

Precise predictions for $t\bar{t}H$ production at the LHC

Chiara Savoini

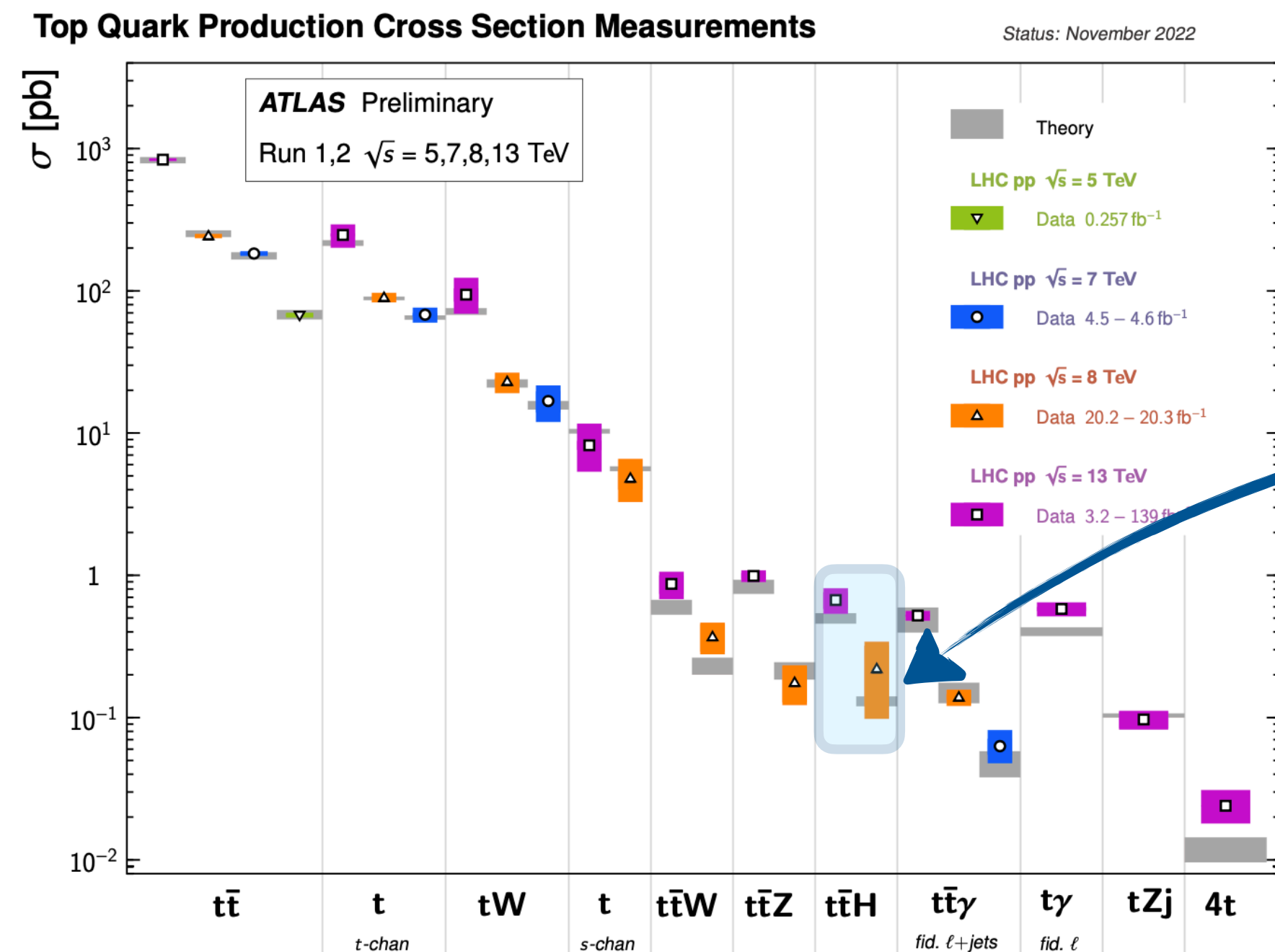
University of Zurich

based on **Phys.Rev.Lett. 130** (2023) in collaboration with
S.Catani, S.Devoto, M.Grazzini, S.Kallweit and J.Mazzitelli
+ **work in progress**

Why is $t\bar{t}H$ production interesting ?

motivations:

- ▶ the study of the Higgs boson is **one of the priorities** in the LHC experimental program, after its discovery in 2012
- ▶ the Higgs boson couplings to SM particles are proportional to their masses: **special role played by the top quark!**
- ▶ only about 1 % of the Higgs bosons are produced in association with a top-quark pair (first observation in 2018) but...
- ▶ the production mode $pp \rightarrow t\bar{t}H$ allows for a direct measurement of the **top-quark Yukawa coupling**

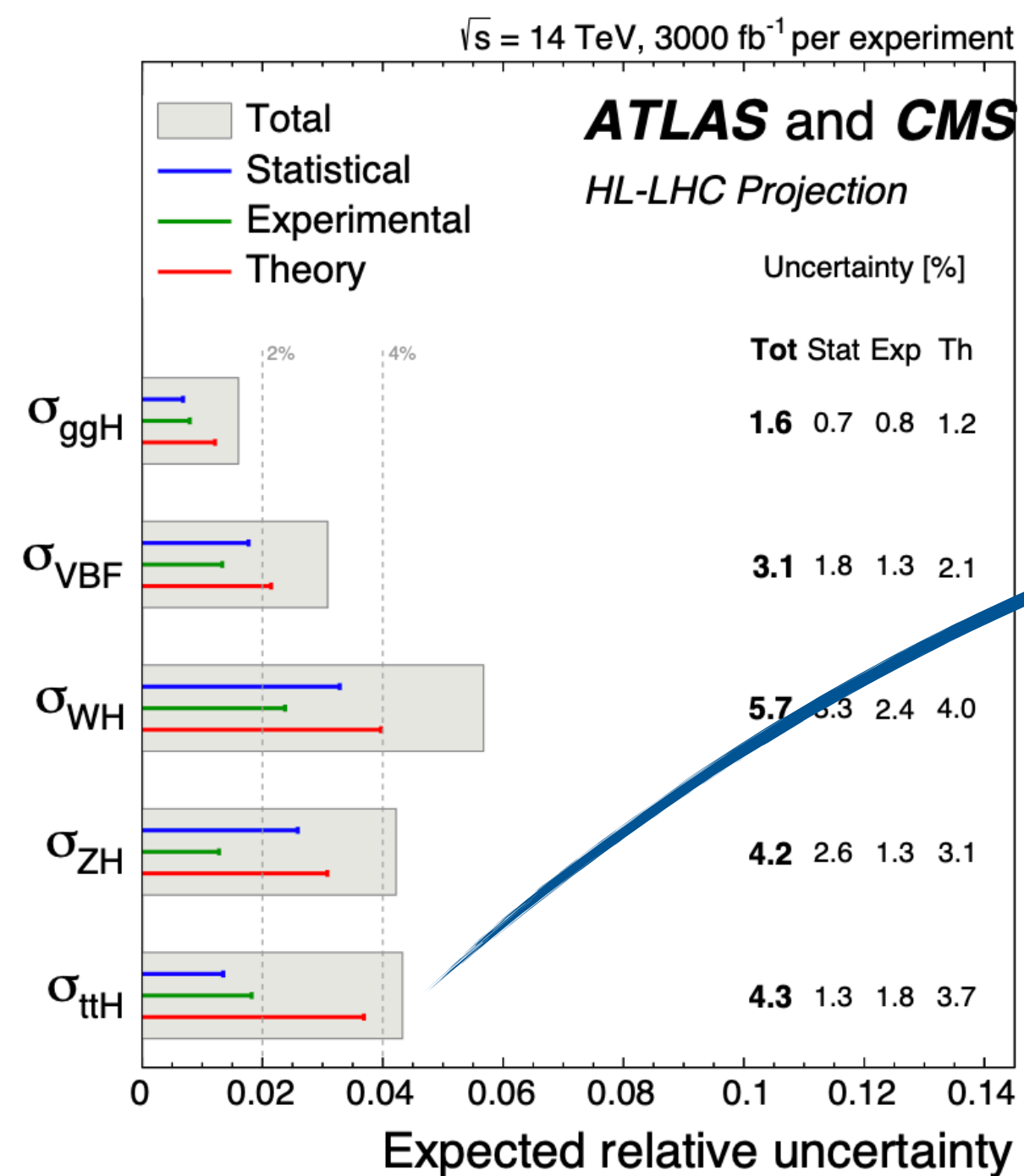


the cross section is at least *two orders of magnitude smaller* than in the case of $t\bar{t}$ production but ...
the process is *crucial* for characterising the interaction of top quarks with the Higgs sector

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[Report from WG2 (2019)]

the current experimental accuracy is $\mathcal{O}(20\%)$ but, according to the HL-LHC projections, it is expected to go down to $\mathcal{O}(2\%)$

the extraction of the $t\bar{t}H(H \rightarrow b\bar{b})$ signal is limited by the theoretical uncertainties in the **modelling of the backgrounds**, mainly $t\bar{t}b\bar{b}$ and $t\bar{t} + \text{light-flavour jets}$

moreover, **NLO QCD + EW** theory predictions equipped with NNLL soft-gluon resummation are affected by $\mathcal{O}(10\%)$ uncertainty

Theoretical predictions for $t\bar{t}H$

state of the art:

- ☑ **NLO QCD** corrections (*on-shell top quarks*) [Beenakker, Dittmaier, Krämer, Plumper, Spira, Zerwas (2001,2003)
[Reina, Dawson, Wackerath, Jackson, Orr (2001,2003)]
- ☑ **NLO EW** corrections (*on-shell top quarks*) [Frixione, Hirschi, Pagani, Shao, Zaro (2015)]
- ☑ **NLO QCD** corrections (*leptonically decaying top quarks*) [Denner, Feger (2015)] [Stremmer, Malgorzata (2022)]
- ☑ **NLO QCD + EW** corrections (*off-shell top quarks*) [Denner, Lang, Pellen, Uccirati (2017)]
- ☑ **NLO QCD + EW** corrections (*on-shell top quarks*), including **NNLL** soft-gluon resummation [Broggio et al.] [Kulesza et al.]
- ☑ **NNLO QCD** contributions for the **off-diagonal** partonic channels [Catani, Fabre, Grazzini, Kallweit (2021)]

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- ☑ **complete NNLO QCD** predictions with approximated two-loop amplitudes [Catani, Devoto, Grazzini, Kallweit, Mazzitelli, CS (2022)]

first NNLO calculation!

FOCUS OF THIS TALK!

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see Anton's talk

Two-loop amplitudes for $t\bar{t}H$ production: the quark-initiated N_f -part
Bakul Agarwal, Gudrun Heinrich, Stephen P. Jones, Matthias Kerner, Sven Yannick Klein, Jannis Lang, Vitaly Magerya, Anton Olsson

main bottleneck

One loop QCD corrections to $gg \rightarrow t\bar{t}H$ at $\mathcal{O}(\epsilon^2)$
Federico Buccioni, Philipp Alexander Kreer, Xiao Liu, Lorenzo Tancredi

Two-loop QCD amplitudes for $t\bar{t}H$ production from boosted limit
Guoxing Wang, Tianya Xia, Li Lin Yang, Xiaoping Ye

see Guoxing's talk



HOT TOPIC !!

Two-Loop Master Integrals for Leading-Color $pp \rightarrow t\bar{t}H$ Amplitudes with a Light-Quark Loop
F. Febres Cordero, G. Figueiredo, M. Kraus, B. Page, L. Reina

Theoretical predictions for $t\bar{t}H$

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viable strategy: development of physically motivated, reasonable and reliable approximations of the double-virtual contribution

see also Vasily's talk ($Zb\bar{b}$)
and Paolo's talk ($WW\gamma$)

Our subtraction framework: q_T -slicing

[Catani, Grazzini (2007)]

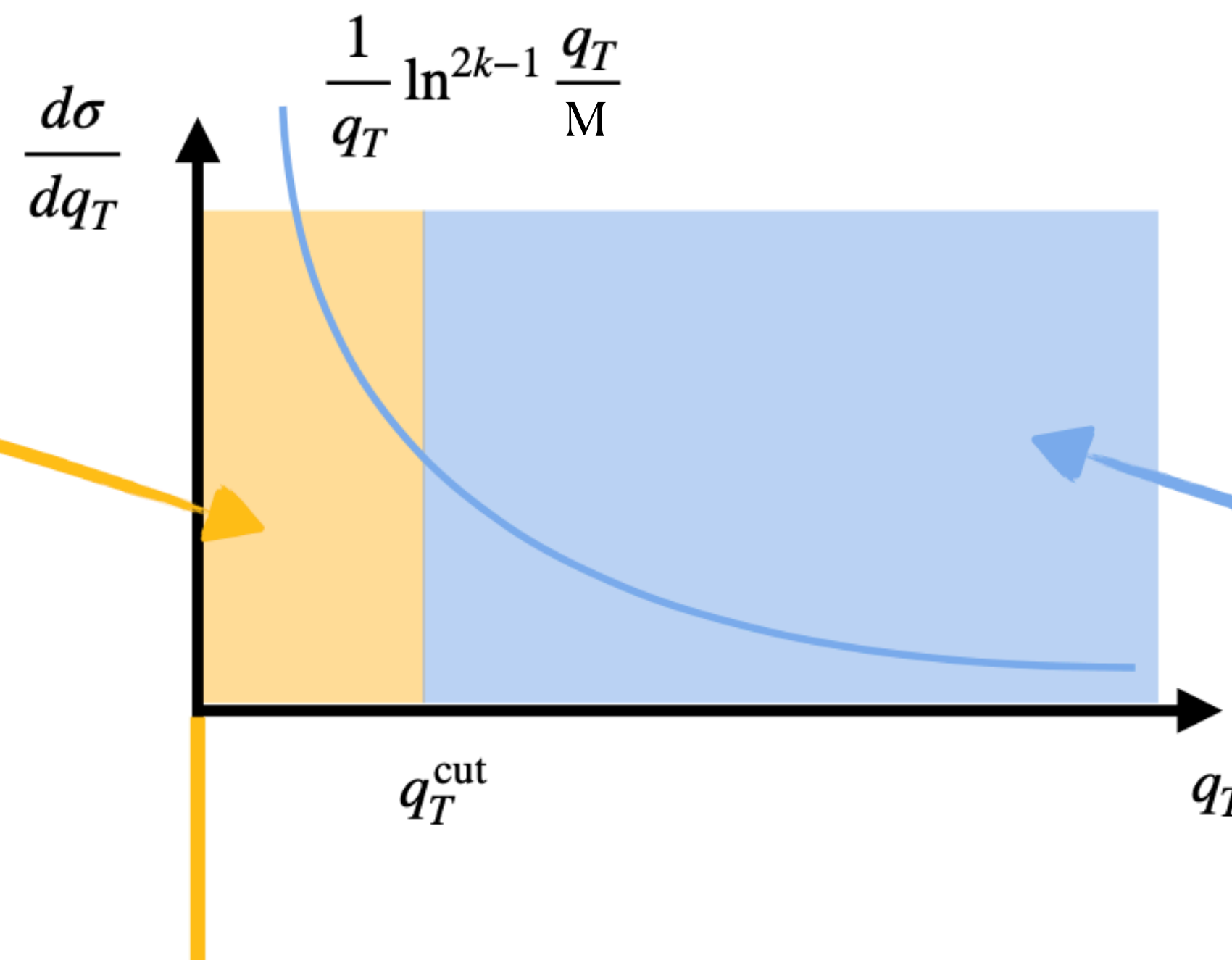
- cross section for the production of a triggered $Q\bar{Q}F$ final state at $N^k\text{LO}$

crucial to keep the mass of the heavy quark m_Q

to complete an NNLO computation: crucial to construct an NNLO subtraction/slicing scheme and have all scattering amplitudes available

$$\sigma = \int_{<q_T^{\text{cut}}} dq_T \frac{d\sigma}{dq_T} + \int_{>q_T^{\text{cut}}} dq_T \frac{d\sigma}{dq_T}$$

all emissions are unresolved
we can exploit the QCD factorisation of the matrix elements in the singular soft and/or collinear limits
ingredients from q_T - resummation



1 emission is always resolved
the complexity of the calculation is reduced by 1 order
logarithmic IR sensitivity to the cut

q_T is the transverse momentum of the $Q\bar{Q}F$ system

$$d\sigma_{N^k\text{LO}} = \mathcal{H}_{N^k\text{LO}} \otimes d\sigma_{\text{LO}} + [d\sigma_{N^{k-1}\text{LO}}^R - d\sigma_{N^k\text{LO}}^{\text{CT}}]_{q_T > q_T^{\text{cut}}} + \mathcal{O}((q_T^{\text{cut}})^p)$$

Our subtraction framework: q_T -slicing

[Catani, Grazzini (2007)]

► master formula at NNLO

$$d\sigma_{NNLO} = \mathcal{H}_{NNLO} \otimes d\sigma_{LO} + [d\sigma_{NLO}^R - d\sigma_{NNLO}^{CT}]_{q_T > q_T^{\text{cut}}} + \mathcal{O}((q_T^{\text{cut}})^p)$$

- ✓ all required **tree-level** and **one-loop** matrix elements are known and can be evaluated with **automated tools** like OpenLoops2 [Buccioni, Lang, Lindert, Maierhöfer, Pozzorini, Zhang, Zoller (2019)]
- ✓ the remaining NLO-type singularities can be removed by applying a **local subtraction** method [Catani, Seymour (1998)] [Catani, Dittmaier, Seymour, Trocsanyi (2002)]
- ✓ **automatised numerical implementation** in the MATRIX framework, which relies on the efficient multi-channel Monte Carlo integrator MUNICH [Grazzini, Kallweit, Wiesemann (2017)]

Our subtraction framework: q_T -slicing

[Catani, Grazzini (2007)]

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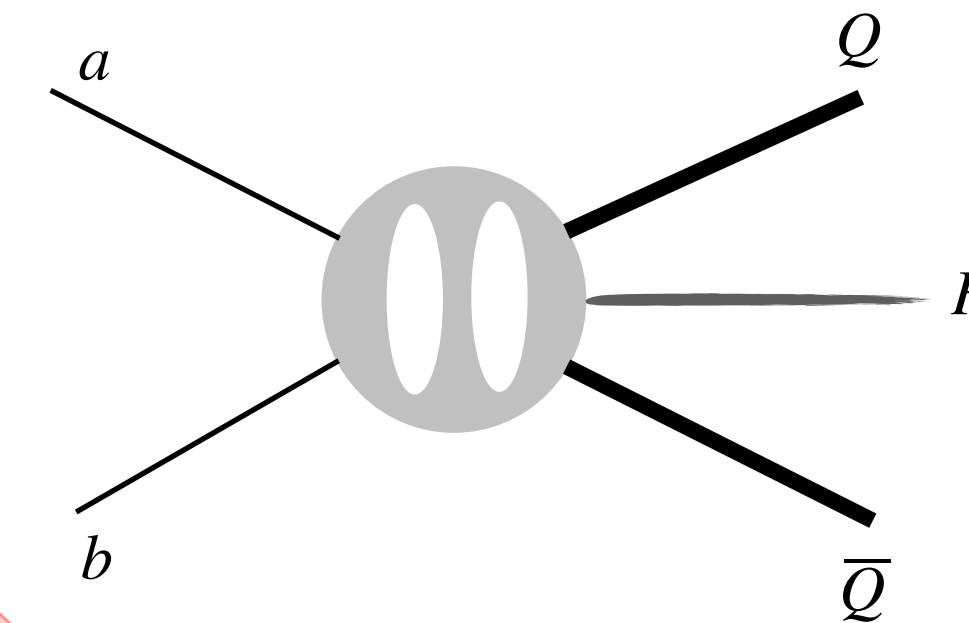
✓ the hard-collinear coefficient receives contributions also from the **two-loop virtual amplitudes**

$$\mathcal{H}_{NNLO} = H^{(2)} \delta(1 - z_1) \delta(1 - z_2) + \delta\mathcal{H}^{(2)}(z_1, z_2)$$

where $H^{(2)} = \frac{2\Re(\mathcal{M}_{fin}^{(2)}(\mu_{IR}, \mu_R) \mathcal{M}^{(0)*})}{|\mathcal{M}^{(0)}|^2} \Big|_{\mu_R = \mu_{IR} = Q}$

UV renormalised and IR subtracted amplitude at scale μ_{IR}

Q is the invariant mass of the $Q\bar{Q}F$ system



conceptual and technical challenges:

1. appearance of new mathematical functions
2. current analytic and numerical methods may not be enough
3. possible to find an amplitude representation that allows us for a numerically stable evaluation?

main bottleneck:

2 → 3 and higher multiplicity two-loop amplitudes involving heavy loops and (many) external massive legs are currently out of reach. They require major breakthroughs

[Ferrogli, Neubert, Pecjac, Yang (2009)]

Our subtraction framework: q_T -slicing

[Catani, Grazzini (2007)]

► master formula at NNLO

$$d\sigma_{NNLO} = \mathcal{H}_{NNLO} \otimes d\sigma_{LO} + [d\sigma_{NLO}^R - d\sigma_{NNLO}^{CT}]_{q_T > q_T^{\text{cut}}} + \mathcal{O}((q_T^{\text{cut}})^p)$$

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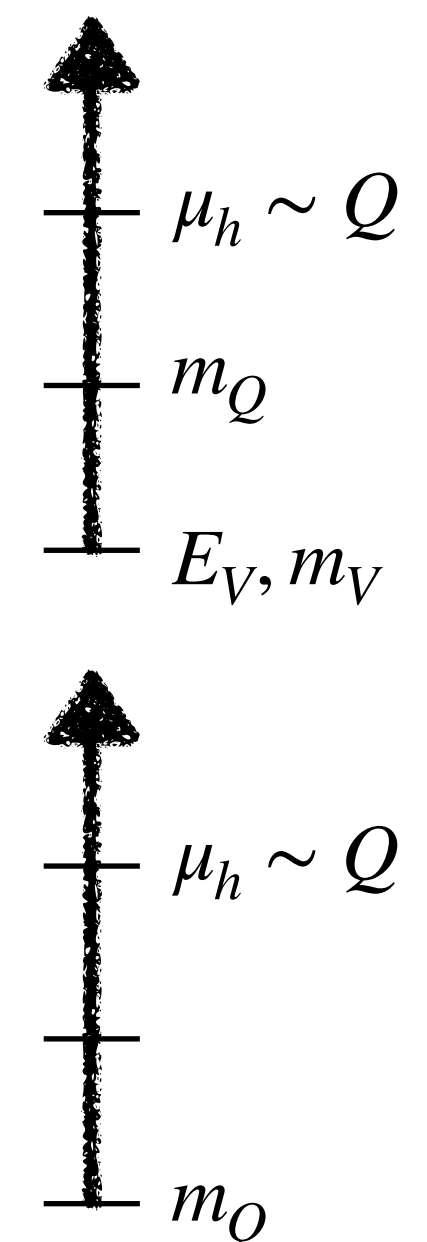
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strategy: exploit the factorisation properties of QCD matrix elements in **two** different and rather complementary **kinematic regimes**

1. soft limit for the external boson v
($E_V \rightarrow 0, m_V \rightarrow 0$)

2. high-energy limit
(ultra-relativistic quarks)
($m_Q \ll \mu_h$)



Soft Higgs-boson approximation

- ▶ We want to study the **soft Higgs-boson** limit for the amplitude associated with

$$a(k_1) + b(k_2) \rightarrow Q(p_1, m)\bar{Q}(p_2, m)\dots Q(p_{N-1}, m)\bar{Q}(p_N, m) + H(q, m_H)$$

one or more heavy-quark pairs
with the same mass

- ▶ at tree-level, it is straightforward to show that the **LP factorisation** reads

$$\lim_{q \rightarrow 0} \left(\text{Amplitude } \mathcal{A} \text{ with } Q(p_i, m) \text{ and } H(q, m_H) \right) = \boxed{\mathcal{J}^{(0)}(q)} \times \left(\text{Amplitude } \mathcal{A} \text{ with } Q(p_i, m) \right)$$

$\mathcal{J}^{(0)}(q) = \frac{m}{v} \sum_i \frac{m}{p_i \cdot q}$ scalar eikonal current

q-independent non-radiative amplitude

- ▶ at bare level, the naïve factorisation formula holds true at all orders in α_s , due to the **abelian nature** of the Higgs boson

Soft Higgs-boson approximation

- ▶ We want to study the **soft Higgs-boson** limit for the amplitude associated with

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one or more heavy-quark pairs
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- ▶ at tree-level, it is straightforward to show that the **LP factorisation** reads

$$\lim_{q \rightarrow 0} \left(\text{Amplitude } \mathcal{A} \text{ with } H(q, m_H) \text{ emission} \right) = \mathcal{J}^{(0)}(q) \times \left(\text{Amplitude } \mathcal{A} \text{ without } H \text{ emission} \right)$$

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q-independent non-radiative amplitude

- ▶ at bare level, the naïve factorisation formula holds true at all orders in α_s , due to the **abelian nature** of the Higgs boson
- ▶ ... but the renormalisation of the heavy-quark mass and wave function changes the **overall normalisation** by

up to two-loop order

soft limit of the scalar form factor for the heavy quark [Bernreuther et al. (2005)] [Blümlein et al. (2017)]

$$F(\alpha_s^{(n_l)}(\mu_R); m/\mu_R) = 1 + \frac{\alpha_s^{(n_l)}(\mu_R)}{2\pi}(-3C_F) + \left(\frac{\alpha_s^{(n_l)}(\mu_R)}{2\pi}\right)^2 \left(\frac{33}{4}C_F^2 - \frac{185}{12}C_FC_A + \frac{13}{6}C_F(n_l + n_h) - 6C_F\beta_0^{(n_l)} \ln \frac{\mu_R^2}{m^2}\right) + \mathcal{O}(\alpha_s^3)$$

Soft Higgs-boson approximation

how did we derive F ?

- ▶ To extract the explicit form of F up to three-loop order, we rely on the well-known **Higgs low-energy theorems (LETs)**
- ▶ LETs provide a connection between amplitudes of two processes which differ by the insertion of an external Higgs-boson line carrying zero momentum
- ▶ in our specific case:

[Shifman, Vainshtein, Voloshin, Zakharov (1979)]

[Kniehl, Spira (1995)]

$$\lim_{q \rightarrow 0} \mathcal{M}_{Q \rightarrow QH}^{\text{bare}}(p, q) = \frac{m_0}{v} \frac{\partial}{\partial m_0} \mathcal{M}_{Q \rightarrow Q}^{\text{bare}}(p) \Big|_{p^2=m^2}$$

$$\mathcal{M}_{Q \rightarrow Q}^{\text{bare}}(p) = \bar{Q}_0 \{ m_0(-1 + \Sigma_S(p^2, m_0)) + \not{p} \Sigma_V(p^2, m_0) \} Q_0$$

unrenormalised heavy-quark self-energy

[Broadhurst, Grafe, Gray, Schilcher (1990)]

[Broadhurst, Gray, Schilcher (1991)]

- ▶ next steps:

- renormalisation of the quark mass and wave function $m_0 \bar{Q}_0 Q_0 = m \bar{Q} Q Z_m Z_2$

- $\overline{\text{MS}}$ renormalisation of the strong coupling $\frac{g_s^2}{4\pi} = \left(\frac{e^{\gamma_E} \mu_R^2}{4\pi} \right)^\epsilon \alpha_s^{(n_f)}(\mu_R) \left\{ 1 - \frac{\alpha_s^{(n_f)}(\mu_R)}{2\pi} \frac{\beta_0^{(n_f)}}{\epsilon} + \left(\frac{\alpha_s^{(n_f)}(\mu_R)}{2\pi} \right)^2 \left[\left(\frac{\beta_0^{(n_f)}}{\epsilon} \right)^2 - \frac{\beta_1^{(n_f)}}{2\epsilon} \right] + \mathcal{O}(\alpha_s^3) \right\}$

+ decoupling of the n_h heavy quarks of mass m

[Chetyrkin, Kniehl, Steinhauser (1997)]

The LETs can be derived by observing that:

1. the Higgs-boson interaction with a massive fermion emerges from the mass term by substituting:

$$m_0 \rightarrow m_0 \left(1 + \frac{H}{v} \right) \equiv m_0(H)$$

2. if the Higgs boson carries zero momentum, the corresponding field is constant

$$\frac{1}{\not{p} - m_0(H)} \simeq \frac{1}{\not{p} - m_0} \frac{m_0}{v} \frac{1}{\not{p} - m_0} H = \frac{m_0}{v} H \left(\frac{\partial}{\partial m_0} \frac{1}{\not{p} - m_0} \right)$$

Soft Higgs-boson approximation

- ▶ **LP master formula** in the soft Higgs limit ($q \rightarrow 0, m_H \ll m$):

$$\mathcal{M}(p_1, p_2 \dots p_N, q) \simeq F(\alpha_s(\mu_R); m/\mu_R) \frac{m}{v} \left(\sum_{i=1}^N \frac{m}{p_i \cdot q} \right) \mathcal{M}(p_1, p_2 \dots p_N)$$

all-order UV
renormalised amplitudes

- ▶ observations:

- $F(\alpha_s(\mu_R); m/\mu_R)$ is perturbatively calculable, finite and gauge-independent
- it can be derived by applying the so-called Higgs Low Energy theorems (LETs)

[Shifman, Vainshtein, Voloshin, Zakharov (1979)]
[Kniehl, Spira (1995)]

we proved the relation with the soft limit of the
scalar FF up to three-loop order
[Fael, Lange, Schönwald, Steinhauser (2022, 2023)]

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[Kniehl, Spira (1995)]
- the IR singularity structure of the scattering amplitude is left changed
- the non-radiative amplitude must be evaluated on a set of projected momenta (to preserve momentum conservation)
- for the specific case of **$t\bar{t}H$ production**, the non-radiative amplitude is known up to two-loop order

[Bärnreuther, Czakon, Fiedler (2013)]

the soft factorisation formulae could provide a powerful cross check of future exact amplitude calculations, in this specific kinematic limit

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why soft Higgs approximation



a careful assessment of the quality of
the approximation is required

Results: systematic uncertainties

setup: NNLO NNPDF31, $m_H = 125\text{GeV}$, $m_t = 173.3\text{GeV}$, $\mu_R = \mu_F = (2m_t + m_H)/2$

σ [fb]	$\sqrt{s} = 13\text{ TeV}$		$\sqrt{s} = 100\text{ TeV}$	
	gg	$q\bar{q}$	gg	$q\bar{q}$
σ_{LO}	261.58	129.47	23055	2323.7
$\Delta\sigma_{\text{NLO,H}}$	88.62	7.826	8205	217.0
$\Delta\sigma_{\text{NLO,H}} _{\text{soft}}$	61.98	7.413	5612	206.0
$\Delta\sigma_{\text{NNLO,H}} _{\text{soft}}$	-2.980(3)	2.622(0)	-239.4(4)	65.45(1)

- ▶ at **NLO**, difference of **5%** (**30%**) in $q\bar{q}$ (gg) channel
- ▶ at **NNLO**, the hard-virtual contribution is about **1%** of the LO cross section in gg and **2-3%** in $q\bar{q}$ *small!*
- ▶ **our prescription** to provide a conservative uncertainty is:
 - ☑ apply the approximation at a **different subtraction scale** (vary μ_{IR} by a factor 2 around Q); add the two-loop shift based on the exact tree-level and one-loop $t\bar{t}H$ amplitudes
 - ☑ take into account the NLO discrepancy and multiply it by a **tolerance factor 3**
 - ☑ combine **linearly** the gg and $q\bar{q}$ channels

Results: systematic uncertainties

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FINAL UNCERTAINTY:

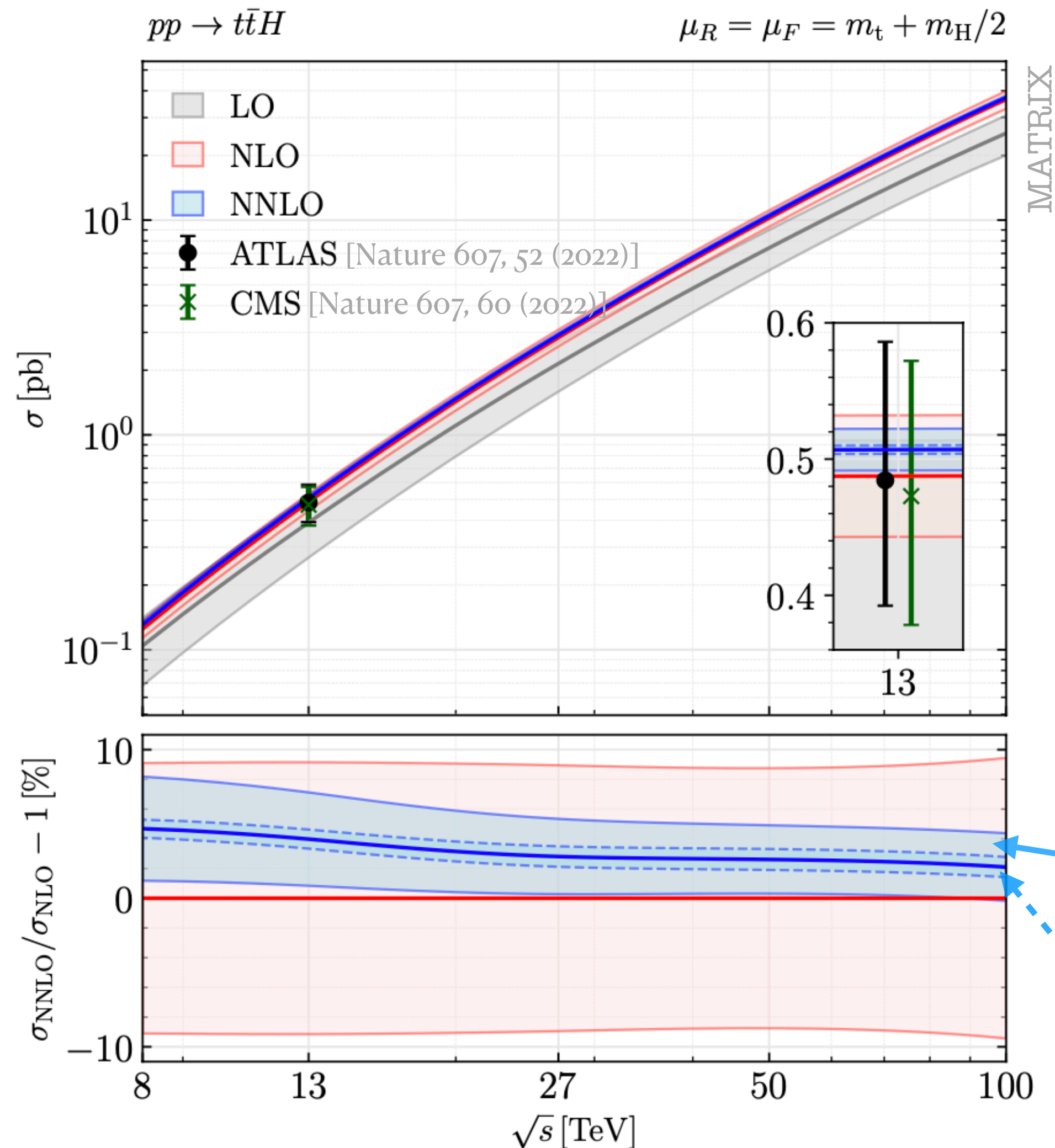
$\pm 0.6\%$ on σ_{NNLO} , $\pm 15\%$ on $\Delta\sigma_{\text{NNLO}}$

it is clear that the quality of the final result depends on the size of the contribution we are approximating

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Results: total cross section

setup: NNLO NNPDF31, $m_H = 125\text{GeV}$, $m_t = 173.3\text{GeV}$, $\mu_R = \mu_F = (2m_t + m_H)/2$



σ [pb]	$\sqrt{s} = 13 \text{ TeV}$	$\sqrt{s} = 100 \text{ TeV}$
σ_{LO}	$0.3910^{+31.3\%}_{-22.2\%}$	$25.38^{+21.1\%}_{-16.0\%}$
σ_{NLO}	$0.4875^{+5.6\%}_{-9.1\%}$	$36.43^{+9.4\%}_{-8.7\%}$
σ_{NNLO}	$0.5070 (31)^{+0.9\%}_{-3.0\%}$	$37.20(25)^{+0.1\%}_{-2.2\%}$

- ▶ at NLO: **+25 (+44)%** at $\sqrt{s} = 13 (100) \text{ TeV}$
- ▶ at NNLO: **+4 (+2)%** at $\sqrt{s} = 13 (100) \text{ TeV}$
- ▶ nice perturbative convergence with **significant reduction** of the theory uncertainties $\mathcal{O}(3\%)$

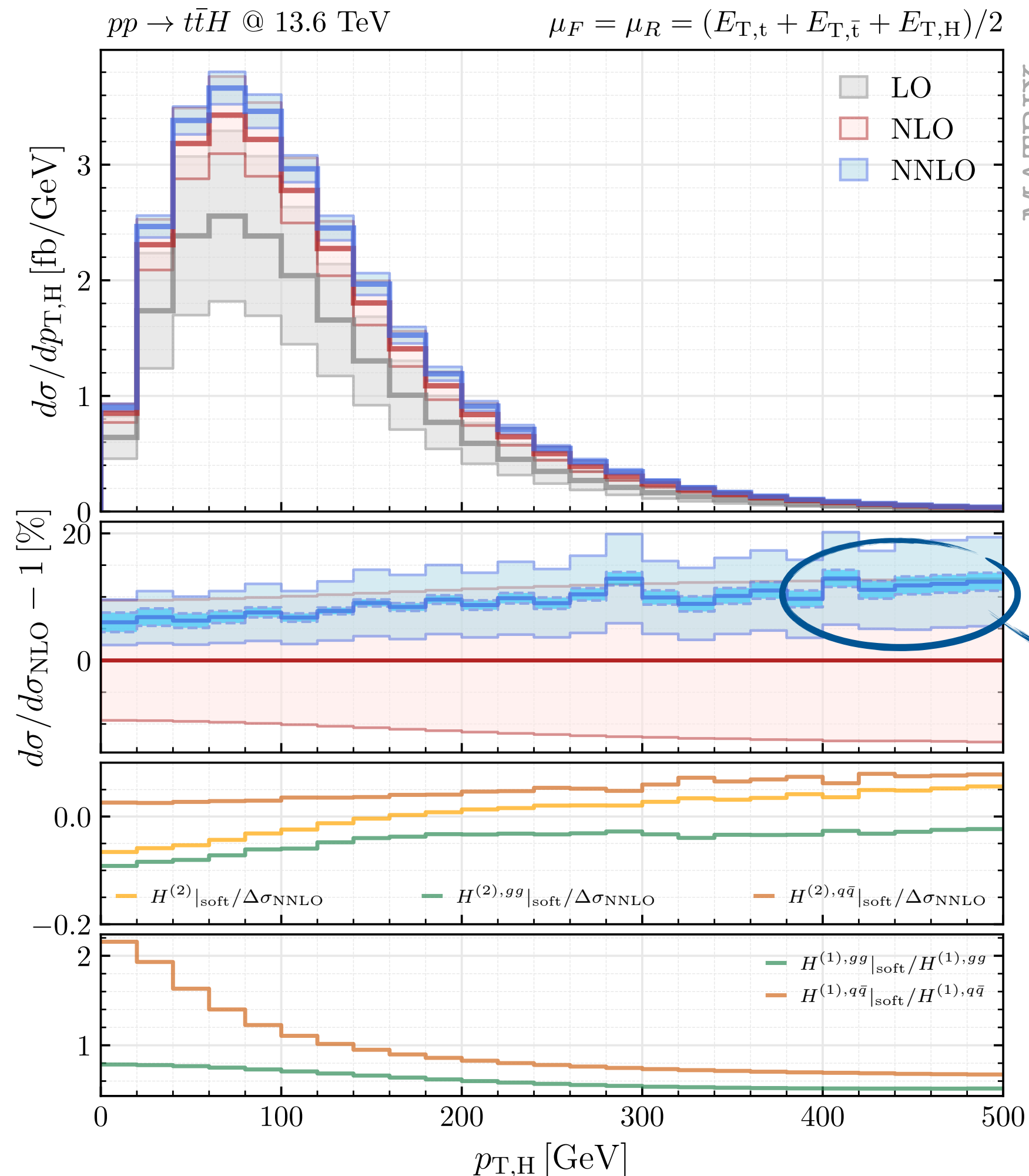
symmetrised 7-point scale variation

systematic + soft-approximation

First differential results: “soft-based”

Higgs transverse momentum

setup: NNLO NNPDF31, $m_H = 125\text{GeV}$, $m_t = 173.3\text{GeV}$, $\mu_R = \mu_F = (E_{T,t} + E_{T,\bar{t}} + E_{T,H})/2$



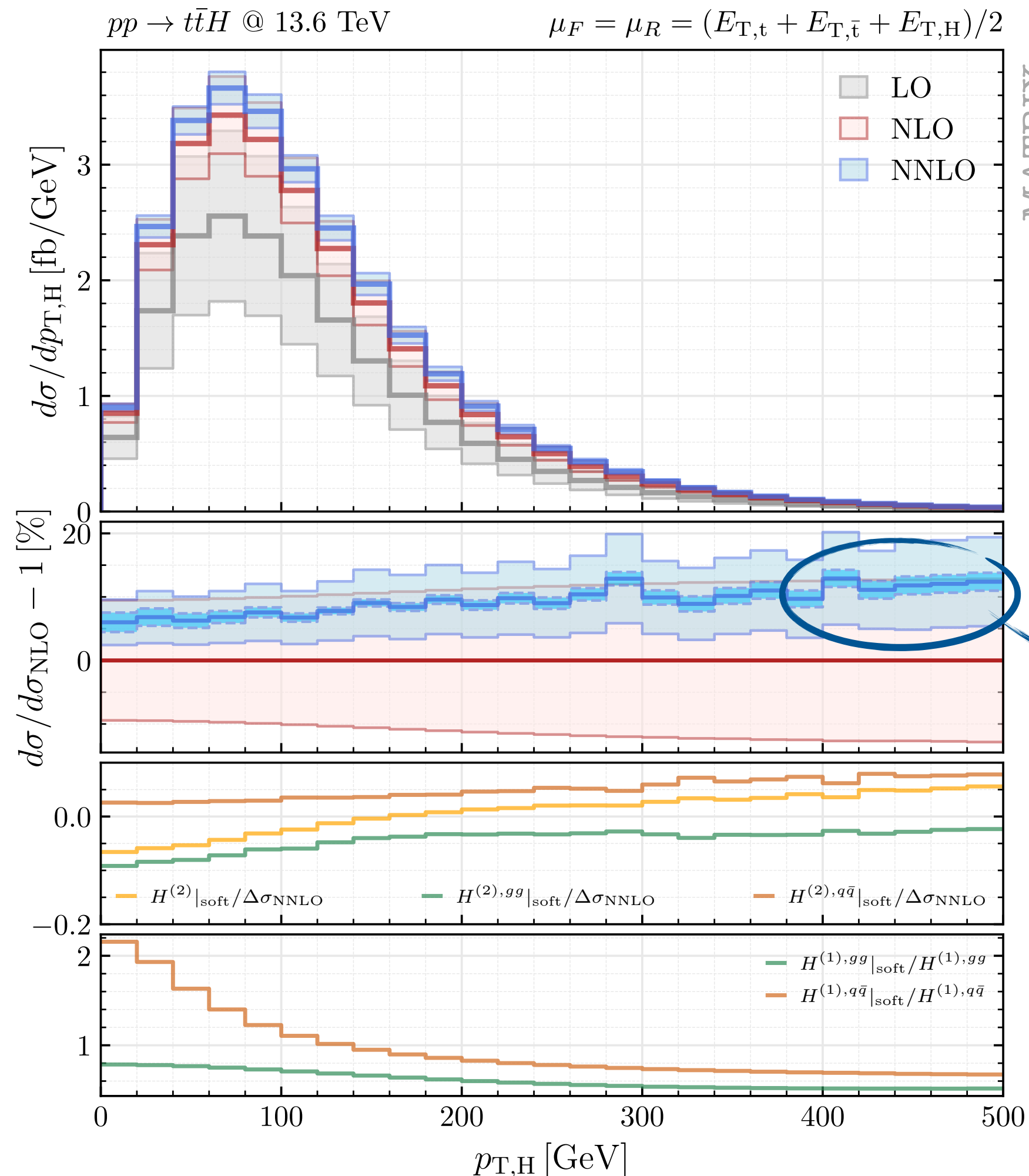
- ▶ significant reduction of the perturbative uncertainties
- ▶ soft-approximation uncertainty computed on a **bin-by-bin basis** (NLO discrepancy multiplied by a constant tolerance factor 3)
oversimplified procedure ...
- ▶ the systematic uncertainties seem to be under control, but are they trustable?

in the tail of the $p_{T,H}$ distribution, far from the region of validity of the soft-approximation, the systematic errors are “artificially” too small

First differential results: “soft-based”

Higgs transverse momentum

setup: NNLO NNPDF31, $m_H = 125\text{GeV}$, $m_t = 173.3\text{GeV}$, $\mu_R = \mu_F = (E_{T,t} + E_{T,\bar{t}} + E_{T,H})/2$



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can we refine our approximation?

our idea consists in exploiting also the **MASSIFICATION** procedure and relying on the LC two-loop massless amplitudes for $pp \rightarrow Hb\bar{b}$

[Badger et al. (2021)]

Mass factorisation or massification

[Penin (2006)]

[Moch, Mitov (2007)]

original formulation

- ▶ **idea**: reconstruct the massive amplitudes, in the ultra-relativistic quark limit $m \ll Q$, up to power corrections $\mathcal{O}(m^2/Q^2)$
- ▶ If contributions from **heavy-quark loops** are neglected, the master formula is

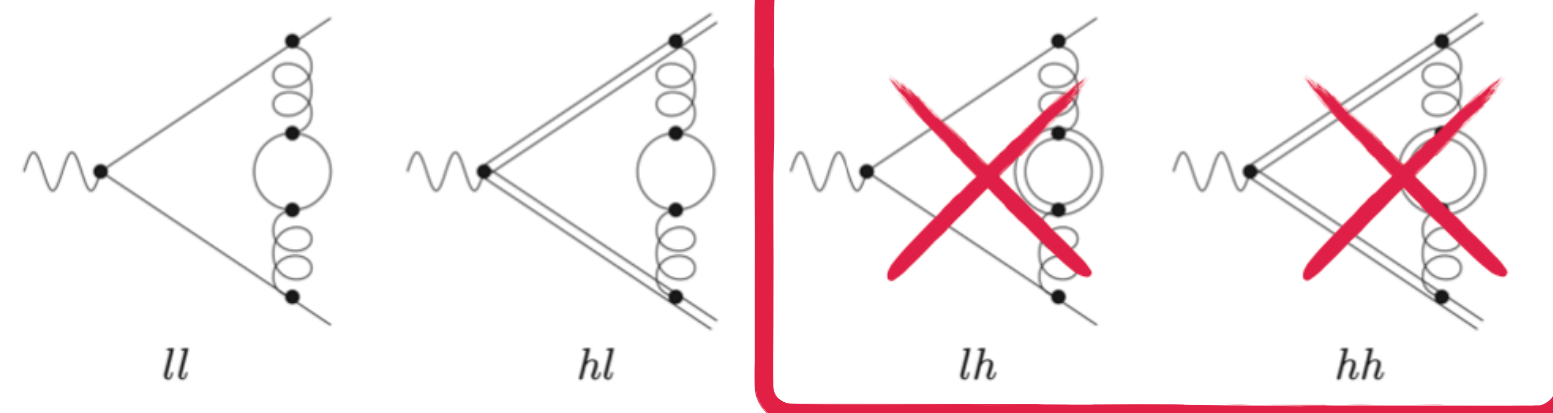
we are "dressing" n_Q external quarks with a mass m

$$|\mathcal{M}_{\mathcal{P}}^{(m)}\rangle = \left(Z_{[Q]}^{(m|0)} \left(\frac{m^2}{\mu^2}, \alpha_s(\mu^2), \epsilon \right) \right)^{n_Q/2} |\mathcal{M}_{\mathcal{P}}\rangle$$

all-order UV renormalised amplitudes in $\overline{\text{MS}}$ scheme with n_l running quarks

universal, perturbatively computable, ratio between massive and massless FFs

$$Z_{[Q]}^{(m|0)} \left(\frac{m^2}{\mu^2}, \alpha_s(\mu^2), \epsilon \right) = \mathcal{F}^{[Q\bar{Q} \rightarrow F]} \left(\frac{Q^2}{\mu^2}, \frac{m^2}{\mu^2}, \alpha_s(\mu^2), \epsilon \right) \left(\mathcal{F}_0^{[q\bar{q} \rightarrow F]} \left(\frac{Q^2}{\mu^2}, \alpha_s(\mu^2), \epsilon \right) \right)^{-1}$$



the mass "screens" collinear singularities

1. all ϵ poles, n_h -independent logarithms of the mass and finite terms of the massive amplitude are predicted

2. it can be viewed as a change in regularisation scheme

Mass factorisation or massification

generalised formulation

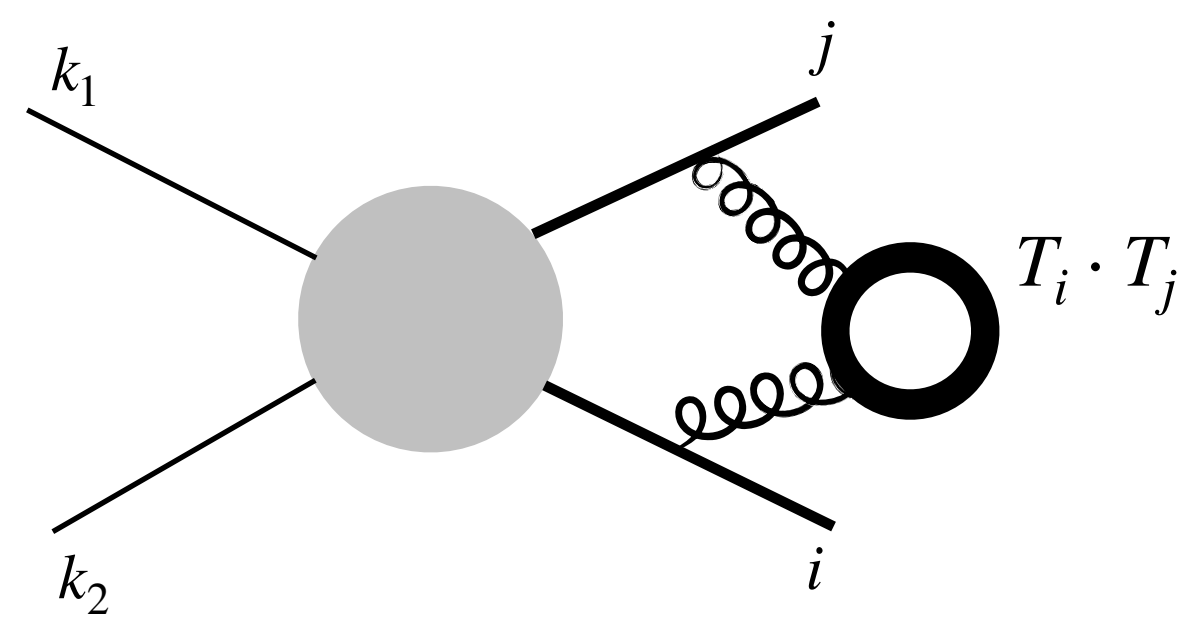
[Wang et al. (2023)]

- ▶ If contributions from **heavy-quark loops** are included, a non-trivial soft function emerges starting from α_s^2 [Becher, Melnikov (2007)]
- ▶ the master formula gets modified as [Engel et al. (2019)]

$$|\mathcal{M}_{\mathcal{P}}^{(m)}\rangle = \prod_i \left(Z_{[i]}^{(m|0)} \left(\frac{m^2}{\mu^2}, \alpha_s^{(n_f)}(\mu^2), \epsilon \right) \right)^{1/2} \mathcal{S} \left(\frac{m^2}{\mu^2}, \frac{m^2}{s_{ij}}, \alpha_s^{(n_f)}(\mu^2), \epsilon \right) |\mathcal{M}_{\mathcal{P}}\rangle$$

all-order UV renormalised amplitudes in $\overline{\text{MS}}$ scheme with $n_f = n_l + n_h$ running quarks

process-dependent **SOFT** function, operator in colour space, it starts contributing at two-loop order



$$\mathcal{S} \left(\frac{m^2}{\mu^2}, \frac{m^2}{s_{ij}}, \alpha_s^{(n_f)}(\mu^2), \epsilon \right) = 1 + \left(\frac{\alpha_s^{(n_f)}}{4\pi} \right)^2 n_h \sum_{i>j} (-\mathbf{T}_i \cdot \mathbf{T}_j) \mathcal{S}^{(2)} \left(\frac{m^2}{\mu^2}, \frac{m^2}{s_{ij}}, \epsilon \right) + \mathcal{O}(\alpha_s^3)$$

with $\mathcal{S}^{(2)} \left(\frac{m^2}{\mu^2}, \frac{m^2}{s_{ij}}, \epsilon \right) = T_R \left(\frac{\mu^2}{m^2} \right)^{2\epsilon} \left(-\frac{4}{3\epsilon^2} + \frac{20}{9\epsilon} - \frac{112}{27} - \frac{4\zeta_2}{3} \right) \log \left(\frac{-s_{ij}}{m^2} \right)$

see Guoxing's talk

Mass factorisation or massification

[Wang et al. (2023)]

generalised formulation

- ▶ If contributions from **heavy-quark loops** are included, a non-trivial soft function emerges starting from α_s^2

[Becher, Melnikov (2007)]

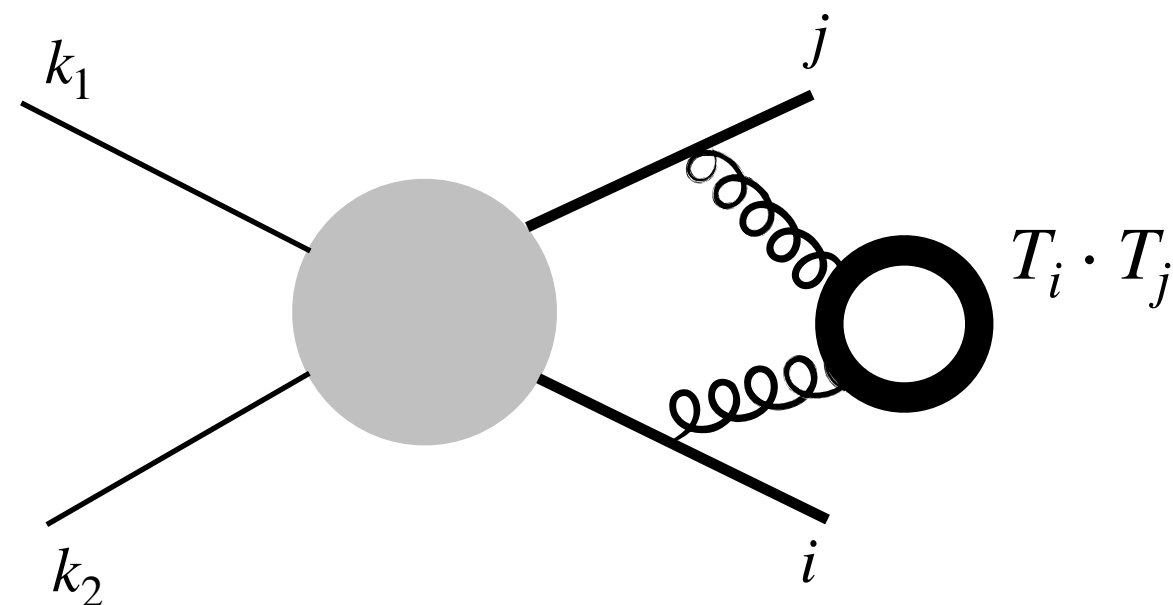
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all-order UV renormalised amplitudes
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$$\text{with } \mathcal{S}^{(2)} \left(\frac{m^2}{\mu^2}, \frac{m^2}{s_{ij}}, \epsilon \right) = T_R \left(\frac{\mu^2}{m^2} \right)^{2\epsilon} \left(-\frac{4}{3\epsilon^2} + \frac{20}{9\epsilon} - \frac{112}{27} - \frac{4\zeta_2}{3} \right) \log \left(\frac{-s_{ij}}{m^2} \right)$$

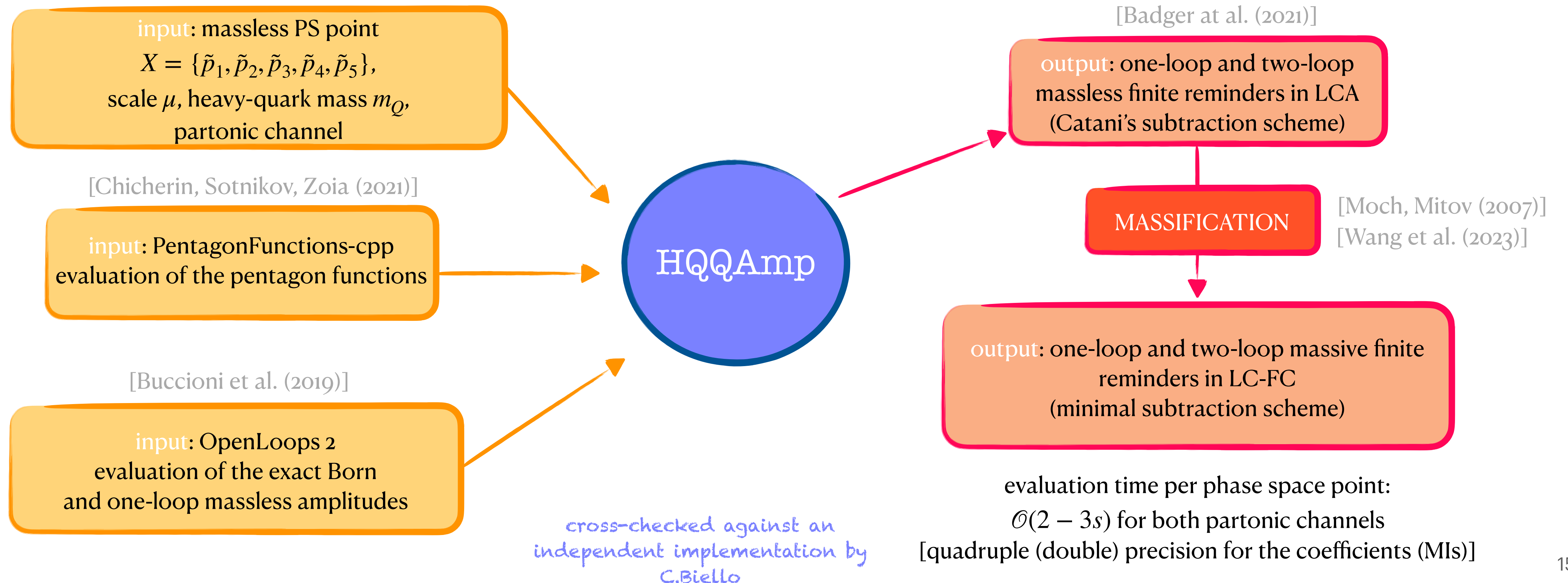
for the specific case of $Q\bar{Q}H$ production we can reconstruct the massive amplitudes, up to power corrections in the heavy-quark mass, by exploiting the corresponding (known) massless amplitudes

[Badger et al. (2021)]

HQQAmp: a massive C++ implementation

- ▶ We implemented the one-loop and two-loop massless amplitudes of [Badger et al. (2021)] in a **C++ library** for the efficient numerical evaluation of the **massified amplitudes**
- ▶ possibility of choosing the **precision** (double, quadruple or octuple) for the MIs and relative coefficients

$$q/g(p_1) + \bar{q}/g(p_2) \rightarrow H(p_3) + t(p_4) + \bar{t}(p_5)$$



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$$q/g(p_1) + \bar{q}/g(p_2) \rightarrow H(p_3) + t(p_4) + \bar{t}(p_5)$$

input: massless PS point $X = \{\tilde{p}_1, \tilde{p}_2, \tilde{p}_3, \tilde{p}_4, \tilde{p}_5\}$,
scale μ , heavy-quark mass m_Q ,
partonic channel

- **mapping 2**: preserve the energy and longitudinal component of the 4-momenta of the heavy quarks

$$\tilde{p}_4^\mu = (E_4, \hat{p}_{4,T} \sqrt{p_{4,T}^2 + m^2}, p_{4,z}),$$

$$\tilde{p}_5^\mu = (E_5, \hat{p}_{5,T} \sqrt{p_{5,T}^2 + m^2}, p_{5,z})$$

prevents potential IS collinear divergences in gg channel
(t-channel diagrams)

- **mapping 0**: preserve the 4-momentum of the heavy-quark pair $s_{QQ} = (p_4 + p_5)^2 = (\tilde{p}_4 + \tilde{p}_5)^2$

$$\begin{aligned} \tilde{p}_4^\mu &= \beta_+ p_4^\mu - \beta_- p_5^\mu, \\ \tilde{p}_5^\mu &= \beta_+ p_5^\mu - \beta_- p_4^\mu \end{aligned} \quad \text{with } \beta_\pm = \frac{1 \pm \beta}{2\beta}, \beta = \sqrt{1 - \frac{4m^2}{s_{QQ}}}$$

prevents potential collinear divergences due to $g \rightarrow b\bar{b}$

- **mapping 1**: preserve the 3-momenta of the heavy quarks and the 4-momentum of the Higgs boson

$$\tilde{p}_1^\mu = \tilde{E}_1(1, 0, 0, 1), \quad \tilde{p}_2^\mu = \tilde{E}_2(1, 0, 0, -1),$$

$$\tilde{p}_3^\mu = p_3^\mu,$$

$$\tilde{p}_4^\mu = (\sqrt{p_{4,T}^2 + p_{4,z}^2}, \vec{p}_{4,T}, p_{4,z}),$$

$$\tilde{p}_5^\mu = (\sqrt{p_{5,T}^2 + p_{5,z}^2}, \vec{p}_{5,T}, p_{5,z})$$

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$$|\mathcal{M}_m^{(\text{fin,SCET})}\rangle = \mathbf{Z}_{m \ll \mu_h}^{-1}(\alpha_s^{(n_l)}, \mu^2, m^2; \epsilon) Z_{[Q]}^{(m|0)}\left(\alpha_s^{(n_l)}, \frac{\mu^2}{m^2}; \epsilon\right) \mathbf{Z}_{(m=0)}(\alpha_s^{(n_l)}, \mu^2; \epsilon) |\mathcal{M}_{(m=0)}^{(\text{fin,SCET})}\rangle + \mathcal{O}\left(\frac{m^2}{\mu_h^2}\right)$$

$$|\mathcal{M}_m^{(\text{fin,SCET})}\rangle = \mathcal{F}\left(\alpha_s^{(n_l)}, \frac{\mu^2}{m^2}\right) |\mathcal{M}_{(m=0)}^{(\text{fin,SCET})}\rangle$$

with

$$\mathcal{F}\left(\alpha_s^{(n_l)}, \frac{\mu^2}{m^2}\right) = 1 + \frac{\alpha_s^{(n_l)}}{4\pi} \mathcal{F}^{(1)}\left(\frac{\mu^2}{m^2}\right) + \left(\frac{\alpha_s^{(n_l)}}{4\pi}\right)^2 \mathcal{F}^{(2)}\left(\frac{\mu^2}{m^2}\right) + \mathcal{O}(\alpha_s^3)$$

it is not anymore an operator in colour space and it contains all mass logarithms!

$$\mathcal{F}^{(1)} = Z_{[Q]}^{(1),\epsilon^0}$$

$$\mathcal{F}^{(2)} = Z_{[Q]}^{(2),\epsilon^0} - Z_{[Q]}^{(1),1/\epsilon} Z_{[Q]}^{(1),\epsilon} - Z_{[Q]}^{(1),1/\epsilon^2} Z_{[Q]}^{(1),\epsilon^2}$$

process-independent!

[Badger et al. (2021)]

output: one-loop and two-loop massless finite reminders in LCA (Catani's subtraction scheme)

MASSIFICATION

[Moch, Mitov (2007)]

output: one-loop and two-loop massive finite reminders in LC-FC (minimal subtraction scheme)

Yukawa renormalised ON-SHELL

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$$|\mathcal{M}_m^{(\text{fin}, \text{SCET})}\rangle = \mathbf{Z}_{m \ll \mu_h}^{-1}(\alpha_s^{(n_l)}, \mu^2, m^2; \epsilon) Z_{[Q]}^{(m|0)}\left(\alpha_s^{(n_l)}, \frac{\mu^2}{m^2}; \epsilon\right) \mathbf{Z}_{(m=0)}(\alpha_s^{(n_l)}, \mu^2; \epsilon) |\mathcal{M}_{(m=0)}^{(\text{fin}, \text{SCET})}\rangle + \mathcal{O}\left(\frac{m^2}{\mu_h^2}\right)$$

$$|\mathcal{M}_m^{(\text{fin}, \text{SCET})}\rangle = \mathcal{F}\left(\alpha_s^{(n_l)}, \frac{\mu^2}{m^2}\right) |\mathcal{M}_{(m=0)}^{(\text{fin}, \text{SCET})}\rangle$$

$$\begin{aligned} |\mathcal{M}_m^{(1), (\text{fin}, \text{SCET})}\rangle &= |\mathcal{M}_{(m=0)}^{(1), (\text{fin}, \text{SCET})}\rangle + \mathcal{F}^{(1)} |\mathcal{M}_{(m=0)}^{(0)}\rangle \\ |\mathcal{M}_m^{(2), (\text{fin}, \text{SCET})}\rangle &= |\mathcal{M}_{(m=0)}^{(2), (\text{fin}, \text{SCET})}\rangle + \mathcal{F}^{(1)} |\mathcal{M}_{(m=0)}^{(1), (\text{fin}, \text{SCET})}\rangle + \mathcal{F}^{(2)} |\mathcal{M}_{(m=0)}^{(0)}\rangle \end{aligned}$$

massless two-loop contribution in LCA. All remaining terms can be “promoted” to FC

no need to implement the higher ϵ orders of the massless one-loop amplitude

[Badger et al. (2021)]

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[Badger et al. (2021)]

output: one-loop and two-loop massless
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(Catani's subtraction scheme)

[Wang et al. (2023)]

MASSIFICATION

output: one-loop and two-loop massive
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Yukawa renormalised ON-SHELL

$$|\mathcal{M}_m^{(\text{fin}, \text{SCET})}\rangle = \mathcal{F}_{[c]}\left(\alpha_s^{(n_f)}, \frac{\mu^2}{m^2}, \frac{\mu^2}{s_{ij}}\right) |\mathcal{M}_{(m=0)}^{(\text{fin}, \text{SCET})}\rangle$$

with

$$\mathcal{F}_{[c]}^{(1)} = \mathcal{F}^{(1)} + \mathcal{F}_{[c]}^{(1)}$$

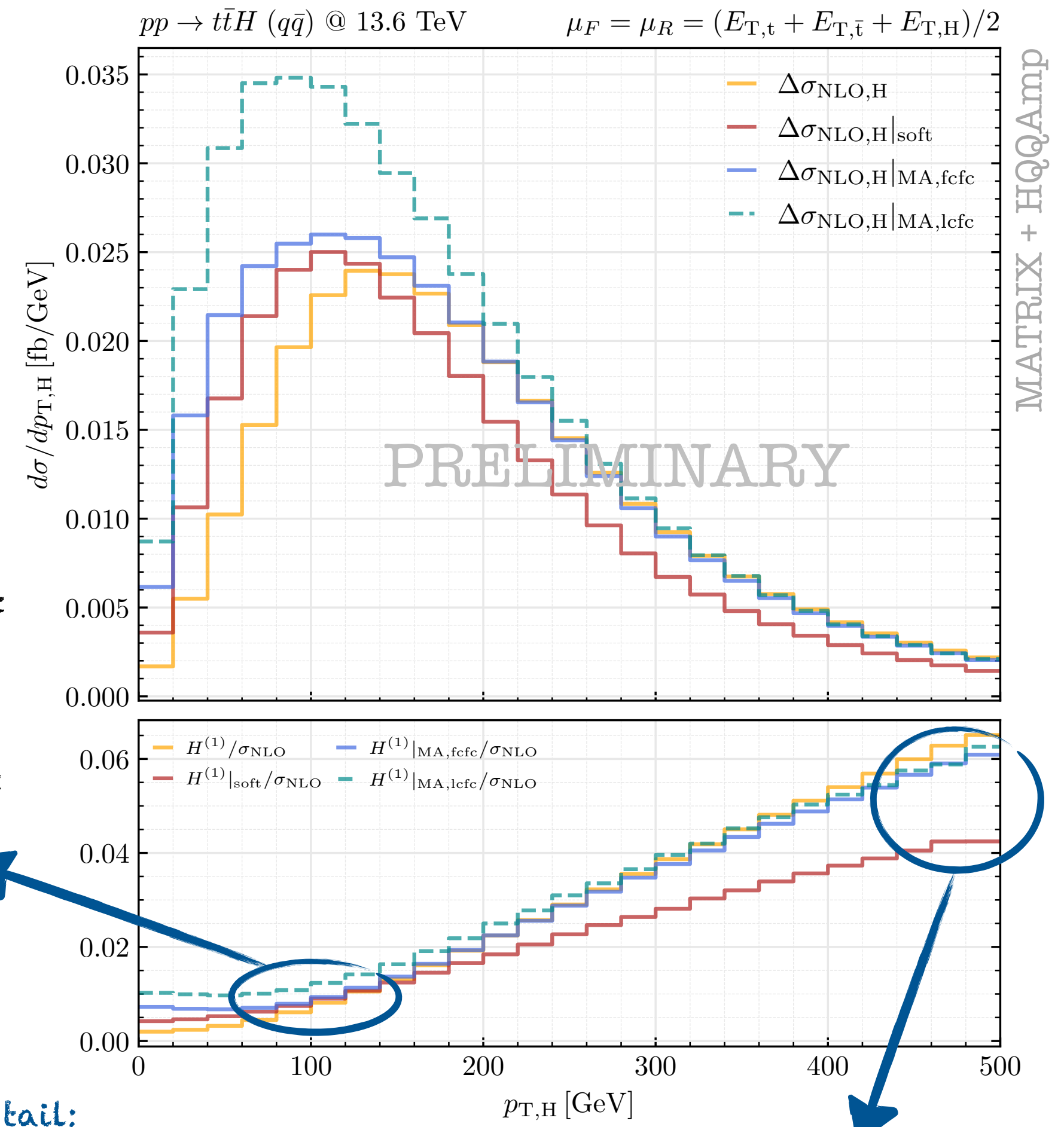
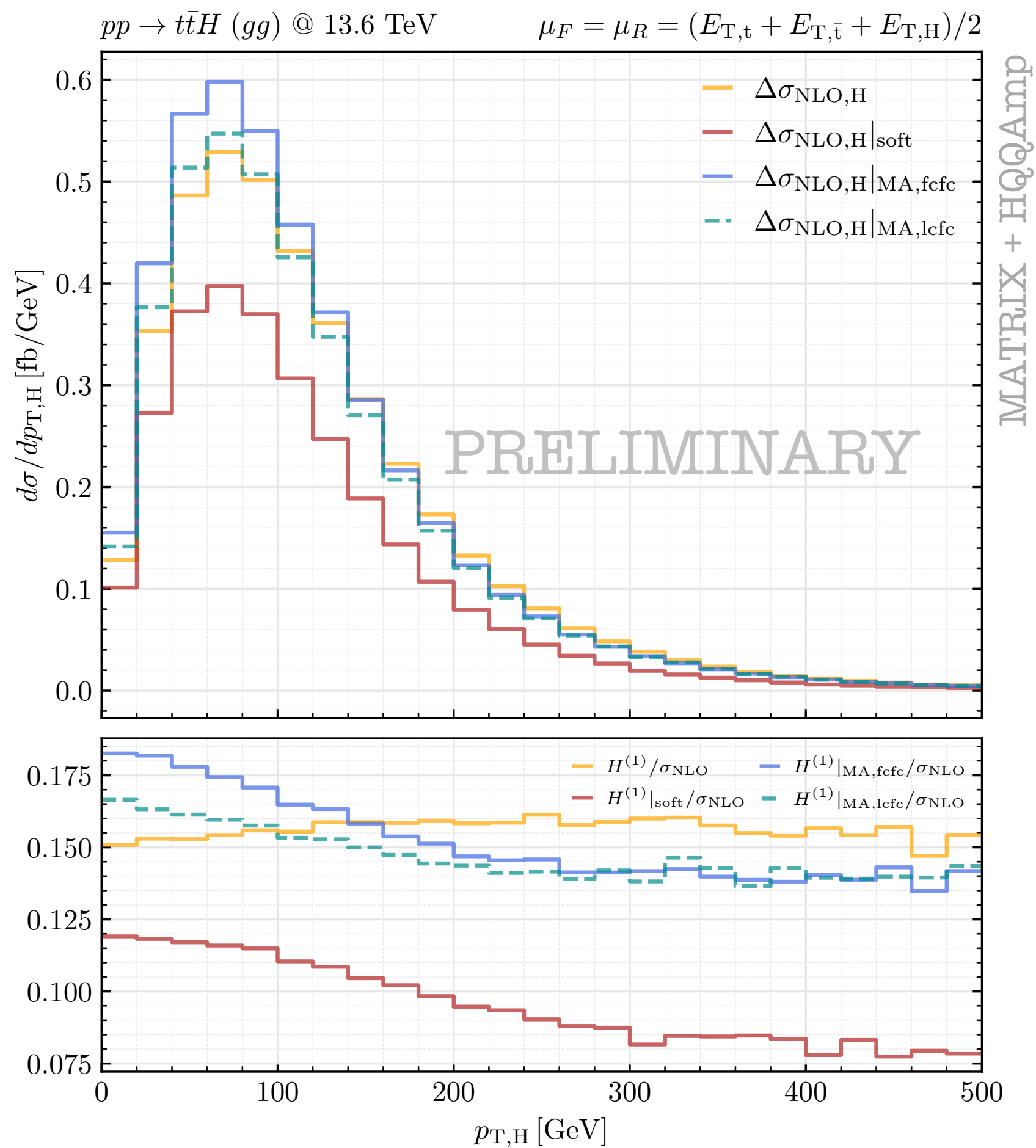
$$\mathcal{F}_{[c]}^{(2)} = \mathcal{F}^{(2)} + \mathcal{S}^{(2), \epsilon^0} + \mathcal{F}_{[c]}^{(2)}$$

$$+ n_h \left(\frac{\pi^2}{18} + \frac{1}{3} l_{\mu m}^2 \right) \mathbf{Z}_{m \ll \mu_h}^{(1), 1/\epsilon} + n_h \left(-\frac{2}{9} \zeta_3 + \frac{\pi^2}{18} l_{\mu m} + \frac{1}{9} l_{\mu m}^3 \right) \mathbf{Z}_{m \ll \mu_h}^{(1), 1/\epsilon^2}$$

it is now an operator in colour space, depending on the partonic channel $c \in \{g, q\}$

Quality of both approximations at NLO

setup: NNLO NNPDF31, $m_H = 125\text{GeV}$, $m_t = 173.3\text{GeV}$, $\mu_R = \mu_F = (E_{T,t} + E_{T,\bar{t}} + E_{T,H})/2$



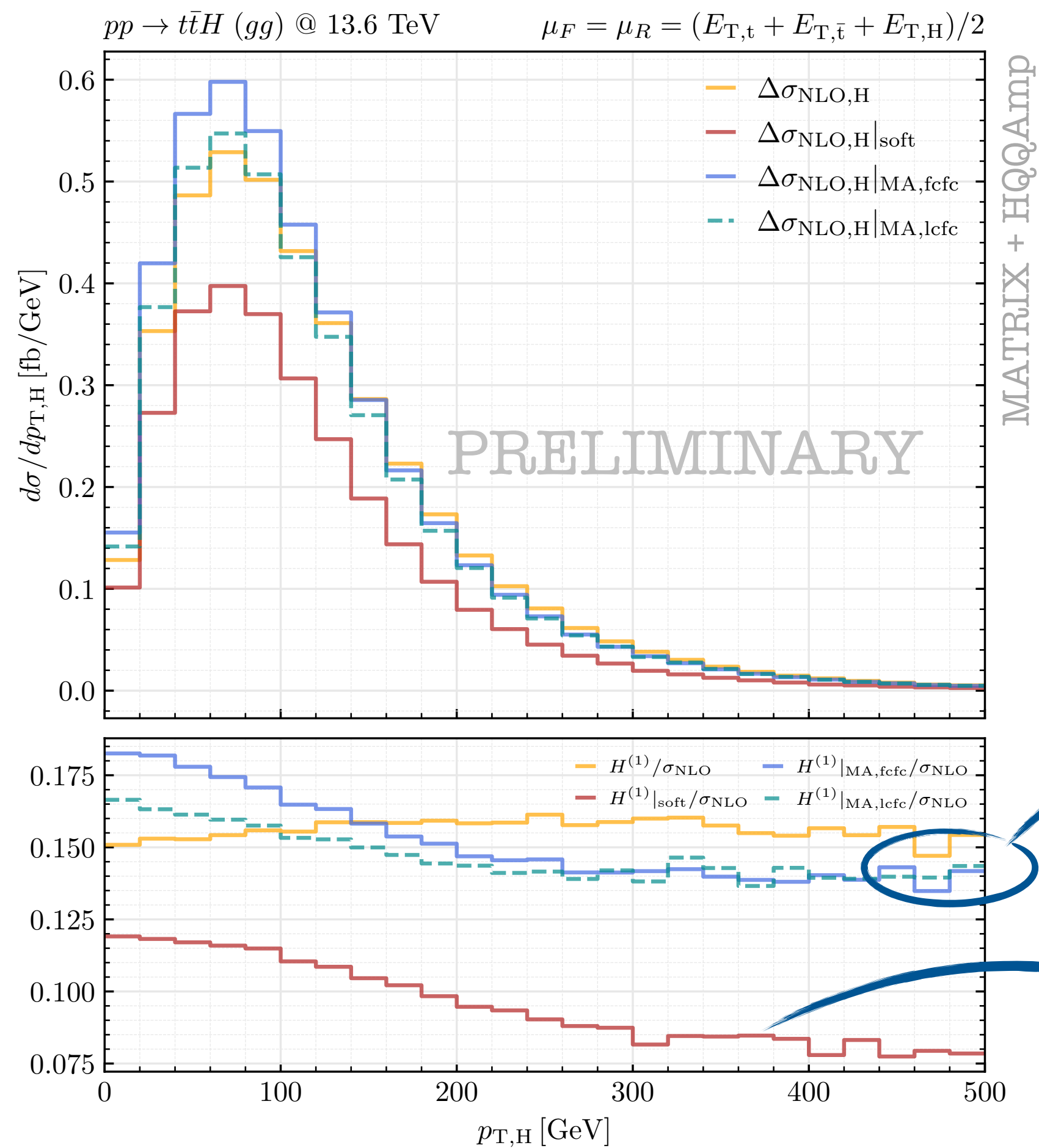
- around the peak:
1. FC-FC massification and soft approximation are nearly equivalent
 2. LC-FC massification overestimates the exact result by almost a factor of 2

in the high- p_T tail:

1. missing subleading colour contributions are less relevant
2. soft approximation underestimates the exact result: $\mathcal{O}(2\%)$ difference of the NLO cross section

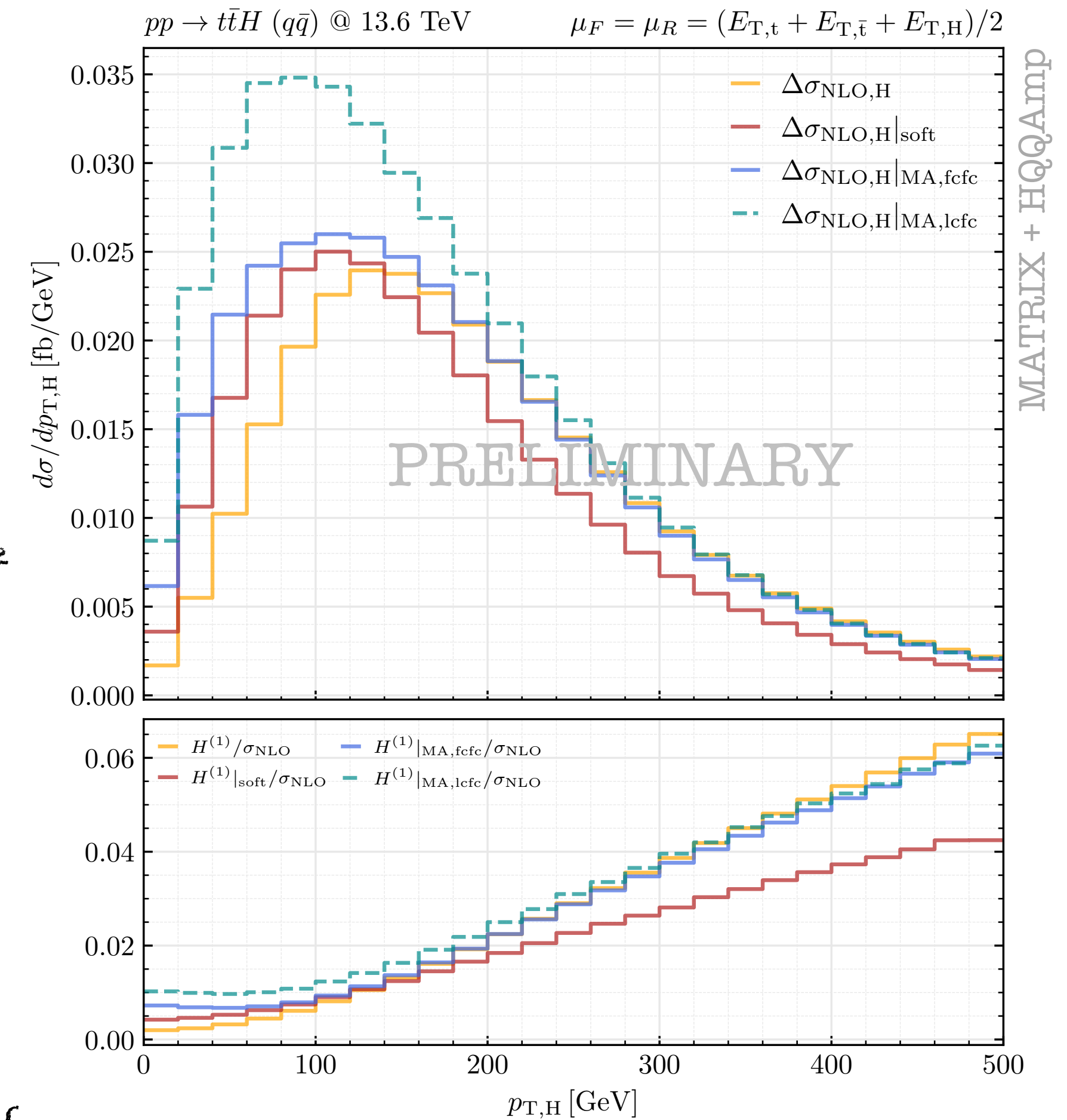
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massified results are in good agreement with the exact one-loop, with effects of $\mathcal{O}(1\%)$ of the NLO cross section in the tail

soft-approximated result is systematically below the exact one-loop, with effects of $\mathcal{O}(8\%)$ of the NLO cross section in the tail



First differential results: “best” $H^{(2)}$ prediction

setup: NNLO NNPDF31, $m_H = 125\text{GeV}$, $m_t = 173.3\text{GeV}$, $\mu_R = \mu_F = (E_{T,t} + E_{T,\bar{t}} + E_{T,H})/2$

H1-based error

$$\epsilon_{\text{soft}} = 2 \times \left| \frac{H^{(1)}|_{\text{soft}}}{H^{(1)}} - 1 \right| \times \max \left(\left| H^{(2)}|_{\text{soft}} \right|, \left| H^{(2)}|_{\text{MA}} \right| \right)$$

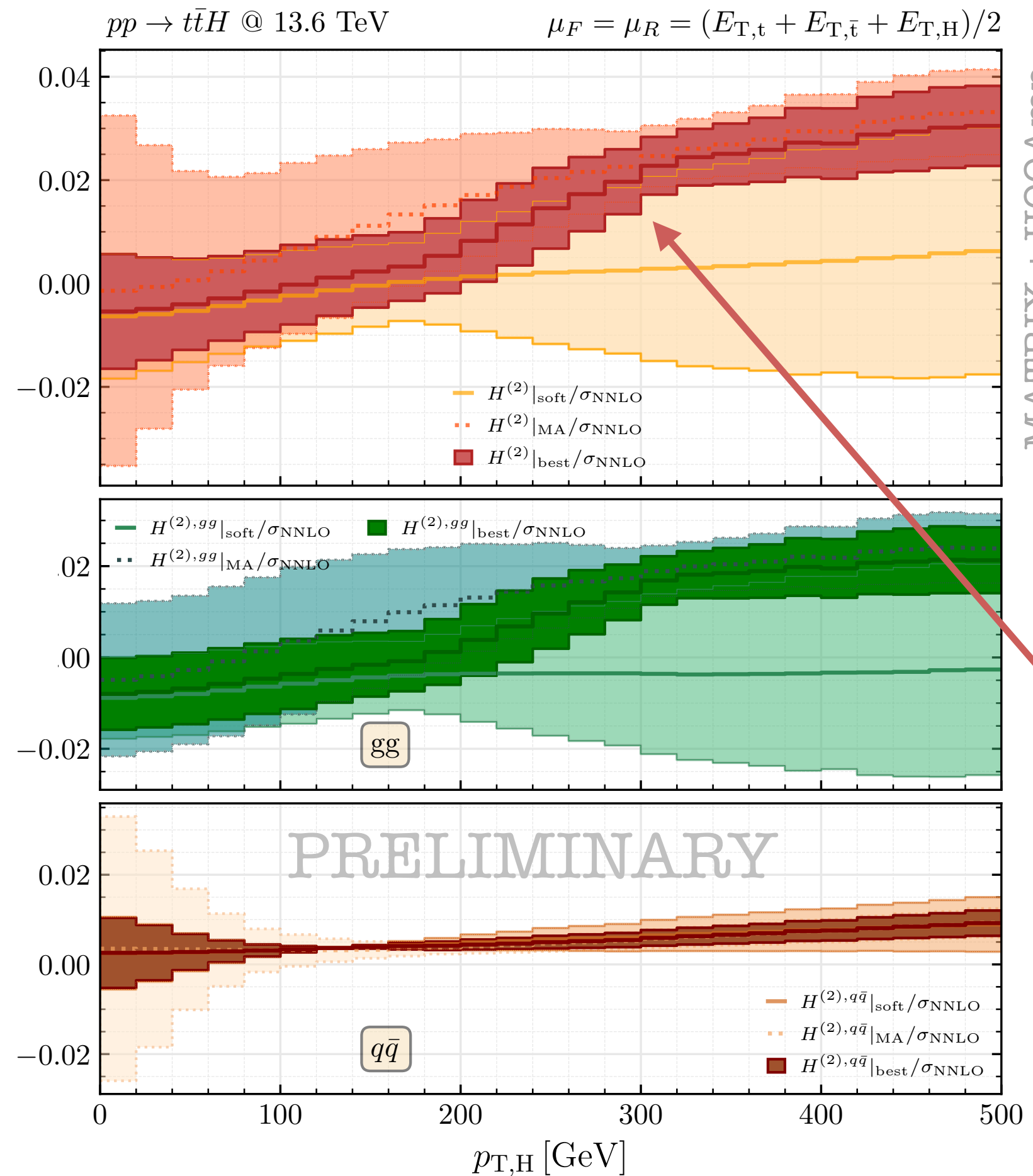
$$\epsilon_{\text{MA}} = 2 \times \max \left(\left| \frac{H^{(1)}|_{\text{MA,fcfc}}}{H^{(1)}} - 1 \right|, \left| \frac{H^{(1)}|_{\text{MA,lfcfc}}}{H^{(1)}} - 1 \right| \right) \times \max \left(\left| H^{(2)}|_{\text{soft}} \right|, \left| H^{(2)}|_{\text{MA}} \right| \right)$$

μ_{IR} -variation error

$$\zeta_{\text{soft}} = \max \left(\left| H^{(2)}|_{\text{soft}}(\tilde{Q}/2) + (Q/2 \rightarrow Q) - H^{(2)}|_{\text{soft}} \right|, \left| H^{(2)}|_{\text{soft}}(2\tilde{Q}) + (2Q \rightarrow Q) - H^{(2)}|_{\text{soft}} \right| \right)$$

$$\zeta_{\text{MA}} = \max \left(\left| H^{(2)}|_{\text{MA}}(\tilde{Q}/2) + (Q/2 \rightarrow Q) - H^{(2)}|_{\text{MA}} \right|, \left| H^{(2)}|_{\text{MA}}(2\tilde{Q}) + (2Q \rightarrow Q) - H^{(2)}|_{\text{MA}} \right| \right)$$

the final systematic error ξ on each approximation and for each partonic channel is obtained by taking the maximum between ϵ and ζ



for each partonic channel:

$$H^{(2)}|_{\text{best}} = \frac{\omega_{\text{soft}} H^{(2)}|_{\text{soft}} + \omega_{\text{MA}} H^{(2)}|_{\text{MA}}}{\omega_{\text{soft}} + \omega_{\text{MA}}}$$

$$\omega_{\text{soft}} = \frac{1}{\xi_{\text{soft}}^2}$$

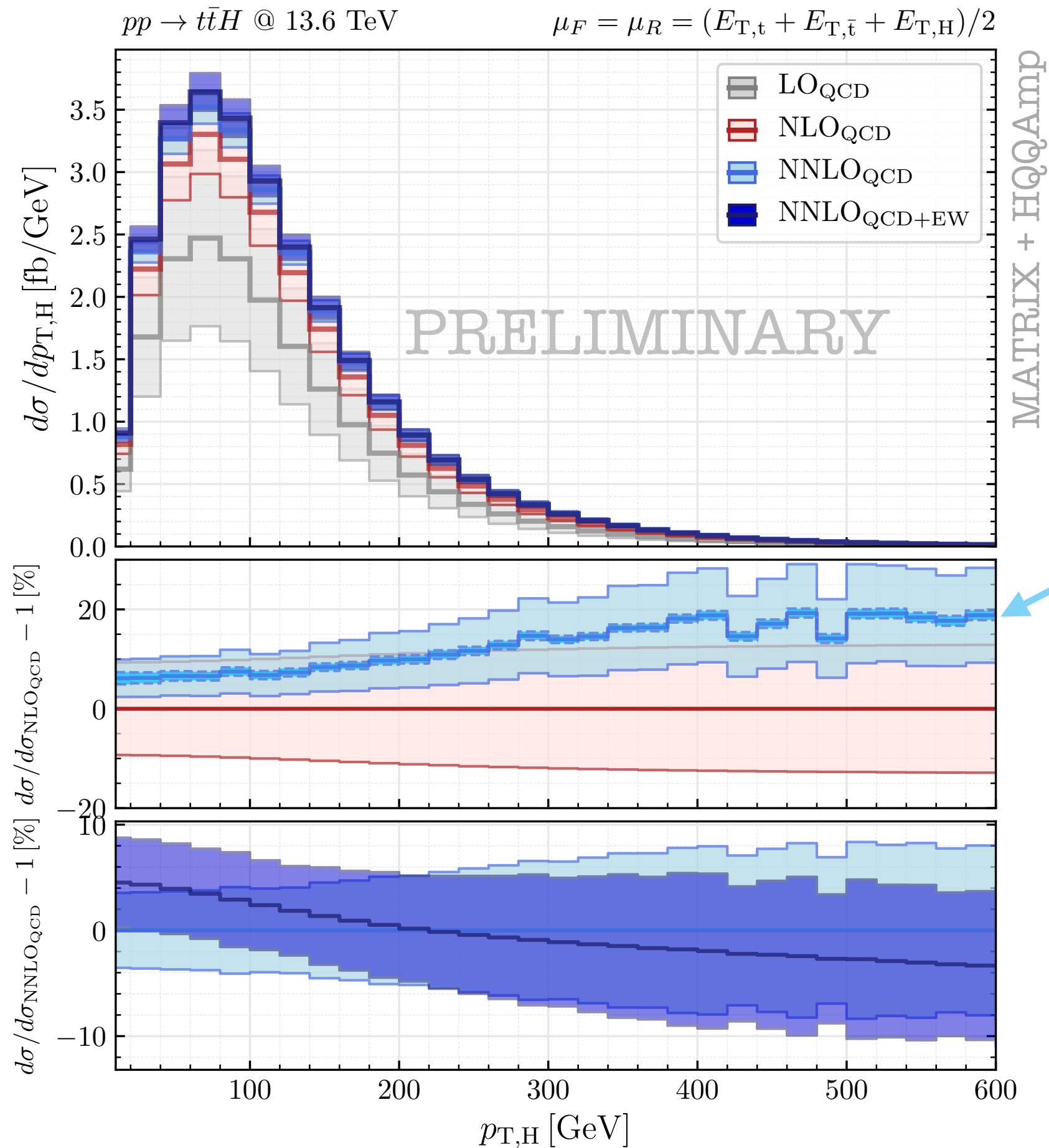
$$\omega_{\text{MA}} = \frac{1}{\xi_{\text{MA}}^2}$$

the errors on each channel are finally combined quadratically

1. the “best” prediction nicely interpolates between the two limits
2. the associated error does not vary strongly over the $p_{T,H}$ range
3. the individual soft and massified predictions have overlapping error bands

NNLO QCD + EW corrections

setup: NNLO NNPDF40_nnlo_as_0118_qed, $m_H = 125.09\text{GeV}$, $m_t = 172.5\text{GeV}$



systematic error associated with the "best" prediction for the double-virtual contribution

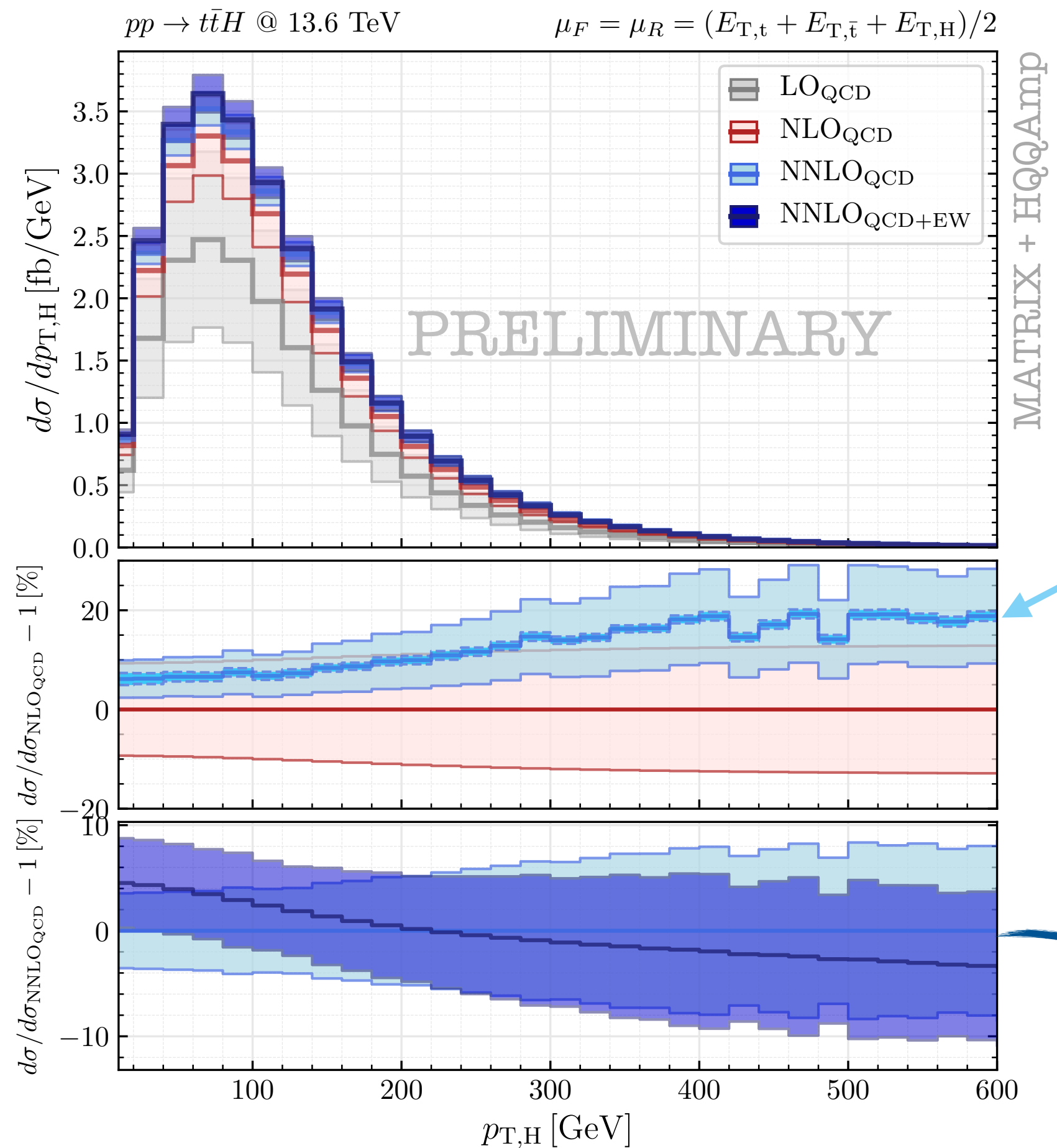
total XS at fixed scale $\mu_R = \mu_F = m_t + m_H/2$

σ [fb]	$\sqrt{s} = 13.6$ TeV
$\sigma_{\text{LO}_{\text{QCD}}}$	423.438 $^{+30.7\%}_{-21.8\%}$
$\sigma_{\text{NLO}_{\text{QCD}}}$	528.665 $^{+5.7\%}_{-9.0\%}$
$\sigma_{\text{NNLO}_{\text{QCD}}}^{\text{SA}}$	548.8 (3.4) $^{+0.8\%}_{-3.0\%}$
$\sigma_{\text{NNLO}_{\text{QCD}}}^{\text{best}}$	550.5 (4.6) $^{+0.9\%}_{-3.0\%}$
$\sigma_{\text{NNLO}_{\text{QCD}+\text{EW}}}^{\text{best}}$	562.3 (4.6) $^{+1.1\%}_{-3.0\%}$

- ▶ NNLO QCD predictions based on the soft-approximated and "best" double virtual are **fully compatible**: difference of 0.3 %
- ▶ the **systematic uncertainty** based on the refined prescription is **slightly larger**: $\mathcal{O}(0.8\%)$ instead of $\mathcal{O}(0.6\%)$ of the NNLO cross section

NNLO QCD + EW corrections

setup: NNLO NNPDF40_nnlo_as_0118_qed, $m_H = 125.09\text{GeV}$, $m_t = 172.5\text{GeV}$



systematic error associated with the "best" prediction for the double-virtual contribution

positive (negative) subdominant LO and NLO corrections in the small (large) $p_{T,H}$ region

total XS at fixed scale $\mu_R = \mu_F = m_t + m_H/2$

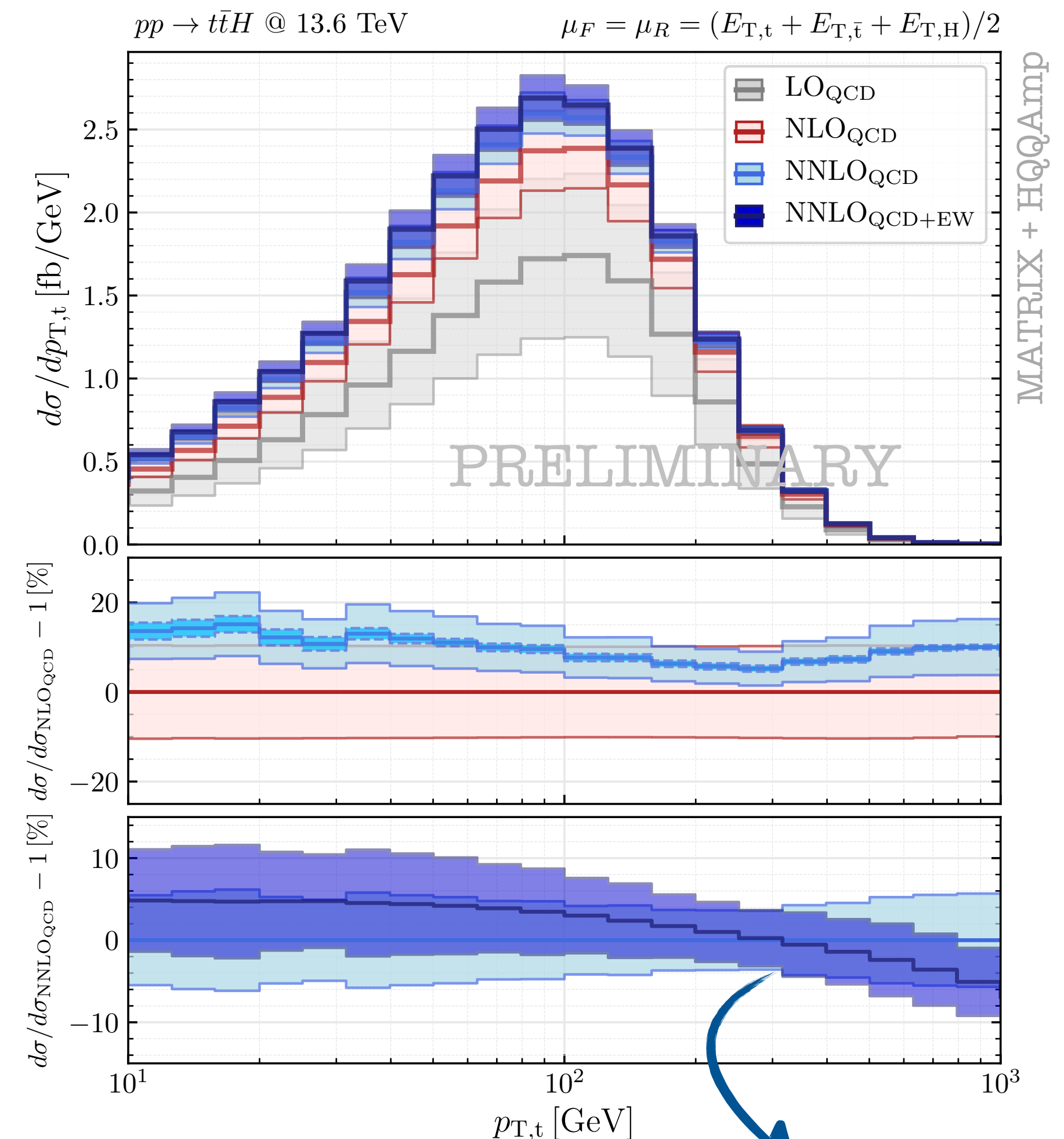
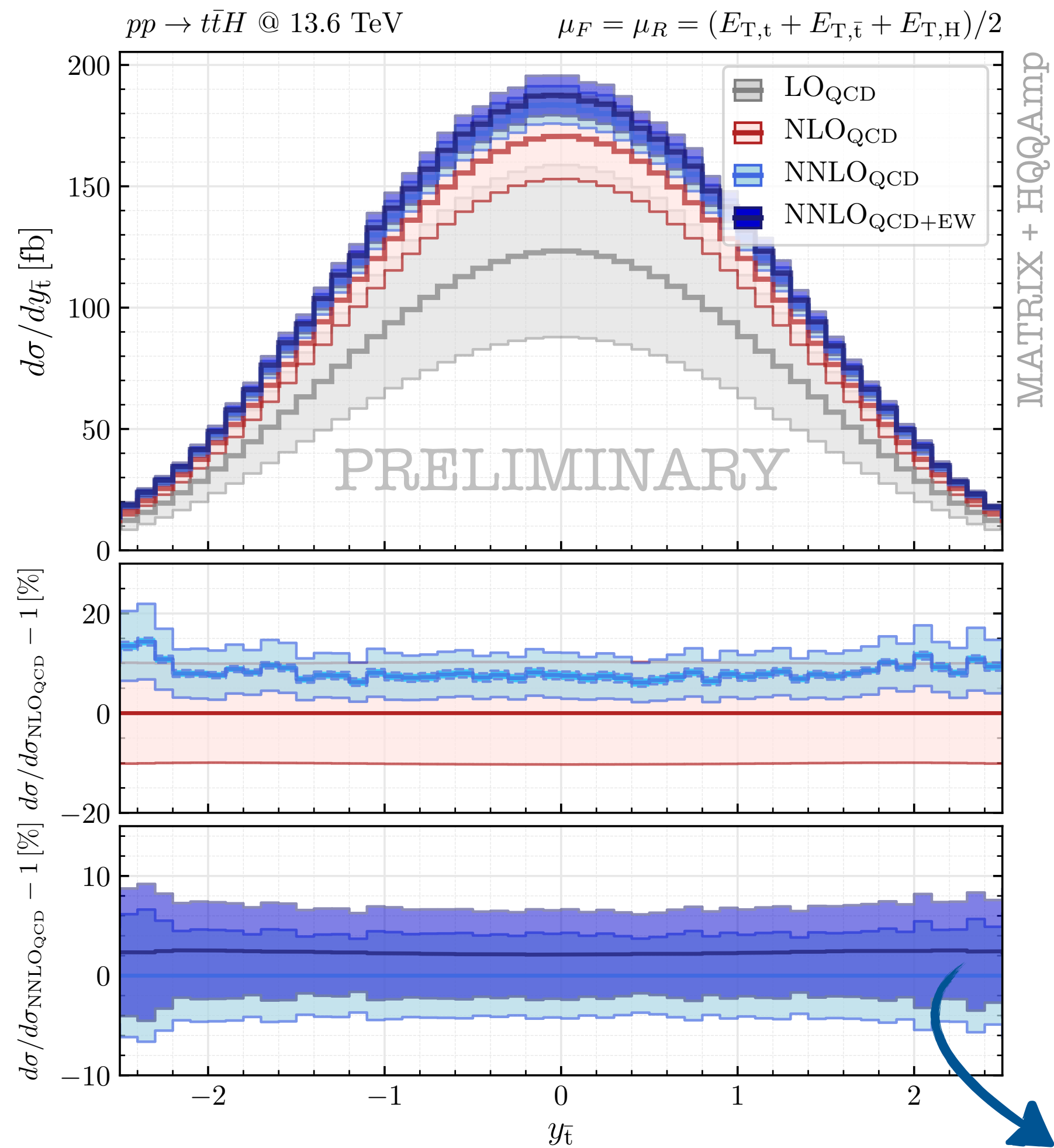
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$\sigma_{\text{NNLO}_{\text{QCD}+\text{EW}}}^{\text{best}}$	562.3 (4.6) $^{+1.1\%}_{-3.0\%}$

- inclusion of all subdominant LO ($\mathcal{O}(\alpha_s\alpha^2)$, $\mathcal{O}(\alpha^3)$) and NLO ($\mathcal{O}(\alpha_s^2\alpha^2)$, $\mathcal{O}(\alpha_s\alpha^3)$, $\mathcal{O}(\alpha^4)$) contributions: +2 % at the cross section level

NNLO QCD + EW corrections

more distributions ...

setup: NNLO NNPDF40_nnlo_as_0118_qed, $m_H = 125.09\text{GeV}$, $m_t = 172.5\text{GeV}$



Conclusions

- ▶ As the LHC has entered its “precision” phase, more accurate theoretical predictions are of paramount importance
- ▶ the current frontier is represented by NNLO corrections for $2 \rightarrow 3$ processes with **several massive external legs**
main bottleneck: two-loop amplitudes
- ▶ the associated production of a Higgs boson with a top-quark pair ($t\bar{t}H$) belongs to this category and it is crucial for the measurement of the top-Yukawa coupling
- ▶ **strategy:** develop physically motivated, reasonable and reliable **approximations** for the double-virtual contribution
 - SOFT-BOSON APPROXIMATION**
 - MASSIFICATION**
- ▶ the quantitative impact of the genuine two-loop contribution, in our computation, is relatively **small** ($\sim 1\%$ on σ_{NNLO})
- ▶ thus we have achieved a **good control** of the systematic uncertainties and a **reduction** of the perturbative uncertainties
- ▶ we have “updated” our previous prediction for the total cross section by designing a **more solid estimate** of the double-virtual contribution based on both approximations
- ▶ we have shown **preliminary differential results** for the Higgs transverse momentum (and few other distributions)
- ▶ we have included the full tower of **EW corrections**

Conclusions

- ▶ As the LHC has entered its “precision” phase, more accurate theoretical predictions are of paramount importance
- ▶ the current frontier is represented by NNLO corrections for $2 \rightarrow 3$ processes with **several massive external legs**
main bottleneck: two-loop amplitudes
- ▶ the associated production of a Higgs boson with a top-quark pair ($t\bar{t}H$) belongs to this category and it is crucial for the measurement of the top-Yukawa coupling
- ▶ **strategy:** develop physically motivated, reasonable and reliable **approximations** for the double-virtual contribution
 - SOFT-BOSON APPROXIMATION**
 - MASSIFICATION**
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THANK YOU!! stay tuned!!