

Rare Top Decays as Probes of Flavorful Higgs Bosons

Wolfgang Altmannshofer
waltmann@ucsc.edu



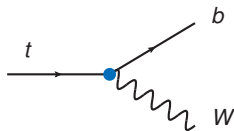
based on arXiv:1904.10956
with Brian Maddock and Douglas Tuckler

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The Challenge

The dominant top decay mode is a
unsuppressed 2 body decay into a W boson and a b quark

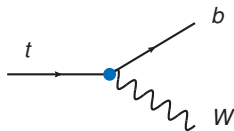


$$\Gamma_t \sim \frac{g^2}{64\pi} \left(\frac{m_t}{m_W} \right)^2 |V_{tb}|^2 m_t$$

$$\rightarrow \frac{\Gamma_t}{m_t} \simeq 1\%$$

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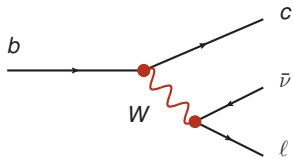
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compare to B meson decay: **3 body + CKM suppression**

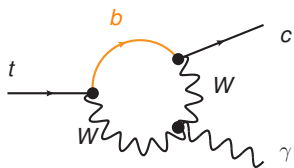


$$\Gamma_{b \rightarrow c \ell \bar{\nu}} \sim \frac{g^4}{384\pi} \frac{1}{16\pi^2} \left(\frac{m_b}{m_W} \right)^4 |V_{cb}|^2 m_b$$

$$\rightarrow \frac{\Gamma_B}{m_B} \simeq 8.2 \times 10^{-13}$$

Top FCNCs in the Standard Model

top FCNCs are 1-loop suppressed, CKM suppressed
and **strongly GIM suppressed**

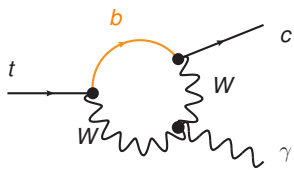


$$\mathcal{A}_{t \rightarrow c\gamma} \propto \frac{e}{16\pi^2} \frac{G_F}{\sqrt{2}} \frac{m_b^2}{m_W^2} V_{tb} V_{cb}^*$$

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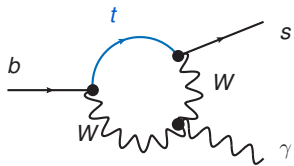
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compare to rare B decays: **GIM breaking by the large top mass**



$$\mathcal{A}_{b \rightarrow s\gamma} \propto \frac{e}{16\pi^2} \frac{G_F}{\sqrt{2}} \frac{m_t^2}{m_W^2} V_{tb} V_{ts}^*$$

$$\rightarrow \text{BR}(B \rightarrow X_s\gamma)_{\text{SM}} \simeq 3.15 \times 10^{-4}$$

Standard Model Predictions

(Aguilar-Saavedra hep-ph/0409342)

$$\text{BR}(t \rightarrow c\gamma) \simeq 5 \times 10^{-14} \quad , \quad \text{BR}(t \rightarrow u\gamma) \simeq 4 \times 10^{-16}$$

$$\text{BR}(t \rightarrow cg) \simeq 5 \times 10^{-12} \quad , \quad \text{BR}(t \rightarrow ug) \simeq 4 \times 10^{-14}$$

$$\text{BR}(t \rightarrow cZ) \simeq 1 \times 10^{-14} \quad , \quad \text{BR}(t \rightarrow uZ) \simeq 8 \times 10^{-17}$$

$$\text{BR}(t \rightarrow ch) \simeq 3 \times 10^{-15} \quad , \quad \text{BR}(t \rightarrow uh) \simeq 2 \times 10^{-17}$$

[side note: these numbers come with large uncertainties from renormalization scale dependence of the bottom mass. In 1904.10956 we did a careful analysis and found

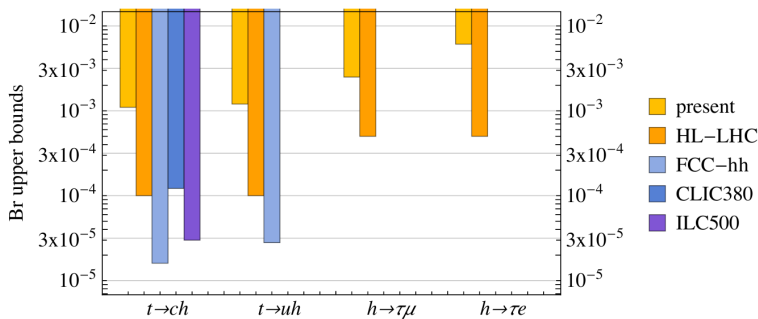
$$\text{BR}(t \rightarrow ch) = (4.19_{-0.80}^{+1.08} \pm 0.16) \times 10^{-15}$$

$$\text{BR}(t \rightarrow uh) \simeq (3.66_{-0.70}^{+0.94} \pm 0.67) \times 10^{-17}]$$

**For practical purposes, the SM predictions are vanishingly small.
Any observation in the foreseeable future
would be a clear sign of New Physics.**

Experimental Status

European Strategy Physics Briefing Book 1910.11775



- ▶ Current constraint: $\text{BR}(t \rightarrow qh) \lesssim 10^{-3}$.
- ▶ Can be improved by an order of magnitude at HL-LHC.
- ▶ A bit better for the other types of rare top decays, but not much.

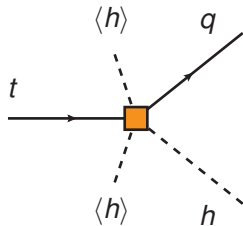
SMEFT Interpretation

- ▶ One can interpret the constraints on the $t \rightarrow ch$ and $t \rightarrow uh$ branching ratios as constraints on flavor changing Higgs couplings
- ▶ or, equivalently, on SMEFT operators that give flavor changing Higgs couplings

“Higgs penguin operators”

$$\frac{1}{\Lambda^2} (H^\dagger H) (\bar{c}_R Q_3) H^c$$

$$\frac{1}{\Lambda^2} (H^\dagger H) (\bar{Q}_2 t_R) H$$

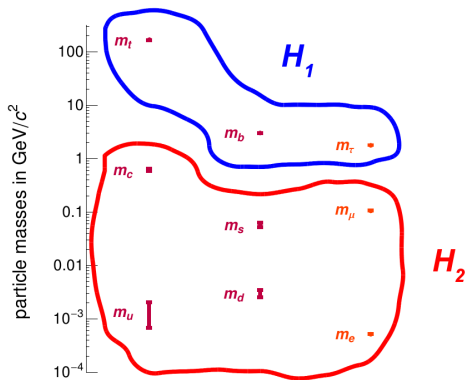


$$\frac{\text{BR}(t \rightarrow qh)}{\text{BR}(t \rightarrow bW)} \sim \frac{v^4}{\Lambda^4} \Rightarrow \Lambda \gtrsim 1 \text{ TeV}$$

Is there a (not entirely unmotivated) model that gives flavor changing Higgs couplings saturating the constraints?

Flavorful Higgs Bosons I

Consider a 2HDM with non-trivial flavor structure



one Higgs is responsible for the masses of the **heaviest flavors**

(we assume it has rank-1 Yukawa couplings)

a second Higgs gives mass to the **light flavors** and is responsible for **flavor mixing**

(could have rank-2 or rank-3 Yukawas)

WA, Gori, Kagan, Silvestrini, Zupan, PRD 93 (2016) no.3, 031301

Flavorful Higgs Bosons II

- ▶ The setup can address part of the [hierarchies in the fermion masses](#)
 $m_{1\text{st}}, m_{2\text{nd}} \ll m_{3\text{rd}}$ if $\tan \beta = v_1/v_2 \gg 1$

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- ▶ The setup goes beyond “natural flavor conservation”
 \Rightarrow expect **flavor changing neutral currents** at tree level.
- ▶ The most constraining flavor probes are transitions between the first and second generation, e.g. $K^0 - \bar{K}^0$ mixing, or $\mu \rightarrow e\gamma$.
- ▶ Since the Yukawa couplings of H_1 are rank-1, such flavor transitions are protected by an **approximate $SU(2)$ symmetry**.
- ▶ Additional Higgs bosons below 1 TeV are compatible with flavor constraints.

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- ▶ Additional Higgs bosons below 1 TeV are compatible with flavor constraints.
- ▶ There are several variations of viable flavor structures.
- ▶ Main distinction: is the **CKM matrix** generated (mainly) in the **up-sector** or in the **down-sector**?

Example of an “Up-Sector Model”

WA, Maddock, Tuckler 1904.10956

Arguably the simplest choice to get **rank-1 Yukawas** for H_1 :
charge H_1 and the 3 generation of LH quarks under a **$U(1)$ symmetry**.

Introduce a **second $U(1)$ flavor symmetry** to model
the remaining mass and mixing hierarchies

$$v\lambda_u \sim v_w \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ \epsilon^{|a|} & \epsilon^1 & 1 \end{pmatrix}, \quad v'\lambda'_u \sim v_w \begin{pmatrix} \epsilon^8 & \epsilon^4 & \epsilon^3 \\ \epsilon^{|b|} & \epsilon^3 & \epsilon^2 \\ 0 & 0 & 0 \end{pmatrix},$$
$$v\lambda_d \sim v_w \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & \epsilon^3 \end{pmatrix}, \quad v'\lambda'_d \sim v_w \begin{pmatrix} \epsilon^7 & \epsilon^6 & 0 \\ \epsilon^{|c|} & \epsilon^5 & 0 \\ 0 & 0 & 0 \end{pmatrix},$$

(Yukawas are uniquely determined up to a few discrete choices for the parameters a, b, c)

Predictions for Top Flavor Violation

- ▶ The resulting model turns out to be **highly predictive**.
- ▶ Flavor violating Higgs couplings are given by CKM matrix elements and quark mass ratios.
- ▶ Rare top branching ratios only depend on **two parameters**:

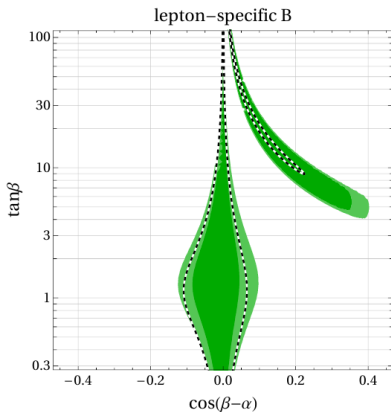
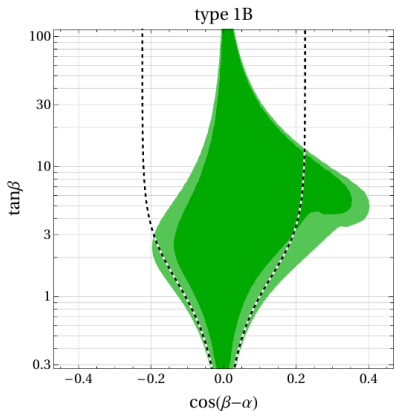
$\tan \beta$ (ratio of the two vevs)

α (mixing angle of the scalar Higgs bosons h and H)

$$\text{BR}(t \rightarrow hq) \simeq 2|V_{qb}|^2 \frac{\cos^2(\beta - \alpha)}{\sin^2 \beta \cos^2 \beta} \frac{(1 - m_h^2/m_{t,\text{pole}}^2)^2}{(1 - m_W^2/m_{t,\text{pole}}^2)^2 (1 + 2m_W^2/m_{t,\text{pole}}^2)}$$
$$\simeq \frac{\cos^2(\beta - \alpha)}{\sin^2 \beta \cos^2 \beta} \times \begin{cases} 9.2 \times 10^{-4} & \text{for } t \rightarrow hc, \\ 8.0 \times 10^{-6} & \text{for } t \rightarrow hu. \end{cases}$$

Constraints from Higgs Precision Program

Precision measurements of Higgs production and decays
constrain the parameters $\tan\beta$ and α

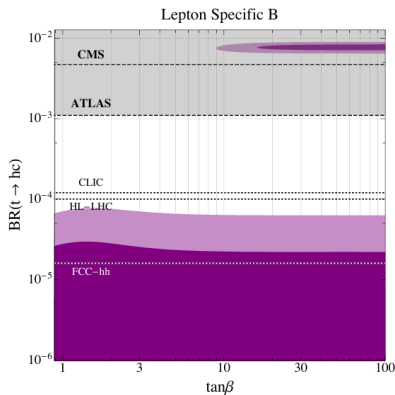
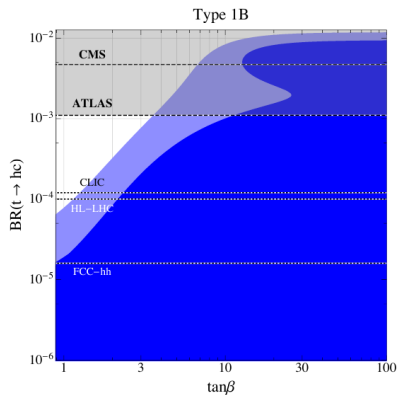


WA, Maddock, Tuckler 1904.10956

(note: plots are 4 years old; current constraints will be somewhat more stringent.)

Rare Top Decays

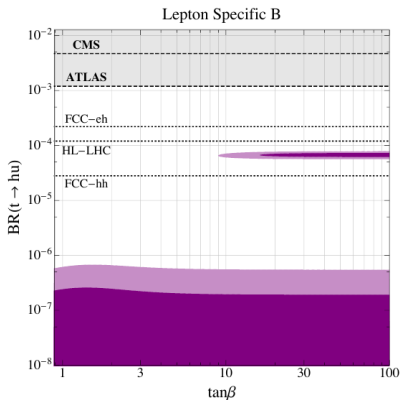
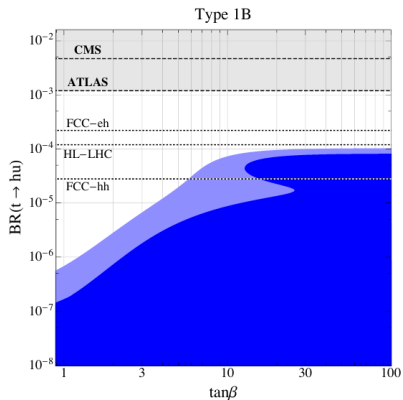
WA, Maddock, Tuckler 1904.10956



current LHC constraints on $t \rightarrow hc$ already probe parameter space.

Rare Top Decays

WA, Maddock, Tuckler 1904.10956



$t \rightarrow hu$ likely out of reach at the LHC and future colliders.

- ▶ Observation of rare top decays would be a clear sign of new physics.
- ▶ Current limits on $t \rightarrow ch$ and $t \rightarrow uh$ probe generic new physics scales of $\Lambda \sim 1$ TeV.
- ▶ In models of “flavorful Higgs bosons” one can saturate the current limits on $t \rightarrow ch$.