



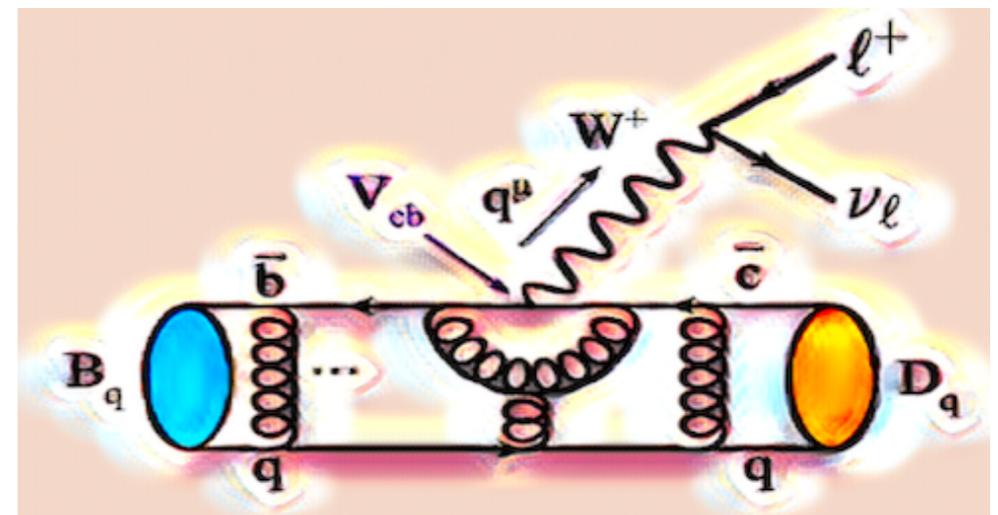
**University of
Zurich**^{UZH}

The Flavor Puzzle: Hints for 3rd Family New Physics

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LHCb Workshop on semi-leptonic exclusive $b \rightarrow c$ decays

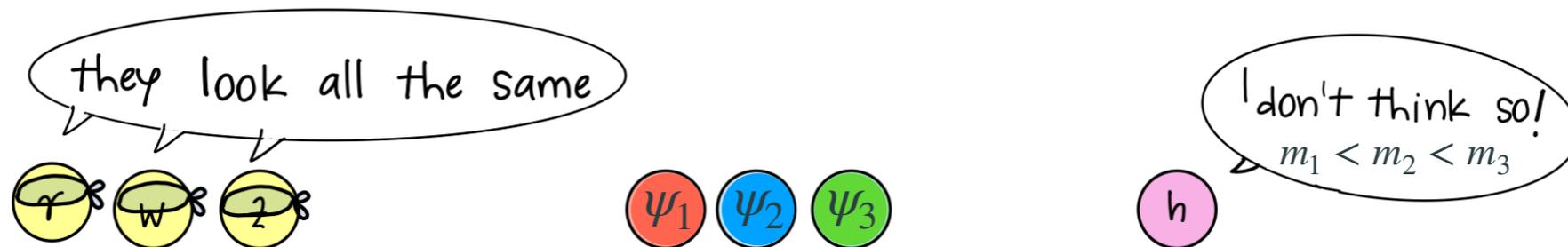
Laboratori Nazionali di Frascati (INFN)

April 12, 2023

It ended, but also begins with the Higgs

- Standard Model (SM) gauge sector is *flavor blind!*

$$\mathcal{G}_F(\text{gauge}) = U(3)^5 \equiv U(3)_q \times U(3)_u \times U(3)_d \times U(3)_\ell \times U(3)_e$$

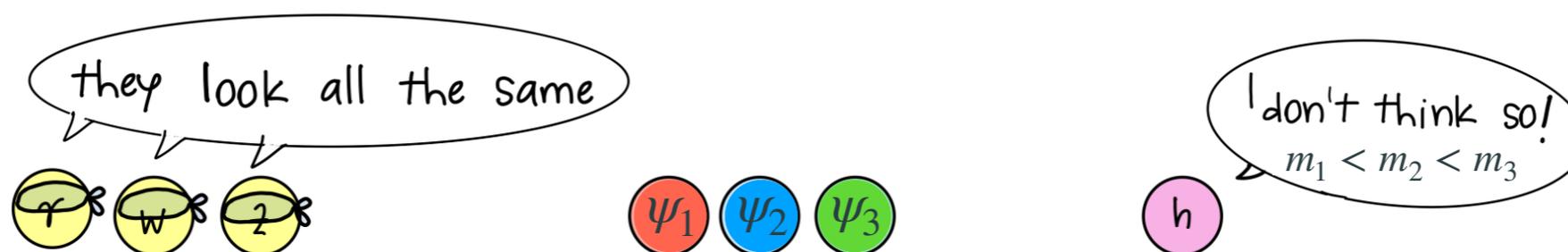


- The Higgs, the last piece of the SM discovered in 2012, strongly disagrees! Yukawas with Higgs are the only source of flavor violation in the SM, with a very hierarchical pattern that does not look accidental- *SM flavor puzzle*.

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**Flavor
Puzzle**

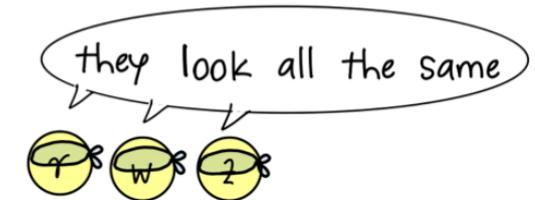
Is there a connection between the nature of the Higgs boson and the SM flavor puzzle? Clues toward the structure and scale of new physics (NP)?



Hints of NP structure: Flavor symmetries of the SM

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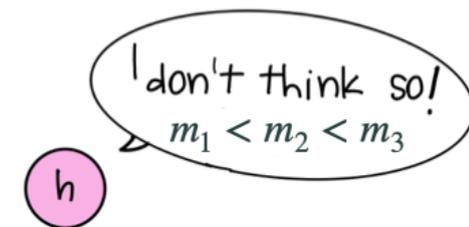
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Turn on Yukawas



$$Y_{ij} \bar{\Psi}_L^i H \Psi_R^j$$

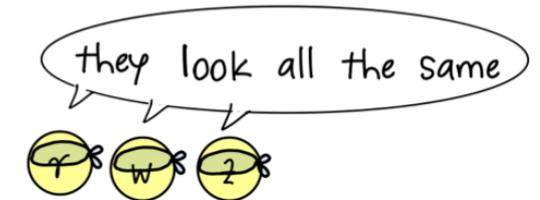


$$\mathcal{G}_F(\text{SM}) = U(1)_B \times U(1)_L$$

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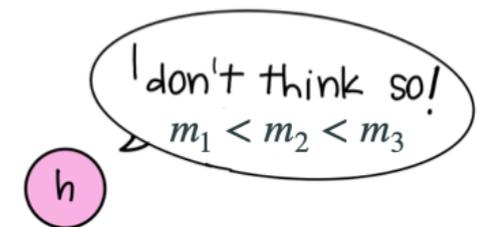
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Turn on Yukawas



$$Y_{ij} \bar{\Psi}_L^i H \Psi_R^j$$



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- But, since the light family Yukawa couplings are very small:

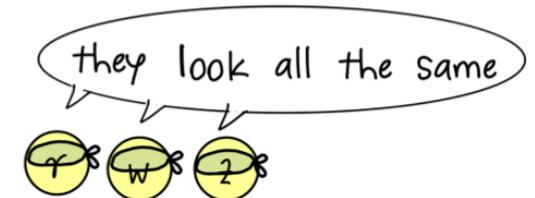
$$\mathcal{G}_F(\text{SM}) \approx U(2)^5 \equiv U(2)_q \times U(2)_u \times U(2)_d \times U(2)_\ell \times U(2)_e$$

$U(2)^5$ is a good accidental approximate symmetry of the SM!

Hints of NP structure: Flavor symmetries of the SM

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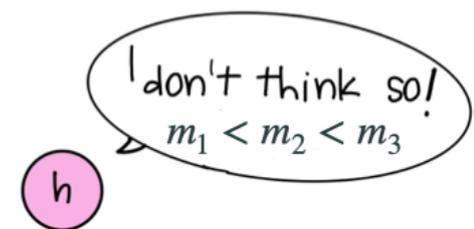
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**Flavor
Puzzle**

Perhaps this is not an accident- maybe there is NP responsible for this pattern that follows the same structure....

Hints towards NP scale: Nature of the Higgs boson



Λ_{NP}^2

Higgs Hierarchy Problem

Pre-LHC viewpoint: Nature must be natural!

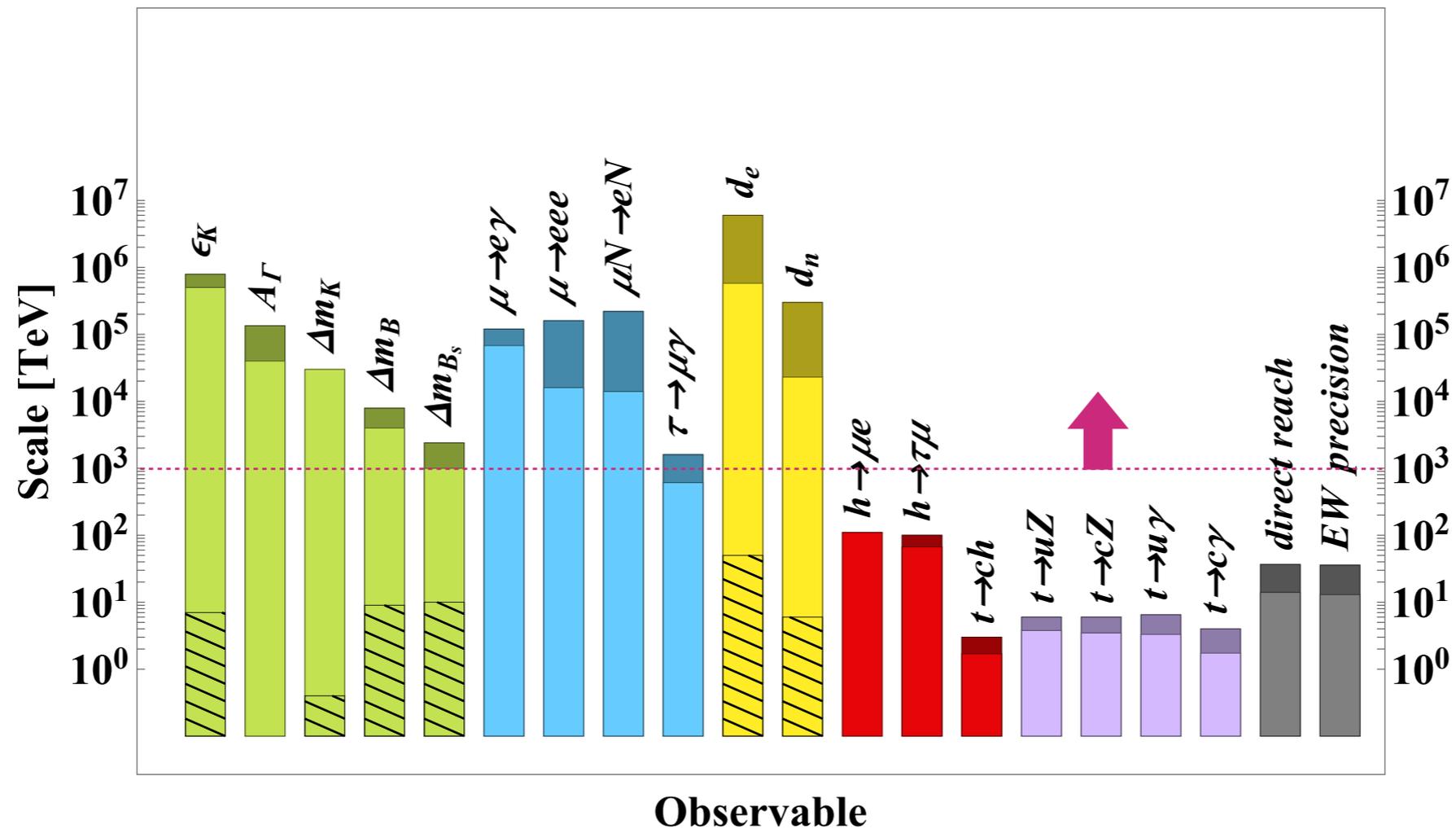
- The Higgs mass is unstable under quantum corrections- *it is quadratically sensitive to NP* in the UV. The top Yukawa gives the largest correction:

$$\Rightarrow \delta m_h^2(\text{top loop}) \approx \frac{3y_t^2}{4\pi^2} \Lambda_{\text{NP}}^2$$

- Naturalness principle: *Light NP that protects the Higgs mass* from large quantum corrections should appear no higher than the TeV scale.

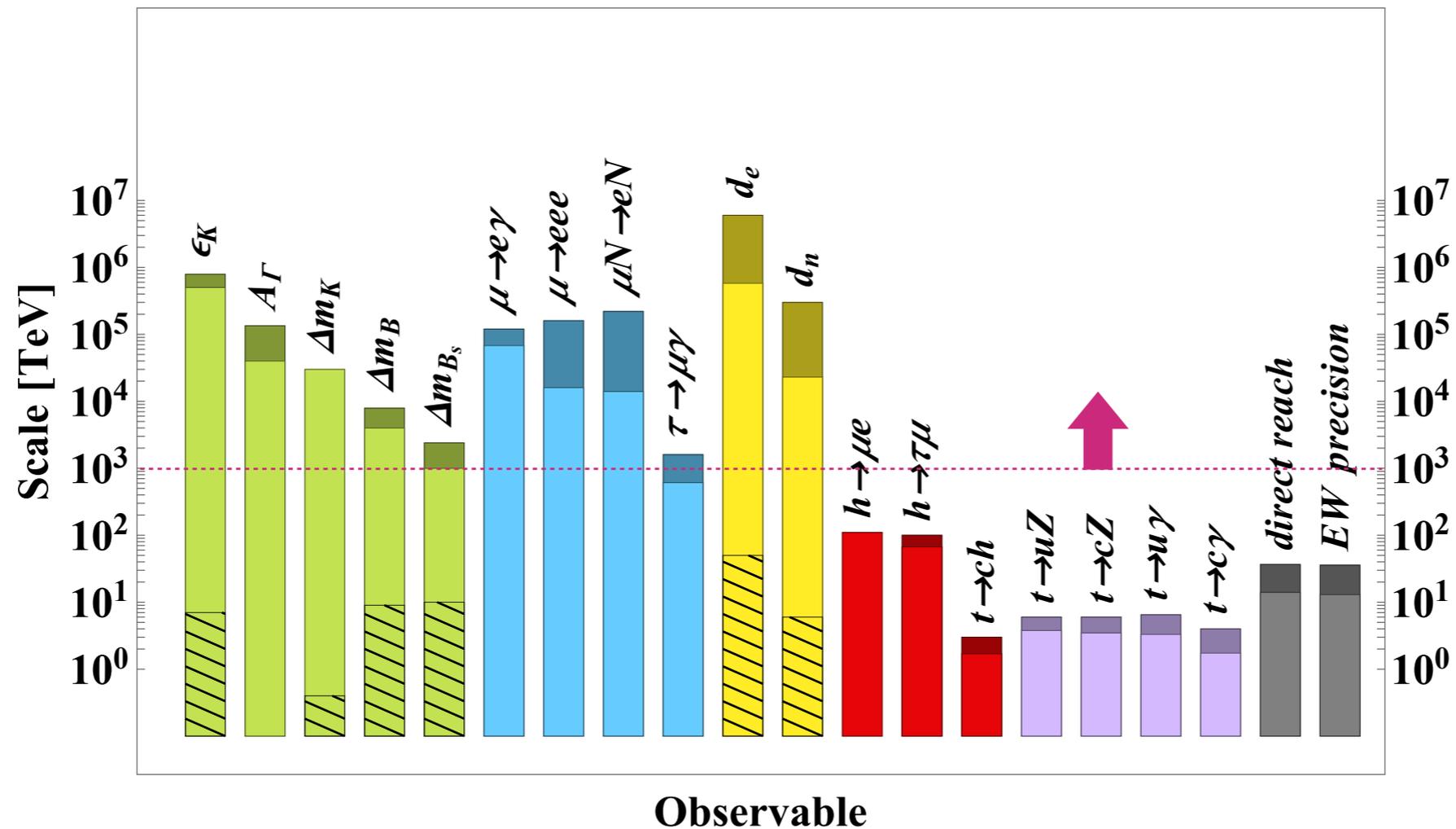
$$\delta m_h^2 / m_h^2 \lesssim 1 \quad \Rightarrow \quad \Lambda_{\text{NP}} \lesssim 500 \text{ GeV}$$

The Flavor Problem of Light New Physics

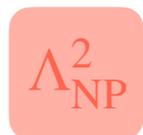


- Flavor bounds push the scale of flavor anarchic new physics (NP) above 1000 TeV.
- But, to address the EW hierarchy problem, NP must be light. It follows that **light NP must have a very specific flavor structure** in order to pass flavor bounds.

The Flavor Problem of Light New Physics



- It follows that light NP must have a very specific flavor structure in order to pass flavor bounds. *SM Yukawa-like flavor protection?*



Higgs Hierarchy Problem



Flavor Puzzle

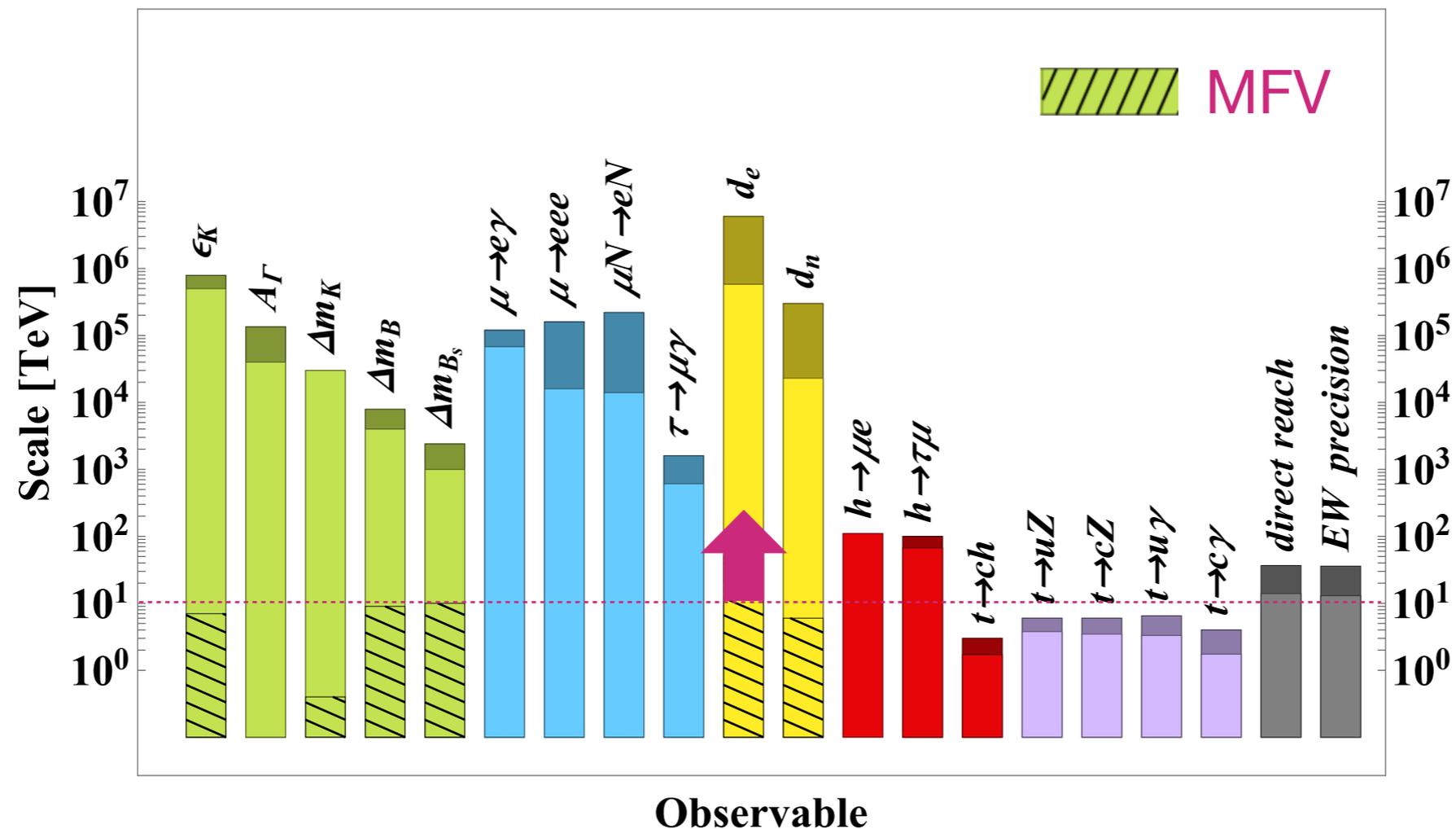
Minimal Flavor Violation (MFV)

- Key idea: Flavor puzzle probably solved at a high scale. Lightest NP can then be nearly flavor universal. All CP and flavor violation in the NP sector originates from the SM Yukawa couplings.

$$\lambda_{\text{FC}} \approx (Y_U Y_U^\dagger)_{\text{FC}} \approx y_t^2 \begin{pmatrix} 0 & V_{td}^* V_{ts} & V_{td}^* V_{tb} \\ V_{td} V_{ts}^* & 0 & V_{ts}^* V_{tb} \\ V_{td} V_{tb}^* & V_{ts} V_{tb}^* & 0 \end{pmatrix} \sim \begin{pmatrix} 0 & \lambda^5 & \lambda^3 \\ \lambda^5 & 0 & \lambda^2 \\ \lambda^3 & \lambda^2 & 0 \end{pmatrix}$$

| Minimally flavour violating dimension six operator | main observables | Λ [TeV] | |
|---|---|-----------------|-------|
| | | - | + |
| $\mathcal{O}_0 = \frac{1}{2}(\bar{Q}_L \lambda_{\text{FC}} \gamma_\mu Q_L)^2$ | $\epsilon_K, \Delta m_{B_d}$ | 6.4 | 5.0 |
| $\mathcal{O}_{F1} = H^\dagger (\bar{D}_R \lambda_d \lambda_{\text{FC}} \sigma_{\mu\nu} Q_L) F_{\mu\nu}$ | $B \rightarrow X_s \gamma$ | 9.3 | 12.4 |
| $\mathcal{O}_{G1} = H^\dagger (\bar{D}_R \lambda_d \lambda_{\text{FC}} \sigma_{\mu\nu} T^a Q_L) G_{\mu\nu}^a$ | $B \rightarrow X_s \gamma$ | 2.6 | 3.5 |
| $\mathcal{O}_{\ell 1} = (\bar{Q}_L \lambda_{\text{FC}} \gamma_\mu Q_L)(\bar{L}_L \gamma_\mu L_L)$ | $B \rightarrow (X) \ell \bar{\ell}, K \rightarrow \pi \nu \bar{\nu}, (\pi) \ell \bar{\ell}$ | 3.1 | 2.7 * |
| $\mathcal{O}_{\ell 2} = (\bar{Q}_L \lambda_{\text{FC}} \gamma_\mu \tau^a Q_L)(\bar{L}_L \gamma_\mu \tau^a L_L)$ | $B \rightarrow (X) \ell \bar{\ell}, K \rightarrow \pi \nu \bar{\nu}, (\pi) \ell \bar{\ell}$ | 3.4 | 3.0 * |
| $\mathcal{O}_{H1} = (\bar{Q}_L \lambda_{\text{FC}} \gamma_\mu Q_L)(H^\dagger i D_\mu H)$ | $B \rightarrow (X) \ell \bar{\ell}, K \rightarrow \pi \nu \bar{\nu}, (\pi) \ell \bar{\ell}$ | 1.6 | 1.6 * |
| $\mathcal{O}_{q5} = (\bar{Q}_L \lambda_{\text{FC}} \gamma_\mu Q_L)(\bar{D}_R \gamma_\mu D_R)$ | $B \rightarrow K \pi, \epsilon'/\epsilon, \dots$ | ~ 1 | |

Minimal Flavor Violation 20 Years Later



- In MFV, NP is flavor universal up to SM Yukawas. NP couples to valence quarks!
- For this reason, flavor bounds are still ok, but **direct searches** at the LHC push MFV new physics to the 10 TeV ballpark.

Naturalness Paradigm 20 Years Later

Higgs Hierarchy Problem

$$\delta m_h^2(\text{top loop}) \approx \frac{3y_t^2}{4\pi^2} \Lambda_{\text{NP}}^2$$

- Light NP protecting the Higgs mass from large corrections should appear. That didn't happen so far. If NP is almost flavor universal as in MFV, we now have an experimentally proven “little hierarchy problem”:

$$\Lambda_{\text{NP}} \gtrsim 10 \text{ TeV} \quad \Rightarrow \quad m_h^2 / \delta m_h^2 \sim 10^{-3}$$

So, did naturalness fail as a paradigm?

- This seems to be an increasingly common viewpoint. **Personal opinion:** Indeed, we were too aggressive, but this view is overly pessimistic.

$$m_h^2 / \delta m_h^2 \sim 10^{-3} \quad \text{vs.} \quad m_h^2 / M_P^2 \sim 10^{-34}$$

$(\Lambda_{\text{NP}} \sim 10 \text{ TeV})$ $(\Lambda_{\text{NP}} \sim M_P)$

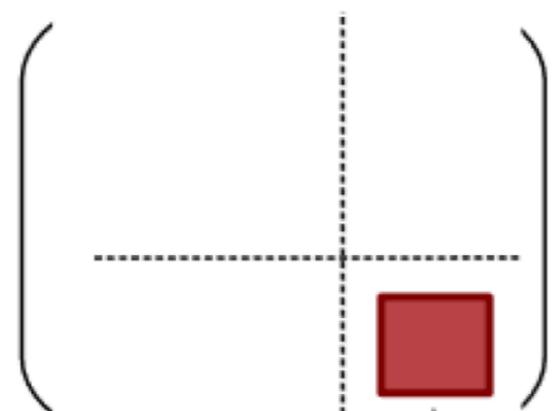
- Nature seems a bit fine-tuned. **However, I would not discard naturalness arguments:** they still provide the best hope that light NP could be around the corner.
- Can we do better than 10 TeV? To answer this question, we need to ask: Is there a “**more natural**” flavor protection for NP than what is provided by MFV?

U(2) is the natural successor to MFV

- Key idea: New physics is **NOT** flavor universal. In particular, there are **new flavor non-universal interactions at the TeV scale coupled dominantly to the third family**. NP coupled to top is what we need to address the **Higgs hierarchy problem**.
- Unlike in the MFV case, **these new interactions see flavor just like the SM Higgs**. They **could be connected to a low scale solution to the SM flavor puzzle**.

U(2) is the natural successor to MFV

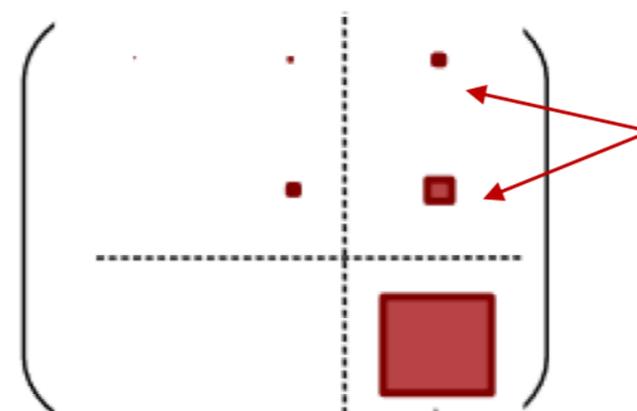
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- Unlike in the MFV case, **these new interactions see flavor just like the SM Higgs**. They **could be connected to a low scale solution to the SM flavor puzzle**.
- NP dominantly coupled to the third family quarks (+leptons) enjoys a $U(2)^3$ ($U(2)^5$) flavor symmetry, just like the SM Yukawa couplings.



Exact $U(2)$ limit

NP coupled only to 3rd family

\approx



Observed Yukawa

Also small couplings to light families

$U(2)$ -breaking effects

Barbieri et al, [1105.2296](#)

Isidori, Straub, [1202.0464](#)

Fuentes-Martin et al, [1909.02519](#)

U(2) compared with MFV

Flavor diagonal couplings (direct searches)

- In the exact U(2) limit, we have flavor diagonal, but non-universal NP.

Exact U(3)

$$\bar{q}_L^a \gamma_\mu q_L^a$$

Exact U(2)

$$\bar{q}_L^3 \gamma_\mu q_L^3 + \epsilon \bar{q}_L^i \gamma_\mu q_L^i$$


- *Key benefit*: Different NP coupling for light families makes it possible to suppress couplings to valence quarks and relax direct search bounds.

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Flavor violating couplings

MFV: Minimally broken U(3)

$$\bar{q}_L^a \lambda_{\text{FC}}^{ab} \gamma_\mu q_L^b$$

Minimally broken U(2)

$$\bar{q}_L^i V_q^i \gamma_\mu q_L^3$$

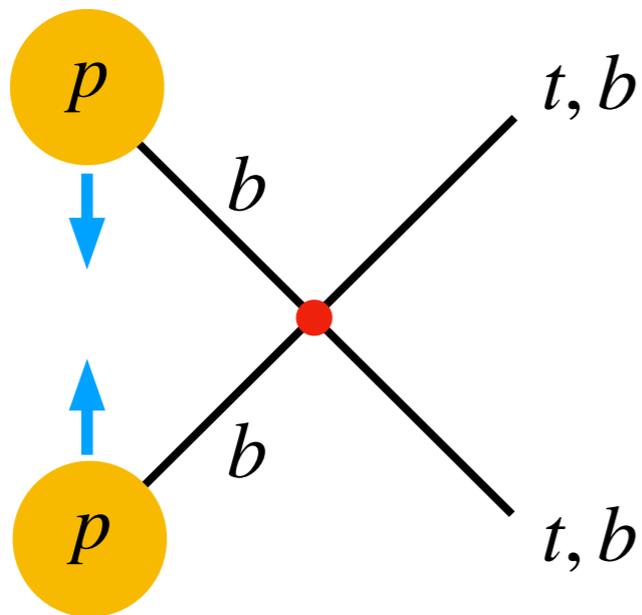
$$V_q \sim \mathcal{O} \begin{pmatrix} 0 \\ V_{cb} \end{pmatrix}$$

Phenomenology of the U(2) hypothesis

Flavor diagonal couplings: $\bar{q}_L^3 \gamma_\mu q_L^3 + \epsilon \bar{q}_L^i \gamma_\mu q_L^i + \bar{\ell}_L^3 \gamma_\mu \ell_L^3$

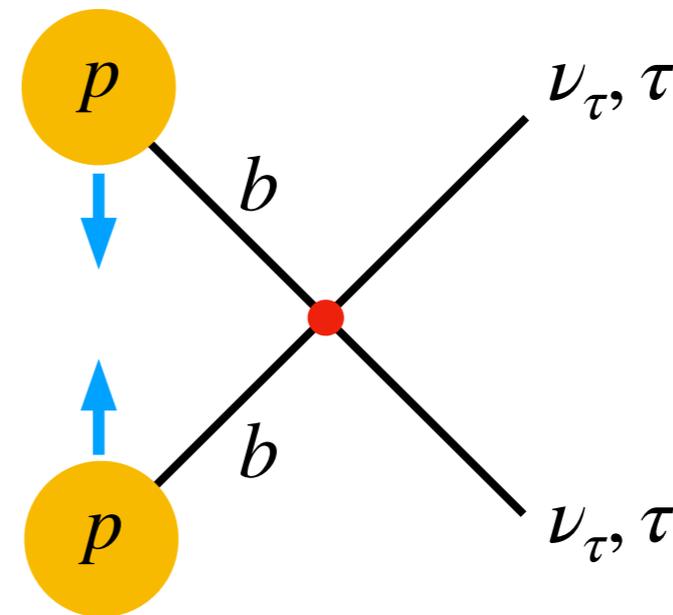
- Third family direct searches at the LHC (limit $\epsilon \rightarrow 0$)

$U(2)^3$ (quarks only)



- Signals: $t\bar{t}$, $b\bar{b}$ and $t\bar{b}$

$U(2)^5$ (also leptons)



Drell-Yan $\tau\bar{\tau}$ and mono- $\tau + E_T$

Phenomenology of the U(2) hypothesis

Flavor violating couplings: $\bar{q}_L^i V_q^i \gamma_\mu q_L^3, \quad V_q^T \sim \mathcal{O}(0, |V_{ts}|)$

- Leading effects: 3 → 2 transitions: top decays, *B*-physics, tau decays. Focus here on the operators for *B*-physics one can construct together with $\bar{\ell}_L^3 \gamma^\mu \ell_L^3$:

| <u>U(2)-breaking operator</u> | <u>Process</u> | <u>Example Observables</u> |
|--|----------------------------------|---|
| $(\bar{q}_L^i V_q^i \gamma_\mu q_L^3)^2$ | <i>B</i> -meson mixing | ΔM_{B_s} |
| $(\bar{q}_L^i V_q^i \gamma_\mu q_L^3)(\bar{\ell}_L^3 \gamma^\mu \ell_L^3)$ | Neutral current <i>B</i> -decays | $B \rightarrow K^{(*)} \tau \bar{\tau}, B \rightarrow K^{(*)} \nu_\tau \bar{\nu}_\tau, B_s \rightarrow \tau \bar{\tau}$ |
| $(\bar{q}_L^i V_q^i \gamma_\mu \sigma^I q_L^3)(\bar{\ell}_L^3 \gamma^\mu \sigma^I \ell_L^3)$ | Charged current <i>B</i> -decays | $B \rightarrow D^{(*)} \tau \bar{\nu}_\tau, \Lambda_b \rightarrow \Lambda_c \tau \bar{\nu}_\tau, B_c \rightarrow \tau \bar{\nu}_\tau$ |
| $(\bar{q}_L^i V_q^i \gamma^\mu q_L^3)(H^\dagger D_\mu H)$ | Neutral current <i>B</i> -decays | $B \rightarrow K^{(*)} \ell \bar{\ell}, B \rightarrow K^{(*)} \nu_\ell \bar{\nu}_\ell, B_s \rightarrow \ell \bar{\ell}$ |
| $y_b (\bar{q}_L^i V_q^i \sigma_{\mu\nu} H b_R) F^{\mu\nu}$ | Neutral current <i>B</i> -decays | $B \rightarrow X_s \gamma$ |

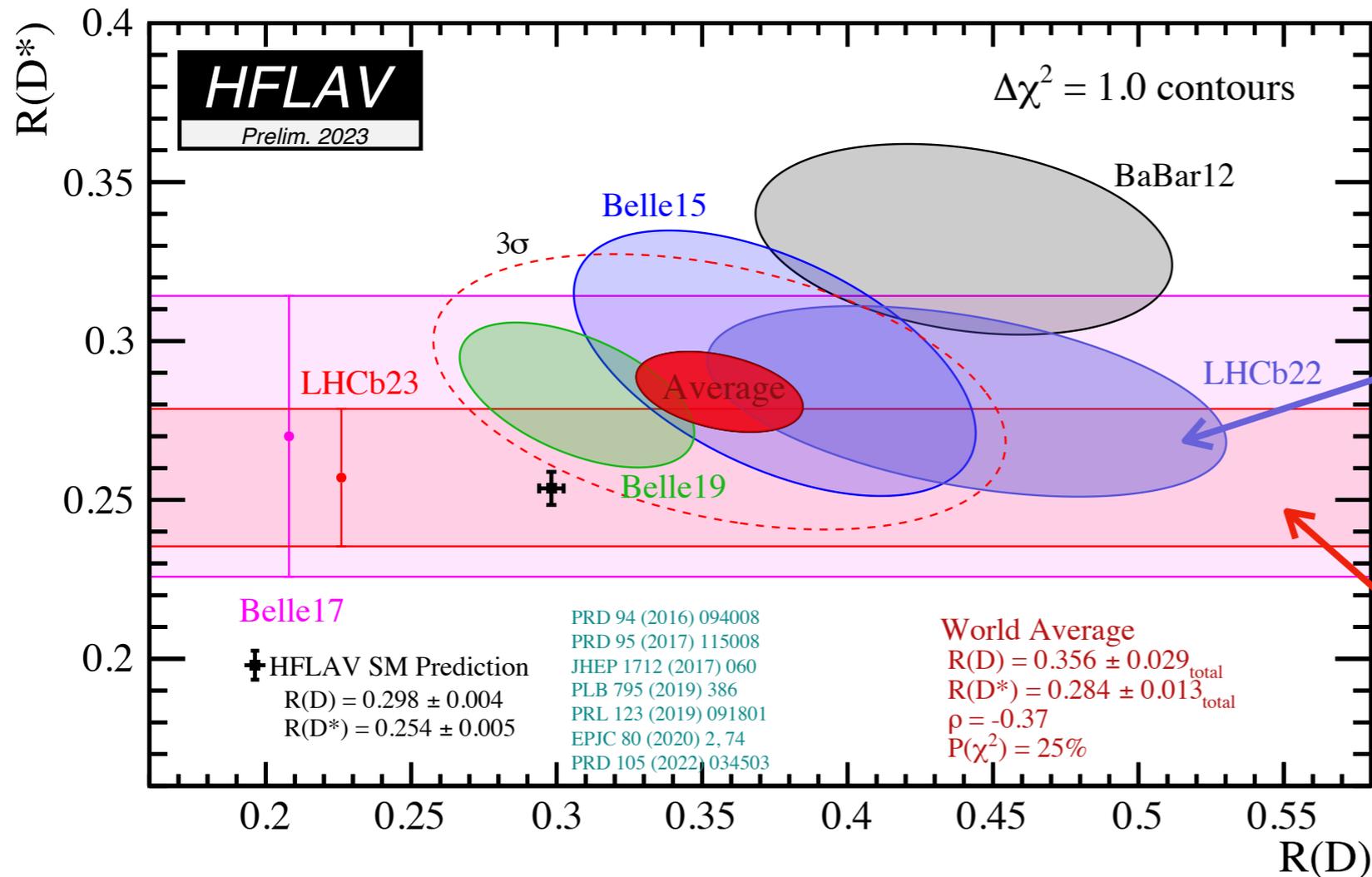
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| $y_b (\bar{q}_L^i V_q^i \sigma_{\mu\nu} H b_R) F^{\mu\nu}$ | Neutral current B-decays | $B \rightarrow X_s \gamma$ |

Anomalies in $b \rightarrow c$ semi-leptonics: R_D and R_{D^*}



$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)}\ell\bar{\nu})}$$

$[\ell = e, \mu]$

2022 LHCb $\tau \rightarrow \mu$: first joint measurement of R_D & R_{D^*} at a hadron collider. Only Run 1 data. [LHCb, 2302.02886]

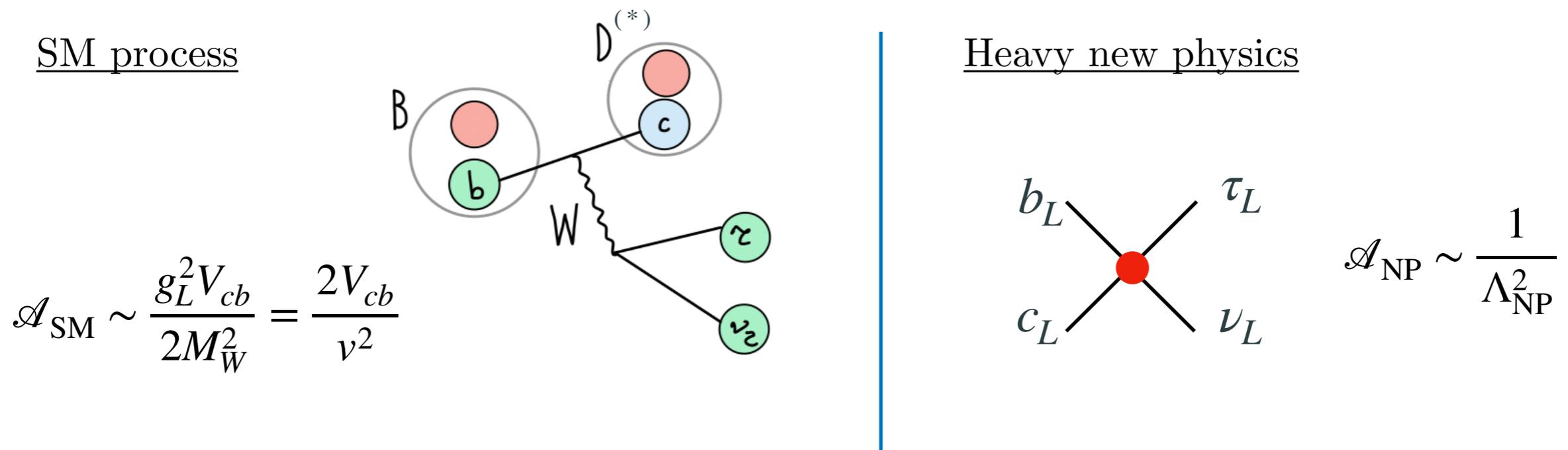
New! 2023 LHCb $\tau \rightarrow \text{had}$: R_{D^*} with Run 1 + partial Run 2 data. Hadronic taus.

- **Theoretically clean.** Measurements by Babar, Belle, LHCb in good agreement.
- **Enhancement of $\sim 10\%$** over SM due to excess in tau mode: $B \rightarrow D^{(*)}\tau\bar{\nu}_\tau$. ✓
- Combined, 3.2σ tension w.r.t SM. Measurement of $R_{\Lambda_c}/R_{\Lambda_c}^{\text{SM}} = 0.73 \pm 0.23$ reduces tension slightly. [LHCb, 2201.03497]

New physics in $b \rightarrow c\tau\nu$ decays

$$\delta R_{D^{(*)}} = R_{D^{(*)}}/R_{D^{(*)}}^{\text{SM}} - 1$$

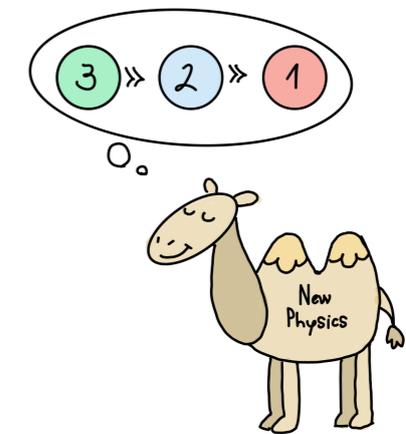
- We need $\sim 10\%$ of a tree-level SM process due to NP. Heavy NP should therefore also be tree-level to compete. Consider Fermi-like LH NP:



- The charged current B -anomalies are calling for a low NP scale!

$$2 \frac{\mathcal{A}_{\text{NP}}}{\mathcal{A}_{\text{SM}}} = \frac{v^2}{V_{cb} \Lambda_{\text{NP}}^2} \approx \delta R_{D^*} \quad \Rightarrow \quad \Lambda_{\text{NP}} \approx \frac{v}{\sqrt{V_{cb} \delta R_{D^*}}} \approx 3.6 \text{ TeV} \left(\frac{0.12}{\delta R_{D^*}} \right)^{1/2}$$

U(2)-like new physics in $b \rightarrow c\tau\nu$ decays



- Actually, following the U(2) hypothesis, we should have:

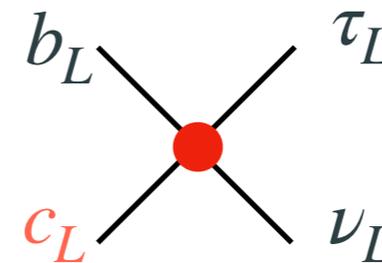
Flavor conserving



$$\mathcal{A}_{\text{NP}}^{33} \sim \frac{1}{\Lambda_{\text{NP}}^2}$$

+

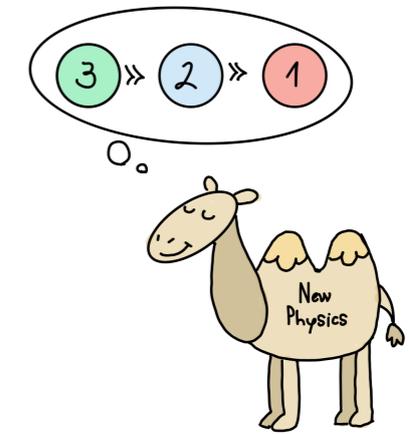
Flavor violating



$$\mathcal{A}_{\text{NP}}^{23} \sim \frac{V_q}{\Lambda_{\text{NP}}^2}$$

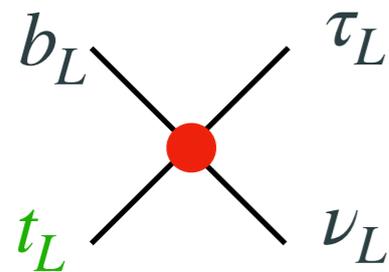
$$\mathcal{A}_{\text{NP}}(b \rightarrow c\tau\nu) = V_{cb}\mathcal{A}_{\text{NP}}^{33} + V_{cs}\mathcal{A}_{\text{NP}}^{23}$$

U(2)-like new physics in $b \rightarrow c\tau\nu$ decays



- Actually, following the U(2) hypothesis, we should have:

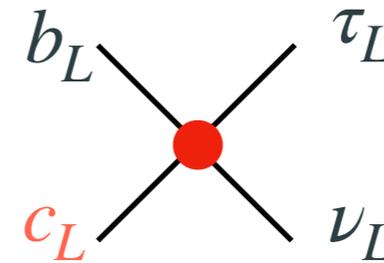
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+

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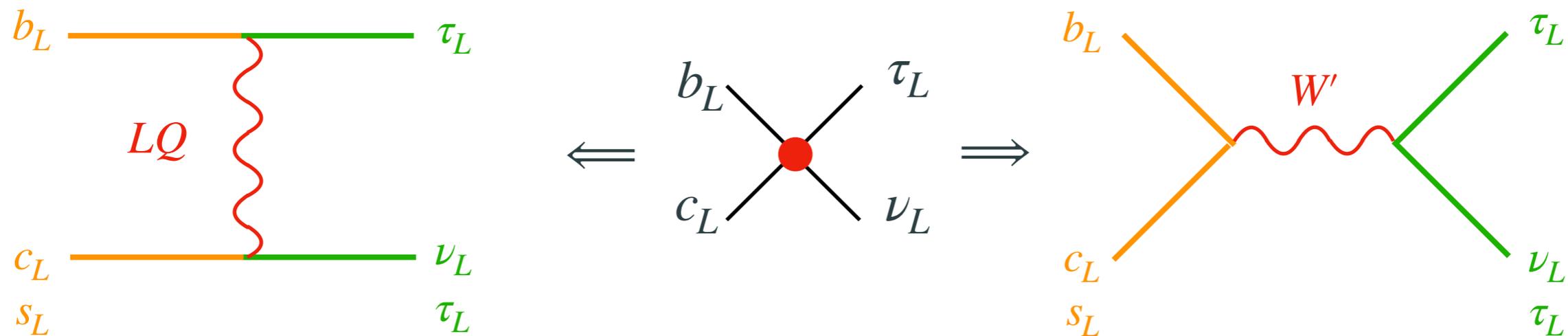
$$\mathcal{A}_{\text{NP}}(b \rightarrow c\tau\nu) = V_{cb}\mathcal{A}_{\text{NP}}^{33} + V_{cs}\mathcal{A}_{\text{NP}}^{23}$$

- U(2) suppressed flavor violation means we need an even lower NP scale!

$$2\frac{\mathcal{A}_{\text{NP}}}{\mathcal{A}_{\text{SM}}} \approx \frac{v^2}{\Lambda_{\text{NP}}^2} \left(1 + \frac{V_q}{V_{cb}} \right) \approx \delta R_{D^*} \quad \Rightarrow \quad \Lambda_{\text{NP}} \approx 1.3 \text{ TeV} \left(\frac{0.12}{\delta R_{D^*}} \right)^{1/2}$$

($V_q = 0.1$)

What kind of new particles could we have?



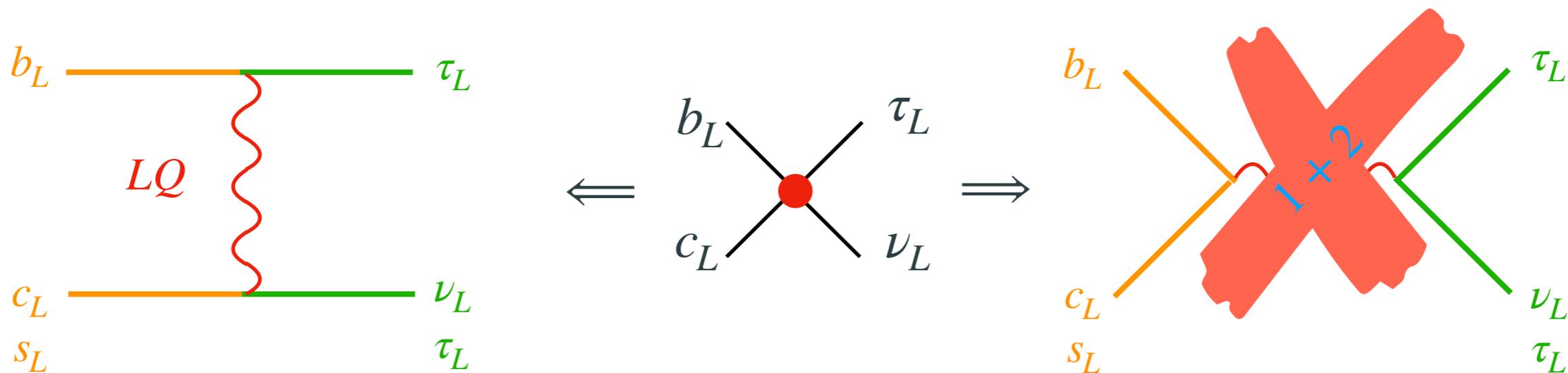
- LH NP $\implies b \rightarrow s\tau\tau(\nu\nu)$ couplings. LQ's have two important advantages

1. $\Delta F = 2$:



2. **Direct searches:** t-channel versus resonant s-channel production

Only leptoquarks are viable mediators!



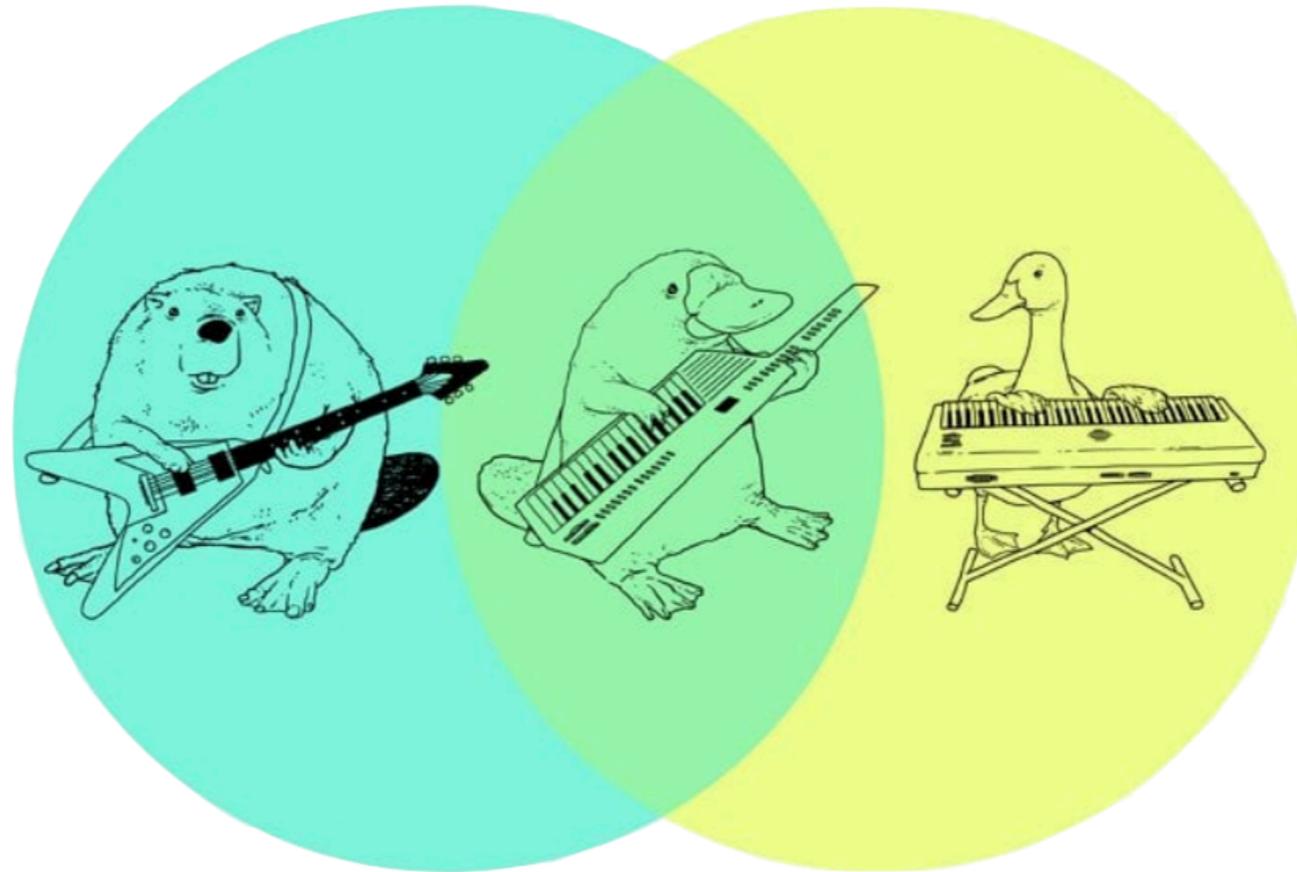
- LH NP $\implies b \rightarrow s\tau\tau(\nu\nu)$ couplings. LQ's have two important advantages

1. $\Delta F = 2$:



2. **Direct searches:** t-channel versus resonant s-channel production

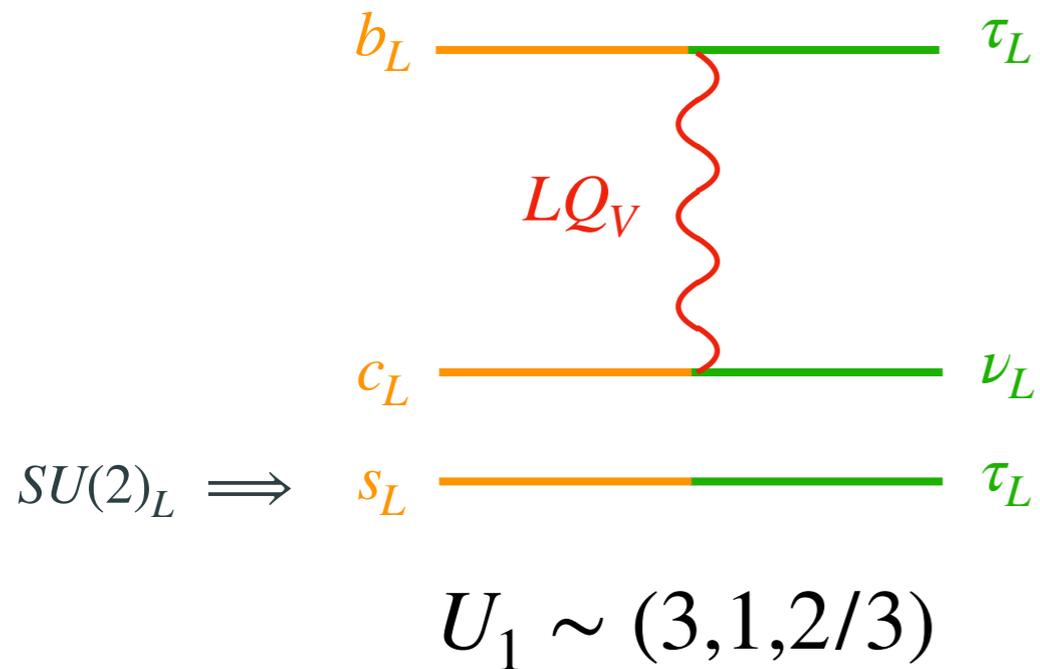
What is a leptoquark?



Like a cross between a beaver & a duck is a platypus or a cross between a keyboard & a guitar is a keytar, a cross between a lepton & a quark is a leptoquark (LQ)

Which leptoquark?

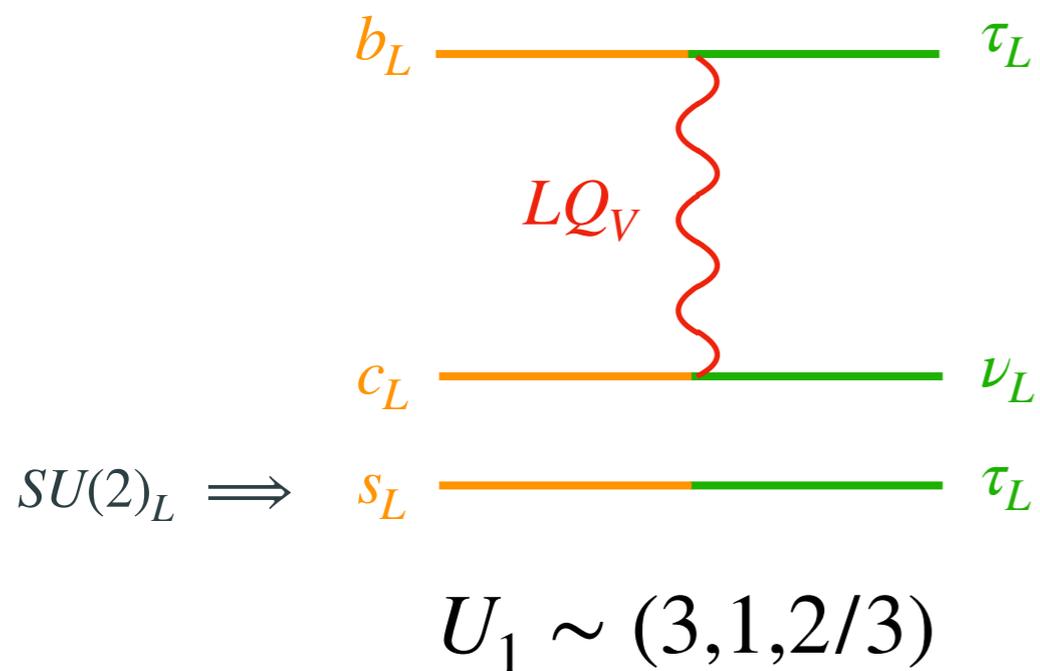
- Two possible options depending on the quark-lepton coupling:



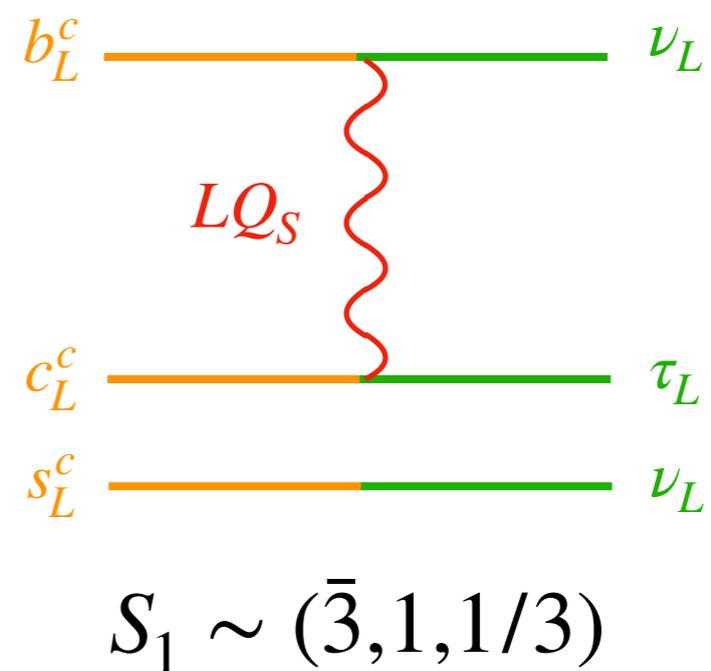
- Vector LQ
- $b \rightarrow c\tau\nu + b \rightarrow s\tau\tau$
- $b \rightarrow s\nu\nu$ at 1-loop
- Pati-Salam LQ
- No di-quark couplings (proton decay)

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- $b \rightarrow s\nu\nu$ at 1-loop
- Pati-Salam LQ
- No di-quark couplings (proton decay)



- Scalar LQ
- $b \rightarrow c\tau\nu + b \rightarrow s\nu\nu$
- Has di-quark couplings
- Works with large $c_R^c \tau_R$
- Doesn't follow U(2)

Simplified model for U_1 leptoquark

$$U_1 \sim (\mathbf{3}, \mathbf{1}, 2/3)$$

$$\mathcal{L} \supset \frac{g_U}{\sqrt{2}} U_1^\mu \left[(\bar{q}_L^3 \gamma_\mu \ell_L^3) + \beta_L^{s\tau} (\bar{q}_L^2 \gamma_\mu \ell_L^3) + \beta_R^{b\tau} (\bar{b}_R \gamma_\mu \tau_R) \right] + \text{h.c.}$$


U(2)-conserving


U(2)-breaking


U(2)-conserving

Simplified model for U_1 leptoquark

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↑ U(2)-conserving ↑ U(2)-breaking ↑ U(2)-conserving

↓ **RUNNING to EW SCALE + MATCHING** ↓

$$\mathcal{L}_{b \rightarrow c \tau \bar{\nu}} = -\frac{2}{v^2} V_{cb} \left[\left(1 + C_{LL}^c \right) (\bar{c}_L \gamma_\mu b_L) (\bar{\tau}_L \gamma^\mu \nu_L) - 2 C_{LR}^c (\bar{c}_L b_R) (\bar{\tau}_R \nu_L) \right]$$

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↑
U(2)-conserving

↑
U(2)-breaking

↑
U(2)-conserving

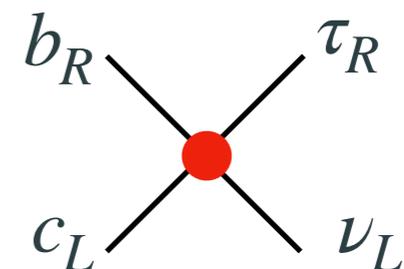
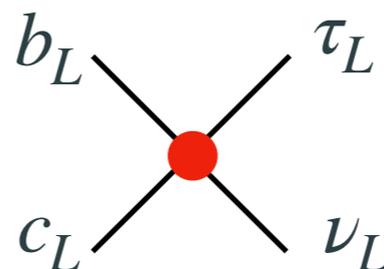


RUNNING to EW SCALE + MATCHING



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Contact interaction:



Low-energy WC's ↔ Model parameters:

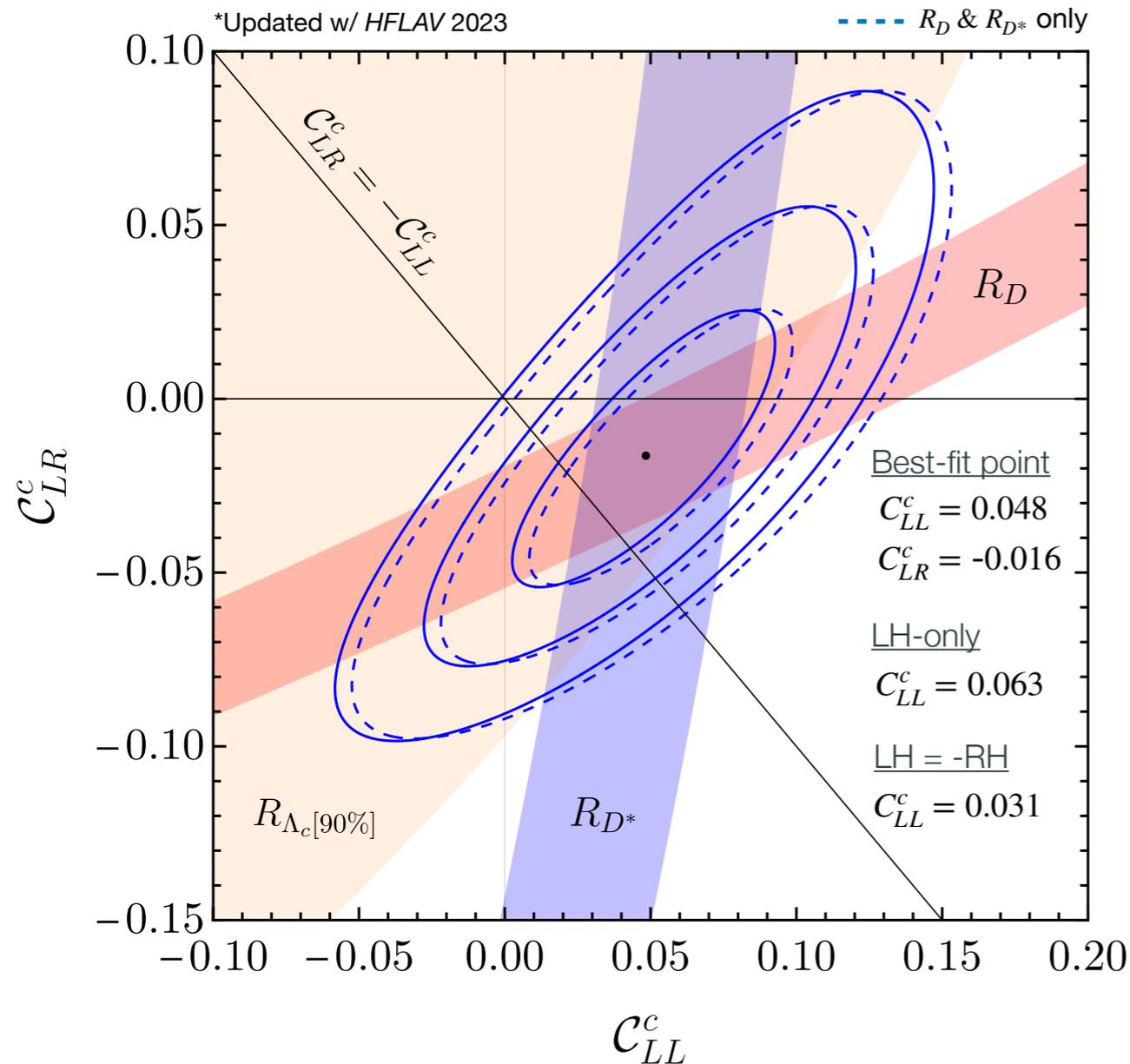
$$C_{LL}^c = \frac{g_U^2 v^2}{4M_U^2} \left(1 + \frac{V_{cs}}{V_{cb}} \beta_L^{s\tau} \right),$$

$$C_{LR}^c = \beta_R^{b\tau*} C_{LL}^c$$

Low-energy fit for U_1 leptoquark model

$$U_1 \sim (3, 1, 2/3)$$

$$\mathcal{L}_{b \rightarrow c \tau \bar{\nu}} = -\frac{2}{v^2} V_{cb} \left[\left(1 + C_{LL}^c \right) (\bar{c}_L \gamma_\mu b_L) (\bar{\tau}_L \gamma^\mu \nu_L) - 2 C_{LR}^c (\bar{c}_L b_R) (\bar{\tau}_R \nu_L) \right]$$



$$\delta R_{D^{(*)}} \approx 2C_{LL}^c - a_{D^{(*)}} C_{LR}^c \quad \begin{cases} a_D \approx 3.00 \\ a_{D^*} \approx 0.24 \end{cases}$$

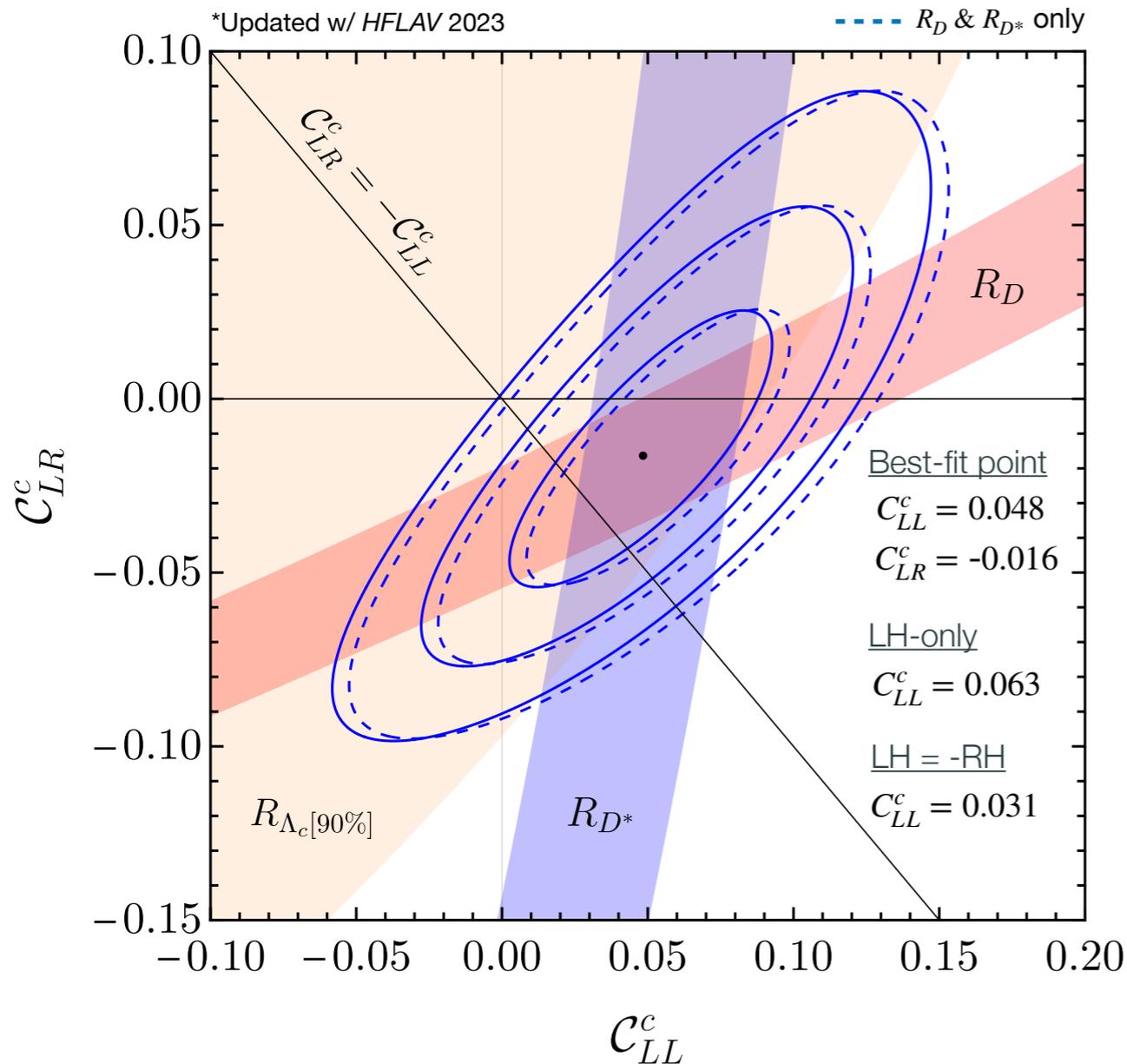
Low-energy WC's \leftrightarrow Model parameters

$$C_{LL}^c = \frac{g_U^2 v^2}{4M_U^2} \left(1 + \frac{V_{cs}}{V_{cb}} \beta_L^{s\tau} \right), \quad C_{LR}^c = \beta_R^{b\tau^*} C_{LL}^c$$

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Matching: NP scale and U(2)-breaking

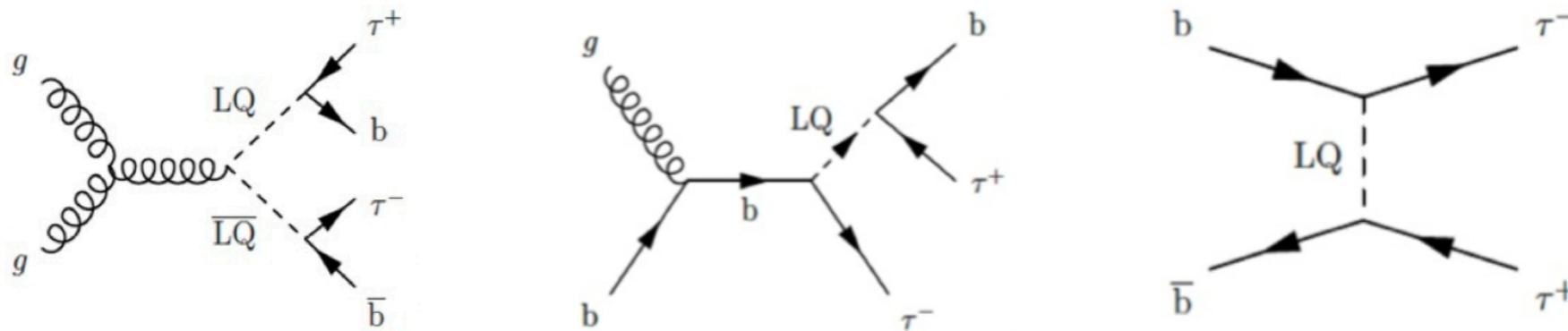
$$\frac{1}{\Lambda_{\text{NP}}^2} = \frac{g_U^2}{2M_U^2}, \quad V_q = \beta_L^{s\tau}$$

New physics scale preferred by low-energy fit:

$$\Lambda_{\text{NP}} \approx \{1.2, 1.5, 1.8\} \text{ TeV}, \quad (V_q = 0.1)$$

{LH-only, BFP, LH=-RH}

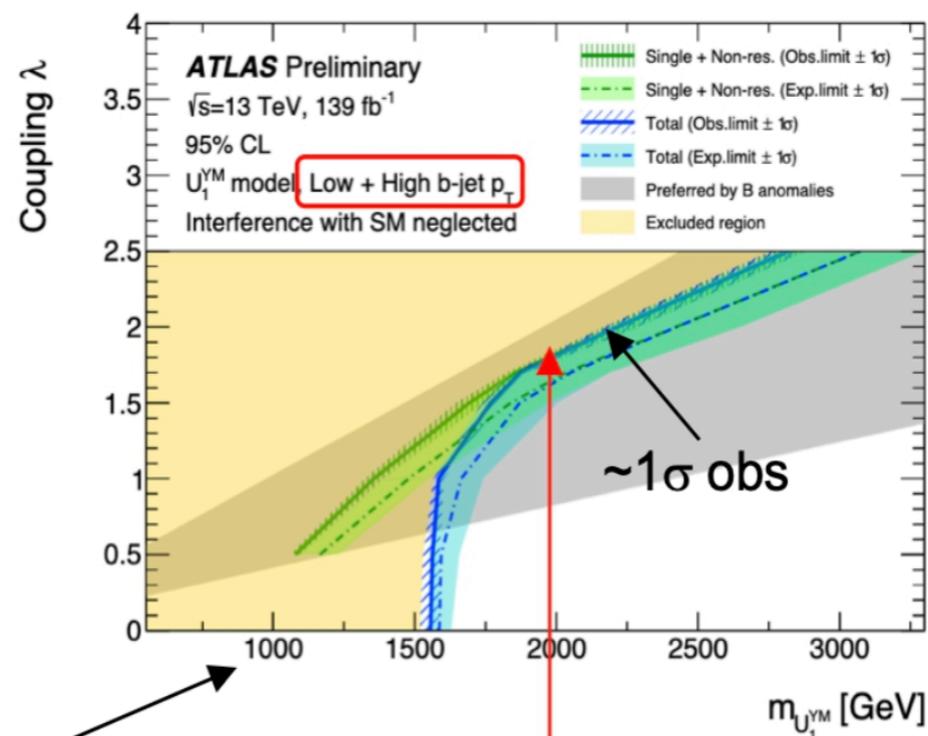
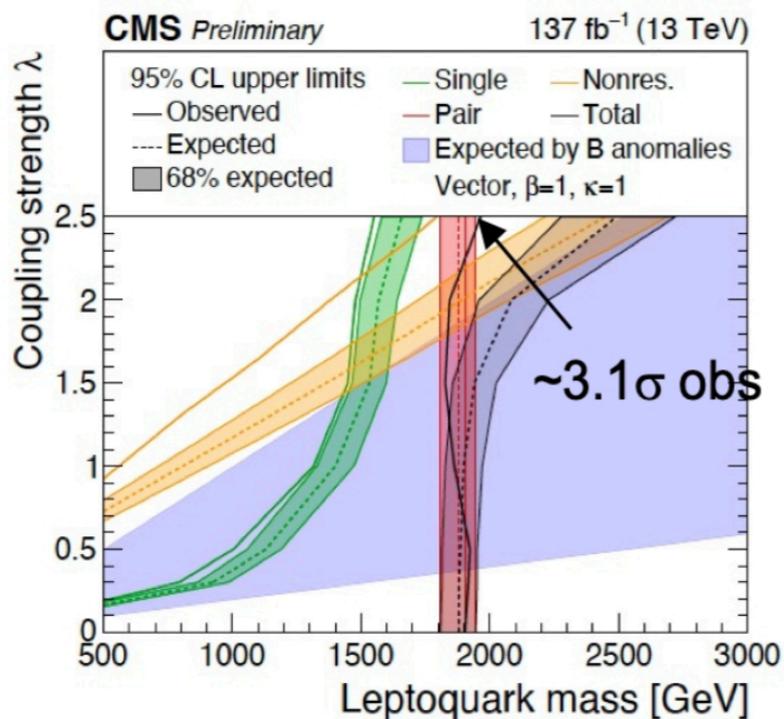
High-energy searches: U_1 leptoquark



Caveat: BR=1 (CMS) vs BR=0.5 (ATLAS)

[CMS-PAS-EXO-19-016](#)

[EXOT-2022-39](#)



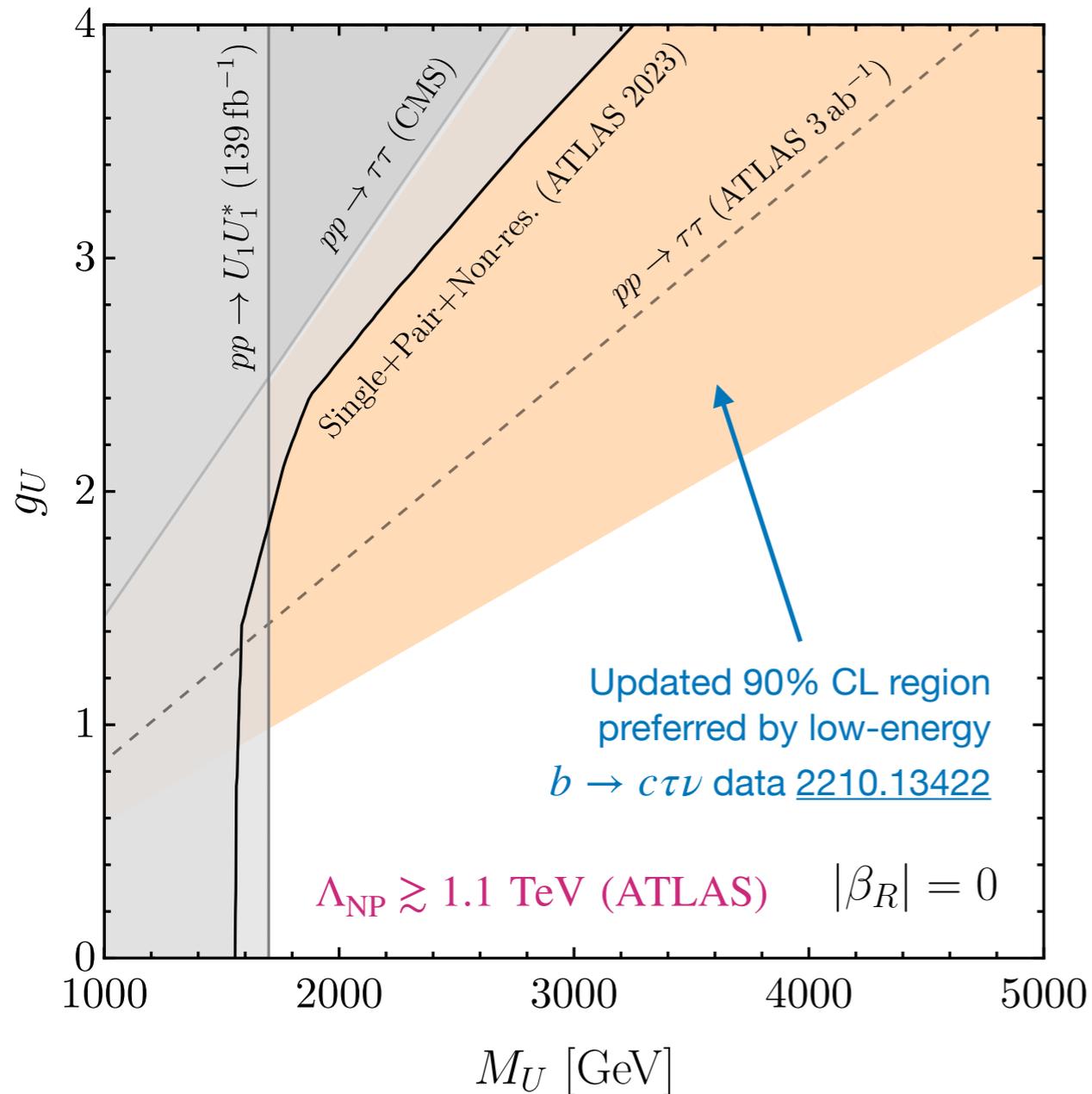
Large improvement in sensitivity when adding low b-jet p_T category

Excludes CMS' excess

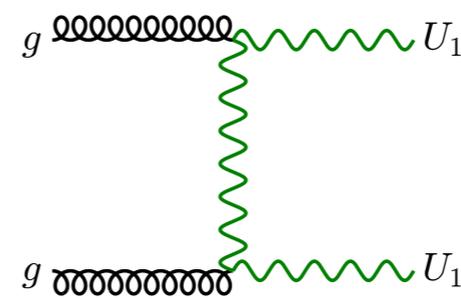


High-energy searches: U_1 leptoquark model (LH)

- The LHC is already probing the preferred region for the U_1 leptoquark model! CMS has a 3σ excess, ATLAS just set weaker than expected limits.....too soon to say.



U_1 pair production



$$U_1 \rightarrow b\tau^+, t\bar{\nu}$$

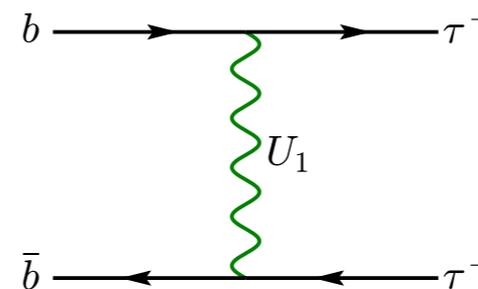
$$\mathcal{B}(U_1 \rightarrow b\tau^+) \approx 0.5$$

$$pp \rightarrow U_1^+ U_1^- \rightarrow b\tau t\nu$$



2012.0417

Drell-Yan t-channel exchange: $\tau\tau$



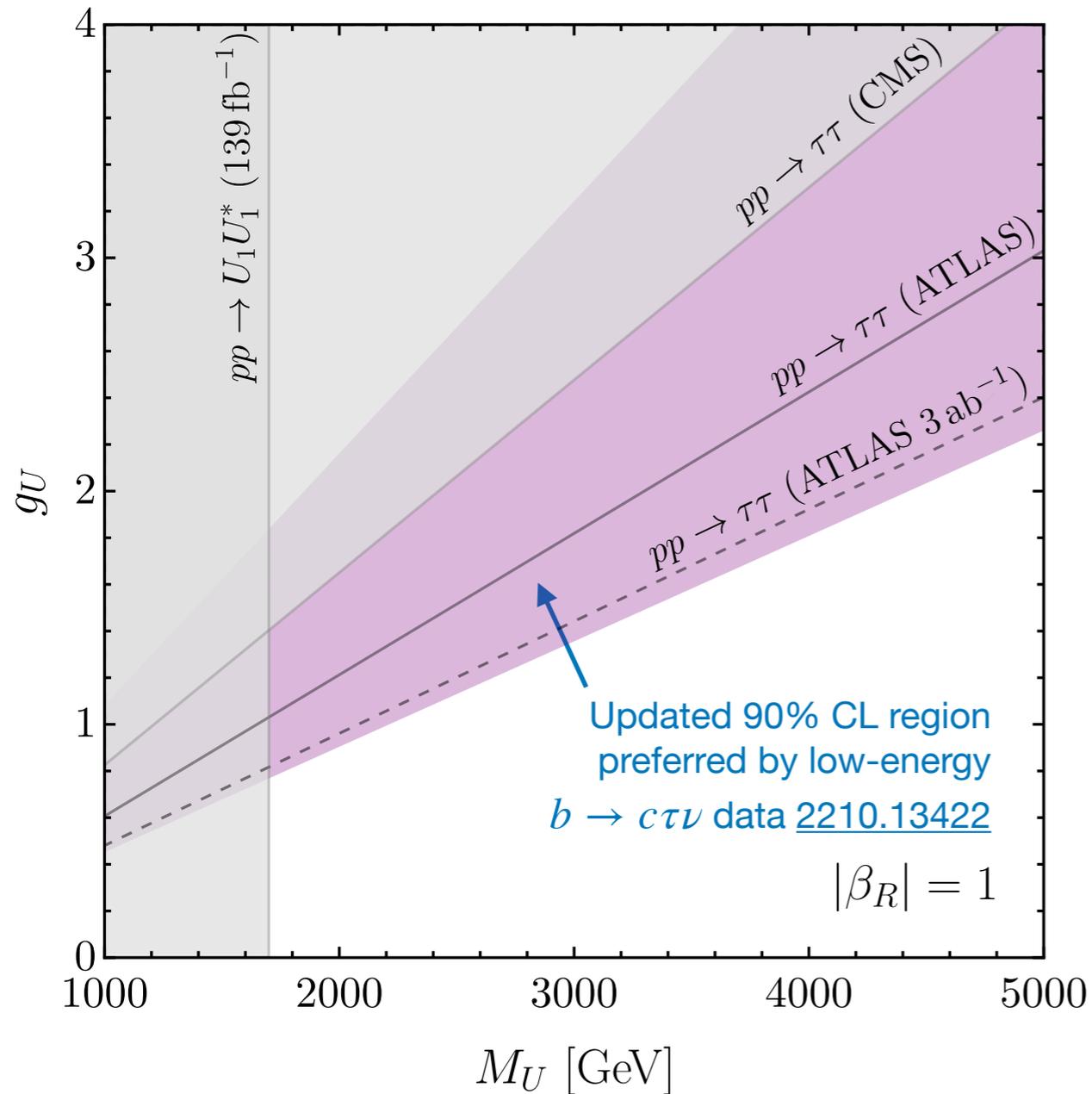
2002.1222

High mass Drell-Yan tails

QCD corrections: [[U. Haisch, L. Schnell, S. Schulte, 2209.12780](#)]

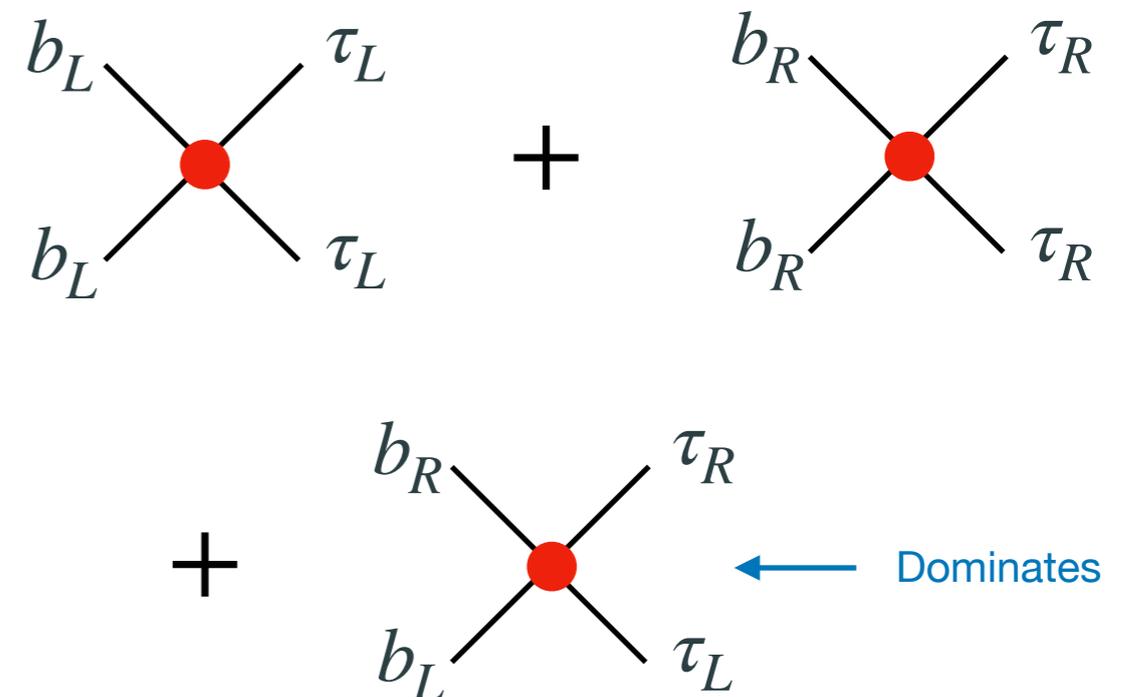
High-energy searches: U_1 leptoquark model (L&R)

- U_1 leptoquark model w/ RH currents preferred region fully within the HL-LHC reach!



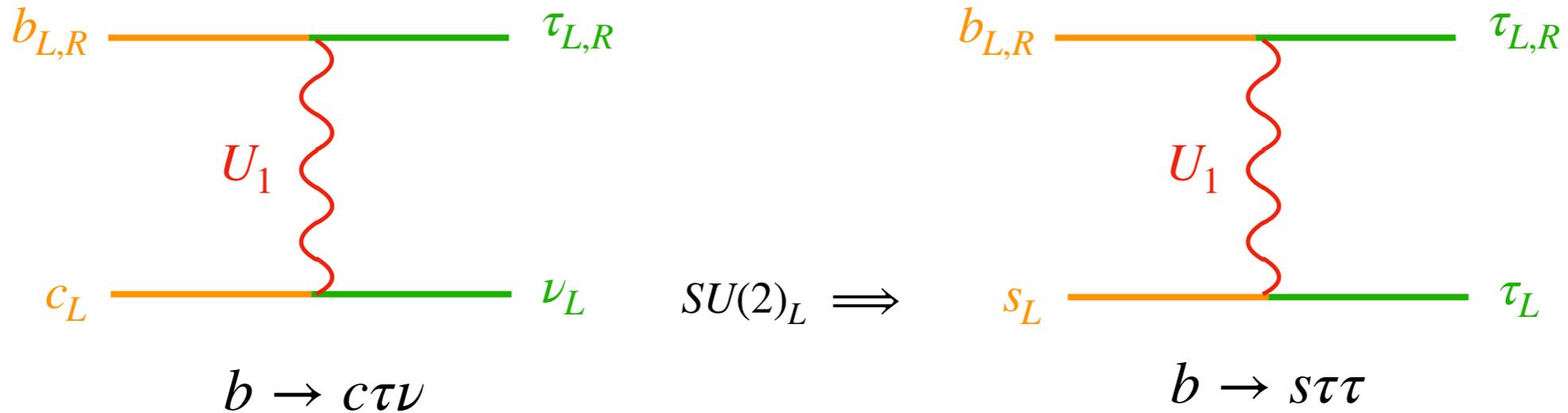
$$\mathcal{L} \supset \frac{g_U}{\sqrt{2}} U_1^\mu \left[(\bar{q}_L^3 \gamma_\mu \ell_L^3) + \beta_R^{b\tau} (\bar{b}_R \gamma_\mu \tau_R) \right] \quad (\beta_R^{b\tau} = -1)$$

- Additional contributions give stronger bound from t-channel Drell-Yan $\tau\tau$:



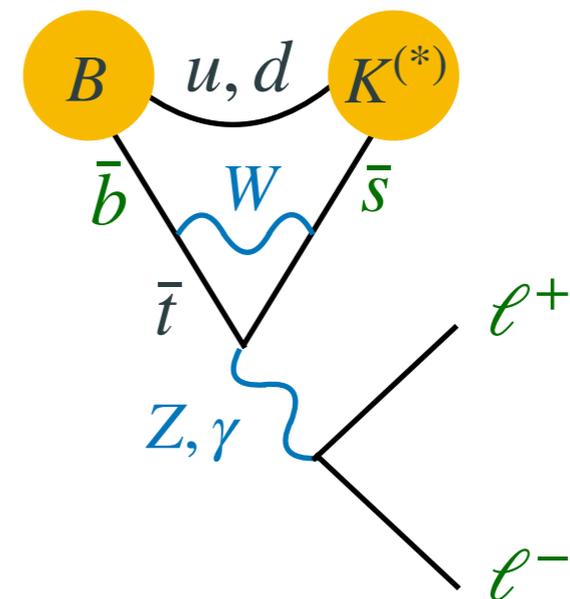
U_1 connects $R_{D^{(*)}}$ to $b \rightarrow s\tau\tau$ observables

- We have tree-level effects in $b \rightarrow s\tau\tau$ connected to the size of $R_{D^{(*)}}$



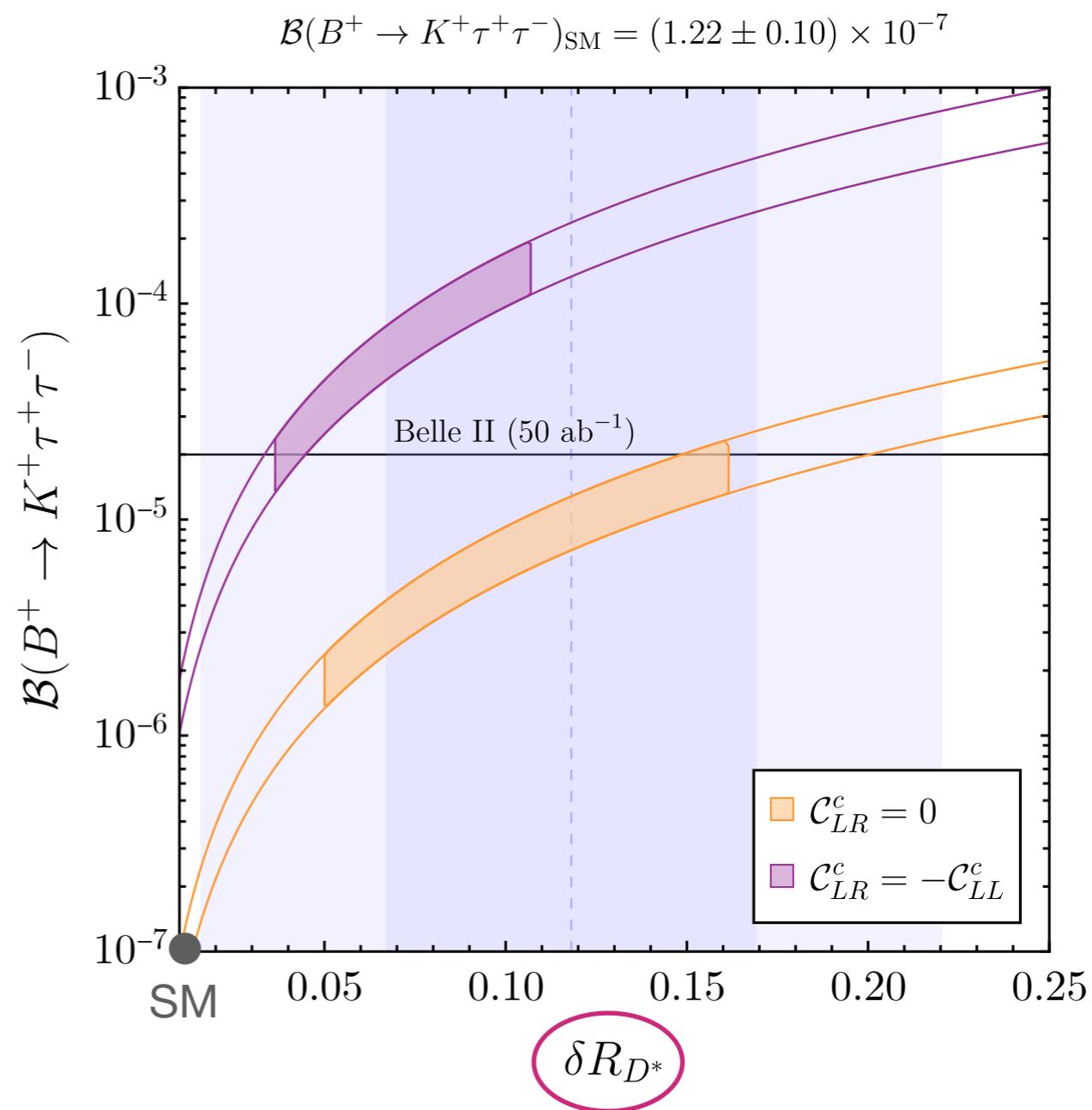
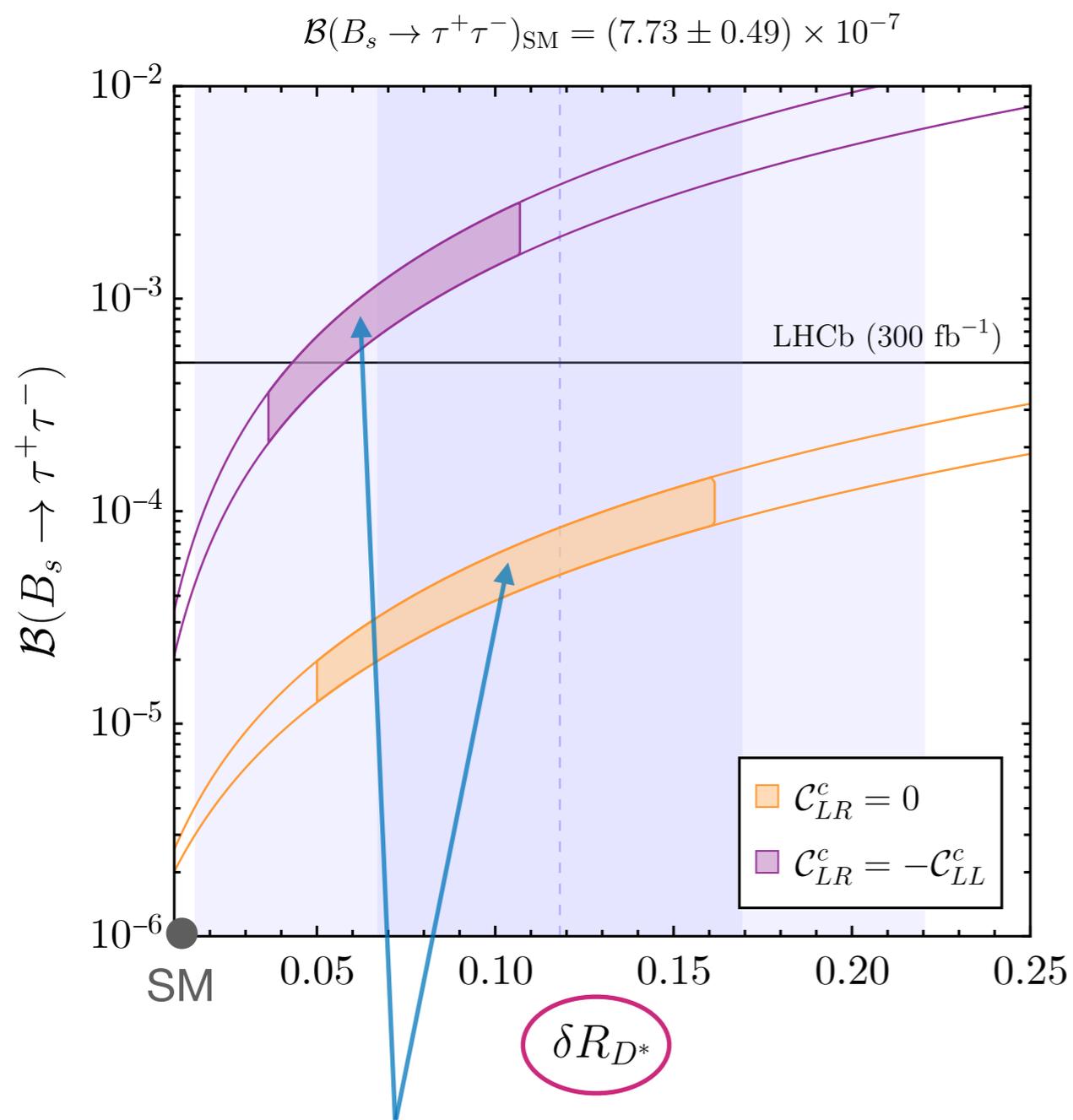
- Since $b \rightarrow s\tau\tau$ is a FCNC, it is a 1-loop process in the SM. We therefore expect a huge NP enhancement in $b \rightarrow s\tau\tau$!

$$\frac{\mathcal{B}(B \rightarrow K^{(*)}\tau\tau)}{\mathcal{B}(B \rightarrow K^{(*)}\tau\tau)_{\text{SM}}} \sim 16\pi^2 \frac{R_{D^{(*)}}}{R_{D^{(*)}}^{\text{SM}}}$$



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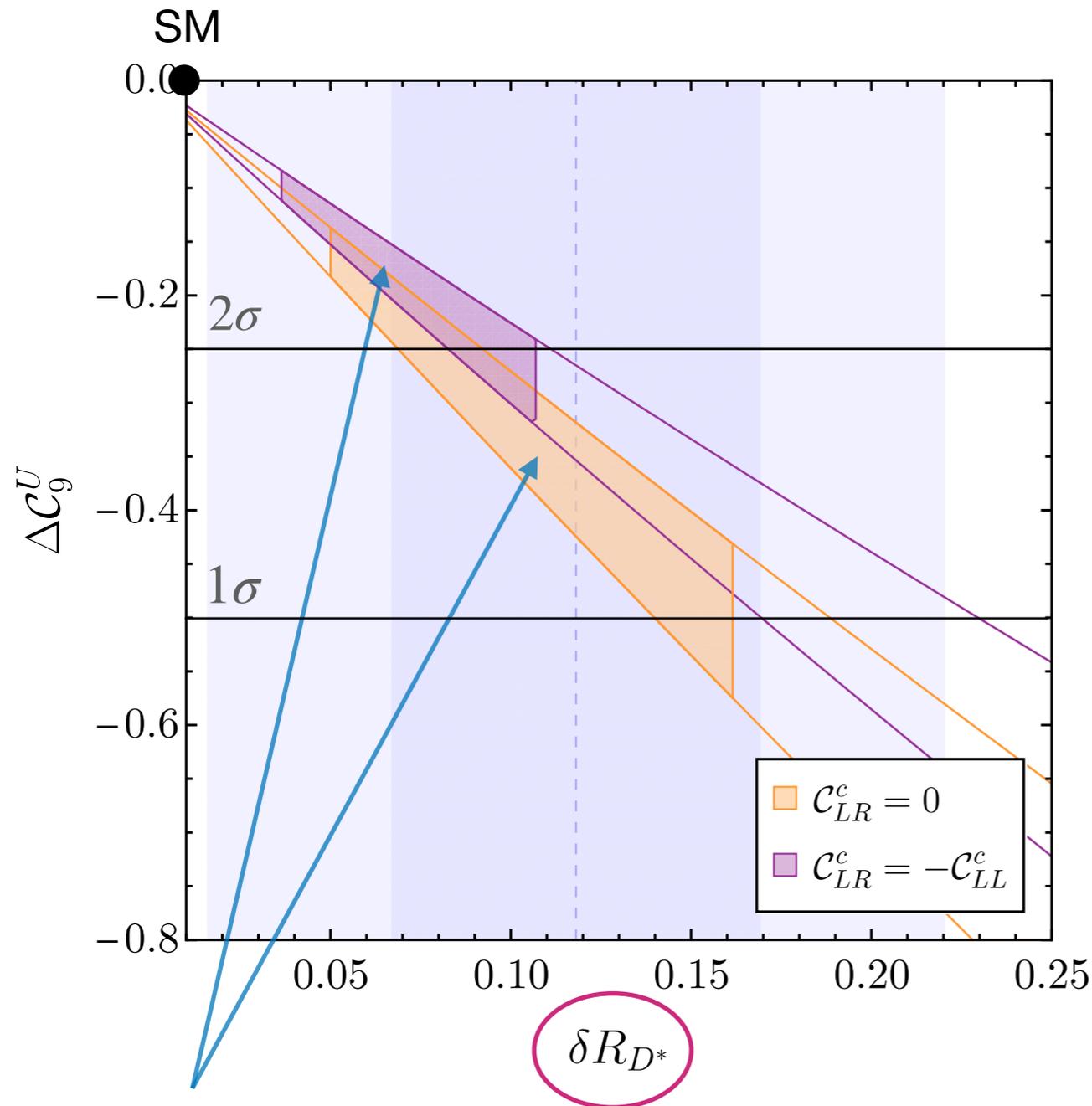


Updated 90% CL region preferred by low-energy $b \rightarrow c\tau\nu$ data [2210.13422](#)

[J. Aebischer, G. Isidori, M. Pesut, BAS, F. Wilsch, [2210.13422](#)]

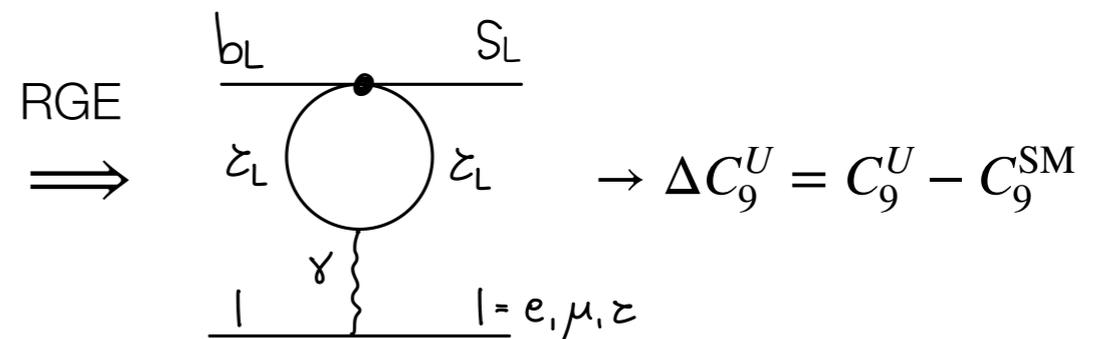
U_1 connects $R_{D^{(*)}}$ to universal $b \rightarrow s\ell\ell$ observables

- Large $b \rightarrow s\tau\tau$ implies a sizable *flavor universal* loop effect in $b \rightarrow s\ell\ell$!



$$\mathcal{L}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} \frac{\alpha}{4\pi} \sum_i C_i^\ell O_i^\ell$$

$$O_9^\ell = (\bar{s}_L \gamma_\mu b_L)(\bar{\ell} \gamma^\mu \ell)$$



Fit to “dirty” $b \rightarrow s\ell^+\ell^-$ data:
 $\Delta C_9^U \approx 0.75 \pm 0.25$

Updated 90% CL region preferred by low-energy $b \rightarrow c\tau\nu$ data [2210.13422](#)

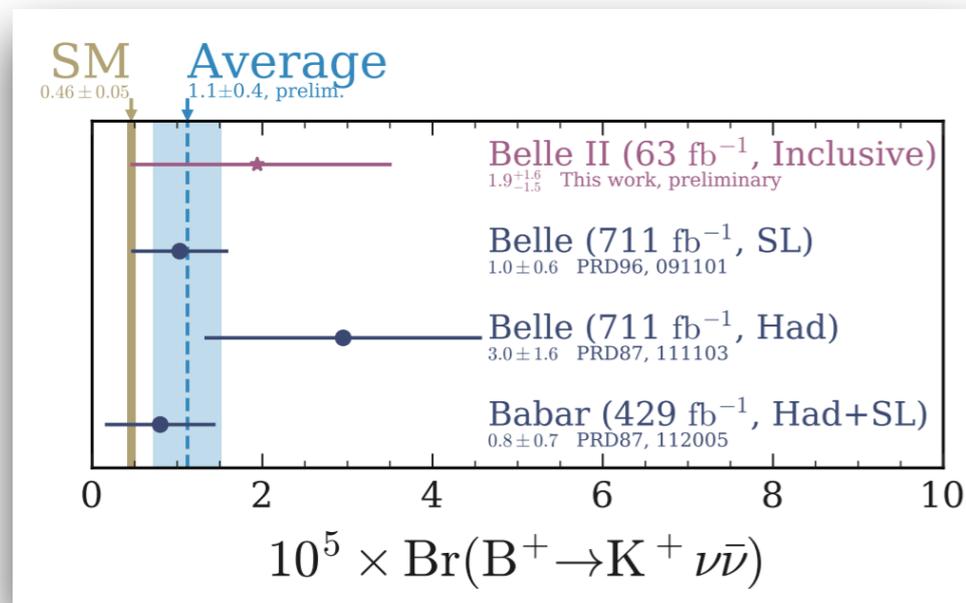
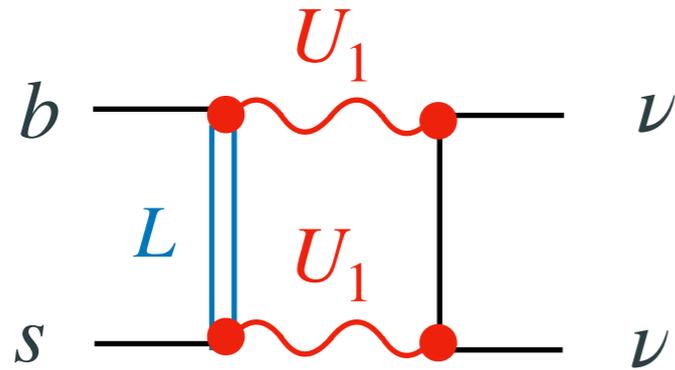
[J. Aebischer, G. Isidori, M. Pesut, BAS, F. Wilsch, [2210.13422](#)]

[Altmannshofer, Stangl [2103.13370](#)
 Bobeth, Haisch, [1109.1826](#); Crivellin
 et al., [1807.02068](#);

Algueró et al., [1809.08447](#)]

Important 1-loop effects: $B \rightarrow K^{(*)}\nu\nu$ (4321 Model)

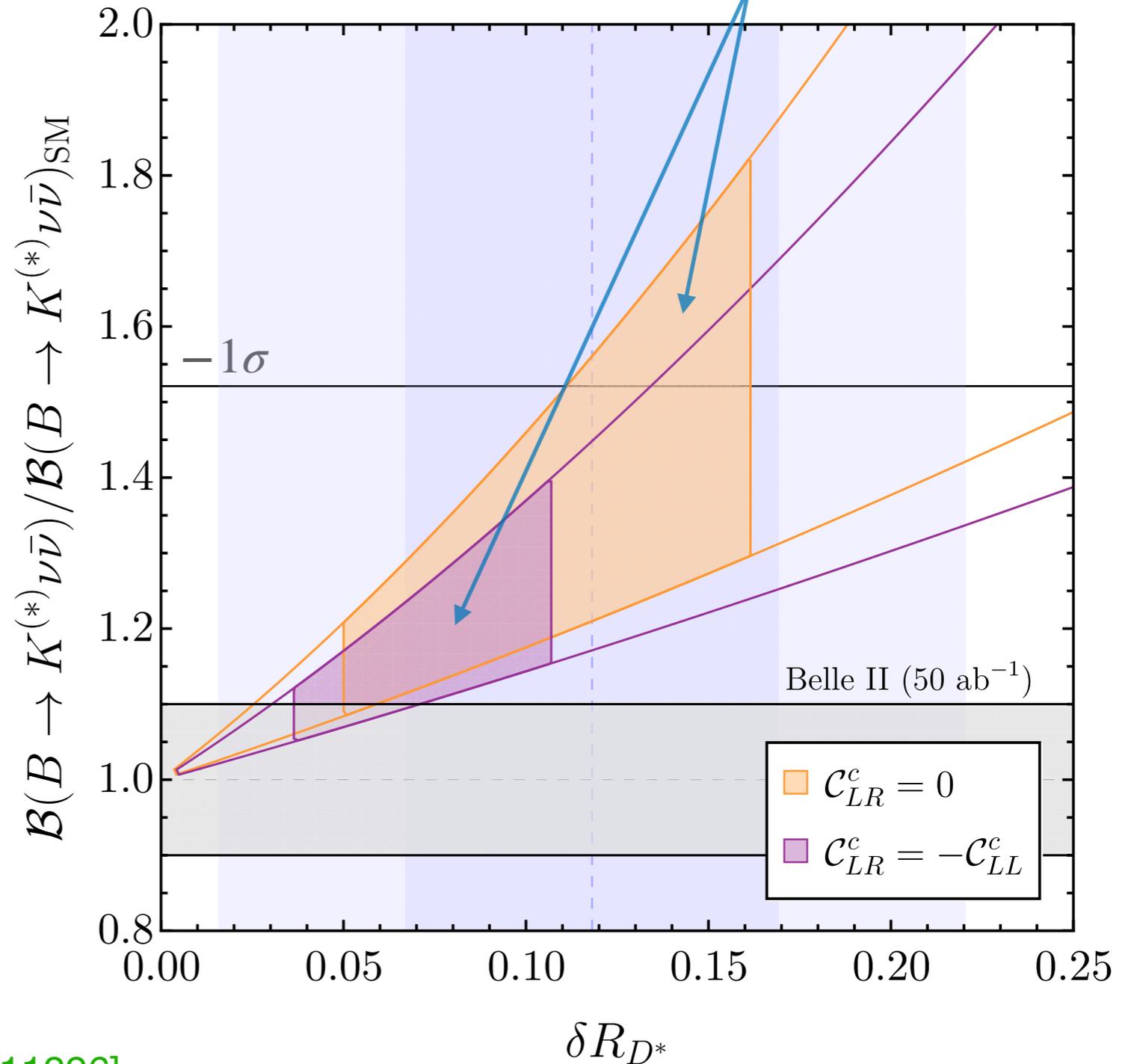
- Some (important) effects appear only at one loop. For U_1 , requires UV model!



[Belle II Collaboration, [2104.12624](https://arxiv.org/abs/2104.12624)]

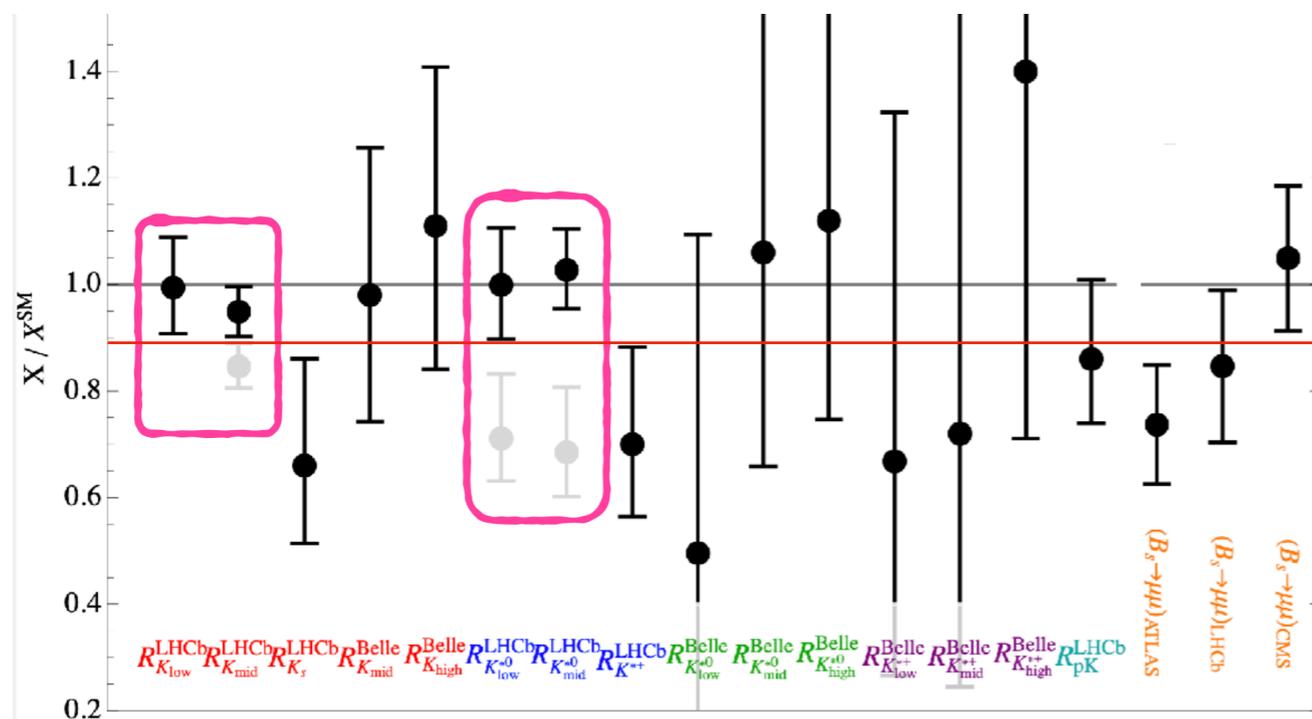
[Fuentes-Martin, Isidori, König, Selimovic, [2009.11296](https://arxiv.org/abs/2009.11296)]

Updated 90% CL region preferred by low-energy $b \rightarrow c\nu\nu$ data [2210.13422](https://arxiv.org/abs/2210.13422)



A final comment on $R_{K^{(*)}}$

- 12/2022: a second LHCb analysis of R_K & R_{K^*} establishes μ/e lepton flavor universality in $b \rightarrow sll$ at $\sim 5\%$ level [LHCb,221209152]



[compilation of $b \rightarrow s\mu\mu$ clean observables as of Dec. 2022 (©David Marzocca)]

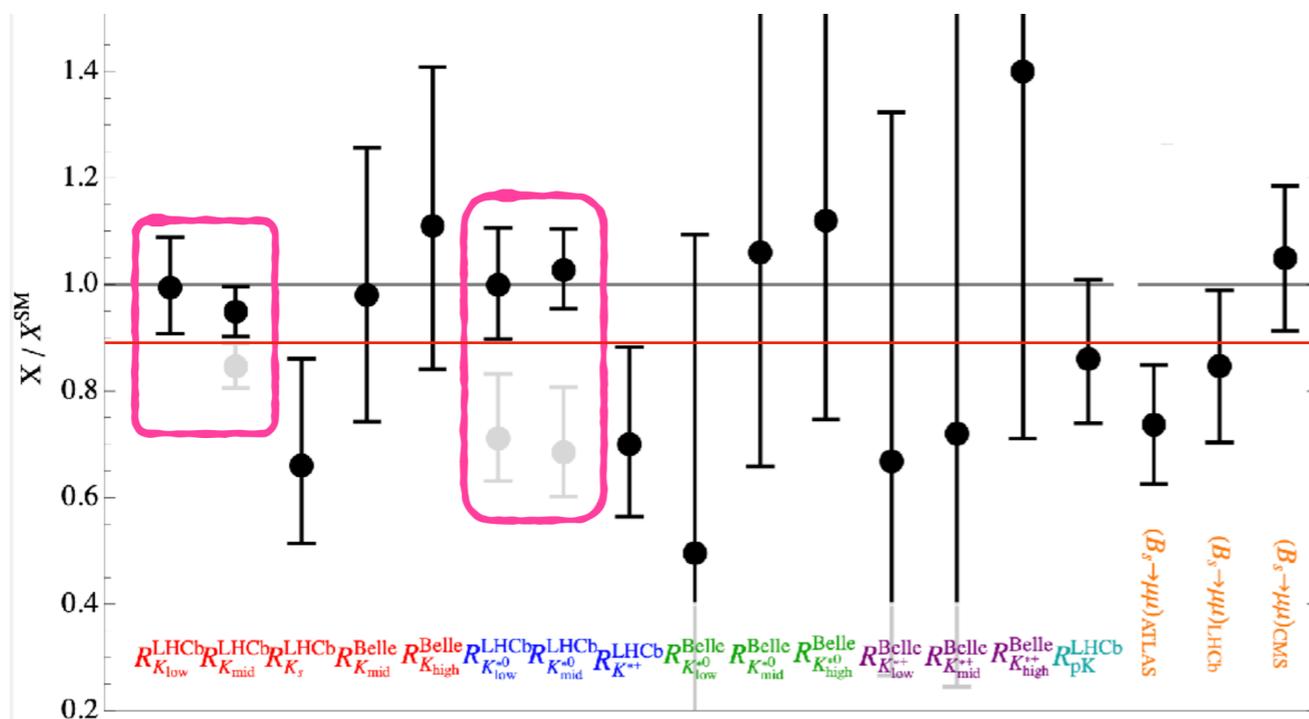
$$\text{low-}q^2 \begin{cases} R_K & = 0.994^{+0.090}_{-0.082} (\text{stat})^{+0.029}_{-0.027} (\text{syst}), \\ R_{K^*} & = 0.927^{+0.093}_{-0.087} (\text{stat})^{+0.036}_{-0.035} (\text{syst}), \end{cases}$$

$$\text{central-}q^2 \begin{cases} R_K & = 0.949^{+0.042}_{-0.041} (\text{stat})^{+0.022}_{-0.022} (\text{syst}), \\ R_{K^*} & = 1.027^{+0.072}_{-0.068} (\text{stat})^{+0.027}_{-0.026} (\text{syst}). \end{cases}$$

- Still room for small μ/e lepton flavor violation at the $\sim 10\%$ level

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U(2)-breaking parameter:

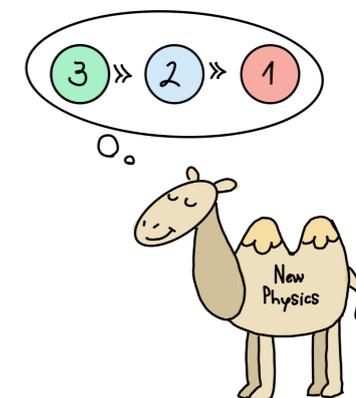
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Nothing changes here, still calls for light NP!

$$R_{D^{(*)}}$$

$U(2)_\ell$ breaking V_ℓ is simply smaller now.

$$R_{K^{(*)}}$$



Wrapping Up:
Key Take-away Points and
Conclusions

B-factories are crucial in the search for NP!

- Remember, NP cannot be light without flavor protection*! (MFV, U(2), etc.). This is completely generic and means we expect the leading NP effects are in purely third-family processes or $3 \rightarrow 2$ transitions, namely: top decays, **B-physics**, LFU and LFV in tau decays (no time, but in general $\tau \rightarrow \mu X$ with $X = \nu\bar{\nu}, \ell\bar{\ell}, \phi, \gamma$, etc.)

| <u>U(2)-breaking operator</u> | <u>Process</u> | <u>Example Observables</u> |
|--|-----------------------------|---|
| $(\bar{q}_L^i V_q^i \gamma_\mu q_L^3)^2$ | B -meson mixing | ΔM_{B_s} |
| $(\bar{q}_L^i V_q^i \gamma_\mu q_L^3)(\bar{\ell}_L^3 \gamma^\mu \ell_L^3)$ | Neutral current B -decays | $B \rightarrow K^{(*)} \tau \bar{\tau}, B \rightarrow K^{(*)} \nu_\tau \bar{\nu}_\tau, B_s \rightarrow \tau \bar{\tau}$ |
| $(\bar{q}_L^i V_q^i \gamma_\mu \sigma^I q_L^3)(\bar{\ell}_L^3 \gamma^\mu \sigma^I \ell_L^3)$ | Charged current B -decays | $B \rightarrow D^{(*)} \tau \bar{\nu}_\tau, \Lambda_b \rightarrow \Lambda_c \tau \bar{\nu}_\tau, B_c \rightarrow \tau \bar{\nu}_\tau$ |
| $(\bar{q}_L^i V_q^i \gamma^\mu q_L^3)(\bar{\ell} \gamma_\mu \ell)$ | Neutral current B -decays | $B \rightarrow K^{(*)} \ell \bar{\ell}$ (flavor universal) |
| $y_b (\bar{q}_L^i V_q^i \sigma_{\mu\nu} H b_R) F^{\mu\nu}$ | Neutral current B -decays | $B \rightarrow X_s \gamma$ |

*Here, light NP still means heavier than the EW scale such that an EFT description is valid.

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U1 LQ models:



V_q Tree-level



V_q or V_q^2 1-loop

*Here, light NP still means heavier than the EW scale such that an EFT description is valid.

B-factories are crucial in the search for NP!

Overview of ongoing LFU measurements

| mode | Run 1: 3 fb ⁻¹ at 7/8 TeV | | Run 2: 6 fb ⁻¹ at 13 TeV | |
|---------------------|--------------------------------------|----------|-------------------------------------|----------|
| | muonic | hadronic | muonic | hadronic |
| $R(D^+)$ | X | X | X | X |
| $R(D^0)$ | ✓ | X | X | X |
| $R(D^{*+})$ | ✓ | ✓ | X | X |
| $R(\Lambda_c)$ | X | ✓ | X | X |
| $R(\Lambda_c^{*+})$ | X | X | X | X |
| $R(J/\psi)$ | ✓ | X | X | X |
| $R(D_s^+)$ | X | X | X | X |
| $R(D_s^{*+})$ | X | X | X | X |

- So far only published Run 1 results; Run 2 has four times as much data
- Many analyses in progress; no timelines
- Work ongoing also in $b \rightarrow u$ sector; and excited states: $\mathcal{R}(D^{**})$, $\mathcal{R}(D_s^{**})$

Suzanne Klaver LFU in charged-current b decays Implication WS 19 October 2022 18

- Also all of these processes yet to be analyzed (or only Run 1 data). Since the underlying partonic $b \rightarrow c\tau\nu$ process is the same, NP expected in all of these!

Conclusions

- The tension in the LFU ratios $R_{D^{(*)}}$ remains an interesting hint of NP at the TeV scale. If we take it seriously, leptoquark models are the only viable mediators. **Important:** These models did not change much without $R_{K^{(*)}}$!

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Thanks a lot for your attention!

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Backup Slides

UV Model: New flavor non-universal gauge interactions

Based on “4321” gauge symmetry:

$$SU(4) \sim \left(\begin{array}{c|c} G^a & U^\alpha \\ \hline (U^\alpha)^* & Z' \end{array} \right)$$

$$\begin{array}{c} \overbrace{SU(4)_h \times SU(3)_l \times SU(2)_L \times U(1)_{l+R}}^{U(1)_Y} \\ \underbrace{\hspace{10em}}_{SU(3)_c} \end{array} \xrightarrow{\langle \Omega_{1,3,15} \rangle \sim \mathcal{O}(\text{TeV})} SU(3)_c \times SU(2)_L \times U(1)_Y + U_1, G', Z'$$

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Third-family quark-lepton unification at the TeV scale: [Greljo, BAS, 1802.04274]

$$\psi_L \sim \begin{pmatrix} q_L^3 \\ \ell_L^3 \end{pmatrix} \quad \psi_R^+ \sim \begin{pmatrix} u_R^3 \\ \nu_R^3 \end{pmatrix} \quad \psi_R^- \sim \begin{pmatrix} d_R^3 \\ e_R^3 \end{pmatrix}$$

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 \implies Direct NP couplings (L+R)
- Light families under 321 (SM-like)
- Accidental approximate $U(2)^5$ flavor symmetry: $\psi = (\psi_1 \psi_2 \psi_3)$
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Leptons as the fourth “color”

[Pati, Salam, Phys. Rev. D10 (1974) 275]
 (only 7 years after the SM was proposed)

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4321 models

[di Luzio, Greljo, Nardecchia [1708.08450](#)
 Bordone, Cornella, Fuentes-Martin, Isidori
[1712.01368](#), [1805.09328](#);
 Greljo, BAS, [1802.04274](#);
 Cornella, Fuentes-Martin, Isidori [1903.11517](#)]

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UV Model: New colored particles and EW observables

- In addition to the U_1 LQ, we also get neutral G', Z' vectors.
- We also need a vector-like quark and lepton Q, L for fermion mixing.

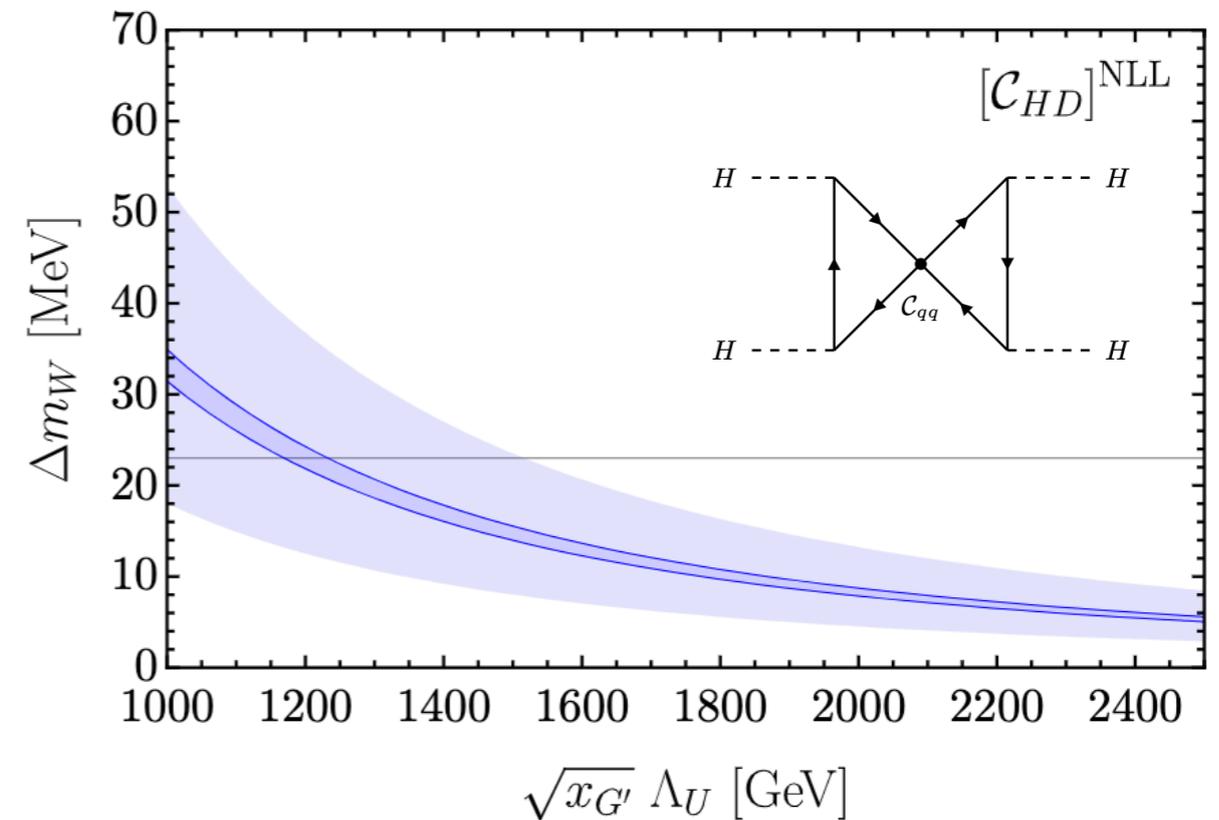
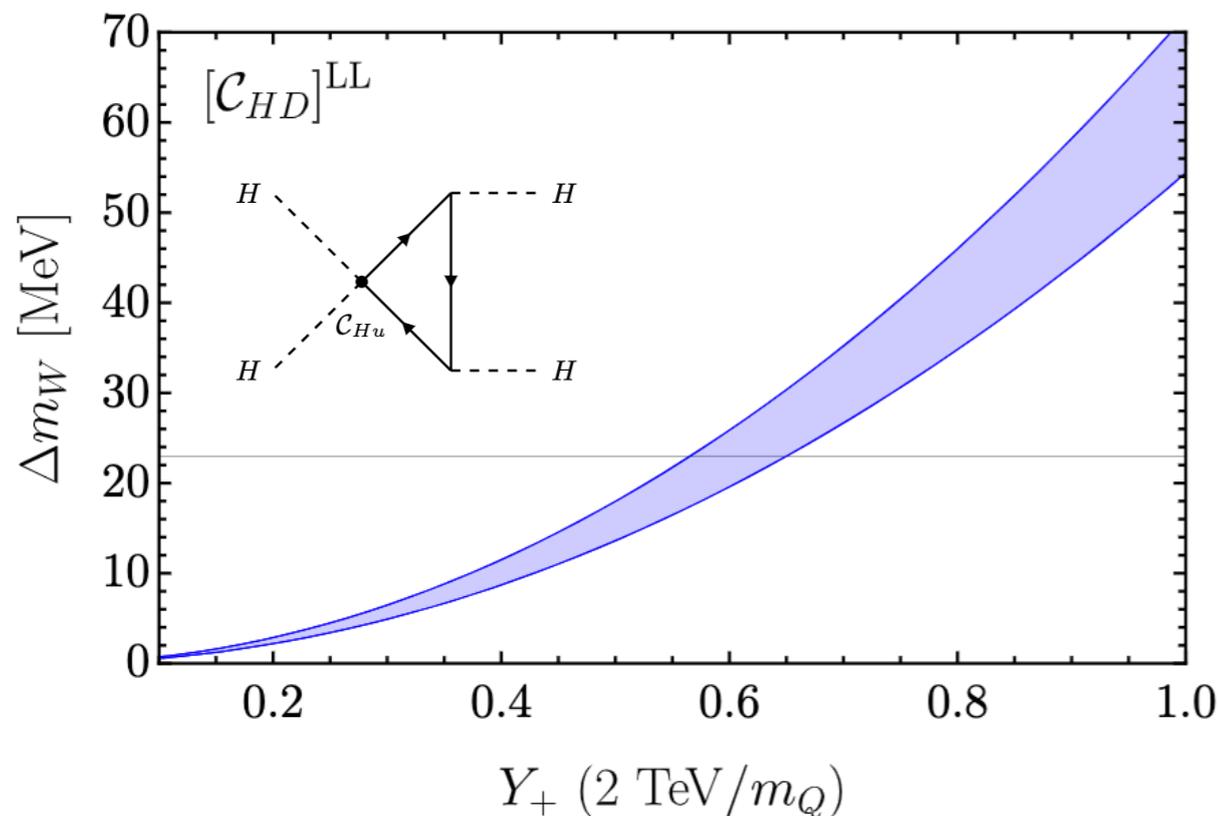
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- New colored states Q, G' give sizable shifts in the W-mass via RGE effects.

$$\frac{\Delta m_W}{m_W} \supset -\frac{v^2}{4} \frac{g_L^2}{g_L^2 - g_Y^2} C_{HD}$$

$$\mathcal{O}_{HD} = |H^\dagger D_\mu H|^2$$

$$\alpha T = -\frac{v^2}{2} C_{HD}$$



- Full EW fit in 4321 model: [\[Allwicher, Isidori, Lizana, Selimovic, BAS, 2302.11584\]](#)