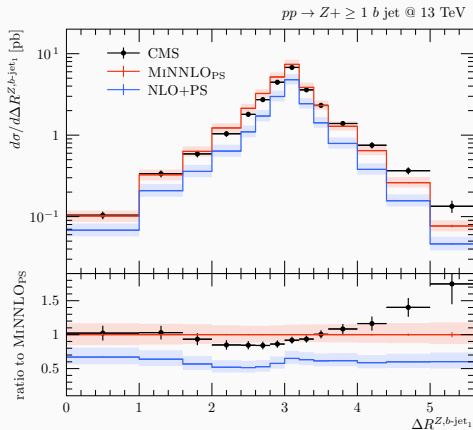
- Normalization slightly higher than data
- Still MINNLO_{PS} predictions in good agreement with data (also seen in other 2- b -jet distributions)

Angular separation between Z boson and leading b -jet



- Data not described well at high $\Delta R^{Z,b\text{-jet}}$

Angular separation between Z boson and leading b -jet



$$\Delta R = \sqrt{\Delta\phi^2 + \Delta\eta^2}$$

- Data not described well at high $\Delta R^{Z, b\text{-jet}}$
- Traced to $\Delta Y^{Z, b\text{-jet}_1}$
- Resummation of m_b logs (5FS) especially important?

Conclusions & Outlook

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- Careful study of PS and MPI effects
- Significantly improved implementation of two-loop corrections
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- Eventually public event generator

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Thank you for your attention! Stay tuned!

Acknowledgments

This work has received funding from the European Research Council (ERC) under the European Union's Horizon 2020 research and innovation programme grant agreement 101019620 (ERC Advanced Grant TOPUP).



European Research Council

Established by the European Commission

Backup

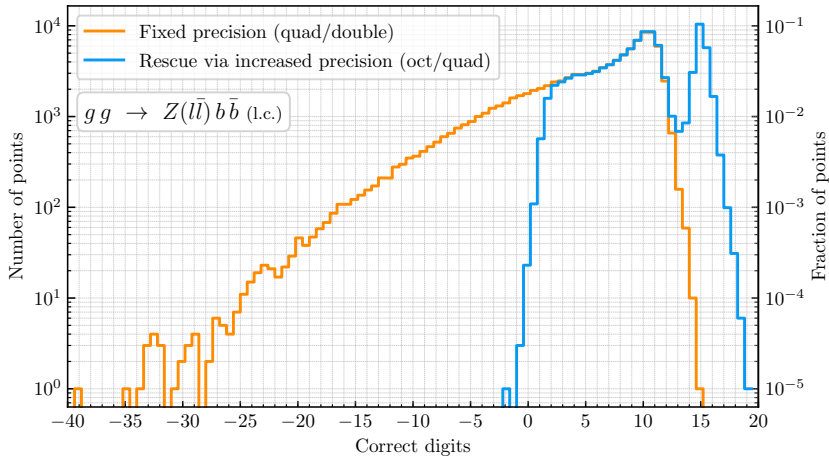
[arXiv:2112.09659]

Final state: $Z \rightarrow \ell^+ \ell^-$ (electrons or muons), and at least one (or two) b -jets.

- $71 \text{ GeV} \leq m_{\ell^+ \ell^-} \leq 111 \text{ GeV}$
- Lepton selection: $p_T^\ell > 25 \text{ GeV}$, $p_T^{\ell_1} > 35 \text{ GeV}$, $|\eta^\ell| < 2.4$
- Events with more than two leptons vetoed
- Leptons “dressed” by adding the momenta of all photons within $\Delta R^{\gamma, \ell} \leq 0.1$
- Anti- k_T b -jets with $R = 0.4$, $p_T^{b\text{-jet}} > 30 \text{ GeV}$ and $|\eta^{b\text{-jet}}| < 2.4$
- b tagged if at least one b -flavored hadron in the jet
- Overlap between leptons and b -jets vetoed: $\Delta R^{\ell, b\text{-jet}} > 0.4$

Two-loop numerical stability

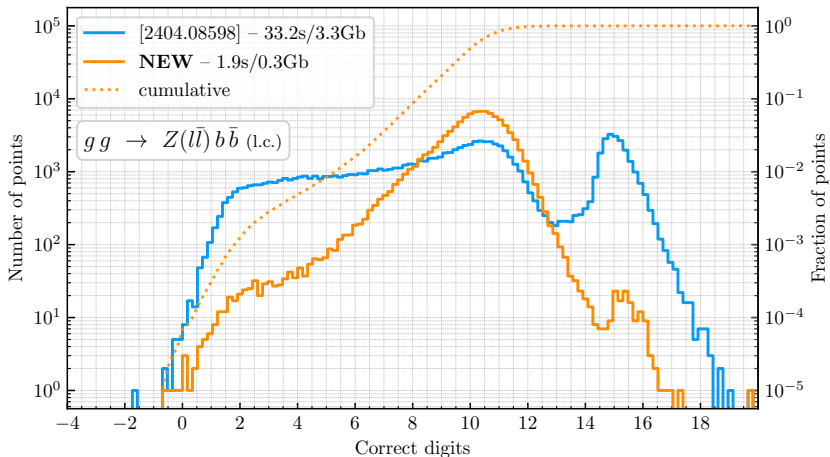
- Learn to detect unstable points **very well**, switch to higher precision dynamically.



New analytic representation

New analytic representation after **basis change** and **iterated pole subtractions**

[de Laurentis, Ita, Page, VS in preparation]



- Significantly improved stability.
- 17 times faster evaluations, 11 times less memory.